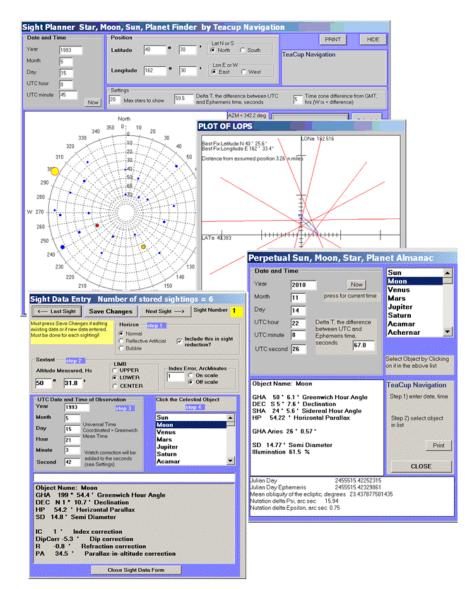
Manual and Documentation for "Teacup Celestial version 3.2f" Software revision 4





By Teacup Navigation

Rodger E. Farley

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1st Edition rev 4

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You can contact the author at milkyway99@verizon.net Please visit my web site where you can download my book 'Celestial Navigation in a Teacup' at http://www.teacupnavigation.net

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Equations for the celestial almanac are partly from Jean Meeus's book 'Astronomical Algorithms' 2nd edit. The ephemerides are calculated with an abridged set of VSOP87 periodic terms.

My thanks to Stan Klein of the USPS Offshore Navigation Committee who was kind enough to review this manual and Teacup Celestial software.

Introduction

This software can calculate and plot a single best fix for multiple target sightings from of any combination of Sun, Moon, planet, or stars taken with a sextant. It will accept up to 25 sights, though in practice 6 is more likely. The session can then be saved in a data file (that has the extension .NAV) so that it can be reopened in the future to relive it or to modify. The sightings are corrected with running fixes if underway, and the final new fix can be to any reference time you choose.

There is a very accurate built-in perpetual almanac for the Sun, Moon, 58 navigational stars, Venus, Mars, Jupiter, and Saturn using VSOP87 periodic terms and knowledge of DeltaT. One simply selects the object being recorded, and the internal computer almanac will supply the astronomical data.

This is the usual order of doing things:

- 1) Sight Planner from the top menu bar to plan your best objects to shoot
- 2) Shoot altitudes with sextant, record data on paper
- 3) Set up main form with fixed data (course, speed, etc..)
- 4) Transcribe altitudes and times and object details in the Sight Data Form

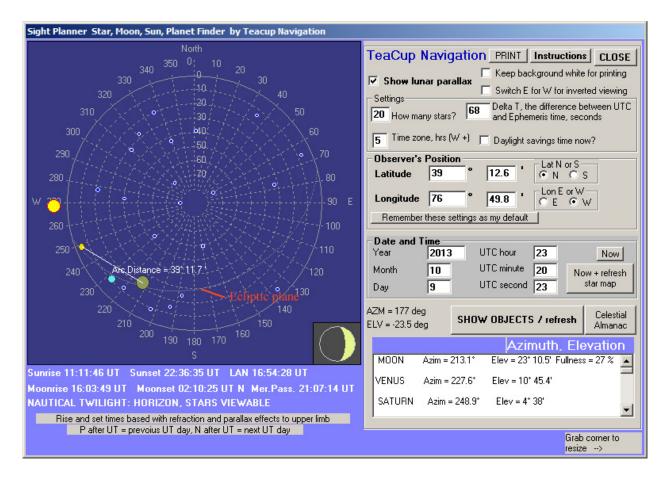
5) After saving the fixes individually, and saving the session with the FILE manager, close the Sight Data Form. Then on the Main Form press the 'Reduce Sight and Plot' button.

Note as to compatibility with older versions before 2.0

Unfortunately, if you had made data files with old versions, they will not carry over to this new version. The data being now simply a selection of the celestial object rather than a nautical almanac facsimile of GHA and DEC inputs, well it would have been too much trouble as the old method did not record the object. Sorry...

Sight Planner

One uses the sight planner to figure out what objects will be up and where. It's up to you determine the best combinations of celestial objects; briefly you will want to take sights of the brightest objects that have a 90° to 120° azimuth spread to cancel out systematic errors. For planning, you don't need a terribly accurate DeltaT, so just leave it at 67 sec. If you want to use the 'Now' button to load the present date and time, you need to have the nominal time zone difference from Greenwich (note the separate daylight savings time check box). This assumes your computer knows the correct local time.



As you can see, one can also get the arc distance between celestial objects. This is done by clicking the left mouse button over the 1st object, then (while still holding the button down) drag the cursor over to the 2nd object and release the mouse button. For doing lunars, while the 'show parallax effects' box is unchecked, this will give the lunar distance cleared from center to center. To see what the arc distance would be with actual parallax (as you would see it for real), check the box. Also shown is a note pointing to the ecliptic plane (earth's

orbital plane) where the sun, moon and planets will be near. For lunars, picking a star or planet hovering near this line will give the greatest accuracy.

The steps 1-5 are listed on a help button on the planner.

Step 1) Modify the settings for your time zone, and the max number of stars to show

Step 2) Enter the date and UT time, or simply press the 'Now' button

Step 3) Enter the latitude and longitude, remembering to select the radio buttons for N, or S, and E, or W

Step 4) Press the Show Objects, or the Now-refresh button

Step 5) View the objects. The moon goes from very dark to light cheese color to indicate fullness (there is also the lower right image to show phase). Stars have sizes according to their brightness magnitude. You can move the mouse cursor over the map to see the azimuth and elevation readout. When the cursor passes over an object of interest, its name appears in a side bar to the right. The parallax or non-parallax position of the moon can be observed according to the upper right check box. Rise/set and LAN for the Sun and meridian passage for the Moon are on the bottom bar. Sometimes after the UT there is a 'P', or an 'N' to indicate this event happened on the previous day (P), or will happen at the next UT day (N).

This planner can be used for sight reduction in its own right if you should be interested. Since you can put in UT time to the second, it will calculate and display the Hc (as Elevation Elev) for the assumed position you list under present latitude and longitude. Making your own index, dip, refraction, and semi diameter corrections to your sextant reading, you can determine the offset distance from the assumed position. By checking the 'Show Parallax Effects' checkbox, you won't have to calculate the parallax correction for the moon as it will already be reflected in the Elevation calculation as Hc – PA.

Your normal default settings for observer's position, time zone, deltaT, etc... can now be set with the "Remember these settings as my default" button. It makes a file called TeacupNav.nv1 which must be in the same folder as the executable file.

Inverse viewing is achieved by checking the Switch E for W box. Stretch the whole form larger by left-click grabbing the lower right corner, then refresh.

Main Form

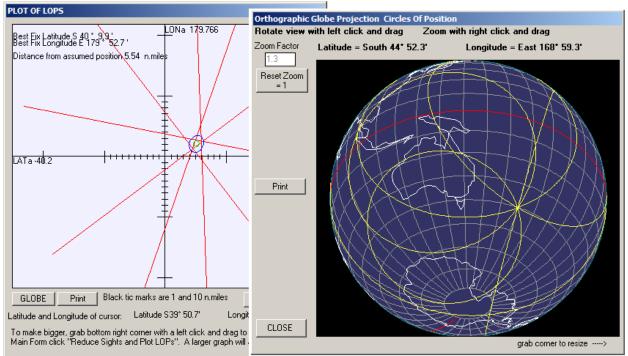
Set up the main form with last fix, new fix time, eye height, true course and speed over ground, air temperature and barometer (you can leave it at the standard settings if you want), and any chronometer corrections. The chronometer correction compensates for watch error (this is under the General Settings form). The UTC in the sightings has this correction added to them to correct to actual UTC. It can be + or - . There is a comment box where you can type any descriptor you want, but don't use any commas! They will not be remembered.

Current Data file: Prob2-3.NAV					
FILE HELP INFO Sight Data Form Celestial Data Sight Planner Lunars Ca	lculators EXIT				
Celestial Navigation Sight-Reduction and	Settings for this leg				
Intercept Plotter by TeaCup Navigation	070 True Course over ground 0-360 deg from true north				
Almanac and Sight Planning also! Version3.2a	6.8 Speed over ground, kts				
Best viewed in 1680 x 1050 resolution					
Best Fix Latitude S40* 9.9'	9 Eye height Om Oft				
Best Fix Longitude E179* 52.7'	General Heading/Course				
Step 1 fill out Lat, Lon, and times	Settings Calculator				
Problem 2-3 from 100 problems in celestial navigation	Step 1: fill out this main form and the				
Last Fix, Latitude 40 ° 30 Lat N or S	General Settings				
Last Fix, Latitude 40 30 North South	Step 2: click View Sight Data Form and fill out according to the 4 steps				
Last Fix, Longitude 178 ° 41 · C Fast C West	indicated				
Last Fix, Longitude 178 41 C East O West	Step 3: click Reduce Sights				
Last Fix, UT 8 Hour 10 Minutes 18 Day 12 Mont	th 1993 Year				
Desired New 15 Hour 52 Minutes 18 Day 12 Month 1993 Year Clear All Data					
The navigator selects the new fix time for which the running fix corrected sight reducti	ions shall apply for this leg				
Preload other forms with data	TeacupCelestial				
Step 2 Step 3	Show LOP Max plotting scale, n.mi. 25				
View Sight Data Form Reduce Sights and Plot LOP's					
	Show COP Detailed Output				

There is a calculator to convert your in-the-water speed and heading measurements into true course and true speed by compensating for current and leeway. Instructions for what to do next are on the main form. After the Sight Data Form has been filled out, close it to come back to the Main Form. Press 'Reduce Sights and Plot LOP's'. The dead reckoning position will show up in a small form, where you can change it if you don't like where the plane sailing calculation places it. For example, if you wish to set it at a whole or half degree instead of to the odd-ball arcminute. If you agree with the recommended assumed position for the fix, the press the 'PRESS' button. The Main Form has the max plotting scale on lower right.

			_	0		
nin N			ing Plane			
١W						
° 31	_'	Lat N or S−	C South			
° 56	_'	C East	 West 			
Accept the calculated assumed position as is pre-entered, or enter a different one manually in the data fields above by clicking it and typing.						
SS to Ente	er Data					
	n W 8 31 9 56 osition as i ove by clic	Sailing • ¥ • 31 • 56 • 56 • ove by clicking it	Sailing techniques W Sailing techniques Lat N or S- North North Sailing techniques Lat N or S- North East Sailing techniques Lat N or S- North East Sailing techniques	Sailing techniques W Sailing techniques Lat N or S North O South South South C East O West Solition as is pre-entered, or enter a differ ove by clicking it and typing.		

After pressing the button, this plot appears of the Line of Positions. The little green circle marks the best fix location. The blue ellipse marks the 95% confidence zone that the fix is somewhere within the ellipse.



A nice feature is the indication of Lat, Lon under the point of the mouse cursor which one can see at the bottom bar. A global plot of the circles of position is also shown.

Sight Data Form

Sight Data Entry Number of stored sightings = 5							
<pre>< Last Sight Save Changes</pre>	Next Sight> This data is Sight Number	1 out of 5					
Must be done for each sighting!	R Index Error, ArcMinutes R 2 On scale						
UTC Date and Time of ObservationYear1993step 3Month7Universal Time Coordinated = GreenwiDay6Mean TimeHour6Watch correction will be added to the seconds.Minute51you change the correct you must "reselect" the Object to record proper	Kaus Aust Kochab	Type notes on individual sights below Type notes on individual sights below Step 5 Save each data entry with "Save Changes", then close data form to return to the main form Close Sight Data Form					
Star: KochabMagnitude 2.2GHAstar164 * 23.18 ' Greenwich Hour AngleDECstarN 74 * 11.17 ' DeclinationSHAstar137 * 18.76 ' Sidereal Hour AngleGHA Aries27 * 4.41 '							

This will carry the measured time, measured sextant angle, and celestial object selected with details. The steps to follow are conveniently on the form. When all the information regarding that shot is in, press the 'Save Changes'' button which allows you to advance to the next blank sight form. After you have saved your sight data, you can advance forwards or backwards to review each one. Also, you should save the whole thing in the Main Form FILE menu button. Watch error correction for seconds inconsistent with UT will be added to the times recorded (from General Settings), but the times are still UT, not local clock time. The horizon can be either the sea (normal), or bubble, or there is a check use an artificial reflective horizon (mineral oil pan). The number of stored sights is listed across the top banner. Also the yellow boxes contain the sighting being viewed and the total saved shots. Unfortunately, there is no way to totally erase a saved shot (you can edit it and resave), but you can take it out of the calculations by un-checking the "Include in the Sight Reduction" check box.

Follow these steps:

Step1) select horizon type

Step2) enter altitude measured, select limb, and enter index error

Step3) enter UTC date and time of sighting knowing the watch correction will be applied internally to the seconds

Step4) click on the celestial object in the list. Some details will appear in the bottom grey pane

Step5) click the Save Changes button on top

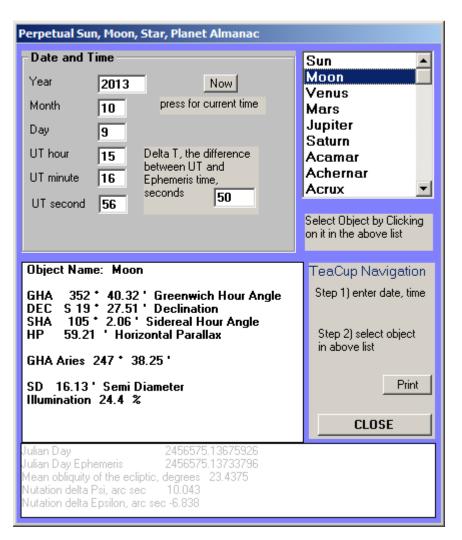
If you go back to Step 3 and change the time, you have repeat Step 4 again and reselect the celestial object. Otherwise it will have in its memory the GHA, DEC of the last time information when the object was previously selected.

You can save typed notes for each shot by typing in the provided text box on the center right.

Mac/		1111								
Sun/Moon	Rise, Set	t, and	Merid	ian Pas	sage 1	limes				
UT Date	and Tim	e —								Close
Year	2013			Now						
Month	10		press fo	or curren	t time		Clic	k here	e to Ca	lculate
UT Day	9	Ь	etween	he differ UT and	ence				Set Tin and M	nes for Ioon
			phemeri econds	s time, 6	7		r loca ngitud		t times,	set
DR Latitud	le 3	39	•		'		l or S orth	C So	uth	
DR Longit	ude 7	76	•		•	C E	E or V ast	√ • w	/est	
Sunrise 1	1:08:18 U	JT 🤅	Sunset	22:33	:25 UT	LAN	16:	51:09	UT	
Moonrise	15:59:49	UT	Moon	iset 02:	07:29	UT N	Me	.Pass.	21:03	:46 UT
Rise	PafterL and set ti								ıpper lim	Ь

Rise/Set Times

Gets you the rise and set times of the Sun and Moon based on the optical position of the upper limb coincident with the horizon. It does this for your local day, so it might report times either in the present UT, or previous/next day UT.



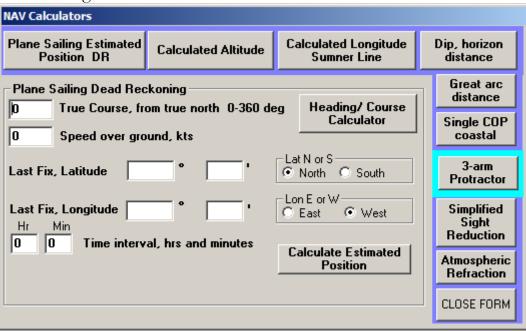
Perpetual Almanac for Sun, Moon, Stars, and Planets

The 2 steps are listed on the form to get the instantaneous GHA and Declination for the object clicked. This is using the actual UT time typed in and does not have watch error included.

DeltaT is the difference between Dynamical Time and UT. It is set from the main form under General Settings. If this value is known then the ephemeris results from the internal celestial almanac will be accurate for perhaps centuries. The US naval observatory has DeltaT information at their web site http://maia.usno.navy.mil/. Look for 'Delta T values' on the web page. See appendix 1 for a list of DeltaT for different years.

Calculator Utilities

Along the top menu bar of the main form is an item labeled "Calculators". In all cases, fill in the text windows, then mouse click the button that says "Calculate...".



Plane Sailing

This should be self-explanatory. Use the Heading/ Course calculator to convert your heading, speed in the water, current and leeway into a true course and speed over ground. It also does the inverse, in that if you wanted a TC to steer by it will calculate the proper heading, accounting for leeway and current.

Current and Course

True course calculator from leeway and currents				
True course calculator from leeway and current CLOSE				
030 Heading (relative to true north) 0-360 degrees				
8 Ship speed in the water, knots				
-3 Leeway angle: pushing the boat to the right is +, to the left is - degrees relative course (discounting tide) would be heading + leeway				
230 Direction of current (forward movement relative to true north) 0-360 degrees				
3 Speed of current, knots Click to calculate				
True course = 14.4 deg from true N				
Speed over ground = 5.4 knots Load Results in Main Form				
Heading calculator from leeway and current Fill in the above fields for ship speed, leeway, and current				
14.4 Desired True Course (relative to true north) 0-360 degrees Click to calculate				
Heading course = 30 deg from true N				
Speed over ground = 5.4 knots				

Current set is the direction the current is moving towards, whereas winds are noted for their origin, where they are coming from.

Atmospheric Refraction

Altitude Correction, Refraction		
Air Temperature, deg C	15	Calculate Refraction Correction
Barometric pressure, millibars	1010	
25 ° 35 ' Apparent	Altitude, Ha	3
Refraction correction = -2.04	l' arc minute	:5

Altitude correction usually involves semidiameter and refraction, but for stars it's just refraction.

Calculated Altitude

I	- Calculated Altitude
	Assumed Latitude 40 • 12 • C North © South
	Assumed Longitude 179 • 45 • Lon E or W
	GHA 171 ° 15 '
	DEC 11 ° 59.6 ' ON CS Calculate Altitude Hc
	Hc = 37° 8.5'

Sumner Line

Calculated Longitude for Sumner Line
Assumed Latitude 40 • 12 • C North • South
Observed Altitude 37 ° 12 '
GHA 171 ° 15 '
DEC 11 ° 59.6 ' • N • S Calculate Longitude
LON west side = W 179* 50.9' LON east side = W 162* 39'

Make 2 calculations with slightly different assumed latitude and you will have two lat-lon points to create your Sumner LOP.

Dip of the Horizon

Dip and Distance to Horizon (to edge of sea, or edge of nearby land) —						
Eye height above water, meters	4					
Distance to sea horizon, nmiles: 4.2						
Dip of horizon, arcminutes: 3.7						
Compensate for land horizon by subtracting 0.2' from the measured sextant altitude						
In the Sight Data Form, normal dip is accounted for internally, so you have to trick the data						

This tells you the dip angle and distance to the visible horizon. Also, if you use the shore edge of land this will tell you the dip angle to that. It also prints the difference in dip correction which can be added to the sextant measurement (normal dip is calculated internally to the software, so you have to "trick" it with additional correction if you want to use the beach edge of land as your horizon.

Great Arc Distance

Great Arc Distance bewteen two locations							
Latitude #1 30 ° 2 '	● North ● South						
Longitude #1 40 ° 31 '	⊂ Lon E or W ◯ East						
Latitude #2 36 ° 56 '	Lat N or S						
Longitude #2 43 ° 16 '	C East West						
436.2 nautical miles 501.7 statute miles	Calculate the Distance						

This should be self-explanatory.

(COP coastal (Circle of Position)							
	-2 known land	marks ar	nd n	neasi	ured a	ngle betv	veen (Circle d	of Position) —
	Latitude #1	0	•	0		─Lat N or ● North	S C South	Known most Western
	Longitude #1	0	•	0	<u>'</u>	 Lon E or East 	W O West	Landmark
	Latitude #2	0	•	2		Lat N or North	S O South	Known most Eastern
	Longitude #2	0	•	3	<u>'</u>	−Lon E or ● East	W O West	Landmark
	Measured Ang	le 3	2	°		_' [Calculate c away from	enter point 1st point
	Center of arc is 3.1 nm East , 1.4 nm South from 1st point							
	Draw arc using center point and radius reaching 1st or 2nd point (observer on arc)							

This gives the location of a circle's center where the arc passes thru both locations and the observer who measures the included angle. The location is in nautical miles away relative to the 1st location. You can then draw an arc on your chart with the given centerpoint, and the radius will be by stretching the compass to either the 1st or 2nd landmark on the chart. Do this this with a 3rd landmark (use 2nd and 3rd as inputs) to get another circle. Where the 2 intersect is you position fix.

3-Arm Protractor (3-Point Resection) using Farley Method giving 2 Circles Of	Position for Coastal Position Fix
3-point problem (3 known landmarks and measured angles between). Best when middle landmark is closest. Fill in landmark data, then angles, then press Calculate	Δ N
Latitude #1 31 ° 0 C S Landmark on Left (point A)	
Longitude #1 65 ° 0 CE CW	-
Latitude #2 31 ° 2 Lat N or S Landmark in Middle (point B)	
Longitude #2 65 ° 3 C E © W	
Latitude #3 31 ° 3 C N C S Landmark on Right (point C)	
Longitude #3 65 ° 8 ' C E • W	
Measured Angle between points A and B 34 ° '	
Measured Angle between points B and C 45	
Calculate Observer Position END PROGRAM 1.0 Zoom Factor	
Position Fix N 31 * 5.45 ' W 65 * 1.41 '	
Radial distance from Left Landmark 5.58 nmiles Radial distance from Middle Landmark 3.71 nmiles Radial distance from Right Landmark 6.15 nmiles	Coastal Circles Of Positions by TeaCup Navigation
Tic marks on plot are 1.0 nautical mile increments	Coastal COP ver 1.0a
Left click and drag cursor to pan plot. Right click and drag to zoom.	Grab corner to resize>

3-arm Protractor (3-point resection in surveyor's parlance)

With 3 landmarks, this automates elements of the last calculator (COP coastal). This plots with N up, E to the right, but the definition of left, middle, right landmarks are all relative to **you** the observer which is marked as a red circle. The small black circles are the landmarks, and the large grey circles are the circles of position created with the two angle measurements. The radial distances between the position fix and the landmarks are graphically represented with the magenta lines.

Simplified Sight Reduction

Single Shot Simplified Reduction Form (good for training)	
Sextant Data Close Close 35 ° 36.7 ' Sextant Altitude Measured, Hs	
1 Index Correction IC, arc minutes (on scale is - IC)	
Corrections -1.33 Altitude Correction, arc minutes (if you include semi diameter, make SD = 0 below)	
15.82 Semi Diameter SD, arc minutes (+ for LL, - for UL) for sun and lunar observations	
0.08 Horizontal Parallax, HP, arc minutes (PA will be calculated internally) mostly for lunar observations	
-2.92 Dip Correction, arc minutes (always a negative number)	
Almanac Data (at time of shot) Assumed Position GHA 138 18.7 Show Almanac DEC 19 1.4 N O S Assumed Position Latitude Latitude 39 43 Longitude 162 48	
Hc = 35* 44' Azimuth = 94.3*	
Observed Altitude Ho = 35* 49.3' Offset Distance = 5.25 nautical miles Towards	
GHA and DEC are gotten either from the Nautical Almanac or from the TeacupNav Almanac using the time of the shot to get the instantaneous values. That is up to you to figure out!	
Local Hour Angle LHA = 301° 6.7′ E Apparent Altitude Ha = 35° 34.7′ Parallax in altitude PA = 0° 0′	

This lets you look up in the Nautical Almanac (or use the built-in Perpetual Almanac tool) the astronomical data, and manually enter all other data so you can excersise the line-by-line hand-shaping of the input data. This gets you an appreciation of whats involved before you even get to calculating altitudes and intercepts. This calculator does the last step of crunching out the altitudes, intercept and azimuth. For the most precise lunar LOPs, the SD should be the augmented SD. The SD as calculated in almanacs is based on being at the center of the Earth, which we of course are not. The higher the altitude measured, the closer you are to the moon (by a wee little bit) and it slightly enlargens the SD. The difference to your LOP will be measured in the tenths of miles.

Lunars

Step 1) Fill out the estimated latitude and longitude

Step 2) Enter the observed arc distance, date, and estimated time. The arc distance entered here should be corrected for index error.

Step 3) Select the object you were measuring to. Click to calculate!

Lunar Distance current Data fil	e: Nov10-2010-Jupiter#2.LUN
OpenFile SaveFile	
Clearing the Lunar Distance with1 m	neasurement and an estimated position CLOSE
Air Temperature, deg C 14 Baro	metric pressure, millibars 1010
Estimated Latitude 39 °	12.6 Lat N or S
Estimated Longitude 76 °	49.8 C East West
Nov 10 2010 Jupiter sight #2	Outer Inner
Lunar Distance Measured corrected for index error	66 ° 13.8 Conter Conter
Date and Estimated Observation TimeYear2010Nowyress for current timeMonth11Day10between UTC andEphemeris time,UTC hour23UTC minute39UTC second41	Sun Venus Mars Jupiter Saturn Acamar Achernar Achernar Acrux Adhara Aldebaran Alioth Alkaid Venus Select Celestial Object you are measuring to from the Moon by clicking on it. US naval observatory has DeltaT information at their web site http://maia.usno.navy.mil/ This makes the assumption that your latitude is fairly
Correct time at observation 23:38:12 Better Longitude W 76 * 49.7 ' Lunar Distance Cleared 65 * 29.1 ' Lunar Distance Apparent 65 * 58.5 ' Augmented Semidiameter -15.32 '	Click here to Calculate Correct Time and Longitude

Internally it is a good algorithm where the assumption is made that your latitude is accurate, but your longitude can be off due to the error in your clock. The altitudes are calculated according to the estimated time and position. It iterates with a new time and new longitude to converge to the proper time and longitude. It's amazing how small errors such as an incorrect index correction or a compromised reading because your arms were shaking holding the sextant in a weird position, can change the results quite a bit. You can use the arc distance function in the Sight Planner to verify the cleared arc distance. See page 5. As you can see, one may save new lunar files and open old ones.

File Management

This method only accesses and can save one leg at a time, not the entire voyage in a single file. You could easily manage that with the file names. For example, a trip from New Zealand to Tahiti could have individual files with saved names NZT-1.nav, NZT-2.nav, etc... The calculated new fix from the previous file becomes the inputted last fix for the next leg of the journey. This info you have to carry over manually, but that is not much of a burden in order to save unnecessary programming complexity. You can open as may windows of TeacupCelestial as you wish, and you can have one open from the last leg while you fill out the next leg info. The lunar distance files have the extension .LUN.

The settings file for the Sight Planner is called TeacupNav.nv1 and should always be in the same folder as the executable file. If you open a data file first and that data file is located in another folder, then it might expect to find a TeacupNav.nv1 file there instead. If one is not there then it will report that there is a problem and continue with blanks in the settings. You should arrange the program such that the executable file, the data files, and the TeacupNav.nv1 file are all in the same folder.

Appendix 1Values for DeltaT, recent, future, and historical

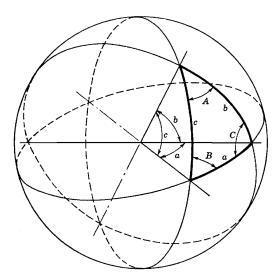
Year 2013.00 2013.25 2013.50 2013.75 2014.00 2014.25 2014.50 2014.50 2014.00 2015.00 2015.00 2015.00 2017.00 2019.00 2020.00 2022.00 2023.00	5 67.026 6 67.121 5 67.158 6 67.267 5 67.379 6 67.8 9 67.9 9 68.4 9 69. 9 70. 9 71.
Recent H 1960 1961 1962 1963 1964 1965 1966 1967 1968 1969 1970 1971 1972 1973 1974 1975 1976 1977 1978 1977 1978 1979 1980 1981 1982 1983 1984 1985 1984 1985 1986 1987 1988 1989 1990 1991 1992	Historical Values for DeltaT 33.150 33.584 33.992 34.466 35.030 35.738 36.546 37.429 38.291 39.204 40.182 41.170 42.227 43.373 44.486 45.477 46.458 47.521 48.535 49.589 50.540 51.382 52.168 52.957 53.789 53.7882 54.3427 54.8712 55.3222 55.8197 56.3000 56.8553 57.5653 58.3092

Appendix 2

Derivation of the equations used in clearing the lunar distance

Useful identities: $sin(\alpha) = cos(\alpha - 90^{\circ})$ $cos(\alpha) = -sin(\alpha - 90^{\circ})$

Spherical Trigonometry



Three Great Circles on a sphere will intersect to form three solid corner angles a, b, c, and three surface angles A, B, C. Every intersecting pair of Great Circles is the same as having two intersecting planes. The angles between the intersecting planes are the same as the surface angles on the surface of the sphere. Relationships between the corner angles and surface angles have been worked out over the centuries, with the law of sines and the law of cosines being the most relevant to navigation.

Law of Sines: $\sin(a)/\sin(A) = \sin(b)/\sin(B) = \sin(c)/\sin(C)$ Law of Cosines: $\cos(a) = \cos(b) \cdot \cos(c) + \sin(b) \cdot \sin(c) \cdot \cos(A)$

(for spherical trigonometry; there are similar ones for plane trig)

Law of Cosines in terms of co-angles: $sin(90-a) = sin(90-b) \cdot sin(90-c) + cos(90-b) \cdot cos(90-c) \cdot cos(A)$

$$S = s + R_s$$

$$M = m + R_m$$

$$d = d_{sextant} + IC + SD_{aug}$$

$$\cos(d) = \sin(s) \cdot \sin(m) + \cos(s) \cdot \cos(m) \cdot \cos(\delta)$$

$$\cos(D) = \sin(S) \cdot \sin(M) + \cos(S) \cdot \cos(M) \cdot \cos(\delta)$$

$$\cos(\delta) = \frac{\cos(d) - \sin(s) \cdot \sin(m)}{\cos(s) \cdot \cos(m)}$$

$$\cos(D) = \sin(S) \cdot \sin(M) + \cos(S) \cdot \cos(M) \cdot \left[\frac{\cos(d) - \sin(s) \cdot \sin(m)}{\cos(s) \cdot \cos(m)}\right]$$

$$\cos(D) = \sin(S) \cdot \sin(M) + (\cos(d) - \sin(s) \cdot \sin(m)) \cdot \left[\frac{\cos(S) \cdot \cos(M)}{\cos(s) \cdot \cos(m)}\right]$$

$$\sin(a) \cdot \sin(b) = -\cos(a + b)$$

$$C_{ratio} = \left[\frac{\cos(S) \cdot \cos(M)}{\cos(s) \cdot \cos(m)}\right]$$

$$\cos(D) = (\cos(d) + \cos(s + m)) \cdot C_{ratio} - \cos(S + M)$$

$$S = s + R_s$$
$$M = m + R_m$$
$$d = d_{sextant} + IC + SD_{aug}$$

$$\cos(d) = \sin(s) \cdot \sin(m) + \cos(s) \cdot \cos(m) \cdot \cos(\delta)$$
$$\cos(D) = \sin(S) \cdot \sin(M) + \cos(S) \cdot \cos(M) \cdot \cos(\delta)$$

$$\cos(\delta) = \frac{\cos(d) - \sin(s) \cdot \sin(m)}{\cos(s) \cdot \cos(m)}$$

$$\cos(D) = \sin(S) \cdot \sin(M) + \cos(S) \cdot \cos(M) \cdot \left[\frac{\cos(d) - \sin(s) \cdot \sin(m)}{\cos(s) \cdot \cos(m)}\right]$$

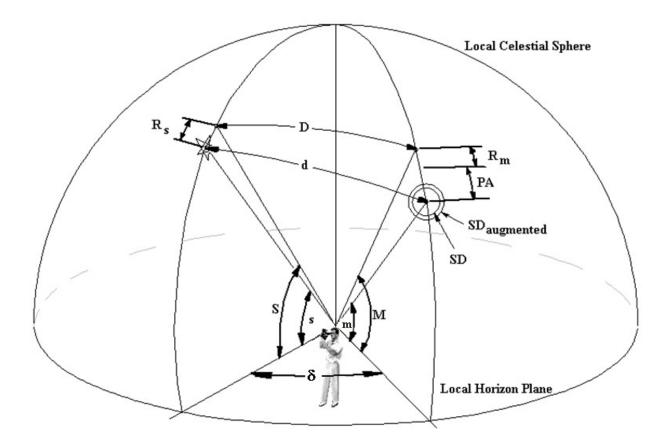
$$\cos(D) = \sin(S) \cdot \sin(M) + \left(\cos(d) - \sin(s) \cdot \sin(m)\right) \cdot \left[\frac{\cos(S) \cdot \cos(M)}{\cos(s) \cdot \cos(m)}\right]$$

 $\sin(a) \cdot \sin(b) = -\cos(a+b)$

$$C_{ratio} = \left[\frac{\cos(S) \cdot \cos(M)}{\cos(s) \cdot \cos(m)}\right]$$

 $\cos(D) = (\cos(d) + \cos(s+m)) \cdot C_{ratio} - \cos(S+M)$

$$D = \operatorname{arcCos}\left[\left(\cos(d) + \cos(s+m)\right) \cdot C_{\operatorname{ratio}} - \cos(S+M)\right]$$



The key to the problem is to realize that the parallax and refraction corrections only change the altitudes, not the 'wedge angle' δ . When the corrections are applied, and using the law of cosines, the equation with s, m can be related to S, M with the common angle δ . Even though refraction corrections are negative, the picture is drawn in the positive direction to establish a consistent sign convention.