# Package 'BEST' 

May 17, 2021

Type Package
Title Bayesian Estimation Supersedes the t -Test
Version 0.5.3
Depends HDInterval
Imports coda, rjags
Date 2021-05-17
Author John K. Kruschke and Mike Meredith
Maintainer Mike Meredith [mike@mmeredith.net](mailto:mike@mmeredith.net)
BugReports https://github.com/mikemeredith/BEST/issues
Description An alternative to t-tests, producing posterior estimates for group means and standard deviations and their differences and effect sizes. It implements the method of Kr uschke (2013) Bayesian estimation supersedes the $t$ test. Journal of Experimental Psychology: General, 142(2):573-603 <doi: 10.1037/a0029146>.
License GPL (>=3)
NeedsCompilation no
Repository CRAN
Date/Publication 2021-05-17 07:30:26 UTC

## $R$ topics documented:

BEST-package ..... 2
BESTmcmc ..... 3
BESTpower ..... 6
makeData ..... 9
pairs.BEST ..... 11
plot.BEST ..... 12
plotAll ..... 13
plotAreaInROPE ..... 14
plotPost ..... 16
plotPostPred ..... 19
postPriorOverlap ..... 20
print.BEST ..... 21
summary.BEST ..... 22

## Description

An alternative to $t$ tests, producing posterior estimates for groups means and standard deviations and their differences and effect sizes. Bayesian estimation provides a much richer picture of the data, and can be summarised as point estimates and credible intervals.

## Details

The core function, BESTmcmc, generates posterior distributions to compare the means of two groups, or to compare the mean of one group with a standard, taking into account the standard deviation(s). It is thus similar to a $t$ test. However, our Bayesian approach results in probability statements about the values of interest, rather than $p$-values and significance levels.
In addition, the procedure accounts for departures from normality by using a $t$-distribution to model the variable of interest and estimating a measure of normality.
Functions to summarise and to visualise the output are provided.
The function BESTpower allows simulation-based estimates of power, either retrospective power directly with BESTmcmc output or prospective power analysis with makeData.

## Author(s)

Original code by John K. Kruschke, packaged by Mike Meredith.

## References

Kruschke, J. K. 2013. Bayesian estimation supersedes the $t$ test. Journal of Experimental Psychology: General 142(2):573-603. doi: 10.1037/a0029146
Kruschke, J. K. 2011. Doing Bayesian data analysis: a tutorial with $R$ and BUGS. Elsevier, Amsterdam, especially Chapter 18.

## Examples

```
## Comparison of two groups:
## =========================
y1 <- c(5.77, 5.33, 4.59, 4.33, 3.66, 4.48)
y2 <- c(3.88, 3.55, 3.29, 2.59, 2.33, 3.59)
# Run an analysis, takes up to 1 min.
BESTout <- BESTmcmc(y1, y2, parallel=FALSE)
# Look at the result:
BESTout
```

```
summary(BESTout)
plot(BESTout)
plot(BESTout, "sd")
plotPostPred(BESTout)
plotAll(BESTout, credMass=0.8, ROPEm=c(-0.1,0.1),
    ROPEeff=c(-0.2,0.2), compValm=0.5)
plotAll(BESTout, credMass=0.8, ROPEm=c(-0.1,0.1),
    ROPEeff=c(-0.2,0.2), compValm=0.5, showCurve=TRUE)
summary(BESTout, credMass=0.8, ROPEm=c(-0.1,0.1), ROPEsd=c(-0.15,0.15),
        ROPEeff=c(-0.2,0.2))
pairs(BESTout)
head(BESTout$mu1)
muDiff <- BESTout$mu1 - BESTout$mu2
mean(muDiff > 1.5)
mean(BESTout$sigma1 - BESTout$sigma2)
hist(BESTout$nu)
# Retrospective power analysis
# -----------------------------
# This takes time, so we do 2 simulations here; a real analysis needs several hundred
powerRet <- BESTpower(BESTout, N1=length(y1), N2=length(y2),
    ROPEm=c(-0.1,0.1), maxHDIWm=2.0, nRep=2, parallel=FALSE)
powerRet
# We only set criteria for the mean, so results for sd and effect size are all NA.
## Analysis with a single group:
## =============================
y0 <- c(1.89, 1.78, 1.30, 1.74, 1.33, 0.89)
# Run an analysis, takes up to 40 secs.
BESTout1 <- BESTmcmc(y0, parallel=FALSE)
BESTout1
summary(BESTout1)
plot(BESTout1)
head(BESTout1$mu)
mean(BESTout1$sigma)
```

BESTmcmc Generate MCMC samples for posterior distributions

## Description

This function is the core of the BEST package. It calls JAGS and passes a description of the model, priors, and data, then retrieves and returns the MCMC samples for the parameters.

## Usage

```
BESTmcmc(y1, y2 = NULL, priors = NULL, doPriorsOnly = FALSE,
    numSavedSteps = 1e+05, thinSteps = 1, burnInSteps = 1000,
verbose=TRUE, rnd.seed=NULL, parallel=NULL)
```


## Arguments

| y1 | a numeric vector of data values. <br> a vector of values for a second group, or NULL if there is only one group of <br> observations. |
| :--- | :--- |
| priors | an optional list of values controlling the priors, see Details. <br> if TRUE, BESTmcmc returns MCMC chains representing the prior distributions, <br> not the posterior distributions for your data set. |
| doPriorsOnly |  |
| numSavedSteps | the number of MCMC observations to be returned. |
| thinSteps | thinning rate. If set to $\mathrm{n}>1, \mathrm{n}$ steps of the MCMC chain are calculated for each <br> one returned. This is useful if autocorrelation is high and you need to run long <br> chains. |
| burnInSteps | number of steps to discard as burn-in at the beginning of the chain. <br> if FALSE, output to the R Console is suppressed. If chains are run in parallel, |
| verbose | the output from JAGS is not displayed in the Console, even if verbose $=$ TRUE. |
| rnd. seed | a positive integer (or NULL): the seed for the random number generator, used to <br> obtain reproducible samples if required. Values generated in different versions <br> of BEST or different versions of JAGS may differ, even with the same seed. |
| parallel | if NULL or TRUE and $>3$ cores are available, the MCMC chains are run in <br> parallel. (If TRUE and < 4 cores are available, a warning is given.) |

## Details

The function uses a $t$-distribution to model each sample, and generates vectors of random draws from the posterior distribution of the center $(\mu)$ and spread or scale $(\sigma)$ of the distribution, as well as a measure of normality $(\nu)$. The procedure uses a Bayesian MCMC process implemented in JAGS (Plummer 2003).
$\mu$ is the population mean, except when $\nu=1$ (which is the Cauchy distribution) or lower, when the mean is undefined.
$\sigma$ is a good approximation to the standard deviation (SD) for values of $\nu>20$. More exactly the SD is $\sigma * \operatorname{sqrt}(\nu /(\nu-2))$. For a normal distribution (with $\nu=\infty$ ), $\mathrm{SD}=\sigma$ is exact. The SD is undefined when $\nu=2$ or less.

If priors $=$ NULL, broad priors as described by Kruschke (2013) are used. For $\mu$, Normal (mean (y) , 1000 * $\operatorname{sd}(y))$; for $\sigma$, Uniform $(\operatorname{sd}(y) / 1000, \operatorname{sd}(y) * 1000)$; for $\nu$, Exponential $(1 / 29)+1$, with the constraint that nu $>=1$. Here $y=c(y 1, y 2)$. Note that priors $=$ NULL is not equivalent to priors $=$ list().
Alternatively, priors can be a list with elements specifying the priors for one or more parameters: $\mu$ : population centers have separate normal priors, with mean muM and standard deviation muSD; if
not included in the list, default values of mum $=$ mean $(y), \operatorname{muSD}=s d(y) * 5$ are used;
$\sigma$ : population scales have separate gamma priors, with mode sigmaMode and standard deviation sigmaSD; defaults are sigmaMode $=s d(y)$, sigmaSD $=s d(y) * 5$;
$\nu$ : the normality parameter has a gamma prior with mean nuMean and standard deviation nuSD; defaults are nuMean $=30$, nuSD $=30$; versions before 0.4 .0 constrained $\nu$ to be $>1$.
If there are 2 groups of observations, muM, muSD, sigmaMode, sigmaSD may be vectors of length 2 or scalar; if scalar, the same value is used for each population.
The model is shown in the diagram below.


Derived parameters, including the differences in means or standard deviations, and effect sizes can be obtained from the results of the BESTmcmc run.

The output from BESTmcmc has class BEST, which has print, plot and summary methods. These permit the extraction and display of credible intervals and proportions of the posterior mass above or below values of interest.

## Value

An object of class BEST inheriting from data.frame. If two samples are compared, the output has the following columns:

$$
\begin{array}{ll}
\text { mu1, mu2 } & \text { simulated observations of center for each population } \\
\text { sigma1, sigma2 } & \text { simulated observations of scale for each population } \\
\text { nu } & \text { simulated observations of normality parameter }
\end{array}
$$

while for a single sample, the columns are mu, sigma, nu.
The output has the following attributes:
call the call to the function.
Rhat the 'potential scale reduction factor'.
n.eff sample size adjusted for autocorrelation.
data a list with elements y 1 and y 2 containing the original data; y2 may be NULL.
priors a list with the priors used, if the priors argument is not NULL.
doPriorsOnly logical, the value of the doPriorsOnly argument.
The package provides print, plot and summary methods for BEST objects.

## Author(s)

Original code by John K. Kruschke, modified by Mike Meredith.

## References

Kruschke, J K. 2013. Bayesian estimation supersedes the $t$ test. Journal of Experimental Psychology: General 142(2):573-603. doi: 10.1037/a0029146
For the informative priors, see Kruschke's blog post at http://doingbayesiandataanalysis. blogspot.com/2015/04/informed-priors-for-bayesian-comparison.html

For the constraint on $\nu$, see the blog post at http://doingbayesiandataanalysis.blogspot. com/2015/12/prior-on-df-normality-parameter-in-t.html
Plummer, Martyn (2003). JAGS: A Program for Analysis of Bayesian Graphical Models Using Gibbs Sampling, Proceedings of the 3rd International Workshop on Distributed Statistical Computing (DSC 2003), March 20-22, Vienna, Austria. ISSN 1609-395X

## See Also

plot, summary, pairs for relevant methods.

## Examples

\#\# See examples in BEST-package help.

## BESTpower Estimating statistical power

## Description

Estimation of the probability of meeting the goals of a study given initial information or assumptions about the population parameters. For prospective power estimation, the sequence makeData -> BESTmcmc -> BESTpower
is recommended: see makeData.

## Usage

BESTpower(BESTobj, N1, N2, credMass=0.95, ROPEm, ROPEsd, ROPEeff, maxHDIWm, maxHDIWsd, maxHDIWeff, compValm $=0$, nRep $=200$, mcmcLength $=10000$, saveName $=$ NULL, showFirstNrep $=0$, verbose $=2$, rnd. seed=NULL, parallel=NULL)

## Arguments

BESTobj
N1

N2
credMass
ROPEm

ROPEsd a two element vector, such as $c(-1,1)$, specifying the limit of the ROPE on the (difference of) standard deviations.
ROPEeff a two element vector, such as $c(-1,1)$, specifying the limit of the ROPE on the effect size.
maxHDIWm
maxHDIWsd the maximum acceptable width for the HDI for the (difference of) standard deviation.
maxHDIWeff the maximum acceptable width for the HDI for the effect size.
compValm for a single group, the value of the mean which represents no effect; used to calculate the effect size. Ignored for 2 groups.
nRep number of simulations to carry out.
mcmcLength length of the MCMC chains to use for each simulation.
saveName if required, the results may saved to a file after each iteration and saveName specifies the file name (or path relative to the current working directory) to use. The power object can be loaded with load. Set to NULL (the default) to disable saving.
showFirstNrep the number of results to display as plots at the beginning of the simulation run. (This uses dev.new(), which does not work in Rstudio. The plots will appear sequentially in the plot window and you will have to use the back arrow to review them.)
verbose controls output to the R Console: 0 suppresses all output; 1 gives just a progress bar; 2 gives maximum detail.
rnd.seed a positive integer (or NULL): the seed for the random number generator, used to obtain reproducible samples if required.
parallel if NULL or TRUE and $>3$ cores are available, the MCMC chains are run in parallel. (If TRUE and $<4$ cores are available, a warning is given.)

## Details

For each of the parameters of interest - (difference in) mean, (difference in) standard deviation and effect size - we consider 4 criteria and the probability that each will be met:

1. The HDI of the posterior density of the parameter lies entirely outside the ROPE and is greater than the ROPE.
2. The HDI of the posterior density of the parameter lies entirely outside the ROPE and is less than the ROPE.
3. The HDI of the posterior density of the parameter lies entirely inside the ROPE.
4. The width of the HDI is less than the specified maxHDIWx.

The mass inside the above HDIs depends on the credMass argument.
A uniform beta prior is used for each of these probabilities and combined with the results of the simulations to give a conjugate beta posterior distribution. The means and $95 \%$ HDI credible intervals are returned.

## Value

A matrix with a row for each criterion and columns for the mean and lower and upper limits of a $95 \%$ credible interval for the posterior probability of meeting the criterion.
Note that this matrix always has 12 rows. Rows corresponding to criteria which are not specified will have NAs.

## Note

At least 1000 simulations are needed to get good estimates of power and these can take a long time. If the run is interrupted, the results so far can be recovered from the file specified in saveName.
The chains in BESTobj must have at least nRep values. To allow for some degree of autocorrelation among values, it would be prudent to make these chains at least $10 *$ nRep in length.

## Author(s)

Original code by John Kruschke, modified by Mike Meredith.

## References

Kruschke, J. K. 2013. Bayesian estimation supersedes the $t$ test. Journal of Experimental Psychology: General 142(2):573-603. doi: 10.1037/a0029146
Kruschke, J. K. 2011. Doing Bayesian data analysis: a tutorial with R and BUGS. Elsevier, Amsterdam, Chapter 13.

## See Also

makeData for details of preparing a BESTobj for a prospective power analysis.

## Examples

```
## For retrospective power analysis, see the example in BEST-package.
# 1. Generate idealised data set:
proData <- makeData(mu1=108, sd1=17, mu2=100, sd2=15, nPerGrp=20,
    pcntOut=10, sdOutMult=2.0, rnd.seed=NULL)
```

```
# 2. Generate credible parameter values from the idealised data:
proMCMC <- BESTmcmc(proData$y1, proData$y2, numSavedSteps=2000, parallel=FALSE)
# 3. Compute the prospective power for planned sample sizes:
# We'll do just 5 simulations to show it works; should be several hundred.
N1plan <- N2plan <- 50
powerPro <- BESTpower(proMCMC, N1=N1plan, N2=N2plan,
                                    ROPEm=c (-1.5,1.5), ROPEsd=c(-2, 2), ROPEeff=c(-0.5,0.5),
                                    maxHDIWm=15.0, maxHDIWsd=10.0, maxHDIWeff=1.0, nRep=5, parallel=FALSE)
powerPro
```

makeData
Population parameter specification for a power analysis

## Description

The function allows the analyst to prepare an idealized data set which exactly matches selected point values, and incorporates uncertainty in these values in terms of sample size.

## Usage

makeData(mu1, sd1, mu2 = NULL, sd2 = NULL, nPerGrp, pcntOut $=0$, sdOutMult $=2$, rnd.seed $=$ NULL, showPlot $=$ TRUE)

## Arguments

mu1 the mean for the first (or only) population.
sd1 the standard deviation for the main part of the first population, excluding outliers.
mu2 the mean for the second population; NULL if only one population is involved.
sd2 the standard deviation for the main part of the second population; NULL if only one population is involved.
nPerGrp sample size per group; large sample size reflects a high degree of precision in the values for the means and standard deviations.
pentOut the percentage of outliers in each population.
sdOutMult the standard deviation of the outliers as a multiple of the standard deviation of the main part of the population.
rnd. seed a seed for the random number generator, used to obtain reproducible samples if required.
showPlot if TRUE, displays the results as a plot (see Details).

## Details

The arguments to this function provide a framework to specify the hypothesised values of the parameters of the populations under study, while the sample size is chosen to reflect the confidence in the values specified.
The function produces idealized samples, ie. samples which exactly match the specified means and standard deviations. If showPlot $=$ TRUE, the results are displayed as a plot:

## Simulated Data



Histograms: actual sample values; red dashed line: distribution of the outliers; blue dashed line: distribution of the non-outliers; black line: combined distribution.
These idealised samples are passed to BESTmcmc, which generates a series of sets of credible values for the parameters, including the normality parameter, taking account of correlations among them.
The sets of credible parameter values which constitute the BESTmcmc output are used by BESTpower to simulate new data sets which might arise during a subsequent experiment.

## Value

A list with two components:
A vector of simulated values for the first (or only) group.
y2
A vector of simulated values for the second group or NULL.

## Author(s)

John Kruschke

## References

Kruschke, J. K. 2013. Bayesian estimation supersedes the $t$ test. Journal of Experimental Psychology: General 142(2):573-603. doi: 10.1037/a0029146

## See Also

BESTpower for examples.

## Examples

```
## See examples for BESTpower.
```

    pairs.BEST Scatterplot matrix for a BEST object
    
## Description

Function to produce a scatterplot matrix of a BEST object produced by BESTmcmc, with correlation coefficients in the lower triangle.

## Usage

\#\# S3 method for class 'BEST'
pairs(x, nPtToPlot $=1000$, col $="$ skyblue",.. )

## Arguments

$x \quad$ an object of class BEST
nPtToPlot number of points to plot
col colour to use for the points plotted.
... other graphical parameters passed to plot.default.

## Value

None; used for its side effect.

## Author(s)

Original code by John Kruschke, adapted as a pairs method by Mike Meredith

## See Also

pairs in package graphics.

## Examples

\# See examples in BEST-package

## Description

Displays a plot showing the posterior probability distribution of one of the parameters of interest, the difference in means by default.

## Usage

\#\# S3 method for class 'BEST'
plot(x, which = c("mean", "sd", "effect", "nu"), credMass = 0.95, ROPE = NULL, compVal = 0, showCurve = FALSE, ...)

## Arguments

x
which
credMass
credMass the probability mass to include in credible intervals, or NULL to suppress plotting of the credible interval.

ROPE a two element vector, such as $c(-1,1)$, specifying the limit of the ROPE on the estimate; see Details.
showCurve logical: if TRUE, the posterior density will be represented by a kernel density function instead of a histogram.
compVal a value for comparison with the (difference of) parameters.
... other graphical parameters.

## Details

The posterior distribution is shown as a histogram or density curve (if showCurve = TRUE), together with the Highest Density Interval. A ROPE and comparison value are also shown if appropriate.
The probability that the difference in means (or effect size, etc.) is precisely zero is zero. More interesting is the probability that the difference may be too small to matter. We can define a region of practical equivalence (ROPE) around zero, and obtain the posterior probability that the true value lies therein.

## Value

Returns an object of class histogram invisibly. Used mainly for the side effect.

## Author(s)

Mike Meredith, adapted from code by John Kruschke.

## References

Kruschke, J. K. 2013. Bayesian estimation supersedes the $t$ test. Journal of Experimental Psychology: General 142(2):573-603. doi: 10.1037/a0029146

## See Also

plotAll for a single plot showing all the parameters, summary for values of the corresponding summary statistics and pairs for a scatterplot matrix plot and correlation coefficients.

## Examples

\# See examples in BEST-package.
plotAll A series of plots displaying the results of 'BEST' analysis.

## Description

Displays a series of plots showing the posterior probability distributions of the parameters of interest.

## Usage

plotAll(BESTobj, credMass = 0.95, ROPEm $=$ NULL, ROPEsd $=$ NULL, ROPEeff $=$ NULL, compValm $=0$, compValsd $=$ NULL, compValeff $=0$, showCurve = FALSE, ...)

## Arguments

| BESTobj | an object of class BEST, as produced by the function BESTmcmc. |
| :---: | :---: |
| credMass | the probability mass to include in credible intervals, or NULL to suppress plotting of the credible interval. |
| ROPEm | a two element vector, such as $c(-1,1)$, specifying the limit of the ROPE on the difference of means (for 2 groups) or the mean (for 1 group). |
| ROPEsd | a two element vector, such as $c(-1,1)$, specifying the limit of the ROPE on the (difference of) standard deviations. |
| ROPEeff | a two element vector, such as $c(-1,1)$, specifying the limit of the ROPE on the effect size. |
| showCurve | logical: if TRUE, the posterior density will be represented by a kernel density function instead of a histogram. |
| compValm | a value for comparison with the (difference of) means. |
| compValsd | a value for comparison with the (difference of) standard deviations. |
| compValeff | a value for comparison with the effect size. |
|  | other graphical parameters (currently ignored). |

## Details

The display has a series of panels displaying the posterior distributions of each of the parameters (and differences between groups) together with summary statistics; see plotPost for details. Also a chart showing approx. 30 plots of posterior predictive distributions, together with histograms of the original data.

## Value

Returns NULL invisibly. Used for the side effect.

## Author(s)

Code by John Kruschke, modified by Mike Meredith.

## References

Kruschke, J. K. 2013. Bayesian estimation supersedes the $t$ test. Journal of Experimental Psychology: General 142(2):573-603. doi: 10.1037/a0029146

## See Also

plot for plots of individual parameters, summary for values of the corresponding summary statistics and pairs for a scatterplot matrix plot and correlation coefficients.

## Examples

\# See examples in BEST-package.
plotAreaInROPE Area of the posterior density in the ROPE as a function of its width.

## Description

Calculates and (optionally) plots the posterior probability mass included in the Region of Practical Equivalence (ROPE: see plot.BEST) as a function of the width of the ROPE.

## Usage

plotAreaInROPE (paramSampleVec, credMass $=0.95$, compVal $=0$, maxROPEradius, $\mathrm{n}=201$, plot $=$ TRUE, ...)

## Arguments

paramSampleVec A vector of samples drawn from the target distribution; see Examples.
credMass The probability mass to include in credible intervals.
compVal a value for comparison with those plotted.
maxROPEradius The maximum value of the ROPE radius (ie. half-width) to include in the plot.
$n \quad$ The number of equally spaced points at which the area in the ROPE is to be estimated.
plot If FALSE, the plot will be suppressed but the values will be returned.
... Other graphical parameters.

## Details

Defining a Region of Practical Equivalence (ROPE) allows decisions on whether a parameter is, for practical purposes, equivalent to a hypothetical null value, given a posterior probability density for the parameter. The null value may be considered credible if (A) $95 \%$ (say) of the probability mass lies within the ROPE, or (B) the $95 \%$ highest density interval ( $95 \% \mathrm{HDI}$ ) lies entirely within the ROPE.
How wide should the ROPE be? Different people at different times will have different ideas on the range of values equivalent to the null. The function plotAreaInROPE plots the probability mass lying within the ROPE for a range of widths (or rather radii or half-widths). It also shows the radius at which the HDI falls entirely within the ROPE.

## Value

Returns invisibly a list with elements:

```
x A vector of ROPE radii from 0 to maxROPEradius.
y The corresponding proportion of the posterior density included in the ROPE.
```


## Author(s)

John K. Kruschke, with minor modifications by Mike Meredith.

## References

http://doingbayesiandataanalysis.blogspot.com/2013/08/how-much-of-bayesian-posterior. html

## Examples

```
\# Generate a fake MCMC posterior for effect size and plot it:
mcmcChain <- rnorm(50000, 0.03, 0.025)
plotPost(mcmcChain, compVal=0, ROPE=c(-0.1, 0.1))
\# How does the mass within the ROPE vary with ROPE radius?
plotAreaInROPE(mcmcChain, credMass \(=0.95\), compVal \(=0\),
    maxROPEradius \(=0.15\) )
```

```
# Generate real MCMC chains, takes up to 1 min:
y1 <- c(4.77, 4.33, 3.59, 3.33, 2.66, 3.48)
y2 <- c(3.88, 3.55, 3.29, 2.59, 2.33, 3.59)
BESTout <- BESTmcmc(y1, y2, parallel=FALSE)
plot(BESTout)
meanDiff <- BESTout$mu1 - BESTout$mu2
plotAreaInROPE(meanDiff, credMass = 0.95, compVal = 0,
    maxROPEradius = 3)
```

plotPost Graphic display of a posterior probability distribution

## Description

Plot the posterior probability distribution for a single parameter from a vector of samples, typically from an MCMC process, with appropriate summary statistics.

## Usage

plotPost(paramSampleVec, credMass = 0.95, compVal = NULL, ROPE = NULL, HDItextPlace $=0.7$, showMode $=$ FALSE, showCurve $=$ FALSE,.. )

## Arguments

paramSampleVec A vector of samples drawn from the target distribution.
credMass the probability mass to include in credible intervals, or NULL to suppress plotting of credible intervals.
compVal a value for comparison with those plotted.
ROPE a two element vector, such as $c(-1,1)$, specifying the limits of the Region Of Practical Equivalence.
HDItextPlace a value in [0,1] that controls the horizontal position of the labels at the ends of the HDI bar.
showMode logical: if TRUE, the mode is displayed instead of the mean.
showCurve logical: if TRUE, the posterior density will be represented by a kernel density function instead of a histogram.
... graphical parameters and the breaks parameter for the histogram.

## Details

The data are plotted either as a histogram (above) or, if showCurve = TRUE, as a fitted kernel density curve (below). Either the mean or the mode of the distribution is displayed, depending on the parameter showMode. The Highest Density Interval (HDI) is shown as a horizontal bar, with labels for the ends of the interval.


Response variable


## Parameter

If values for a ROPE are supplied, these are shown as dark red vertical dashed lines, together with the percentage of probability mass within the ROPE. If a comparison value (compVal) is supplied, this is shown as a vertical green dotted line, together with the probability mass below and above this value.

## Value

Returns an object of class histogram invisibly. Used for its plotting side-effect.

## Author(s)

John Kruschke, modified by Mike Meredith

## See Also

For details of the HDI calculation, see hdi.

## Examples

```
# Generate some data
tst <- rnorm(1e5, 3, 1)
plotPost(tst)
plotPost(tst, col='wheat', border='magenta')
```

```
plotPost(tst, credMass=0.8, ROPE=c(-1,1), xlab="Response variable")
plotPost(tst, showMode=TRUE, showCurve=TRUE, compVal=5.5)
# For integers:
tst <- rpois(1e5, 12)
plotPost(tst)
# A severely bimodal distribution:
tst2 <- c(rnorm(1e5), rnorm(5e4, 7))
plotPost(tst2) # A valid 95% CrI, but not HDI
plotPost(tst2, showCurve=TRUE) # Correct 95% HDI
```

    plotPostPred Plots for Posterior Predictive checks.
    
## Description

Plots a number (default 30) of credible t-distributions based on posterior values of the mean, standard deviation, and normality for each group, together with histograms of the data.

## Usage

plotPostPred(BESTobj, nCurvesToPlot = 30)

## Arguments

BESTobj an object of class BEST, as produced by the function BESTmcmc.
nCurvesToPlot the number of posterior predictive curves to plot.

## Value

Nothing, used for its side effect.

## Author(s)

John Kruschke, modified by Mike Meredith.

## References

Kruschke, J. K. 2013. Bayesian estimation supersedes the $t$ test. Journal of Experimental Psychology: General 142(2):573-603. doi: 10.1037/a0029146

## Examples

\#\# See examples in BEST-package.

## Description

Calculates and displays the overlap between a posterior distribution (as a vector of samples, typically from an MCMC process) and a prior distribution (as a vector of samples or as a function). Unidentifiable parameters will have high overlap: Gimenez et al (2009) suggest that overlap greater than $35 \%$ indicates weak identifiability.

## Usage

```
    postPriorOverlap(paramSampleVec, prior, ..., yaxt="n", ylab="",
    xlab="Parameter", main="", cex.lab=1.5, cex=1.4,
    xlim=range(paramSampleVec), breaks=NULL)
```


## Arguments

paramSampleVec a vector of samples drawn from the target distribution.
prior either a vector of samples drawn from the prior distribution or the name for the density function of the distribution; standard $R$ functions for this have a dprefix, eg. dbeta. Arguments required by the function must be specified by their (abbreviated) names in the . . . argument; see the examples.
... named parameters to be passed to prior when it is a function.
yaxt a character which specifies the $y$ axis type; the default, " $n$ ", suppresses plotting.
ylab text to use as the label of the $y$ axis.
$x l a b \quad$ text to use as the label of the $x$ axis.
cex.lab the magnification to be used for $x$ and $y$ labels relative to the current setting of cex
cex a numerical value giving the amount by which plotting text and symbols should be magnified relative to the default
$x \lim \quad$ a vector of length 2 giving the limits for the x axis.
main text to use as the main title of the plot
breaks controls the histogram break points or the number of bars; see hist.

## Value

Returns the overlap, the area lying under the lower of the two density curves.

## Author(s)

Mike Meredith

## References

Gimenez, Morgan and Brooks (2009) Weak identifiability in models for mark-recapture-recovery data. pp.1055-1068 in Thomson, Cooch and Conroy (eds) Modeling demographic processes in marked populations Springer

## Examples

```
# Generate some data
tst <- rbeta(1e6, 5, 7)
# check overlap with a Beta(0.2, 0.2) prior:
postPriorOverlap(tst, dbeta, shape1=0.2, shape2=0.2)
# check overlap with a Uniform(0, 1) prior:
postPriorOverlap(tst, runif(1e6))
```

print.BEST
Printing a BEST object

## Description

Print method for objects of class BEST, such as produced by BESTmcmc.

## Usage

\#\# S3 method for class 'BEST'
print(x, digits $=4, \ldots$ )

## Arguments

x an object of class BEST, as produced by BESTmcmc.
digits the number of digits to print.
... further arguments for the print function.

## Details

The print method displays summary statistics for the parameters and two MCMC diagnostic measures:

Rhat is the 'potential scale reduction factor', which is 1 on convergence; if any parameter has a value $>1.05$, rerun with increased burnInSteps. See gelman.diag.
n. eff is the sample size adjusted for autocorrelation; for stable estimates of credible intervals this should be $>10,000$. Rerun with increased numSavedSteps or increased thinSteps. See effectiveSize.

Value
Returns x invisibly.

## Author(s)

Mike Meredith

## See Also

BESTmcmc.

## Examples

\#\# See examples in BEST-package help.

```
summary.BEST
```

Extract summary statistics from an object of class BEST.

## Description

Provides summary statistics for each of the parameters (mean and standard deviation) of the group(s) of observations and their differences.

## Usage

\#\# S3 method for class 'BEST'
summary (object, credMass $=0.95$, ROPEm $=$ NULL, ROPEsd $=$ NULL, ROPEeff $=$ NULL,
compValm $=0$, compValsd $=$ NULL, compValeff $=0, \ldots$ )

## Arguments

| object | an object of class BEST, as produced by the function BESTmcmc. |
| :--- | :--- |
| credMass | the probability mass to include in credible intervals. <br> a two element vector, such as $c(-1,1)$, specifying the limit of the ROPE on the <br> difference of means (for 2 groups) or the mean (for 1 group). See plot. BEST <br> for an explanation of ROPE. |
| ROPEsd | a two element vector, such as $c(-1,1)$, specifying the limit of the ROPE on the <br> (difference of) standard deviations. |
| ROPEeff | a two element vector, such as $c(-1,1)$, specifying the limit of the ROPE on the <br> effect size. |
| compValm | a value for comparison with the (difference of) means. |
| compValsd | a value for comparison with the (difference of) standard deviations. <br> compValeff |
| a value for comparison with the effect size. |  |

## Value

Returns a matrix with the parameters in rows and the following columns:
mean, median, mode
the mean, median and mode of the MCMC samples for the corresponding parameter.
hdi\%, hdiLow, hdiHigh
the percentage of posterior probability mass included in the highest density interval and the lower and upper limits.
compVal, \%>compVal
the value for comparison and the percentage of the posterior probability mass above that value.
ROPElow, ROPEhigh, \%InROPE
the lower and upper limits of the Region Of Practical Equivalence (ROPE) and the percentage of the posterior probability mass within the region.

If the analysis concerns a comparison of two groups, the matrix will have rows for:
mu1, mu2, muDiff
the means of each group and the difference in means
sigma1, sigma2, sigmaDiff
the standard deviations of each group and the difference in standard deviations
nu, $\log 10 n u \quad$ the normality parameter and its $\log$
effSz the effect size; $d[a]$ from Macmillan \& Creelman (1991).
For a single group, the rows will be:

| mu | the mean |
| :--- | :--- |
| sigma | the standard deviation |
| nu, log10nu | the normality parameter and its log |
| effSz | the effect size. |

Many of the elements of the matrix will be NA. The print method for the summary attempts to print this nicely.

## Author(s)

Mike Meredith, based on code by John K. Kruschke.

## References

Kruschke, J K. 2013. Bayesian estimation supersedes the $t$ test. Journal of Experimental Psychology: General 142(2):573-603. doi: 10.1037/a0029146
Macmillan, N. A., \& Creelman, C. D. (1991). Detection Theory: A User's Guide. New York, Cambridge University Press

## See Also

Use the plotAll function for a graphical display of these same values.

## Examples

\#\# see "BEST-package"

## Index

```
* hplot
    plotAreaInROPE, 14
    plotPost, 16
    plotPostPred,19
* htest
        BEST-package, 2
* methods
        summary.BEST, }2
* package
    BEST-package, 2
* print
    print.BEST, 21
BEST (BEST-package), 2
BEST-package, 2
BESTmcmc, 2, 3, 10-13, 19, 21, 22
BESTpower, 2, 6, 10, 11
effectiveSize, 21
gelman.diag, 21
hdi,}1
hist,20
load, }
makeData, 2, 6, 8, }
pairs, 6, 11, 13, 14
pairs.BEST,11
plot, 6,14
plot.BEST, 12, 14,22
plotAll, 13, 13,23
plotAreaInROPE, 14
plotPost,14,16
plotPostPred,19
postPriorOverlap, 20
print.BEST,21
summary, 6, 13, 14
summary.BEST, 22
```

