# Numerical models of lithospheric deformation forming the Southern Alps of New Zealand

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[1] Compression of the entire continental lithosphere is considered using two-6 dimensional numerical models to study the influence of the lithospheric mantle on the 7 geometry of continental collision in its initial stages. The numerical scheme incorporates 8 brittle-elastic-ductile rheology, heat transfer, surface processes, and fault localization. 9 Models are based on the central section of the New Zealand Southern Alps, where 10 11 continental collision has occurred along the Alpine Fault since about 7 Ma. The results are compared to the surface relief, the GPS convergence velocity, the measured electrical 12 conductivity, and the geometry of the crustal root imaged from seismic velocity 13measurements. The crustal deformation is characterized by localized uplift at the 14plate boundary (Alpine Fault) and by two secondary zones of faulting. One is located 15 $\sim$ 60-80 km east of the Alpine Fault, at the start of upper crust bending (or tilting), and the 16 other is located  $\sim 100-130$  km east of the Alpine Fault as a result of shear strain 17propagating to the surface through the ductile lower crust. The observed asymmetric shape 18 of the crustal root is best reproduced for mantle lithosphere strength of the order of 19200 MPa and an intermediate rate of strain softening. A lower strength of the mantle 20lithosphere can produce symmetric thickening, but the amplitude of the crustal root is too 21small when compared to observations. The observed 20 km offset between the maximum 22in surface relief and the crustal root was not satisfactorily reproduced. This offset is 23most likely due to the three dimensionality of oblique collision in the Southern 24INDEX TERMS: 3902 Mineral Physics: Creep and deformation; 8102 Tectonophysics: Continental 25Alps. contractional orogenic belts; 8120 Tectonophysics: Dynamics of lithosphere and mantle-general; 8159 26Tectonophysics: Rheology-crust and lithosphere; 9355 Information Related to Geographic Region: Pacific 2728Ocean; KEYWORDS: mechanical modeling, theology of the lithosphere, strain localization, decoupled crust and mantle, continental collision, Southern Alps 29

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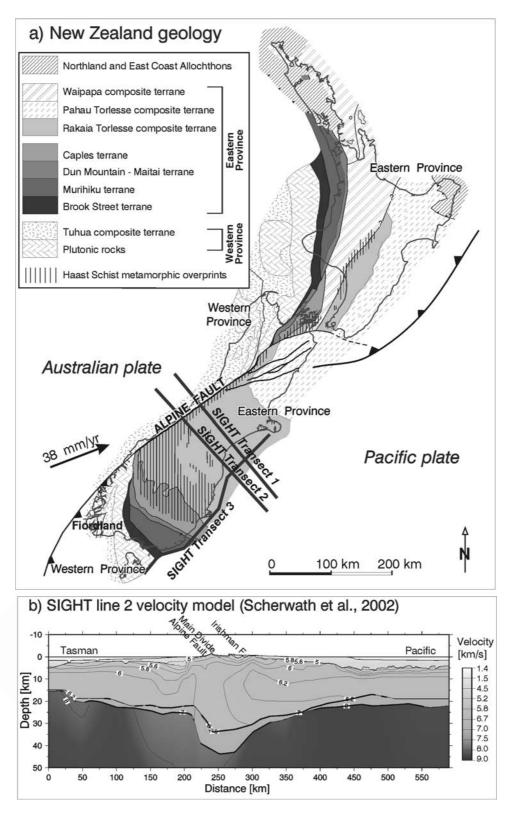
#### 33 1. Introduction

[2] The South Island of New Zealand provides a simple 34 setting in which geodynamic models of active convergent 35 mountain belts can be compared to observations. The 36 Australian/Pacific plate boundary through the South Island 37 has progressively formed about 45 Ma, transforming an 38 initial Eocene passive margin into the dextral strike-slip 39 Alpine fault, with ~450 km of offset [Wellman and Willet, 40 41 1942; Carter and Norris, 1976; Sutherland et al., 2000]. Oblique convergence commenced about 7 Ma and has 42 resulted in  $\sim 100$  km of shortening and the uplift of the 43 Southern Alps mountain range [Wellman, 1979; DeMets et 44 al., 1990; Beavan and Haines, 2001] (Figure 1). 45

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[3] In regions of oblique relative plate motion and where 46 both shear and compressive deformation occur together, 47 two-dimensional (2-D) models [e.g., Willett, 1999; Batt and 48 Braun, 1999] can help understand which deformation 49 structures are due solely to the compressive component 50 of the system. Koons [1990] and Beaumont et al. [1996] 51 first applied such models to the Southern Alps of New 52 Zealand. They identified that the parameters that control 53 the large-scale geometry of the orogen are a combination of 54 crustal rheological properties, surface processes, and 55 boundary conditions applied at the base of the crust. 56 However, these models assume that the Pacific crust is 57 driven by lithospheric mantle against the Australian litho- 58 sphere, so that an imposed basal velocity discontinuity 59 (commonly referred to as the "S point") controls the 60 location of deformation. Modeling of the interaction be- 61 tween the crust and the mantle lithosphere is biased by this 62 prescribed discontinuous boundary condition. During the 63 mountain building process, deflection of the Moho should 64 also be constrained by the ability of the underlying mantle 65 lithosphere to deform. In this paper we incorporate the 66

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**Figure 1.** (a) Geological setting in the Southern Alps of New Zealand [*Mortimer*, 2000]: Eastern Province terranes on the Pacific plate deform against Western Province terranes. Dark gray lines show approximate location of geophysical transects for the SIGHT experiment. (b) Seismic velocity model across SIGHT line 2 from *Scherwath et al.* [1998]. Note that horizontal coordinates do not coincide with the following model coordinates. Vertical exaggeration is 4.

mantle lithosphere when examining the growth of theSouthern Alps.

[4] The lithospheric mantle can undergo tectonic short-69 70 ening in three principal ways: homogeneous shortening by distributed thickening, folding (or buckling) by subperiod-71 ical bending of competent lithospheric layers, or intraconti-72nental subduction by asymmetric underthrusting of one 73 block under the other along a major shear zone. While the 74occurrence of symmetric or asymmetric mantle thickening 75 is an old debate [Houseman et al., 1981; Mattauer, 1986], it 76 is only recently that large-scale folding is understood to be a 77 primary response of the lithosphere to induced compres-78 sional stress [e.g., Martinod and Davy, 1992; Burov et al., 791993; Gerbault et al., 1999; Cloetingh et al., 1999]. 80 81 Lithospheric folding develops due to its strength contrast 82 with low-viscosity asthenosphere and evolves as a single 83 megafold where rheological weaknesses concentrate [Burg and Podladchikov, 1999; Cloetingh et al., 1999]. 84

[5] At the timescale of 10-20 Myr, symmetric down-85 welling of the mantle lithosphere may also result from a 86 convective or a Rayleigh-Taylor instability, due to cold 87 and dense thickening mantle lithosphere [e.g., Houseman 88 et al., 1981]. This mechanism has been proposed for the 89 Southern Alps of New Zealand to explain the observed 90 negative gravity anomaly and P wave delays [Stern, 1995; Molnar et al., 1999; Stern et al., 2000]. Using 9192 large-scale models that include the lithosphere and upper 93 mantle, Pysklywec et al. [2000] showed that a Rayleigh-94 95Taylor-type instability or asymmetric intracontinental sub-96 duction can evolve into dripping or slab break off of the 97 mantle lithosphere, depending on the rate of convergence, the density distribution, and the strength of the mantle 98 lithosphere. 99

[6] In contrast to the approach of *Pysklywec et al.* [2000], 100we investigate the smaller-scale deformation within the 101lithosphere. We incorporate preexisting heterogeneities 102based on known rheological discontinuities (terranes of 103different tectonic history, Figure 1a). For example, the 104Alpine Fault is a major strike-slip feature that has been in 105existence for  $\sim 45$  Myr prior to the actual compressional 106 episode [Sutherland et al., 2000], and we model it as an 107initial vertical zone of weakness. Since we ask how the 108 strength contrasts determine the asymmetry of the litho-109110 spheric mantle and its effects on crustal deformation, our formulation of the initial state of the plate boundary is 111 112intermediate between two opposing approaches. One end-113member assumes complete stress and deformation disconti-114nuity across a narrow zone (the S point models are related to 115this approach), and the other end-member accounts for lateral continuity of stresses across the plate boundary and 116allows for lithospheric-scale folding. We performed a series 117 of model calculations to examine the mechanical properties 118 of the lithosphere (on geological timescales) that give rise to 119the present Southern Alps. Instead of presenting an exhaus-120tive set of results, several new geophysical observations 121 allow us to confine the range of numerical parameters and 122therefore constrain model calculations. The most important 123data sets we choose to compare models to are the present 124 surface elevation, mapped faults, contemporary GPS mea-125surements, the image of the crustal root deduced from 126127 seismic velocity modeling [Scherwath et al., 1998] (Figure 1281b), gravity and magnetotelluric observations, and the distribution of earthquakes. In this paper we demonstrate how a 129 well-constrained numerical model can bring insight into the 130 development of a young continental collision zone such as 131 the New Zealand Southern Alps. 132

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#### 2. Numerical Modeling

#### 2.1. Numerical Approach

#### 2.1.1 General Features

[7] We use the mixed finite element-finite difference code 136 Parovoz [Poliakov and Podladchikov, 1992]. It is based on 137 the fast Lagrangian analysis continuum method (FLAC 138 [Cundall and Board, 1988]), which incorporates an explicit 139 time-marching scheme, and allows the use of a wide range 140 of constitutive laws such as brittle-elastic-ductile rheology 141 derived by rock experimentalists [e.g., Brace and Kohlstedt, 142 1980; Ranalli, 1995]. Parovoz handles initiation and prop- 143 agation of nonpredefined faults (shear bands). The present 144 version also includes diffusive surface processes, heat 145 advection and conduction including initial age-dependent 146 temperature field. This code has proved efficient in model- 147 ing many tectonic features, such as salt diapirism [Poliakov 148 and Podladchikov, 1992], lithospheric folding [Gerbault et 149 al., 1999], lithospheric rifting [Buck and Poliakov, 1998; 150 Burov and Poliakov, 2001]. More details are given in 151 Appendix A concerning the numerical method, calculation 152 of the geotherm, and rheological laws. 153

[8] The lithosphere is modeled as a medium of 300 by 30 154 quadrilateral elements, with a total length of 600 km and 155 depth of 60 km (Figure 2). Both lateral borders are free to 156 slip vertically, the left border is fixed in the horizontal 157 direction and a velocity  $V_x = 4.5 \times 10^{-10} \text{m s}^{-1} (15 \text{ mm yr}^{-1})$  158 is applied on the right border. The lithosphere floats on the 159 asthenosphere within the gravity field; hydrostatic boundary 160 conditions are applied at the bottom of the model, with an 161 underlying density of 3250 kg m<sup>-3</sup>. The surface is stress 162 free.

[9] An initial temperature distribution is calculated, 164 which includes a thermomechanical age dependency, anal- 165 ogous to that of oceanic lithospheres, and incorporates 166 crustal radioactive heat [*Burov and Diament*, 1995] (see 167 Appendix A). A thermomechanical age equal to 100 Ma is 168 assigned here, based on the last episode of extension that 169 affected the New Zealand shelf [*Laird*, 1993] and was likely 170 to have rejuvenated most of the lithosphere. 171

[10] The model lithospheric plate is divided into areas of 172 different mechanical properties (Table 1). The initial crustal 173 thickness, or the depth to the Moho, is set at 25 km; this 174 choice is constrained by several observations from seismo-175 logical studies, indicating a "far-field" crustal thickness of 176 22-26 km [*Scherwath et al.*, 1998; *Godfrey et al.*, 2001]. 177 The density distribution is 2650, 2900, and 3200 kg m<sup>-3</sup>, 178 respectively for the first 19 km, from 19 to 25 km, and from 179 25 to 60 km depth.

#### 2.2. Rheology

[11] Elastic-viscous-brittle behavior is modeled with a 182 pressure-dependent Coulomb criterion for brittle failure, 183 and a temperature-dependent creep power law for ductile 184 behavior (see Table 1 and Appendix A). For each element of 185 the model and at any time step, if the shear stress provided by 186 the creep law reaches the Mohr-Coulomb plastic yield, then 187

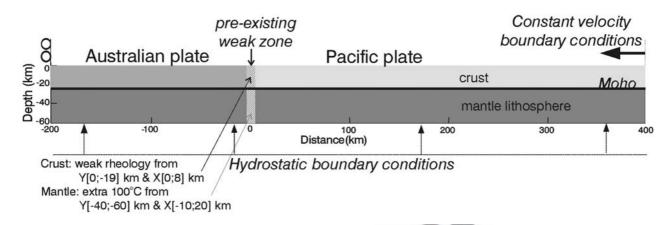


Figure 2. Initial conditions for the 2-D model (see text).

nonassociative failure occurs. In this sense, the brittle-ductiletransition is self-consistently defined in the modeling.

[12] Above the Moho, a vertical division separates the 190Australian crust, to the left (west) from the Pacific crust to 191 the right (east). The "Australian crust" and "Pacific crust" 192rheologies are based on geological mapping and petrology 193of basement terranes (Figure 1a) and regional geophysical 194data. The Australian crust is composed of Paleozoic plu-195tonic rocks (Western Province) that are found in northwest 196 South Island, in Fiordland, and offshore on the Challenger 197 and Campbell Plateaus (Figure 1a). There is no evidence for 198199internal deformation in the Australian lithosphere, apart 200 from a broad flexural bending toward the Alpine Fault [Sircompe and Kamp, 1998]. Power law creep parameters 201for the Australian crust are thus chosen so that the lower 202203crust remains elastobrittle (Table 1). East of the Alpine Fault, the Eastern Province rocks are composed of low-204grade metasediments (graywacke to schist) that were ac-205creted in Mesozoic times. These rocks are younger than the 206Western Province rocks, and are likely to be mechanically 207weaker. A dominant quartzite rheology (Table 1) best 208matches the observed geology, the seismological brittle-209ductile transition at 12 km [Leitner et al., 2001], the 210convergence rate, and constraints on the geotherm. 211

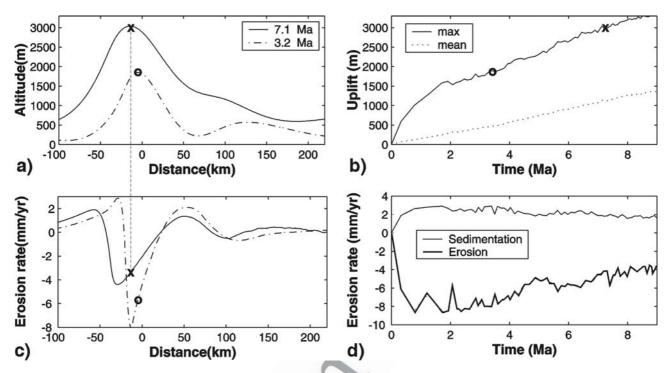
212 [13] In between the Australian and Pacific crust, a zone 213 of weakness is inserted (four elements wide and located at X = [0; 10] km) and simulates the Alpine Fault (Figure 2). 214 Inclusion of a preexisting fault zone derives from the 215 observation that Neogene plate boundary deformation 216 along the Alpine Fault is most likely an inherited Eocene 217 older structure [*Sutherland et al.*, 2000]. If this preexisting 218 fault zone is not present, then a folding instability develops 219 in the Pacific crust. The strength (or viscosity) contrast 220 between the brittle crust and the deeper ductile crust only 221 needs to be of ~3 orders of magnitude for folding to 222 develop after ~5% of homogeneous shortening [e.g., *Bull* 223 *et al.*, 1992; *Burov and Diament*, 1995; *Gerbault et al.*, 224 1999].

[14] Below the Moho, dry olivine is assumed to control 226 the strength of the mantle lithosphere (see creep law 227 parameters in Table 1). Strain softening is included, with 228 details in Appendix A: its effects are discussed later in the 229 paper. A zone of weakness must also be inserted in the 230 mantle else periodic undulations develop, due to periodic 231 folding of the "strong" mantle lithosphere. Preliminary 232 numerical tests show that both assumptions of a preexisting 233 zone of weak rheology or a preexisting thermal perturbation 234 lead to similar results. Since a thermal anomaly would better 235 correspond to extra heat present at depth due to sustained 236 shear along the trend of the Alpine Fault, a perturbation of 237 100°C is inserted below the crustal weak zone, at X = [-10; 238+20] km and Y = [-40; -60] km. 239

t1.1 **Table 1.** Rheological Properties for Reference Model<sup>a</sup>

	-	1					
t1.2					Activation Energy Q,	Mohr-Coulomb	Friction/Viscosity
				Constant A,		Brittle	Softening
t1.3	Layers	Creep Law	Power n	$Pa^{-n} s^{-1}$	$J mol^{-1}$	properties	Rates
t1.4	Mantle lithosphere	olivine	3	$7 \times 10^4$	$5.2 \times 10^{5}$	$S_0 = 200 \text{ MPa} \rightarrow 50 \text{ MPa}$	$\varepsilon_{\rm s} = 0.1 \rightarrow 1.$
t1.5	•					$\phi = 0^{\circ}$	
t1.6	Australian crust	olivine				$\phi = 30^{\circ} \rightarrow 10^{\circ}$	$\varepsilon_{\rm s} = 0.1 \rightarrow 1.$
t1.7						$S_{\rm o} = 20$ MPa	-
t1.8	Lower crust					$S_{\rm o} = 200$ MPa, $\phi = 0^{\circ}$	no softening
t1.9	Pacific crust	wet quartzite	2.3	$3.2 \times 10^{-4}$	$1.54 \times 10^{5}$	$\phi = 30^\circ, S_o = 20$ MPa	$\varepsilon_{\rm s} = 0.1 \rightarrow 2$ : $\mu = \mu/10$
t1.10	Lower crust	*					no softening
t1.11	Weak zone crust	wet granite	1.9	$2 \times 10^{-4}$	$1.37 \times 10^{5}$	$S_0 = 20$ MPa, $\phi = 15^{\circ}$ , $\lambda = 0.33$	$\varepsilon_{\rm s} = 0.1 \rightarrow 2$ : $\mu = \mu/10$
t1.12	Lower crust	-					no softening
t1.13	Sediments and top	wet granite				$S_0 = 20$ MPa, $\phi = 15^{\circ}$ , $\lambda = 0.33$	no softening
	3 km Austral. crust	-					-

<sup>a</sup>Power law creep parameters are from *Ranalli* [1995]. Mohr-Coulomb parameters are cohesion So, friction angle  $\phi$ , and fluid pressure ratio  $\lambda$  (normal stress proportional to lithostatic pressure). Strain softening acts within both given values of the total shear strain, and modifies the value located on the same t1.14 line in the previous column. Where specified, strain softening acts instead on viscosity  $\mu$ .



**Figure 3.** Surface deformation for reference model: (a and b) topography and (c and d) erosion rates plotted against horizontal distance (Figures 3a and 3c) and time (Figures 3b and 3d). Circles and crosses correspond to the spatial maximum of topography after 3.2 and 7 Myr. After 7 Myr this maximum is located  $\sim$ 15 km east from the maximum erosion rate.

[15] Results after 7 Myr of shortening are presented in 240Figures 3 and 4 for the reference model. In Figures 3 and 4, 241the origin of the horizontal axis (X = 0) is located at the 242 initial preexisting crustal weak zone. Comparisons with 243electrical conductivity, geodesy, seismic Moho, and gravity 244anomaly are shown in Figures 5, 6, and 7. The following 245sections discuss deformation in the crust, the role of 246lithospheric mantle strength on the geometry of the orogen, 247and the relative position of the maximum topography and 248249the crustal root, compared to observations across the South-250ern Alps. The discussion also includes additional models that use a number of supplementary parameters. The results 251and comments on these models in relation to the reference 252model are summarized in Table 2. 253

#### **3. Deformation in the Crust**

#### 256 3.1. Surface Uplift

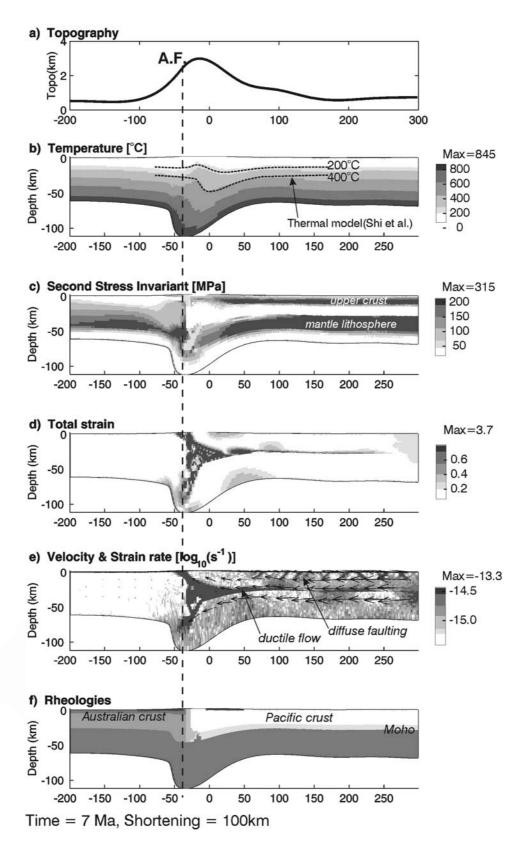
[16] Surface deformation is displayed through time in Figure 3. Maximum elevation develops above the initial weak zone (at X = 0), evolves 10 km toward the west, and reaches ~3000 m within 7 Myr (Figure 3a). A secondary maximum develops close to X = 100 km (this position reduces as time progresses).

[17] The whole lithosphere is affected by a component of 263regional surface uplift (Figure 3b), due to homogeneous 264thickening. This regional or mean surface uplift (different 265from rock exhumation) is around 0.15 mm  $yr^{-1}$ , with a 266maximum of 5 mm yr<sup>-1</sup> (3000 m in 7 Myr, Figures 3a and 2673b), with respect to the initial zero level. The mean density 268of the lithosphere is likely to increases with increasing 269distance away from the South Island as the lithospheric 270

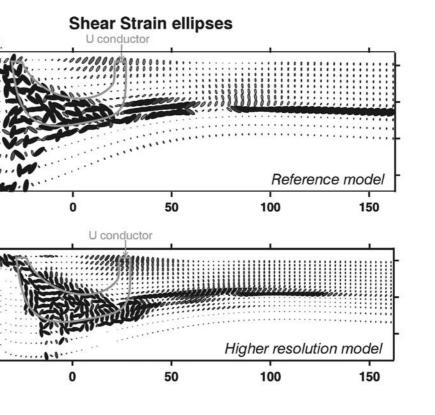
rock composition becomes more similar to oceanic litho- 271 sphere. Therefore our model cannot fit real far-field surface 272 elevations, because such lateral density contrasts are not 273 taken into account. Homogeneous thickening is the change 274 in shape of a layer that is compressed horizontally and 275 thickens vertically due to mass conservation. Homogeneous 276 (or uniform) thickening is primarily, a fundamental way to 277 accommodate lithosphere compression and is complemen- 278 tary to localized deformation and mountain growth. It 279 occurs as a consequence of elastic and viscous rheologies, 280 and also diffuse faulting [Bull et al., 1992; Martinod and 281 Davy, 1992; Burov et al., 1993; Burg and Podladchikov, 282 1999; Gerbault, 2000]. Although uniform shortening is 283 generally difficult to quantify from the geology because of 284 its continuous character, vertically elongated structures in 285 the lower crust exhumed at the Alpine Fault are interpreted 286 by Little et al. [2001] as markers of uniform shortening that 287 develops at least 100 km east from the plate boundary. 288 Furthermore, GPS and shear wave splitting data show 289 evidence for "distributed deformation" [e.g., Moore et al., 290 2002, and references therein]. 291

[18] The maximum erosion rate is located  $\sim 10$  km west 292 of the maximum of the topography (Figure 3c). It reaches a 293 quasi-stable value of  $\sim 5$  mm yr<sup>-1</sup> after 2 Myr (Figure 3d). 294 The sedimentation rate is lower than the erosion rate, partly 295 because of the open mass flow condition at the borders of 296 the model and partly because of the numerical approxima-297 tion of sedimentation (see Appendix A). 298

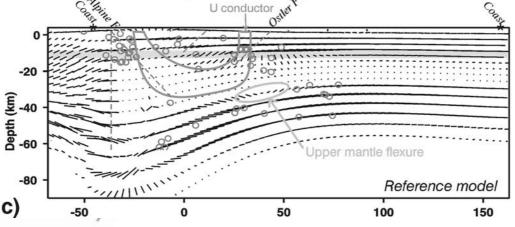
[19] Sediment budget studies [e.g., *Griffiths and McSave-* 299 *ney*, 1983; *Adams and Gabites*, 1985] and cooling ages 300 [*Tippett and Kamp*, 1993] both indicate that uplift rates 301 increase exponentially up to  $\sim 10 \text{ mm yr}^{-1}$  at the Alpine 302



**Figure 4.** Reference model after 7 Myr of shortening (100 km). A.F. is Alpine Fault. (a) Surface topography, (b) temperature field, (c) deviatoric shear stress, (d) total shear strain (elastic, viscous and brittle), (e) shear strain rate and instantaneous velocity vectors, and (f) rheological phases (layers). Dark elements close to the surface are sediments. The vertical dashed line is positioned with reference to Figure 4e shear zone rising to the surface, namely, which we call the Alpine Fault zone.



Most compressive principal stress lines



**Figure 5.** Shear strain ellipses after 7 Myr. (a) Reference model. Numerical values of the shear strain are same as for Figure 4d. (b) Higher-resolution model ( $400 \times 40$  elements). Superimposition of the high electrical conductivity signal in thick gray contour: note the "flip" of shear strain ellipses in the ductile lower crust, at  $X \sim 25$  km. (c) Most compressive principal stress lines for the reference model. Gray circles are earthquakes distribution, dashed lines are presumed geometry of faults at depth, and thick gray line is the 12 km deep seismogenic zone (all data from *Leitner et al.* [2001]).

Fault. There is also an indication for the initiation of rapid erosion in the Southern Alps beginning at 2–3 Ma [*Tippett and Kamp*, 1993]. *Koons* [1989, 1990] studied the role of asymmetric erosion and recognized that rapid removal of material from the West Coast controls the asymmetry of deformation on either side of the Main Divide, a point developed also by *Beaumont et al.* [1992, 1996].

0

-20

40

-60

0

Depth (km) -50 -40

b)

-50

-50

Depth (km)

a)

310 [20] The factor of 2 difference in the erosion rate between 1 311 our models and the observations is due to surface processes

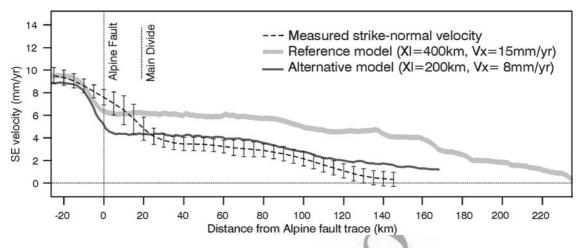
being modeled with a numerical algorithm that smoothes 312 surface deformation. This is also the reason why fluvial 313 transport is not incorporated in the modeling, as developed 314 by *Koons* [1990] and *Beaumont et al.* [1992, 1996]. 315

#### **3.2. Temperature, Strain, and Stress Distribution** 316

[21] Figure 4b displays the deflection of initially horizon- 317 tal isotherms after 7 Myr of shortening. Isotherms are 318 elevated in the upper crustal area just east of the modeled 319

ETG

**X** - 8



**Figure 6.** Comparison of surface convergence velocity with GPS measurements [*Beavan and Haines*, 2001]. Thick light gray line is the reference model, with distance from the plate boundary to the eastern border of the model  $X_1 = 400$  km, and applied convergence rate  $V_x = 15$  mm yr<sup>-1</sup>. Thin dark gray line is an alternative model with smaller distance  $X_1 = 200$  km and slower convergence rate  $V_x = 8$  mm yr<sup>-1</sup>. Note the difference in velocity increase at the Alpine Fault, and the similar change in slope at a distance of ~80 km to the east.

"Alpine Fault zone" (see vertical dashed line referring to its 320 modeled position on Figure 4). They are deflected down-321 ward at midcrustal depths. This geometry is very similar to 322 results obtained from previous thermal modeling [Shi et al., 323 1996] (dashed lines on Figure 4b), which was compared to 324 heat flow measurements. This supports the fact that advec-325tion is the main mode of heat transfer as a response to 7 Myr 326of compression. 327

<sup>328</sup> [22] Figure 4c displays distribution of the shear stress  $\sigma_s =$ <sup>329</sup>  $[(\sigma_{xx} - \sigma_{yy})^2/2 + \sigma_{xy}^2]^{1/2}$ . One can identify three strong <sup>330</sup> layers: the Australian lithosphere, the Pacific upper crust, <sup>331</sup> and the Pacific lithospheric mantle. Note the geometry of <sup>332</sup> weak zones that develop in the center of the model, at the <sup>333</sup> plate boundary.

[23] Figure 4d displays the accumulated total shear strain  $\varepsilon_s = [(\varepsilon_{xx} - \varepsilon_{yy})^2/2 + \varepsilon_{xy}^2]^{1/2}$ , with time, while Figure 4e 334335 displays the instantaneous shear strain rate and instantaneous 336velocity vectors. Deformation accumulates in a "crustal 337 root", which progressively increases in width and depth. 338 Low-strength Pacific material accumulates against the Aus-339 tralian lithosphere, connecting (1) the Alpine Fault zone in 340 341the upper crust, emerging to the surface at  $X \sim -30$  km, (2) a horizontal shear zone in the ductile lower crust, extending 342 toward the east, and (3) a "west dipping" shear zone 343 344propagating downward into the lithospheric mantle.

#### 345 3.3. Shear Strain Localization: The Alpine Fault

[24] The Alpine Fault shear zone develops at the site of 346 the initial vertical weak zone in the crust. This active zone 347 progressively inclines and propagates into the Australian 348 crust and toward the surface (compare Figure 4e with 349inclined shear zone and Figure 4f, which shows rheological 350layers and vertical initial plate boundary zone). Its geometry 351 is determined by two conditions: (1) the preexisting vertical 352weak zone and (2) the development of a shear zone inclined 353 between 30° and 45° from the maximum principal strain 354and principal stress orientation (nonassociated plasticity 355with friction angle  $\phi = 30^{\circ}$  and dilatation angle  $\psi = 0^{\circ}$ 356[Vermeer, 1990; Gerbault et al., 1998]). 357

[25] The Alpine Fault shear zone is wider than the 358 mapped fault: the numerical model produces shear bands 359 that occupy a width of about five numerical elements. 360 Since the present model deals with 2 km wide elements, 361 the modeled Alpine Fault zone is thus 10 km wide. 362 Because the initial vertical weak zone is not in the 363 "correct" orientation to accommodate thrust faulting in-364 clined at  $30^{\circ}-45^{\circ}$ , the active shear zone is superimposed 365 only on part of the initial weak zone: this superimposition 366 (Figures 4d and 4f) occurs around 10-15 km depth, where 367 the shear strength is highest with depth, but lowest in 368 horizontal direction. This geometry is logical if one con-369 siders how a fault would develop according to minimized 370 energy patterns. 371

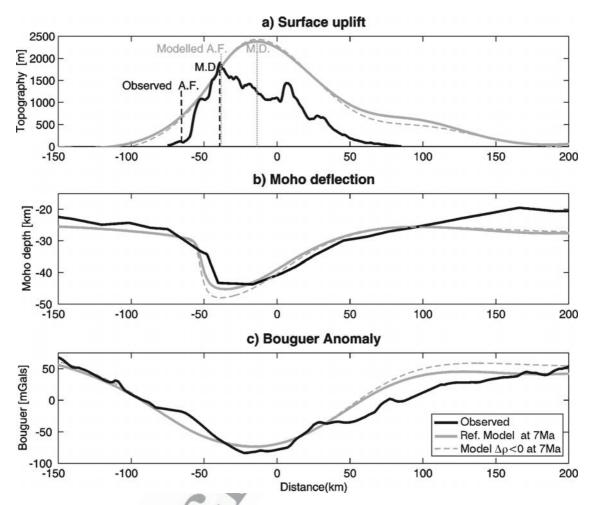
[26] The present-day transform shear zone corresponds to 372 the active shear zone in the model, after 7 Myr, and not to 373 the initial vertical weak zone. While 2-D modeling cannot 374 address the issue of strain partitioning, 3-D modeling 375 [*Gerbault et al.*, 2002] also indicates a progressive inclination with time of the vertical plate boundary, along which 377 transcurrent shear occurs. This is consistent with indications 378 of nonpartitioned strain in the Southern Alps [e.g., *Braun* 379 *and Beaumont*, 1995]. 380

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#### **3.4.** Shear Strain Localization: General Features

[27] The modeled Alpine Fault shear zone curves at depth 382 to merge with a ductile shear zone in the lower crust 383 (Figures 4d and 4e). At this level, deformation propagates 384 to the east, within the  $\sim 10$  km thick low-viscosity lower 385 crust, and allows the upper crust to detach from the 386 lithospheric mantle. In section 4, we illustrate how the 387 eastern tip of this lower crust ductile shear zone can 388 propagate via upper crustal faulting to the surface, at a 389 characteristic distance ranging from 100 to 130 km from the 390 Alpine Fault shear zone. 391

[28] In contrast to the development of localized shear 392 strain at the Alpine Fault zone, diffuse faulting in the brittle 393 upper crust is represented numerically by conjugate shear 394 bands alternating in both dip directions in time and space 395



**Figure 7.** Comparisons of reference model with observed (a) topography, (b) Moho, and (c) gravity anomaly. Black lines are observed topography, Moho from seismic velocity models along transect 2 [*Scherwath*, 2001], and measured Bouguer gravity anomaly. Gray lines are same horizons obtained with the reference model. Dashed gray lines are an additional model with a density of 3300 kg m<sup>-3</sup> for the mantle lithosphere and basal hydrostatic compensation of 3250 kg m<sup>-3</sup>. In Figure 7a, vertical dashed lines are the observed (in black) and modeled (in gray) positions of the Alpine Fault (A.F.) and of the main divide (M.D.). Five hundred meters have been subtracted from the model topography (Figure 7a), and 100 mGal have been added to the model gravity (Figure 7c) (see text for justification).

t2.1 Table 2. Summary of Numerical Models Illustrated in This Paper<sup>a</sup>

t2.2	Models	Model-Associated Figures	Characteristics	General Results
t2.3	Reference model	Figures 3, 4, 5, 6, 7	$k_{er} = 1000 \text{ m}^2 \text{ yr}^{-1}$	highest surface relief to the west.
t2.4			mantle strength $So = 200$ MPa	crustal root depth of 45 km
t2.5			softening rate $\varepsilon_s = 0.1 \rightarrow 1$ .	subducting mantle lithosphere to the west
t2.6			density contrast 3250/3200	higher horizontal velocity than GPS
t2.7			length = 600 km, $V_x = 15 \text{ mm yr}^{-1}$	
t2.8	GPS modeling	Figure 4	length = 400 km, $V_x = 8 \text{ mm yr}^{-1}$	crustal root depth of 40 km
t2.9				matches GPS horizontal velocity
t2.10	Gravity modeling	Figure 7	density contrast 3300/3250	no significant difference to reference model
t2.11				gravity anomaly too small
t2.12	Low strength	Figure 8a	mantle strength $S_0 = 50$ MPa	low symmetric surface relief
t2.13				crustal root depth of 35 km
t2.14				subducting mantle lithosphere to the east
t2.15	Low strength	Figure 8b	$k_{er} = 500 \text{ m}^2 \text{ yr}^{-1}$	low symmetrical surface relief
t2.16	plus rapid softening		mantle strength $S_0 = 50$ MPa	crustal root depth of 35 km
t2.17	plus low erosion		softening rate $\varepsilon_s = 0.05 \rightarrow 0.5$	symmetric thickening of mantle lithosphere
t2.18	Slow strain softening	Figure 9	mantle strength $S_0 = 200$ MPa	two topographic highs
t2.19			softening rate $\varepsilon_s = 0.1 \rightarrow 2$	subducting mantle lithosphere to the west

t2.20

<sup>a</sup>Models characteristics and results are described in terms of changes from the first reference model.

(Figure 4e). This model behavior may correspond to the
abundant reactivated faults observed within the Torlesse
graywackes east of the Alpine Fault [*Oliver and Keene*,
1990; *Cox and Findlay*, 1995; *Long et al.*, 2003].

[29] Figure 5a displays the shear strain using ellipses 400where each ellipse represents how an initially perfect circle 401 is deformed through time. Darkest ellipses are those that 402 undergo the most shear strain (same shading distribution as 403Figure 4d). Figure 5b shows shear strain ellipse representa-404 tion for a model identical to the reference model, but using a 405more refined grid ( $400 \times 40$  elements). A higher resolution 406allows us to reproduce a narrower Alpine Fault zone and 407examine lower crustal deformation in more detail. 408

[30] In the crustal root, progressive rotation of the high-409strain ellipses demonstrates how the Pacific crust diverges 410411 in response to indentation by the Australian plate (the sharp 412 western border of high strain ellipses coincides with rheological discontinuities inserted in the model). The Alpine 413Fault zone consists of multiple ellipse directions, associated 414 with thickening of the crust, and fault shearing (Figure 5). 415[31] Inclined ellipses located at the base of the lower crust 416 suggest that mantle lithosphere drives material from beneath 417 the crustal root. This shows that although a uniform velocity 418 is applied at the east end of the model, the mantle and the 419

420 crust move with different rates with respect to each other 421 from  $\sim$ 130 km east of the plate boundary (Figure 5).

[32] In the lower crust at about  $X \sim 25$  km, 60 km east of 422the plate boundary, the shear orientation of ellipses shifts, 423 424 with locally a horizontal orientation corresponding to less 425horizontal compression. Above, brittle deformation accumulates in the upper crust, in a zone located  $\sim 60$  km east 426from the Alpine Fault zone: it is the resulting of uplift of the 427upper crust, as it is tilted (or flexed), and dragged with the 428ductile lower crust (Figures 4d and 5). Tilting and flexure of 429the upper crust are consistent with the fan shape of geolog-430ical strain markers [Little et al., 2001]. 431

## 432 3.5. Modeled Strain, Observed Faults, and Electrical433 Conductivity in the Southern Alps

434 [33] The localization of high strain  $\sim 60-80$  km southeast 435of the Alpine Fault (Figure 5) is in very good agreement with a series of active structures, the Lake Heron-Forest 436Creek Faults and the Irishman Creek Fault, which are 437 structurally similar faults that dip either east or west [Bean-438land, 1987; Oliver and Keene, 1990; Woodward et al., 4391994]. This characteristic distance also coincides with the 440 eastern edge of the Bouguer gravity anomaly. 441

[34] Electrical resistivity models derived from a magneto-442telluric profile experiment show a U-shaped high-conduc-443tivity structure under the Southern Alps [Wannamaker et al., 444 2002]. The lowest resistivities  $(40-100 \text{ ohm m}^{-1})$  lie at 25– 44530 km depth below the surface (Figure 5) and extend upward 446 447 as narrow near-vertical conductors near the Alpine Fault trace and 60-70 km to the east. This latter branch of the 448 449 conductor appears to coincide with fault zones (the Forest Creek-Lake Heron Faults), which would allow deep crustal 450fluids to migrate to the surface [Templeton et al., 1998]. 451Among the deformation mechanisms that are expected to 452operate in lower crustal ductile rocks, diffusion creep may 453dominate when the volume of fluids is small (<0.5 vol %), 454and under relatively low stress conditions [Tullis and Yund, 4551991]. Wannamaker et al. [2002] discuss the cause of the 456

high conductivity in the crust and favor the presence of 457 interconnected fluids resulting from prograde metamorphic 458 reactions occurring in the crustal root. Excess water is likely 459 to lead to increased fluid pressure. High pore pressure is also 460 inferred to be the origin of a low *P* wave velocities [*Stern et 461 al.*, 2001; *Eberhart-Phillips and Bannister*, 2002] that are 462 coincident with the high-conductivity structure. 463

[35] In the present numerical models, we have not 464 accounted for the presence of fluids being produced and 465 evolving with time. However, the coincidence of the shape 466 of the high-conductivity zone with the area of high strain 467 (Figure 5b) suggests a link between conductivity and fluids 468 as an image of the high shear zones in the crust. The change 469 in ellipse orientations at about X = 25 km, is interpreted as a 470 zone of less compression due to clockwise bending of the 471 upper crust to the west, and in which interconnected fluids 472 may accumulate.

[36] Figure 5c represents stress lines, each line showing 474 the local orientation of the most compressive stress. 475 Figure 5c suggests that the conductivity signal is caused 476 by internal crustal deformation mechanisms, because it is 477 located above and to the west of the change in stress 478 orientation corresponding to extensional flexure of the 479 upper mantle. Earthquakes superimposed on our 2-D model 480 [*Leitner et al.*, 2001] show good agreement with areas of 481 enhanced compression and also seem to coincide with local 482 stress orientation changes but, at the same time, surround 483 the zone of inferred high pore fluids. 484

#### **3.6.** Comparison to Contemporary Plate Motion and 485 Width of the Orogen 486

[37] Figure 6 displays a comparison between the observed 487 GPS convergence velocity and the result from the model. 488 This modeled convergence velocity is evaluated after 489  $\sim$ 7 Myr of shortening, for one time step, which is typically 490 of the order of 30 years. We see that the reference model has 491 a generally higher convergence rate than observations (thick 492 light gray line on Figure 6). This is because the reference 493 model is defined to be extending for 400 km east of the plate 494 boundary, and to have a convergence rate of 15 mm yr<sup>-1</sup>. 495 These values were used, first, to avoid numerical border 496 effects on the resulting deformation and, second, to match 497 plate tectonic models that indicate  $\sim 100$  km of convergence 498 within 7 Myr. Present convergent rates based on GPS 499 observations [Beavan and Haines, 2001], however, record 500 a velocity of  $\sim 8 \text{ mm yr}^{-1}$ , as measured across the width of 501 the South Island (200 km), over a 10 year time period. We 502 also plotted the resulting velocity for an alternative model, 503 in which the distance from the border of the model to the 504 plate boundary has been reduced to 200 km and a conver- 505 gence rate of 8 mm yr<sup>-1</sup> has been imposed (Table 2). After 506 7 Myr, the crust and mantle deformation from this alterna- 507 tive model are similar to those from the reference model, 508 except that the crustal root is less deep, since the shortening 509 rate is slower. Comparison of the surface velocity with the 510 GPS data is now more consistent (thin dark gray line on 511 Figure 6). 512

[38] Two interesting features are noticable on Figure 6: 513 First, we note a similar stabilization of convergence veloc- 514 ity, in the data and in the models, at  $\sim 80-100$  km from the 515 Alpine Fault; this feature can be related to the area where 516 the crust detaches from the mantle lithosphere. Second, the 517 extent of increasing convergence velocity at the Alpine
Fault is broader in the data than in the model. This is due
to elastic strain accumulating from the last earthquake cycle,
and we would expect the velocity increase, over time, to
become sharper in GPS measurements and thus more
similar to the models.

[39] About 100 km east of the Alpine Fault in the central 524Southern Alps, the topography increases to  $\sim 1500$  m. Many 525strike-slip and reverse faults coexist in this area. Previous 526analytic, analog and numerical models also reproduce this 527zone of secondary surface uplift, which represents conjugate 528brittle shear with respect to the Alpine fault, i.e., the other 529edge of the double-vergent wedge characteristic of orogenic 530process [Koons, 1990; Koons and Henderson, 1995; Beau-531*mont et al.*, 1996]. Our models emphasize that the amplitude 532533of this secondary zone of uplift depends on a number of 534parameters. First, erosion and sedimentation processes are known to help localize deformation [Beaumont et al., 1996]. 535If surface processes are imposed slowly, deformation is less 536asymmetric and diffuses over a broader area, to the east in 537the case of the Southern Alps. Second, if the lower crust is 538assumed to be relatively stronger than in the reference 539model, then ductile shear deformation is confined to a 540smaller depth range, and tends to propagate more to the 541east, in order to occupy the same volume. If the Moho is 542chosen initially deeper (say at 30 km), then the distance at 543which this secondary uplift occurs increases. Finally, a 544strong mantle lithosphere also contributes to producing 545546wider surface deformation. This is discussed in section 4.

# 548 4. Deformation in the Lithospheric Mantle549 4.1. Observations of Deformation at and Under the

#### 549 4.1. Observations of Deformation at and Under the 550 Moho in the Southern Alps

[40] Seismic velocity models [Davey et al., 1998; Scher-551wath et al., 2000; Eberhart-Phillips and Bannister, 2002] 552provide an image of a crustal root ~100 km wide, with a 553maximum depth of 40-45 km, and increasing southward 554between transect 1 and transect 2 (Figures 1a and 1b). The 555556deepest part of the crust lies  $\sim 20$  km east from the Main Divide (itself  $\sim 20$  km east from the Alpine Fault). The 557thickness and location of the crustal root indicate that the 558orogen is overcompensated and is marked by large negative 559(-30 mGal) isostatic gravity anomalies [Woodward, 1979]. 560[41] Stern [1995] first proposed an elastic flexure model 561where a subducting mantle lithosphere body 100 km wide 562and centered at 120 km depth (density contrast  $+30 \text{ kg m}^{-3}$ ) 563was able to match both the observed amplitude and wave-564length of observed Bouguer gravity data (-100 mGal). 565Support for the existence a cold subducting mantle is found 566 in teleseismic P waves arrivals recorded on two dense 567 profiles across the Southern Alps [Stern et al., 2000]. To 568569match the observed 1 s advance in P wave travel times, recorded from three teleseismic earthquakes, requires a 570high-speed body (up 7% velocity perturbation) extending 571to over 160 km depth. Using a larger set of teleseims, 572Kohler and Eberhart-Phillips [2002] are able to map a 573similar west dipping high-velocity sheet that varies from 60 574to 100 km in width and extends to  $\sim$ 180 km depth with a 575maximum 3% perturbation. Furthermore, a few well-located 576577mantle earthquakes have been recorded beneath the central 578Southern Alps at depths from 25 to 60 km deep (shown in Figure 5c) [*Reyners*, 1987]. They correspond to the faster 579 portion of the high-velocity zone determined from tele- 580 seismic *P* wave travel time inversion [*Kohler and Eber-* 581 *hart-Phillips*, 2002]. 582

[42] In section 4.2 we compare our "reference" model to 583 the observed topography and Moho in the Southern Alps. In 584 section 4.3 we discuss the role of lithospheric mantle 585 rheology, using additional models that were modified from 586 the reference model (Table 2). 587

588

#### 4.2. Comparison to the Seismic Moho and Gravity

[43] Figure 7 shows comparisons of the model and observed surface topography (Figure 7a) and Moho (Figure 7b) 590 across the Southern Alps. Since our models do not account 591 for progressive change in lithospheric rock composition, 592 away from the plate boundary, we are unable to match 593 these boundaries in the far field. Indeed, the modeled 594 topography is consistently higher than observed since 595 uniform uplift acts in our model by raising the entire 596 surface. Since the base level of topography corresponds 597 to a regional value, in isostatic equilibrium, the data in 598 Figure 7a therefore have 500 m subtracted so that far-field 599 data are at mean sea level 600

[44] The resultant Moho wavelength and depth are a good 601 match to the shape of the crustal root (Figure 7b) derived 602 from ray trace modeling. However, the model shows no 603 significant offset between maximum topography and deep- 604 est portion of the crustal root. In the present reference 605 model, it is even slightly to the east of the crustal root, 606 but in alternative models (not shown) with a slightly weaker 607 Australian upper crust, we obtain a maximum topography 608 located  $\sim 10$  km west of the crustal root. The cause for this 609 discrepancy of offset in the model, when compared to 610 observations is further discussed in section 4.6.

[45] Figure 7c shows the comparison between observed 612 and modeled gravity anomaly. The detail of gravity calcu-613 lation is given in Appendix A. One hundred milligals were 614 added to the overall modeled anomaly, which is again 615 justified by the fact that the modeled far field is in isostatic 616 equilibrium. The geodynamic models do not include preex-617 isting basins or paleobathymetry in the initial set up. 618 Therefore the comparison between the model gravity and 619 observed data does not match to the east of the central 620 gravity low, where the anomaly, owing to the presence of a 621 thick Cenozoic sedimentary basin [*Field and Browne*, 622 1989], is greatest. The mismatch in detail to the west of 623 the crustal root is most likely due to density variations in the 624 Australian crust. 625

[46] The density contrast (300 kg m<sup>-3</sup>) at the Moho 626 contributes to ~50% to the negative gravity anomaly, and 627 the upper and lower crust density contrast (250 kg m<sup>-3</sup>) 628 contributes ~30%. The reference model (gray line) has a 629 positive density contrast (50 kg m<sup>-3</sup>) across the lithosphere- 630 asthenosphere boundary that contributes a small (<10 mGal) 631 long-wavelength (>200 km) component to the gravity 632 anomaly. Figure 7c also shows an additional model in which 633 hydrostatic compensation at the base of the model is handled 634 with a negative density contrast. In this model the colder 635 mantle lithosphere is assigned a density of 3300 kg m<sup>-3</sup>, and 636 Archimede's force acts with a density equal to 3250 kg m<sup>-3</sup>. 637 Results from this model (dashed line in Figure 7c) show that 638 the Moho is deeper, by ~5 km, compared to Moho observed 639

by seismic velocity modeling, while the wavelength and 640 641 maximum amplitude of Bouguer anomaly remain the same as our reference model. These results suggest that a 10-20%642 643 change of density at the lithosphere-asthenosphere boundary is not diagnostic in fitting the observed gravity anomaly. 644 While density distribution at depths of transition from the 645 lithosphere to the asthenosphere remains difficult to resolve 646 with seismological data [e.g., Karato, 1993; Ishii and 647 Tromp, 1999; Sabadini et al., 2002], our result supports 648 the assumption of gravity modeling studies that use a 649 constant density distribution at these depths (e.g., Vacher 650and Souriau [2001] for the Pyrenees). 651

[47] On the other hand, the lithospheric root calculated 652from our modeling (center of mass at 80 km depth) is 653smaller than that delineated by Stern et al. [2000]. An 654655 accurate comparison with this work would require a test 656 of the dependency of density (and viscosity) on both increasing temperature and pressure with deforming mantle 657 lithosphere. If we are to model accurately the dynamics of 658 the lithosphere-asthenosphere in the Southern Alps, then the 659 depth of our modeling needs to be increased to 120 km, and 660 how compression applies down to such depth should also be 661 questioned. This additional modeling is beyond the scope of 662 this paper where we have chosen to focus on deformation of 663the crust and mantle lithosphere. 664

# 665 4.3. Remarks on the Rheology of the666 Lithospheric Mantle

[48] Lateral density contrasts and the geometry of rheo-667 logical boundaries between the Australian and Pacific plates 668 can clearly be a first-order cause of the direction of "mantle 669 subduction" in the Southern Alps of New Zealand. Howev-670 er, the mantle's strength and rate of strain softening are also 671 first-order controls on the geometry of mantle lithosphere 672 673 thickening, as recently illustrated by Pysklywec et al. [2000]. [49] There are several ways in which the strength of the 674 mantle lithosphere can vary. For example, a warmer geo-675 therm tends to induce lower viscosity, due to the tempera-676 ture-dependent power law constitutive behavior. Parameters 677 of the power law may vary when extrapolated to real mantle 678 depths, and other mechanisms of deformation than disloca-679 tion creep may even dominate [Karato, 1993] (see review 680 by Ranalli [1995]). The choice of dry versus wet olivine 681 creep parameters modifies the depth of the brittle-ductile 682 transition in the mantle lithosphere [e.g., Rannalli, 1995; 683 Pysklywec et al., 2002], and thus the thickness of its strong 684 685layer and, consequently, the length scale of mantle deflection are modified. As a consequence of the large uncertain-686 ties in a realistic constitutive law for the mantle lithosphere, 687 and after having tested about 300 models, we choose to 688 demonstrate the control of strength and strain softening in a 689 simple manner. Regardless of which mechanism controls 690 691the strength of the mantle lithosphere in detail, since maximum strength is bounded by both friction and cohe-692 sion, we prescribe zero friction and vary the cohesion (see 693 694 Table 1). However, this cohesion should not be considered as a physical cohesive value for rocks. 695

## 696 4.4. Effect of Lithospheric Mantle's Strength and697 Symmetry of its Deformation

[50] From a mechanical point of view, Moho topography(i.e., wavelength and amplitude) is dependent on the ability

of mantle lithosphere to deform. The stronger the lithospher- 700 ic mantle (either viscous or brittle), the easier it is to deflect 701 because it can support large internal stress contrasts respond- 702 ing to lateral loading. This is similar to the mechanism of 703 lithospheric folding [e.g., *Gerbault et al.*, 1999], in which the 704 strong mantle lithosphere (dark layer in Figure 4c) can 705 buckle "plastically" with a wavelength proportional to 706  $\sim$ 4–6 times its thickness, and an amplitude proportional to 707 its strength ratio with the surrounding layers. In contrast, a 708 mantle with relatively low viscosity deforms by uniform 709 viscous thickening. In this case the amplitude of localized 710 deformation is diminished, so that the crust is less affected 711 by deformation in the mantle. 712

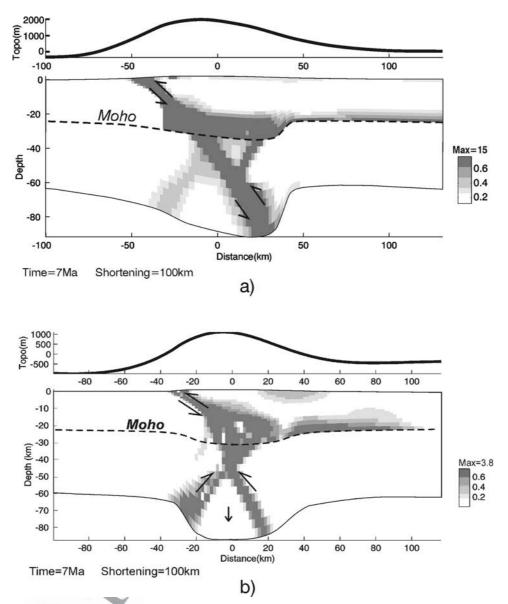
[51] Models were produced for mantle lithosphere 713 strength of 500 MPa (not shown). As expected, broad 714 flexure of the mantle lithosphere leads to broad surface 715 deformation. The secondary maximum of topography, men-716 tioned previously, tends to develop more easily, as it 717 coincides with flexural uplift of the mantle lithosphere. 718 [52] Figure 8 displays two models with an initial mantle 719 strength of 50 MPa, which reduces to 20 MPa by strain 720 softening (Table 2). In the first model (Figure 8a), the 721 "Australian" mantle underthrusts the "Pacific" mantle after 722 7 Myr of convergence. In the second model (Figure 8b), in 723 which the rate of strain softening has been increased and the 724 coefficient of erosion reduced (see Figure 8 caption for 725 values), two conjugate shear zones develop so that mantle 726 deformation remains symmetric. These models show that in 727 case the mantle lithosphere has a low strength (of the order 728 of magnitude of cohesion, 20 MPa), then the stress magni- 729 tude involved in lithospheric deformation compete with 730 stresses due to mass transfer at the surface. This is under-731 standable given the unpredictability of preferential move-732 ment along two conjugate thrust faults, which results from 733 local equilibrium in mass transfer along vertical columns. 734 However, none of our models with initial mantle strength of 735 50 MPa allow for a large width and amplitude of crustal 736 thickening because there is insufficient build up of stress to 737 support significant mantle lithosphere deflection. Models 738 with an initial mantle strength of 50 MPa produce a crustal 739 root  $\sim$ 50 km wide and <35 km deep, in contrast to models 740 with an initial strength >200 MPa, in which "Pacific plate" 741 subduction always develops. 742

[53] In our models, (a)symmetry of the crustal root devel-743 ops associated with (a)symmetry of entire lithospheric thick-744 ening. The symmetrical deformation of Figure 8b is in 745 agreement with indications from *P* wave delays for symmet-746 ric lithospheric thickening. However, the significantly 747 smaller shape of the Moho renders this model unsatisfactory. 748 More complex constitutive laws, such as temperature-depen-749 dent strain softening [*Zhang et al.*, 2000], may be required in 750 order to reproduce asymmetric crustal root and symmetric 751 mantle lithosphere thickening, as indicated by teleseismic 752 arrivals across the Southern Alps [*Stern et al.*, 2000]. 753

#### 4.5. Effect of Strain Softening

[54] Our models, together with other studies [*Pysklywec* 755 *et al.*, 2000; *Huismans and Beaumont*, 2002], show that if 756 strain softening is too rapid, deformation remains localized 757 over a narrower region than indicated by observations from 758 the Southern Alps. An extreme situation is that deformation 759 remains concentrated in the initial vertical zones of weak- 760

754



**Figure 8.** Models with mantle lithosphere strength of 50 MPa, reducing to 20 MPa, total shear strain (maximum in dark gray) and topography. (a) Model with strain softening in the range  $\varepsilon_s = [0.01;1]$ , and  $k_{er} = 1000 \text{ m}^2 \text{ yr}^{-1}$ ; underthrusting of the "Australian" mantle. (b) Model with strain softening in the range  $\varepsilon = 0.05-0.5$  and  $k_{er} = 500 \text{ m}^2 \text{ yr}^{-1}$ ; symmetric thickening of the mantle lithosphere. Because the lithospheric mantle has a small strength, amplitude and wavelength of Moho deflection are small.

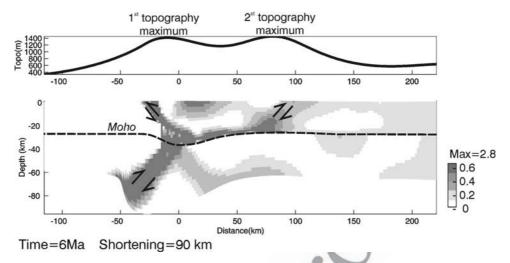
nesses. In contrast, if strain softening is imposed too slowly,
then lithospheric thickening is too broad. In the absence of
strain softening, large-scale folding of the Pacific mantle
develops.

[55] Models of initial mantle strength equal to 50 MPa 765 766 (Figure 8 and Table 2) illustrate the importance of strain 767softening on the geometry of mantle deformation. To further illustrate its effect on the width of the orogen for a stronger 768 mantle lithosphere, Figure 9 depicts the case where strain 769 softening is imposed more slowly than in the reference 770 model (reduction from 200 to 50 MPa after 200% of shear 771strain rather than 100%, Table 2). Broad surface deforma-772 tion occurs, with development of another maximum of 773 topography located  $\sim$ 120 km east of the Alpine Fault zone. 774Shear strain propagates to the east into the ductile lower 775

crust, and emerges to the surface via thrust faults: the 776 secondary maximum of topography becomes as high as 777 the primary one after 6 Myr of shortening. 778

#### 4.6. Discussion of S Point Models 779

[56] Uniform lithospheric thickening can be approximat- 780 ed by considering simple elastic compressibility: results of 781 models for a purely elastic lithosphere provide after 5 Myr 782 and 75 km of shortening, surface uplift  $y_t = 750$  m (uplift 783 rate of 0.15 mm yr<sup>-1</sup>) and bottom subsidence  $y_b = 2000$  m 784 (thickening of 4 mm yr<sup>-1</sup>). By assuming a linear depen- 785 dency of the vertical displacements with depth,  $D(y) = y_t + 786$  $(y_t - y_b)y/h_o$ , the depth at which material diverges upward 787 or downward (D(y) = 0) is found to be located at the 788 midcrustal depth S = 16.4 km. 789



**Figure 9.** Model with mantle lithosphere cohesion set at 200 MPa, with slower rate of strain softening (linear decrease from 200 to 50 MPa within the range  $\varepsilon_s = 0.1-2$ ). Deformation propagates "more" into the ductile lower crust, producing thrust faulting from  $X \sim 90-130$  km. As a result, the secondary maximum of topography reaches the same height as the primary one, after only 6 Myr of shortening.

[57] Plastic and viscous behaviors trigger heterogeneous 790 deformation that lead to continuous readjustment of the S 791 792 point position, through time and space: the S point evolves within the crustal root, and would be best represented by a 793 794diffuse zone, rather than a point. Our numerical models show that the present geometry of upper crustal deformation 795 in the Southern Alps is not very sensitive to the strength of 796 the mantle lithosphere, because it is <200 MPa (and under-797 goes sufficiently rapid strain softening). In this sense, 798 Beaumont et al.'s [1996] assumption of S point discontinu-799 ity at the base of the crust is a realistic approximation, as 800 long as interest is not in the shape of the base of the crust 801 and deeper deformation. 802

[58] In the present numerical models, the maximum of the 803 topography and the deepest part of the crustal root remain 804 on the same vertical axis (see Figure 7). The observed 805 806  $\sim 20$  km offset was never satisfactorily reproduced, despite 807 a large number of parametrical tests, including a variation of rheological properties, a varying coefficient of erosion 808 between west and east of the Main Divide, and a tuning 809 of strain softening coefficients. An offset of  $\sim 10$  km at best 810 was obtained when the friction angle for the Australian crust 811 is reduced to  $10^{\circ}$ , rather than  $30^{\circ}$ . The reason for the model 812 not producing significant offset of surface and crustal root 813 deformation may be that only diffusive surface processes 814 were taken into account in our models. When Beaumont et 815 al. [1996, model 9] account for strain softening and asym-816 metric erosion processes, a significant offset is obtained [see 817 also Willett, 1999]. However, we suggest that the achieve-818 ment of this offset by *Beaumont et al.* [1996] is probably 819 due to the overconstraint imposed by their basal velocity 820 821 discontinuity.

[59] The observation of increasing offset of the Bouguer gravity anomaly with respect to the plate boundary, toward the southeast, where compression and surface topography decrease, indicates that this offset may find its cause in the three dimensionality of the orogen. Recent 3-D numerical modeling [*Gerbault et al.*, 2002] supports the occurrence of southward ductile lateral flow within the lower crust and along the plate boundary. Crustal thickening tends to 829 develop toward the southeast, showing that the overall 830 deformation results from a tendency to equilibrate buoyancy 831 forces in both the vertical section and laterally, according to 832 pressure variations. This thickening results from the geom-833 etry of rheological discontinuities with respect to the orien-834 tation of the relative plate velocity vector, and coincides 835 with the shape of the Bouguer anomaly. 836

838

#### 5. Conclusion

[60] Our numerical models involve compression of the 839 entire continental lithosphere during the first 10 Myr of 840 orogenic growth. While the models presented are non- 841 unique, they are, nonetheless, the culmination of a number 842 of tests that provide a mechanism explaining within a single 843 self-consistent geodynamical framework to compare with 844 crustal deformation data from the Southern Alps of New 845 Zealand (surface structures, GPS, electrical conductivity, 846 seismic velocities). The modeling also demonstrates the 847 importance of the strength of the lithospheric mantle on 848 the geometry of the collision process. 849

[61] 1. Advection appears to be the main mechanism that 850 accounts for the deflection/uplift of isotherms after 7 Myr of 851 shortening (Figure 4b). This confirms the validity of the 852 thermokinematical approach of *Shi et al.* [1996]. 853

[62] 2. Crustal deformation is characterized by a major 854 shear zone that one can associate with the Alpine Fault, 855 which from being initially vertical, inclines to  $\sim 45^{\circ}$  and 856 curves at depth to merge with a ductile shear in the lower 857 crust (Figure 4e). This illustrates the inclination through 858 time of an initially vertical transcurrent shear zone, and is 859 consistent with 3-D modeling [*Gerbault et al.*, 2002]. 860

[63] 3. Flexure of the brittle upper crust above the crustal 861 root is responsible for faulting being concentrated 60–80 km 862 east from the Alpine Fault (Figure 5) and is coincident with 863 several active faults and with the boundary of the observed 864 U-shaped electrical conductor [*Wannamaker et al.*, 2002]. 865 The argument that midcrustal fluids accumulate in a locally 866

extended zone (less compressed) in the lower crust and then
migrate to the surface finds further support here in our
dynamical modeling.

[64] 4. Comparison with GPS data of horizontal conver-870 gence velocity shows that the change in slope at a distance 871 of 80-100 km from the Alpine Fault can be related to the 872 873 place where the upper crust detaches from the mantle lithosphere (Figures 5 and 6). The increase in velocity at 874 the Alpine Fault, in the model, is sharper than in GPS data, 875 because geodetic measurements account for short timescale 876 aseismic deformation. 877

[65] 5. As compression increases, flow in the ductile 878 lower crust propagates to the east, so that the upper crust 879 detaches from the lithospheric mantle. The tip of this ductile 880shear zone, located  $\sim 100-130$  km from the Alpine Fault, 881 882 can connect to thrust faults in the upper crust, and generate 883 surface uplift. This characteristic distance and the amount of surface uplift associated with it are not only dependent on 884 the (low) strength of the ductile lower crust but also on the 885 high strength of the lithospheric mantle (200 MPa). The 886 occurrence of mantle earthquakes beneath the South Island 887 may be controlled by large shear strain associated with 888 mantle subduction. In addition, the large strain modeled in 889 the crust and lithospheric mantle under the Southern Alps 890 may also generate heterogeneity that could be manifested as 891 seismic anisotropy. 892

[66] 6. The crustal root develops and resembles the image 893 obtained from seismic velocity models in the central South-894 895 ern Alps, with "subduction of Pacific" mantle. If the strength of the lithospheric mantle is weaker than 200 MPa, 896 the amplitude and wavelength of the crustal root are too 897 small (Figure 8). If the rate of softening is too slow then the 898 resulting surface deformation is too broad (Figure 9); a result 899 that was also demonstrated by Pysklywec et al. [2000, 2002]. 900 Satisfactory models with softening ranging from 200 to 901 50 MPa are consistent with a number of geophysical studies 902 that estimated maximum stress contrast that a lithosphere can 903 support [e.g., McNutt, 1980; Molnar and England, 1990; 904Gerbault, 2000]. The typical horizontal integrated force in 905our models is  $2-6 \ 10^{12}$  N m. 906

[67] 7. A satisfactory fit is obtained to the measured 907 gravity anomaly for our reference model, without needing 908 to account for denser mantle lithosphere [Stern, 1995; Stern 909 et al., 2000]. This difference, however, warrants further 910 investigation. The lithosphere-asthenosphere boundary in 911 912 our models was taken as a basal boundary condition, and 913 modeling the full dynamics of this zone requires extending our initial model to greater depth (at least 120 km). While 914915 numerical modeling such as that of *Pysklywec et al.* [2000, 2002] or Arnold et al. [2001] addresses the possible modes 916 of deformation at depths corresponding to the lithosphere-917 asthenosphere boundary, there is still a lot to learn from 918 worldwide variations in density, elastic parameters, and 919 viscosity at these depths [e.g., Karato, 1993; Ishii and 920 Tromp, 1999; Petrini et al., 2001; Sabadini et al., 2002]. 921 In relation to this, an appropriate constitutive law for the 922 upper mantle is still missing, while modeling confirms its 923control on the (a)symmetry of deformation (e.g., strain 924 softening of Huismans and Beaumont [2002]). Our model-925926ing indicates that for the Southern Alps, an asymmetric 927 crustal root but symmetric lithosphere thickening would 928 require more complex constitutive laws than those used here.

[68] 8. The 20 km offset between the maximum topogra- 929 phy and maximum depth of the crustal root were not 930 reproduced in the models, despite a number of parametric 931 tests. Because the observed Bouguer gravity low increases 932 progressively to the southeast and away from the plate 933 boundary, indicating that deep crustal thickening does not 934 strike parallel to the plate boundary, we suggest that the 935 dynamic equilibrium of the orogen is three dimensional. 936 Although many of the observed deformational structures at 937 an obliquely converging zone like the Southern Alps may 938 be modeled using 2-D orthogonal compression, structures 939 that do not strikeparallel require 3-D modeling. 940

[69] Finally, here we modeled the first stage of mountain 941 growth, also called the linear growth stage [e.g., *Shen et al.*, 942 2001]. At times greater than 10 Myr, several studies 943 emphasize the role of ductile, channel flow in the lower 944 crust in monitoring the lateral expansion of the orogen 945 [*Royden*, 1996; *Vanderhaeghe et al.*, 1999]. In our models, 946 the change in shear direction within the ductile lower crust 947 (see Figure 5) illustrates the complexity of ductile flow 948 processes at the edge of a continental orogen, in its initial 949 stages. 950

951

#### Appendix A: Numerical Method

[70] Algorithm Parovoz [*Poliakov and Podladchikov*, 952 1992] belongs to the fast Lagrangian analysis of continua 953 (FLAC) family [*Cundall and Board*, 1988; *Cundall*, 1989], 954 which is a large-strain fully explicit time-marching numer-955 ical algorithm exploiting the Lagrangian moving grid meth-956 od. The latter allows for solution of Newton's equation of 957 motion in large strain mode, holding a locally symmetric 958 small strain formulation commonly used in continuum 959 mechanics. The method can reproduce initialization and 960 evolution of nonpredefined faults (treated as large shear 961 bands). 962

[71] The time-marching scheme of the algorithm means 963 that one loop represents one time step, which must be small 964 enough to prevent the physical information propagating 965 from one element to its neighbor during this interval of 966 time. Each loop contains the following procedure: velocities 967 are calculated from Newton's law, with density  $\rho$ , time *t*, 968 velocity vector *v*, and gravity acceleration *g*: 969

$$\rho \delta v_i / \delta t = \delta \sigma_{ij} / \delta x_j + \rho g.$$

Components for the deformation rate are deduced from  $\varepsilon_{ij} = 971$ 1/2  $(\delta v_i / \delta x_i + \delta v_i / \delta x_i)$ . 972

[72] Brittle-elastic-viscous constitutive laws then provide 973 the stress distribution and equivalent forces  $\rho \delta v_i / \delta t$ , which in 974 turn provide input for the next time step. The algorithm 975 employs a dynamic relaxation technique based on the 976 introduction of artificial masses in the dynamic system, 977 permitting to handle strain localization. The adaptive 978 remeshing technique allows the models to be run up to 979 ~25% of total shortening. 980

[73] Brittle-elastic-viscous behavior is modeled so that 981 the minimum deviatoric stress produced by Mohr-Coulomb 982 elastoplasticity and Maxwell viscoelasticity is retained, at 983 each time step and for each element. Thus the brittle-ductile 984 transition is self-defined in the model and is referred to as 985 the depth at which the deviatoric shear stress becomes lower 986

than  $\sim 20$  MPa, regardless of which brittle or ductile 987 behavior actually dominates [e.g., Rannali, 1995]. The 988 failure criterion is reached when the relationship between 989 990 normal and tangential stresses,  $\sigma_n$  and  $\tau$ , along any given orientation equals  $\tau = S_0 - \tan \phi \sigma_n$ ,  $S_0$  being the cohesion 991 and  $\phi$  the friction angle for a given material property. 992 Dilatancy angle  $\psi = 0$ , so that nonassociated plasticity 993 occurs [see Vermeer, 1990]. 994

995 [74] Viscous behavior is prescribed by power law dislo-996 cation creep, and *Chen and Morgan's* [1990] expression of 997 the effective viscosity is used, with Q the activation energy, 998 *R* the gas constant, *A* the material constant, and *T* the 999 absolute temperature (see text for definitions of  $\sigma_s$  and  $\varepsilon_s$ ):

$$\mu^* = 1/4[4/(3A)]^{1/n} \varepsilon_s^{1/n-1} \exp(Q/nRt) = \sigma_s/2\varepsilon_s.$$

1001 When the stresses are evaluated, the increase in strain rate is 1002 greater than the decrease in effective viscosity, so that the 1003 shear stress actually increases in a shear zone. For this 1004 reason, in the Pacific crust, we introduce softening of the 1005 viscosity by a factor 10 within a certain range of the total 1006 shear strain  $\varepsilon_s$  (see Table 1).

[75] Extrapolation of the power law creep parameters for 1007 1008 olivine in the upper mantle lithosphere may provide greater 1009 shear stress than the Mohr-Coulomb yield stress. Since 1010 dominant deformation processes at mantle depth are poorly 1011 known, a number of studies then assume a brittle behavior 1012 [see Ranalli, 1995; Burov and Diament, 1995]. For this 1013 reason, we chose to empirically assign zero friction and test 1014 the cohesion for the mantle lithosphere. Also, we test 1015 cohesion strain softening of the mantle lithosphere, as it 1016 appears necessary to allow for localized thickening (see 1017 Table 1 for parameters and section 4.3). Pysklywec et al. 1018 [2002], for example, apply friction strain softening. Cohe-1019 sion or friction strain softening is achieved by reducing their 1020 value according to a linear equation that depends on the 1021 amount of total shear strain (see Table 1). Softening of 1022 friction angle in the Australian crust is introduced to allow 1023 deformation to propagate to the right of the modeled plate 1024 boundary, and allows the maximum of topography to 1025 develop to the right of the thickened crust. Softening of 1026 the viscosity of the Pacific crust allows the deformation to 1027 remain localized close to the plate boundary.

1028 [76] Temperature is updated through time. The heat flux 1029 through an element of volume is equal to the heat produced 1030 by internal sources plus the variation of volume. If heat is 1031 advected with velocity  $V_i$ , H is the heat production per unit 1032 mass, k is the thermal diffusivity, and  $\rho$  is the density, the 1033 general equation of heat is [*Ranalli*, 1995]

$$\partial T/\partial t + V_i \nabla T - k \nabla^2 T = \rho H.$$

1035 The initial continental temperature field is calculated 1036 according to the age-dependent procedure developed by 1037 *Burov and Diament* [1995], with a crustal heat production 1038  $H = H_s \exp - y/h_r$ ), and  $H_s = 9 \times 10^{-10}$  W kg<sup>-1</sup>,  $h_r = 10$  km, 1039 and crust and mantle thermal conductivities  $\kappa_c = \kappa_m = 3$  W 1040 K<sup>-1</sup> m<sup>-1</sup> ( $\kappa = k\rho C_p$ ,  $C_p = 1$  kJ kg<sup>-1</sup> K<sup>-1</sup> the specific heat). 1041 For a lithosphere of thermal age of 100 Ma, a temperature 1042  $T_b = 1350^{\circ}$ C at the base of the lithosphere  $h_1 = 60$  km, the 1043 resulting geotherm leads to the 600°C isotherm lying at  $\sim$ 25 km depth. After 7 Myr of shortening, the far-field 1044 surface heat flux is  $\sim$ 60 mW m<sup>-1</sup> K<sup>-1</sup>, increasing to 1045  $\sim$ 120 mW m<sup>-1</sup> K<sup>-1</sup> at the topography maximum. 1046

[77] Erosion and sedimentation processes are taken into 1047 account with a classic equation of diffusion. The equation of 1048 mass conservation is written in terms of a linear relationship 1049 between the variation of surface elevation *h* with time and 1050 the surface slope derivative. We adopt a constant value for 1051 the coefficient of diffusion  $k_{er}$  (set to 1000 m<sup>2</sup> yr<sup>-1</sup>), so that 1052  $\partial h/\partial t = k_{er}\partial^2 h/\partial x^2$ . If the area of an element increases by 1053 more than half of its initial value, then the element's 1054 "phase" switches to a "sediment" rheology (Table 1).

[78] The Bouguer gravity anomaly is modeled from the 1056 progressive displacement of layers since time 0 when the 1057 model is assumed to be in equilibrium with no anomaly. 1058 The gravity anomaly relates to the vertical displacement dz 1059 of element (*i*) of width dx located at the boundary between 1060 layers of different density  $\Delta\rho$ . Element (*i*) contributes to the 1061 gravity anomaly by  $dg_i = 2G \Delta\rho dx dz$ , where the gravitation 1062 tional constant  $G = 6.67 \times 10^{-11} \text{ m}^3 \text{ kg}^{-1} \text{ s}^{-2}$ .

[79] Each element (*k*) at the surface of the model is thus 1064 subjected to anomalous gravity acceleration created by the 1065 displacement of elements (*i*) that compose the layer bound-1066 ary (*l*) of contrasted density. Three layers (*l*) of contrasted 1067 density exist: the upper and lower crust boundary ( $\Delta \rho = 250$  1068 kg m<sup>-3</sup>), the crust and the mantle boundary at the Moho 1069 ( $\Delta \rho = 300$  kg m<sup>-3</sup>), and the base of the model ( $\Delta \rho = 1070$ 50 kg m<sup>-3</sup>). For elements (*i*) at depth  $z_i$ , located on (*l*), and 1071 with  $r_i$  the distance between (*k*) and (*i*): 1072

$$gb(k) = \sum_l \sum_i (dg_i \ z_i) / r_i^2.$$

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