## Molecular Composition of Gases

Honors chemistry - Semester 2

## Objectives

Understand and use ideal gas law

Describe relationship between gas behavior and chemical formulas of gases

Apply reaction stoichiometry to gas stoichiometry

## Key Terms

Ideal gas
Ideal gas law
Diffusion and Graham's Law

## Effusion

Gay-Lussac's Law of combining volumes
Partial pressure and Dalton's Law

## Ideal Gas

= hypothetical gas that perfectly follows gas laws

- Does not condense to liquid at low temp

- Has no attraction/repulsion between particles
- Particles with zero volume


## Gas Laws

No gas obeys gas laws perfectly

Gas laws good enough in most cases

What if we change temp, pressure and volume??

Boyle's Law<br>+ Charles' Law<br>+ Avogadro's Law<br>= Ideal Gas Law

## Ideal Gas Law

Ideal gas law combines four laws into one

$$
\mathrm{PV}=\mathrm{nRT}
$$

$$
\begin{aligned}
& \mathrm{P}=\text { pressure } \\
& \mathrm{V}=\text { volume } \\
& \mathrm{n}=\# \text { moles }
\end{aligned}
$$

$\mathrm{T}=$ temperature (in kelvin)
R = constant


## Ideal Gas Law

Value of $R$ depends upon units of pressure


Pay attention to units ideal gas law problems!

## Ideal Gas Law

Works well in most common settings

Fails under very high pressure or very low temp

## Why?

- Intermolecular forces become a factor
- Volume of particles becomes non-trivial


## Example

How many moles of gas are contained 22.41 L at 101.325 kPa and $0^{\circ} \mathrm{C}$ ?

$$
\begin{aligned}
& \mathrm{PV}=\mathrm{nRT} \\
& \mathrm{R}=8.314 \mathrm{~L} \cdot \mathrm{kPa} / \mathrm{mol} \cdot \mathrm{~K}
\end{aligned}
$$

$$
\mathrm{n}=\mathrm{PV} / \mathrm{RT}
$$

$$
=(101.325 \mathrm{kPa})(22.41 \mathrm{~L}) /(8.314 \mathrm{~L} \cdot \mathrm{kPa} / \mathrm{mol} \cdot \mathrm{~K})(273 \mathrm{~K})
$$

$$
=1.00 \mathrm{~mol}
$$

## Example

What is the volume of 17.5 mol of $\mathrm{H}_{\mathbf{2}}$ at 2.75 atm and 385 K ?

$$
\begin{aligned}
& \mathrm{PV}=\mathrm{nRT} \\
& \mathrm{R}=0.0821 \mathrm{~L} \cdot \mathrm{~atm} / \mathrm{mol} \cdot \mathrm{~K}
\end{aligned}
$$

$\mathrm{V}=\mathrm{nRT} / \mathrm{P}$
$=((17.5 \mathrm{~mol})(0.0821 \mathrm{~L} \cdot \mathrm{~atm} / \mathrm{mol} \cdot \mathrm{K})(385 \mathrm{~K})) /(2.75 \mathrm{~atm})$
$=201 \mathrm{~L}$

## Practice

Calculate the pressure in kPa exerted by 43 mol of nitrogen in a 65 L cylinder at $5^{\circ} \mathrm{C}$.
1500 kPa

How many moles of air molecules are contained in a 2.00 L flask at 98.8 kPa and $25.0^{\circ} \mathrm{C}$ ?
$7.98 \times 10^{-2} \mathbf{~ m o l}$


## Gas Stoichiometry

Stoichiometry = ratios between compounds in a chemical equation
$\underline{\text { Ratio of gas volumes }=\underline{\text { ratio of moles }} \text { of those gases }}$ (Avogadro's Law)

## Gas Stoichiometry

Example
$2 \mathrm{H}_{2(\mathrm{~g})}+\mathrm{O}_{2(\mathrm{~g})} \rightarrow 2 \mathrm{H}_{2} \mathrm{O}_{(\mathrm{g})}$

Mole ratio
$\mathrm{H}_{2}: \mathrm{O}_{2}=2: 1$
$\mathrm{H}_{2}: \mathrm{H}_{2} \mathrm{O}=1: 1$
$\mathrm{O}_{2}: \mathrm{H}_{2} \mathrm{O}=1: 2$

Volume ratio
$\mathrm{H}_{2}: \mathrm{O}_{2}=2: 1$
$\mathrm{H}_{2}: \mathrm{H}_{2} \mathrm{O}=1: 1$
$\mathrm{O}_{2}: \mathrm{H}_{2} \mathrm{O}=1: 2$

## Gas Stoichiometry

To find volume of gas produced in reaction you may need to use:

- mole ratio between chemicals
- volume ratio between gasses
- ideal gas law to convert moles to volume


## Example

How many liters of hydrogen gas are produced at 280.0 K and 96.0 kPa if 1.74 mol sodium react with excess water?

$$
2 \mathrm{Na}_{(\mathrm{s})}+2 \mathrm{H}_{2} \mathrm{O}_{(\mathrm{l})} \rightarrow 2 \mathrm{NaOH}_{(\mathrm{aq})}+\mathrm{H}_{2(\mathrm{~g})}
$$

Gather information:
$\mathrm{R}=8.314 \mathrm{~L} \cdot \mathrm{kPa} / \mathrm{mol} \cdot \mathrm{K}$
P = 96.0 kPa
$\mathrm{T}=280.0 \mathrm{~K}$
$\mathrm{n}_{\mathrm{H} 2}=$ ? $\mathrm{mol} \mathrm{H}_{2}$

$$
\begin{aligned}
& \mathrm{n}_{\mathrm{Na}}=1.74 \mathrm{~mol} \mathrm{Na} \\
& \mathrm{~V}_{\mathrm{H} 2}=\text { ? } \mathrm{LH}_{2}
\end{aligned}
$$

## Example

Use mole ratio to find \# moles of $\mathrm{H}_{2}$ produced

Now use ideal gas law to find volume of $\mathrm{H}_{2}$

## Example

What volume of $\mathrm{O}_{2}$ gas is collected at $25^{\circ} \mathrm{C}$ and 101 kPa from decomposition of 37.9 g potassium chlorate?

$$
2 \mathrm{KClO}_{3(\mathrm{~s})} \rightarrow 2 \mathrm{KCl}_{(\mathrm{s})}+3 \mathrm{O}_{2(\mathrm{~g})}
$$

Collect information:

$$
\begin{array}{ll}
\mathrm{R}=8.314 \mathrm{~L} \cdot \mathrm{kPa} / \mathrm{mol} \cdot \mathrm{~K} & \mathrm{P}=101 \mathrm{kPa} \\
\mathrm{~T}=25^{\circ} \mathrm{C}=298 \mathrm{~K} & \mathrm{~m}_{\mathrm{KClO3}}=37.9 \mathrm{~g} \mathrm{KClO}_{3} \\
\mathrm{n}=? \mathrm{~mol} \mathrm{O}_{2} & \mathrm{~V}=? \mathrm{~L} \mathrm{O}_{2}
\end{array}
$$

## Example

Convert grams $\mathrm{KClO}_{3}$ to moles

Use mole ratio to find moles of $\mathrm{O}_{2}$

Use ideal gas law to find volume of $\mathrm{O}_{2}$

## Example

$37.9 \mathrm{~g} \mathrm{KClO}_{3} \times \frac{1 \mathrm{~mol} \mathrm{KClO}_{3}}{122.6 \mathrm{~g}}=0.309 \mathrm{~mol}$
$\mathrm{KClO}_{3}: \mathrm{O}_{2}=2: 3$
$0.309 \mathrm{~mol} \mathrm{KClO}_{3} \times \frac{3 \mathrm{~mol} \mathrm{O}_{2}}{2 \mathrm{~mol} \mathrm{KClO}_{3}}=0.464 \mathrm{~mol} \mathrm{O}_{2}$
$\mathrm{V}=\mathrm{nRT} / \mathrm{P}$
$=\frac{0.464 \mathrm{~mol} \mathrm{O}}{2}\left(\frac{8.314 \mathrm{~L} \cdot \mathrm{kPa}}{\mathrm{mol} \cdot \mathrm{K}}\right) 298 \mathrm{~K}, 11.4 \mathrm{~L} \mathrm{O} \mathrm{O}_{2}$


## Practice

Liquid hydrogen and oxygen are burned in a rocket. What volume of water vapor at $555^{\circ} \mathrm{C}$ and 76.4 kPa can be produced from 4.67 kg of $\mathrm{H}_{2}$ ?

$$
2 \mathrm{H}_{2(I)}+\mathrm{O}_{2(I)} \rightarrow 2 \mathrm{H}_{2} \mathrm{O}_{(\mathrm{g})}
$$

Hint:
Convert kg $\mathrm{H}_{2}$ to moles $\mathrm{H}_{2}$
Use mole ratio $\mathrm{H}_{2}: \mathrm{H}_{2} \mathrm{O}$ to find moles $\mathrm{H}_{2} \mathrm{O}$
Use ideal gas law to find volume of $\mathrm{H}_{2} \mathrm{O}$
$2.1 \times 10^{5} \mathrm{LH}_{2} \mathrm{O}$

## Practice

How many grams of sodium are needed to produce 2.24 L of hydrogen at $23{ }^{\circ} \mathrm{C}$ and 92.5 kPa ? $2 \mathrm{Na}_{(\mathrm{s})}+2 \mathrm{H}_{2} \mathrm{O}_{(\mathrm{l})} \rightarrow 2 \mathrm{NaOH}_{(\mathrm{aq})}+\mathrm{H}_{2(\mathrm{~g})}$

Hint:
Use ideal gas law to find moles of $\mathrm{H}_{2}$
Use mole ratio $\mathrm{H}_{2}$ : Na to find moles Na needed
Convert moles Na to grams Na
3.87 g Na

## Diffusion

Diffusion = the mixing of different gases by random molecular motion and collision

Gases spread from areas of high concentration to low concentration

Increases entropy

Heavy molecules move slower than light ones


## Effusion

Effusion = gas escapes through a tiny hole under pressure

Rate of effusion inversely proportional to mass of molecule (light gasses effuse faster)

Think about it:
Would $\mathrm{H}_{2}$ or $\mathrm{CO}_{2}$ leak out of small hole faster? Why?

(b)

## Graham's Law

- Graham's Law: Rate of diffusion is inversely proportional to the square root of its mass
- Speed of two molecules, A and B, at same temp and pressure related by

$$
\frac{V_{A}}{V_{B}}=\sqrt{\frac{M_{B}}{M_{A}}}
$$

- Re-write equation as $\frac{1}{2} M_{A} V_{A}^{2}=\frac{1}{2} M_{B} V_{B}^{2}$ (kinetic energy)


## Example

If $\mathrm{O}_{2}$ moves at $480 \mathrm{~m} / \mathrm{s}$ at room temp, how fast does $\mathrm{SF}_{6}$ move?
Use Graham's Law

$$
\begin{gathered}
\frac{V_{A}}{V_{B}}=\sqrt{\frac{M_{B}}{M_{A}}} \\
\frac{V_{\mathrm{SF} 6}}{V_{02}}=\sqrt{\frac{M_{02}}{M_{\mathrm{SF} 6}}}
\end{gathered}
$$

## $V_{\text {SF6 }}=220 \mathrm{~m} / \mathrm{s}$

## Dalton's Law

of Partial Pressure
In mixture of gasses, each gas exerts a partial pressure proportional to \# moles of that gas

Total system pressure $=$ sum of all the partial pressures

- $P_{\text {total }}=P_{A}+P_{B}+P_{C}+\ldots$


## Example:

- A system has $\mathrm{P}_{\mathrm{O} 2}$ of 1.0 atm and $\mathrm{P}_{\mathrm{co2}}$ of 3.5 atm
- $\mathrm{P}_{\text {total }}=\mathrm{P}_{\mathrm{O} 2}+\mathrm{P}_{\mathrm{co} 2}=1.0 \mathrm{~atm}+3.5 \mathrm{~atm}=4.5 \mathrm{~atm}$

