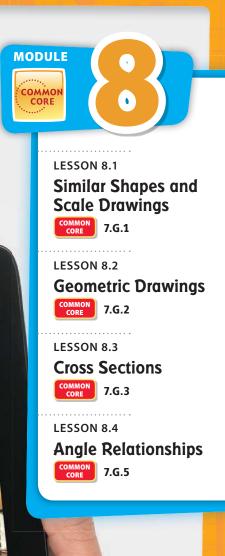
Modeling Geometric Figures



ESSENTIAL QUESTION

How can you use proportions to solve real-world geometry problems?





Real-World Video

Architects make blueprints and models of their designs to show clients and contractors. These scale drawings and scale models have measurements in proportion to those of the project when built.





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Are **VOU** Ready?

Complete these exercises to review skills you will need for this module.



Personal

Online Practice

and Help

Solve Two-Step Equations

EXAMPLE 5x + 3 = -75x + 3 - 3 = -7 - 3Subtract 3 from both sides. 5x = -10Simplify. $\frac{5x}{5} = \frac{-10}{5}$ Divide both sides by 5. x = -2

Solve.

1. $3x + 4 = 10$	2. 5 <i>x</i> − 11 = 34	3. $-2x+5=-9$	4. $-11 = 8x + 13$
5. $4x - 7 = -27$	6. $\frac{1}{2}x + 16 = 39$	7. $12 = 2x - 16$	8. $5x - 15 = -65$

Solve Proportions

EXAMPLE	$\frac{a}{4} = \frac{27}{18}$	
	$a \times 18 = 4 \times 27$	Write the cross products.
	18 <i>a</i> = 108	Simplify.
	$\frac{18a}{18} = \frac{108}{18}$	Divide both sides by 18.
	a = 6	

Solve for *x*.

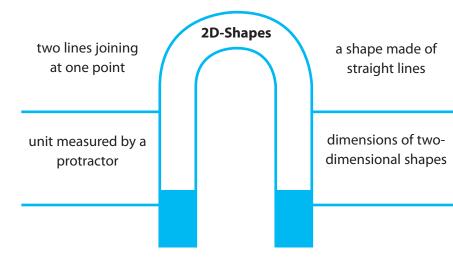
9.	$\frac{x}{5} = \frac{18}{30}$	10. $\frac{x}{12} = \frac{24}{36}$	11. $\frac{3}{9} = \frac{x}{3}$	12. $\frac{14}{15} = \frac{x}{75}$
13.	$\frac{8}{x} = \frac{14}{7}$	14. $\frac{14}{x} = \frac{2}{5}$	15. $\frac{5}{6} = \frac{x}{15}$	16. $\frac{81}{33} = \frac{x}{5.5}$

Company Company (Company)

Reading Start-Up

Visualize Vocabulary

Use the 🖌 words to complete the graphic. You may put more than one word on each line.



Understand Vocabulary

Complete each sentence using a preview word.

- 1. What is a proportional two-dimensional drawing of an object?
- 2. _____ are angles that have the same measure.
- 3. _____ are angles whose measures have a

sum of 90°.

Vocabulary

Review Words

- ✓ angle (ángulo)
- ✓ degree (grado) dimension (dimensión)
- length (longitud)
 proportion (proporción)
- ✓ polygon (polígono) ratio (razón)
- ✔ width (ancho)

Preview Words

adjacent angles (ángulos adyacentes) complementary angles (ángulos complementarios) congruent angles (ángulos congruentes) cross section (sección transversal) intersection (intersección) scale (escala) scale drawing (dibujo a escala) supplementary angles (ángulos suplementarios) vertical angles (ángulos verticales)

Active Reading

Key-Term Fold Before beginning the module, create a key-term fold to help you learn the vocabulary in this module. Write each highlighted vocabulary word on one side of a flap. Write the definition for each word on the other side of the flap. Use the key-term fold to quiz yourself on the definitions in this module.



GETTING READY FOR Modeling Geometric Figures

Understanding the standards and the vocabulary terms in the standards will help you know exactly what you are expected to learn in this module.

COMMON 7.G.1

Solve problems involving scale drawings of geometric figures, including computing actual lengths and areas from a scale drawing and reproducing a scale drawing at a different scale.

Key Vocabulary

scale (escala)

The ratio between two sets of measurements.

What It Means to You

You will learn how to calculate actual measurements from a scale drawing.

EXAMPLE 7.G.1

A photograph of a painting has dimensions 5.4 cm and 4 cm. The scale factor is $\frac{1}{15}$. Find the length and width of the actual painting.

$\frac{1}{15} = \frac{4}{w}$
$\frac{1\times4}{15\times4}=\frac{4}{W}$
$15 \times 4 = w$
60 = w

The painting is 81 cm long and 60 cm wide.

COMMON 7.G.5

Use facts about supplementary, complementary, vertical, and adjacent angles in a multistep problem to write and solve simple equations for an unknown angle in a figure.

Key Vocabulary

supplementary angles

(ángulos suplementarios) Two angles whose measures have a sum of 180°.



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What It Means to You

You will learn about supplementary, complementary, vertical, and adjacent angles. You will solve simple equations to find the measure of an unknown angle in a figure.

EXAMPLE 7.G.5

Suppose $m \angle 1 = 55^{\circ}$.

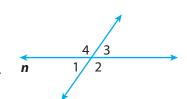
Adjacent angles formed by two intersecting lines are supplementary.

 $m \angle 1 + m \angle 2 = 180^{\circ}$

 $55^{\circ} + m \angle 2 = 180^{\circ}$ Substitute.

 $m\angle 2 = 180^{\circ} - 55^{\circ}$

$$= 125^{\circ}$$



LESSON **Similar Shapes and 8.1** Scale Drawings

7.G.1 Solve problems involving scale drawings of geometric figures, including computing actual lengths and areas from a scale drawing and reproducing a scale drawing at a different scale. Also 7.RP.1, 7.RP.2b

ESSENTIAL QUESTION

How can you use scale drawings to solve problems?

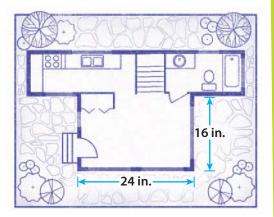
7.G.1



Finding Dimensions

Scale drawings and scale models are used in mapmaking, construction, and other trades.

A blueprint is a technical drawing that usually displays architectural plans. Pete's blueprint shows a layout of a house. Every 4 inches in the blueprint represents 3 feet of the actual house. One of the walls in the blueprint is 24 inches long. What is the actual length of the wall?



A Complete the table to find the actual length of the wall.

Blueprint length (in.)	4	8	12	16	20	24
Actual length (ft)	3	6				

Reflect

- 1. In Pete's blueprint the length of a side wall is 16 inches. Find the actual length of the wall.
- 2. The back wall of the house is 33 feet long. What is the length of the back wall in the blueprint?
- 3. Check for Reasonableness How do you know your answer to 2 is reasonable?

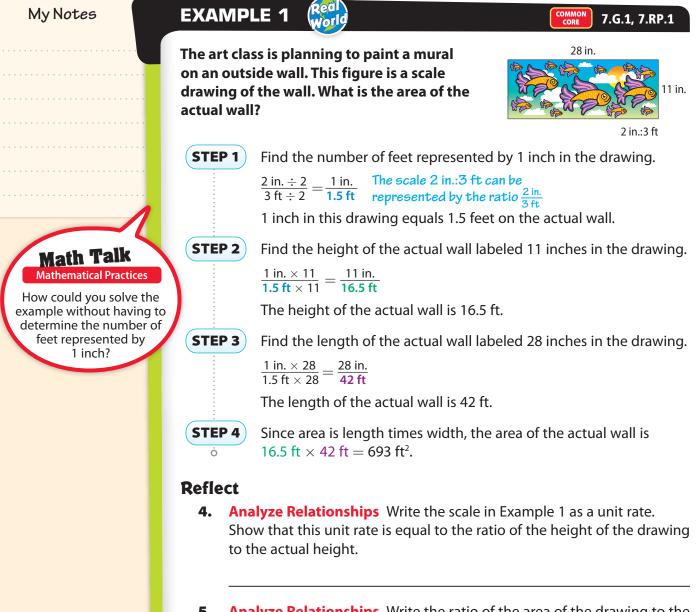


Using a Scale Drawing to Find Area

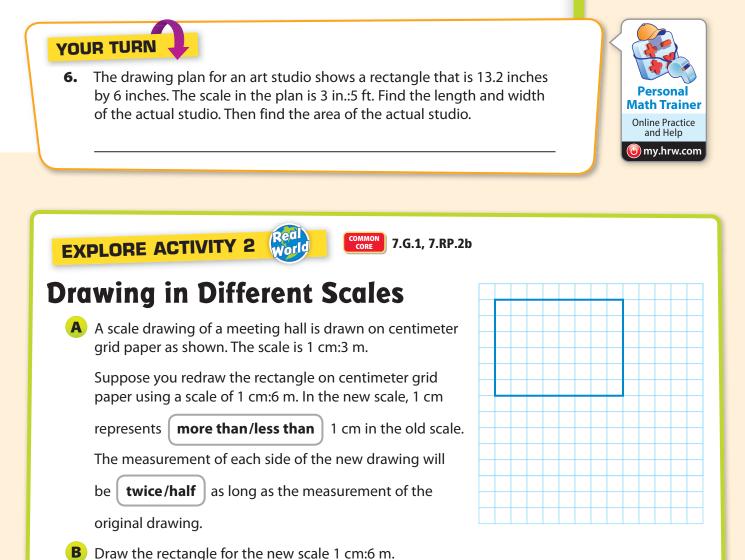
Similar shapes are proportional figures that have the same shape but not necessarily the same size.

A **scale drawing** is a proportional two-dimensional drawing that is *similar* to an actual object. Scale drawings can represent objects that are smaller or larger than the actual object.

A **scale** is a ratio between 2 sets of measurements. It shows how a dimension in a scale drawing is related to the actual object. Scales are usually shown as two numbers separated by a colon such as 1:20 or 1 cm:1 m. Scales can be shown in the same unit or in different units.



5. Analyze Relationships Write the ratio of the area of the drawing to the area of the actual mural. Write your answer as a unit rate. Show that this unit rate is equal to the square of the unit rate in **4**.



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Reflect

8. Explain how you know that there is a proportional relationship between the first and second drawings.

7. Find the actual length and width of the hall using the original scale. Then find the actual length and width of the hall using the new scale. How do

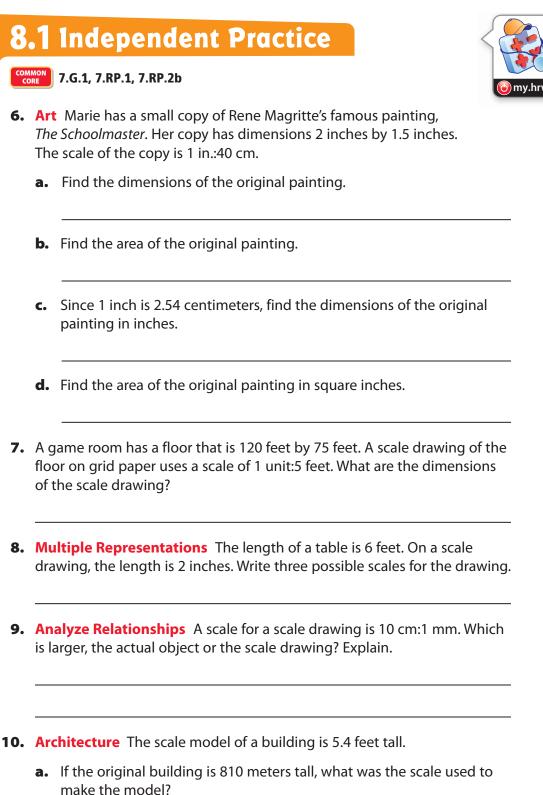
you know your answers are correct?

Guided Practice

1. The scale of a room in a blueprint is 3 in.:5 ft. A wall in the same blueprint is 18 in. Complete the table. (Explore Activity 1)

a. How long is the acb. A window in the ro			2 5 foot				
Find the width of t							
The scale in the drawin width of the actual roc						14 in.	
(Example 1)				-	7 in.		
The scale in the drawin	•				th	1	0 cm
of the actual room? Fin	d the area of the	actual roo	m. <mark>(Exa</mark>	mple 1)		6 cm	
A scale drawing of a ca	feteria is drawn	on centim	eter grig	d paper			
shown. The scale is 1 c	m:4 m. <mark>(Explore</mark>)	Activity 2					
a. Redraw the rectance	Jle on centimeter	r grid papeı	⁻ using a	scale of	f 1 cm:6	m.	
		-					
		-					
b. What is the actual le scale? What are the	-			-	-	102	

Class.



b. If the model is made out of tiny bricks each measuring 0.4 inch in height, how many bricks tall is the model?

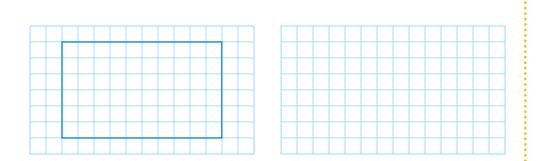


- **11.** You have been asked to build a scale model of your school out of toothpicks. Imagine your school is 30 feet tall. Your scale is 1 ft:1.26 cm.
 - **a.** If a toothpick is 6.3 cm tall, how many toothpicks tall will your model be?
 - **b.** Your mother is out of toothpicks, and suggests you use cotton swabs instead. You measure them, and they are 7.6 cm tall. How many cotton swabs tall will your model be?

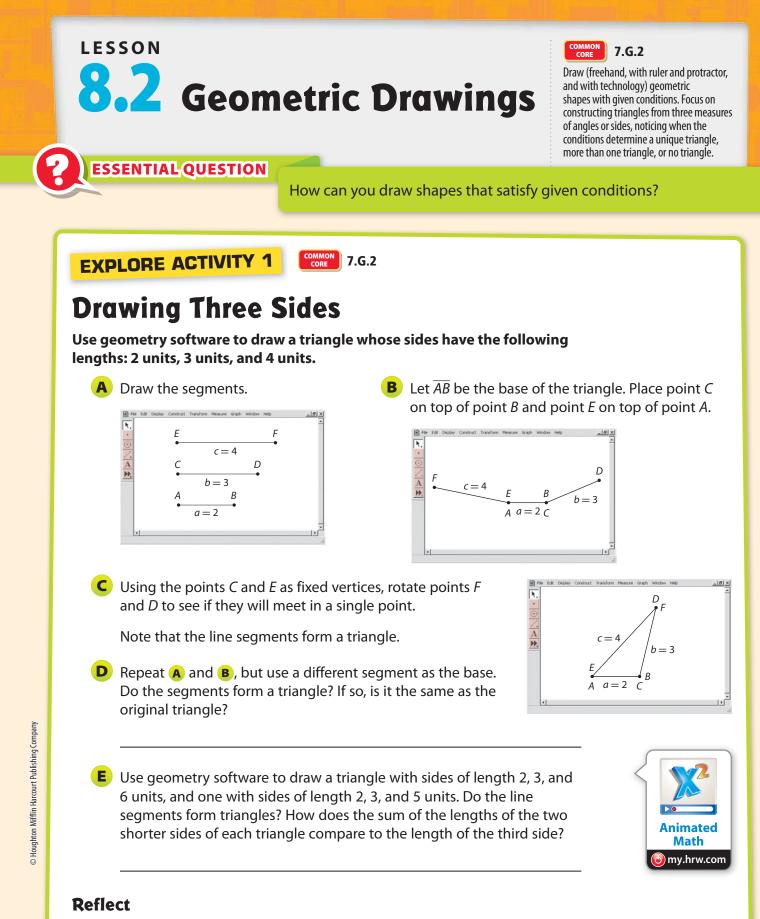


- **12. Draw Conclusions** The area of a square floor on a scale drawing is 100 square centimeters, and the scale of the drawing is 1 cm:2 ft. What is the area of the actual floor? What is the ratio of the area in the drawing to the actual area?
- **13.** Multiple Representations Describe how to redraw a scale drawing with a new scale.

14. The scale drawing of a room is drawn on a grid that represents quarterinch grid paper. The scale is $\frac{1}{4}$ in.:4 ft. Redraw the scale drawing of the same room using a different scale. What scale did you use? What is the length and width of the actual room? What is the area of the actual room?



Work Area



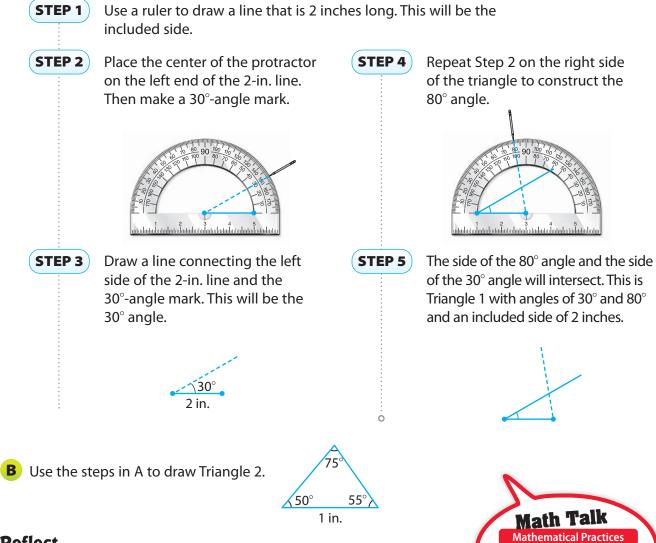
1. Conjecture Do two segments of lengths *a* and *b* units and a longer segment of length *c* units form one triangle, more than one, or none?

Two Angles and Their Included Side

Use a ruler and a protractor to draw each triangle.

Triangle 1	Triangle 2
Angles: 30° and 80°	Angles: 55° and 50°
Length of included side: 2 inches	Length of included side: 1 inch

A Draw Triangle 1.



Reflect

2. Will a triangle be unique if you know all three angle measures but no side lengths? Make a sketch and explain your answer.

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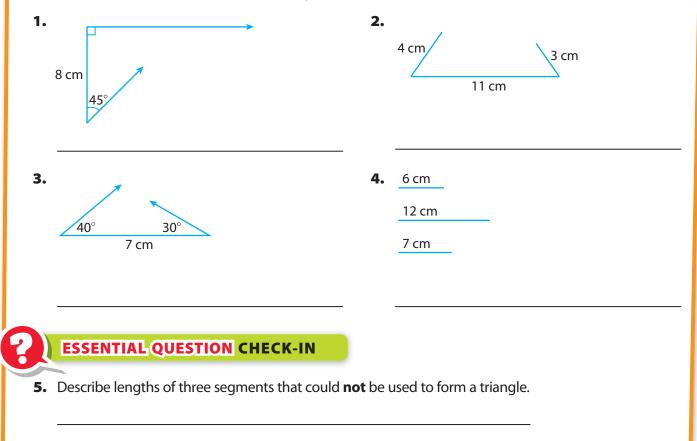
Are Triangle 1 and Triangle 2

unique? Explain.

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Guided Practice

Tell whether each figure creates the conditions to form a unique triangle, more than one triangle, or no triangle. (Explore Activities 1 and 2)



8.2 Independent Practice



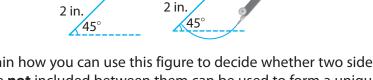
COMMON 7.G.2

- 6. On a separate piece of paper, try to draw a triangle with side lengths of 3 centimeters and 6 centimeters, and an included angle of 120°. Determine whether the given segments and angle produce a unique triangle, more than one triangle, or no triangle.
- 7. A landscape architect submitted a design for a triangle-shaped flower garden with side lengths of 21 feet, 37 feet, and 15 feet to a customer. Explain why the architect was not hired to create the flower garden.

8. Make a Conjecture The angles in an actual triangle-shaped traffic sign all have measures of 60°. The angles in a scale drawing of the sign all have measures of 60°. Explain how you can use this information to decide whether three given angle measures can be used to form a unique triangle or more than one triangle.



9. Communicate Mathematical Ideas The figure on the left shows a line segment 2 inches long forming a 45° angle with a dashed line whose length is not given. The figure on the right shows a compass set at a width of $1\frac{1}{2}$ inches with its point on the top end of the 2-inch segment. An arc is drawn intersecting the dashed line twice.



Explain how you can use this figure to decide whether two sides and an angle **not** included between them can be used to form a unique triangle, more than one triangle, or no triangle.

10. Critical Thinking Two sides of an isosceles triangle have lengths of 6 inches and 15 inches, respectively. Find the length of the third side. Explain your reasoning.





Work Area

8.3 Cross Sections

COMMON CORE **7.G.3** Describe the two-dimensional figures that result from slicing three-dimensional figures, as in plane sections of right rectangular prisms and right rectangular pyramids.

ESSENTIAL QUESTION

How can you describe cross sections of three-dimensional figures?

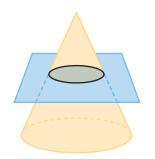
EXPLORE ACTIVITY 1

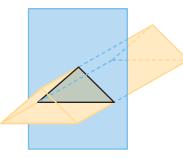
COMMON CORE 7.G.3

Cross Sections of a Right Rectangular Prism

An **intersection** is a point or set of points common to two or more geometric figures. A **plane** is a flat surface that extends forever in all directions. A **cross section** is the intersection of a three-dimensional figure and a plane. Imagine a plane slicing through the pyramid shown, or through a cone or a prism.







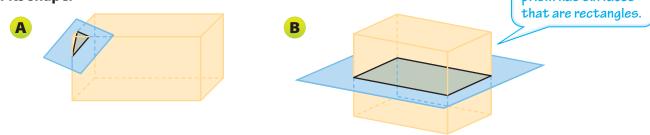
This figure shows the intersection of a cone and a plane. The cross section is a circle.

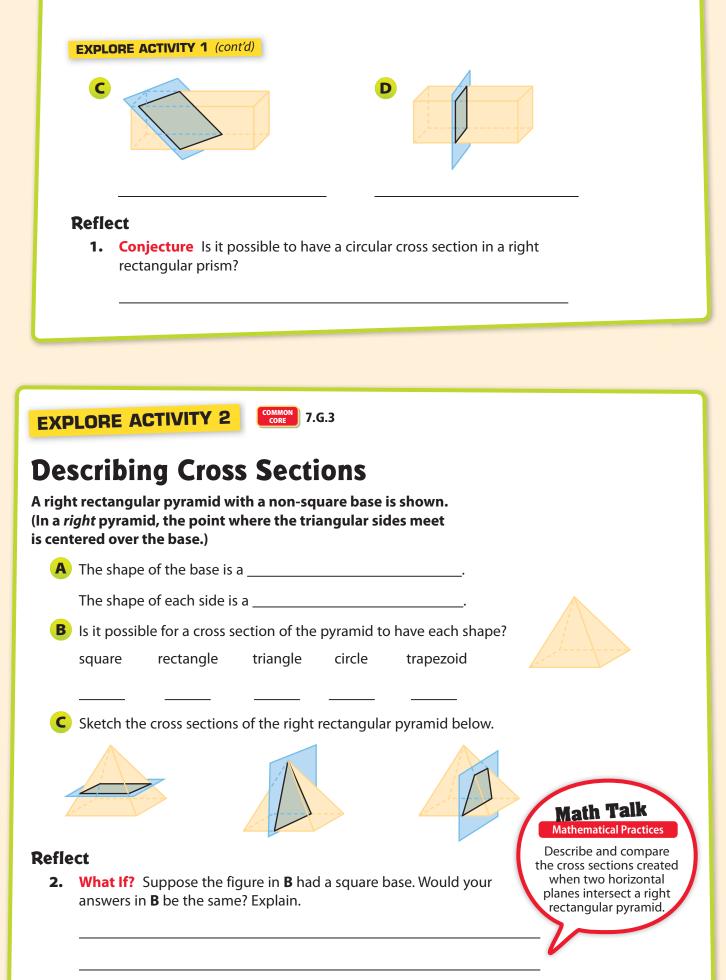
This figure shows the intersection of a triangular prism and a plane. The cross section is a triangle.

A three-dimensional figure can have several different cross sections depending on the position and the direction of the slice. For example, if the intersection of the plane and cone were vertical, the cross section would form a triangle.



A right rectangular prism has six faces that are rectangles.



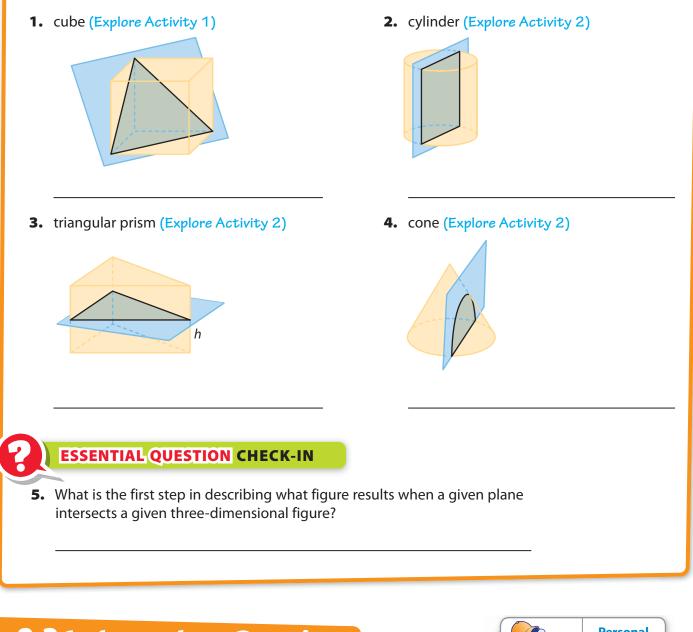


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Guided Practice

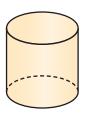
Describe the cross section of each given figure with the name of its shape.







6. Describe different ways in which a plane might intersect the cylinder and the cross section that results.



7. Make a Conjecture What cross sections might you see when a plane intersects a cone that you would **not** see when a plane intersects a

pyramid or a prism? _____



FOCUS ON HIGHER ORDER THINKING

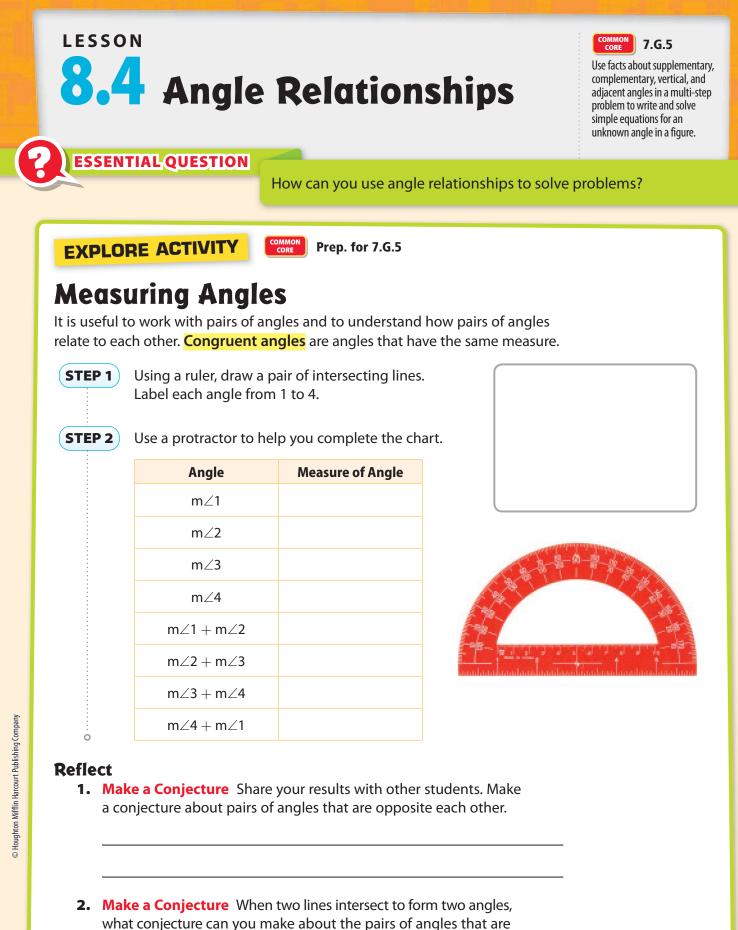
8. Critical Thinking The two figures on the left below show that you can form a cross section of a cube that is a pentagon. Think of a plane cutting the cube at an angle in such a way as to slice through five of the cube's six faces. Draw dotted lines on the third cube to show how to form a cross section that is a hexagon.



- **9.** Analyze Relationships A sphere has a radius of 12 inches. A horizontal plane passes through the center of the sphere.
 - **a.** Describe the cross section formed by the plane and the sphere.
 - **b.** Describe the cross sections formed as the plane intersects the interior of the sphere but moves away from the center.

- **10.** Communicate Mathematical Ideas A right rectangular prism is intersected by a horizontal plane and a vertical plane. The cross section formed by the horizontal plane and the prism is a rectangle with dimensions 8 in. and 12 in. The cross section formed by the vertical plane and the prism is a rectangle with dimensions 5 in. and 8 in. Describe the faces of the prism, including their dimensions. Then find its volume.
- **11. Represent Real-World Problems** Describe a real-world situation that could be represented by planes slicing a three-dimensional figure to form cross sections.

Work Area



next to each other?



Math Talk

Mathematical Practices Are $\angle BFD$ and $\angle AFE$ vertical angles?

Why or why not?

Angle Pairs and One-Step Equations

Vertical angles are the opposite angles formed by two intersecting lines. Vertical angles are congruent because the angles have the same measure.

Adjacent angles are pairs of angles that share a vertex and one side but do not overlap.

Complementary angles are two angles whose measures have a sum of 90°.

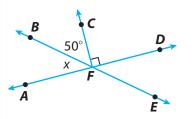
Supplementary angles are two angles whose measures have a sum of 180°. You discovered in the Explore Activity that adjacent angles formed by two intersecting lines are supplementary.

COMMON CORE

7.G.5

EXAMPLE 1

Use the diagram.



A Name a pair of vertical angles.

Vertical angles are opposite angles formed by intersecting lines.

 $\angle AFB$ and $\angle DFE$ are vertical angles.

Name a pair of adjacent angles.

Adjacent angles share a vertex and a side but do not overlap.

 $\angle AFB$ and $\angle BFD$ are adjacent angles.

C Name a pair of supplementary angles.

Adjacent angles formed by intersecting lines are supplementary.

 $\angle AFB$ and $\angle BFD$ are supplementary angles.



B

D Name two pairs of supplementary angles that include $\angle DFE$.

Any angle that forms a line with $\angle DFE$ is a supplementary angle to $\angle DFE$.

 $\angle DFE$ and $\angle EFA$ are supplementary angles, as are $\angle DFE$ and $\angle DFB$.

Find the measure of $\angle AFB$.

Use the fact that $\angle AFB$ and $\angle BFD$ in the diagram are supplementary angles to find m $\angle AFB$.

 $m \angle AFB + m \angle BFD = 180^{\circ}$ They are supplementary angles. $x + 140^{\circ} = 180^{\circ}$ $m \angle BFD = 50^{\circ} + 90^{\circ} = 140^{\circ}$ -140° -140° $x = 40^{\circ}$ Subtract 140° from both sides.

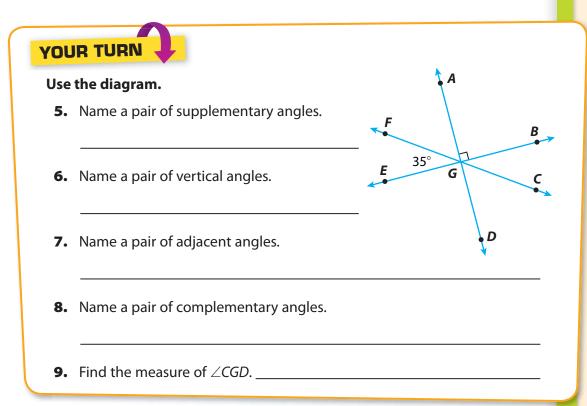
The measure of $\angle AFB$ is 40°.

Reflect

E

3. Analyze Relationships What is the relationship between $\angle AFB$ and $\angle BFC$? Explain.

4. Draw Conclusions Are $\angle AFC$ and $\angle BFC$ adjacent angles? Why or why not?





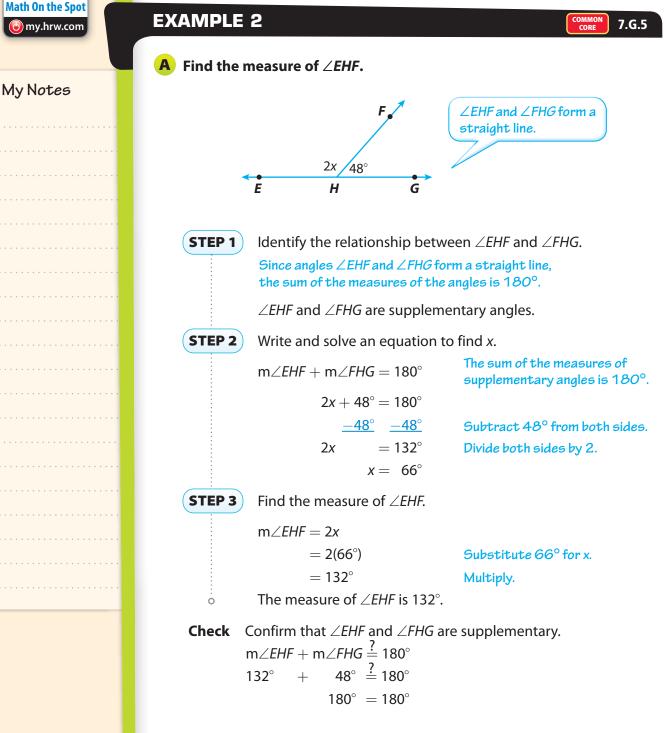
My Notes

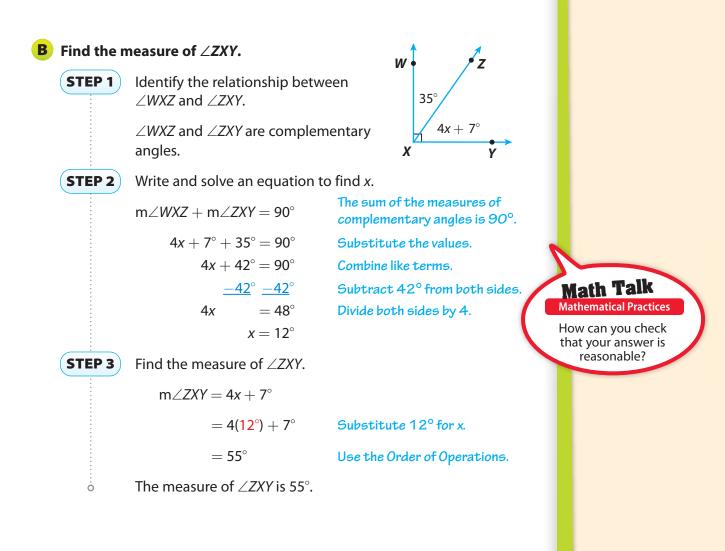
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Angle Pairs and Two-Step Equations

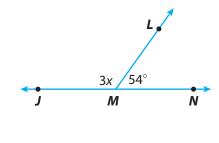
Sometimes solving an equation is only the first step in using an angle relationship to solve a problem.





YOUR TURN

10. Write and solve an equation to find the measure of $\angle JML$.

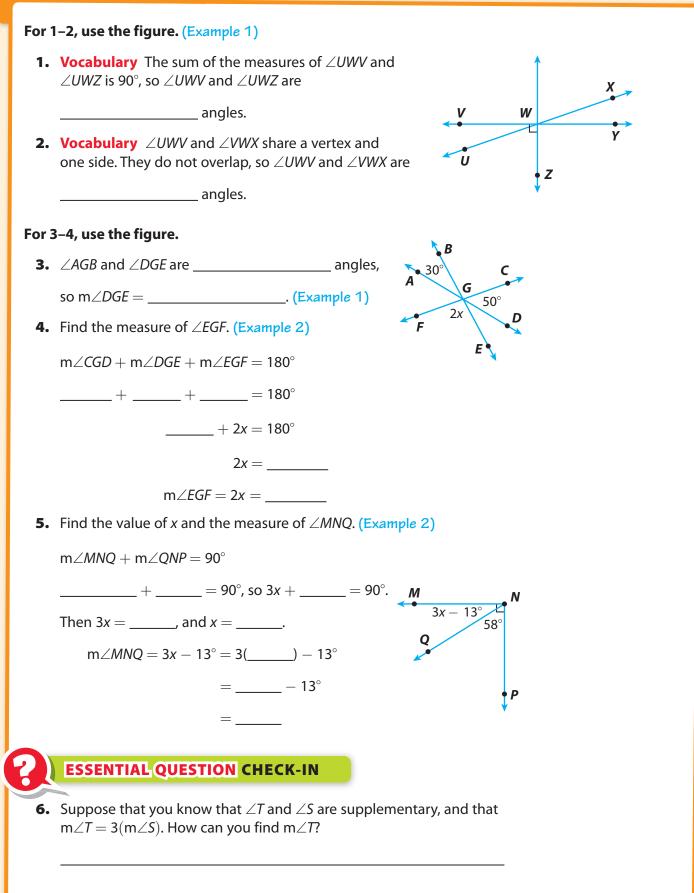


11. Critique Reasoning Cory says that to find m $\angle JML$ above, you can stop when you get to the solution step $3x = 126^\circ$. Explain why this works.



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Guided Practice

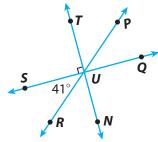


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8.4 Independent Practice

COMMON CORE 7.G.5

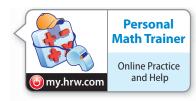
For 7–11, use the figure.



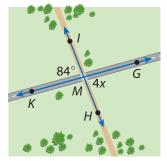
7. Name a pair of adjacent angles. Explain why they are adjacent.

- 8. Name a pair of acute vertical angles.
- 9. Name a pair of supplementary angles.
- **10.** Justify Reasoning Find m∠QUR. Justify your answer.

11. Draw Conclusions Which is greater, m∠*TUR* or m∠*RUQ*? Explain.

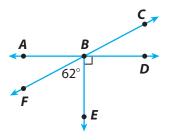


For 12–13, use the figure. A bike path crosses a road as shown. Solve for each indicated angle measure or variable.



- **12.** *x*_____
- **13.** m∠*KMH*_____

For 14–16, use the figure. Solve for each indicated angle measure.

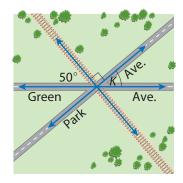


- **14.** m∠*CBE*_____
- **15.** m∠*ABF*_____
- **16.** m∠*CBA*_____
- **17.** The measure of $\angle A$ is 4° greater than the measure of $\angle B$. The two angles are complementary. Find the measure of each angle.
- **18.** The measure of $\angle D$ is 5 times the measure of $\angle E$. The two angles are supplementary. Find the measure of each angle.

19. Astronomy Astronomers sometimes use angle measures divided into degrees, minutes, and seconds. One degree is equal to 60 minutes, and one minute is equal to 60 seconds. Suppose that $\angle J$ and $\angle K$ are complementary, and that the measure of $\angle J$ is 48 degrees, 26 minutes, 8 seconds. What is the measure of $\angle K$?

FOCUS ON HIGHER ORDER THINKING

- **20. Represent Real-World Problems** The railroad tracks meet the road as shown. The town will allow a parking lot at angle *K* if the measure of angle *K* is greater than 38°. Can a parking lot be built at angle *K*? Why or why not?
- **21.** Justify Reasoning Kendra says that she can draw $\angle A$ and $\angle B$ so that $m \angle A$ is 119° and $\angle A$ and $\angle B$ are complementary angles. Do you agree or disagree? Explain your reasoning.



Work Area

- **22. Draw Conclusions** If two angles are complementary, each angle is called a *complement* of the other. If two angles are supplementary, each angle is called a *supplement* of the other.
 - **a.** Suppose $m \angle A = 77^{\circ}$. What is the measure of a complement of a complement of $\angle A$? Explain.

b. What conclusion can you draw about a complement of a complement of an angle? Explain.

MODULE QUIZ

Ready to Go On?

8.1 Similar Shapes and Scale Drawings



 A house blueprint has a scale of 1 in.:4 ft. The length and width of each room in the actual house are shown in the table. Complete the table by finding the length and width of each room on the blueprint.

	Living room	Kitchen	Office	Bedroom	Bedroom	Bathroom
$\begin{array}{c} \textbf{Actual} \\ \boldsymbol{\ell} \times w (ft) \end{array}$	16 × 20	12 × 12	8 × 12	20 × 12	12 × 12	6 × 8
$\frac{Blueprint}{\boldsymbol{\ell}\times\boldsymbol{w}(in.)}$						

8.2 Geometric Drawings

- 2. Can a triangle be formed with the side lengths of 8 cm, 4 cm, and 12 cm?
- **3.** A triangle has side lengths of 11 cm and 9 cm. Which could be the value of

the third side, 20 cm or 15 cm? ______

8.3 Cross Sections

- 4. Name one possible cross section of a sphere.
- 5. Name at least two shapes that are cross sections of a cylinder.

8.4 Angle Relationships

- **6.** $\angle BGC$ and $\angle FGE$ are _____ angles, so m $\angle FGE$ = _____.
- **7.** Suppose you know that $\angle S$ and $\angle Y$ are complementary, and

that $m \angle S = 2(m \angle Y) - 30^\circ$. Find $m \angle Y$.

ESSENTIAL QUESTION

8. How can you model geometry figures to solve real-world problems?

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a (Se A. B. C. 2. Th te Ch A. B. 3. Th an ha	onsider each figu cross section of elect Yes or No for a triangle circle rectangle the temperature bega noose True or Fa At 10 p.m. the At midnight th –12.5 ° F. At 9 p.m. the trian of the trian the floor of the error of the trian the a length of 8 ale of 1 cm : 2 m	the cone as see or A–C. Yes Yes Yes at 7 p.m. at a we an changing at a lse for each stat temperature we ne temperature wa ne temperature wa net temperature wa ne temperature wa ne temperature wa net semperature wa net semperature wa net semperature wa net semperature wa	n at right? No No No No No Pather station a rate of -2.5 rement. Vas -7.5 °F. (was (s -10 °F. (ffice building e 40°, and the s scale drawin	in Minneso °F per hou) True) True) True will be trian e side betw g of the en	r. False False False ngular. Two een them w	ill	
A	e diagram show construction wo orker correct? Us	rker says that \angle	BDA measure	s 30° more t	than ∠DAC.	ls the nswer.	р)8° С