| Q | Scheme | Marks | AOs | Pearson Progression Step and Progress descriptor | |
|--|---|-------|------|---|--|
| 1 | Makes an attempt to expand $(5-3\sqrt{x})(5-3\sqrt{x})$. Must be 4 | M1 | 3.1 | 5th | |
| | terms (or 3 if \sqrt{x} terms collected). | | | Integrate more complicated | |
| | Fully correct expansion $25 - 30\sqrt{x} + 9x$ or $25 - 30x^{\frac{1}{2}} + 9x$ | A1 | 1.1b | functions such as those requiring simplification or rearrangement. | |
| | Writes \sqrt{x} as $x^{\frac{1}{2}}$ (or subsequently correctly integrates this term) | B1 | 1.1b | | |
| | Makes an attempt to find $\int (25 - 30x^{\frac{1}{2}} + 9x) dx$. Raising x | M1 | 1.1b | | |
| | power by 1 at least once would constitute an attempt. | | | | |
| | Fully correct integration. $25x - 20x^{\frac{3}{2}} + \frac{9}{2}x^2 + C$ o.e. | A1 | 1.1b | | |
| (5 marks) | | | | | |
| Notes | | | | | |
| Award all 5 marks for a fully correct final answer, even if some working is missing. | | | | | |

| Q | Scheme | Marks | AOs | Pearson Progression Step and Progress descriptor | |
|---|---|-------|------|--|--|
| 2 | Uses laws of indices correctly at least once anywhere in solution (e.g. $\frac{1}{\sqrt{x}} = x^{-\frac{1}{2}}$ or $\sqrt{x} = x^{\frac{1}{2}}$ or $x\sqrt{x} = x^{\frac{3}{2}}$ seen or implied). | B1 | 2.2a | 5th Find the equation of a curve given the gradient function and a point on the curve. | |
| | Makes an attempt at integrating $h'(x) = 15x^{\frac{3}{2}} - 40x^{-\frac{1}{2}}$ Raising at least one <i>x</i> power by 1 would constitute an attempt. | M1 | 1.1b | | |
| | Fully correct integration. $6x^{\frac{5}{2}} - 80x^{\frac{1}{2}}$ (no need for + <i>C</i> here). | A1 | 1.1b | | |
| | Makes an attempt to substitute (4, 19) into the integrated expression. For example, $19 = 6 \times 4^{\frac{5}{2}} - 80 \times 4^{\frac{1}{2}} + C$ is seen. | M1 | 1.1b | | |
| | Finds the correct value of C. $C = -13$ | A1 | 1.1b | | |
| | States fully correct final answer $h(x) = 6x^{\frac{5}{2}} - 80\sqrt{x} - 13$ or any equivalent form. | A1 | 2.2a | | |
| | (6 marks) | | | | |

Notes

Award all 6 marks for a fully correct final answer, even if some working is missing.

| Q | Sch | eme | Marks | AOs | Pearson Progression Step and Progress descriptor | |
|------------|---|--|-------|------|---|--|
| 3 a | Makes an attempt to find $\int (10-6x) dx$ | | M1 | 1.1b | 5th Find definite | |
| | Raising <i>x</i> powers by 1 would c | constitute an attempt. | | | integrals | |
| | Shows a fully correct integral | with limits. $\left[10x - 3x^2\right]_a^{2a} = 1$ | A1 | 2.2a | analytically. | |
| | Makes an attempt to substitute For example, $(10(2a) - 3(2a))$ | the limits into their expression. $\binom{2}{-(10(a)-3(a)^2)}$ or | M1ft | 1.1b | _ | |
| | $(20a-12a^2)-(10a-3a^2)$ is | seen. | | | | |
| | Rearranges to a 3-term quadrative $9a^2 - 10a + 1 = 0$ | tic equation (with $= 0$). | M1ft | 1.1b | | |
| | Correctly factorises the LHS: (valid method for solving a qua by correct answers). | (9a-1)(a-1) = 0 or uses a dratic equation (can be implied | M1ft | 1.1b | | |
| | States the two fully correct ans | swers $a = \frac{1}{9}$ or $a = 1$ | A1 | 1.1b | | |
| | For the first solution accept aw | vrt 0.111 | | | | |
| | | | (6) | | | |
| 3b | Figure 1 | Straight line sloping downwards with positive x and y intercepts. Ignore portions of graph outside $0 \le x \le 2$ | M1 | 3.1 | 1st Assumed Knowledge | |
| | 8 7 6 5 4 3 2 1 | Fully correct sketch with points (0, 10), and $(\frac{5}{3}, 0)$ labelled. Ignore portions of graph outside $0 \le x \le 2$ | A1 | 2.2a | | |
| | $0 \qquad 1 \qquad \frac{5}{3} \qquad \frac{2}{3} \qquad x$ | | (2) | | | |

| 3c | Statements to the effect that the (definite) integral will only equal the area (1) if the function is above the <i>x</i> -axis (between the limits) AND when $a = 1$, $2a = 2$, so part of the area will be above the <i>x</i> - axis and part will be below the <i>x</i> -axis. | B1 | 2.1 | 5th Find an area below the <i>x</i> -axis using integration (including an appreciation of the meaning of a negative definite integral). |
|----|---|-----|------|---|
| | Greater than 1. | B1 | 2.2a | |
| | | (2) | | |
| | | | | (10 marks) |
| | Notes | | | |
| | | | | |
| | | | | |
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| Q | Scheme | Marks | AOs | Pearson Progression Step and Progress descriptor | |
|----------|--|-------|------|---|--------------------------------------|
| 4 | Writes \sqrt{t} as $t^{\frac{1}{2}}$ or $50\sqrt{t}$ as $50t^{\frac{1}{2}}$ (can be implied by correct integral). | B1 | 2.2a | 5th Integrate more complicated functions such as those requiring simplification or rearrangement. | 5th Integrate more complicated |
| | Makes an attempt to find $\frac{1}{20}\int (50t^{\frac{1}{2}} + 20t^2 - t^3)dt$. Raising at least one <i>t</i> power by 1 would constitute an attempt. | M1 | 1.1b | | |
| | Makes a fully correct integration (ignore limits at this stage). $s = \frac{1}{20} \left[\frac{100}{3} t^{\frac{3}{2}} + \frac{20}{3} t^{3} - \frac{t^{4}}{4} \right]_{0}^{20}$ | M1 | 1.1b | | |
| | Makes an attempt to substitute the limits into their integrated function. For example, $\frac{1}{20} \left[\left(\frac{100}{3} \times 20^{\frac{3}{2}} + \frac{20 \times 20^{3}}{3} - \frac{20^{4}}{4} \right) - \left(\frac{100}{3} \times 0^{\frac{3}{2}} + \frac{20 \times 0^{3}}{3} - \frac{0^{4}}{4} \right) \right]$ is seen. Award mark even if the 0 limit is not shown. | M1ft | 1.1b | | |
| | States fully correct answer. $s = 816$ cao. | A1 | 1.1b | | |
| (5 marks | | | | | |
| | Notes | | | | |
| | | | | | |

| Q | Scheme | Marks | AOs | Pearson Progression Step and Progress descriptor |
|----|--|-------|------|--|
| 5a | Attempts to take out x or $-x$. | M1 | 3.1 | 4th |
| | $y = x(-x^2 + 2x + 8)$ or $y = -x(x^2 - 2x - 8)$ | | | Factorise cubic expressions with |
| | Fully and correctly factorised cubic. | M1 | 1.1b | monomial factors. |
| | y = x(4-x)(2+x) or $y = -x(x-4)(x+2)$ | | | |
| | Correct coordinates written. $A(-2,0)$ and $B(4, 0)$. | A1 | 1.1b | |
| | | (3) | | |
| 5b | Makes an attempt to find $\int (-x^3 + 2x^2 + 8x) dx$ | M1 | 3.1a | 5th |
| | Raising at least one <i>x</i> power by 1 would constitute an attempt. | | | Find an area below the <i>x</i> -axis |
| | Fully correct integration seen. | A1 | 1.1b | using integration (including an |
| | $\left[-\frac{x^4}{4} + \frac{2}{3}x^3 + 4x^2\right]_{-2}^0$ (ignore limits at this stage) | | | appreciation of the meaning of a negative definite integral). |
| | Makes an attempt to substitute limits into integrated function to find the area between $x = -2$ and $x = 0$ | M1 | 1.1b | |
| | $(0) - \left(-4 - \frac{16}{3} + 16\right)$ | | | |
| | Finds the correct answer. $-\frac{20}{3}$ | A1 | 1.1b | |
| | $+\frac{20}{3}$ stated or used as area here or later in solution (could be implied by correct final answer). | B1 | 3.2 | |
| | Makes an attempt to substitute limits into integrated function to find the area between $x = 0$ and $x = 4$ | M1 | 1.1b | |
| | $\left(\frac{-04+\frac{1}{3}+04}{-0}\right)^{-(0)}$ | | | |
| | Finds the correct answer. $\frac{128}{3}$ | A1 | 1.1b | |

| | Correctly adds the two areas. $\frac{148}{3}$ o.e. | A1 | 2.2a | | | |
|---|--|-----|------|--|--|--|
| | | (8) | | | | |
| | (11 marks) | | | | | |
| Notes | | | | | | |
| 5a Award method marks for substituting limits even if evaluation at $x = 0$ is not seen. | | | | | | |
| 5b For the first integral, candidates may integrate $-f(x)$ between -2 and 0 to obtain a positive answer directly. | | | | | | |

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| Q | Scheme | Marks | AOs | Pearson Progression Step and Progress descriptor |
|----|---|-------|------|---|
| 6a | Equates the curve and the line. $x^2 - 8x + 20 = x + 6$ | M1 | 3.1 | 4th |
| | Simplifies and factorises. $(x - 7)(x - 2) = 0$ (or uses other valid method for solving a quadratic equation). | M1 | 1.1b | Interpret solutions to simultaneous equations graphically. |
| | Finds the correct coordinates of A. $A(2, 8)$. | A1 | 1.1b | |
| | Finds the correct coordinates of B . $B(7, 13)$. | A1 | 1.1b | |
| | | (4) | | |
| 6b | Makes an attempt to find the area of the trapezium bounded by $x = 2, x = 7$, the <i>x</i> -axis and the line. For example, $\frac{5}{2}(8+13)$ or $\int_{2}^{7} (x+6)dx$ seen. | M1 | 3.1 | 1st Assumed Knowledge |
| | Correct answer. Area = 52.5 o.e. | A1 | 1.1b | |
| | | (2) | | |
| 6с | $\int_{2}^{7} (x^2 - 8x + 20) \mathrm{d}x .$ | B1 | 3.1 | 5th Find the area |
| | Makes an attempt to find the integral. Raising at least one x power by 1 would constitute an attempt. | M1 | 1.1b | under a curve using integration. |
| | Correctly finds $\left[\frac{1}{3}x^3 - 4x^2 + 20x\right]_2^7$ | A1 | 1.1b | |
| | Makes an attempt to substitute limits into the definite integral. $\left[\left(\frac{343}{3} - 196 + 140 \right) - \left(\frac{8}{3} - 16 + 40 \right) \right]$ | M1 | 1.1b | |
| | Correct answer seen. $\frac{95}{3}$ or 31.6 oe seen. | A1 | 1.1b | |
| | | (5) | | |

Mark scheme

| 6d | Understands the need to subtract the two areas. $\pm(52.5 - 31.6)$ | M1 | 2.2a | 5th Find the eree | | |
|---|--|-----|------|-------------------------------------|--|--|
| | 20.8 units ² seen (must be positive). | A1 | 2.2a | under a curve using integration. | | |
| | | (2) | | | | |
| | | | | (13 marks) | | |
| Notes | | | | | | |
| 6a If A0A0, award A1 for full solution of quadratic equation (i.e. $x = 2, x = 7$). | | | | | | |
| | | | | | | |

Pearson Edexcel AS and A level Mathematics

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