# Mining Large Graphs and Tensors - Patterns, Tools and Discoveries. 

Christos Faloutsos CMU


## Thank you!

- Nikos Sidiropoulos
- Kuo-Chu Chang

- Zhi (Gerry) Tian


## Roadmap

$\Rightarrow$ - Introduction - Motivation

- Why 'big data'
- Why (big) graphs?
- Problem\#1: Patterns in graphs
- Problem\#2: Tools
- Conclusions


## Why 'big data'

- Why?
- What is the problem definition?


## Main message: Big data: often $>$ experts

- 'Super Crunchers’ Why Thinking-By-Numbers is the New Way To Be Smart by Ian Ayres, 2008
- Google won the machine translation competition 2005
- http://www.itl.nist.gov/iad/mig//tests/mt/2005/doc/ mt05eval official results release 20050801 v3.html


## Problem definition - big picture



# Tera/Peta-byte data 

Analytics
Insights, outliers

## Problem definition - big picture



# Tera/Peta-byte data 

Analytics

Main emphasis in this talk

## Roadmap

- Introduction - Motivation
- Why 'big data’
- Why (big) graphs?

- Problem\#1: Patterns in graphs
- Problem\#2: Tools
- Problem\#3: Scalability
- Conclusions


## Graphs - why should we care?



Food Web
[Martinez '91]

## >\$10B revenue

$>0.5 \mathrm{~B}$ users


> Internet Map
[lumeta.com]

## Graphs - why should we care?

- IR: bi-partite graphs (doc-terms)


- web: hyper-text graph
- ... and more:


## Graphs - why should we care?

- web-log ('blog') news propagation
- computer network security: email/IP traffic and anomaly detection
- 'viral' marketing
- Supplier-supply business chains (-> instabilities)
- Subject-verb-object -> graph
- Many-to-many db relationship -> graph


## Outline

- Introduction - Motivation Problem\#1: Patterns in graphs

- Static graphs
- Time evolving graphs
- Problem\#2: Tools
- Conclusions


## Problem \#1 - network and graph mining

- What does the Internet look like?
- What does FaceBook look like?
- What is 'normal'/‘abnormal'?
- which patterns/laws hold?


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## Problem \#1 - network and graph mining

- What does the Internet look like?
- What does FaceBook look like?
- What is 'normal'/‘abnormal'?
- which patterns/laws hold?


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- To spot anomalies (rarities), we have to discover patterns
- Large datasets reveal patterns/anomalies that may be invisible otherwise...
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## Graph mining

- Are real graphs random?


## Laws and patterns

- Are real graphs random?
- A: NO!!
- Diameter
- in- and out- degree distributions
- other (surprising) patterns
- So, let's look at the data


## Solution\# S. 1

- Power law in the degree distribution [SIGCOMM99] internet domains



## Solution\# S. 1

- Power law in the degree distribution [SIGCOMM99] internet domains



## Solution\# S. 1

- Q: So what?


## internet domains



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## Solution\# S. 1

- Q: So what?
- A1: \# of two-step-away pairs: $\mathrm{O}\left(\mathrm{d}_{-} \max \wedge^{\wedge}\right) \sim 10 \mathrm{M}^{\wedge} 2$ internet domains




## Solution\# S. 1

- Q: So what?
- A1: \# of two-step-aw ${ }^{\text {an }}$ ?) $\sim 10 \mathrm{M}^{\wedge} 2$ SUCM


## Solution\# S.2: Eigen Exponent $E$

Eigenvalue


Exponent $=$ slope
$E=-0.48$

May 2001

Rank of decreasing eigenvalue

- A2: power law in the eigenvalues of the adjacency matrix


## Many more power laws

- \# of sexual contacts
- Income [Pareto] -'80-20 distribution'
- Duration of downloads [Bestavros+]
- Duration of UNIX jobs ('mice and elephants')
- Size of files of a user
- 'Black swans’


## Roadmap

- Introduction - Motivation
- Problem\#1: Patterns in graphs

- Static graphs
- degree, diameter, eigen,
- triangles
- cliques
- Weighted graphs
- Time evolving graphs
- Problem\#2: Tools


## Solution\# S.3: Triangle 'Laws'



- Real social networks have a lot of triangles


## Solution\# S.3: Triangle 'Laws’



- Real social networks have a lot of triangles
- Friends of friends are friends
- Any patterns?


## Triangle Law: \#S. 3 [Tsourakakis ICDM 2008]





X-axis: degree Y-axis: mean \# triangles $n$ friends -> $\sim n^{1.6}$ triangles

## Triangle Law: Computations [Tsourakakis ICDM 2008]

But: triangles are expensive to compute
(3-way join; several approx. algos) - $\mathrm{O}\left(\mathrm{d}_{\text {max }}{ }^{2}\right)$
$\mathrm{Q}:$ Can we do that quickly?
A:

## Triangle Law: Computations [Tsourakakis ICDM 2008]

But: triangles are expensive to compute
(3-way join; several approx. algos) $-\mathrm{O}\left(\mathrm{d}_{\text {max }}{ }^{2}\right)$
Q : Can we do that quickly?
A: Yes!
\#triangles $=\mathbf{1 / 6 ~ S u m ~}\left(\lambda_{i}{ }^{3}\right)$
(and, because of skewness (S2),
we only need the top few eigenvalues! - $\mathrm{O}(\mathrm{E})$
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# Triangle Law: Computations [Tsourakakis ICDM 2008] 

Wikipedia graph 2006-Nov-04
$\approx 3, \mathrm{IM}$ nodes $\approx 37 \mathrm{M}$ edges

$1000 x+$ speed-up, $>90 \%$ accuracy

## Triangle counting for large graphs?



Anomalous nodes in Twitter( 3 billion edges)
[U Kang, Brendan Meeder, +, PAKDD'11]
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- Problem\#1: Patterns in graphs

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## T. 1 : popularity over time

\# in links


Post popularity drops-off - exponentially?


## T. 1 : popularity over time

\# in links
(log)

days after post (log)

Post popularity drops-off - expon $e^{\dagger}$ ally? POWER LAW!
Exponent?

## T. 1 : popularity over time

\# in links
(log)

days after post (log)

Post popularity drops-off - expon ent ally? POWER LAW!
Exponent? -1.6

- close to -1.5: Barabasi's stack model
- and like the zero-crossings of a random walk


## - 1.5 slope

J. G. Oliveira \& A.-L. Barabási Human Dynamics: The Correspondence Patterns of Darwin and Einstein. Nature 437, 1251 (2005) . [PDF]


Response time (log)

## - 1.5 slope

J. G. Oliveira \& A.-L. Barabási Human Dynamics: The Correspondence Patterns of Darwin and Einstein. Nature 437, 1251 (2005) . [PDF]

## Roadmap

- Introduction - Motivation
- Problem\#1: Patterns in graphs

- Problem\#2: Tools
- (Belief Propagation)
- Tensors
- Spike analysis
- Conclusions


## GigaTensor: Scaling Tensor Analysis Up By 100 Times Algorithms and Discoveries

\(\begin{array}{cccc}U \& Evangelos \& Abhay \& Christos<br>Kang \& Papalexakis \& Harpale \& Faloutsos\end{array}\)



## KDD'12

## Background: Tensor

- Tensors (=multi-dimensional arrays) are everywhere
- Hyperlinks \&anchor text [Kolda+,05]



## Time evolving graphs: Tensors



## Background: Tensor

- Tensors (=multi-dimensional arrays) are everywhere
- Sensor stream (time, location, type)
- Predicates (subject, verb, object) in knowledge base


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(48M) verbs subjects (26M)


NELL (Never Ending Language Learner) data Nonzeros $=144 \mathrm{M}$

## Background: Tensor

- Tensors (=multi-dimensional arrays) are everywhere
- Sensor stream (time, location, type)
- Predicates (subject, verb, object) in knowledge base


Anomaly
Detection in
Computer
networks

IP-destination


Nikos Sidiropoulos
UMN

NSF, 3/2013


Tamara Kolda, Sandia Labs (tensor toolbox)

## Problem Definition

- How to decompose a billion-scale tensor?
- Corresponds to SVD in 2D case



## Problem Definition

- How to decompose a billion-scale tensor?
- Corresponds to SVD in 2D case $=$ soft clustering



## Problem Definition

- Q1: Dominant concepts/topics?
$\square$ Q2: Find synonyms to a given noun phrase?
- (and how to scale up: |data|>RAM)
(48M) verbs


NELL (Never Ending Language Learner) data Nonzeros $=144 \mathrm{M}$

## Experiments

- GigaTensor solves $100 x$ larger problem



Number of nonzero
= I / 50

## A1: Concept Discovery

## - Concept Discovery in Knowledge Base



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## A1: Concept Discovery

| Noun Phrase 1 | Noun <br> Phrase 2 | Context |
| :---: | :---: | :---: |
| Concept 1: "Web Protocol"   <br> internet protocol 'np1' 'stream' ' $n$ 2, <br> file software ' $n$ 1' 'marketing' <br> data suite 'np1' 'dating' <br> 'np2'   |  |  |
| Concept 2: <br> credit <br> Credit <br> library | Credit Cards <br> information <br> debt <br> number | $\begin{aligned} & \text { 'np1' 'card' 'np2' } \\ & \text { 'np1' 'report' 'np2' } \\ & \text { 'np1' 'cards' 'np2' } \end{aligned}$ |
| Concept 3: health child home | Health Systen provider providers system | $\begin{aligned} & \text { 'np1' 'care' 'np2' } \\ & \text { 'np' 'insurance' 'np2' } \\ & \text { 'np1' 'service' 'np2' } \end{aligned}$ |

## A2: Synonym Discovery

## (Given) <br> Noun Phrase

| pollutants | dioxin, sulfur dioxide, <br> greenhouse gases, particulates, <br> nitrogen oxide, air pollutants, cholesterol |
| :--- | :--- |
| disabilities | infections, dizziness, <br> injuries, diseases, drowsiness, <br> stiffness, injuries |
| vodafone | verizon, comcast |

Christian history European history, American history, Islamic history, history
disbelief dismay, disgust, astonishment

## Roadmap

- Introduction - Motivation
- Problem\#1: Patterns in graphs

- Problem\#2: Tools
- Belief propagation
- Tensors
- Spike analysis
- Graph summarization
- Conclusions


## Rise and fall patterns in social media

- Meme (\# of mentions in blogs)
- short phrases Sourced from U.S. politics in 2008
"you can put lipstick on a pig"

"yes we can"

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## Rise and fall patterns in social media

- Can we find a unifying model, which includes these patterns?
- four classes on YouTube [Crane et al. '08]
- six classes on Meme [Yang et al. '11]



## Rise and fall patterns in social media

- Answer: YES!

- We can represent all patterns by single model


## In Matsubara+ SIGKDD 2012

## Main idea - SpikeM

- 1. Un-informed bloggers (uninformed about rumor)
- 2. External shock at time nb (e.g, breaking news)
- 3. Infection (word-of-mouth)


Time $\mathrm{n}=0$


Time $\mathrm{n}=\mathrm{n}_{\mathrm{b}}$


Time $\mathrm{n}=\mathrm{n}_{\mathrm{b}}+1$

Infectiveness of a blog-post at age $n$ :
$\beta \quad$ - Strength of infection (quality of news)
$f(n)$ - Decay function

## Main idea - SpikeM



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Infectiveness of a blog-post at age $n$ :
$\beta \quad$ - Strength of infection (quality of news)
$f(n)$ - Decay function $\quad f(n)=\beta^{*} n^{-1.5}$

## SpikeM - with periodicity

- Full equation of SpikeM

$$
\begin{array}{|c}
\hline \Delta B(n+1)=\frac{p(n+1)}{\text { Periodicity }} \cdot\left[U(n) \cdot \sum_{t=n_{b}}^{n}(\Delta B(t)+S(t)) \cdot f(n+1-t)+\varepsilon\right] \\
\begin{array}{c}
\text { Bloggers change their } \\
\text { activity over time } \\
(\text { e.g., daily, weekly, } \\
\text { yearly) }
\end{array} \\
\text { C. Faloutsos (CMU) }
\end{array}
$$

## Details

- Analysis - exponential rise and power-raw fall




## Details

- Analysis - exponential rise and power-raw fall




## Tail-part forecasts

- SpikeM can capture tail part




## "What-if" forecasting



## "What-if" forecasting



SpikeM can forecast upcoming spikes
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- Belief Propagation
- Tensors
- Spike analysis
- Graph understanding (through MDL)
- Conclusions


## Summarizing Graphs

## Goal:



Main Idea: MDL + 'syllables' :
star, clique, chain, bi-partite core


Koutra, Kang, Vreeken, et al, (subm.)

## Summarizing Wiki-controversy


top-8 stars: admins, bots

$\checkmark \uparrow$
top-1 and top-2 bipartite cores: edit wars. Left: warring factions ('Kiev’ vs 'Kyev’) Right: between vandals

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## OVERALL CONCLUSIONS low level:

- Several new patterns (power laws, trianglelaws, etc)
- New tools:
- belief propagation, gigaTensor, etc
- Scalability: PEGASUS / hadoop


## OVERALL CONCLUSIONS high level

- BIG DATA: Large datasets reveal patterns/ outliers that are invisible otherwise





## References

- Leman Akoglu, Christos Faloutsos: RTG: A Recursive Realistic Graph Generator Using Random Typing. ECML/PKDD (1) 2009: 13-28
- Deepayan Chakrabarti, Christos Faloutsos: Graph mining: Laws, generators, and algorithms. ACM Comput. Surv. 38(1): (2006)


## References

- D. Chakrabarti, C. Faloutsos: Graph Mining - Laws, Tools and Case Studies, Morgan Claypool 2012
- http://www.morganclaypool.com/doi/abs/10.2200/ S00449ED1V01Y201209DMK006

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Graph Mining

Laws, Tools, and Case Studies

## References

- Deepayan Chakrabarti, Yang Wang, Chenxi Wang, Jure Leskovec, Christos Faloutsos: Epidemic thresholds in real networks. ACM Trans. Inf. Syst. Secur. 10(4): (2008)
- Deepayan Chakrabarti, Jure Leskovec, Christos Faloutsos, Samuel Madden, Carlos Guestrin, Michalis Faloutsos: Information Survival Threshold in Sensor and P2P Networks. INFOCOM 2007: 1316-1324


## References

- Christos Faloutsos, Tamara G. Kolda, Jimeng Sun: Mining large graphs and streams using matrix and tensor tools. Tutorial, SIGMOD Conference 2007: 1174


## References

- T. G. Kolda and J. Sun. Scalable Tensor Decompositions for Multi-aspect Data Mining. In: ICDM 2008, pp. 363-372, December 2008.


## References

- Jure Leskovec, Jon Kleinberg and Christos Faloutsos Graphs over Time: Densification Laws, Shrinking Diameters and Possible Explanations, KDD 2005 (Best Research paper award).
- Jure Leskovec, Deepayan Chakrabarti, Jon M. Kleinberg, Christos Faloutsos: Realistic, Mathematically Tractable Graph Generation and Evolution, Using Kronecker Multiplication. PKDD 2005: 133-145


## References

- Yasuko Matsubara, Yasushi Sakurai, B. Aditya Prakash, Lei Li, Christos Faloutsos, "Rise and Fall Patterns of Information Diffusion: Model and Implications", KDD'12, pp. 6-14, Beijing, China, August 2012


## References

- Jimeng Sun, Yinglian Xie, Hui Zhang, Christos Faloutsos. Less is More: Compact Matrix Decomposition for Large Sparse Graphs, SDM, Minneapolis, Minnesota, Apr 2007.
- Jimeng Sun, Spiros Papadimitriou, Philip S. Yu, and Christos Faloutsos, GraphScope: Parameterfree Mining of Large Time-evolving Graphs ACM SIGKDD Conference, San Jose, CA, August 2007


## References

- Jimeng Sun, Dacheng Tao, Christos Faloutsos: Beyond streams and graphs: dynamic tensor analysis. KDD 2006: 374-383


## References

- Hanghang Tong, Christos Faloutsos, and Jia-Yu Pan, Fast Random Walk with Restart and Its Applications, ICDM 2006, Hong Kong.
- Hanghang Tong, Christos Faloutsos, Center-Piece Subgraphs: Problem Definition and Fast Solutions, KDD 2006, Philadelphia, PA


## References

- Hanghang Tong, Christos Faloutsos, Brian Gallagher, Tina Eliassi-Rad: Fast best-effort pattern matching in large attributed graphs. KDD 2007: 737-746
- (Best paper award, CIKM'12) Hanghang Tong, B. Aditya Prakash, Tina Eliassi-Rad, Michalis Faloutsos and Christos Faloutsos
Gelling, and Melting, Large Graphs by Edge Manipulation, Maui, Hawaii, USA,


## References

- Hanghang Tong, Spiros Papadimitriou, Christos Faloutsos, Philip S. Yu, Tina Eliassi-Rad: Gateway finder in large graphs: problem definitions and fast solutions. Inf. Retr. 15(3-4): 391-411 (2012)


## Project info \& 'thanks'

Www.cs.cmu.edu/~pegasus


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## Cast



Akoglu, Leman


Beutel, Alex


Chau, Polo

Kang, U



Koutra, Danai


McGlohon, Mary


Papalexakis, Vagelis

## Take-home message



## Big data reveal insights that would be invisible otherwise (even to experts)

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