

Oakhurst Primary School
Swindon
KS2 Mathematics
Calculation Policy



Number – addition and subtraction

Number – multiplication and division

- add numbers mentally, including:
- a three-digit number and ones
 - a three-digit number and tens
 - a three-digit number and hundreds

<p>Counting on</p> $115 + 2$ "Put 115 in your head, 116, 117" Partition number and recombine $127 + 90 = 100 + 20 + 7 + 90$ $= 100 + 110 + 7$ $= 100 + 117$ $= 217$	<p>Adding near numbers and adjusting</p> $433 + 90 = 433 + 100 - 10$ $= 533 - 10$ $= 523$ Count on by splitting units to make next multiple of ten/hundred $360 + 80 = 360 + 40 + 40$ $= 400 + 40$ $= 440$
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- two two-digit numbers (including answer crossing 100)

<p>Counting on with number lines</p> $48 + 36 = 84$ 	<p>Partition both numbers and recombine</p> $27 + 82 = 20 + 7 + 80 + 2$ $= 100 + 9$ $= 109$
<p>Add the nearest multiple of 10, then adjust</p> $63 + 59$ is the same as $63 + 60 - 1$	<p>Count on by partitioning the second number only</p> $36 + 93 = 93 + 30 + 6$ $= 123 + 6$ $= 129$

- subtract numbers mentally, including:
- a three-digit number and ones
 - a three-digit number and tens
 - a three-digit number and hundreds

<p>Counting back: $263 - 5$</p> <p>"Put 263 in your head, 262, 261, 260, 259, 258"</p> <p>Subtract mentally a near multiple of 10 to or from a two-digit number:</p> $678 - 90 = 678 - 100 + 10$	<p>Use unprepared numbered lines to subtract, by counting back</p> $516 - 400 = 116$
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- two two-digit numbers (including answer crossing 100)

<p>Use known number facts and place value to subtract (partition second number only)</p> $37 - 12 = 37 - 10 - 2$ $= 27 - 2$ $= 25$	<p>Find a small difference by counting up</p> $42 - 39 = 3$
<p>Subtract mentally a number near 10 to or from a two-digit number</p> $35 - 19 = 35 - 20 + 1$ 	

recall and use multiplication facts for the 3, 4 and 8 multiplication tables

Play games, chant, test etc to increase speed of recalling facts. Make models and images to display facts. Investigate patterns within tables.

understand and use mental methods using commutativity and associativity (for example, $4 \times 12 \times 5 = 4 \times 5 \times 12 = 20 \times 12 = 240$)

Use a variety of resources (including a calculator) to investigate order of multiplication. Make models and images to display facts.

understand and use mental methods using multiplication facts (e.g. using $3 \times 2 = 6$, $6 \div 3 = 2$ and $2 = 6 \div 3$) to derive related facts (e.g. $30 \times 2 = 60$, $60 \div 3 = 20$ and $20 = 60 \div 3$)

$30 \times 5 = 150$	$50 \times 3 = 150$	$150 \div 5 = 30$	$150 \div 3 = 50$
$3 \times 50 = 150$	$5 \times 3 = 15$	$15 \div 3 = 5$	$150 \div 30 = 5$
$5 \times 30 = 150$	$50 \times 30 = 1500$	$30 \times 50 = 1500$	$150 \div 50 = 3$

add numbers with up to three digits, using formal written methods of columnar addition (See Appendix 1)

<p>Column addition</p> $\begin{array}{r} 367 \\ +185 \\ \hline 552 \\ \hline 11 \end{array}$	<p>Vertical expansion</p> $\begin{array}{r} 367 \\ +185 \\ \hline 12 \\ 140 \\ 400 \\ \hline 552 \end{array}$
<p>Including money</p> $\begin{array}{r} £ 2.50 \\ + £ 1.75 \\ \hline £ 4.25 \\ \hline £ \end{array}$	

Use base 10 (diennes) or place value counters to support understanding of carrying and to ensure conceptual understanding of place value.

If children are experiencing persistent difficulties, they could use the partitioned column method with carrying (using diennes for support).

subtract numbers with up to three digits, using formal written methods of columnar subtraction (See Appendix 1)

Use base 10 (diennes) as a practical method to introduce exchanging

$31 - 18 = 13$

When pupil(s) are confident in doing this practically and verbalizing the calculation, begin to record using partitioned column method:

200	70	9
-	40	8
200	30	1

When secure with exchanging, use partitioned column method to solve calculations involving 3 digit numbers. Repeating the practical stage if necessary.

Introduce Column Subtraction without decomposition:

458
- 232
226

develop reliable written methods for multiplication, starting with calculations of two-digit numbers by one-digit numbers and progressing to the formal written methods of short multiplication

Start by reinforcing mental methods of partitioning:

$15 \times 2 = 30$

$13 \times 3 = (10 \times 3) + (3 \times 3) = 30 + 9 = 39$

Grid Method

1. Introduce the grid method by linking it to arrays initially (using counters)
2. Use base 10 (diennes) with grid method to support understanding of place value.
3. Use the grid method

13×4

13×4

40	12
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develop reliable written methods for division, starting with calculations of two-digit numbers by one-digit numbers and progressing to the formal written methods of short division

Use counters and a number line to support pupils understanding. Number lines: How many 3's make 18? Hoops and dots: $16 \div 2 = 8$

Move on to calculations that leave remainders and/or require tables knowledge: $15 \div 3 = 5$

When pupils have had experience with and demonstrated understanding of grouping for division, begin to look at short division with no remainders in the final answer.

Use counters/Diennes to support understanding.

3	2
3	9
2	6

Answer: 14

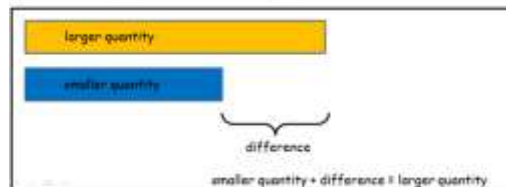
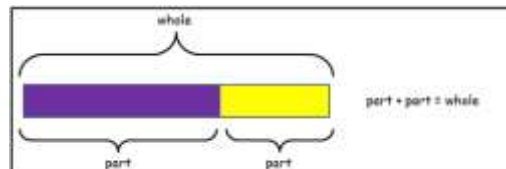
- 47
- +35
- 12
- 70
- 82

solve problems, including missing number problems, using number facts, place value, and more complex addition

Missing numbers should be placed in all possible places:
 $3 + 4 = \square$ $\square = 4 + 3$
 $3 + \square = 7$ $7 = \square + 4$
 $4 + \square = 7$ $7 = 3 + \square$
 $\square + \square = 7$ $7 = \square + \square$

Use all the models and images mentioned above. Discuss which is most effective and why.

Singapore Bar Method



estimate the answer to a calculation and use inverse operations to check answers

Estimate answers before solving any calculation.
Once inverse operation has been learnt use as a method for checking.

use a variety of language to describe addition

+, add, addition, more, plus, make, sum, total, altogether, score, double, near double, one more, two more... ten more... one hundred more, how many more to make...? how many more is... than...? how much more is...?

= equals, sign, is the same as

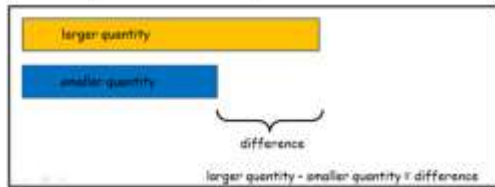
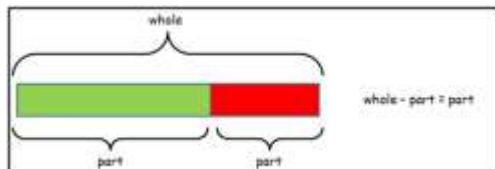
tens boundary, hundreds boundary

solve problems, including missing number problems, using number facts, place value, and more complex subtraction

Missing numbers should be placed in all possible places:
 $16 - 9 = \square$ $\square = 16 - 9$
 $16 - \square = 7$ $7 = \square - 9$
 $\square - 9 = 7$ $7 = 16 - \square$
 $\square - \square = 7$ $7 = \square - \square$

Use all the models and images mentioned above. Discuss which is most effective and why.

Singapore Bar Method



estimate the answer to a calculation and use inverse operations to check answers

Estimate answers before solving any calculation.
Once inverse operation has been learnt use as a method for checking.

use a variety of language to describe subtraction

- subtract, subtraction, take (away), minus, leave, how many are left/left over? one less, two less... ten less... one hundred less, how many fewer is... than...? how much less is...? difference between, half, halve

= equals, sign, is the same as

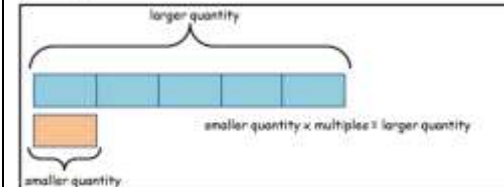
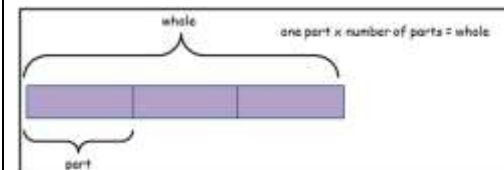
solve problems, including missing number problems, involving multiplication, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects
 solve simple problems in contexts, deciding which of the four operations to use and why

Missing numbers placed in all possible places.
 $7 \times 2 = \square$ $\square = 2 \times 7$
 $7 \times \square = 14$ $14 = \square \times 7$
 $\square \times 2 = 14$ $14 = 2 \times \square$
 $\square \times \square = 14$ $14 = \square \times \square$

Extend to
 $2 \times 6 = 3 \times \square$
 and using three numbers
 $10 \times \square \times \square = 60$ $12 = 2 \times \square \times 2$

Use all the models and images mentioned above. Discuss which is most effective and why.

Singapore Bar Method



write and calculate mathematical statements for multiplication using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods

See models and images above.

use a variety of language to describe multiplication

count, count (up) to, count on (from, to), count back (from, to), count in ones, twos, threes, fours, fives... count in tens, hundreds, lots of, groups of, times, multiply, multiplication, multiplied by, multiple of, product, once, twice, three times... ten times... times as (big, long, wide... and so on), repeated addition, array, row, column

= equals, sign, is the same as

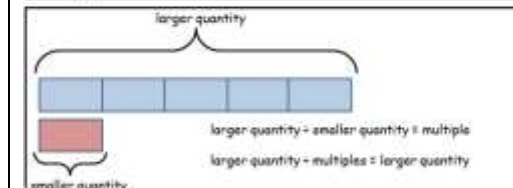
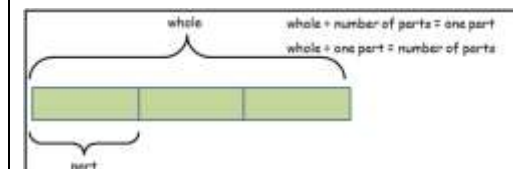
solve problems, including missing number problems, involving division, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects
 solve simple problems in contexts, deciding which of the four operations to use and why

Missing numbers placed in all possible places.
 $6 \div 2 = \square$ $\square = 6 \div 2$
 $6 \div \square = 3$ $3 = 6 \div \square$
 $\square \div 2 = 3$ $3 = \square \div 2$
 $\square \div \square = 3$ $3 = \square \div \square$

Extend to
 $12 = 6 \div 8 \div \square$
 and using three numbers
 $10 \div 5 \div \square = 1$ $3 = 12 \div \square \div 2$

Use all the models and images mentioned above. Discuss which is most effective and why.

Singapore Bar Method



write and calculate mathematical statements for division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods

See models and images above.

use a variety of language to describe division

Array, row, column, halve, share, share equally, one each, two each, three each... group in pairs, threes... tens, equal groups of, divide, division, divided by, divided into, left, left over, remainder

= equals, sign, is the same as

Number – addition and subtraction

Number – multiplication and division

add numbers mentally, including:

- a four-digit number and ones
- a four-digit number and tens
- a four-digit number and hundreds
- a four-digit number and thousands

Counting on 3115 + 2 "Put 3115 in your head, 3116, 3117."	Adding near numbers and adjusting 7433 + 90 = 7433 + 100 - 10 = 7533 - 10 = 7523
Partition, number and recombine 5127 + 2000 = 5000 + 100 + 20 + 7 + 2000 = 7000 + 100 + 20 + 7 = 7127	Count on by splitting units to make next multiple of ten/hundred 2360 + 500 = 2360 + 400 + 40 + 60 = 2400 + 400 + 60 = 2860

three and two-digit numbers

Partition both numbers into hundreds, tens and ones and recombine 358 + 72 = 300 + 50 + 8 + 70 + 2 = 300 + 120 + 11 = 420 + 11 = 431	Partition second number only into hundreds, tens and ones and recombine 358 + 72 = 358 + 70 + 2 = 428 + 3 = 431
Partitioning with number lines 	Add the nearest multiple of 10 or 100, then adjust 458 + 79 = 458 + 80 - 1

subtract numbers mentally, including:

- a four-digit number and ones
- a four-digit number and tens
- a four-digit number and hundreds
- a four-digit number and thousands

Counting back: 5263 - 5 "Put 5263 in your head, 5262, 5261, 5260, 5259, 5258."	Use unprepared numbered lines to subtract, by counting back: 1516 - 400 = 1116
Subtract mentally a 'near multiple of 10' to or from a two-digit number: 3678 - 90 = 3678 - 100 + 10	

three and two-digit numbers

Use known number facts and place value to subtract (partition second number only) 437 - 12 = 437 - 10 - 2 = 427 - 2 = 425	Find a small difference by counting up 6003 - 5998 = 5 +2 +3
Subtract mentally a number near 10 to or from a two-digit number: 425 - 2 = 423 427 - 10 = 417 437 - 10 = 427	Subtract mentally a number near 10 to or from a two-digit number: 305 - 19 = 305 - 20 + 1 = 285 + 1 = 286

add numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate (see Appendix 1)

Column addition

$$\begin{array}{r} 2358 \\ + 373 \\ \hline 2731 \\ 11 \end{array} \qquad \begin{array}{r} 4587 \\ + 2364 \\ \hline 6951 \\ 11 \end{array}$$

To ensure conceptual understanding, it is essential that place value is reinforced by frequently. Discussing the actual value of each digit, e.g. the 5 digit represents 5 hundreds.

Use base 10 (Diennes) or place value counters to support understanding of carrying and to ensure conceptual understanding of place value (see year 2 and 3 for how to use these manipulatives).

Including decimals

$$\begin{array}{r} 72.8 \\ + 54.6 \\ \hline 127.4 \\ 1 \end{array}$$

To ensure conceptual understanding, it is essential that place value is reinforced by frequently discussing the actual value of each digit, e.g. the 2 digit represents 2 tens.

Use money to support understanding.

subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate (see Appendix 1)

Revision of partitioned column method from Year 3. Moving on to numbers with 4 digits: (use Diennes to support when required.)

$$\begin{array}{r} 700 \ 20 \ 3 \\ 400 \ 50 \ 8 \\ 600 \ 110 \ 13 \\ 400 \ 50 \ 8 \\ \hline 200 \ 60 \ 5 \end{array}$$

Column Subtraction without decomposition

$$\begin{array}{r} 458 \\ - 232 \\ \hline 226 \end{array}$$

Column Subtraction with decomposition

Once pupils are confident in exchanging and have a clear understanding of place value, move towards the formal compact column method: (use Diennes to support when required.)

$$\begin{array}{r} 2 \overset{5}{\cancel{7}} 5 4 \\ - 1 5 6 2 \\ \hline 1 1 9 2 \end{array}$$

Model with base 10 when needed

recall multiplication facts for multiplication tables up to 12 x 12

Play games, chant, test etc to increase speed of recalling facts. Make models and images to display facts. Investigate patterns within tables.

Use place value, known and derived facts to multiply mentally, including: multiplying by 0 and 1; multiplying together three numbers

practise and extend mental methods to three-digit numbers to derive facts, (for example 600 ÷ 3 = 200 can be derived from 2 x 3 = 6)

Use knowledge of multiplication facts and place value to derive related facts.

$$\begin{array}{l} 30 \times 5 = 150 \quad 50 \times 3 = 150 \quad 150 \div 5 = 30 \quad 150 \div 3 = 50 \\ 3 \times 5 = 15 \quad 5 \times 3 = 15 \quad 15 \div 3 = 5 \\ 3 \times 50 = 150 \quad 5 \times 30 = 150 \quad 150 \div 30 = 5 \\ 5 \times 30 = 150 \quad 50 \times 30 = 1500 \quad 30 \times 50 = 1500 \quad 150 \div 50 = 3 \end{array}$$

Partition

$$18 \times 9 = (10 \times 9) + (8 \times 9) = 90 + 72 = 162$$

recognise and use commutativity in mental calculations

write statements about the equality of expressions (for example, use the distributive law $39 \times 7 = 30 \times 7 + 9 \times 7$ and associative law $(2 \times 3) \times 4 = 2 \times (3 \times 4)$)

Use a variety of resources (including a calculator) to investigate order of multiplication. Make models and images to display facts.

recall division facts for multiplication tables up to 12 x 12

Play games, chant, test etc to increase speed of recalling facts. Make models and images to display facts. Investigate patterns within tables.

Use place value, known and derived facts to divide mentally, including: dividing by 1 practise and extend mental methods to three-digit numbers to derive facts, (for example 600 ÷ 3 = 200 can be derived from 2 x 3 = 6)

Use knowledge of multiplication facts and place value to derive related facts.

$$\begin{array}{l} 30 \times 5 = 150 \quad 50 \times 3 = 150 \quad 150 \div 5 = 30 \quad 150 \div 3 = 50 \\ 3 \times 5 = 15 \quad 5 \times 3 = 15 \quad 15 \div 3 = 5 \\ 3 \times 50 = 150 \quad 5 \times 30 = 150 \quad 150 \div 30 = 5 \\ 5 \times 30 = 150 \quad 50 \times 30 = 1500 \quad 30 \times 50 = 1500 \quad 150 \div 50 = 3 \end{array}$$

Partitioning/Chunking

$$77 \div 5 = (50 \div 5) + (25 \div 5) + (\text{remainder } 2) = 10 + 5 + (\text{remainder } 2) = 15 \text{ remainder } 2$$

recognise and use factor pairs in mental calculations

Use a variety of resources (including a calculator) to investigate factor pairs. Make models and images to display facts.

multiply two-digit and three-digit numbers by a one-digit number using formal written layout (see Appendix 1)

Grid method

231 x 7 is approximately 200 x 10 = 2000

x	200	30	1
7	1400	210	7

Use of expanded method:

$$\begin{array}{r} 24 \\ \times 6 \\ \hline 24 \\ 120 \\ \hline 144 \end{array}$$

move onto formal method of short multiplication when proficient

$$\begin{array}{r} 452 \\ \times 3 \\ \hline 1356 \\ 1 \end{array}$$

divide numbers up to 3 digit by a one-digit number using the formal written method of short division and begin to interpret remainders.

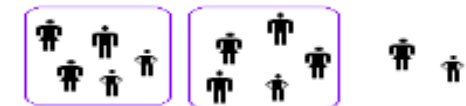
Short division with no remainders in the final answer, use place value counters/Diennes where support is required.

$$\begin{array}{r} 037 \\ 5 \overline{) 185} \\ \underline{5} \\ 18 \\ \underline{15} \\ 35 \\ \underline{35} \\ 0 \end{array} \qquad \begin{array}{r} 218 \\ 4 \overline{) 872} \\ \underline{8} \\ 7 \\ \underline{8} \\ 0 \end{array}$$

Remainders

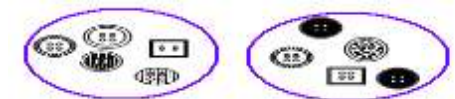
Begin to interpret remainders by looking at word problems to give context and small numbers to start with.

Cars carry 5 people. 12 people are going on a trip. How many cars will they need?

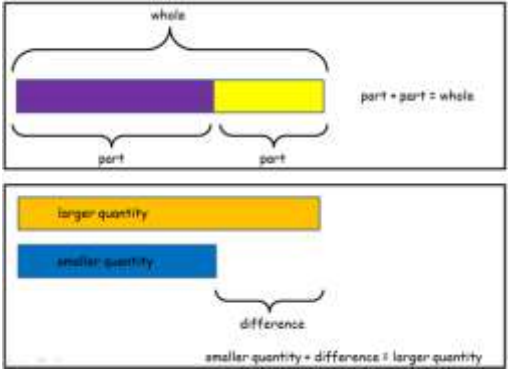
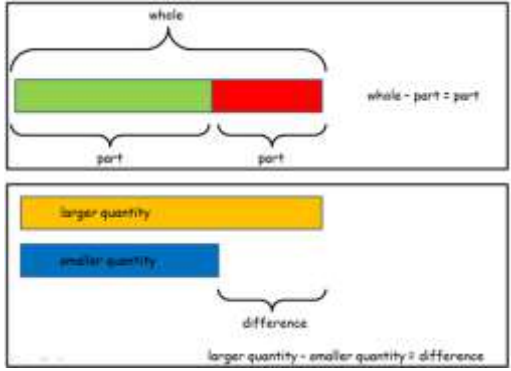
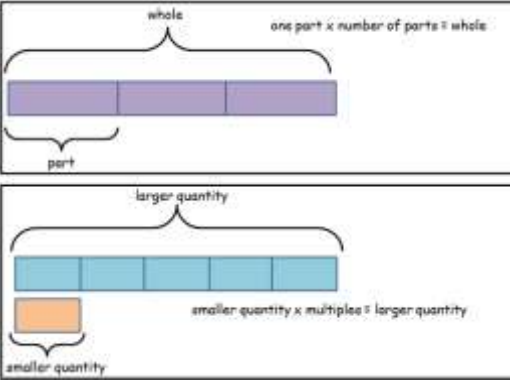
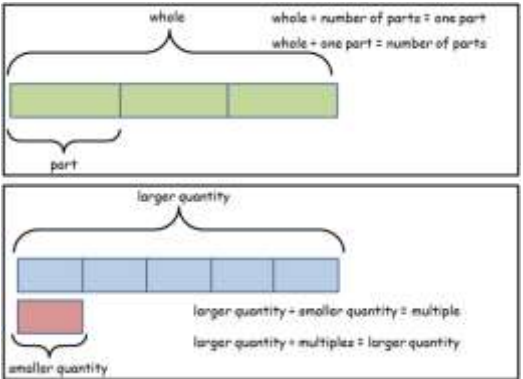


12 ÷ 5 = 2 r 2 So they would need 3 cars.

5 buttons are packed in a bag. How many full bags would there be if there were 12 buttons?



12 ÷ 5 = 2 r 2. So there are 2 full bags and 2 r 5

<p>solve addition two-step problems in contexts, deciding which operations and methods to use and why</p> <p>Use all the models and images mentioned above. Discuss which is most effective and why.</p> <p>Singapore Bar Method</p> 	<p>solve subtraction two-step problems in contexts, deciding which operations and methods to use and why</p> <p>Use all the models and images mentioned above. Discuss which is most effective and why.</p> <p>Singapore Bar Method</p> 	<p>solve problems involving multiplying and adding, including using the distributive law to multiply two digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects</p> <p>solve two-step problems in contexts, choosing the appropriate operation, working with increasingly harder numbers</p> <p>Use all the models and images mentioned above. Discuss which is most effective and why.</p> <p>Singapore Bar Method</p> 	<p>solve two-step problems in contexts, choosing the appropriate operation, working with increasingly harder numbers</p> <p>Use all the models and images mentioned above. Discuss which is most effective and why.</p> <p>Singapore Bar Method</p> 
<p>estimate and use inverse operations to check answers to a calculation</p> <p>Estimate answers before solving any calculation. Once inverse operation has been learnt use as a method for checking.</p>	<p>estimate and use inverse operations to check answers to a calculation</p> <p>Estimate answers before solving any calculation. Once inverse operation has been learnt use as a method for checking.</p>	<p>estimate and use inverse operations to check answers to a calculation</p> <p>Estimate answers before solving any calculation. Once inverse operation has been learnt use as a method for checking.</p>	<p>estimate and use inverse operations to check answers to a calculation</p> <p>Estimate answers before solving any calculation. Once inverse operation has been learnt use as a method for checking.</p>
<p>use a variety of language to describe addition</p> <p>+ add, addition, more, plus, increase, sum, total, altogether, score, double, near double, how many more to make...? tens boundary, hundreds boundary, inverse</p> <p>= equals, sign, is the same as</p>	<p>use a variety of language to describe subtraction</p> <p>- subtract, subtraction, take (away), minus, decrease, leave, how many are left/left over? difference between, half, halve, how many more/fewer is... than...? how much more/less is...? tens boundary, hundreds boundary, inverse</p> <p>= equals, sign, is the same as</p>	<p>use a variety of language to describe multiplication</p> <p>times, multiply, multiplication, multiplied by, multiple of, product once, twice, three times... ten times... times as (big, long, wide... and so on) repeated addition array, row, column, double, inverse</p> <p>= equals, sign, is the same as</p>	<p>use a variety of language to describe division</p> <p>Array, row, column, halve, share, share equally, one each, two each, three each... group in pairs, threes... tens. equal groups of, divide, division, divided by, divided into, remainder, factor, quotient, divisible by, inverse</p> <p>= equals, sign, is the same as</p>

Number – addition and subtraction

Number – multiplication and division

add numbers mentally with increasingly large numbers (e.g. 12 462 - 2300 = 10 162)

Partition both numbers and recombine

$$\begin{aligned} 2358 + 773 \\ = 2000 + 300 + 50 + 8 + 700 + 70 + 3 \\ = 2000 + 1000 + 120 + 11 \\ = 3000 + 100 + 30 + 1 \\ = 3131 \end{aligned}$$

Partitioning with number lines



Partition second number only into hundreds, tens and ones and recombine

$$\begin{aligned} 2358 + 773 &= 2358 + 700 + 70 + 3 \\ &= 3058 + 70 + 3 \\ &= 3128 + 3 \\ &= 3131 \end{aligned}$$

Add the nearest multiple of 10 or 100, then adjust

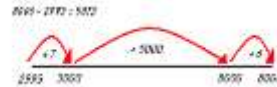
$$458 + 79 = 458 + 80 - 1$$

subtract numbers mentally with increasingly large numbers (e.g. 12 462 - 2300 = 10 162)

Subtract the nearest multiple of 10 or 100, then adjust

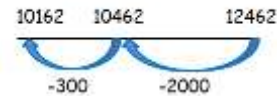
$$\begin{aligned} 458 - 79 &= 458 - 80 + 1 \\ &= 378 + 1 \\ &= 379 \end{aligned}$$

Find a difference by counting up



Use known number facts and place value to subtract (partition second number only)

$$\begin{aligned} 12\ 462 - 2300 \\ = 12\ 462 - 2000 - 300 \\ = 10\ 462 - 300 \\ = 10\ 162 \end{aligned}$$



multiply numbers mentally drawing upon known facts

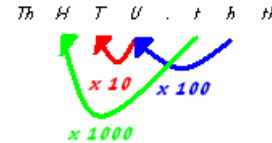
Partition

$$\begin{aligned} 47 \times 6 &= (40 \times 6) + (7 \times 6) \\ &= (240) + (42) \\ &= 282 \end{aligned}$$

Double and halve

$$25 \times 16 = 50 \times 8 = 100 \times 4 = 200 \times 2 = 400$$

multiply whole numbers and those involving decimals by 10, 100 and 1000



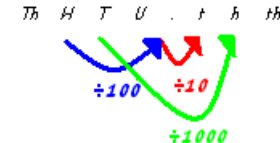
divide numbers mentally drawing upon known facts

Partitioning

$$\begin{aligned} 72 : 3 &= (60 : 3) = (12 : 3) \\ &= 20 + 4 \\ &= 24 \end{aligned}$$

divide whole numbers and those involving decimals by 10, 100 and 1000

Place Value



identify multiples, (and use them to construct equivalence statements, e.g. 4 x 35 = 2 x 2 x 35; 3 x 270 = 3 x 3 x 9 x 10 = 9^2 x 10)

Use a variety of resources (including a calculator) to investigate multiples. Make models and images to display facts.

identify factors, including finding all factor pairs of a number, and common factors of two numbers (and use them to construct equivalence statements, e.g. 4 x 35 = 2 x 2 x 35; 3 x 270 = 3 x 3 x 9 x 10 = 9^2 x 10)

Use a variety of resources (including a calculator) to investigate factors. Make models and images to display facts.

recall prime numbers up to 19
establish whether a number up to 100 is prime

Play games, chant, test etc to increase speed of recalling facts.
Make models and images to display facts.
Investigate patterns within primes.

recall prime numbers up to 19
establish whether a number up to 100 is prime

Play games, chant, test etc to increase speed of recalling facts.
Make models and images to display facts.
Investigate patterns within primes.

recognise and use square numbers and cube numbers, and the notation for squared (²) and cubed (³)

Use a variety of resources (including a calculator) to investigate square and cubed numbers. Make models and images to display facts.
Investigate the patterns within squared and cubed numbers.

add numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction - see Appendix 1)

Column addition

$$\begin{array}{r} 124.90 \\ + 117.25 \\ \hline 242.15 \\ \text{11} \end{array}$$

(add in a zero to keep the place value)

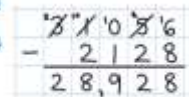
To ensure conceptual understanding, it is essential that place value is reinforced by frequently. Discuss the value of each digit. Use base 10 (Diennes) to support understanding of exchanging and to ensure conceptual understanding of place value. Where there is an 'empty' space in a decimal column, pupils should insert a zero to show the value. Children should be made aware that it is essential to align the columns carefully.

Pupils should be able to add more than 2 numbers using the compact column method.

$$\begin{array}{r} 3.25 \\ + 4.13 \\ \hline 0.76 \\ \hline 8.14 \\ \hline 11 \end{array}$$

subtract numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction - see Appendix 1)

Revision of formal compact column method extending to calculations involving numbers with more than 4 digits (use Diennes to support understanding of decomposition and place value).



When confident in using formal compact column method with integers and decimals involving money (always 2 decimal places), extend to subtraction with mixtures of integers and decimals. A clear understanding of place value is essential. Align the decimal point and use 'place holders', if needed.

$$\begin{array}{r} 263.0 \\ - 26.5 \\ \hline 236.5 \end{array}$$

Use Diennes or place value counters (add counters with 0.1) to support understanding of decomposition and place value.

multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers

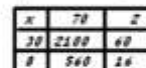
Review formal method of short multiplication (for multiplying by one digit numbers) when proficient

$$\begin{array}{r} 452 \\ \times 3 \\ \hline 1356 \end{array}$$

$$\begin{array}{r} 1243 \\ \times 8 \\ \hline 9924 \end{array}$$

Start with grid method when multiplying by 2 digit numbers

$$72 \times 38 \text{ is approximately } 70 \times 40 = 2800$$



$$\begin{array}{r} 2160 \\ + 576 \\ \hline 2736 \end{array}$$

Move onto formal long multiplication

$$\begin{array}{r} 34 \\ \times 13 \\ \hline 102 \\ 340 \\ \hline 442 \end{array}$$

Then formal multiplication with more complex numbers:

$$\begin{array}{r} 1234 \\ \times 16 \\ \hline 7404 \\ 12340 \\ \hline 19744 \end{array}$$

divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context (as fractions, as decimals or by rounding (for example, 98 ÷ 4 = 24 r 2 = 24 ½ = 24.5 = 25))

Bus shelter method (short division)

and 86 2/5

$$\begin{array}{r} 86r2 \\ 5 \overline{) 432} \\ \underline{20} \\ 23 \\ \underline{20} \\ 32 \\ \underline{30} \\ 2 \end{array}$$

Pupils should consider whether remainders should be left as a remainder, rounded to the nearest whole or converted into a decimal or fraction.

Introduce long division (dividing by single digits)

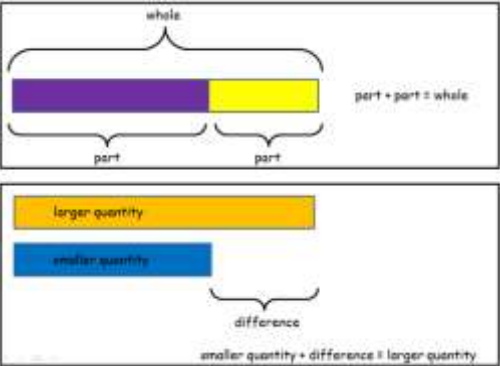
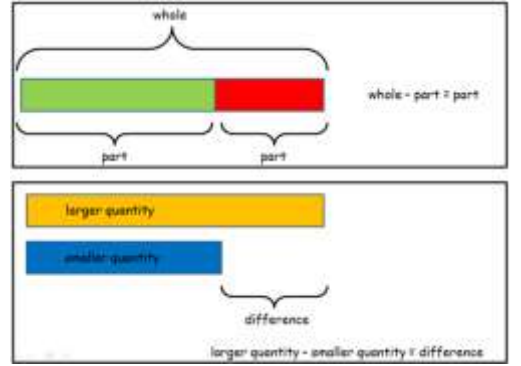
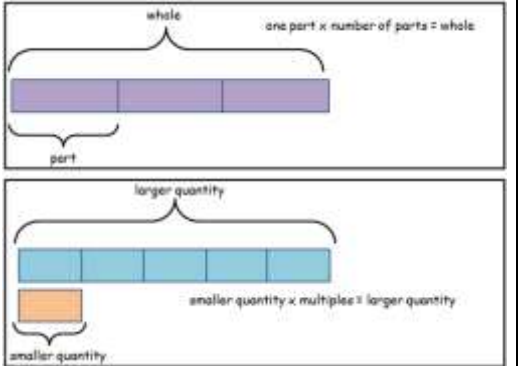
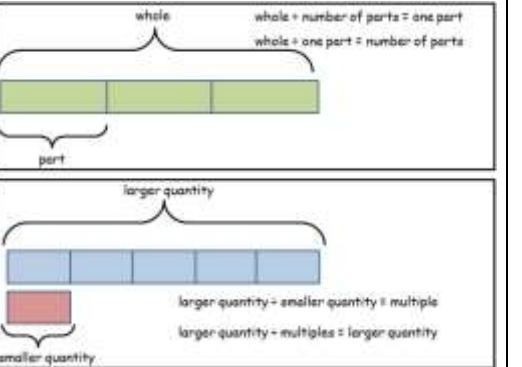
$$256 \div 7 \text{ lies between } 210 \div 7 = 30 \text{ and } 280 \div 7 = 40$$

$$\begin{array}{r} 256 \\ - 70 \\ \hline 186 \\ - 140 \\ \hline 46 \\ - 42 \\ \hline 4 \end{array}$$

(10 groups) or (10 x 7)
(20 groups) or (20 x 7)
(6 groups) or (6 x 7)
(36 groups) or (36)

Answer: 36 remainder 4

and 36 4/7

<p>solve addition multi-step problems in contexts, deciding which operations and methods to use and why</p> <p>Use all the models and images mentioned above. Discuss which is most effective and why.</p> <p>Singapore Bar Method</p> 	<p>solve subtraction multi-step problems in contexts, deciding which operations and methods to use and why</p> <p>Use all the models and images mentioned above. Discuss which is most effective and why.</p> <p>Singapore Bar Method</p> 	<p>Solve problems that use multiplication and division as inverses, for example, by multiplying and dividing by powers of 10 in scale drawings or by multiplying and dividing by powers of a 1000 in converting between units such as kilometres and metres</p> <p>Use all the models and images mentioned above. Discuss which is most effective and why.</p> <p>Singapore Bar Method</p>  <p>use and explain the equals sign to indicate equivalence, including missing number problems (e.g. $13+24 = 12+25$; $33 = 5 \times []$) express distributivity, for example as $a(b + c) = ab + ac$</p> <p>Use all of the models and images above to investigate a range of statements, ensuring the equals sign is in different positions. Allow time for discussion and reasoning. Display solutions and reasoning. Also use errors or misconceptions as a starting point.</p>	<p>Solve problems that use multiplication and division as inverses, for example, by multiplying and dividing by powers of 10 in scale drawings or by multiplying and dividing by powers of a 1000 in converting between units such as kilometres and metres</p> <p>Use all the models and images mentioned above. Discuss which is most effective and why.</p> <p>Singapore Bar Method</p>  <p>use and explain the equals sign to indicate equivalence, including missing number problems (e.g. $13+24 = 12+25$; $33 = 5 \times []$)</p> <p>Use all of the models and images above to investigate a range of statements, ensuring the equals sign is in different positions. Allow time for discussion and reasoning. Display solutions and reasoning. Also use errors or misconceptions as a starting point.</p>
<p>use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy</p> <p>Estimate answers before solving any calculation. Check against estimate after calculating (and use inverse check).</p>	<p>use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy</p> <p>Estimate answers before solving any calculation. Check against estimate after calculating (and use inverse check).</p>	<p>use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy</p> <p>Estimate answers before solving any calculation. Check against estimate after calculating (and use inverse check).</p>	<p>use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy</p> <p>Estimate answers before solving any calculation. Check against estimate after calculating (and use inverse check).</p>
<p>use a variety of language to describe addition</p> <p>+ add, addition, more, plus, increase, sum, total, altogether, score, double, near double, how many more to make...? tens boundary, hundreds boundary, units boundary, tenths boundary, inverse</p> <p>= equals, sign, is the same as</p>	<p>use a variety of language to describe subtraction</p> <p>- subtract, subtraction, take (away), minus, decrease, leave, how many are left/left over? difference between, half, halve, how many more/fewer is... than...? how much more/less is...? tens boundary, hundreds boundary, units boundary, tenths boundary, inverse</p> <p>= equals, sign, is the same as</p>	<p>use a variety of language to describe multiplication</p> <p>know and use the vocabulary of prime numbers, prime factors and composite (nonprime) numbers</p> <p>lots of, groups of, times, multiply, multiplication, multiplied by, multiple of, product, once, twice, three times... ten times... times as (big, long, wide... and so on), repeated addition, array, row, column, double,, inverse, prime,</p> <p>equals, sign, is the same as</p>	<p>use a variety of language to describe division</p> <p>Array, row, column, halve, share, share equally one each, two each, three each... group in pairs, threes... tens, equal groups of, divide, division, divided by, divided into, remainder, factor, quotient, divisible by, inverse, Prime, factors</p> <p>equals, sign, is the same as</p>

Number – addition and subtraction

Number – multiplication and division

perform mental calculations, including with mixed operations and large numbers (and decimals)

Partition both numbers into hundreds, tens, ones and decimal fractions and recombine

$$35.8 + 7.3 = 30 + 5 + 0.8 + 7 + 0.3$$

$$= 30 + 12 + 1.1$$

$$= 42 + 1.1$$

$$= 43.1$$

Partition second number only into hundreds, tens, ones and decimal fractions and recombine

$$35.8 + 7.3 = 35.8 + 7 + 0.3$$

$$= 42.8 + 0.3$$

$$= 43.1$$

Add the nearest whole number then adjust


$$52 + 11.9 = 52 + 12 - 0.1$$

$$= 64 - 0.1$$

$$= 63.9$$

practise addition for larger numbers, using the formal written methods of columnar addition (see Appendix 1)

Extend the use of compact column method to adding several numbers with mixed decimals.

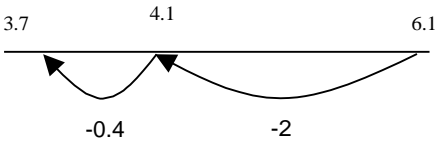


Children should be reminded of the importance of aligning the columns accurately.

Where there is an 'empty' space in a decimal column, pupils could insert a zero to show the value.

perform mental calculations, including with mixed operations and large numbers (and decimals)

Use known number facts and place value to subtract

$$6.1 - 2.4 = 3.7$$


Subtract the nearest whole number then adjust

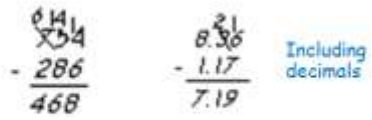
$$52 - 11.9 = 52 - 12 + 0.1$$

$$= 40 + 0.1$$

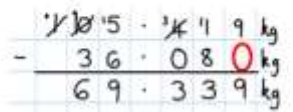
$$= 40.1$$

practise subtraction for larger numbers, using the formal written methods of columnar subtraction (see Appendix 1)

Column Subtraction with decomposition



Revision of formal compact column method extending to more complex integers and applying to problem solving using money and measures, including decimals with different numbers of decimal places. Align the decimal point when setting out calculations. Use 'place holders' to aid understanding of the value in that column.



perform mental calculations, including with mixed operations and large numbers (and decimals)

Partitioning

$$4.7 \times 6 = (4 \times 6) + (0.7 \times 6)$$

$$= (24) + (4.2)$$

$$= 28.2$$

Double and halve

$$4.25 \times 32 = 8.5 \times 16$$

$$= 17 \times 8$$

$$= 34 \times 4$$

$$= 68 \times 2$$

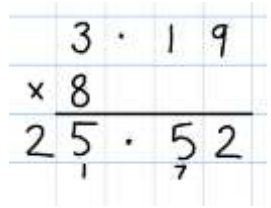
$$= 136$$

identify common factors, common multiples and prime numbers

Use a variety of resources (including a calculator) to investigate common factors, common multiples and prime numbers. Make models and images to display facts. Investigate the patterns within the numbers.

multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of short and long multiplication (Appendix 1)

Short multiplication and Long multiplication as in Year 5, but apply to numbers with decimals.



Pupils may need reminding that single digits belong in the ones (units) column. A sound understanding of place value and the formal method itself are required before progressing to decimal multiplication.

perform mental calculations, including with mixed operations and large numbers (and decimals)

Partitioning

$$7.2 \div 3 = (6 \div 3) = (1.2 \div 3)$$

$$= 2 + 0.4$$

$$= 2.4$$


identify common factors, common multiples and prime numbers

Use a variety of resources (including a calculator) to investigate common factors, common multiples and prime numbers. Make models and images to display facts. Investigate the patterns within the numbers.

divide numbers up to 4 digits by a two-digit whole number using the formal written method of short and long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context (Appendix 1)

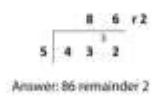
Short division

98 ÷ 7 becomes



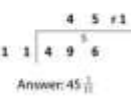
Answer: 14

432 ÷ 5 becomes



Answer: 86 remainder 2

496 ÷ 11 becomes

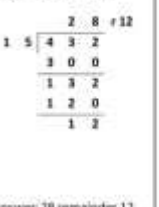


Answer: 45

Long division (for dividing by 2 digits)

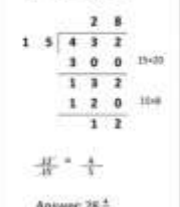
Long division

432 ÷ 15 becomes



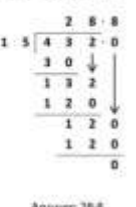
Answer: 28 remainder 12

432 ÷ 15 becomes



Answer: 28 $\frac{2}{5}$

432 ÷ 15 becomes

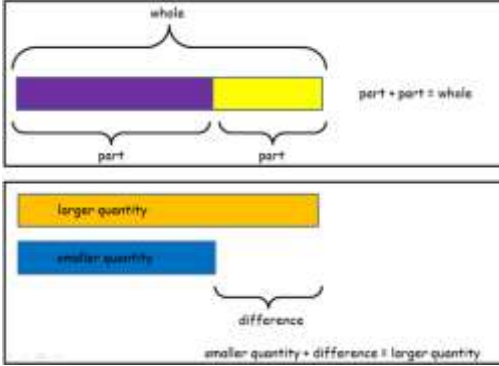
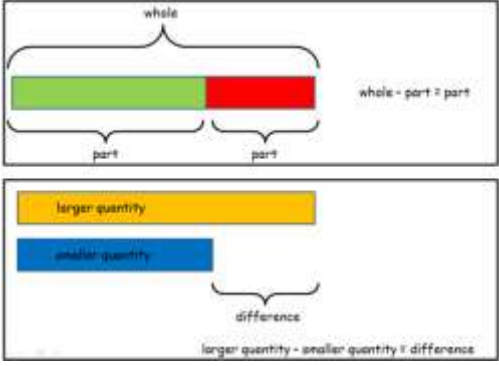
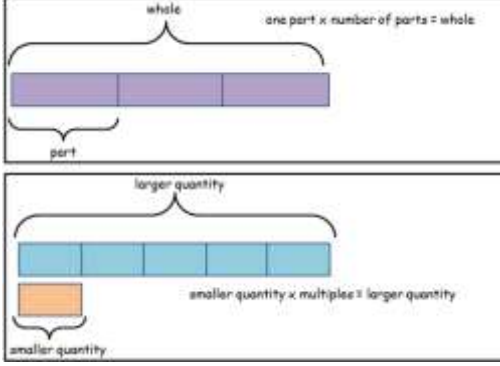
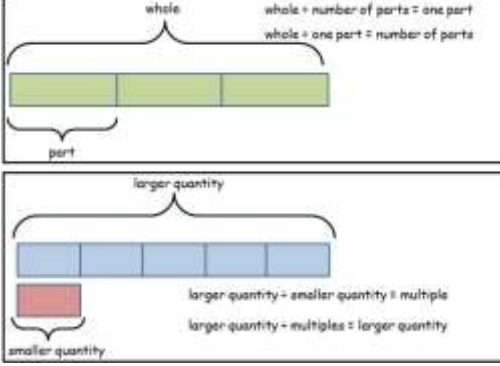


Answer: 28.8

Remainders

Quotients expressed as fractions or decimal fractions

$$61 \div 4 = 15 \frac{1}{4} \text{ or } 15.25$$

<p>solve addition multi-step problems in contexts, deciding which operations and methods to use and why</p> <p>Use all the models and images mentioned above. Discuss which is most effective and why.</p> <p>Singapore Bar Method</p> 	<p>solve subtraction multi-step problems in contexts, deciding which operations and methods to use and why</p> <p>Use all the models and images mentioned above. Discuss which is most effective and why.</p> <p>Singapore Bar Method</p> 	<p>solve problems involving multiplication</p> <p>Use all the models and images mentioned above. Discuss which is most effective and why.</p> <p>Singapore Bar Method</p> 	<p>solve problems involving division</p> <p>Use all the models and images mentioned above. Discuss which is most effective and why.</p> <p>Singapore Bar Method</p> 
<p>round answers to a specified degree of accuracy, e.g. to the nearest 10, 20, 50 etc., but not to a specified number of significant figures</p> <p>Use knowledge of rounding (see fraction Policy) to create estimates.</p>	<p>round answers to a specified degree of accuracy, e.g. to the nearest 10, 20, 50 etc., but not to a specified number of significant figures</p> <p>Use knowledge of rounding (see fraction Policy) to create estimates.</p>	<p>round answers to a specified degree of accuracy, for example, to the nearest 10, 20, 50 etc., (not to specified number of significant figures)</p> <p>Use knowledge of rounding (see fraction Policy) to create estimates.</p>	<p>round answers to a specified degree of accuracy, e.g. to the nearest 10, 20, 50 etc., but not to a specified number of significant figures</p> <p>Use knowledge of rounding (see fraction Policy) to create estimates.</p>
<p>use their knowledge of the order of operations to carry out calculations involving the four operations explore the order of operations using brackets; for example, $2 + 1 \times 3 = 5$ and $(2 + 1) \times 3 = 9$</p> <p>Review and investigate the effect of carrying out operations in different orders. Explore the effect. Introduce and use BODMAS to solve calculations.</p>	<p>use their knowledge of the order of operations to carry out calculations involving the four operations explore the order of operations using brackets; for example, $2 + 1 \times 3 = 5$ and $(2 + 1) \times 3 = 9$</p> <p>Review and investigate the effect of carrying out operations in different orders. Explore the effect. Introduce and use BODMAS to solve calculations.</p>	<p>use their knowledge of the order of operations to carry out calculations involving the four operations explore the order of operations using brackets; for example, $2 + 1 \times 3 = 5$ and $(2 + 1) \times 3 = 9$</p> <p>Review and investigate the effect of carrying out operations in different orders. Explore the effect. Introduce and use BODMAS to solve calculations.</p>	<p>use their knowledge of the order of operations to carry out calculations involving the four operations explore the order of operations using brackets; for example, $2 + 1 \times 3 = 5$ and $(2 + 1) \times 3 = 9$</p> <p>Review and investigate the effect of carrying out operations in different orders. Explore the effect. Introduce and use BODMAS to solve calculations.</p>
<p>use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy</p> <p>Estimate answers before solving any calculation. Check against estimate after calculating (and use inverse check).</p>	<p>use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy</p> <p>Estimate answers before solving any calculation. Check against estimate after calculating (and use inverse check).</p>	<p>use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy</p> <p>Estimate answers before solving any calculation. Check against estimate after calculating (and use inverse check).</p>	<p>use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy</p> <p>Estimate answers before solving any calculation. Check against estimate after calculating (and use inverse check).</p>
<p>use a variety of language to describe addition</p> <p>+ add, addition, more, plus, increase, sum, total, altogether, score, double, near double, how many more to make...? tens boundary, hundreds boundary, units boundary, tenths boundary, inverse</p> <p>= equals, sign, is the same as</p>	<p>use a variety of language to describe subtraction</p> <p>- subtract, subtraction, take (away), minus, decrease, leave, how many are left/left over? difference between, half, halve, how many more/fewer is... than...? how much more/less is...? tens boundary, hundreds boundary, units boundary, tenths boundary, inverse</p> <p>= equals, sign, is the same as</p>	<p>use a variety of language to describe multiplication</p> <p>x lots of, groups of, times, multiply, multiplication, multiplied by, multiple of, product, once, twice, three times... ten times... times as (big, long, wide... and so on), repeated addition, array, row, column double, inverse</p> <p>= equals, sign, is the same as</p>	<p>use a variety of language to describe division</p> <p>Array, row, column, halve, share, share equally one each, two each, three each... group in pairs, threes... tens, equal groups of, divide, division, divided by, divided into, remainder, factor, quotient, divisible by, inverse</p> <p>= equals, sign, is the same as</p>

