

### **Cambridge International Examinations**





MATHEMATICS 0580/43
Paper 4 (Extended) May/June 2017

MARK SCHEME

Maximum Mark: 130

Published

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#### **Abbreviations**

cao correct answer only

dependent dep

follow through after error FT ignore subsequent working isw

or equivalent oe Special Case SC

nfww not from wrong working

seen or implied soi

Question	Answer	Marks	Part marks
1(a)(i)	9550	1	
1(a)(ii)	23 158 750	2FT	FT their (a)(i) × 2425 correctly evaluated M1 for their lower bound × 2425
1(a)(iii)	23 160 000	1FT	FT their (a)(ii) rounded to 4 sf
1(a)(iv)	$2.316 \times 10^7$	1FT	FT their (a)(iii) or their (a)(ii) rounded to 3sf or more and in standard form
1(b)	520 nfww	3	M2 for $546 \times \frac{100}{(100+5)}$ oe or M1 for $105[\%]$ associated with 546 oe
1(c)	3380 or 3376 to 3377	2	<b>M1</b> for $3000 \times \left(1 + \frac{3}{100}\right)^4$ oe
2(a)	38	1	
	118	1	
	62	1FT	<b>FT</b> 180 – <i>their y</i>
2(b)	69	3	<b>B2</b> for $ACB = 42$ or <b>B1</b> for $ADB = 42$ If zero scored, <b>SC1</b> for $ACB = their ADB$
2(c)	107	2	<b>B1</b> for <i>QPS</i> = 73 or [reflex] <i>QOS</i> = 214
3(a)	0 2.25 2 1.25	4	B1 for each
3(b)	Fully correct smooth curve	4	B3 FT for 7 or 8 points or B2 FT for 5 or 6 points or B1 FT for 3 or 4 points

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Question	Answer	Marks	Part marks
3(c)	1	1	
3(d)(i)	[y=]x+1	1	
3(d)(ii)	-2.2 to -2.1	1	
	-0.45 to -0.4	1	
	0.51 to 0.6	1	If zero scored, <b>SC1</b> for <i>their</i> line in <b>(d)(i)</b> drawn. It must be of the form $y = mx + c$ $(m \ne 0)$ and drawn 'fit for purpose'
3(e)	-1.33 < k < 0  to $0.1$	2FT	FT Strict ft of <i>their</i> max point and min point dep on cubic graph or accept correct answer from calculus B1 for each If zero scored, SC1 for two correct values reversed
4(a)(i)	17.5 or 17.46nfww	6	<b>B3</b> for triangle height 3.46[4] or $\sqrt{12}$ oe or <b>M2</b> for $\sqrt{4^2 - 2^2}$ or <b>M1</b> for $h^2 + 2^2 = 4^2$ and <b>M2</b> for $2 \times 7 + \frac{1}{2} \times 2 \times their \ h$ oe or <b>M1</b> for $\frac{1}{2} \times 2 \times their \ h$
4(a)(ii)	140 or 139.6 to 139.7	1FT	FT their (a) × 8
4(b)(i)	2.62 or 2.618	3	<b>M2</b> for $[r^2 = ] \frac{280}{13\pi}$ oe or <b>M1</b> for $280 = \pi \times r^2 \times 13$
4(b)(ii)	10.2 or 10.20 or $10\frac{10}{49}$	3	<b>M2</b> for $\frac{280}{14^3}$ [×100] oe
			or <b>B1</b> for 2744 or 14 <sup>3</sup> seen
5(a)(i)	80 33 20	1, 1, 1	
5(a)(ii)	17.3 nfww	4	<b>M1</b> for 5, 15, 22.5, 27.5, 40 soi
			M1 for $\sum fx$ with <i>their f</i> 's and x in correct interval including both boundaries
			<b>M1</b> (dep on 2nd <b>M1</b> ) for $\sum fx \div 200$

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Question	Answer	Marks	Part marks
5(b)(i)	$\frac{30}{210}$ oe	2	M1 for $\frac{6}{15} \times \frac{5}{14}$ If zero scored, SC1 for answer $\frac{36}{225}$ oe
5(b)(ii)	$\frac{108}{210}$ oe	3	M2 for $\frac{6}{15} \times \frac{9}{14} + \frac{9}{15} \times \frac{6}{14}$ oe or $1 - \frac{9}{15} \times \frac{8}{14} - \frac{6}{15} \times \frac{5}{14}$ or M1 for $\frac{6}{15} \times \frac{9}{14}$ or $\frac{9}{15} \times \frac{6}{14}$ or $\frac{9}{15} \times \frac{8}{14} + \frac{6}{15} \times \frac{5}{14}$ If zero scored, SC1 for answer $\frac{108}{225}$ oe
5(c)	150	1	
6(a)(i)	Translation	1	
	$\begin{pmatrix} 3 \\ -13 \end{pmatrix}$ oe	1	
6(a)(ii)	Enlargement	1	
	$[sf] - \frac{1}{2}$ oe	1	
	(0, -4)	1	
6(b)	Image at (0,0)(0,6)(-4,6)(-4,2)	2	B1 for rotation of 90° anticlockwise about the wrong centre or 90° clockwise about (3, -1) or 4 points correct but not joined.
6(c)	Image at (4,0)(10,0)(10,-4)(6,-4)	2	<b>B1</b> for reflection in $y = k$ or in $x = 1$ or 4 points correct but not joined
6(d)	Enlargement	1	
	[sf] 3	1	
	Origin oe	1	

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Question	Answer	Marks	Part marks
7(a)	[x=]-5	4	M1 for correctly equating one set of coefficients
	[y =] 7 with correct working		M1 for correct method to eliminate one variable
			OR
			M1 for correctly rearranging one equation
			M1 for correct method to eliminate one variable
			A1 $x = -5$ A1 $y = 7$ both dep on M2
			If zero scored, <b>SC1</b> for 2 values satisfying one of the original equations
			SC1 if no correct working shown, but 2 correct answers given
7(b)	[a =] 36 [b =] -6	3	<b>B2</b> for either correct or <b>M1</b> for $a = b^2$ or for $x^2 + bx + bx + b^2$ or better or for $(x - 6)^2$ seen and <b>M1</b> for $2b = -12$ soi
7(c)	$\frac{7x^2 - 12x - 10}{(2x - 5)(x - 1)}$ oe final answer nfww	4	<b>B1</b> for common denom $(2x-5)(x-1)$ seen oe isw <b>M1</b> for $x(x-1)+(3x+2)(2x-5)$ soi isw <b>B1</b> for $6x^2-15x+4x-10$ soi
8(a)(i)	4 points correctly plotted	2	<b>B1</b> for 2 or 3 points correctly plotted
8(a)(ii)	Positive	1	
8(b)	mean 3.1	3	M2 for $\frac{\text{sum of products}}{30}$
			or M1 for at least 4 correct products soi
	median 3	2	M1 for 15.5 oe indicated
	mode 5	1	
	range 5	1	
8(c)	24 nfww	3	M1 for $\frac{x \times 52 + 45 \times 75 + 11 \times 91}{x + 45 + 11}$ [= 70.3] M1 for clearing <i>their</i> fraction

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Question	Answer	Marks	Part marks
9(a)	1120 or 1121	4	M2 for $[AC^2 =]$ $525^2 + 872^2 - 2 \times 525 \times 872 \times \cos 104$ or M1 for implicit version A1 for 1257000 to 1258000
9(b)	$[QB \text{ or } x =] 872 \times \tan 1 \text{ seen}$	M2	<b>M1</b> for tan $1 = \frac{QB}{872}$
	$tan = their QB \div 525$	M1	
	1.7 or 1.660 to 1.661 nfww	A1	dep on M3
9(c)(i)	222 000 or 222 100 or 222 101	2	<b>M1</b> for $\frac{1}{2} \times 525 \times 872 \times \sin 104$
9(c)(ii)	5.55 or 5.550 to 5.553 nfww	2FT	FT their (c)(i) × $100^2 \div 20000^2$ M1 for their (c)(i) × $100^2 \div 20000^2$ or restart
10(a)	26 28 22 25 28 27 29 29 29 20 21 22 22 25 C	4	All 8 regions correct  M3 for 6 or 7 regions correct  M2 for 4 or 5 regions correct  M1 for 3 regions correct
10(b)(i)	∉	1	
10(b)(ii)	Ø	1	
10(c)	21, 23, 24, 29	2FT	Correct or FT SC1 for 1 omission or 4 correct and 1 extra
10(d)(i)	5	1FT	Correct or <b>FT</b> if less than 10
10(d)(ii)	9	1FT	Correct or <b>FT</b> if less than 10
10(e)		1	

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Question	Answer	Marks	Part marks
11	$(n+3)^2$ oe final answer	1, 2	M1 for a quadratic expression seen or second differences 2
	3n+2 oe final answer	1, 2	<b>B1</b> for $3n + k$ (any k) or $kn + 2$ ( $k \ne 0$ )
	47 $(n+3)^2 - (3n+2)$ oe isw	1, 2FT	FT their difference expressions $A - B$ M1 for expression $an^2 + bn + c$ seen or second differences 2
	$\frac{7}{6}$ $\frac{n+2}{n+1}$ oe final answer	1, 2	<b>B1</b> for $\frac{n+k+1}{n+k}$ seen