

Third Edition Numerical Methods for Scientists and Engineers

K. Sankara Rao



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Third Edition

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NUMERICAL METHODS FOR SCIENTISTS AND ENGINEERS, 3rd ed. K. Sankara Rao

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 $\begin{array}{c} To \\ my \ wife \ \boldsymbol{Leela} \end{array}$

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