



# **AS Level Mathematics A**

**H230/02** Pure Mathematics and Mechanics Sample Question Paper

# Date - Morning/Afternoon

Time allowed: 1 hour 30 minutes

#### You must have:

· Printed Answer Booklet

#### You may use:

· a scientific or graphical calculator



# **INSTRUCTIONS**

- Use black ink. HB pencil may be used for graphs and diagrams only.
- Complete the boxes provided on the Printed Answer Booklet with your name, centre number and candidate number.
- Answer all the questions.
- Write your answer to each question in the space provided in the Printed Answer Booklet. Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do not write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.
- The acceleration due to gravity is denoted by  $gm s^{-2}$ . Unless otherwise instructed, when a numerical value is needed, use q = 9.8.

### **INFORMATION**

- The total number of marks for this paper is **75**.
- The marks for each question are shown in brackets [ ].
- · You are reminded of the need for clear presentation in your answers.
- The Printed Answer Booklet consists of 12 pages. The Question Paper consists of 8 pages.

# Formulae AS Level Mathematics A (H230)

# **Binomial series**

$$(a+b)^{n} = a^{n} + {}^{n}C_{1} a^{n-1}b + {}^{n}C_{2} a^{n-2}b^{2} + \dots + {}^{n}C_{r} a^{n-r}b^{r} + \dots + b^{n} \qquad (n \in \mathbb{N}),$$
where  ${}^{n}C_{r} = {}_{n}C_{r} = \binom{n}{r} = \frac{n!}{r!(n-r)!}$ 

# Differentiation from first principles

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

# **Standard deviation**

$$\sqrt{\frac{\Sigma(x-\overline{x})^2}{n}} = \sqrt{\frac{\Sigma x^2}{n} - \overline{x}^2} \text{ or } \sqrt{\frac{\Sigma f(x-\overline{x})^2}{\Sigma f}} = \sqrt{\frac{\Sigma f x^2}{\Sigma f} - \overline{x}^2}$$

# The binomial distribution

If 
$$X \sim B(n, p)$$
 then  $P(X = x) = \binom{n}{x} p^x (1-p)^{n-x}$ , Mean of  $X$  is  $np$ , Variance of  $X$  is  $np(1-p)$ 

# **Kinematics**

$$v = u + at$$

$$s = ut + \frac{1}{2}at^2$$

$$s = \frac{1}{2}(u+v)t$$

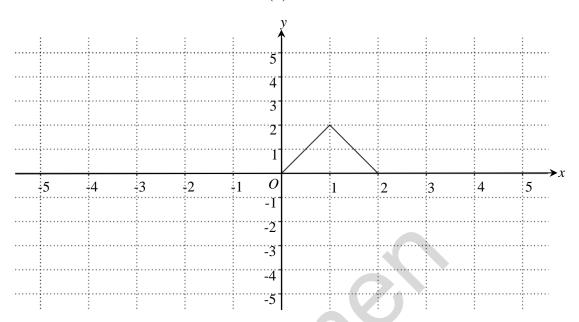
$$v^2 = u^2 + 2as$$

$$s = vt - \frac{1}{2}at^2$$

### **Section A: Pure Mathematics**

Answer **all** the questions

1 (i) The diagram below shows the graph of y = f(x).



- (a) On the diagram in the Printed Answer Booklet draw the graph of y = f(x+3). [2]
- (b) Describe fully the transformation which transforms the graph of y = f(x) to the graph of y = -f(x).
- (ii) The point (2, 3) lies on the graph of y = g(x). State the coordinates of its image when y = g(x) is transformed to

(a) 
$$y = 4g(x)$$
, [1]

**(b)** 
$$y = g(4x)$$
.

2 In this question you must show detailed reasoning.

Solve the equation  $2\cos^2 x = 2 - \sin x$  for  $0^\circ \le x \le 180^\circ$ . [5]

- 3 The number of members of a social networking site is modelled by  $m = 150e^{2t}$ , where m is the number of members and t is time in weeks after the launch of the site.
  - (i) State what this model implies about the relationship between m and the rate of change of m. [2]
  - (ii) What is the significance of the integer 150 in the model? [1]
  - (iii) Find the week in which the model predicts that the number of members first exceeds 60 000. [3]
  - (iv) The social networking site only expects to attract 60 000 members. Suggest how the model could be refined to take account of this. [1]
- 4 The points A, B and C have position vectors  $\begin{pmatrix} -2\\1 \end{pmatrix}$ ,  $\begin{pmatrix} 2\\5 \end{pmatrix}$  and  $\begin{pmatrix} 6\\3 \end{pmatrix}$  respectively. M is the midpoint of BC.
  - (i) Find the position vector of the point *D* such that  $\overrightarrow{BC} = \overrightarrow{AD}$ .
  - (ii) Find the magnitude of  $\overrightarrow{AM}$ .

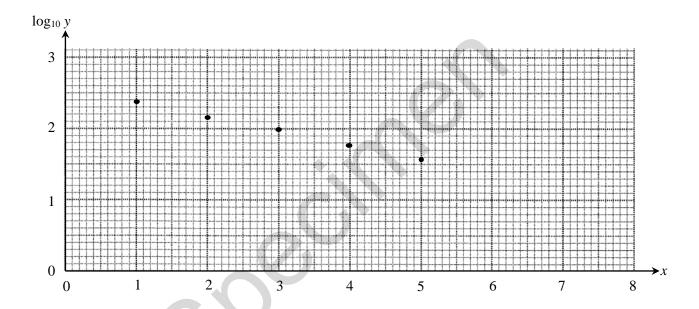
A doctors' surgery starts a campaign to reduce missed appointments. The number of missed appointments for each of the first five weeks after the start of the campaign is shown below.

Number of weeks after	1	2	3	4	5
the start $(x)$					
Number of missed	235	149	99	59	38
appointments (y)					

It was felt that this data could be modelled by an equation of the form  $y = pq^x$  where p and q are constants.

(i) Show that this relationship may be expressed in the form  $\log_{10} y = mx + c$ , expressing m and c in terms of p and/or q. [2]

The diagram below shows  $\log_{10} y$  plotted against x, for the given data.



(ii) Estimate the values of p and q. [3]

(iii) Use the model to predict when the number of missed appointments will fall below 20. Explain why this answer may not be reliable. [2]

(i) A student suggests that, for any prime number between 20 and 40, when its digits are squared and then added, the sum is odd. For example, 23 has digits 2 and 3 which gives 2² + 3² = 13, which is odd. Show by counter example that this suggestion is false.

(ii) Prove that the sum of the squares of any three consecutive positive integers cannot be divided by 3. [3]

7 Differentiate  $f(x) = x^4$  from first principles. [5]

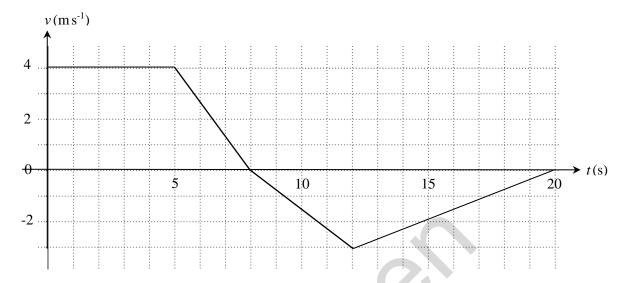
A curve has equation  $y = kx^{\frac{3}{2}}$  where k is a constant. The point P on the curve has x-coordinate 4. The normal to the curve at P is parallel to the line 2x + 3y = 0 and meets the x-axis at the point Q. The line PQ is the radius of a circle centre P.

Show that  $k = \frac{1}{2}$ . Find the equation of the circle.



# **Section B: Mechanics** Answer **all** the questions

The diagram below shows the velocity-time graph of a car moving along a straight road, where  $v \text{ m s}^{-1}$  is the velocity of the car at time t s after it passes through the point A.



(i) Calculate the acceleration of the car at t = 6.

[2]

- (ii) Jasmit says "The distance travelled by the car during the first 20 seconds of the car's motion is more than five times its displacement from A after the first 20 seconds of the car's motion". Give evidence to support Jasmit's statement. [3]
- A student is attempting to model the flight of a boomerang. She throws the boomerang from a fixed point O and catches it when it returns to O. She suggests the model for the displacement, s metres, after t seconds is given by  $s = 9t^2 \frac{3}{2}t^3$ ,  $0 \le t \le 6$ . For this model

(i) determine what happens at 
$$t = 6$$
,

[2]

(ii) find the greatest displacement of the boomerang from O,

[4]

(iii) find the velocity of the boomerang 1 second before the student catches it,

- [2]
- (iv) find the acceleration of the boomerang 1 second before the student catches it.

[2]

11 In this question the unit vectors **i** and **j** are in the directions east and north respectively.

Distance is measured in metres and time in seconds.

A ship of mass  $100\,000\,\mathrm{kg}$  is being towed by two tug boats. The cables attaching each tug to the ship are horizontal. One tug produces a force of  $(350\mathbf{i} + 400\mathbf{j})\,\mathrm{N}$  and the other tug produces a force of  $(250\mathbf{i} - 400\mathbf{j})\,\mathrm{N}$ . The total resistance to motion is  $200\,\mathrm{N}$ . At the instant when the tugs begin to tow the ship, it is moving east at a speed of  $1.5\,\mathrm{m\,s^{-1}}$ .

(i) Explain why the ship continues to move directly east. [2]

(ii) Find the acceleration of the ship. [2]

(iii) Find the time which the ship takes to move 400 m while it is being towed. Find its speed after moving that distance. [6]

# END OF QUESTION PAPER

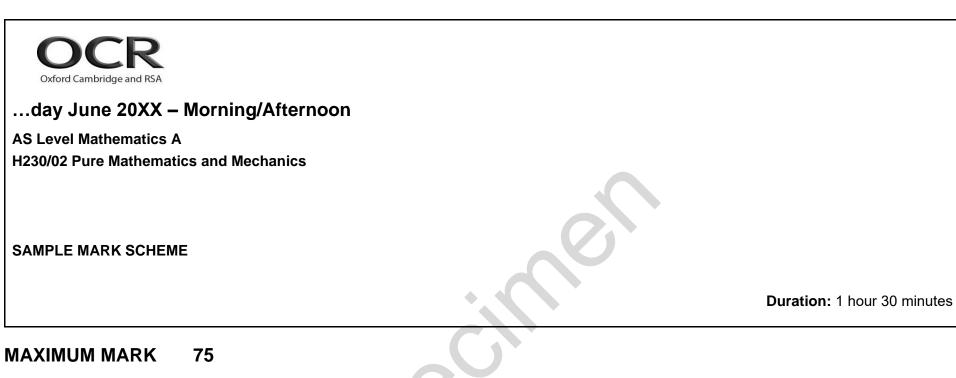
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This document consists of 12 pages

# **Text Instructions**

# 1. Annotations and abbreviations

Annotation in scoris	Meaning
√and <b>≭</b>	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
۸	Omission sign
MR	Misread
Highlighting	
Other abbreviations in	Meaning
mark scheme	
E1	Mark for explaining a result or establishing a given result
dep*	Mark dependent on a previous mark, indicated by *
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working
AG	Answer given
awrt	Anything which rounds to
BC	By Calculator
DR	This question included the instruction: In this question you must show detailed reasoning.

# 2. Subject-specific Marking Instructions for AS Level Mathematics A

- a Annotations should be used whenever appropriate during your marking. The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
- An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

  If you are in any doubt whatsoever you should contact your Team Leader.
- c The following types of marks are available.

#### М

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

#### Α

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

#### В

Mark for a correct result or statement independent of Method marks.

### Ε

Mark for explaining a result or establishing a given result. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep\*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

  Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.
- f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.) We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so. When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case. When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f. Follow through should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination. There is no penalty for using a wrong value for g. E marks will be lost except when results agree to the accuracy required in the question.
- Rules for replaced work: if a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others. NB Follow these maths-specific instructions rather than those in the assessor handbook.
- h For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. 'Fresh starts' will not affect an earlier decision about a misread. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.
- i If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
- j If in any case the scheme operates with considerable unfairness consult your Team Leader.

	Questic	on	Answer	Marks	AOs	Guidar	ıce
1	(i)	(a)		M1	1.1	A horizontal translation only is seen	
			Coordinates $(-3, 0)$ , $(-1, 0)$ and $(-2, 2)$	<b>A1</b>	1.1		
			seen				
				[2]			
1	(i)	<b>(b)</b>	Reflection in the <i>x</i> -axis	<b>B1</b>	1.2	Must be a complete statement	
				[1]			
1	(ii)	(a)	(2, 12)	B1	1.1		
1	(**)	(1.)		[1]	1.1		
1	(ii)	<b>(b)</b>	$\left(\frac{1}{2},3\right)$	<b>B</b> 1	1.1		
				[1]			
2			DR				
			$2(1-\sin^2 x) = 2-\sin x$	M1	3.1a	Use $\cos^2 x = 1 - \sin^2 x$ and simplify	One step of simplification must be seen
			$2\sin^2 x - \sin x = 0$	A1	1.1	Obtain $2\sin^2 x - 1\sin x = 0$	
			$\sin x(2\sin x - 1) = 0$	M1	1.1a	Attempt to solve a 2 term quadratic in	Use any valid method
						sin x and use correct order of	Must be seen
						operations to obtain x	
			$\sin x = \frac{1}{2}$ so $x = 30$ or $x = 150$	A1	1.1	Both values are required	
			$\sin x = 0 \text{ so } x = 0 \text{ or } x = 180$	A1	1.1	Both values are required	
				[5]			

	Question	Answer	Marks	AOs	Guidance	
3	(i)	The model is exponential so the rate of change of <i>m</i> is proportional to <i>m</i>	M1	1.1	Gradient of $e^{kx} = ke^{kx}$	
		In this case, the rate of change of $m$ is $2m$	E1 [2]	2.2a	In context	
3	(ii)	The initial membership	B1	1.1		
3	(:::)	10000 170 21	[1] M1	3.4	Correct equation and use correct order	
3	(iii)	$60000 = 150e^{2t}$	IVII	3.4	Correct equation and use correct order of operations	
		ln 400 = 2t	<b>A1</b>	1.1	Obtain correct intermediate step Or $\ln 60000 = \ln 150 + 2t$	
		2.995 = t and hence 3	<b>A1</b>	1.1	Obtain correct answer	
			[3]			
3	(iv)	E.g. When the graph reaches 60 000 the	B1	3.5c	Correct suggestion	
		graph becomes constant.	[1]			
4	(i)	(1)	[1] B1	1.1		
-		$\overrightarrow{BC} = \begin{pmatrix} 4 \\ -2 \end{pmatrix}$				
		$\begin{pmatrix} 4 \\ -2 \end{pmatrix} = \begin{pmatrix} x \\ y \end{pmatrix} - \begin{pmatrix} -2 \\ 1 \end{pmatrix} = \mathbf{d} - \mathbf{a} = \overrightarrow{AD}$	M1	3.1a	soi	
		$\overrightarrow{OD} = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$	A1	1.1		
4	(ii)	$\overrightarrow{OM} = \begin{pmatrix} 4 \\ 4 \end{pmatrix}$	[3] B1	1.1		
		$\overrightarrow{AM} = \overrightarrow{OM} - \overrightarrow{OA} = \begin{pmatrix} 6\\3 \end{pmatrix}$ $\left  \overrightarrow{AM} \right  = \sqrt{6^2 + 3^2} = 3\sqrt{5}$	M1	1.1	soi	
		$\left  \overrightarrow{AM} \right  = \sqrt{6^2 + 3^2} = 3\sqrt{5}$	A1	2.2a	Accept 6.71	
		<u> </u>	[3]			

	Questic	on	Answer	Marks	AOs	Guid	lance
5	(i)		$\log_{10} y = \log_{10} p + x \log_{10} q$	B1	2.1		
			$m = \log_{10} q$ , $c = \log_{10} p$	<b>B</b> 1	2.4		
				[2]			
5	(ii)		E.g. $\log_{10} q = \frac{2.4 - 1.6}{1 - 5} = -0.2$	M1	3.3	Measure gradient from graph and identify it as $\log q$	
			$q = 10^{-0.2} = 0.63$	<b>A1</b>	1.1		Accept $q in [0.6, 0.7]$
			$\log_{10} p = 2.5$ so $p = 320$	B1	1.1		Accept pin [300, 400]
				[3]			
5	(iii)		$\log_{10} 20 = 1.3$ so week 7	<b>B</b> 1	3.4		
			E.g. Extrapolation is unjustified because it assumes that the assumptions made in the model will hold true in the long term	E1	3.5b	One valid explanation	
6	(i)		22 12 12	[2] M1	2.1		OP
0	(1)		31 gives $3^2 + 1^2 = 10$ 10 is even and hence the suggestion is false	E1 [2]	2.1	<b>M1</b> 37 gives $3^2 + 7^2 = 10^{-10}$	
6	6 (ii)		$n^{2} + (n+1)^{2} + (n+2)^{2}$ $3n^{2} + 6n + 5$ $3(n^{2} + 2n + 1) + 2$ which always leaves a remainder of 2 and so cannot be divided by 3	M1 A1FT E1	2.1 1.1 2.1	Any valid expressions for three consecutive integers FT <i>their</i> expressions Correct conclusion.	

Question	Answer	Marks	AOs	Guidar	nce
7	$f(x+h) = x^4 + 4x^3h + 6x^2h^2 + 4xh^3 + h^4$	M1	1.1	Attempt at expansion with product of	
				powers of x and h summing to 4 and	
				some attempt at coefficients, not	
				necessarily correct	
	$f(x+h) - f(x) - 4x^3h + 6x^2h^2 + 4xh^3 + h^4$	M1	1.1	Attempt $\frac{f(x+h)-f(x)}{h}$	
	$\frac{}{h} = \frac{}{h}$			$\frac{1}{h}$	
	n n			Allow at most two errors	
	$=4x^3+6x^2h+4xh^2+h^3$	<b>A1</b>	1.1	All terms correct	
	As $h \rightarrow 0$ all the terms in h tend to zero.	<b>A1</b>	2.4	Accept some indication that as <i>h</i> tends	
	Therefore			to 0, the terms involving h vanish and	
	$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h} = 4x^3$			leave $4x^3$	
		<b>E</b> 1	2.1	Award for good use of language, and	Only requires the two M1 marks
				of limit and function notation	to be awarded.
		[5]			

C	Question	Answer	Marks	AOs	Guida	nce
8		$2x+3y=0$ $\Rightarrow y=-\frac{2}{3}x \text{ and gradient } -\frac{2}{3}$	M1	3.1a	Identify gradient of line $\left(=-\frac{2}{3}\right)$ anywhere	Allow sign slip
		Hence, gradient of the tangent is $\frac{3}{2}$	A1FT	1.1	Use $m_1 m_2 = -1$ anywhere $\left(=\frac{3}{2}\right)$ FT	
			M1	1.1a	their gradient Attempt differentiation	The power must be seen to decrease
		$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{3}{2}kx^{\frac{1}{2}}$	<b>A1</b>	1.1	Obtain $\frac{3}{2}kx^{\frac{1}{2}}$	
		At $x = 4$ , $\frac{3}{2}k(4)^{\frac{1}{2}} = 3k$	M1	1.1	Substitute $x=4$ and equate to the normal gradient	Tangent gradients may also be used i.e. $-\frac{1}{3k} = -\frac{2}{3}$
		Hence $3k = \frac{3}{2}$ , so $k = \frac{1}{2}$	<b>E</b> 1	1.1	AG	
		At <i>P</i> , $y = \frac{1}{2}(4)^{\frac{3}{2}} = 4$ so $P = (4, 4)$ so equation of normal through <i>P</i> is $(y-4) = -\frac{2}{3}(x-4)$	M1	3.1a	Identify coordinates, gradient of normal and form equation with their coordinates	Accept $y = 4$
		When $y = 0$ , $x = 10$ so $Q = (10, 0)$	A1	1.1	Substitute $y = 0$ and obtain $x = 10$	
		Using $P(4, 4)$ and $Q(10, 0)$ $PQ^2 = (10-4)^2 + (0-4)^2$ Circle equation is $(x-4)^2 + (y-4)^2 = 52$	M1 A1FT	1.1 1.1	Use Pythagoras to obtain length $PQ^2$ Accept equivalent forms	
		()	[10]		FT their coordinates for P and Q	

	Questic	on	Answer	Marks	AOs	Guida	nce
9	(i)		$-\left(\frac{4-0}{8-5}\right)$	M1	1.1	Attempt at acceleration calculation with at most one error	Or use of $v = u + at$ with $v = 0, u = 4$ and $t = 3$ with at least 2 values correct
			Acceleration = $-\frac{4}{3}$	<b>A1</b>	1.1	Or equivalent	ioust 2 values correct
				[2]			
9	(ii)		Distance travelled $= \frac{1}{2} (5+8)(4) + \frac{1}{2} (12)(3) = 44$ Displacement	M1	1.1	Attempt at both areas; the trapezium and triangle	
			$= \frac{1}{2}(5+8)(4) - \frac{1}{2}(12)(3) = 8$	<b>A1</b>	1.1	Either distance travelled or displacement correct	
			44  m > 40  m so distance travelled is more than five times the displacement	<b>E</b> 1	2.2a	Must see relevant comparison	
				[3]			
10	(i)		$s = 9(6)^2 - 1.5(6)^3 = 0$	M1	1.1		
			E.g. The boomerang is at <i>O</i> E.g. She catches the boomerang	E1 [2]	3.4		
10	(ii)		$v = 18t - \frac{9}{2}t^2$	M1	1.1		
			When $v=0$ , t=0 or $t=4At t=0, s=0, so maximumdisplacement must be when t=4 giving$	M1 A1 E1	1.1 1.1 3.4	Imply deduction that greatest distance is when velocity $= 0$ and solve	
			$s = 48 \mathrm{m}$	F41			
10	(iii)	1	<i>t</i> = 5	[4] B1	3.1b		
			v = -22.5	B1	3.4		
10	(iv)	+	a = 18 - 9t	[2] M1	1.1		
10			Acceleration = $-27 (\text{m s}^{-2})$	A1 [2]	1.1		

(	Questic	on Answer	Marks	AOs	Guida	nce
11	(i)	Resultant force from the tug boats is positive so it is moving east	E1	2.2a	(600i)	
		There is zero resultant force in the <b>j</b> direction, so it is not moving north o south		2.2a		
			[2]			
11	(ii)	350+250-200=100000a	M1	3.3	Use $F = ma$ . Allow sign errors and	
					one missing force	
		Obtain 0.004 m s <sup>-2</sup>	A1 [2]	1.1		
11	(iii)	$400 = 1.5t + \frac{1}{2}(0.004)t^2$	M1	3.1b	Use $s = ut + \frac{1}{2}at^2$	
		$0.002t^2 + 1.5t - 400 = 0$	A1	1.1	Obtain correct quadratic. Any equivalent form	
			M1	3.4	Use any method to solve their quadratic	Including BC
		Obtain 209 (seconds)	A1	1.1	If negative root given (-958.63088) this must be clearly discarded	Accept better (208.630877) but not 208
		$v^2 = 1.5^2 + 2(0.004)(400)$	M1	3.4	Use $v^2 = u^2 + 2as$ with their a	
		Obtain 2.33 (m s <sup>-1</sup> )	A1 [6]	1.1	or $v = u + at$ with their $a$ and $t$ Accept better (2.3345235)	

# Assessment Objectives (AO) Grid

Question	AO1	AO2	AO3(PS)	AO3(M)	Total
Pure					
1(i)(a)	2				2
1(i)(b)	1				1
1(ii)(a)	1				1
1(ii)(b)	1				1
2	4		1		5
3(i)	1	1			2
3(ii)	1				1
3(iii)	2			1	3
3(iv)				1	1
4(i)	2		1		3
<b>4</b> (ii)	2	1			3
5(i)		2			2
5(ii)	2			1	3
5(iii)				2	2 2
6(i)		2			2
6(ii)	1	2			3
7	3	2			5
8	8		2		10
				•	
Mechanics					
9(i)	2				2
9(ii)	2	1			3
10(i)	1			1	2
10(ii)	3			1	4
10(iii)			1	1	2
10(iv)	2				2
11(i)		2			2
11(ii)	1			1	2
11(iii)	3		1	2	6
Totals	45	13	6	11	75

PS = Problem Solving M = Modelling





# **AS Level Mathematics A**

**H230/02** Pure Mathematics and Mechanics Printed Answer Booklet

# Date - Morning/Afternoon

Time allowed: 1 hour 30 minutes

#### You must have:

· Question Paper H230/02 (inserted)

#### You may use:

· a scientific or graphical calculator



First name	
Last name	
Centre number	Candidate number

### **INSTRUCTIONS**

- The Question Paper will be found inside the Printed Answer Booklet.
- Use black ink. HB pencil may be used for graphs and diagrams only.
- Complete the boxes provided on the Printed Answer Booklet with your name, centre number and candidate number.
- · Answer all the questions.
- Write your answer to each question in the space provided in the Printed Answer Booklet. Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do **not** write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.
- The acceleration due to gravity is denoted by  $g \, \text{m s}^{-2}$ . Unless otherwise instructed, when a numerical value is needed, use g = 9.8.

### **INFORMATION**

- You are reminded of the need for clear presentation in your answers.
- The Printed Answer Booklet consists of 12 pages. The Question Paper consists of 8 pages.



# **Section A: Pure Mathematics**

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			4									
1(ii)(a)												
1(ii)(b)												

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3(i)	
3(ii)	
3(iii)	
3(iv)	

<b>4</b> (i)	
4(ii)	
<b>4</b> (II)	
<b>5(i)</b>	

5(ii)	
	$\log_{10} y$ $0$ $0$ $1$ $2$ $3$ $4$ $5$ $6$ $7$ $8$
5(iii)	

6(i)	
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6(ii)	
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# **Section B: Mechanics**

9(i)	
9(ii)	
10(i)	

10(ii)	
10(**)	
<b>10(iii)</b>	
10(iv)	
10(11)	
11(i)	

11(ii)	
<b>11(iii)</b>	

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