## PARTICLE SIZE ANALYSIS

# CHARACTERIZATION OF SOLID PARTICLES 

- SIZE
- SHAPE
- DENSITY


SPHERICAL


FLAKEY


ROUNDED


SPONGY
1
ACICULAR

Roundness and Sphericity




well
rounded


## Equivalent diameter, Nominal diameter

- $\varphi_{s}=\frac{\text { Surface of a sphere of same volume as particle }}{\text { surface area of the particle }}$
- Let
- $v_{p}=$ volume of particle,$s_{p}=$ surface area of tha particle,
- $D_{p}=$ Equivalent diameter $=$

Diameter of sphere which has same volume as particlev $v_{p}=$ $\frac{\pi}{6} D_{p}{ }^{3}$

- Surface area of the sphere of diameter $\mathrm{Dp}, S_{p}=\pi D_{p}{ }^{2}=\frac{6 v_{p}}{D_{p}}$

$$
\varphi_{s}=\frac{S_{p}}{s_{p}}=\frac{6 v_{p}}{s_{p} D_{p}}
$$

It is often difficult to calculate volume of particle, to calculate equivalent diameter, Dp is taken as nominal diameter based on screen analysis or microscopic analysis

## Sphericity of particles having different shapes

Particle SphericitySphere1.0cube0.81Cylinder, length $=\quad 0.87$diameterhemisphere 0.84sandCrushed particlesFlakes0.2

## Sphericity, Table 7.1, McCabe Smith

- Sphericity of sphere, cube, short cylinders(L=Dp) = 1


## VOLUME SHAPE FACTOR

$$
\begin{gathered}
v_{p} \propto D_{p}^{3} \\
v_{p}=a D_{p}^{3}
\end{gathered}
$$

Where , a = volume shape factor
For sphere, $v_{p}=\frac{\pi}{6} D_{p}^{3}$ or $a=\frac{\pi}{6}$

## Commonly used measurements of particle size



Feret's diameter

Martin's diameter
Projected area diameter
Maximum horizontal intercept

## Particle size/ units

- Equivalent diameter : Diameter of a sphere of equal volume
- Nominal size : Based on;
$\checkmark$ Screen analysis and
$\checkmark$ Microscopic analysis
- For Non equidimensional particles Diameter is taken as second longest major dimension.
- Units:
$\checkmark$ Coarse particles - mm
$\checkmark$ Fine particles in micrometer, nanometers
$\checkmark$ Ultrafine - surface area per unit mass, sq m/gm


## Particle size determination

- Screening $>50 \mu m$
- Sedimentation and elutriation - $>1 \mu m$
- Permeability method - > $1 \mu m$
- Instrumental Particle size analyzers : Electronic particle counter - Coulter Counter, Laser diffraction analysers, Xray or photo sedimentometers, dynamic light scattering techniques


## Screening

- Mesh Number = Number of opening per linear inch
- Clear opening $=\frac{1}{\text { mesh number }}$ - Wire thickness



## Standard Screen Sizes

BSS= British Standard Screen
IMM = Institute of Mining \& Metallurgy
U.S. Tyler mesh

US. ASTM= American Institute for testing Materials

- Ratio of aperture of two consecutive sieves=2,
$\sqrt{2}, \sqrt[4]{2}[2,1.41,1.18]$

| British fine mesh (B.S.S. 410) ${ }^{(3)}$ |  |  | I.M.M. ${ }^{(4)}$ |  |  | U.S. Tyler ${ }^{(5)}$ |  |  | U.S. A.S.T.M. ${ }^{(5)}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Sieve | Nominal aperture |  | Sieve no. | Nominal aperture |  | Sieve no. | Nominal aperture |  | Sieve no. | Nominal aperture |  |
|  | in. | $\mu \mathrm{m}$ |  | in. | $\mu \mathrm{m}$ |  | in. | $\mu \mathrm{m}$ |  | in. | $\mu \mathrm{m}$ |
|  |  |  |  |  |  | 325 | 0.0017 | 43 | 325 | 0.0017 | 44 |
|  |  |  |  |  |  | 270 | 0.0021 | 53 | 270 | 0.0021 | 53 |
| 300 | 0.0021 | 53 |  |  |  | 250 | 0.0024 | 61 | 230 | 0.0024 | 61 |
| 240 | 0.0026 | 66 | 200 | 0.0025 | 63 | 200 | 0.0029 | 74 | 200 | 0.0029 | 74 |
| 200 | 0.0030 | 76 |  |  |  |  |  |  | 170 | 0.0034 | 88 |
| 170 | 0.0035 | 89 | 150 | 0.0033 | 84 | 170 | 0.0035 | 89 |  |  |  |
| 150 | 0.0041 | 104 |  |  |  | 150 | 0.0041 | 104 | 140 | 0.0041 | 104 |
| 120 | 0.0049 | 124 | 120 | 0.0042 | 107 | 115 | 0.0049 | 125 | 120 | 0.0049 | 125 |
| 100 | 0.0060 | 152 | 100 | 0.0050 | 127 | 100 | 0.0058 | 147 | 100 | 0.0059 | 150 |
|  |  |  | 90 | 0.0055 | 139 | 80 | 0.0069 | 175 | 80 | 0.0070 | 177 |

## MIXED PARTICLE SIZE ANALYSIS:

Differential and Cumulative Screen Analysis

- Average particle size, $\overline{D_{p_{i}}}$
- Mass fraction, $x_{i}$
- Cumulative mass fraction,$\phi$
- Cumulative mass fraction bigger than a particle size
- Cumulative mass fraction smaller than a particle size
- Differential screen analysis curve
- Plot Mass fraction vs Average particle size
- Cumulative screen analysis curve
- Plot Cumulative mass fraction vs Average particle size


| Sl. <br> No. | Mes <br> h <br> No. | Screen Opening $\mathrm{D}_{\mathrm{pi}}(\mathrm{~cm})$ | Mass retained on a screen $\mathrm{m}_{\mathrm{i}}(\mathrm{gm})$ | Mass <br> Fraction $x_{i}=\mathrm{m}_{\mathrm{i}} / \mathrm{M}$ | Average particle diameter $\overline{D_{p i}}$ | $\Phi$, <br> Cumulative fraction <br> Larger than $\overline{D_{p i}}$ | Cumulative Fraction <br> Smaller <br> than $\overline{D_{p i}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |  | 1.00 |
| 2 |  |  |  |  |  |  |  |
| 3 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| Pan |  |  |  |  |  | 1.00 | 0.00 |
|  |  |  | $\sum m_{i}=M$ | $\sum x_{i}=1$ |  |  |  |

## Differential and Cumulative Screen Analysis Curves




## MIXED PARTICLE SIZES : Surface area, Specific Surface area, Volume surface mean diameter

- $v_{p}=$ volume of particle,
- $s_{p}=$ surface area of particle,
- $D_{p}=$ Diameter of particle
- $\rho_{p}=$ density of material
- Number of particles in a mass of " $m$ "
- $N=\frac{\text { Total volume }}{\text { volume of one particle }}=\frac{m / \rho_{p}}{v_{p}}$
- Total surface area:
- $A=N s_{p}=\frac{m}{v_{p} \rho_{p}} \frac{6 v_{p}}{D_{p} \varphi_{s}}=\frac{6 m}{\varphi_{s} \rho_{p} D_{p}}$

$$
\left[\varphi_{s}=\frac{6 v_{p}}{D_{p} s_{p}}\right]
$$

## Specific surface area, $A_{w}$,area/mass

- $A=N s_{p}=\frac{m}{v_{p} \rho_{p}} \frac{6 v_{p}}{D_{p} \varphi_{s}}=\frac{6 m}{\varphi_{s} \rho_{p} D_{p}}$

$$
\left[\varphi_{s}=\frac{6 v_{p}}{D_{p} s_{p}}\right]
$$

- $A_{\text {total }}=\frac{6 m_{1}}{\varphi_{s} \rho_{p} \overline{D_{p 1}}}+\frac{6 m_{2}}{\varphi_{s} \rho_{p} \overline{D_{p 2}}}+\cdots \ldots+\frac{6 m_{n}}{\varphi_{s} \rho_{p} \overline{D_{p n}}}$
- $A_{w}=\frac{A_{\text {total }}}{M}=\frac{6 m_{1 / M}}{\varphi_{s} \rho_{p} \overline{D_{p 1}}}+\frac{6 m_{2} / M}{\varphi_{s} \rho_{p} \overline{p_{p 2}}}+\cdots \ldots+\frac{6 m_{n} / M}{\varphi_{s} \rho_{p} \overline{D_{p n}}}$
- $A_{w}=\frac{6 x_{1}}{\varphi_{s} \rho_{p} \overline{D_{p 1}}}+\frac{6 x_{2}}{\varphi_{s} \rho_{p} \overline{D_{p 2}}}+\cdots \ldots+\frac{6 x_{n}}{\varphi_{s} \rho_{p} \overline{D_{p n}}}$
- $A_{w}=\frac{6}{\varphi_{s} \rho_{p}} \sum_{i=1}^{n} \frac{x_{i}}{\overline{p_{p i}}}$

Volume surface mean diameter
[also known as Sauter Diameter]

- $\overline{D_{s}}=\frac{6}{\varphi_{s} \rho_{p} A_{w}}=\frac{6}{\varphi_{s} \rho_{p} \frac{6}{\varphi_{s} \rho_{p}} \sum_{i=1}^{n} \frac{x_{i}}{D_{p i}}}=\frac{1}{\sum_{i=1}^{n} \frac{x_{i}}{\overline{D_{p i}}}}$


## AVERAGE PARTICLE SIZE

- Volume surface mean diameter:

$$
\overline{D_{s}}=\frac{6}{\varphi_{s} \rho_{p} A_{w}}=\frac{1}{\sum_{i=1}^{i=n} \frac{x_{i}}{\overline{D_{p i}}}}
$$

- Arithmetic Mean Diameter:

$$
\overline{D_{N}}=\frac{\sum_{i=1}^{n}\left(N_{i} \overline{D_{p i}}\right)}{\sum_{i=1}^{n} N_{i}}=\frac{\sum_{i=1}^{n}\left(N_{i} \overline{D_{p i}}\right)}{N_{T}}
$$

- Mass Mean diameter

$$
\overline{D_{w}}=\sum_{i=1}^{n} x_{i} \overline{D_{p i}}
$$

- Number of particles:

$$
N_{i}=\frac{m_{i} / \rho_{p}}{a{\overline{D_{p i}}}^{3}} \quad \text { and } N_{T}=\sum_{i=1}^{n} N_{i}=\frac{1}{a \rho_{p}} \sum_{i=1}^{n} \frac{m_{i}}{{\overline{D_{p i}}}^{3}}
$$

## VOLUME MEAN DIAMETER

- Volume mean diameter: Diameter of a particle with average volume:
- Average particle vol $=\frac{\text { Total volume }}{N_{T}}=a{\overline{D_{v}}}^{3}$

$$
\begin{gathered}
N_{i}=\frac{m_{i} / \rho_{p}}{a{\overline{D_{p i}}}^{3}} \quad \text { and } N_{T}=\sum_{i=1}^{n} N_{i}=\frac{1}{a \rho_{p}} \sum_{i=1}^{n} \frac{m_{i}}{{\overline{D_{p i}}}^{3}} \\
a{\bar{D}_{v}}^{3}=\frac{\text { Total volume }}{\text { Total number }}=\frac{M / \rho_{p}}{\frac{1}{a \rho_{p}} \sum_{i=1}^{n} \frac{m_{i}}{{\overline{D_{p i}}}^{3}}=\frac{1 / \rho_{p}}{\frac{1}{a \rho_{p}} \sum_{i=1}^{n} \frac{x_{i}}{{\overline{D_{p i}}}^{3}}}} \begin{array}{c}
D_{v}=\left[\frac{1}{\left.\sum_{i=1}^{n} \frac{x_{i}}{{\overline{D_{p i}}}^{3}}\right]^{1 / 3}}\right.
\end{array} .
\end{gathered}
$$

## Number of particles Shape Factor a

- $v_{p}=a D_{p}{ }^{3}$
- $N_{T}=\sum_{i=1}^{n} \frac{m_{i}}{a \rho_{p} \overline{D_{p i}}}$
- Number of particles per unit mass

$$
\begin{gathered}
N_{w}=\frac{N_{T}}{M}=\frac{1}{M} \sum_{i=1}^{n} \frac{m_{i}}{a \rho_{p}{\overline{D_{i}}}^{3}}=\frac{1}{a \rho_{p}} \sum_{i=1}^{n} \frac{x_{i}}{{\overline{D_{p i}}}^{3}} \\
N_{w}=\frac{1}{a \rho_{p}{\overline{D_{v}}}^{3}}
\end{gathered}
$$

| SI. No. | Mesh No. | Screen <br> Opening $\mathrm{D}_{\mathrm{pi}}(\mathrm{~cm})$ | Mass retained on a screen $\mathrm{m}_{\mathrm{i}}$ (gm) | Mass Fraction $x_{i}=\mathrm{m}_{\mathrm{i}} / \mathrm{M}$ | Average particle diameter $\overline{D_{p i}}$ | $\Phi$, <br> Cumulative <br> fraction <br> Larger <br> than $\overline{D_{p i}}$ | Cumulative Fraction <br> Smaller <br> than, $\overline{D_{p i}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 4 |  | 0 |  |  |  |  |
|  | 6 |  | 25 |  |  |  |  |
|  | 8 |  | 125 |  |  |  |  |
|  | 10 |  | 325 |  |  |  |  |
|  | 14 |  | 250 |  |  |  |  |
|  | 20 |  | 160 |  |  |  |  |
|  | 28 |  | 50 |  |  |  |  |
|  | 35 |  | 20 |  |  |  |  |
|  | 48 |  | 10 |  |  |  |  |
|  | 65 |  | 8 |  |  |  |  |
|  | 100 |  | 6 |  |  |  |  |
|  | 150 |  | 4 |  |  |  |  |
|  | 200 |  | 3 |  |  |  |  |
|  | pan |  | 2 |  |  |  |  |
|  |  |  |  |  |  |  | 21 |

## PROPTERTIES OF MASSES OF PARTICLES

- Bulk density or apparent density, $\rho_{b}$, is defined as the weigh per unit volume of material including voids inherent in the material as tested. It i: a measure of the fluffiness of the material.

$$
\rho_{b}=\frac{m}{V_{T}}=\frac{m}{V_{p}+V_{v}} \text { and } \rho_{t}=\frac{m}{V_{p}}
$$

- Porosity, It is the ratio of the void volume and bulk volume.


## OPEN PORES BETWEEN PARTICLES



$$
\begin{gathered}
\varepsilon=\frac{V_{v}}{V_{T}} \\
\varepsilon=\frac{V_{T}-V_{p}}{V_{T}}=1-\frac{V_{p}}{m} \frac{m}{V_{T}}=1-\frac{\rho_{b}}{\rho_{t}}
\end{gathered}
$$

FLOWMETER

Pourabilityis defined as a measure of the time required for a standard quality of material to flow through a funnel of specified dimension. It characterizes the handling properties of fine particles



- Angle of repose, $\alpha_{\tau}$, is defined as the angle formed between sloping side of a cone shaped pile of material and the horizontal if the mass is truly homogeneous, $\boldsymbol{\alpha}_{\tau}$ would be equal to $\alpha_{m}$, the angle of internal friction. In practice, the angle of repose is smaller than the angle of internal friction, of those inside the mass and are often drier and sticker.
- Coefficient of internal friction is the measure of resistance present when one layer of solids over another layer of same particles. It is defined as:

Coeff. Of internal friction $=\tan \alpha_{m}$

- For free flowing material $\alpha_{m}$ is between $15^{\circ}$ to $30^{\circ}$
- In solid masses the pressure is not the same in all directions. If pressure is applied in one direction it creates some pressure in other directions, but it is always smaller than the applied pressure. It is minimum I the direction at right angles to the applied pressure. The ratio of the normal pressure to the applied pressure in a mass of solid, is a material constant, generally denoted by $\mathrm{K}^{\prime}$

$$
K^{\prime}=\frac{\text { normal pressure }}{\text { applied pressure }}=\frac{1-\sin \alpha_{m}}{1+\sin \alpha_{m}}
$$

$\mathrm{K}^{\prime}$ approaches zero for cohesive solids and free flowing material its value is between 0.36 to 0.6

- Coefficient of external friction is the measure of the resistance at an interface between particles and the wall of different material of construction.

Coefficient of External friction $=\tan \beta_{S}$

- Where $\beta_{\mathrm{S}}$ is the angle of external friction of solid and material ${ }_{24}$


## solids Convering

- Screw conveyors
- Belt conveyors
- Bucket elevators
- Spaced-Bucket Centrifugal-Discharge Elevators
- Spaced-Bucket Positive-Discharge Elevators
- Continuous-Bucket Elevators
- Super-capacity Continuous-Bucket Elevators
- V-Bucket Elevator-Conveyors
- Skip Hoists
- Vibrating or oscillating conveyors
- Continuous flow conveyors
- Apron Conveyors
- Pneumatic conveyors
- Hydraulic Conveyors


## SELECTION OF CONVEYORS

- Capacity requirement : Belt for larger capacity and screw cannot handle large capacity
- Length of travel : belt conveyors ; miles, Pneumatic convey 300 m , vibrating conveyor even less
- Lift or lift and horizontal shift : single or mixed
- Material characteristics - chemical and physical, size, friability, flowability abrasiveness, moisture or oxidation effect
- Processing requirement; dewatering, heating cooling


## Screw conveyor

- Helicoid ( helix rolled from flat steel bar) or sectional flight mounted on a pipe or shaft rotating in a $U$ shaped trough
- Horizontal of slight incline upto 20ofinely divided solids, sticky material, semisolid materials, boiler ash. Etc.
- Continuous spiral for dry granular free flowing material
- Discontinuous spirals for wet, muddy and thick materials.
- Short distance upto about 40m
- Types of flow :
- Archemedian flow or
- Plug flow
- Unit operation - mixing, heating \& cooling with hollow shaft



## BELT CONVEYORS

- Continuous belt passing around two large pulleys at two ends, one drive pulley other tail pulley.
- Universal application
- Very long distances several km
- Speed up to $300 \mathrm{~m} / \mathrm{min} 5000 \mathrm{tons} / \mathrm{hr}$
- Slope upto 30o
- Material - neoprene, Teflon, natural rubber, vinyls, cotton, asbestos fibre, etc.
- Various designs of idlers
- May require cleaning by revolving brush, metal or rubber scraper, taut wire



## Idlers and Plate support arrangements:

 (a) Flat belt on idler (b) flat belt on continuous plate (c)troughed belt on 20 deg idler (d) troughed belt on 45 deg idler (e) Same as d but with rolls of equal lengths (f) troughed plate on continuous plate
(a)

(d)

(b)

(e)

(c)

(f)


## Feeders to Belt conveyorsVibratory and Star Feeder



# belt conveyor discharge arrangements: <br> (a) over end pulley (b) over end pulley by reversible shuttle conveyor (c) through travelling tripper(d) through fixed trippers 



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| :--- |
| Telephone Number |
| E-Mail Address |

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- Bucket elevator consists of a number of buckets attached to a continuous double strand chain which passes over two pulleys
- Solids fed directly to bucket and also scooped up from the bottom.
- Emptied from the top by turning of the bucket.
- Line speed 1-2m/s

BUCKET ELEVATORS
(a)Spaced-Bucket Centrifugal-Discharge Elevators
(b)Spaced-Bucket Positive-Discharge Elevators
(c)Continuous-Bucket Elevators
(d)Supercapacity Continuous-Bucket Elevators


- Spaced bucket ; Centrifugal discharge - free flowing, fine or small lump material like grain, coal, sand or dry chemicals
- Spaced bucket positive discharge- buckets are for sticky materials which tend to lump, inverted for positive discharge, knockers can also be used
- Continuous - finely pulverized or fluffy materials, the back of the preceding bucket serves as a discharge chute for the bucket. Gentle movement Preventing degradation
- Super capacity continuous bucket: Very high tonnage, big particles, Generally inclined


## SKIPHOIST: Batch bucket elevator



- Uncounter weighted: only winding machine power requirement is high
- Counter weight : reduces power consumption
- Balanced use two buckets and hence works twice as fast


## CONTINUOUS FLOW CONVEYOR

- Principle: When a surface is pulled transversely through a mass of granular powder or small lump material it will pull a cross section of material along with it which is greater than the area of the surface itself.
- Generally a chain with blades is operated in a powder to cause the powder to flow in the same direction.


## FLIGHTS FOR CONTINUOUS FLOW CONVEYORS



- L- highly adhesive powder
- B-moderate adhesive powder
- KL highly adhesive powder containing granular material
- KB1 - Moderately adhesive powder containing some granular material



## CONTINUOUS FLOW CONVEYORS:

 (a) Horizontal (b) Z type (c) Loop feed elevator for dewatering

## APRON COVEYORS

- A type of continuous flow conveyor where series of overlapping pans are mounted between two strands of roller chains



## PRESSURE, VACUUM, PRESSURE-VACUUM PNEUMATIC TRANSPORTATION



(b) Vocuum

## FLUIDIZATION



- Gas flow between 15 to $30 \mathrm{~m} / \mathrm{s}$ in pipes ranging from 50 to 400 mm diameter.
- Particle size range from fine powder to 6.5 mm , Bulk density from 16 to $3200 \mathrm{~kg} / \mathrm{m} 3$
- Pressure System
- 1-5 atm gauge
- Free flowing material for any particle size - 5-6 mm
- Flow rates more than $9000 \mathrm{~kg} / \mathrm{hr}$
- Pressure loss in the system 0.5 atm
- Rotary Air lock valve required
- Vacuum System
- Lower flow rates $7000 \mathrm{~kg} / \mathrm{hr}$ and 300 m
- Fine powders
- No Rotary air lock valve required.
- Pressure Vacuum system


## HYDRAULIC CONVEYING /SLURRY TRANSPORTATION

- Generally particles less than 50 micron
- Main application in Mining industry
- Fluid used is water
- Velocity more than settling velocity of particles,
- Critical velocity , below which particles will settle out range between $1-5 \mathrm{~m} / \mathrm{s}$,
- Pressure drop calculated using same equation with allowance for increase in density and viscosity.


## STORAGE OF SOLIDS

- BULK STORAGE

Coarse large quantity solids like gravel and coal outside in large piles.
Protection from

- BIN STORAGE -
$\checkmark$ Silos - tall and small diameter
$\checkmark$ Bins - fairly wide and Not tall
$\checkmark$ Hoppers - Small vessel with sloping bottom, generally temporary storage before feeding solids to a process.



## Types of Bins

Wedge/Plane Flow



Pyramidal


## Types of Bins

Conical


Pyramidal


## PRESSURE IN BINS AND SILOS

Janssen Equation: Pressure at any height h , from the base

$$
P=\frac{\rho_{b} g D}{4 f_{w} k}\left[1-\exp \frac{4 f_{w} K(h-H)}{D}\right]
$$

If value of H is sufficiently large which is the case at the base of the base of the cylindrical portion of the hopper:

$$
P_{O}=\frac{\rho_{b} g D}{4 f_{w} K}
$$

$\rho_{b}=$ Bulk density
$\mathrm{H}=$ level of solid bed,
$\mathrm{g}=$ acceleration due to gravity
D = Diameter of hopper
$f_{w}=$ Coefficient of friction between solids and wall

$$
K^{\prime}=\frac{\text { normal pressure }}{\text { applied pressure }}=\frac{1-\sin \alpha_{m}}{1+\sin \alpha_{m}}
$$

$\alpha_{m}=$ effective angle of internal friction.

## Pressure at the base of a vertical bin filled with particulate solids



Fig. 4.5 A Vertical bin filled with particulate solids.

$$
P=\frac{\rho_{b} g D}{4 f_{w} k}\left[1-\exp \frac{4 f_{w} K(h-H)}{D}\right]
$$

Height (in)

## FLOW OUT OF BINS

- Mass Flow - all the material in the hopper is in motion, but not necessarily at the same velocity [Cone angle from vertical axis=0-40o]
- Funnel Flow - centrally moving core, dead or non-moving annular region
- Expanded Flow - mass flow cone with funnel flow above it


(A) MASS FLOW

(B) FUNNEL FLOW
funnel FLOW

Figure 10-1. In mass flow (A) all material moves in the bin including near the walls. In funnel flow (B) the material moves in a central core with stagnant material near the walls. Expanded flow (C) is a combination of mass flow in the hopper exit and funnel flow in the bin above the hopper (normally used in retrofit situations).

## COMMON DESIGNS FOR MASS FLOW HOPPERS



## Design for Funnel Flow


(A) PYRAMID,

SQUARE OPENING

(B) CONICAL

(C) CYLINDRICAL FLAT-BOTTOMED SLOT OPENING


## HOPPER DESIGN PROBLEMS



## HOPPER DESIGN PROBLEMS

- RATHOLING/PIPING. Ratholing or piping occurs when the core of the hopper discharges (as in funnel flow) but the stagnant sides are stable enough to remain in place without flowing, leaving a hole down through the center of the solids stored in the bin
- FLOW IS TOO SLOW. The material does not exit from the hopper fast enough to feed follow on processes.
- NO FLOW DUE TO ARCHING OR DOMING. The material is cohesive enough that the particles form arch bridges or domes that hold overburden material in place and stop the flow completely.
- FLUSHING. Flushing occurs when the material is not cohesive enough to form a stable dome, but strong enough that the material discharge rate slows down while air tries to penetrate into the packed material to loosen up some of the material. The resulting effect is a sluggish flow of solids as the air penetrates in a short distance freeing a layer of material and the process starts over with the air penetrating into the freshly exposed surface of material.


## HOPPER DESIGN PROBLEMS

- INCOMPLETE EMPTYING. Dead spaces in the bin can prevent a bin from complete discharge of the material.
- SEGREGATION. Different size and density particles tend to segregate due to vibrations and a percolation action of the smaller particles moving through the void space between the larger particles
- TIME CONSOLIDATION. For many materials, if allowed to sit in a hopper over a long period of time the particles tend to rearrange themselves so that they become more tightly packed together. The consolidated materials are more difficult to flow and tend to bridge or rat hole.
- CAKING. Caking refers to the physiochemical bonding between particles what occurs due to changes in humidity. Moisture in the air can react with or dissolve some solid materials such as cement and salt. When the air humidity changes the dissolved solids re-solidify and can cause particles to grow together.

