

## Molecular Speed and Energy

- Gas molecules travel at a range of speeds -some molecules move much faster than others.
- The average speed of a gas depends on its molar mass-the lighter the mass, the faster the average speed.



## Molecular Speed and Energy

- Average speed can be defined several ways for molecules:
- The most probable speed corresponds to the speed at the maximum in a plot of molecules vs speed-if we could measure the speed of individual gas molecules, more of them would have this value than any other value.



## Molecular Speed and Energy

Kinetic energy is given by
$\mathrm{E}_{\mathrm{T}}=1 / 2 \mathrm{mu}^{2}$
$\mathrm{m}=$ mass $\quad \mathrm{u}=$ velocity (speed)
$\mathrm{m}_{\mathrm{H} 2}=\left(2.0158 \mathrm{~g} \mathrm{~mol}^{-1}\right) /\left(6.022 \times 10^{23} \mathrm{H}_{2} \mathrm{~mol}^{-1}\right)$
$=3.347 \times 10^{-24} \mathrm{~g}=3.347 \times 10^{-27} \mathrm{~kg}$
$\mathrm{u}_{\mathrm{mp}}=1.57 \times 10^{3} \mathrm{~m} \mathrm{~s}^{-1}$
$\mathrm{E}_{\mathrm{T}}=1 / 2\left(3.347 \times 10^{-27} \mathrm{~kg}\right)\left(1.57 \times 10^{3} \mathrm{~m} \mathrm{~s}^{-1}\right)^{2}$
$=4.13 \times 10^{-21} \mathrm{~kg} \mathrm{~m}^{2} \mathrm{~s}^{-2}=4.13 \times 10^{-21} \mathrm{~J}$

## Molecular Speed and Energy

$$
\mathrm{u}_{\mathrm{mp}}\left(\mathrm{CH}_{4}\right)=557 \mathrm{~m} \mathrm{~s}^{-1}
$$

$$
\mathrm{E}_{\mathrm{T}}\left(\mathrm{CH}_{4}\right)=1 / 2\left(2.664 \times 10^{-26} \mathrm{~kg}\right)\left(557 \mathrm{~m} \mathrm{~s}^{-1}\right)^{2}
$$

$$
=4.13 \times 10^{-21} \mathrm{~J}
$$

$$
\mathrm{u}_{\mathrm{mp}}\left(\mathrm{CO}_{2}\right)=337 \mathrm{~m} \mathrm{~s}^{-1}
$$

$$
=4.15 \times 10^{-21} \mathrm{~J}
$$

Even though the three gases $\left(\mathrm{H}_{2}, \mathrm{CH}_{4}\right.$, and $\left.\mathrm{CO}_{2}\right)$ have different speeds, they all possess the same amount of kinetic energy.

## Molecular Speed and Energy

The average kinetic energy of a gas is determined by its temperature:

$$
\mathrm{E}_{\mathrm{T}}(\mathrm{~T})=3 / 2 \mathrm{RT} / \mathrm{N}_{\mathrm{A}}
$$

R is the gas constant

$$
\mathrm{E}_{\mathrm{T}}\left(\mathrm{CO}_{2}\right)=1 / 2\left(7.308 \times 10^{-26} \mathrm{~kg}\right)\left(337 \mathrm{~m} \mathrm{~s}^{-1}\right)^{2}
$$

$\mathrm{R}=8.314 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}=.08206 \mathrm{~L} \mathrm{~atm} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}$

- The kinetic energy of the gas depends only on its temperature, not the identity of the gas.



## Molecular Speed and Energy

The average speed of a gas is important because it determines a number of properties of a gas:
$\rightarrow$ pressure exerted by a gas-pressure depends on the rate of collision with the walls of a vessel and the force of those collisions.
$\rightarrow$ collision rate-how frequently gas molecules collide, and for reactive collisions, have the opportunity to undergo reaction.
$\rightarrow$ rate of diffusion-how fast one gas mixes with another


## Ideal Gas Equation

The properties of an ideal gas lead to an equation that relates the temperature, pressure, and volume of the gas:

$$
\begin{aligned}
& \hline \mathrm{PV}=\mathrm{nRT} \\
& \hline \mathrm{P}=\text { pressure }(\text { atm }) \\
& \mathrm{V}=\text { volume }(\mathrm{L}) \\
& \mathrm{n}=\text { number of moles of gas } \\
& \mathrm{T}=\text { temperature }(\mathrm{K}) \\
& \mathrm{R}=0.08206 \mathrm{~L} \text { atm } \mathrm{mol}^{-1} \mathrm{~K}^{-1}
\end{aligned}
$$




## Ideal Gas Equation

What volume would 2.00 mol of an ideal gas with a
${ }^{\circ} \mathrm{C}$ occupy?
$(1000$ Torr $)(1 \mathrm{~atm} / 760$ Torr $)=1.32 \mathrm{~atm}$
$-25.0^{\circ} \mathrm{C}+273.2{ }^{\circ} \mathrm{C}=248.2 \mathrm{~K}$
$\mathrm{V}=\mathrm{nRT} / \mathrm{P}$
$=\underline{(2.00 \mathrm{~mol})\left(.08206 \mathrm{~L} \mathrm{~atm} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}\right)(248.2 \mathrm{~K})}$
(1.32 atm)
$\mathrm{V}=30.9 \mathrm{~L}$


## Variations of the Ideal Gas Law

At constant volume:

$$
\begin{aligned}
& \mathrm{nR} / \mathrm{V}=\mathrm{a} \text { constant } \\
& \therefore \mathrm{P}_{1} / \mathrm{T}_{1}=\mathrm{P}_{2} / \mathrm{T}_{2}
\end{aligned}
$$

If the pressure [temperature] is increased, the temperature [pressure] will increase.
If the pressure [temperature] is decreased, the temperature [pressure] will decrease.

## Variations of the Ideal Gas Law

- At constant pressure:

$$
\mathrm{nR} / \mathrm{P}=\mathrm{a} \text { constant }
$$

$\therefore \mathrm{V}_{1} / \mathrm{T}_{1}=\mathrm{V}_{2} / \mathrm{T}_{2} \quad$ Charles' Law
If the volume [temperature] is increased, the temperature [volume] will increase.
If the volume [temperature] is decreased, the temperature [volume] will decrease.


## Dalton's Law of Partial Pressures

The total pressure of a gas mixture is given by:
$P_{\text {tot }}=n_{\text {tot }} R T / V$
$\mathrm{n}_{\text {tot }}=$ total number of moles of all gases in container
Also
$\frac{\mathrm{P}_{\text {tot }}=\mathrm{P}_{\mathrm{A}}+\mathrm{P}_{\mathrm{B}}+\mathrm{P}_{\mathrm{C}}+\ldots}{\text { Dalton's Law of Partial Pressures }}$
$P_{A}=n_{A} R T / V$ partial pressure of $A$
$P_{B}=n_{B} R T / V$ partial pressure of $B$
$\mathrm{P}_{\mathrm{C}}=\mathrm{n}_{\mathrm{C}} \mathrm{RT} / \mathrm{V}$ partial pressure of C


## Relative Humidity

- The amount of water in air is frequently expressed as relative humidity.
$\mathrm{RH} \equiv\left(\mathrm{P}_{\mathrm{H} 2 \mathrm{O}} / \mathrm{VP}_{\mathrm{H} 2 \mathrm{O}}\right) \times 100 \%$
$\mathrm{P}_{\mathrm{H} 2 \mathrm{O}}$ is partial pressure of water in air
$\mathrm{VP}_{\text {н2O }}$ is vapor pressure of water at a specific temperature
Vapor pressure is the pressure exerted by $\mathrm{H}_{2} \mathrm{O}(\mathrm{g})$ over a water sample in which equilibrium with the liquid is established. Vapor pressure depends on the temperature of the liquid - the higher the temperature, the higher the vapor pressure.






## AQMD Regulations to improve air quality

The South Coast Air Quality Management District (AQMD) is the governmental agency charged with improving air quality in the LA Basin.
Steps taken include:

- Decreased automotive emissions
- Restrictions on solvent use-LA Times required to change type of ink used
- Severe restrictions on industrial emissionsrefineries in South Bay
- Required change in barbecue lighter fluids


## AQMD Regulations to improve air quality

Proposed ideas for further improvement:

- Regulations on diesel engines-reduce emissions of both hydrocarbons and particulates
- Ban of "drive-thru" restaurants-idling cars emit hydrocarbons and NO without useful work being done
- Impose strict emission technologies on drycleaners
- Further restrictions on industrial emissions
- 1 out of 7 vehicle must ZEV by 2025



## The van der Waals' Equation

- To better describe real gases, we can use a different equation of state to predict their behavior:
$P=\frac{n R T}{V-n b}-\frac{a n^{2}}{V^{2}}$ Van der Waals' Equation
where a and b are measured constants
The vdw $b$ constant is a measure of the volume of the gas molecules
The vdw a constant is a measure of the internuclear attractive forces


## Real Gases vs Ideal Gases

Gases tend to behave ideally under low pressure conditions

- The time between collisions is much longer so there is less relative time for attractive forces to affect pressure (minimizes effect of a constant)
- The volume occupied by the gas molecules is much smaller than the total volume of the container (minimizes effect of $b$ constant)

