## UNIT 7

## GRAPHING TRIG FUNCTIONS

| DATE | PAGE | TOPIC | HOMEWORK |
| :---: | :---: | :--- | :--- |
| $2 / 10$ | 2,3 | The Sin graph <br> The Cos graph | No Homework |
| $2 / 11$ | 4,5 | Investigation of Amplitudes | AMPLITUDE Homework Worksheet |
| $2 / 12$ | 6 | Investigation of Frequencies | FREQUENCY Homework Worksheet |
| $2 / 13$ | 7 | Finding periods and sketching <br> graphs | PERIOD Homework Worksheet |
| $2 / 14$ | x | Graphing Sin and Cos <br> QUIZ | No Homework |
| $2 / 17-$ <br> $2 / 21$ |  | WINER BREAK | Relax and enjoy your break |
| $2 / 24$ | 8 | Graphing Tan | No Homework |
| $2 / 25$ | x | More Tan and Review of all trig <br> functions | FINISH REVIEW! |
| $2 / 26$ |  | REVIEW | STUDY |
| $2 / 27$ |  | TEST | NO HOMEWORK! |

## Graphing Sin x

In order to graph $y=\sin x$, we will use the $x$-axis as a number line in terms of pi .
We will start by filling in the chart below:

| X <br> (radians) | 0 | $\pi / 6$ | $\pi / 3$ | $\pi / 2$ | $2 \pi / 3$ | $5 \pi / 6$ | $\pi$ | $7 \pi / 6$ | $4 \pi / 3$ | $3 \pi / 2$ | $5 \pi / 3$ | $11 \pi /$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Now we will take the values that we just found and sketch a graph.

**This curve represents the basic sine

Fill in the questions below using Increases or Decreases
From 0 to pi/2 (quadrant I), $\sin x$ $\qquad$ from 0 to 1 .

From pi/2 to pi (quadrant II), $\sin x$ $\qquad$ from 1 to 0.

From pi to 3pi/2 (quadrant III), $\sin x$ $\qquad$ from 0 to -1 .

From 3pi/2 to 2pi (quadrant IV), $\sin x$ $\qquad$ from -1 to 0 .

## Graphing $\operatorname{Cos} \mathbf{x}$

Now we will do the same thing for the graph of $\operatorname{Cos} x$
$\left.\begin{array}{|l|l|l|l|l|l|l|l|l|l|l|l|l|l|}\hline \begin{array}{l}\text { X } \\ \text { (radians) }\end{array} & 0 & \pi / 6 & \pi / 3 & \pi / 2 & 2 \pi / 3 & 5 \pi / 6 & \pi & 7 \pi / 6 & 4 \pi / 3 & 3 \pi / 2 & 5 \pi / 3 & 11 \pi / & 2 \pi \\ 6\end{array}\right]$


Fill in the questions below using Increases or Decreases

From 0 to $\mathrm{pi} / 2$ (quadrant I), $\cos \mathrm{x}$ $\qquad$ from 0 to 1 .

From pi/2 to pi (quadrant II), $\cos x$ $\qquad$ from 1 to 0 .

From pi to 3pi/2 (quadrant III), $\cos x$ $\qquad$ from 0 to - 1 .

From 3pi/2 to 2pi (quadrant IV), $\cos x$ $\qquad$ from -1 to 0 .

## Investigation of Amplitude

The basic Sine and Cosine graphs can be manipulated by changing $a$ and $b$ in the equations below:

## $Y=a \operatorname{Sin} b x$ and $y=a \operatorname{Cos} b x$

Use your Graphing Calculator to find out what the "a" does to the graph:
STEP 1: Graph $y=\sin x$ (in this case $a=1$ )

- Change your window. Your $x$-min should be $0, x$-max should be $2 \pi, y$-min should be $-5, y$-max should be 5 .
- Go to $y=$ and input $\operatorname{Sin} x$
- Hit GRAPH

STEP 2: Investigate the graph of $y=\sin x$

- What is the maximum value of the graph? $\qquad$
- What is the minimum value of the graph? $\qquad$
- When does the graph hit the $x$-axis (in terms of $\pi$ )? $\qquad$
STEP 3: Graph $y=2 \sin x \quad(a=2)$
- What is the maximum value of the graph? $\qquad$
- What is the minimum value of the graph? $\qquad$
- When does the graph hit the $x$-axis (in terms of $\pi$ )? $\qquad$
STEP 4: Graph $y=3 \sin x \quad(a=3)$
- What is the maximum value of the graph? $\qquad$
- What is the minimum value of the graph? $\qquad$
- When does the graph hit the $x$-axis (in terms of $\pi$ )? $\qquad$

STEP 5: Make a conjecture (best guess) about the effect of "a" on the graph of the equation $y=a \sin x$

STEP 6: Test your guess by predicting the maximum and minimum values for the graphs below:

- $Y=1 / 2 \sin x$

Max: $\qquad$

Min: $\qquad$

$$
y=4 \sin x
$$

Max: $\qquad$

Min: $\qquad$

STEP 7: Think about what would happen if "a" was negative.

- Graph $y=-\sin x$
- Graph $y=-2 \sin x$
- What happens? $\qquad$

STEP 8: Make a sketch.

- Sketch all of the graphs above and label them.


- What Equations are "missing" if you wanted to "complete" the picture?

1. $\qquad$
2. $\qquad$
3. $\qquad$

## INVESTIGATION OF FREQUENCY

The basic Sine and Cosine graphs can be manipulated by changing $a$ and $b$ in the equations below:

$$
\mathbf{Y}=\mathbf{a} \operatorname{Sin} \mathbf{b x} \text { and } \mathbf{y}=\mathbf{a} \operatorname{Cos} \mathbf{b x}
$$

Use your Graphing Calculator to find out what the " $b$ " does to the graph:
STEP 1: Graph $y=\sin x$ (in this case $b=1$ )

- Your $x$-min should be $0, x$-max should be $2 \pi, y$-min should be $-5, y$-max should be 5.
- Go to $y=$ and input $\operatorname{Sin} x$
- Hit GRAPH
- Sketch the basic sin curve from $0-2 \pi$ :

STEP 2: Graph $y=\sin 2 x$

- How many sin curves do you see?

STEP 3: Graph $\mathrm{y}=\sin 3 \mathrm{x}$

- How many sin curves do you see?

STEP 4: Make a Conjecture (best guess) as to what effect " $b$ " has on the graph:

STEP 5: Testing your conjecture

- Sketch what you think $y=\sin (1 / 2) x$ will look like:
- Now graph $\mathrm{y}=\sin (1 / 2) \mathrm{x}$ in your graphing calculator. Were you right?

STEP 6: Sketching more graphs

- Sketch $\mathrm{y}=\sin 4 \mathrm{x}$ :


## THE PERIOD OF A GRAPH

Based on what we've learned we know that

- "a" is for $\qquad$ and determines the $\qquad$ of the graph.
- "b" is for $\qquad$ and determines the number of curves
between $\qquad$ and $\qquad$
- The Period of a graph is $\qquad$ .
- To find the period of a graph use:
- To determine what interval to use on the $x$-axis:
1.) $y=3 \cos 1 / 2 x$

Amplitude:

Frequency:

Period:
x-interval:
3.) Sketch the graph of the curve $y=2 \cos 2 x$ :
4.) Sketch the graph of the curve $y=-\sin 1 / 2 x$ :

## GRAPHING TAN FUNCTION

Start out by making sure that your mode is set to degrees.

Now set up your window as follows:
Xmin: $-2 \pi$
Xmax: $2 \pi$
Ymin: -3
Ymax: 3
1.) In the " $Y=$ " menu, type " $\operatorname{Tan}(x)$

To see the graph use the "graph" key.
2.) There will be several vertical lines on the graph. These lines are called $\qquad$
3.) At the asymptotes for the function $y=\tan (x)$ is $\qquad$
4.) What are the $x$ values for these asymptotes? $\qquad$
5.) What are the values for when $y=0$ ? $\qquad$
6.) What are the Max and min of the graph? $\qquad$
7.) Sketch the graph below:


