## Module 5: Number Systems

Instructor Materials

Introduction to Networks v7.0 (ITN)

## What to Expect in this Module

- To facilitate learning, the following features within the GUI may be included in this module:

| Feature | Description |
| :--- | :--- |
| Animations | Expose learners to new skills and concepts. |
| Videos | Expose learners to new skills and concepts. |
| Check Your <br> Understanding(CYU) | Per topic online quiz to help learners gauge content understanding. |
| Interactive Activities | A variety of formats to help learners gauge content understanding. |
| Syntax Checker | Small simulations that expose learners to Cisco command line to practice <br> configuration skills. |
| PT Activity | Simulation and modeling activities designed to explore, acquire, reinforce, and <br> expand skills. |

## What to Expect in this Module (Cont.)

- To facilitate learning, the following features may be included in this module:

| Feature | Description |
| :--- | :--- |
| Hands-On Labs | Labs designed for working with physical equipment. |
| Class Activities | These are found on the Instructor Resources page. Class Activities are <br> designed to facilitate learning, class discussion, and collaboration. |
| Module Quizzes | Self-assessments that integrate concepts and skills learned throughout the <br> series of topics presented in the module. |
| Module Summary | Briefly recaps module content. |

## Module 5: Number Systems

Introduction to Networks v7.0 (ITN)

## Module Objectives

Module Title: Number Systems
Module Objective: Calculate numbers between decimal, binary, and hexadecimal systems.

| Topic Title | Topic Objective |
| :--- | :--- |
| Binary Number System | Calculate numbers between decimal and binary <br> systems. |
| Hexadecimal Number System | Calculate numbers between decimal and <br> hexadecimal systems. |

### 5.1 Binary Number System

## Binary Number System

## Binary and IPv4 Addresses

- Binary numbering system consists of 1 s and 0 s , called bits
- Decimal numbering system consists of digits 0 through 9
- Hosts, servers, and network equipment using binary addressing to identify each other.
- Each address is made up of a string of 32 bits, divided into four sections called octets.
- Each octet contains 8 bits (or 1 byte) separated by a dot.
- For ease of use by people, this dotted notation is converted to dotted decimal.



## Binary Number System

## Video - Convert Between Binary and Decimal Numbering

 SystemsThis video will cover the following:

- Positional notation review
- Powers of 10 review
- Decimal - base 10 numbering review
- Binary - base 2 numbering review
- Convert an P address in binary to decimal numbering


## Binary Number System

## Binary Positional Notation

- Positional notation means that a digit represents different values depending on the "position" the digit occupies in the sequence of numbers.
- The decimal positional notation system operates as shown in the tables below.

|  |  |  |  |  |  | Thousands | Hundreds | Tens | Ones |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Radix | 10 | 10 | 10 | 10 | Positional Value | 1000 | 100 | 10 | 1 |
| Position in Number | 3 | 2 | 1 | 0 | Decimal Number (1234) | 1 | 2 | 3 | 4 |
| Calculate | $\left(10^{3}\right)$ | (102) | $\left(10^{1}\right)$ | $\left(10^{\circ}\right)$ | Calculate | $1 \times 1000$ | $2 \times 100$ | $3 \times 10$ | $4 \times 1$ |
| Position Value | 1000 | 100 | 10 | 1 | Add them up... | 1000 | + 200 | + 30 | +4 |
|  |  |  |  |  | Result | 1,234 |  |  |  |

## Binary Number System

Binary Positional Notation (Cont.)
The binary positional notation system operates as shown in the tables below.

| Radix | $\mathbf{2}$ | $\mathbf{2}$ | $\mathbf{2}$ | $\mathbf{2}$ | $\mathbf{2}$ | $\mathbf{2}$ | $\mathbf{2}$ | $\mathbf{2}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Position in Number | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |
| Calculate | $\left(2^{7}\right)$ | $\left(2^{6}\right)$ | $\left(2^{5}\right)$ | $\left(2^{4}\right)$ | $\left(2^{3}\right)$ | $\left(2^{2}\right)$ | $\left(2^{1}\right)$ | $\left(2^{0}\right)$ |
| Position Value | 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 |


| Positional Value | 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Binary Number (11000000) | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| Calculate | 1×128 | 1x64 | $0 \times 32$ | $0 \times 16$ | 0x8 | 0x4 | $0 \times 2$ | $0 \times 1$ |
| Add Them Up... | 128 | + 64 | + 0 | + 0 | + 0 | + 0 | + 0 | + 0 |
| Result | 192 |  |  |  |  |  |  |  |

## Binary Number System

## Convert Binary to Decimal

Convert 11000000.10101000.00001011.00001010 to decimal.

| Positional Value | 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Binary Number (11000000) | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| Calculate | 1x128 | 1x64 | $0 \times 32$ | 0x16 | 0x8 | 0x4 | 0x2 | 0x1 |
| Add Them Up... | 128 | + 64 | + 0 | $+0$ | + 0 | $+0$ | + 0 | $+0$ |
| Binary Number (10101000) | 1 | 0 | 1 | 0 | 1 | 0 | 0 | 0 |
| Calculate | 1x128 | 0x64 | $1 \times 32$ | $0 \times 16$ | $1 \times 8$ | 0x4 | 0x2 | $0 \times 1$ |
| Add Them Up... | 128 | + 0 | + 32 | + 0 | + 8 | + 0 | + 0 | + 0 |
| Binary Number (00001011) | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 |
| Calculate | $0 \times 128$ | 0x64 | $0 \times 32$ | $0 \times 16$ | 1x8 | 0x4 | $1 \times 2$ | 1x1 |
| Add Them Up... | 0 | $+0$ | + 0 | $+0$ | $+8$ | $+0$ | $+2$ | + 1 |
| Binary Number (00001010) | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 0 |
| Calculate | $0 \times 128$ | $0 \times 64$ | $0 \times 32$ | $0 \times 16$ | $1 \times 8$ | 0x4 | $1 \times 2$ | 0x1 |
| Add Them Up... | 0 | + 0 | + 0 | + 0 | + 8 | $+0$ | $+2$ | $+0$ |

## Binary Number System

## Decimal to Binary Conversion

The binary positional value table is useful in converting a dotted decimal IPv4 address to binary.

- Start in the 128 position (the most significant bit). Is the decimal number of the octet ( n ) equal to or greater than 128?
- If no, record a binary 0 in the 128 positional value and move to the 64 positional value.
- If yes, record a binary 1 in the 128 positional value, subtract 128 from the decimal number, and move to the 64 positional value.
- Repeat these steps through the 1
 positional value.


## Binary Number System

## Decimal to Binary Conversion Example

- Convert decimal 168 to binary

Is $168>128$ ?

- Yes, enter 1 in 128 position and subtract 128 (168-128=40)

Is $40>64 ?$

- No, enter 0 in 64 position and move on

Is $40>32$ ?

- Yes, enter 1 in 32 position and subtract 32 (40-32=8)

Is $8>16$ ?

- No, enter 0 in 16 position and move on

Is $8>8$ ?

- Equal. Enter 1 in 8 position and subtract 8 ( $8-8=0$ )

No values left. Enter 0 in remaining binary positions

| $\mathbf{1 2 8}$ | $\mathbf{6 4}$ | $\mathbf{3 2}$ | $\mathbf{1 6}$ | $\mathbf{8}$ | $\mathbf{4}$ | $\mathbf{2}$ | $\mathbf{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 1 | 0 | 1 | 0 | 0 | 0 |

Decimal 168 is written as 10101000 in binary

- Routers and computers only understand binary, while humans work in decimal. It is important for you to gain a thorough understanding of these two numbering systems and how they are used in networking.



### 5.2 Hexadecimal Number System

## Hexadecimal Number System

 Hexadecimal and IPv6 Addresses- To understand IPv6 addresses, you must be able to convert hexadecimal to decimal and vice versa.
- Hexadecimal is a base sixteen numbering system, using the digits 0 through 9 and letters A to $F$.
- It is easier to express a value as a single hexadecimal digit than as four binary bit.
- Hexadecimal is used to

| Decimal |
| :---: |
| 0 |
| 1 |
| 2 |
| 3 |
| 4 |
| 5 |
| 6 |
| 7 |
| 8 |
| 9 |
| 10 |
| 11 |
| 12 |
| 13 |
| 14 |
| 15 |


| Binary |
| :---: |
| 0000 |
| 0001 |
| 0010 |
| 0011 |
| 0100 |
| 0101 |
| 0110 |
| 0111 |
| 1000 |
| 1001 |
| 1010 |
| 1011 |
| 1100 |
| 1101 |
| 1110 |
| 1111 |

Hexadecimal

| 0 |
| :--- |
| 1 |
| 2 |
| 3 |
| 4 |
| 5 |
| 6 |
| 7 |
| 8 |
| 9 |
| A |
| B |
| C |
| D |
| E |
| F | represent IPv6 addresses and MAC addresses.

## Hexadecimal Number System

## Hexadecimal and IPv6 Addresses (Cont.)

- IPv6 addresses are 128 bits in length. Every 4 bits is represented by a single hexadecimal digit. That makes the IPv6 address a total of 32 hexadecimal values.
- The figure shows the preferred method of writing out an IPv6 address, with each $X$ representing four hexadecimal values.
- Each four hexadecimal character group is referred to as a hextet.



## \section*{Hexadecimal Number System} <br> Video - Converting Between Hexadecimal and Decimal Numbering Systems

This video will cover the following:

- Characteristics of the Hexadecimal System
- Convert from Hexadecimal to Decimal
- Convert from Decimal to Hexadecimal


## Hexadecimal Number System

## Decimal to Hexadecimal Conversions

Follow the steps listed to convert decimal numbers to hexadecimal values:

- Convert the decimal number to 8-bit binary strings.
- Divide the binary strings in groups of four starting from the rightmost position.
- Convert each four binary numbers into their equivalent hexadecimal digit.

For example, 168 converted into hex using the three-step process.

- 168 in binary is 10101000 .
- 10101000 in two groups of four binary digits is 1010 and 1000.
- 1010 is hex A and 1000 is hex 8 , so 168 is A8 in hexadecimal.


## Hexadecimal Number System

 Hexadecimal to Decimal ConversionsFollow the steps listed to convert hexadecimal numbers to decimal values:

- Convert the hexadecimal number to 4-bit binary strings.
- Create 8 -bit binary grouping starting from the rightmost position.
- Convert each 8-bit binary grouping into their equivalent decimal digit.

For example, D2 converted into decimal using the three-step process:

- D2 in 4-bit binary strings is 1110 and 0010.
- 1110 and 0010 is 11100010 in an 8 -bit grouping.
- 11100010 in binary is equivalent to 210 in decimal, so D2 is 210 is decimal


### 5.3 Module Practice and Quiz

## Module Practice and Quiz

## What did I learn in this module?

- Binary is a base two numbering system that consists of the numbers 0 and 1 , called bits.
- Decimal is a base ten numbering system that consists of the numbers 0 through 9.
- Binary is what hosts, servers, and networking equipment uses to identify each other.
- Hexadecimal is a base sixteen numbering system that consists of the numbers 0 through 9 and the letters $A$ to $F$.
- Hexadecimal is used to represent IPv6 addresses and MAC addresses.
- IPv6 addresses are 128 bits long, and every 4 bits is represented by a hexadecimal digit for a total of 32 hexadecimal digits.
- To convert hexadecimal to decimal, you must first convert the hexadecimal to binary, then convert the binary to decimal.
- To convert decimal to hexadecimal, you must first convert the decimal to binary and then the binary to hexadecimal.

$$
\begin{aligned}
& .1|1,1| 1 \\
& \text { cISco }
\end{aligned}
$$

