| Q | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Makes an attempt to expand $(5-3 \sqrt{x})(5-3 \sqrt{x})$. Must be 4 terms (or 3 if $\sqrt{x}$ terms collected). | M1 | 3.1 | 5th <br> Integrate more complicated functions such as those requiring simplification or rearrangement. |
|  | Fully correct expansion $25-30 \sqrt{x}+9 x$ or $25-30 x^{\frac{1}{2}}+9 x$ | A1 | 1.1b |  |
|  | Writes $\sqrt{x}$ as $x^{\frac{1}{2}}$ (or subsequently correctly integrates this term) | B1 | 1.1b |  |
|  | Makes an attempt to find $\int\left(25-30 x^{\frac{1}{2}}+9 x\right) \mathrm{d} x$. Raising $x$ power by 1 at least once would constitute an attempt. | M1 | 1.1b |  |
|  | Fully correct integration. $25 x-20 x^{\frac{3}{2}}+\frac{9}{2} x^{2}+C$ o.e. | A1 | 1.1b |  |
| (5 marks) |  |  |  |  |
| Notes |  |  |  |  |
| Award all 5 marks for a fully correct final answer, even if some working is missing. |  |  |  |  |


| Q | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
| 2 | Uses laws of indices correcty at least once anywhere in solution <br> (e.g. $\frac{1}{\sqrt{x}}=x^{-\frac{1}{2}}$ or $\sqrt{x}=x^{\frac{1}{2}}$ or $x \sqrt{x}=x^{\frac{3}{2}}$ seen or implied). | B1 | 2.2a | Find the equation of a curve given the gradient function and a point on the curve. |
|  | Makes an attempt at integrating $\mathrm{h}^{\prime}(x)=15 x^{\frac{3}{2}}-40 x^{-\frac{1}{2}}$ <br> Raising at least one $x$ power by 1 would constitute an attempt. | M1 | 1.1b |  |
|  | Fully correct integration. $6 x^{\frac{5}{2}}-80 x^{\frac{1}{2}}$ (no need for $+C$ here). | A1 | 1.1b |  |
|  | Makes an attenpt to substitute $(4,19)$ into the integrated expression. For example, $19=6 \times 4^{\frac{5}{2}}-80 \times 4^{\frac{1}{2}}+C$ is seen. | M1 | 1.1b |  |
|  | Finds the correct value of C. $C=-13$ | A1 | 1.1b |  |
|  | States fully correct final answer $\mathrm{h}(x)=6 x^{\frac{5}{2}}-80 \sqrt{x}-13$ or any equivalent form. | A1 | 2.2a |  |
| (6 marks) |  |  |  |  |
| Notes |  |  |  |  |
| Award all 6 marks for a fully correct final answer, even if some working is missing. |  |  |  |  |


| Q | Scheme |  | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3a | Makes an attempt to find $\int(10-6 x) \mathrm{d} x$ <br> Raising $x$ powers by 1 would constitute an attempt. |  | M1 | 1.1b | 5th <br> Find definite integrals |
|  | Shows a fully correct integral with limits. $\left[10 x-3 x^{2}\right]_{a}^{2 a}=1$ |  | A1 | 2.2a |  |
|  | Makes an attempt to substitute the limits into their expression. For example, $\left(10(2 a)-3(2 a)^{2}\right)-\left(10(a)-3(a)^{2}\right)$ or $\left(20 a-12 a^{2}\right)-\left(10 a-3 a^{2}\right)$ is seen. |  | M1ft | 1.1b |  |
|  | Rearranges to a 3-term quadratic equation (with $=0$ ).$9 a^{2}-10 a+1=0$ |  | M1ft | 1.1b |  |
|  | Correctly factorises the LHS: $(9 a-1)(a-1)=0$ or uses a valid method for solving a quadratic equation (can be implied by correct answers). |  | M1ft | 1.1b |  |
|  | States the two fully correct answers $a=\frac{1}{9}$ or $a=1$ <br> For the first solution accept awrt 0.111 |  | A1 | 1.1b |  |
|  |  |  | (6) |  |  |
| 3b | Figure 1 | Straight line sloping downwards with positive $x$ and $y$ intercepts. Ignore portions of graph outside $0 \leqslant x \leqslant 2$ | M1 | 3.1 | 1st <br> Assumed <br> Knowledge |
|  |  | Fully correct sketch with points $(0,10)$, and $\left(\frac{5}{3}, 0\right)$ <br> labelled. Ignore portions of graph outside $0 \leqslant x \leqslant 2$ | A1 | 2.2a |  |
|  |  |  | (2) |  |  |



| Q | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
| 4 | Writes $\sqrt{t}$ as $t^{\frac{1}{2}}$ or $50 \sqrt{t}$ as $50 t^{\frac{1}{2}}$ (can be implied by correct integral). | B1 | 2.2a | Integrate more complicated functions such as those requiring simplification or rearrangement. |
|  | Makes an attempt to find $\frac{1}{20} \int\left(50 t^{\frac{1}{2}}+20 t^{2}-t^{3}\right) \mathrm{d} t$. Raising at least one $t$ power by 1 would constitute an attempt. | M1 | 1.1b |  |
|  | Makes a fully correct integration (ignore limits at this stage). $s=\frac{1}{20}\left[\frac{100}{3} t^{\frac{3}{2}}+\frac{20}{3} t^{3}-\frac{t^{4}}{4}\right]_{0}^{20}$ | M1 | 1.1b |  |
|  | Makes an attempt to substitute the limits into their integrated function. For example, $\frac{1}{20}\left[\left(\frac{100}{3} \times 20^{\frac{3}{2}}+\frac{20 \times 20^{3}}{3}-\frac{20^{4}}{4}\right)-\left(\frac{100}{3} \times 0^{\frac{3}{2}}+\frac{20 \times 0^{3}}{3}-\frac{0^{4}}{4}\right)\right]$ <br> is seen. Award mark even if the 0 limit is not shown. | M1ft | 1.1b |  |
|  | States fully correct answer. $s=816$ cao. | A1 | 1.1b |  |
|  |  |  |  | (5 marks) |
|  | Notes |  |  |  |


| Q | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
| 5a | Attempts to take out $x$ or $-x$. $y=x\left(-x^{2}+2 x+8\right) \text { or } y=-x\left(x^{2}-2 x-8\right)$ | M1 | 3.1 | 4th <br> Factorise cubic expressions with monomial factors. |
|  | Fully and correctly factorised cubic. $y=x(4-x)(2+x) \text { or } y=-x(x-4)(x+2)$ | M1 | 1.1b |  |
|  | Correct coordinates written. $A(-2,0)$ and $B(4,0)$. | A1 | 1.1b |  |
|  |  | (3) |  |  |
| 5b | Makes an attempt to find $\int\left(-x^{3}+2 x^{2}+8 x\right) \mathrm{d} x$ <br> Raising at least one $x$ power by 1 would constitute an attempt. | M1 | 3.1a | 5th <br> Find an area below the $x$-axis using integration (including an appreciation of the meaning of a negative definite integral). |
|  | Fully correct integration seen. <br> $\left[-\frac{x^{4}}{4}+\frac{2}{3} x^{3}+4 x^{2}\right]_{-2}^{0}$ (ignore limits at this stage) | A1 | 1.1b |  |
|  | Makes an attempt to substitute limits into integrated function to find the area between $x=-2$ and $x=0$ $(0)-\left(-4-\frac{16}{3}+16\right)$ | M1 | 1.1 b |  |
|  | Finds the correct answer. $-\frac{20}{3}$ | A1 | 1.1b |  |
|  | $+\frac{20}{3}$ stated or used as area here or later in solution (could be implied by correct final answer). | B1 | 3.2 |  |
|  | Makes an attempt to substitute limits into integrated function to find the area between $x=0$ and $x=4$ $\left(-64+\frac{128}{3}+64\right)-(0)$ | M1 | 1.1b |  |
|  | Finds the correct answer. $\frac{128}{3}$ | A1 | 1.1b |  |



| Q | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
| 6a | Equates the curve and the line. $x^{2}-8 x+20=x+6$ | M1 | 3.1 | 4th <br> Interpret solutions to simultaneous equations graphically. |
|  | Simplifies and factorises. $(x-7)(x-2)=0$ (or uses other valid method for solving a quadratic equation). | M1 | 1.1b |  |
|  | Finds the correct coordinates of $A$. $A(2,8)$. | A1 | 1.1b |  |
|  | Finds the correct coordinates of $B . B(7,13)$. | A1 | 1.1b |  |
|  |  | (4) |  |  |
| 6b | Makes an attempt to find the area of the trapezium bounded by $x=2, x=7$, the $x$-axis and the line. <br> For example, $\frac{5}{2}(8+13)$ or $\int_{2}^{7}(x+6) \mathrm{d} x$ seen. | M1 | 3.1 | 1st <br> Assumed <br> Knowledge |
|  | Correct answer. Area $=52.5$ o.e. | A1 | 1.1b |  |
|  |  | (2) |  |  |
| 6c | $\int_{2}^{7}\left(x^{2}-8 x+20\right) \mathrm{d} x$. | B1 | 3.1 | 5th <br> Find the area under a curve using integration. |
|  | Makes an attempt to find the integral. Raising at least one $x$ power by 1 would constitute an attempt. | M1 | 1.1b |  |
|  | Correctly finds $\left[\frac{1}{3} x^{3}-4 x^{2}+20 x\right]_{2}^{7}$ | A1 | 1.1b |  |
|  | Makes an attempt to substitute limits into the definite integral. $\left[\left(\frac{343}{3}-196+140\right)-\left(\frac{8}{3}-16+40\right)\right]$ | M1 | 1.1b |  |
|  | Correct answer seen. $\frac{95}{3}$ or $31 . \dot{6}$ oe seen. | A1 | 1.1b |  |
|  |  | (5) |  |  |


| 6d | Understands the need to subtract the two areas. $\pm(52.5-31.6)$ | M1 | 2.2a | 5th <br> Find the area under a curve using integration. |
| :---: | :---: | :---: | :---: | :---: |
|  | 20.8 units $^{2}$ seen (must be positive). | A1 | 2.2a |  |
|  |  | (2) |  |  |
| (13 marks) |  |  |  |  |
| Notes |  |  |  |  |
| 6a If A 0 A 0 , award A 1 for full solution of quadratic equation (i.e. $x=2, x=7$ ). |  |  |  |  |

