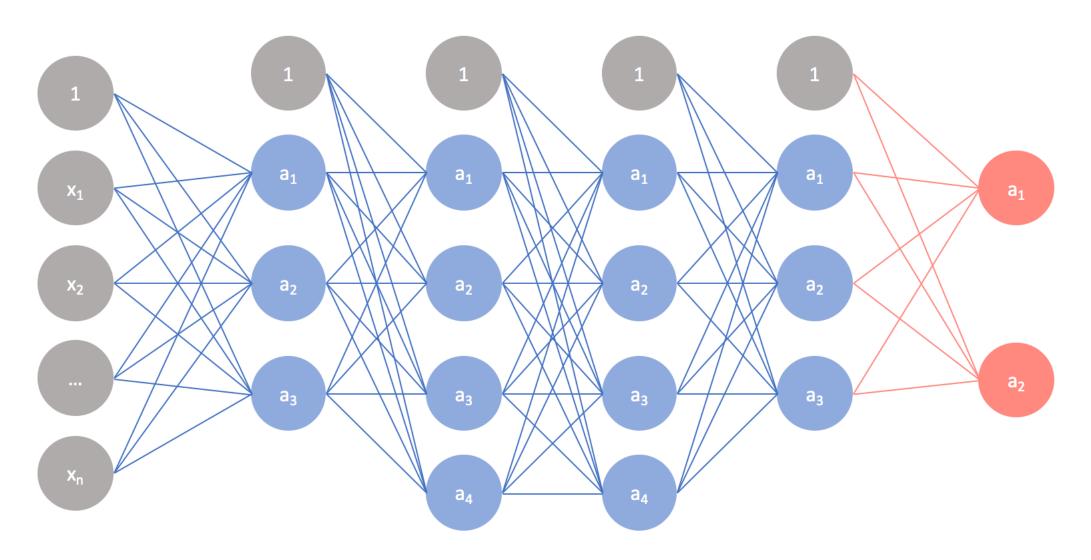
## **NN** basics



#### References

- http://cs231n.stanford.edu/index.html
- http://www.cs.cornell.edu/courses/cs5670/2019sp/lectures/lectures.html
- http://www.cs.cmu.edu/~16385/

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### What will we know to do?

- Hopefully by the end of the course:
- https://teachablemachine.withgoogle.com/

### What is a neural network

- Artificial neural networks (ANN / NN) are computing systems vaguely
  inspired by the biological neural networks that constitute animal brains. Such
  systems "learn" to perform tasks by considering examples, generally without
  being programmed with task-specific rules.
  - [Wikipedia]

### What does a NN needs?



### What a neural network can do?

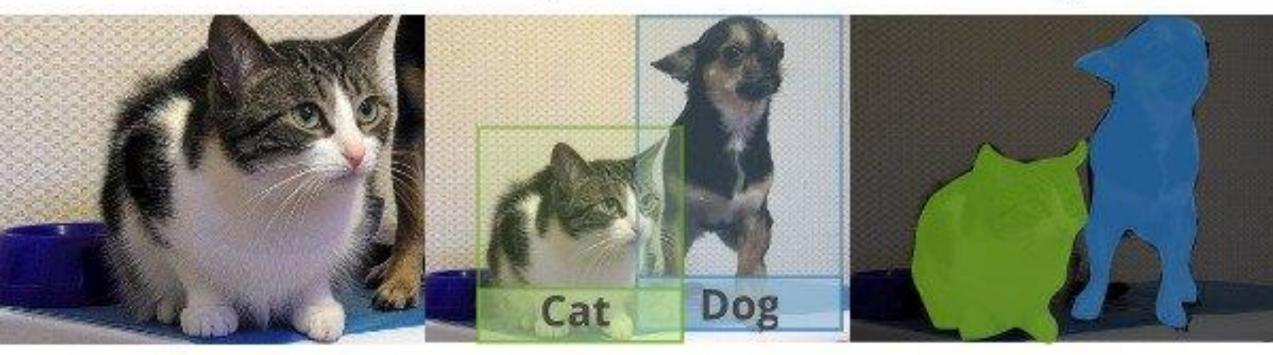
- Image based:
  - Object recognition
  - Human pose detection
  - 3D reconstruction from a signal image
  - Image captioning
  - Style transfer
- Non image based:
  - Language translation
  - Game playing
- And much-much more...

## **Object recognition**

Classification

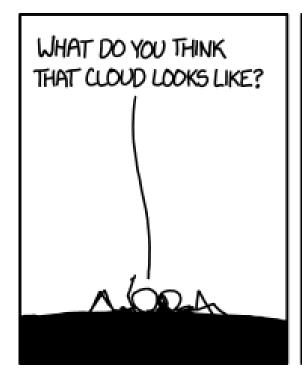
Object Detection

Semantic Segmentation

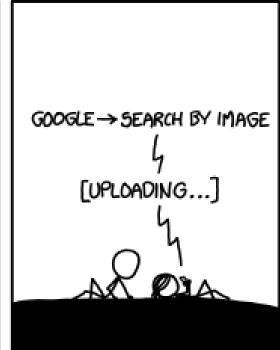


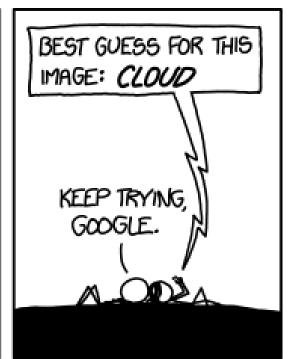
Cat

## **Object recognition**

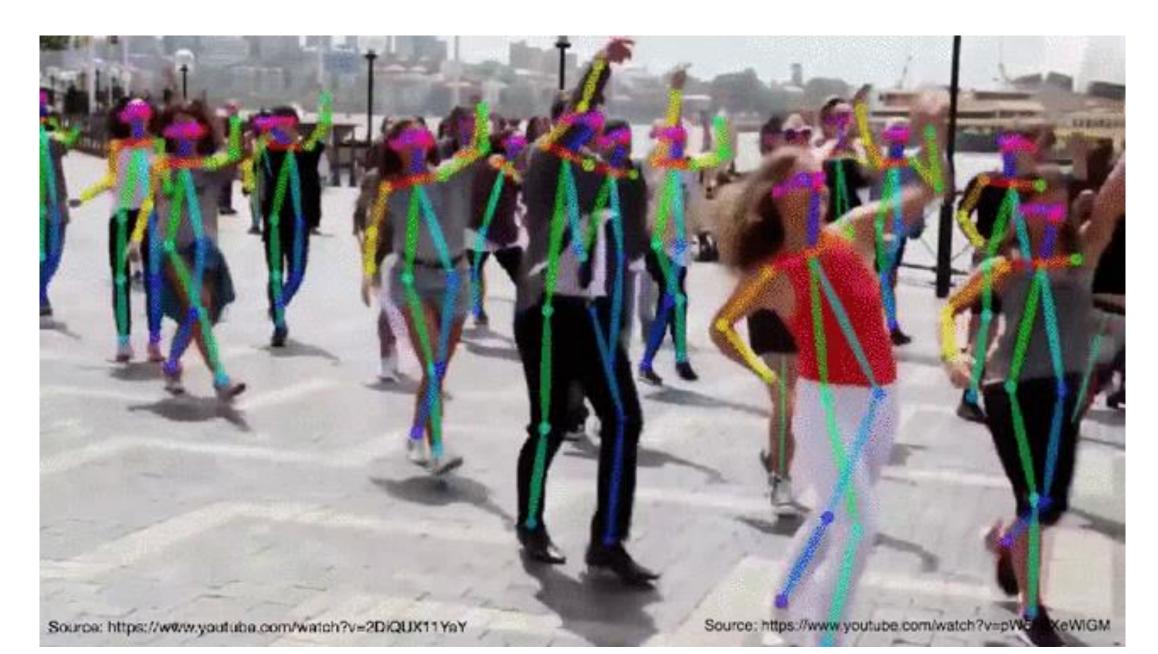








## **Human pose detection**



## 3D reconstruction from a single image











## Image captioning



a little girl sitting on a bench holding an umbrella.



a herd of sheep grazing on a lush green hillside.



a close up of a fire hydrant on a sidewalk.



a yellow plate topped with meat and broccoli.



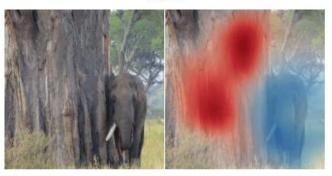
a zebra standing next to a zebra in a dirt field.



a stainless steel oven in a kitchen with wood cabinets.



two birds sitting on top of a tree branch.



an elephant standing next to rock wall.



a man riding a bike down a road next to a body of water.

# **Style transfer**







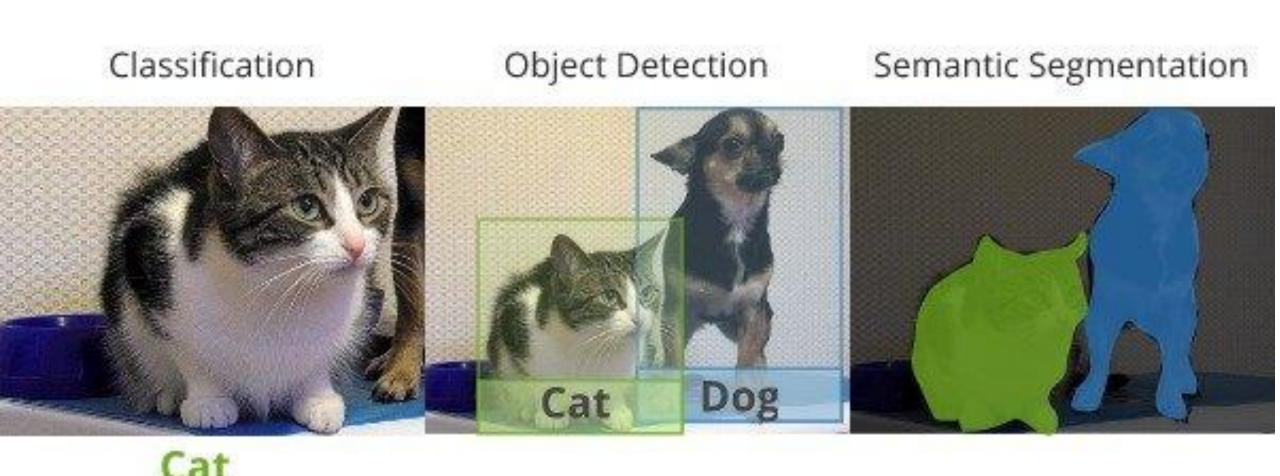




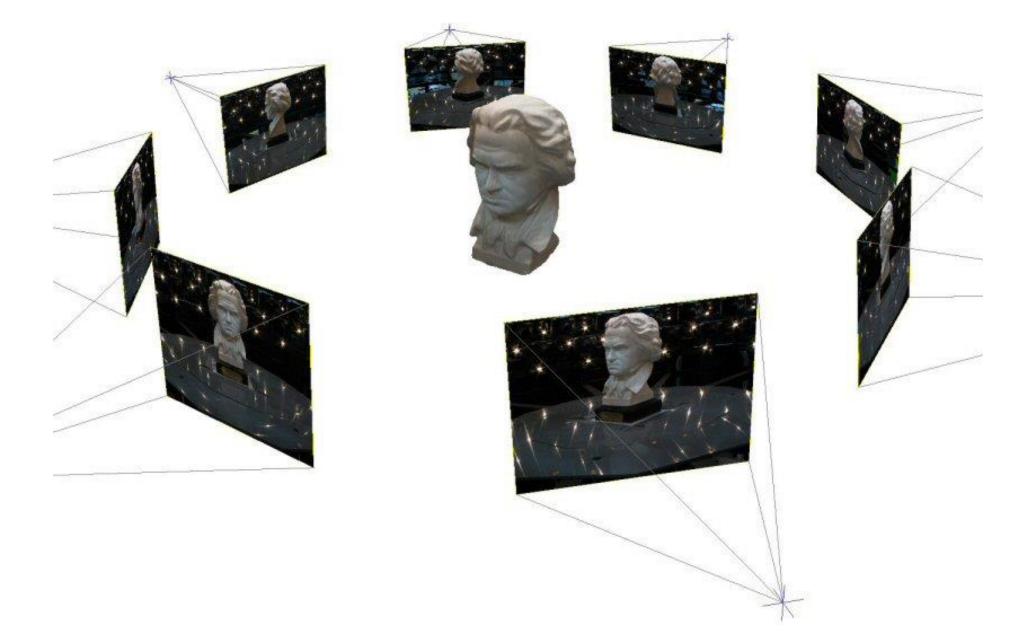


## Object recognition challenges

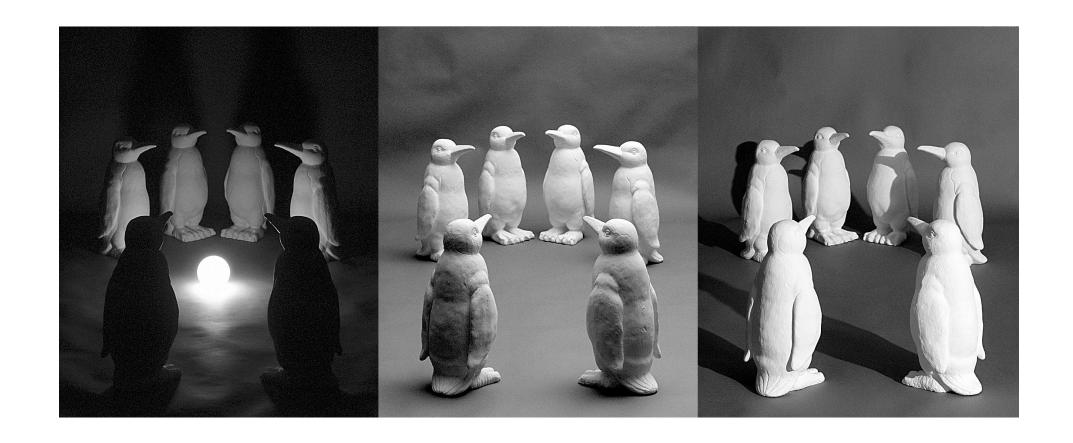
• As we've seen before- object recognition is hard!



# **Challenge: variable viewpoint**



## **Challenge: variable illumination**

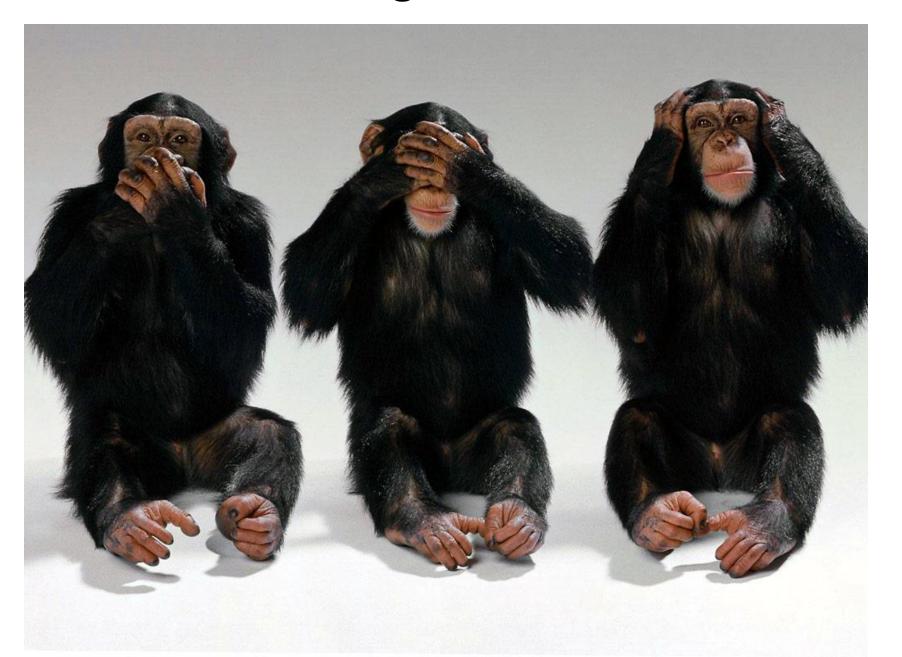


and small things Challenge: scale from Apple. (Actual size)

## **Challenge: deformation**



# **Challenge: occlusion**



## **Challenge: background clutter**



## **Challenge: intra-class variations**



## Object recognition challenges

- We've already seen that this is a hard problem to tackle with "classic" CV algorithms like SIFT and template matching.
  - Template matching does a relatively good job to find the same template instance in an image.
  - SIFT can extend this to find the instance with changing viewpoint/scale/illumination and rotation.
- What happens when want to find similar object that are not the same?
  - NN for the win!

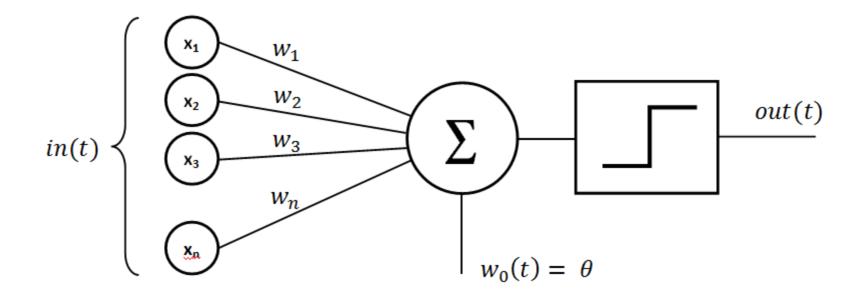


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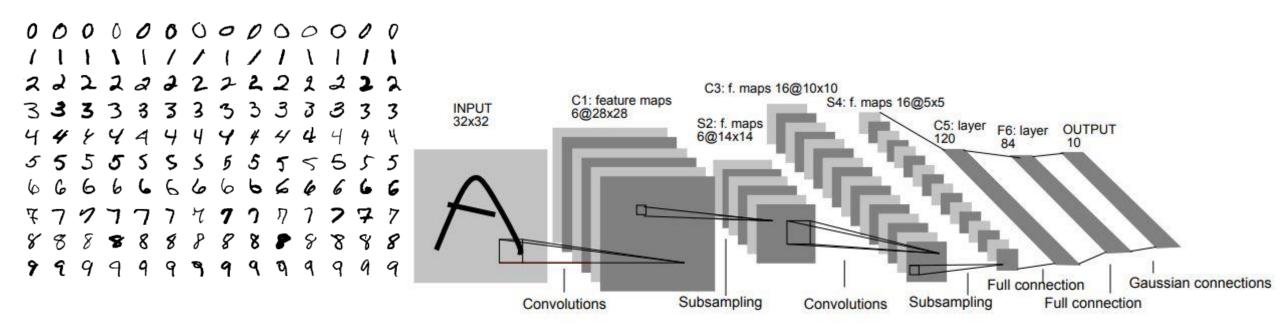
### perceptron

- The basic building block of all NN.
- First introduced in 1958 at Cornell Aeronautical Laboratory by Frank Rosenblatt.
- We will talk more about it in a moment...



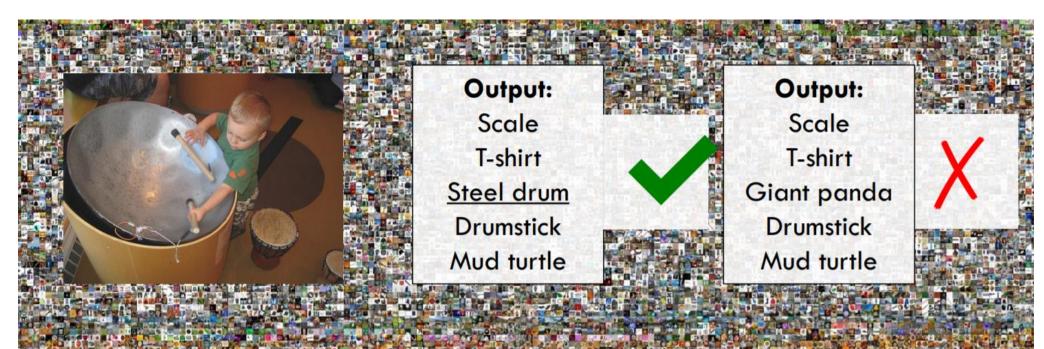
#### MNIST + LeNet-5

- MNIST is a large dataset of handwritten digits used in training of LeNet-5.
- LeNet-5 is the first known NN to solve a major computer vision problem:
  - Classifies digits, was applied by several banks to recognize hand-written numbers on checks.
  - Used 7 trainable layers with a total of 60K params (sounds a lot?).
  - Yann LeCun at el., 1998, 23000 citations.

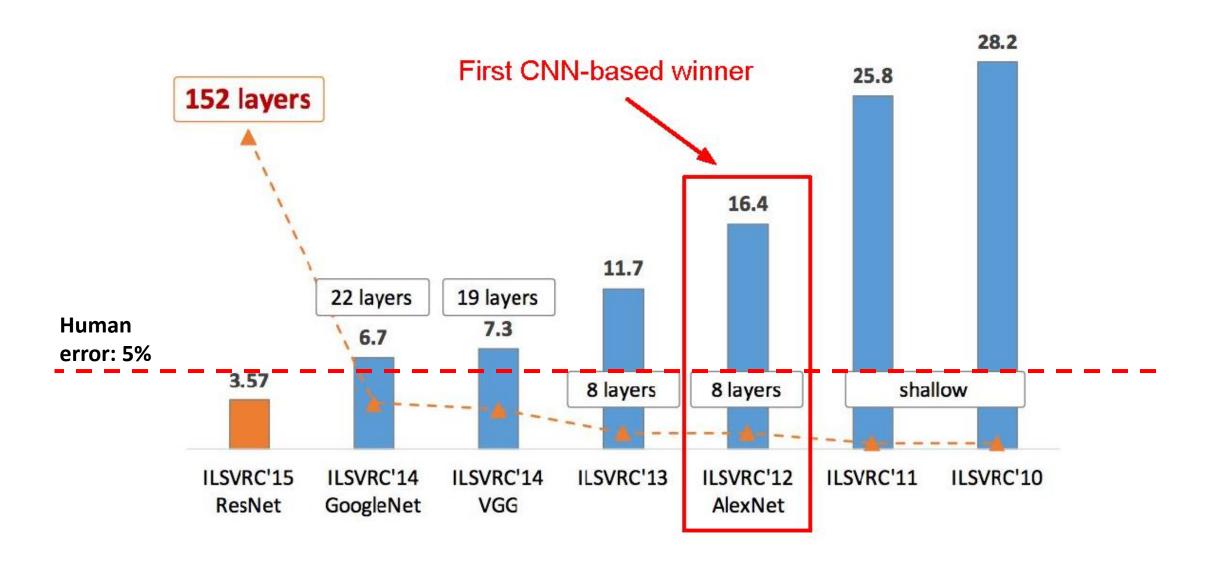


## IMAGENET Large Scale Visual Recognition Challenge (ILSVRC)

- ImageNet is an image database most known for its ILSVRC challenge, and specifically for the image classification contest:
  - 1000 object classes
  - 1,431,167 images
  - Winner has the minimum mean labeling error out of 5 gausses for a given unknown test set.



### **ILSVRC** winners

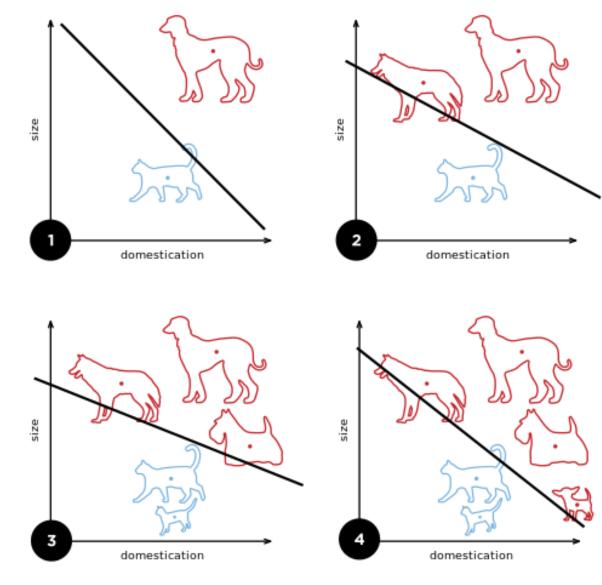


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### **Perceptron**

- the perceptron is an algorithm for supervised learning of binary classifiers.
  - The perceptron determines a hyperplane separator which is determined by a set of weights (W).
  - A feature vector is the representation of the object to be classified which the perceptron receives as input (x).
- The weights (W) determine the separator are what we need to learn in order to optimize the classification.



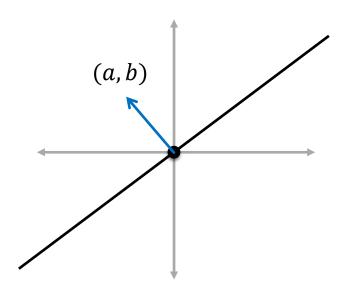
• Paramtrization of a line in 2D:

$$ax + by + c = 0$$

- if c = 0:

$$ax + by = 0 \leftrightarrow (a,b) \cdot (x,y) = 0 \leftrightarrow (a,b) \perp (x,y)$$

• (a, b) defines the normal to the line



Paramtrization of a line in 2D:

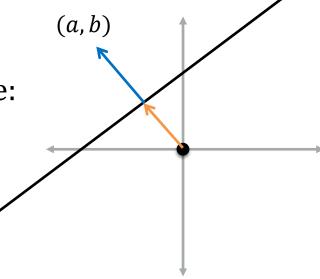
$$ax + by + c = 0$$

- if c = 0:

$$ax + by = 0 \leftrightarrow (a,b) \cdot (x,y) = 0 \leftrightarrow (a,b) \perp (x,y)$$

- (a, b) defines the normal to the line
- $if c \neq 0$ :
  - This is the **bias** factor.
  - Defines the distance of (0,0) from the line:
    - Point-line distance:  $d = \frac{|ax+by+c|}{\sqrt{a^2+b^2}}$

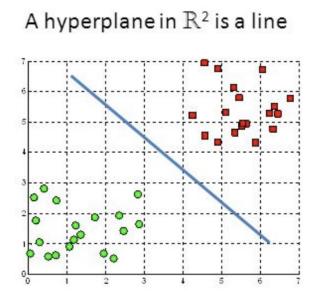
$$-bias = \frac{|c|}{\sqrt{a^2 + b^2}}$$

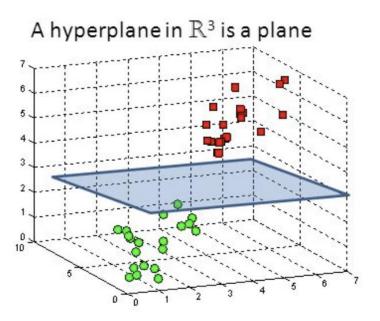


• This is the same for 3D representation of a plane as well:

$$ax + by + cz + d = 0$$

- (a, b, c) defines the normal to the plane, d defines the bias of the plane from (0,0,0).
- And the same representation can be done for ND space. The ND plane is called a hyperplane.





 Writing the hyperplane representation vector vise will result the equation below:

$$[w_1 \cdots w_n] \begin{bmatrix} x_1 \\ \vdots \\ x_n \end{bmatrix} + b = w^T x + b = 0$$

• Points x above the hyperplane (in the direction of the normal) will result in  $w^Tx + b > 0$ , and points x below the hyperplane will result in  $w^Tx + b < 0$ .

 Another option is to write the hyperplane representation with homogenous vectors, this will result with the (more compact) equation below:

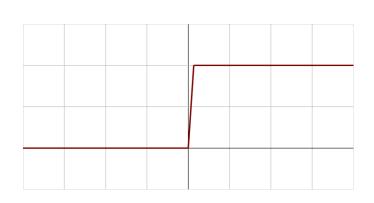
$$\begin{bmatrix} w_1 & \cdots & w_n & b \end{bmatrix} \begin{bmatrix} x_1 \\ \vdots \\ x_n \\ 1 \end{bmatrix} = w^T x = 0$$

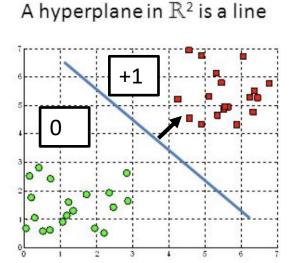
• Points x above the hyperplane (in the direction of the normal) will result in  $w^T x > 0$ , and points x below the hyperplane will result in  $w^T x < 0$ .

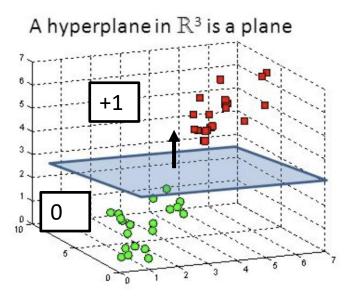
### **Activation function**

- A non-linear function f() that appends the perceptron's hyperplane equation y = f(Wx).
- If we have a problem of classifying two groups with a single hyperplane, we can use a step activation function:

$$f(x) = step(x) = \begin{cases} 0, & x < 0 \\ 1, & x \ge 0 \end{cases}$$





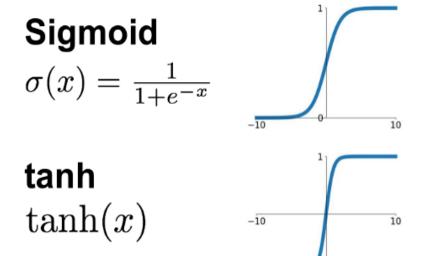


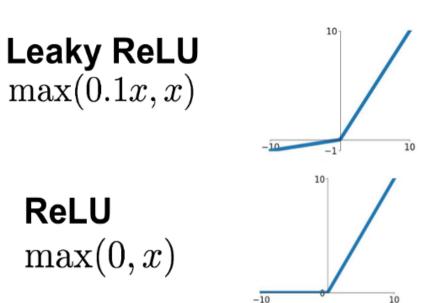
#### **Activation function**

- Later we will use more common activation functions.
- One of them is the rectified linear unit (ReLU) function:

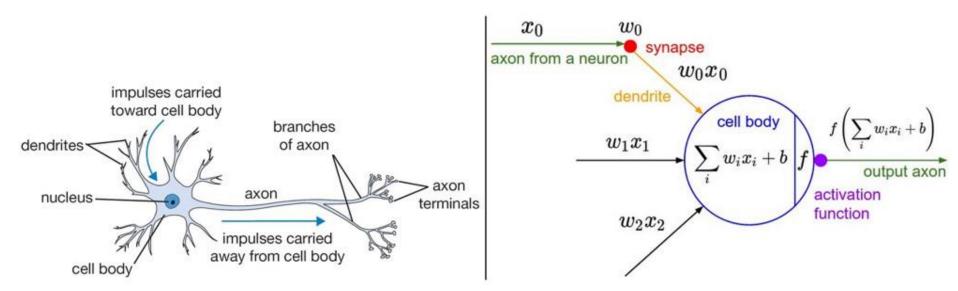
$$f(x) = \max(x, 0) = \begin{cases} 0, & x < 0 \\ x, & x \ge 0 \end{cases}$$

Other known activation functions: sigmoid, tanh, leaky ReLU.





# perceptron: Inspiration from Biology

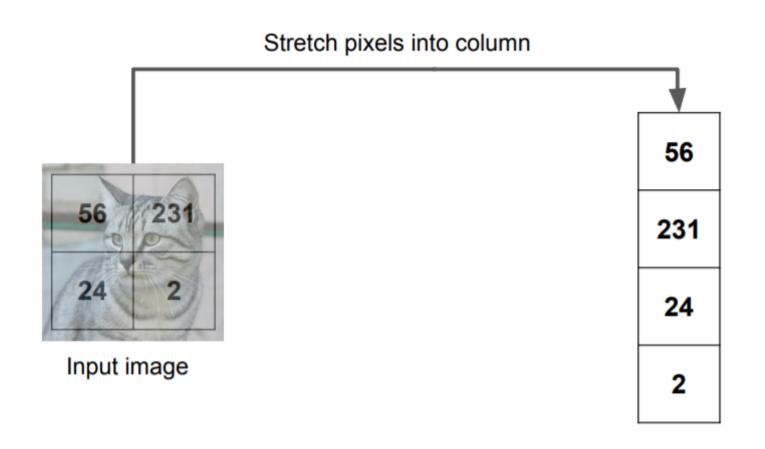


A cartoon drawing of a biological neuron (left) and its mathematical model (right).

- Neural nets/perceptrons are loosely inspired by biology.
- But they certainly are not a proper model of how the brain works, or even how neurons work.

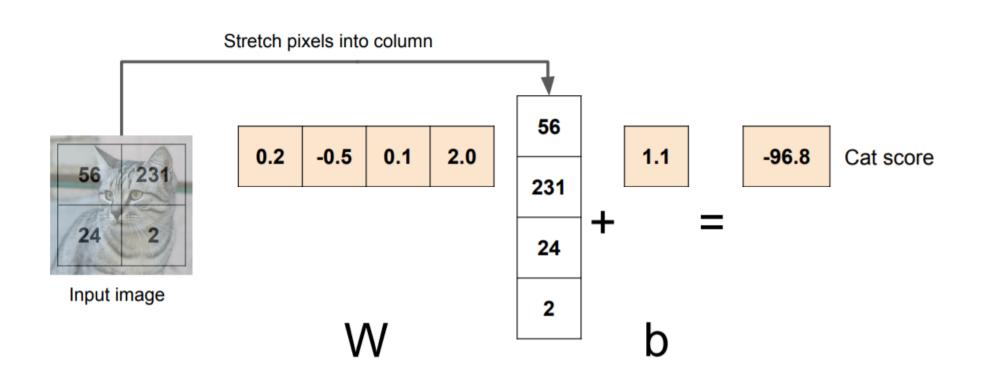
# **Images as inputs**

• In images, the pixels can be the input feature vector.



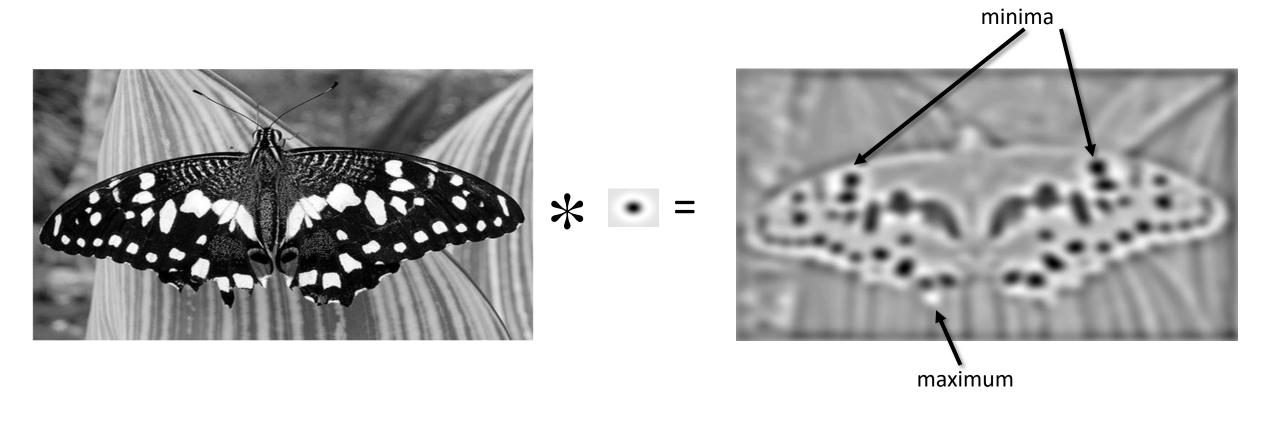
#### **Images as inputs**

• We want to find a hyperplane in 4D space that puts all cats' vectors in one side of it, and all other images in the other side.



#### Perceptron: template matching interpretation

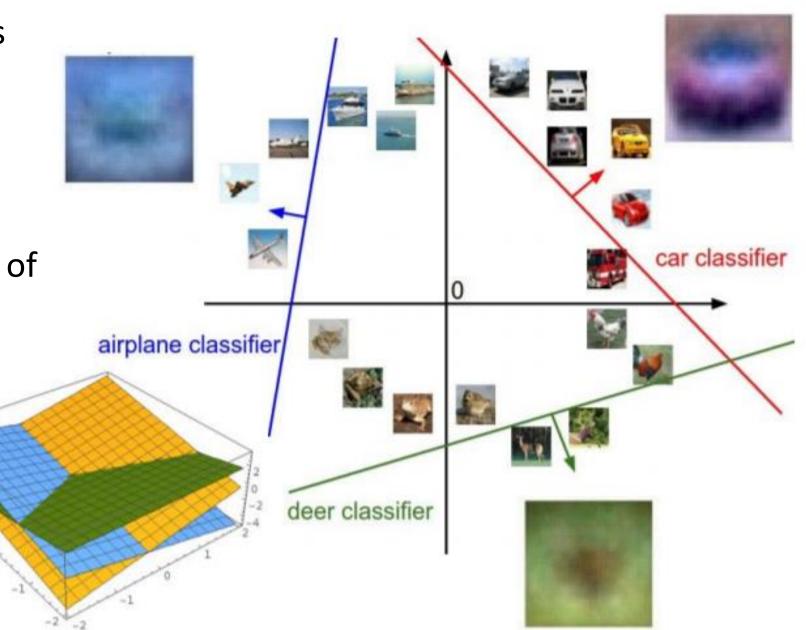
- We can think about the optimized weights as a template in template matching cross correlation algorithm.
  - We get a strong positive response when the template matches the image area.



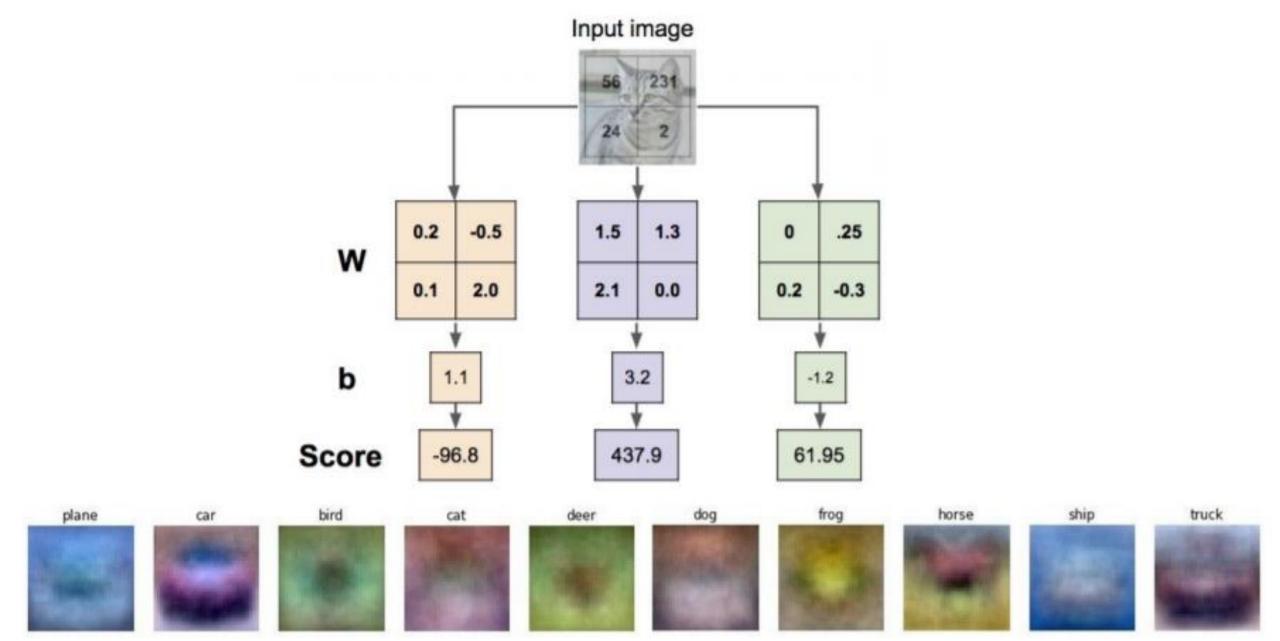
#### Perceptron: template matching interpretation

• In our case the template is the size of the image.

 We can see examples of templates for different groups- the optimized template can bee thought of as the mean of the class.



### Perceptron: template matching interpretation

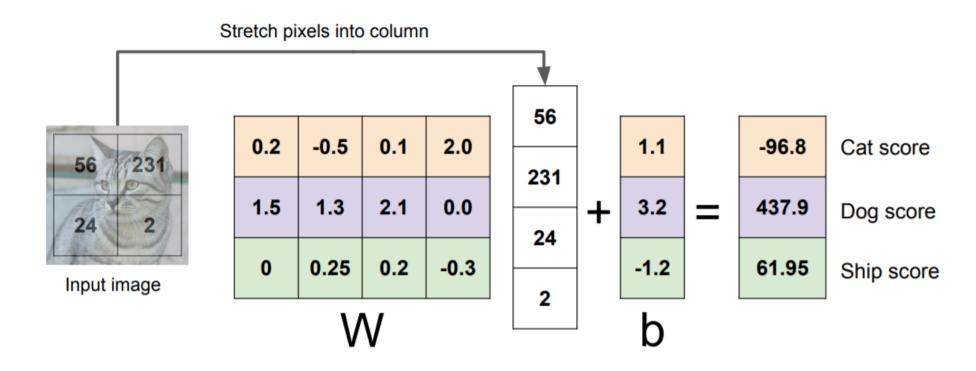


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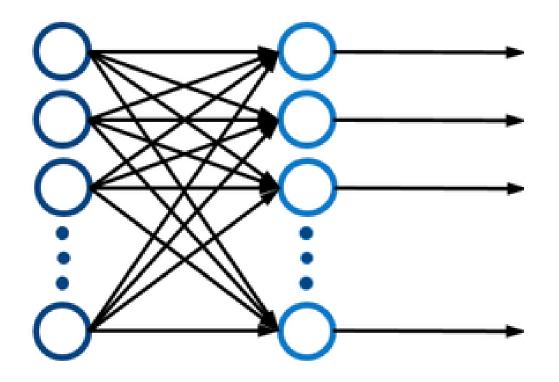
#### Hyperplanes and image classification

- We want to find a hyperplane in 4D space that puts all cats' vectors in one side of it, and all other images in the other side.
- Let's assume there are 2 more classes. In total: cats, dogs and ships. Now, W is a matrix rather than a vector
  - Find 3 separating planes, one for each class.



#### **Dense layer**

- This is the first NN layer we encounter- all inputs are going through multiple perceptrons at the same time.
- This layer is called dense layer or fully-connected layer.



# **Dense layer**

• Sometimes you can see W and b concatenated like this:

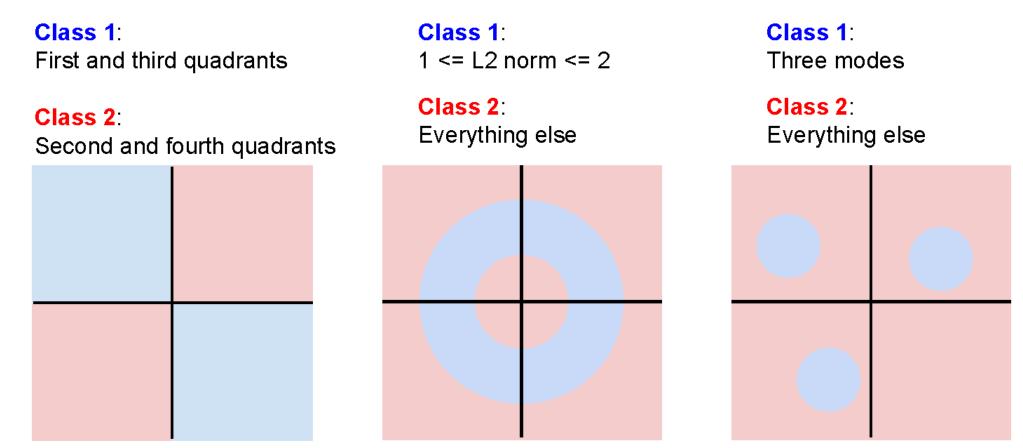
															_	$x_i$
					x	į				new, single W						1
W								b	l	W = b						2
	0	0.25	0.2	-0.3	24			-1.2		0	0.25	0.2	-0.3	-1.2		24
	1.5	1.3	2.1	0.0	23	1	+	3.2		1.5	1.3	2.1	0.0	3.2		231
	0.2	-0.5	0.1	2.0	56	5		1.1		0.2	-0.5	0.1	2.0	1.1		56

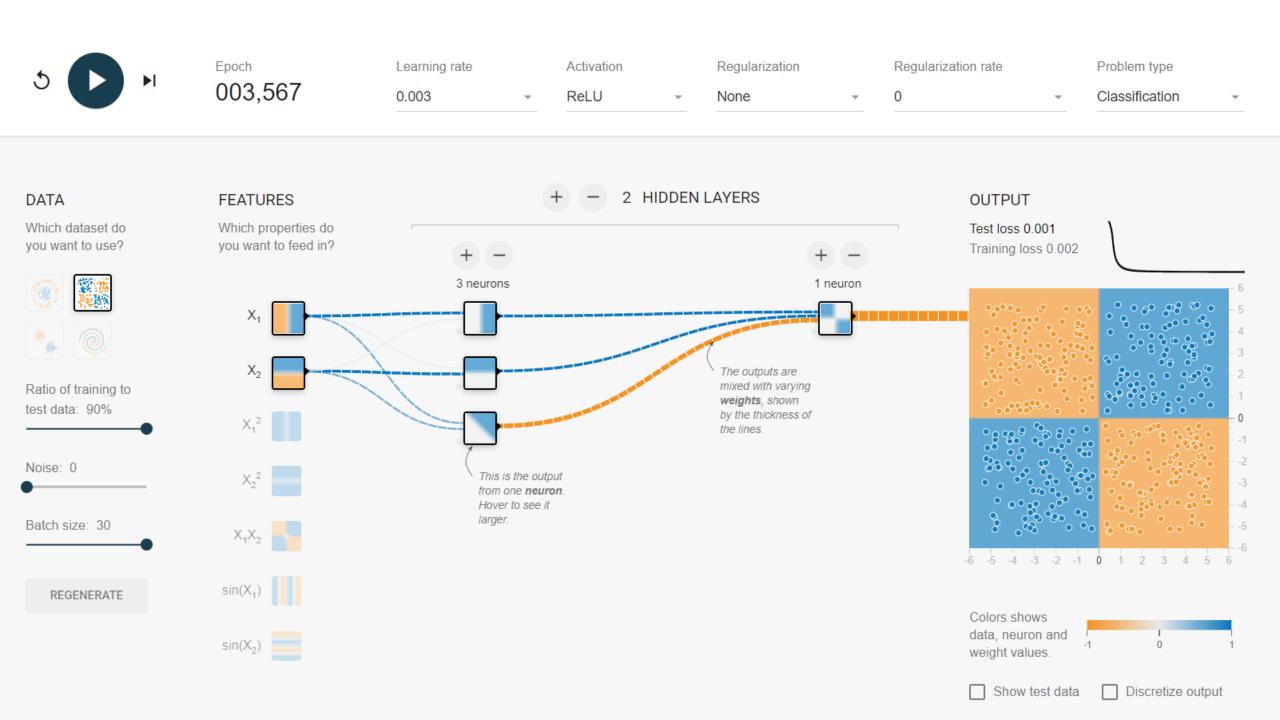
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### Multi-layer perceptron

- Perceptron plane separation is not enough for all data sets- some are not linearly separable.
- multi-layer perceptron (MLP), or in a more common name- **neural network**, is a better approach to try to handle this data.





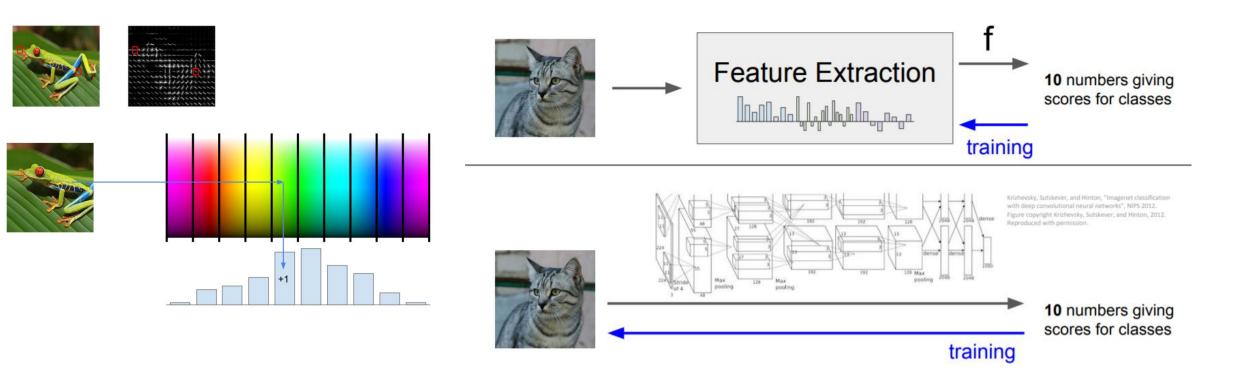
## Multi-layer NN: intuition

- We can use the data of **all** the responses to all "templates" of weights from the first layer to better represent the result.
- In this way, instead of one best fit for a template, we can use all the responses to all templates of the first layer to learn a better classification.
- This is also correct for any number of layers in an NN.

(**Before**) Linear score function: 
$$f=Wx$$
 (**Now**) 2-layer Neural Network  $f=W_2\max(0,W_1x)$  or 3-layer Neural Network  $f=W_3\max(0,W_2\max(0,W_1x))$ 

## Multi-layer NN: intuition

- Before: human "hand engineered" features as input into a machine learning (ML) framework.
  - Examples of features we've seen: SIFT, HOG, color histograms.
- Now: the NN finds best features.



#### **CIFAR10** dataset

- CIFAR10 (Canadian Institute For Advanced Research) is a known dataset of 10 classes of small images.
- 32X32X3=3072 DOFs in this problem, and images vary a lot. This is not possible to linearly separate.

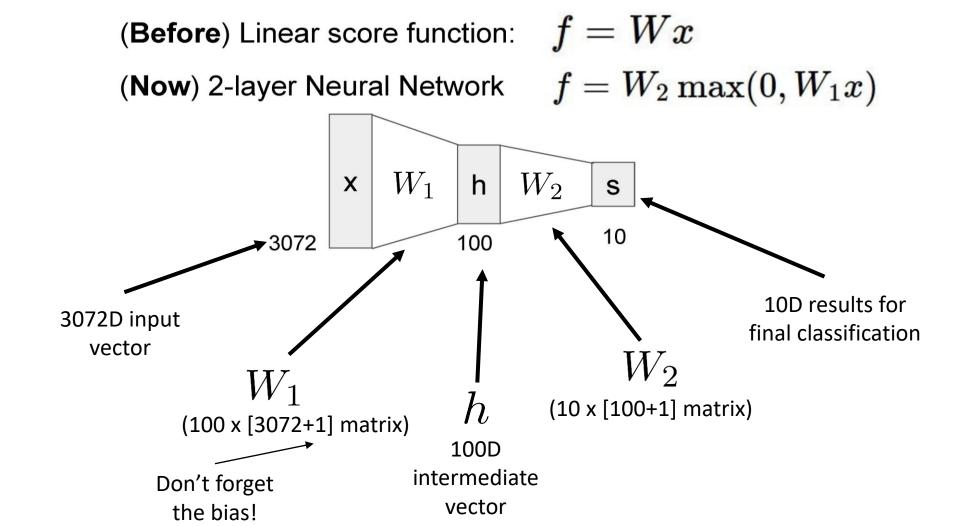


10 classes

50,000 training images each image is 32x32x3

10,000 test images.

• 2-layer NN example: Learned 100 different templates in the first layer and input them into a second layer for final classification.

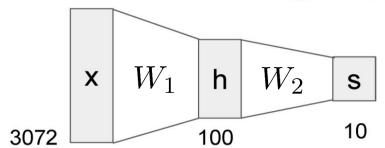


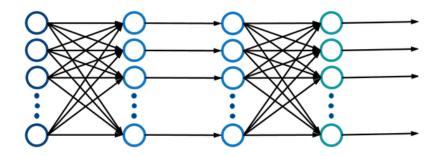
Total number of weights to learn:

$$[3,072+1] \times 100 + [100+1] \times 10 = 308,310$$

(**Before**) Linear score function: f=Wx

(Now) 2-layer Neural Network  $f = W_2 \max(0, W_1 x)$ 





What happens if we remove the non-linear activation?

$$f = W_2 \max(0, W_1 x)$$

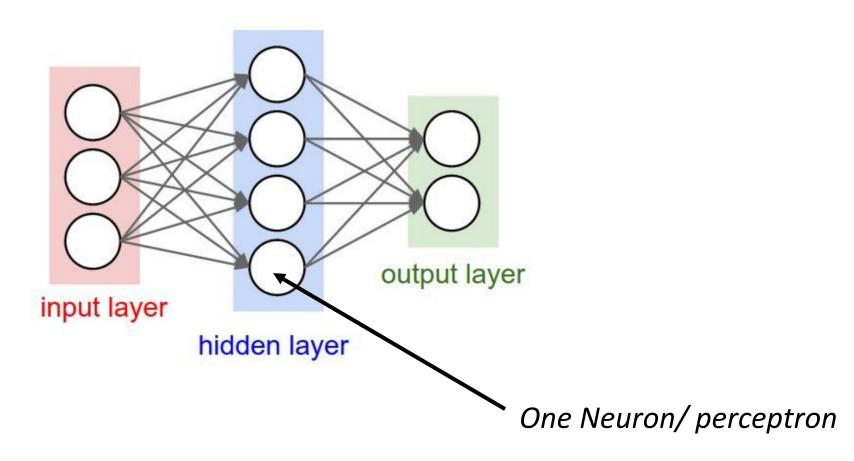
What happens if we remove the non-linear activation?

$$f = W_2 \max(0, W_1 x) \rightarrow W_2 W_1 x = \widetilde{W} x$$

- We've gotten a linear separator again... not good.
- Remember the activation function!

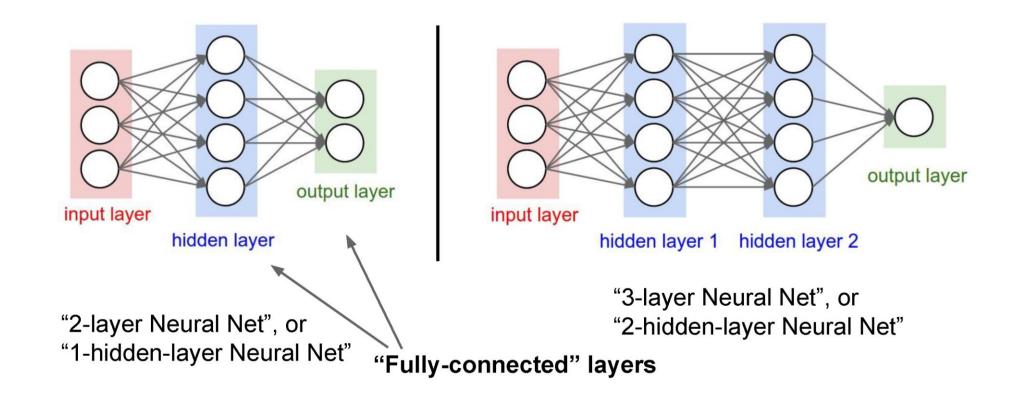
#### **Neural network architecture**

- Computation graph for a 2-layer neural network.
  - Only count layers with tunable weights (so don't count the input layer).
  - Each layer is built from perceptrons: weights + bias + activation function.



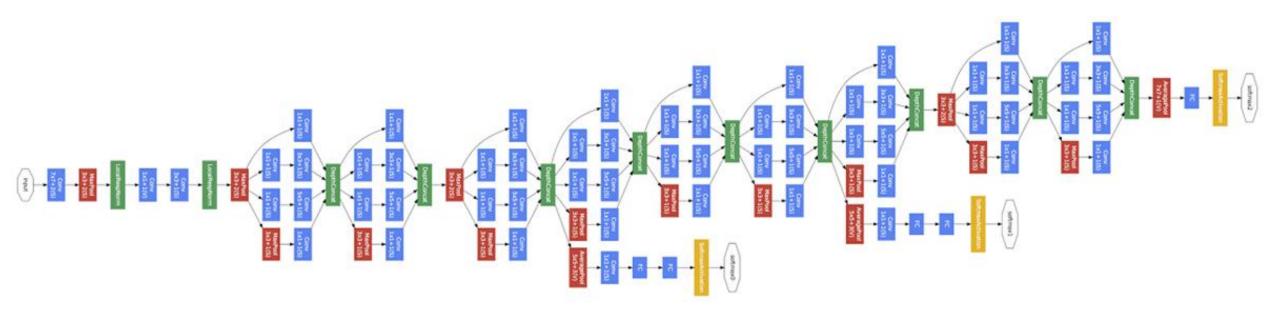
#### **Neural network architecture**

- Deep networks typically have many layers and potentially millions of parameters.
- Fully connected layer is a layer in which all inputs are multiplied for each perceptron with different weights. (this is what we saw until now).



#### **Neural network architecture**

- Example of a deep NN: Inception network (GoogLeNet, Szegedy et al, 2015)
- 22 layers



## A good fully connected example

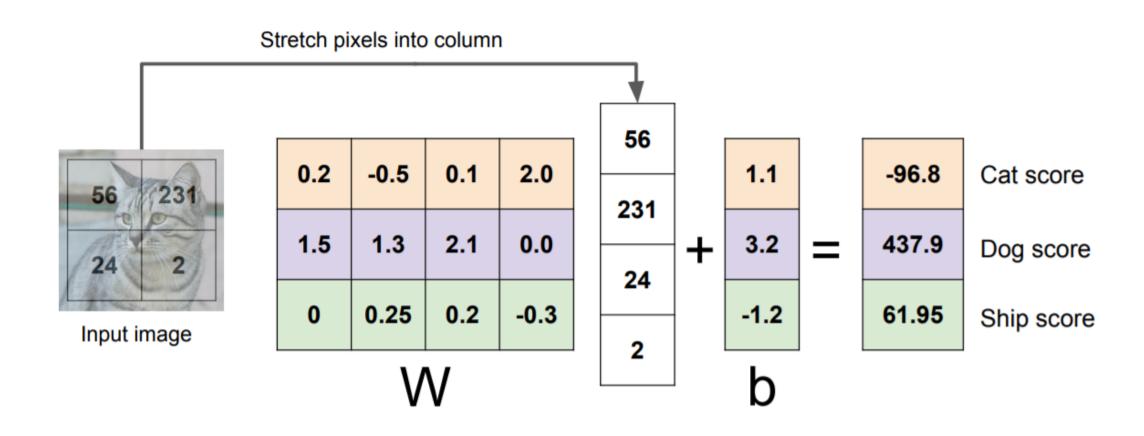
 https://playground.tensorflow.org/#activation=tanh&batchSize=10&dataset= spiral&regDataset=regplane&learningRate=0.03&regularizationRate=0&noise=0&networkShape=8,8 ,8&seed=0.68609&showTestData=false&discretize=false&percTrainData=50& x=true&y=true&xTimesY=true&xSquared=true&ySquared=true&cosX=false&s inX=true&cosY=false&sinY=true&collectStats=false&problem=classification&i nitZero=false&hideText=false

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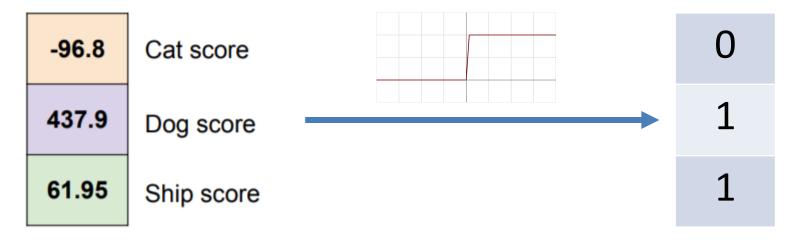
#### Optimizing the weights

- We have this results for each possible label.
- which is the best result currently? Which should be the best result?



### Optimizing the weights- first try

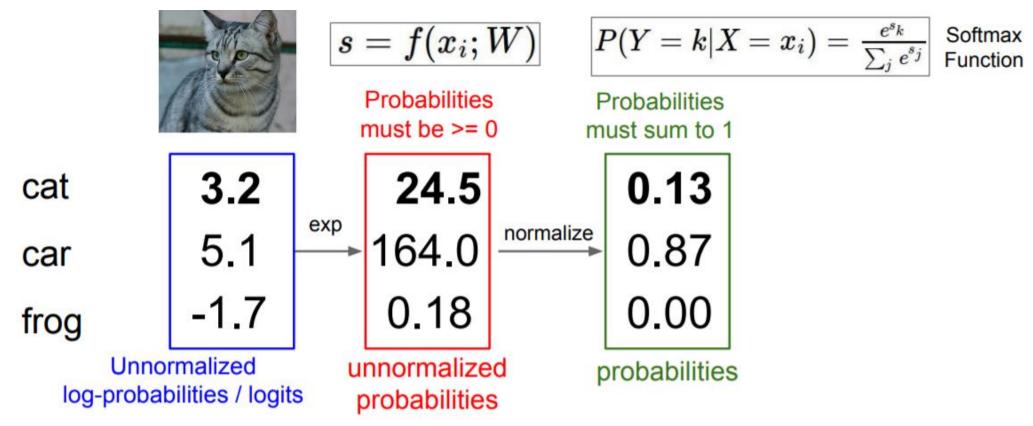
- We have this results for each possible label.
- which is the best result currently? Which should be the best result?
  - Let's use our step activation function from before.



- Can't tell us which class is better... not good enough.
  - We need a way to quantify the results as more/less likely.

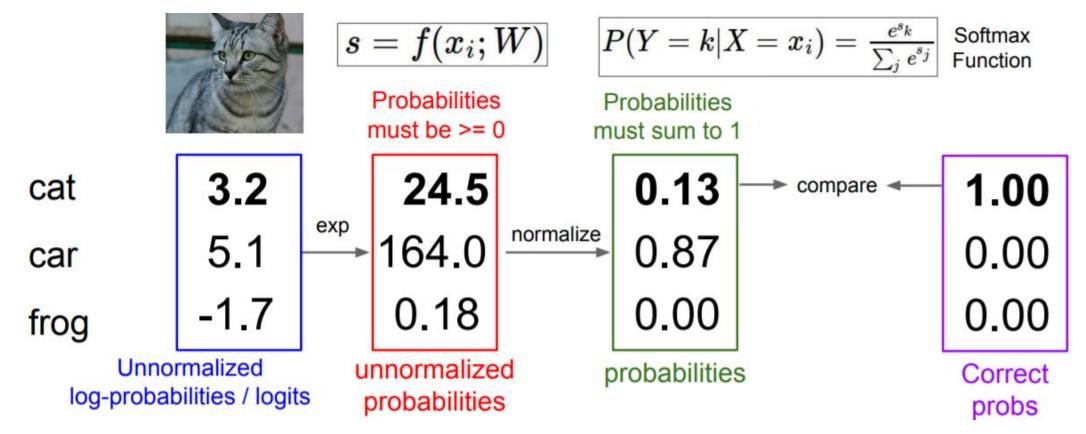
### Softmax layer

- The softmax layer normalizes all the results so that you get a percentage of correctness for each label and in use with the classification problem.
- The softmax is usually added as the last layer in a NN to normalize the results instead of an activation function.



#### **Cross entropy loss function**

- Only during training time, we need to define an error of the given probabilities and the correct (wanted) probabilities.
- A known loss function for the classification problem is called cross entropy loss.



# **Cross entropy loss + softmax**

 Cross entropy is a way to measure "distance" between the wanted distribution of results p and given distribution of results q:

$$L_{i} = -\sum_{j \in labels} p(j) \log q(j)$$

$$\begin{cases} p(j) = 1 \text{ if } j = y_{i} \text{ (right label)} \\ p(j) = 0 \ \forall \ j \neq y_{i} \end{cases}$$

$$L_{i} = -\log q(y_{i})$$

$$\frac{\text{plug in with softmax classifier}}{L_{i} = -\log(\frac{e^{sy_{i}}}{\sum_{j} e^{s_{j}}})}$$

#### **Total loss**

- This  $L_i$  is the loss of a single **given** input image  $x_i$ .
- Let's say we have all possible images in the world, so the total loss will be:

$$L = \frac{1}{N} \sum_{i=1}^{N} L_i$$

- A mean of all possible losses, where N is number of images.
- We want to find the best W that minimizes L.
- How do we do this?

#### **Total loss**

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- A mean of all possible losses, where N is number of images.
- We want to find the best W that minimizes L.
- How do we do this?
  - − Derive over W:  $\nabla_W L$

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### Finding the best W

- How do we do this?
  - − Derive over W:  $\nabla_W L$
- Problems:
  - We don't have all images, and even if we do, it will take forever...
  - No one said L is a convex function.
  - It's sometimes hard to compute the analytic derivative of the function L in order to naively find all extremum points.
- An approximate solution to find best W is called **mini-batch gradient descent.**

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#### Mini-batch

 In mini-batch gradient descent we take only a small subset of images and compute their average loss:

$$\tilde{L} = \frac{1}{\tilde{N}} \sum_{i=1}^{\tilde{N}} L_i$$

- A mean of the subset losses, where  $\widetilde{N}$  is the size of images subset.
- This approximation of the loss function is **faster to compute but less** accurate.

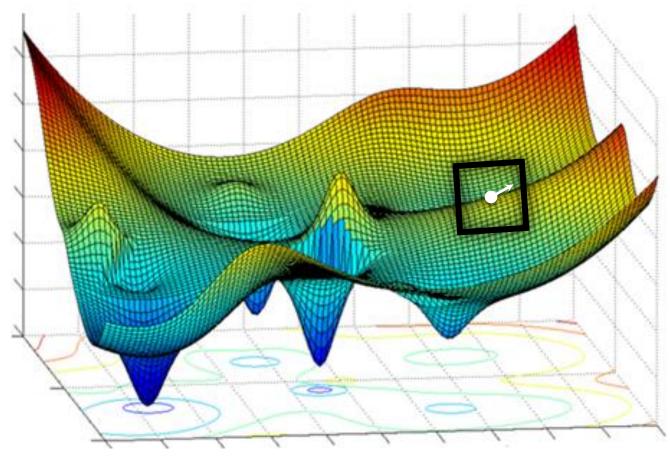
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# What is a gradient?

- describes the direction and magnitude of the fastest increase around a point  $\boldsymbol{x}$ .
- Example: gradient of a function of 2 variables:

$$\frac{\partial f(\boldsymbol{x})}{\partial \boldsymbol{x}} = \left[ \frac{\partial f(\boldsymbol{x})}{\partial x}, \frac{\partial f(\boldsymbol{x})}{\partial y} \right]$$

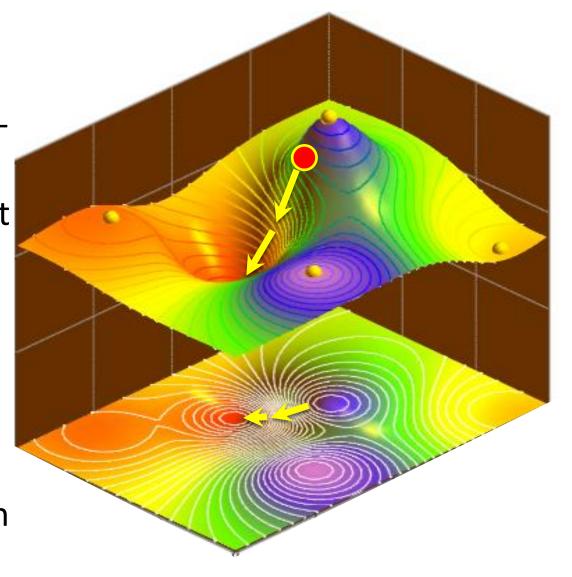


#### **Gradient descent**

- An iterative algorithm for finding local minima of functions.
- starts at a random point and moves stepby-step in the direction and proportional magnitude of the negative of the gradient of the point he is currently in:

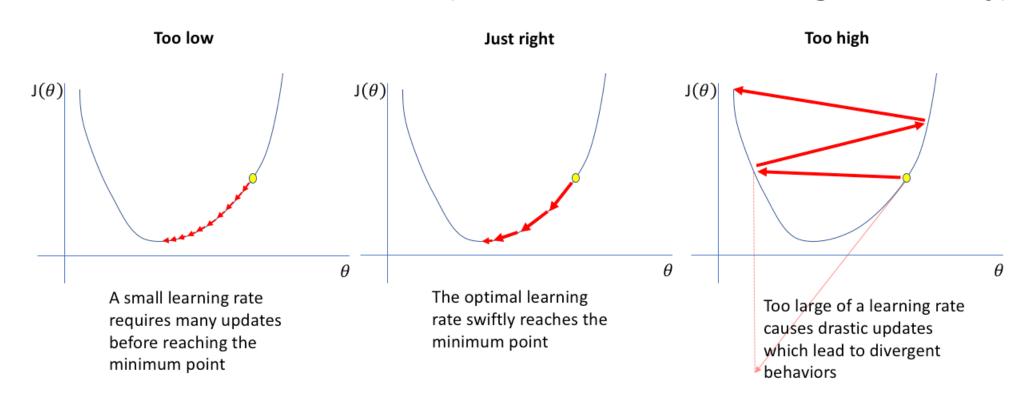
$$\boldsymbol{x}_{n+1} = \boldsymbol{x}_n - \eta \cdot \nabla f(\boldsymbol{x}_n)$$

- "proportional magnitude" == step size  $\eta$ .
- In "proper use" this algorithm converges to a local minimum which is depended on the starting point.



## **Gradient descent- step size**

- Also known as learning rate.
- This is known as a **hyperparameter**: an unknown variable that is configured by the user (unlike the weights W which the system "learns").
- The learning rate can change over time- after several steps you can make the step size smaller for finer results (this is known as **learning rate decay**).



# **Examples of learning rates**

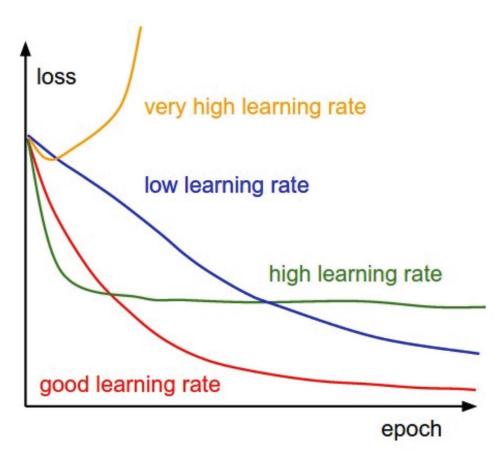


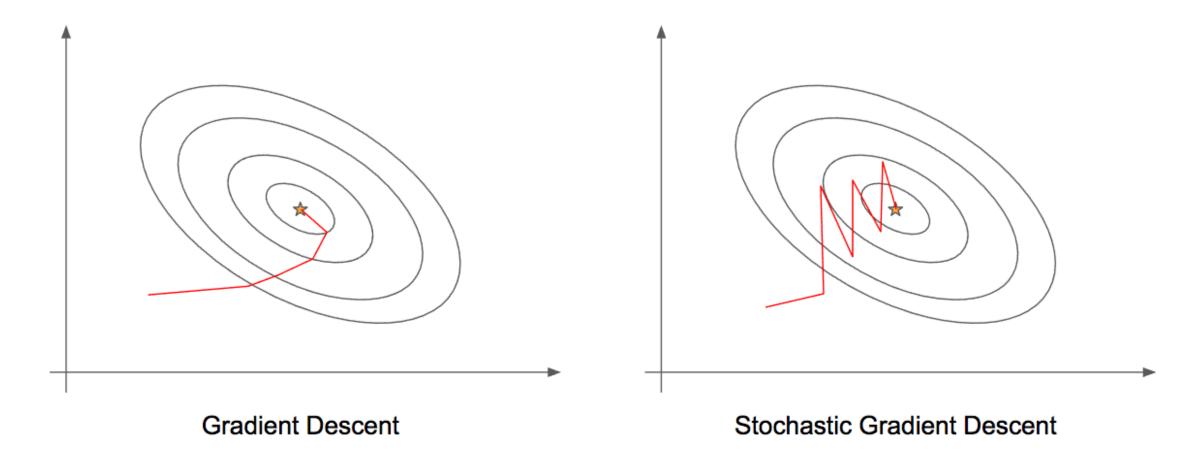
Figure: Andrej Karpathy

#### **Gradient descent- local minima**

- An iterative algorithm for finding local minima of functions.
- we can initiate this procedure several times from several random staring points and take the minimum of all output minimum points- this way we can get a better result.

## Mini-batch gradient descent

- Combining the two methods is called Mini-batch gradient descent.
- Almost always mis-called stochastic gradient descent (SGD)...
  - This is the name only if the batch size is 1.



## Loss noise

## **Typical training loss:**

Why is it varying so rapidly?

The width of the curve is related to the batchsize — if too noisy, increase the batch size

Possibly too linear (learning rate too small)

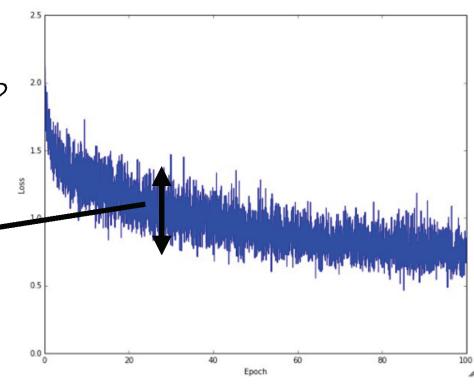


Figure: Andrej Karpathy

#### contents

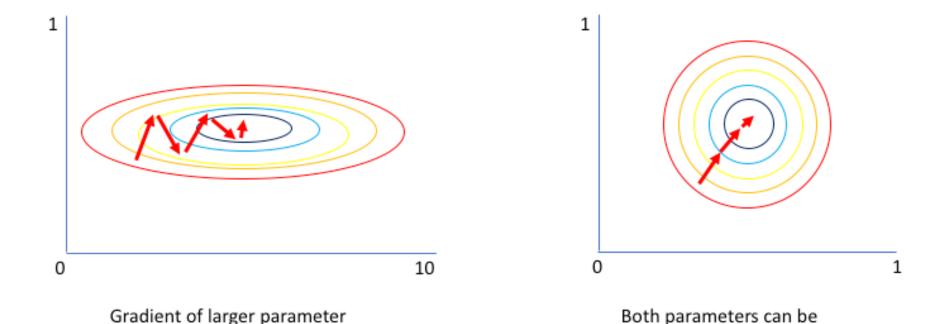
- The classification problem- again
- NN history
- Perceptron
  - Hyperplanes
  - Activation
- Dense layer
- Multi-layer perceptron (MLP)
- Optimization
  - Softmax + cross entropy + loss
  - Gradient descent
- Basic data preprocessing
  - Data normalization
  - Train, validation and test splits

#### **Data normalization**

• Assuming 2D input data with different scales  $(x_1 \in [0,1], x_2 \in [0,1000])$ 

dominates the update

- The weights needed to make  $x_1$  significant as  $x_2$  are much larger and hence make the loss function ellipsoid in one direction.
- This will cause the gradient descent method to converge in more steps than if the two axis where at the same scale.



updated in equal proportions

#### **Data normalization**

• In order to overcome this, we shall normalize the data before the entrance to the NN:

$$\mu = \frac{1}{m} \sum_{i=0}^{m} x_i, \sigma^2 = \frac{1}{m-1} \sum_{i=0}^{m} (x_i - \mu)^2$$

$$\widetilde{x}_i = \frac{x_i - \mu}{\sigma^2}$$

- This should be done for each dimension of the input vector independently.
- The test data should be normalized with the same variables found in the train data.
- This is a common practice to do even if the data are at the same scale for all dimensions since the default hyperparameters for all NN are based on such normalized data.

# Testing the results

- NN frameworks are build on learning from examples, so the data is important.
- Usually, we split the data to 3 different datasets:
  - Train: to train the weights.
  - Validation: test the resulted NN with specific architecture on unseen data.
  - Test: compare different types of NN architectures/ change in hyperparameters which are not learned.
- If we don't have a validation dataset, we will eventually change the architecture/ hyperparameters so they will fit the test data- basically learning on the unseen dataset- **not good**.

train	validation	test
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• Fully connected colab