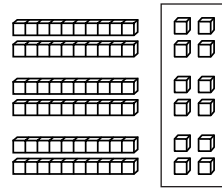


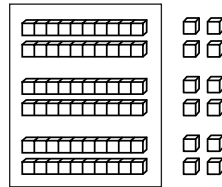
# Multiply 2-Digit Numbers

**Example**    24  
               × 3  
               —



(3 × 4 ones)

- Multiply the ones.  
 $3 \times 4 \text{ ones} = 12 \text{ ones}$



(3 × 2 tens)

- Multiply the tens.  
 $3 \times 2 \text{ tens} = 6 \text{ tens}$
- Record the products under the original problem.
- Add the two products.

$$\begin{array}{r}
 24 \\
 \times 3 \\
 \hline
 12 \leftarrow 3 \times 4 \text{ ones} \\
 +60 \leftarrow 3 \times 2 \text{ tens} \\
 \hline
 72 \leftarrow \text{total}
 \end{array}$$

Find the product. You may wish to use base-ten blocks.

1.    13  
       × 2  
       —  
       ← product of ones  
       .....  
       ← product of tens  
       +  
       .....  
       .....

2.    23  
       × 4  
       —  
       ← product of ones  
       .....  
       ← product of tens  
       +  
       .....  
       .....

3.    15  
       × 3  
       —  
       ← product of ones  
       .....  
       ← product of tens  
       +  
       .....  
       .....

4.    16  
       × 5  
       —  
       ← product of ones  
       .....  
       ← product of tens  
       +  
       .....  
       .....

5.    12  
       × 3  
       —  
       ← product of ones  
       .....  
       ← product of tens  
       +  
       .....  
       .....

6.    22  
       × 5  
       —  
       ← product of ones  
       .....  
       ← product of tens  
       +  
       .....  
       .....

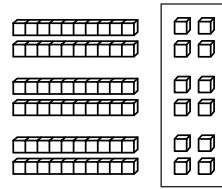
7.    32  
       × 4  
       —

8.    25  
       × 4  
       —

9.    36  
       × 5  
       —

# Multiply 2-Digit Numbers

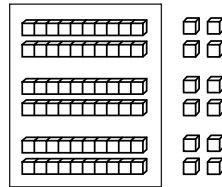
**Example** 
$$\begin{array}{r} 24 \\ \times 3 \\ \hline \end{array}$$



(3 × 4 ones)

- Multiply the ones.  
3 × 4 ones = 12 ones

- Multiply the tens.  
3 × 2 tens = 6 tens



(3 × 2 tens)

- Record the products under the original problem.
- Add the two products.

$$\begin{array}{r} 24 \\ \times 3 \\ \hline 12 \leftarrow 3 \times 4 \text{ ones} \\ +60 \leftarrow 3 \times 2 \text{ tens} \\ \hline 72 \leftarrow \text{total} \end{array}$$

Find the product. You may wish to use base-ten blocks.

1. 
$$\begin{array}{r} 13 \\ \times 2 \\ \hline 6 \\ \hline +20 \\ \hline 26 \end{array}$$

← product of ones  
← product of tens

2. 
$$\begin{array}{r} 23 \\ \times 4 \\ \hline 12 \\ \hline +80 \\ \hline 92 \end{array}$$

← product of ones  
← product of tens

3. 
$$\begin{array}{r} 15 \\ \times 3 \\ \hline 15 \\ \hline +30 \\ \hline 45 \end{array}$$

← product of ones  
← product of tens

4. 
$$\begin{array}{r} 16 \\ \times 5 \\ \hline 30 \\ \hline +50 \\ \hline 80 \end{array}$$

← product of ones  
← product of tens

5. 
$$\begin{array}{r} 12 \\ \times 3 \\ \hline 6 \\ \hline +30 \\ \hline 36 \end{array}$$

← product of ones  
← product of tens

6. 
$$\begin{array}{r} 22 \\ \times 5 \\ \hline 10 \\ \hline +100 \\ \hline 110 \end{array}$$

← product of ones  
← product of tens

7. 
$$\begin{array}{r} 32 \\ \times 4 \\ \hline 128 \end{array}$$

8. 
$$\begin{array}{r} 25 \\ \times 4 \\ \hline 100 \end{array}$$

9. 
$$\begin{array}{r} 36 \\ \times 5 \\ \hline 180 \end{array}$$

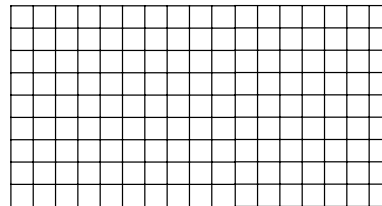
## Multiply 2-Digit Numbers

You can use grid paper to help you find the product of a 1-digit number and a 2-digit number.

### EXAMPLE

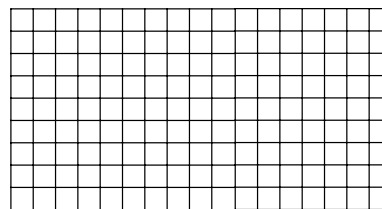
Find the product  $7 \times 15$ .

**Step 1** Draw a rectangle with 7 rows and 15 columns.



**Step 2** Draw a line after the tenth column to make two rectangles.

- There are 7 rows of 10.       $7 \times 10 = 70$
- There are 7 rows of 5.       $7 \times 5 = 35$
- There are 105 squares in all.       $70 + 35 = 105$



So,  $7 \times 15 = 105$ .

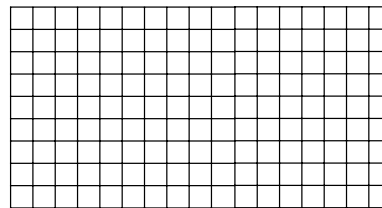
1. Use grid paper to model  $6 \times 13$ .

a. How many rows of 10 are there? \_\_\_\_\_

b. How many rows of 3 are there? \_\_\_\_\_

c. How many squares are there in all? \_\_\_\_\_

d. What is  $6 \times 13$ ? \_\_\_\_\_



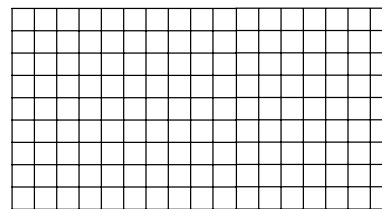
2. Use grid paper to model  $4 \times 11$ .

a. How many rows of 10 are there? \_\_\_\_\_

b. How many rows of 1 are there? \_\_\_\_\_

c. How many squares are there in all? \_\_\_\_\_

d. What is  $4 \times 11$ ? \_\_\_\_\_



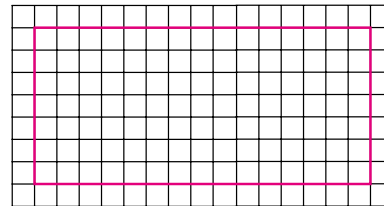
## Multiply 2-Digit Numbers

You can use grid paper to help you find the product of a 1-digit number and a 2-digit number.

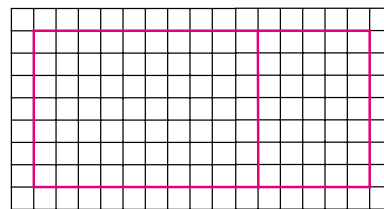
### EXAMPLE

Find the product  $7 \times 15$ .

**Step 1** Draw a rectangle with 7 rows and 15 columns.



**Step 2** Draw a line after the tenth column to make two rectangles.



- There are 7 rows of 10.  $7 \times 10 = 70$
- There are 7 rows of 5.  $7 \times 5 = 35$
- There are 105 squares in all.  $70 + 35 = 105$

So,  $7 \times 15 = 105$ .

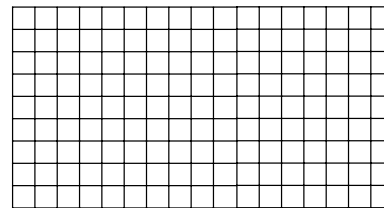
1. Use grid paper to model  $6 \times 13$ .

a. How many rows of 10 are there? 6

b. How many rows of 3 are there? 6

c. How many squares are there in all? 78

d. What is  $6 \times 13$ ? 78



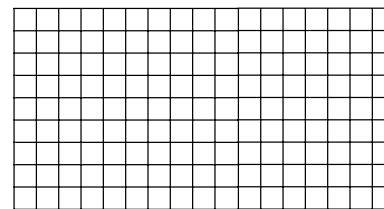
2. Use grid paper to model  $4 \times 11$ .

a. How many rows of 10 are there? 4

b. How many rows of 1 are there? 4

c. How many squares are there in all? 44

d. What is  $4 \times 11$ ? 44



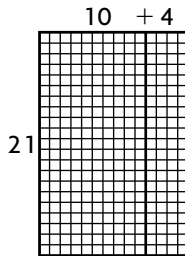
## Multiply by 2-Digit Numbers

You can multiply by two-digit numbers by breaking apart one of the factors.

To find  $21 \times 14$ , you can break apart 14 into 1 ten 4 ones.

**Step 1** Multiply by the ones.

$$\begin{array}{r} 21 \\ \times 4 \\ \hline \end{array}$$



**Step 3** Add the products.

$$\begin{array}{r} 21 \\ \times 14 \\ \hline 84 \leftarrow 4 \times 21 \\ +210 \leftarrow 10 \times 21 \\ \hline 294 \end{array}$$

**Step 2** Multiply by the tens.

$$\begin{array}{r} 21 \\ \times 10 \\ \hline 210 \end{array}$$

So,  $21 \times 14 = 294$ .

Complete to find the product.

1.  $\begin{array}{r} 13 \\ \times 12 \\ \hline \end{array}$   
 $\leftarrow$  \_\_\_\_\_  $\times$  \_\_\_\_\_  
 $+$  \_\_\_\_\_  $\leftarrow$  \_\_\_\_\_  $\times$  \_\_\_\_\_

2.  $\begin{array}{r} 22 \\ \times 15 \\ \hline \end{array}$   
 $\leftarrow$  \_\_\_\_\_  $\times$  \_\_\_\_\_  
 $+$  \_\_\_\_\_  $\leftarrow$  \_\_\_\_\_  $\times$  \_\_\_\_\_

3.  $\begin{array}{r} 30 \\ \times 17 \\ \hline \end{array}$   
 $\leftarrow$  \_\_\_\_\_  $\times$  \_\_\_\_\_  
 $+$  \_\_\_\_\_  $\leftarrow$  \_\_\_\_\_  $\times$  \_\_\_\_\_

4.  $\begin{array}{r} 28 \\ \times 14 \\ \hline \end{array}$   
 $\leftarrow$  \_\_\_\_\_  $\times$  \_\_\_\_\_  
 $+$  \_\_\_\_\_  $\leftarrow$  \_\_\_\_\_  $\times$  \_\_\_\_\_

5.  $\begin{array}{r} 40 \\ \times 19 \\ \hline \end{array}$   
 $\leftarrow$  \_\_\_\_\_  $\times$  \_\_\_\_\_  
 $+$  \_\_\_\_\_  $\leftarrow$  \_\_\_\_\_  $\times$  \_\_\_\_\_

6.  $\begin{array}{r} 45 \\ \times 15 \\ \hline \end{array}$   
 $\leftarrow$  \_\_\_\_\_  $\times$  \_\_\_\_\_  
 $+$  \_\_\_\_\_  $\leftarrow$  \_\_\_\_\_  $\times$  \_\_\_\_\_

7.  $\begin{array}{r} 37 \\ \times 15 \\ \hline \end{array}$   
 $\leftarrow$  \_\_\_\_\_  $\times$  \_\_\_\_\_  
 $+$  \_\_\_\_\_  $\leftarrow$  \_\_\_\_\_  $\times$  \_\_\_\_\_

8.  $\begin{array}{r} 28 \\ \times 16 \\ \hline \end{array}$   
 $\leftarrow$  \_\_\_\_\_  $\times$  \_\_\_\_\_  
 $+$  \_\_\_\_\_  $\leftarrow$  \_\_\_\_\_  $\times$  \_\_\_\_\_

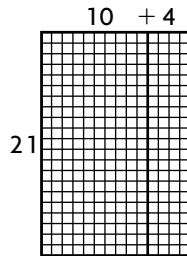
## Multiply by 2-Digit Numbers

You can multiply by two-digit numbers by breaking apart one of the factors.

To find  $21 \times 14$ , you can break apart 14 into 1 ten 4 ones.

**Step 1** Multiply by the ones.

$$\begin{array}{r} 21 \\ \times 4 \\ \hline \end{array}$$



**Step 3** Add the products.

$$\begin{array}{r} 21 \\ \times 14 \\ \hline 84 \leftarrow 4 \times 21 \\ +210 \leftarrow 10 \times 21 \\ \hline 294 \end{array}$$

**Step 2** Multiply by the tens.

$$\begin{array}{r} 21 \\ \times 10 \\ \hline 210 \end{array}$$

So,  $21 \times 14 = 294$ .

Complete to find the product.

$$\begin{array}{r} 1. \quad 13 \\ \times 12 \\ \hline 26 \leftarrow 2 \times 13 \\ +130 \leftarrow 10 \times 13 \\ \hline 156 \end{array}$$

$$\begin{array}{r} 2. \quad 22 \\ \times 15 \\ \hline 110 \leftarrow 5 \times 22 \\ +220 \leftarrow 10 \times 22 \\ \hline 330 \end{array}$$

$$\begin{array}{r} 3. \quad 30 \\ \times 17 \\ \hline 210 \leftarrow 7 \times 30 \\ +300 \leftarrow 10 \times 30 \\ \hline 510 \end{array}$$

$$\begin{array}{r} 4. \quad 28 \\ \times 14 \\ \hline 112 \leftarrow 4 \times 28 \\ +280 \leftarrow 10 \times 28 \\ \hline 392 \end{array}$$

$$\begin{array}{r} 5. \quad 40 \\ \times 19 \\ \hline 360 \leftarrow 9 \times 40 \\ +400 \leftarrow 10 \times 40 \\ \hline 760 \end{array}$$

$$\begin{array}{r} 6. \quad 45 \\ \times 15 \\ \hline 225 \leftarrow 5 \times 45 \\ +450 \leftarrow 10 \times 45 \\ \hline 675 \end{array}$$

$$\begin{array}{r} 7. \quad 37 \\ \times 15 \\ \hline 185 \leftarrow 5 \times 37 \\ +370 \leftarrow 10 \times 37 \\ \hline 555 \end{array}$$

$$\begin{array}{r} 8. \quad 28 \\ \times 16 \\ \hline 168 \leftarrow 6 \times 28 \\ +280 \leftarrow 10 \times 28 \\ \hline 448 \end{array}$$

## Multiply 3- and 4-Digit Numbers

You can use place value and the expanded form of a 3- or 4-digit number to multiply it by another number.

**Step 1** Write the expanded form of the 3-digit or 4-digit number.

**Step 2** Multiply each addend by the one-digit number.

**Step 3** Add these numbers.

Multiply. $4 \times 324$		Multiply. $3 \times 2,642$	
<b>Expand</b>	<b>Multiply by 4</b>	<b>Expand</b>	<b>Multiply by 3</b>
300	1,200	2,000	6,000
20	80	600	1,800
4	+ 16	40	120
	<u>1,296</u> ← <b>Sum</b>	2	+ 6
		<u>7,926</u> ← <b>Sum</b>	

Use place value and the expanded form of the 3-digit or 4-digit number to find the product.

1.  $2 \times 456$

<b>Expand</b>	<b>Multiply by 2</b>
400	_____
50	_____
6	+ _____
	_____ ← <b>Sum</b>

2.  $3 \times 619$

<b>Expand</b>	<b>Multiply by _____</b>
_____	_____
_____	_____
_____	+ _____
	_____ ← <b>Sum</b>

3.  $5 \times 631$

<b>Expand</b>	<b>Multiply by _____</b>
_____	_____
_____	_____
_____	+ _____
	_____ ← <b>Sum</b>

4.  $4 \times 2,351$

<b>Expand</b>	<b>Multiply by _____</b>
_____	_____
_____	_____
_____	+ _____
	_____ ← <b>Sum</b>

5.  $3 \times 4,263$

<b>Expand</b>	<b>Multiply by _____</b>
_____	_____
_____	_____
_____	+ _____
	_____ ← <b>Sum</b>

6.  $8 \times 3,142$

<b>Expand</b>	<b>Multiply by _____</b>
_____	_____
_____	_____
_____	+ _____
	_____ ← <b>Sum</b>

## Multiply 3- and 4-Digit Numbers

You can use place value and the expanded form of a 3- or 4-digit number to multiply it by another number.

**Step 1** Write the expanded form of the 3-digit or 4-digit number.

**Step 2** Multiply each addend by the one-digit number.

**Step 3** Add these numbers.

Multiply. $4 \times 324$		Multiply. $3 \times 2,642$	
<b>Expand</b>	<b>Multiply by 4</b>	<b>Expand</b>	<b>Multiply by 3</b>
300	1,200	2,000	6,000
20	80	600	1,800
4	+ 16	40	120
	<u>1,296</u> ← <b>Sum</b>	2	+ 6
		<u>7,926</u> ← <b>Sum</b>	

Use place value and the expanded form of the 3-digit or 4-digit number to find the product.

1.  $2 \times 456$

<b>Expand</b>	<b>Multiply by 2</b>
400	<u>800</u>
50	<u>100</u>
6	+ <u>12</u>
	<u>912</u> ← <b>Sum</b>

2.  $3 \times 619$

<b>Expand</b>	<b>Multiply by <u>3</u></b>
<u>600</u>	<u>1,800</u>
<u>10</u>	<u>30</u>
<u>9</u>	+ <u>27</u>
	<u>1,857</u> ← <b>Sum</b>

3.  $5 \times 631$

<b>Expand</b>	<b>Multiply by <u>5</u></b>
<u>600</u>	<u>3,000</u>
<u>30</u>	<u>150</u>
<u>1</u>	+ <u>5</u>
	<u>3,155</u> ← <b>Sum</b>

4.  $4 \times 2,351$

<b>Expand</b>	<b>Multiply by <u>4</u></b>
<u>2,000</u>	<u>8,000</u>
<u>300</u>	<u>1,200</u>
<u>50</u>	<u>200</u>
<u>1</u>	+ <u>4</u>
	<u>9,404</u> ← <b>Sum</b>

5.  $3 \times 4,263$

<b>Expand</b>	<b>Multiply by <u>3</u></b>
<u>4,000</u>	<u>12,000</u>
<u>200</u>	<u>600</u>
<u>60</u>	<u>180</u>
<u>3</u>	+ <u>9</u>
	<u>12,789</u> ← <b>Sum</b>

6.  $8 \times 3,142$

<b>Expand</b>	<b>Multiply by <u>8</u></b>
<u>3,000</u>	<u>24,000</u>
<u>100</u>	<u>800</u>
<u>40</u>	<u>320</u>
<u>2</u>	+ <u>16</u>
	<u>25,136</u> ← <b>Sum</b>



## Multiply 2-Digit Numbers

Solve  $12 \times 15$  by using the partial-products method.

**Step 1**

$$\begin{array}{r} 15 \\ \times 12 \\ \hline \end{array}$$

**Step 2**

$$\begin{array}{r} 15 \\ \times 12 \\ \hline \end{array}$$

**Step 3**

$$\begin{array}{r} 15 \\ \times 12 \\ \hline \end{array}$$

**Step 4**

$$\begin{array}{r} 15 \\ \times 12 \\ \hline \end{array}$$

**Partial Products**

		1	5
×		1	2
	$2 \times 5 =$	1	0
	$2 \times 10 =$	2	0
	$10 \times 5 =$	5	0
	$10 \times 10 =$	1	0
product →		1	8

**Step 5**

Add partial products together.

$$10 + 20 + 50 + 100 = 180$$

The product of 12 and 15 is 180.

Multiply by using the partial-products method.

1.

		3	1
×		1	7
$7 \times 1 =$			
$7 \times 30 =$			
$10 \times 1 =$			
$10 \times 30 =$			
product →			

2.

		4	6
×		2	8
$8 \times 6 =$			
$8 \times 40 =$			
$20 \times 6 =$			
$20 \times 40 =$			
product →			

3.

		7	9
×		5	6
$6 \times 9 =$			
$6 \times 70 =$			
$50 \times 9 =$			
$50 \times 70 =$			
product →			

4. 
$$\begin{array}{r} 82 \\ \times 25 \\ \hline \end{array}$$

5. 
$$\begin{array}{r} 63 \\ \times 47 \\ \hline \end{array}$$

6. 
$$\begin{array}{r} 92 \\ \times 34 \\ \hline \end{array}$$

## Multiply 2-Digit Numbers

Solve  $12 \times 15$  by using the partial-products method.

**Step 1**

$$\begin{array}{r} 15 \\ \times 12 \\ \hline \end{array}$$

**Step 2**

$$\begin{array}{r} 15 \\ \times 12 \\ \hline \end{array}$$

**Step 3**

$$\begin{array}{r} 15 \\ \times 12 \\ \hline \end{array}$$

**Step 4**

$$\begin{array}{r} 15 \\ \times 12 \\ \hline \end{array}$$

**Partial Products**

		1	5
	×	1	2
<hr/>			
$2 \times 5 =$		1	0
$2 \times 10 =$		2	0
$10 \times 5 =$		5	0
$10 \times 10 =$	1	0	0
product $\rightarrow$	1	8	0

**Step 5**

Add partial products together.

$$10 + 20 + 50 + 100 = 180$$

The product of 12 and 15 is 180.

Multiply by using the partial-products method.

1.

		3	1
	×	1	7
<hr/>			
$7 \times 1 =$			7
$7 \times 30 =$	2	1	0
$10 \times 1 =$		1	0
$10 \times 30 =$	3	0	0
product $\rightarrow$	5	2	7

2.

		4	6
	×	2	8
<hr/>			
$8 \times 6 =$		4	8
$8 \times 40 =$	3	2	0
$20 \times 6 =$	1	2	0
$20 \times 40 =$	8	0	0
product $\rightarrow$	1	2	8

3.

		7	9
	×	5	6
<hr/>			
$6 \times 9 =$		5	4
$6 \times 70 =$	4	2	0
$50 \times 9 =$	4	5	0
$50 \times 70 =$	3	5	0
product $\rightarrow$	4	4	2

4.

$$\begin{array}{r} 82 \\ \times 25 \\ \hline 10 \\ 400 \\ 40 \\ 1,600 \\ \hline 2,050 \end{array}$$

5.

$$\begin{array}{r} 63 \\ \times 47 \\ \hline 21 \\ 420 \\ 120 \\ 2,400 \\ \hline 2,961 \end{array}$$

6.

$$\begin{array}{r} 92 \\ \times 34 \\ \hline 8 \\ 360 \\ 60 \\ 2,700 \\ \hline 3,128 \end{array}$$