## M.Sc.(MATHEMATICS) SEMESTER-1 Math-551 REAL ANALYSIS

#### 12<sup>th</sup> July - 31<sup>st</sup> August-

- Unit 1:Set Theory, Countable And Uncountable Sets, Open And Closed Sets, Compact Sets And Their Different Properties, Compact Subsets Of Euclidean Spaces
- Unit 2:Perfect Sets, Compact Sets, Separated Sets, Connected Sets, Components, Functions Of Bounded Variations
- Unit 3:Sequences In Metric Spaces, Baire' Theorem, Banach Contraction Principle, Cantor's Intersection

#### 1<sup>st</sup> September – 15<sup>th</sup> September-

• Unit 4:Limits Of Functions, Continuity Of Functions, Continuity And Compactness, Connectedness And Continuity, Discontinuities, Monotonic Functions

<u>16<sup>th</sup> September – 30<sup>th</sup> September -</u>

College House Exams

<u>10<sup>th</sup> October – 5<sup>th</sup> November-</u>

• Unit 5:Reimann Stieltje's Integrals, Theorems Related to Integration

5<sup>th</sup> November – 20<sup>th</sup> November-

#### Math-552 Complex Analysis

#### <u>12<sup>th</sup> July - 31<sup>st</sup> August-</u>

- Unit 1:Functions of Complex Variables ,Continuity And Differentiability, Analytic Functions, Cauchy's Riemann Equations, Construction Of Analytic Functions
- Unit 2:Complex Line Integral, Cauchy's Theorem, Cauchy's Inequalities, Poisson's Integral Formula, Morera & Liouville's Theorem
- Unit 3:Conformal And Bilinear Transformations, Fixed Points, Analytical Continuation, Natural Boundary, Schwartz Reflection Principle

### 1<sup>st</sup> September – 15<sup>th</sup> September-

 Unit 4: Power Series, Taylor's Theorem, Laurent's Theorem, Max. Modulus Principle, Schwarz's Lemma, Poles And Zeros, Argument Principle, Fundamental Theorem Of Algebra And Rouche's Theorem

<u>16<sup>th</sup> September – 30<sup>th</sup> September –</u>

College House Exams

<u>10<sup>th</sup> October – 5<sup>th</sup> November-</u>

• Unit 5: Zeros And Singularities Of Functions, Evaluation Of Integrals, Integration Involving Many Valued Functions

5<sup>th</sup> November – 20<sup>th</sup> November-

#### MATH-553 ALGEBRA-1

<u>12<sup>th</sup> July - 31<sup>st</sup> August-</u>

- Unit 1: Groups, Subgroups, Normal Subgroups, Quotient Groups, Lagrange's Theorem
- Unit 2: Generating Sets, Cyclic Groups, Commutator Subgroups, Homomorphism, Isomorphism Theorems, Automorphisms
- Unit 3: Permutation Groups, The Alternating Groups, Cayley's Theorems, Fundamental Theorems For Finitely Generated Abelian Groups And Applications, Structure Of Such Groups

#### 1<sup>st</sup> September – 15<sup>th</sup> September-

 Unit 4: Conjugate Elements, Class Equation With Applications, Cauchy's Theorem, Sylow's Theorems And Applications, Jordan Holder Theorem, Solvable Groups, Composite Series

#### <u>16<sup>th</sup> September – 30<sup>th</sup> September –</u>

College House Exams

#### <u>10<sup>th</sup> October – 5<sup>th</sup> November-</u>

• Unit 5: Rings, Subrings, Ideals, Factor Rings, Homomorphism, Integral Domain, Maximal And Prime Ideals, The Field Of Quotients Of Integral Domain

5<sup>th</sup> November – 20<sup>th</sup> November-

#### MATH 555 DIFFERENTIAL EQUATIONS

<u>12<sup>th</sup> July - 31<sup>st</sup> August-</u>

- Unit 1: Existence And Uniqueness Theorems For Solution Of Differential Equations, Methods For Successive Approximation, General Properties Of Solution Of Linear Differential Equation Of Order n, Adjoint And Self Adjoint Equations
- Unit 2: Laplace Transforms, Inverse Laplace Convolution Theorem, Complex Inversion Formula
- Unit 3: Infinite Fourier Transforms, Problems Based on Infinite Fourier Transforms, Problems Based On Finite Fourier Transforms

### <u>1<sup>st</sup> September – 15<sup>th</sup> September-</u>

 Unit 4: Generating Functions, Recurrence Relation And Orthogonality Of Legendre Polynomials, Bessel Functions, Hermit And Laguerre Polynomials

<u>16<sup>th</sup> September – 30<sup>th</sup> September –</u>

College House Exams

<u>10<sup>th</sup> October – 5<sup>th</sup> November-</u>

 Unit 5: Total Differential Equations, Orthogonal Trajectory, Sturm Liouville's Boundary Value Problem, Sturm Comparison And Separation Theorems, Orthogonality Solution

5<sup>th</sup> November – 20<sup>th</sup> November-

#### MATH 554 MECHANICS-1

12<sup>th</sup> July - 31<sup>st</sup> August-

- Unit 1: Kinematics Of Particles And Rigid Bodies, Moving Axis, Instantaneous Axis Of Rotation And Instantaneous Centre Of Rotation
- Unit 2: Newton's Law Of Motion, Work, Energy And Power, Conservative Forces, Potential Energy, Impulsive Forces, Rectilinear particle Motion
- Unit 3: Projectile Motion Under Gravity, The Cycloid And Its Dynamical Properties

<u>1<sup>st</sup> September – 15<sup>th</sup> September-</u>

• Unit 4: Motion Of Particles Under A Central Force, Kepler's Laws Of Planetary Motion And Newton's Law Of Gravitation, Disturbed Orbits, Elliptic Harmonic Motion

<u>16<sup>th</sup> September – 30<sup>th</sup> September –</u>

**College House Exams** 

<u>10<sup>th</sup> October – 5<sup>th</sup> November-</u>

 Unit 5: Moment Of Inertia, Product Of Inertia, Theorems Of Parallel And Perpendicular Axis, Principle Axis, Coplanar Distribution

5<sup>th</sup> November – 20<sup>th</sup> November-

#### MATH-563 ALGEBRA

#### 6<sup>th</sup> January – 5<sup>th</sup> March -

- Unit 1: Principal Ideal Domains, Euclidean Rings, The Ring Of Guassian Integers, U.F.D , Polynomials Rings, Chain Conditions.
- Unit 2: Extension Field , Finite Algebraic , Simple , Separable Extensions , Algebraic Closed Fields.
- Unit 3: Splitting Fields: Existence And Uniqueness, Finite Fields, Existence Of Gf(P^N), Constructive Polygons.
- Unit 4: Galois Theory : Normal Extension Galois Group , Symmetric Rational Functions , Fundamental Theorem , Solvability By Radicals

6<sup>th</sup> March- 14<sup>th</sup> March-

College House Exams

15<sup>th</sup> March – 5<sup>th</sup> April-

 Unit 5: Modules, Cyclic Modules, Simple Modules, Free Modules, Fundamental Structure Theorem For Finitely Generated Module (Statement Only)

6<sup>th</sup> April – 20<sup>th</sup> April-

## M.Sc.(Mathematics) Semester-2 Math-561 Real Analysis

#### 6<sup>th</sup> January – 5<sup>th</sup> March -

- Unit 1: Sequence And Series Of Function, Discussion Of Main Problem, Uniform Convergence, Arzelas Theorem, Weierstrass Approximation Theorem.
- Unit 3: Measurable Function, Definition And Properties, Characterstic Function, Step Function And Simple Function, Little Wood's Three Principles.
- Unit 4: Lebesgue Integrals Of Bounded Function, Comparison Of Riemann And Lebesgue Integral. Convergence In Measure
- Unit 2: Outer Measure , Lebesgue Measure, Properties Of Measurable Sets , Non Measurable Sets

#### 6<sup>th</sup> March- 14<sup>th</sup> March-

College House Exams

15<sup>th</sup> March – 5<sup>th</sup> April-

• Unit 5: Differentiation Of Monotone Functions, Differentiation Of An Integral , Convergence In Measure.

6<sup>th</sup> April – 20<sup>th</sup> April-

#### Math-563 Tensors And Differential Geometry

6<sup>th</sup> January – 5<sup>th</sup> March –

- Unit 1: Notation And Summation Convention, Differentiation Of Cartesian Tensors, Metric Tensors, Contravariant, Covariant And Mixed Tensors.
- Unit 2: Theory Of Space Curve: Tangent , Principal Normal , Bi Normal , Curvature And Torsion.
- Unit 3: Spherical Indicatrix, Bertands Curve, Surfaces, Envelopes, Edge Of Regression, Developable Surfaces
- Unit 4:Curves On A Surface, Principal Of Curvature, Asymptotic Lines, Mainardi Codazzi Equations

## 6<sup>th</sup> March- 14<sup>th</sup> March-

College House Exams

## 15<sup>th</sup> March – 5<sup>th</sup> April-

 Unit 5: Geodesic, Differential Equation Of Geodesics, Geodesic Curvature, Clairaut's Theorem, Guass Bonnet Theorem, Joachimsthal's Theorem, Geodestic Mapping, Tissot's Theorem

6<sup>th</sup> April – 20<sup>th</sup> April-

#### Math-564 MECHANICS-2

## 6<sup>th</sup> January – 5<sup>th</sup> March –

- Unit 1: Motion & Linear Momentum Of System Of Particals, Angular Momentum Of System, Use Of Centroid, Moving Origins, Impulsive Forces, Problem In Two Dimensional Rigid Body Motion, Conservation Of Angular Momentum, Impulsive Motion
- Unit 2: Eular's dynamical Equations For Motion Of rigid Body About A Fixed Point, Problem Of General Three Dimensional Body
- Unit 3: Generalised Co-ordinate & Velocities Virtual Work, Generalised Forces, Lagrage's Equation For Holonomic System & For Impulsive Forces, K.E. As Quadratic Function Of Velocities, Small Oscillation Of Conservative Holonomic Dynamical System
- Unit 4: Linear Functioanal, Euler's & Lagrange's Equations For Single Dependent & Independent Variable, Hamilton's Principle And Principle Of Least Action

6<sup>th</sup> March-14<sup>th</sup> March-

College House Exams

15<sup>th</sup> March – 5<sup>th</sup> April-

 Unit 5: Euler's & Lagrange's Equation For Several Dependent & Independent Variables, Functions Involving Higher Order Derivatives, Approximate Sol<sup>n</sup> For Bondary Value Problems

6<sup>th</sup> April – 20<sup>th</sup> April-

#### Math-565 DIFFERENTIAL AND INTEGRAL EQUATIONS

6<sup>th</sup> January – 5<sup>th</sup> March –

- Unit 1: Origin Of 1<sup>st</sup> Order Partial Differential Equation, Cauchy Problem For 1<sup>st</sup> Order Equation,Surface Orthogonal To Given Surface, Charpit's & Jacobi's Method
- Unit 2: Origin Of Partial Differential Equation Of 2<sup>nd</sup> Order, Linear p.d.e. With Constant Coeff. & Complete Sol<sup>n</sup>, Non Linear Equation Of 2<sup>nd</sup> degree, Monge's Method
- Unit 3: Solution Of Laplace, Wave & Diffusion Equations By Method Of Separation Of Variables & Fourier Transforms, Greenfunction For These Equations
- Unit 4: Volterra Equations L<sub>2</sub> Kernals & Functions, Volterra Equations Of 1<sup>st</sup> & 2<sup>nd</sup> Kind, Volterra Integral Equations

## 6<sup>th</sup> March-14<sup>th</sup> March-

College House Exams

## <u>15<sup>th</sup> March – 5<sup>th</sup> April-</u>

 Unit 5: Fredholm's Equations With Pincherte-Goursat Kernel's, The Fredholm Theorem, Neumann's Series ,Methods Of Successive Approximations

6<sup>th</sup> April – 20<sup>th</sup> April-

#### Math-578 OPERATIONS RESEARCH

<u>12<sup>th</sup> July - 31<sup>st</sup> August-</u>

- Unit 1: The Linear Programming Problem, Generating Extreme Point Solution, The Artificial Basis Techniques, A First Feasible Solution Using Slack Variables, Two Phase And Big-M Method With Artificial Variables
- Unit 2: General Primal-Dual Prime, Primal Dual Pair In Matrix Form, Slackness Theorem, Duality And Simplex Method, Dual Simplex Method
- Unit 3: General Transportation Problem, Duality And Loops In Transportation, Test For Optimality, Degeneracy

1<sup>st</sup> September – 15<sup>th</sup> September-

 Unit 4: Mathematical Formulation Of Assignment Problem, Game Theory, Dominance Property, General Solution Of m\*n Rectangular Games

<u>16<sup>th</sup> September – 30<sup>th</sup> September -</u>

College House Exams

<u>10<sup>th</sup> October – 5<sup>th</sup> November-</u>

 Unit 5: Gomory's all I.P.P., Branch And Bound Method, Applications Of Integer Programming, Dynamic Programming Algorithm, Application And Solution Of L.P.P. By Dynamic Programming

5<sup>th</sup> November – 20<sup>th</sup> November-

## M.Sc.(MATHEMATICS) SEMESTER-3 Math-571 FUNCTIONAL ANALYSIS

#### 12<sup>th</sup> July - 31<sup>st</sup> August-

- Unit 1: Normed Linear Spaces, Banach Spaces, Subspaces, Quotient Spaces, L<sup>P</sup>–Spaces: Holder's And Minkowski's Inequalities, Convergence And Completeness, Riesz-Fischer Theorem
- Unit 2: Continuous Linear Transformations, Equivalent Norms, Finite Dimensional Normed Linear Spaces And Riesz Theorem
- Unit 3: The Conjugate Space N<sup>\*</sup>, The Hahn-Banach Theorem And Its Consequences, Natural Imbedding Of N into N<sup>\*\*</sup>, Reflexivity Of Normed Spaces

<u>1<sup>st</sup> September – 15<sup>th</sup> September-</u>

 Unit 4:Open Mapping Theorem, Projections On A Banach Space, Closed Graph Theorem, Uniform Boundedness Principle, Conjugate Operators

<u>16<sup>th</sup> September – 30<sup>th</sup> September -</u>

College House Exams

<u>10<sup>th</sup> October – 5<sup>th</sup> November-</u>

 Unit 5: Inner Product Spaces, Hilbert Spaces, Orthogonal Complements, Orthogonal Sets, The Conjugate Space H<sup>\*</sup>

5<sup>th</sup> November – 20<sup>th</sup> November-

#### Math-575 DISCRETE MATHEMATICS

#### 12<sup>th</sup> July - 31<sup>st</sup> August-

- Unit 1:Binary Relations, Equivalence Relations And Partitions, Inclusion And Exclusion Principle, Hasse Diagram, Pigeon Hole Principle
- Unit 2: Basic Logical operations, Conditional And Biconditional Statements, Tautologies, Contradiction, Quantifiers, Prepositional Calculus
- Unit 3: Definition And Examples Of Semigroups And Monoids, Homomorphism Of Semigroups And Monoids, Congruence Relations And Quotient Subgroups

## 1<sup>st</sup> September – 15<sup>th</sup> September-

 Unit 4: Phrase Structure Grammars, Rewriting Rules, Derivation Sentential Forms, Languauge Generated By Grammar, Regular, Context Free And Context Sensitive Grammar And Languages

<u>16<sup>th</sup> September – 30<sup>th</sup> September -</u>

College House Exams

<u>10<sup>th</sup> October – 5<sup>th</sup> November-</u>

 Unit 5: Polynomial Expressions, Telescopic Form, Recursion Theorem, Closed Form Expression, Generating Function, Solution Of Recurrence Relation Using Generating Function

5<sup>th</sup> November – 20<sup>th</sup> November-

#### Math-577 STATISTICS

#### <u>12<sup>th</sup> July - 31<sup>st</sup> August-</u>

- Unit 1:Measures Of Central Tendency And Dispersion, Moments, Measure Of Skewness And Kurtosis, Classical And Axiomatic Approach To The Theory Of Probability
- Unit 2: Random Variable, Probability Mass Function, Probability Density Function, Cumulative Distribution Function, Two And Higher Dimensional Random Variables, Stochastic Independence
- Unit 3: Mathematical Expectations And Moments, Moment Generating Function And Its Properties, Chebyshev's Inequality And Its Application, Stochastic Convergence, Central Limit

#### 1<sup>st</sup> September – 15<sup>th</sup> September-

 Unit 4: Uniform Hyper Geometric, Binomial, Poisson, Geometric, Hyper Geometric, Multinomial, Uniform, Exponential, Gamma, Beta, Normal Distribution

<u>16<sup>th</sup> September – 30<sup>th</sup> September -</u>

College House Exams

<u>10<sup>th</sup> October – 5<sup>th</sup> November-</u>

• Unit 5: Least Square Principle, Correlation And Linear Regression Analysis For Bi-variate Data, Partial And Multiple Correlation Coefficients, Correlation Ratio, Association Of Attributes

5<sup>th</sup> November – 20<sup>th</sup> November-

## MATH- 585 DISCRETE MATHS

## 6<sup>th</sup> January – 5<sup>th</sup> March-

- Unit 1: Lattices,Lattices As Partially Ordered Sets, Properties, Lattices As Algebraic Systems, Sublattices, Direct Products, Homomorphism
- Unit 2: Boolean Algebra, Boolean Algebra As Lattices, Boolean Identities, Sub-Algebra, Direct Product, Homomorphism, Join-Irreducible Elements, Atoms And Minterms, Boolean Forms And Their Equivalence
- Unit 3: Graph Theory: Definition, Undirected Graphs, Paths, Circuits, Cycles, Subgraphs, Induced Subgraphs, Degree Of Vertex, Connectivity, Planner Graph, Complete
- Unit 4: Euler's Theorem On The Existence Of Eulerian Paths And Circuits, Directed Graphs, In-Degree And Out-Degree Of A Weighted Graphs, Cut Set, Fundamental Cut Sets And Cycles

6<sup>th</sup> March – 14<sup>th</sup> March-

**Revision And Class Tests** 

15<sup>th</sup>march- 5<sup>th</sup> April-

• Unit 5: Trees: Rooted Tree, Directed Trees, Search Tree, Tree Traversals, Spanning Trees, Minimal Spanning Trees

6<sup>th</sup> April -20<sup>th</sup> April-

## M.Sc (MATHEMATICS) SEMESTER 4 MATH-581 FUNCTIONAL ANALYSIS

### 6th January – 5th March

- Unit 1: Strong And Weak Convergence In Finite And Infinite Dimensional Normed Linear Spaces, Weak Convergences In Hilbert Spaces
- Unit 2: The Adjoint Of An Operator, Self Adjoint Operators, Normal Operators, Unitary Operators
- Unit 3: Finite Dimensional Spectral Theory, Eigen-Values And Eigen Vectors, Spectrum Of A Bounded Linear Operator
- Unit 4: Compact Linear Operator On Normed Spaces, Properties Of Compact Linear Operators, Spectral Properties Of Compact Linear Operators

6<sup>th</sup> March – 14<sup>th</sup> March-

Revision And Class Tests

15<sup>th</sup>march- 5<sup>th</sup> April -

• Unit-V : Banach Algebras, Definitions And Simple Examples, Regular And Singular Elements, Topological Divisors Of Zero

6<sup>th</sup> April -20<sup>th</sup> April-

## MATH-588 OPERATIONS RESEARCH

## 6<sup>th</sup> January – 5<sup>th</sup> March

- Unit 1 : Queueing Theory, Introduction, Queueing System, Elements Of Queueing System, Distributions Of Arrivals, Inter Arrivals
- Unit 2: Queueing Models, (M/M/1): (N/FIFO), Generalized Model: Birth-Death Process, (M/M/C): (/FIFO), (M/M/C) (N/FIFO), (M/M/R) (KIGD), Power Supply Model.
- Unit 3: Inventory Controlthe Inventory Decisions, Costs Associated With Inventories, Factors Affecting Inventory Control, Economic Order Quantity (EOQ)
- Unit 4: Replacement Problems, Replacement Of Equipment/Asset That Deteriorates Gradually

6<sup>th</sup> March – 14<sup>th</sup> March-

**Revision And Class Tests** 

15<sup>th</sup>march- 5<sup>TH</sup> APRIL-

 Unit 5: Need Of Simulation, Methodology Of Simulation.
Simulation Models, Event- Type Simulation, Generation Of Random Numbers

<u>6<sup>th</sup> April -20<sup>th</sup> April</u>

## MATH- 587 STATISTICS

## 6<sup>th</sup> January – 5<sup>th</sup> March-

- Unit1: Sampling Distributions: Chi-square, t And F-Distributions With Their Properties, Distribution Of Sample Mean And Variance, Distribution Of Order Statistics
- Unit-2: Point Estimation: Estimators, Properties Of Unbiased Ness, Consistency, Sufficiency, Efficiency, Completeness, Uniqueness, Methods Of Estimation
- Unit 3: Testing Of Hypothesis: Null Hypothesis And Its Test Of Significance, Simple And Composite Hypothesis, M.P. Test, UMP Test, Likelihood Tests
- Unit 4: Applications Of Sampling Distributions: Test Of Mean And Variance In The Normal Distribution

6<sup>th</sup> March – 14<sup>th</sup> March-

**Revision And Class Tests** 

15<sup>th</sup> March- 5<sup>TH</sup> April-

• Unit 5 :Linear Estimation: Gauss Markoff Linear Models, Gauss Markoff Theorem

6<sup>th</sup> April -20<sup>th</sup> April-

# MATH- 581 TOPOLOGY

### 6th January – 5th March

- Unit 1: Higher Separation Axioms, Completely Regular Spaces. Tychonoff Spaces, Completely Normal Space
- Unit2: Compact Spaces, Compact Sets, Subsets Of Compact Space, Finite Intersection Property, Compactness Of Subsets Of Real Line.
- Unit3: Sequentially Compact Spaces, Bolzano Weierstrass Property, Countably Compact Spaces, Locally Compact Spaces. Tychonoff theorem,One Point Compactification.
- Unit4: The Stone-Čech Compactification, Evaluation Mappings, Separate Point Family, Separate Point And Closed Set Family.

6<sup>th</sup> March – 15<sup>th</sup> March-

**Revision And Class Tests** 

15<sup>th</sup>march- 5<sup>th</sup> April-

• Unit5: Directed Sets And Nets. Convergence Of A Net In A Space, Clustering Of A Net, Nets And Continuity, Nets In Product Spaces, Ultra Nets.

6<sup>th</sup> April -20<sup>th</sup> April-

## MATH 572 TOPOLOGY

## 12<sup>TH</sup> JULY- 31<sup>ST</sup> AUGUST-

- UNIT- I Topological Spaces, Basic concepts, closure, interior, exterior and boundary of a set. Dense sets, Closure operator [Kuratowski function] and Interior operator. Neighbourhoods and neighbourhood system, Coarser and finer topologies.
- Unit II Sub-spaces, Hereditary properties, Separated sets, Connected sets, Connected and disconnected spaces, Connectedness on real line
- Unit III Continuous functions, Restriction and extension of a mapping. Sequential continuity at point. Invariants under a continuous mapping. Open and closed mappings.

## 1<sup>ST</sup> SEPTEMBER-16<sup>TH</sup> SEPTEMBER

 Unit – IV Product of two spaces, The product of n spaces. Base for a finite product topology. General product spaces.

## 17<sup>th</sup> SEPTEMBER-30th SEPTEMBER

College house exam

9<sup>TH</sup> OCTOBER-5<sup>TH</sup> NOVEMBER

 Unit – V Separation Axioms: T0, T1, T2 – spaces. Regular spaces, T3 – spaces, Normal spaces, T4 – space. Tychonoff lemma, Urysohn lemMA

6<sup>TH</sup> NOVEMBER-15<sup>TH</sup> NOVEMBER-

Revision and class test