

Q	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
1	Correctly shows that either $f(3) = 0$ , $f(-2) = 0$ or $f\left(-\frac{1}{2}\right) = 0$	M1	3.1a	4th  Divide polynomials by linear expressions with no remainder
	Draws the conclusion that $(x - 3)$ , $(x + 2)$ or $(2x + 1)$ must therefore be a factor.	M1	2.2a	
	Either makes an attempt at long division by setting up the long division, or makes an attempt to find the remaining factors by matching coefficients. For example, stating $(x - 3)(ax^2 + bx + c) = 2x^3 - x^2 - 13x - 6$ or $(x + 2)(rx^2 + px + q) = 2x^3 - x^2 - 13x - 6$ or $(2x + 1)(ux^2 + vx + w) = 2x^3 - x^2 - 13x - 6$	M1	1.1b	
	For the long division, correctly finds the the first two coefficients.  For the matching coefficients method, correctly deduces that $a = 2$ and $c = 2$ or correctly deduces that $r = 2$ and $q = -3$ or correctly deduces that $u = 1$ and $w = -6$	A1	2.2a	
	For the long division, correctly completes all steps in the division.  For the matching coefficients method, correctly deduces that $b = 5$ or correctly deduces that $p = -5$ or correctly deduces that $v = -1$	A1	1.1b	
	States a fully correct, fully factorised final answer: $(x - 3)(2x + 1)(x + 2)$	A1	1.1b	
(6 marks)				

**Notes**

Other algebraic methods can be used to factorise  $h(x)$ . For example, if  $(x - 3)$  is known to be a factor then

$$2x^3 - x^2 - 13x - 6 = 2x^2(x - 3) + 5x(x - 3) + 2(x - 3) \text{ by balancing (M1)}$$

$$= (2x^2 + 5x + 2)(x - 3) \text{ by factorising (M1)}$$

$$= (2x + 1)(x + 2)(x - 3) \text{ by factorising (A1)}$$

Q	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
<b>2a</b>	States or implies the expansion of a binomial expression to the 8th power, up to and including the $x^3$ term. $(a+b)^8 = {}^8C_0a^8 + {}^8C_1a^7b + {}^8C_2a^6b^2 + {}^8C_3a^5b^3 + \dots$ or $(a+b)^8 = a^8 + 8a^7b + 28a^6b^2 + 56a^5b^3 + \dots$	<b>M1</b>	1.1a	5th Understand and use the general binomial expansion for positive integer n
	Correctly substitutes 1 and $3x$ into the formula: $(1+3x)^8 = 1^8 + 8 \times 1^7 \times 3x + 28 \times 1^6 \times (3x)^2 + 56 \times 1^5 \times (3x)^3 + \dots$	<b>M1</b>	1.1b	
	Makes an attempt to simplify the expression (2 correct coefficients (other than 1) or both $9x^2$ and $27x^3$ ). $(1+3x)^8 = 1^8 + 24x + 28 \times 9x^2 + 56 \times 27x^3 + \dots$	<b>M1 dep</b>	1.1b	
	States a fully correct answer: $(1+3x)^8 = 1 + 24x + 252x^2 + 1512x^3 + \dots$	<b>A1</b>	1.1b	
		<b>(4)</b>		
<b>2b</b>	States $x = 0.01$ or implies this by attempting the substitution: $1 + 24(0.01) + 252(0.01)^2 + 1512(0.01)^3 + \dots$	<b>M1</b>	2.2a	5th Find approximations using the binomial expansion for positive integer n
	Attempts to simplify this expression (2 calculated terms correct): $1 + 0.24 + 0.0252 + 0.001512$	<b>M1</b>	1.1b	
	$1.266712 = 1.2667$ (5 s.f.)	<b>A1</b>	1.1b	
		<b>(3)</b>		
<b>(7 marks)</b>				
<b>Notes</b>				

Q	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
<b>3a</b>	States or implies the expansion of a binomial expression to the 9th power, up to and including the $x^3$ term. $(a+b)^9 = {}^9C_0a^9 + {}^9C_1a^8b + {}^9C_2a^7b^2 + {}^9C_3a^6b^3 + \dots$ or $(a+b)^9 = a^9 + 9a^8b + 36a^7b^2 + 84a^6b^3 + \dots$	<b>M1</b>	1.1a	5th Use the binomial expansion to find arbitrary terms for positive integer n
	Correctly substitutes 2 and $px$ into the formula. $(2+px)^9$ $= 2^9 + 9 \times 2^8 \times px + 36 \times 2^7 \times (px)^2 + 84 \times 2^6 \times (px)^3 + \dots$	<b>M1</b>	1.1b	
	Makes an attempt to simplify the expression (at least one power of 2 calculated and one bracket expanded correctly). $(2+px)^9 = 512 + 9 \times 256 \times px + 36 \times 128 \times p^2x^2 + 84 \times 64 \times p^3x^3 + \dots$	<b>M1dep</b>	1.1b	
	States a fully correct answer: $(2+px)^9 = 512 + 2304px + 4608p^2x^2 + 5376p^3x^3 + \dots$	<b>A1</b>	1.1b	
		<b>(4)</b>		
<b>3bi</b>	States that $5376p^3 = -84$	<b>M1ft</b>	2.2a	5th Understand and use the general binomial expansion for positive integer n
	Correctly solves for $p$ : $p^3 = -\frac{1}{64} \Rightarrow p = -\frac{1}{4}$	<b>A1ft</b>	1.1b	
<b>3bii</b>	Correctly find the coefficient of the $x$ term: $2304\left(-\frac{1}{4}\right) = -576$	<b>B1ft</b>	1.1b	5th Understand and use the general binomial expansion for positive integer n
	Correctly find the coefficient of the $x^2$ term: $4608\left(-\frac{1}{4}\right)^2 = 288$	<b>B1ft</b>	1.1b	
		<b>(4)</b>		
<b>(8 marks)</b>				

**Notes**

ft marks – pursues a correct method and obtains a correct answer or answers from their 5376 from part **a**.

Q	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
4a	Attempt is made at expanding $(p+q)^5$ . Accept seeing the coefficients 1, 5, 10, 10, 5, 1 or seeing $(p+q)^5 = {}^5C_0p^5 + {}^5C_1p^4q + {}^5C_2p^3q^2 + {}^5C_3p^2q^3 + {}^5C_4pq^4 + {}^5C_5q^5$ o.e.	M1	1.1a	5th Understand and use the general binomial expansion for positive integer n
	Fully correct answer is stated: $(p+q)^5 = p^5 + 5p^4q + 10p^3q^2 + 10p^2q^3 + 5pq^4 + q^5$	A1	1.1b	
		(2)		
4b	States that $p$ , or the probability of rolling a 4, is $\frac{1}{4}$	B1	3.3	5th Use the binomial expansion to find arbitrary terms for positive integer n
	States that $q$ , or the probability of not rolling a 4, is $\frac{3}{4}$	B1	3.3	
	States or implies that the sum of the first 3 terms (or $1 -$ the sum of the last 3 terms) is the required probability. For example, $p^5 + 5p^4q + 10p^3q^2$ or $1 - (10p^2q^3 + 5pq^4 + q^5)$	M1	2.2a	
	$\left(\frac{1}{4}\right)^5 + 5\left(\frac{1}{4}\right)^4\left(\frac{3}{4}\right) + 10\left(\frac{1}{4}\right)^3\left(\frac{3}{4}\right)^2$ or $\frac{1}{1024} + \frac{15}{1024} + \frac{90}{1024}$ or $1 - \left(10\left(\frac{1}{4}\right)^2\left(\frac{3}{4}\right)^3 + 5\left(\frac{1}{4}\right)\left(\frac{3}{4}\right)^4 + \left(\frac{3}{4}\right)^5\right)$ or $1 - \left(\frac{270}{1024} + \frac{405}{1024} + \frac{243}{1024}\right)$	M1	1.1b	
	Either $\frac{53}{512}$ o.e. or awrt 0.104	A1	1.1b	
		(5)		

**(7 marks)****Notes**

Q	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
5a	Makes an attempt to interpret the meaning of $f(5) = 0$ . For example, writing $125 + 25 + 5p + q = 0$	M1	2.2a	5th Solve non-linear simultaneous equations in context
	$5p + q = -150$	A1	1.1b	
	Makes an attempt to interpret the meaning of $f(-3) = 8$ . For example writing $-27 + 9 - 3p + q = 8$	M1	2.2a	
	$-3p + q = 26$	A1	1.1b	
	Makes an attempt to solve the simultaneous equations.	M1ft	1.1a	
	Solves the simultaneous equations to find that $p = -22$	A1ft	1.1b	
	Substitutes their value for $p$ to find that $q = -40$	A1ft	1.1b	
		(7)		
5b	Draws the conclusion that $(x - 5)$ must be a factor.	M1	2.2a	5th Divide polynomials by linear expressions with a remainder
	Either makes an attempt at long division by setting up the long division, or makes an attempt to find the remaining factors by matching coefficients. For example, stating: $(x - 5)(ax^2 + bx + c) = x^3 + x^2 - 22x - 40$ (ft their $-22$ or $-40$ )	M1ft	1.1b	
	For the long division, correctly finds the the first two coefficients. For the matching coefficients method, correctly deduces that $a = 1$ and $c = 8$	A1	2.2a	
	For the long division, correctly completes all steps in the division. For the matching coefficients method, correctly deduces that $b = 6$	A1	1.1b	
	States a fully correct, fully factorised final answer: $(x - 5)(x + 4)(x + 2)$	A1	1.1b	
		(5)		



**(12 marks)****Notes**

Award full marks for correct attempt/answers to solving their simultaneous equations.

In part **b** other algebraic methods can be used to factorise:

$x - 5$  is a factor (M1)

$x^3 - x^2 - 22x - 40 = x^2(x - 5) + 6x(x - 5) + 8(x - 5)$  by balancing (M1)

$= (x^2 + 6x + 8)(x - 5)$  by factorising (M1)

$= (x + 4)(x + 2)(x - 5)$  by factorising (A1 A1) (i.e. A1 for each factor other than  $(x - 5)$ )

Q	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
6	Considers the expression $x^2 + \frac{13}{2}x + 16$ either on its own or as part of an inequality/equation with 0 on the other side.	M1	3.1a	6th Complete algebraic proofs in unfamiliar contexts using direct or exhaustive methods
	Makes an attempt to complete the square. For example, stating: $\left(x + \frac{13}{4}\right)^2 - \frac{169}{16} + \frac{256}{16}$ (ignore any (in)equation)	M1	1.1b	
	States a fully correct answer: $\left(x + \frac{13}{4}\right)^2 + \frac{87}{16}$ (ignore any (in)equation)	A1	1.1b	
	Interprets this solution as proving the inequality for all values of $x$ . Could, for example, state that $\left(x + \frac{13}{4}\right)^2 \geq 0$ as a number squared is always positive or zero, therefore $\left(x + \frac{13}{4}\right)^2 + \frac{87}{16} > 0$ . Must be logically connected with the statement to be proved; this could be in the form of an additional statement. So $x^2 + 6x + 18 > 2 - \frac{1}{2}x$ (for all $x$ ) or by a string of connectives which must be equivalent to “if and only if”s.	A1	2.1	
		(4)		
(4 marks)				
<p><b>Notes</b></p> <p>Any correct and complete method (e.g. finding the discriminant and single value, finding the minimum point by differentiation or completing the square and showing that it is both positive and a minimum, sketching the graph supported with appropriate methodology etc) is acceptable for demonstrating that <math>x^2 + \frac{13}{2}x + 16 &gt; 0</math> for all <math>x</math>.</p>				

Q	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
<b>7a</b>	Makes an attempt to expand the binomial expression $(1+x)^3$ (must be terms in $x^0, x^1, x^2, x^3$ and at least 2 correct).	<b>M1</b>	1.1a	6th Solve problems using the binomial expansion (for positive integer n) in unfamiliar contexts (including the link to binomial probabilities)
	$1+3x^2+x^3 < 1+3x+3x^2+x^3$	<b>A1</b>	1.1b	
	$0 < 3x$	<b>A1</b>	1.1b	
	$x > 0^*$ as required.	<b>A1*</b>	2.2a	
		<b>(4)</b>		
<b>7b</b>	Picks a number less than or equal to zero, e.g. $x = -1$ , and attempts a substitution into both sides. For example, $1+3(-1)^2+(-1)^3 < 1+3(-1)+3(-1)^2+(-1)^3$	<b>M1</b>	1.1a	5th Use the binomial expansion to find arbitrary terms for positive integer n
	Correctly deduces for their choice of $x$ that the inequality does not hold. For example, $3 \not< 0$	<b>A1</b>	2.2a	
		<b>(2)</b>		
<b>(6 marks)</b>				
<b>Notes</b>				