Patterns, Pairs & Variables



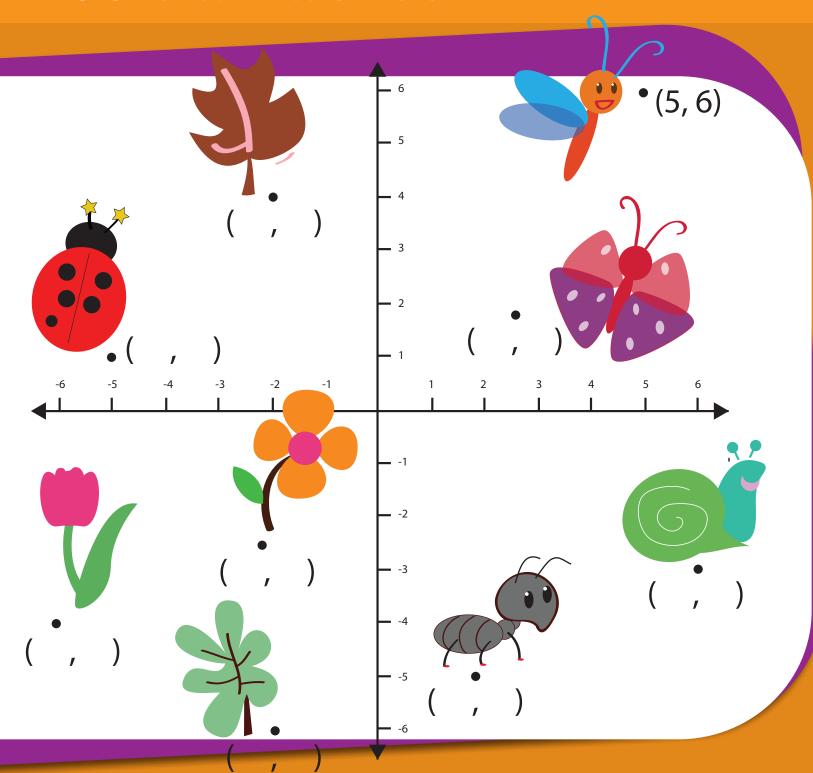




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Certificate of Completion
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Find out what number is added or subtracted to get the next number. Repeat the process to fill in the missing numbers. Write the pattern used on the blank lines to the right. (Hint: The patterns can be whole numbers OR fractions.) Example:

LXG	5	10 15	20	25	30 35	40	45	+5	
1.		4	7	10				21	
2.	3		11	15		23			
3.	5		11		17		23		
4.		8		4		0		-4	
5.	56		32		8		-16		
6.	45		37		29	25	21		
7.	5 2	4	11 2	7					
8.		9		8	15 2			6	
9.	11		37			76	89		
10.	15			33		45		57	
11.	7 2	6		11		16		21	
12.	20				15		50 4	45	
13.			57	41		9		-23	
14.	-52		2		56	83			
15.	<u>1</u> 5	1	9 5				5		

Find out what whole number OR fraction is multiplied or divided to get the next number. Repeat the process to fill in the missing numbers. Write down the pattern used on the blank lines to the right. Example:

 $\chi\left(\frac{3}{2}\right)$

2

2.

3.

5.

6.

7.

8.

9.

10.

11. 81

12.1024

14.

Treasure-hunter Jack has received a secret message in a sequence of numbers. Decoded, it will tell him the location of the world's largest diamond, the Golden Jubilee. The message is encoded in a "letter number" cipher. This is when letters are replaced as numbers. However only the MISS-ING NUMBERS will reveal the true location. Find out what these numbers are!

(Hint: The numbers follow a pattern. You will have to subtract, divide, add or multiply by a whole number or fraction to find the missing numbers.)

Example:

(+5) 5

10

15

20

25

Then the letter is Y

A	В	С	D	Е	F	G	Н	ı	J	K	L	M
1	2	3	4	5	6	7	8	9	10	11	12	13
N	0	Р	Q	R	S	T	U	V	W	Χ	Υ	Z
14	15	16	17	18	19	20	21	22	23	24	25	26

1. 5

10

O

40

80

2.

29

22

15

8

3.

 $\frac{27}{2}$

-60

-36

-12

6

4

36

5.

4.

81

27

9

3

6.

7.

3024

20

504

16

84

12

8

3



Where is the location of the Golden Jubilee Diamond?

1

2a

2b

3

4

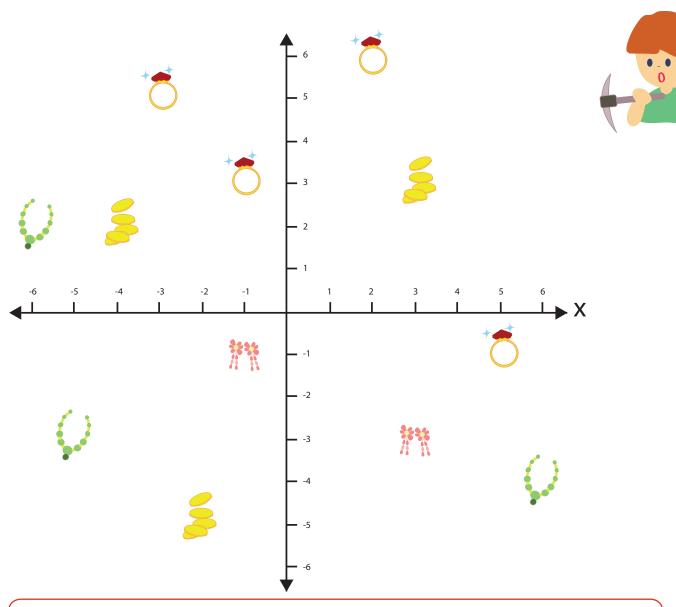
5

6

7

Coordinates Treasure Hunt!

Help the treasure hunter by looking at the coordinate plane below and answering the questions.



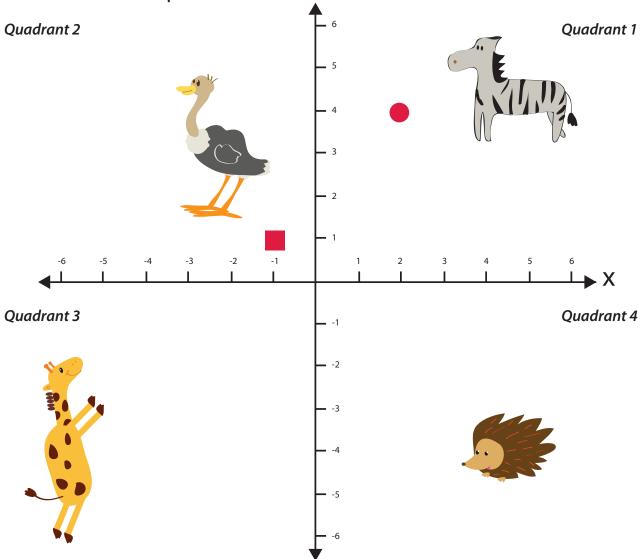
- 1. What treasure is located at (5, -1)?
- 2. What treasure is located at (-2, -5)?
- 3. What treasure is located at (6, -4)?
- 4. Write the coordinates of the earrings below.



5. Which quadrant has the most treasure in it?

Name the Quadrant

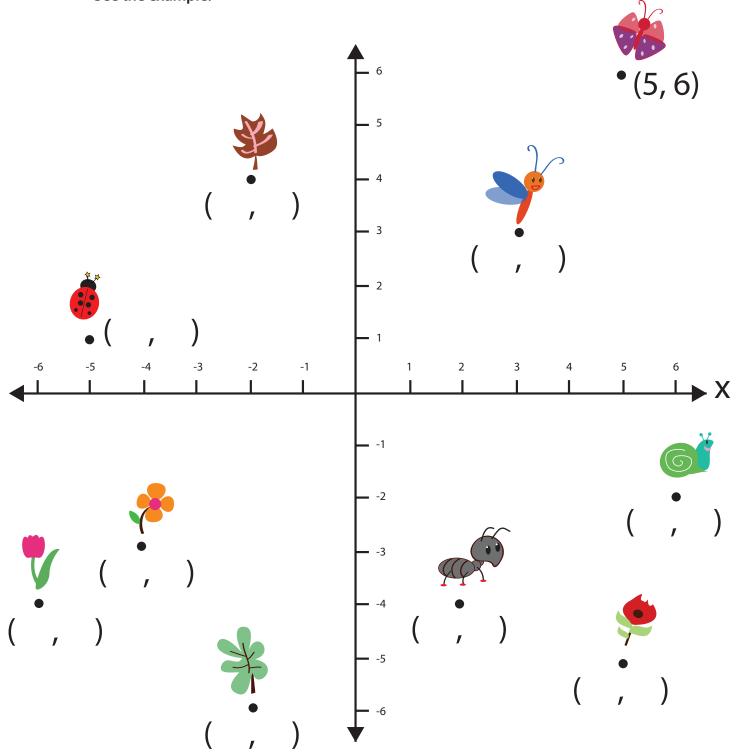
The coordinate plane is divided into four quadrants. Look at the coordinate plane below and answer the questions.



- 1. Which quadrant is the giraffe in?
- 2. Which quadrant is the zebra in?
- 3. Which quadrant is the ostrich in?
- 4. Draw a triangle and a rectangle in quadrant four.
- 5. Draw a circle and a square in quadrant three.
- 6. The coordinates of the square in quadrant 2 are (-1, 1). What are the coordinates of the circle in quadrant one?

Write the Coordinates

Look at the position of each object below, and write the coordinates in the parentheses. See the example.



Which quadrant does not contain an insect?

Expression vs. Equation

An expression in math is a sentence containing numbers and the operations. Below are examples of expressions:

$$2 + 3$$

$$\frac{2}{5}$$
 x $\frac{6}{6}$

An equation is the statement of numbers, expressions, operations that are equal. **Examples:**

$$2 + 3 = 4 + 1$$

$$2+3=4+1$$
 $17-16+2=3$

$$\frac{2}{5} \times \frac{6}{6} = \frac{12}{30}$$

$$6 = 6$$

$$(3 \times 5) - (6 \times 2) = 15 - 12$$
 $y - 20 = 10 + x$

$$y - 20 = 10 + x$$

Look at the statements below. Write "ex" if the statement is an expression. Write "eq" if the statement is an equation.

$$\frac{(40-5)}{7}=5$$

$$(6 \times 4) = (3 \times 8)$$

$$(5 \times 5 \times 5)$$

$$0.1 + 0.5 = 0.3 + 0.3$$

$$\frac{9}{2} \times \frac{4}{3} = 6$$

Challenge

Complete the equation by writing the expression on the other side of equation. See the example.

$$60 + 4 = 8 \times 8$$

$$4 \times 2 =$$

Writing Expressions

With Variables #1



An expression in math is a sentence containing numbers and the operations. Below are examples of expressions:

$$17 - 16 + 2$$

$$\frac{2}{5}$$
 x $\frac{6}{6}$

$$(3 \times 5) - (6 \times 2)$$

A variable represents the unknown number in the expression or equation. For example, $4 \times t = 12$. The letter "t" represents the number which multiplies by 4 to equal 12.

Read the sentences below and write an expression. See the example.

Robin has 10 chocolates and Martin has m chocolates. Write an expression of chocolates that Martin and Robin have together.

> Robin has 10 Martin has m

The expression is 10 + m



Bobby grows 20 carrots and Tommy grows k carrots. Write the expression of carrots that both Bobby and Tommy have.



Julie has 7 jelly beans. She gave **y** jelly beans to Susie. Write the expression of jelly beans that she has left.





Sally at 2 pieces of cake in the morning and n pieces in the evening. Write the expression for the amount of cake she had today.

Ronny had 12 paper clips. He lost **p** of them. Write the expression of paper clips Ronny has left.



Writing Expressions With Variables #2

An expression in math is a sentence containing numbers and the operations. Below are examples of expressions:

$$(3x) - (6x + 2)$$

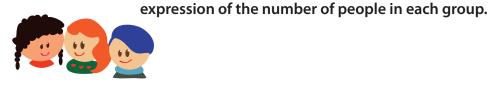
A variable is a letter (x, y, t, etc.) that represents the unknown number in an expression or equation. When a variable is next to a number, it means multiply. For example: 4t = 12 means 4 multiplied by t equals 12.

Read the sentences below and write an expression. See the example below.

There are y letters in the bag. They are divided into 4 equal groups. Write an expression of the letters after dividing.

Number of letters is **y** Divided into 4

There are 20 people in the room. They are divided into $m{m}$ equal groups. Write the division





Ashley has 25 flowers. The number of flowers Sam has is **z** times more than what Ashley has. Write a multiplication expression of flowers that Sam has.

A piece of wood is 20 feet long. It was cut into k equal pieces to make a track. Write a division expression of the length of each piece of wood.



Mary has p handbags. Lynn has 2 times more than Mary. Write the multiplication expression of the handbags that Lynn has.



Algebraic Expressions

Simplify the following expressions.

1.)
$$5a + 6a =$$

$$2.) 3a + a =$$

$$3.) 8a - 3a =$$

4.)
$$10a - 2a =$$

$$5.) 9a + 4a =$$

6.)
$$11a - 7a =$$

$$7.) 4b + 3b =$$

8.)
$$12b - 6b =$$

$$9.) 5b + 9b =$$

Complete the following expressions.

1.)
$$12 \times 3 - 5 + 4 =$$

$$2.) 4 + 7 \times 2 - 8 =$$

3.)
$$5 - 7 + 2 \times 10 =$$

4.)
$$15 \div 3 + 8 \times 5 =$$

5.)
$$11 \times 3 - 12 \div 4 =$$

5.)
$$11 \times 3 - 12 \div 4 =$$
 6.) $5 + 9 - 16 \div 2 =$

Combine like terms to simplify the following expressions.

1.)
$$3a(a+4) - 2a + 7 =$$

2.)
$$5a + 3a - 15 \div 3 =$$

$$3.) 4(3+9) + 10a - 4a =$$

4.)
$$(21 \div 7)(4a + a) - 12 =$$

5.)
$$17 + 4(3 + a) - a =$$

6.)
$$10a - 4a + 27 \div 3 =$$

Algebra Action! Value of The Expression

A variable represents the unknown number in the expression or equation. For example, $4 \times t = 12$. The letter "t" represents the number which multiplies by 4 to equal 12.

An expression in math is a sentence containing numbers and the operations. Below are examples of expressions:

$$\frac{2}{5}$$
x

We can find the value of the expression 7 + y by placing the variable with the number. For example: if y = 5

$$7 + 5 = 12$$

Find the value of the expressions below. Show your work.

$$4+y+7$$

$$(12 - b) + 5$$

If
$$h = 4$$

If
$$y = 8$$

If
$$b = 3$$

$$(5 x m) + 1$$

If
$$m = 6$$

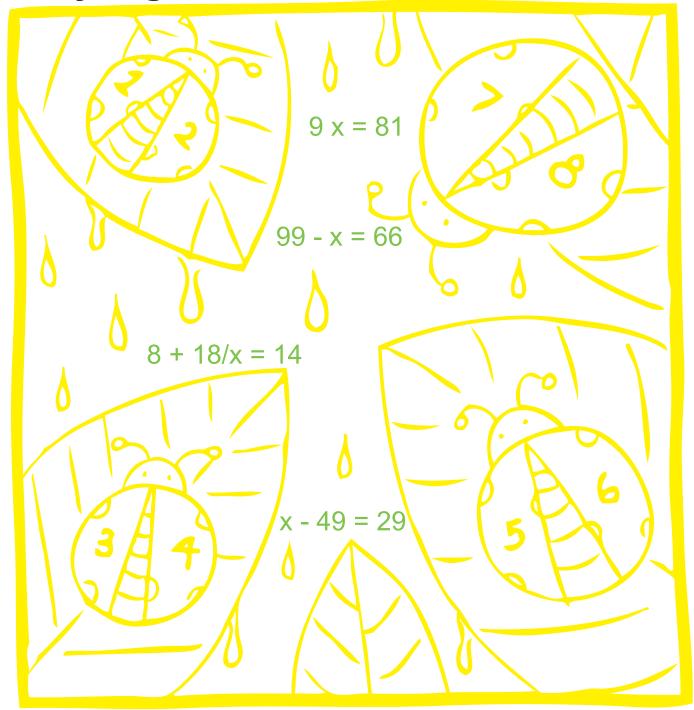
$$(4 \times p) \times 2$$

If
$$p = 10$$

$$20 + (6 \times w)$$

If
$$w = 3$$

Ladybug Math

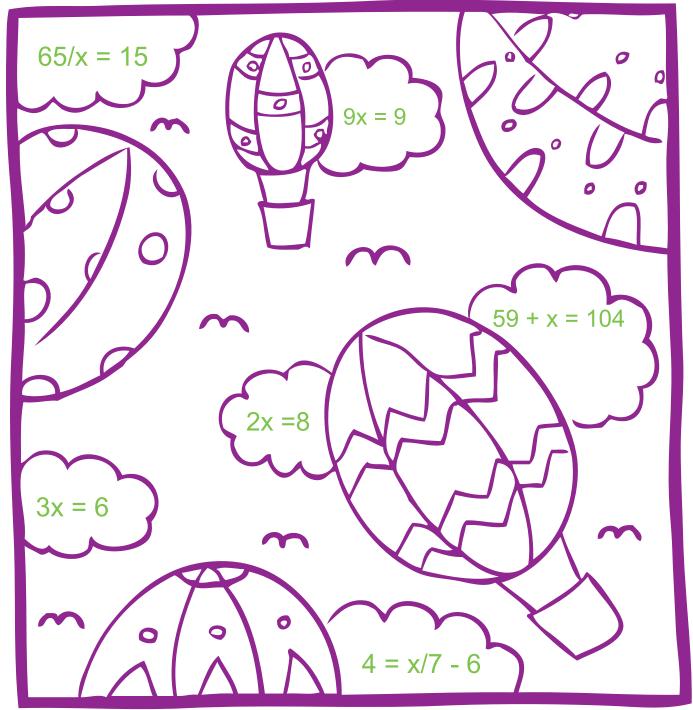


Note: More worksheets at www.education.com/worksheets

Instructions:



Air Balloon Math

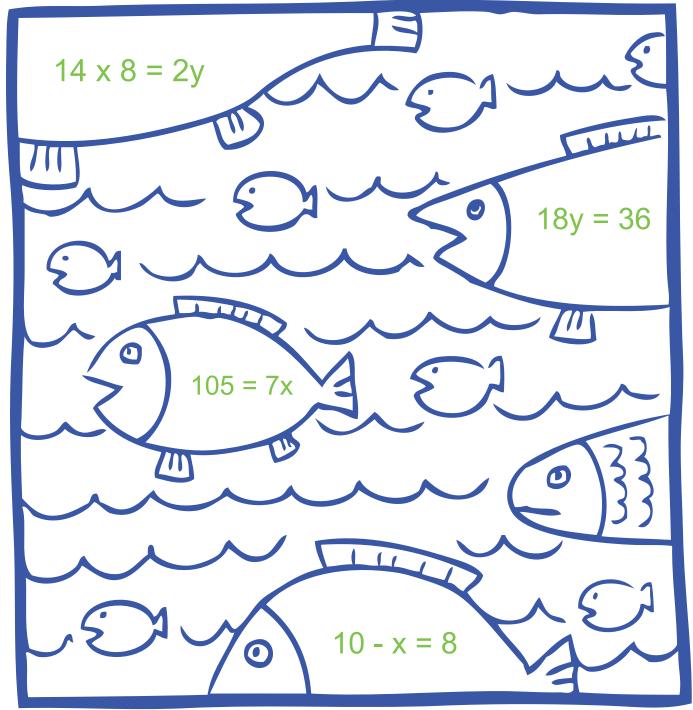


Note: More worksheets at www.education.com/worksheets

Instructions:



Fish Math

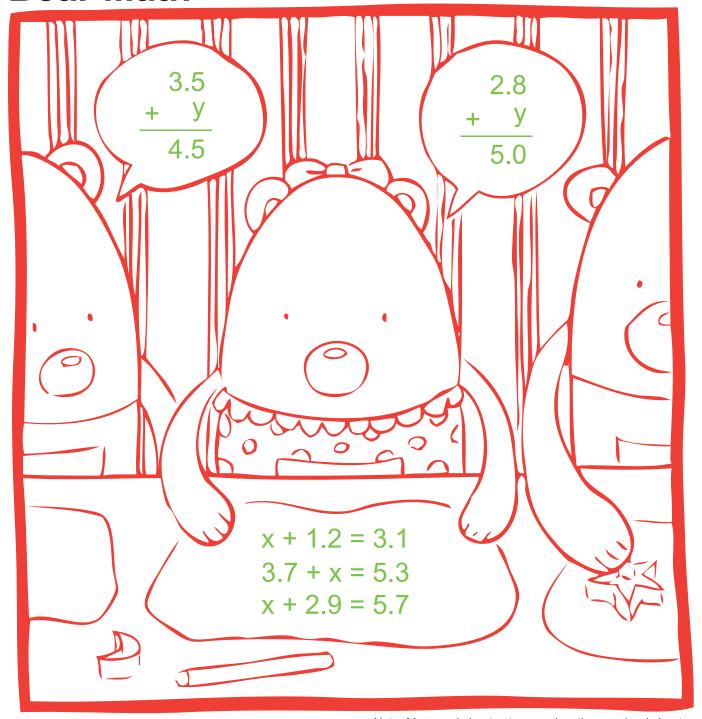


Note: More worksheets at www.education.com/worksheets

Instructions:



Bear Math



Note: More worksheets at www.education.com/worksheets

Instructions:



Forest Math

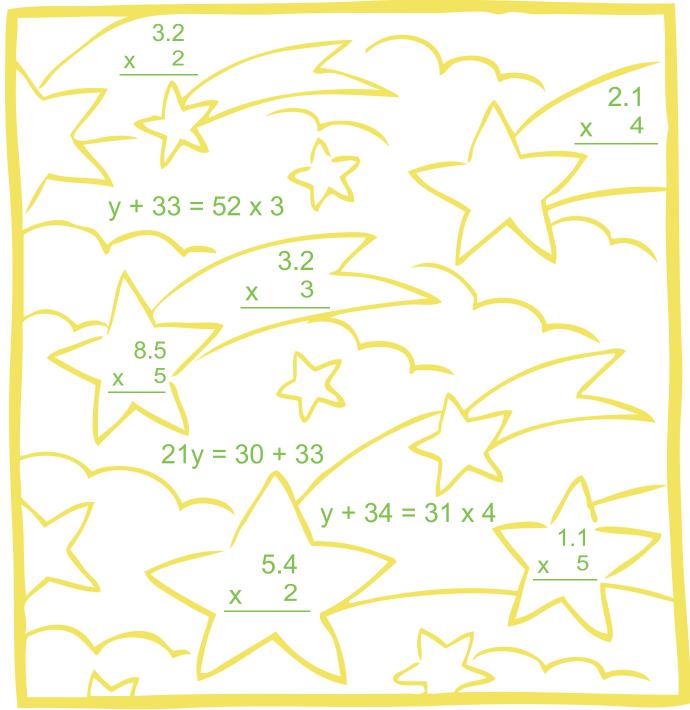


Note: More worksheets at www.education.com/worksheets

Instructions:



Star Math



Note: More worksheets at www.education.com/worksheets

Instructions:





Patterns, Pairs and Variables

Number Patterns #1 Number Patterns #2 Number Patterns #3 Coordinates Treasure Hunt Name the Quadrant Write the Coordinates Expression vs. Equation Writing Expressions with Variables #1 Writing Expressions with Variables #2 Algebraic Expressions Algebra Action! Value of the Expression Ladybug Math Air Balloon Math Fish Math Bear Math Forest Math Star Math

NUMBER PATTERNS

Find out what number is added or subtracted to get the next number. Repeat the process to fill in the missing numbers. Write the pattern used on the blank lines to the right. (Hint: The patterns can be whole numbers OR fractions.) Example:

EXO	mpie: 5	10 15	20	25	30 35	40	45	+5	
1.	1	4	7	10	13	16	19	21	+ 3
2.	3	7	11	15	19	23	27	31	+ 4
3.	5	8	11	14	17	20	23	26	+ 3
4.	10	8	6	4	2	0	-2	-4	- 2
5.	56	44	32	20	8	-4	-16	-28	- 12
6.	45	41	37	33	29	25	21	17	- 4
7.		4	11 2	7	<u>17</u>	10	23 2	13	+ 3/2
8.	19 2	9	17 2	8	15 2	7	13 2	6	- 1
9.	11	24	37	50	63	76	89	102	+13
10.	15	21	27	33	39	45	51	57	+6
11.	7 2	6	<u>17</u> 2	11	27 2	16	37 2	21	+ 5 2
12.	20	<u>75</u> 4	<u>70</u> 4	<u>65</u> 4	15	<u>55</u> 4	50 4	45	- 5 4
13.	89	73	57	41	25	9	-7	-23	- 16
14.	-52	- 25	2	29	56	83	110	137	+ 27
15.	<u>1</u> 5	1	9 5	13 5	<u>17</u> 5	<u>21</u> 5	5	<u>29</u> 5	+ -4 5

NUMBER PATTERNS

Find out what whole number OR fraction is multiplied or divided to get the next number. Repeat the process to fill in the missing numbers. Write down the number pattern on the right blank lines. Example:

шріє	⇒.			0.1	242	720	, 3 \
Ω	12	1.0	27	01	243	/29	$\chi\left(\frac{3}{2}\right)$
O	1 2	10	21	2	4	8	_ ^(2 /

8	12	18 2	$\frac{81}{2}$	243 <u>72</u> 4 8				
1	<u> </u>	3 -	9 27 2	81 2	243	729	<u>2187</u> 2	x 3
2.	5 1	2	0 40	80	160	320	640	x 2
3. 31:	2 <u>5</u>	250 10	00 800	640	512	<u>2048</u> 5	8192 25	$x\left(\frac{4}{5}\right)$
4. 10	00 50	00 25	50 125	125	125	<u>125</u> 8	<u>125</u> 16	÷ 2
5.	3	11 3	3 99	297	891	2673	8019	x3
6. <i>7</i>	7 1	2	8 56	112	224	448	896	x 2
7. 8	1	1	8 27	81 2	234	702	2106 16	$x\left(\frac{3}{2}\right)$
8. 43	74 29	16 19	1296	864	576	384	256	$x\left(\frac{2}{3}\right)$
9. <u>3</u>	2	3 6	12	24	48	96	192	x 2
10. 7	1	14 2	56	112	224	448	896	x 2
11. 8	1 2	27	3	1	<u>1</u> 3	1 9	<u>1</u> 27	÷ 3
12. 10	24 2	56 6	4 16	4	1	1 4	16	÷ 4
13. 12	28	16	4	32	256	2048	16384	x 8
14. <mark>12</mark>	<mark>500</mark> 28	500 50	100	20	4	<u>4</u> <u>5</u>	<u>4</u> 25	÷ 5
15. 8	<u> </u>	$\frac{2}{9}$	18	162	1458	13122	118098	

Treasure-hunter Jack has received a secret message in a sequence of numbers. Decoded, it will tell him the location of the world's largest diamond, the Golden Jubilee. The message is encoded in a "letter number" cipher. This is when letters are replaced as numbers. However only the MISS-ING NUMBERS will reveal the true location. Find out what these numbers are!

(Hint: The numbers follow a pattern. You will have to subtract, divide, add or multiply by a whole number or fraction to find the missing numbers.)

Example:

(+5) 5 10 15

20

25

Then the letter is Y

A	В	С	D	Е	F	G	Н	ı	J	K	L	M
1	2	3	4	5	6	7	8	9	10	11	12	13
N	0	Р	Q	R	S	T	U	V	W	Χ	Υ	Z
14	15	16	17	18	19	20	21	22	23	24	25	26

- 1. 5
- 10
- 20
- 40

- 2. 29
- 22
- 15

- 3.
- 6
- 4

4. -60

5.

- -36
- -12

12

- 12
- 27
- 3

36

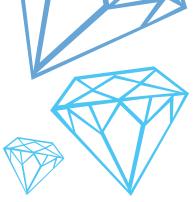
80

3024 6.

81

- 504
- 84
- 14

- 7. 20
- 16
- 8



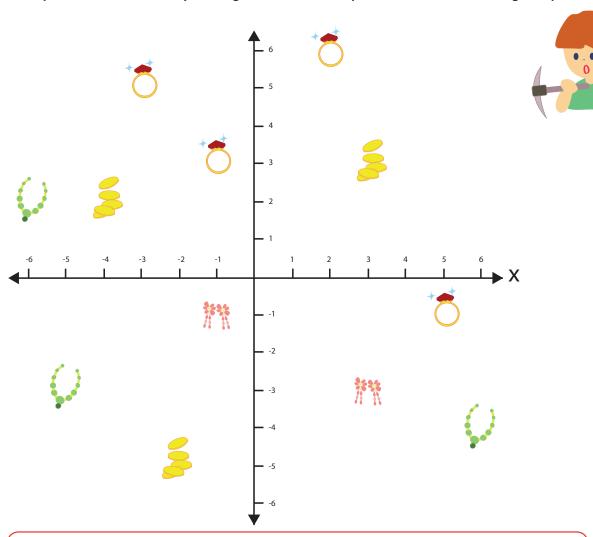
Where is the location of the Golden Jubilee Diamond?

2a 2b



Coordinates Treasure Hunt!

Help the treasure hunter by looking at the coordinate plane below and answering the questions.



- 1. What treasure is located at (5, -1)? **RING**
- 2. What treasure is located at (-2, -5)? **COINS**
- 3. What treasure is located at (6, -4)? **NECKLACE**
- 4. Write the coordinates of the earrings below.

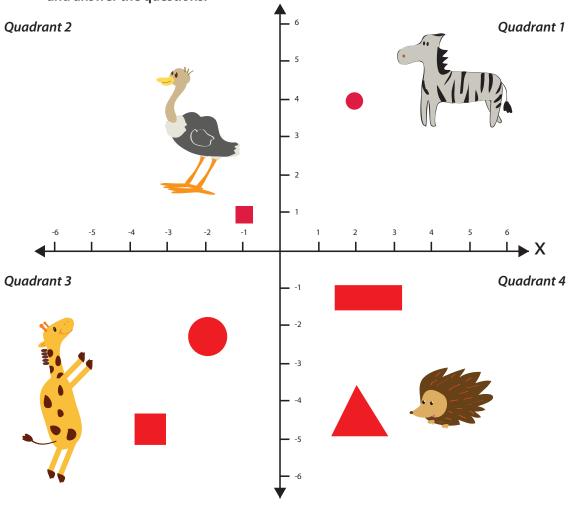


5. Which quadrant has the most treasure in it? QUADRANT 2



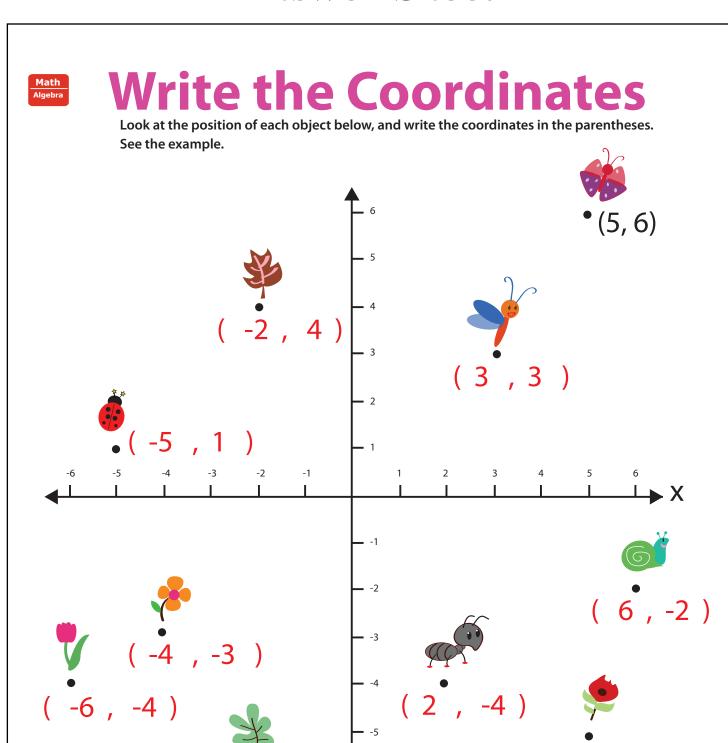
Name the Quadrant

The coordinate plane is divided into four quadrants. Look at the coordinate plane below and answer the questions.



- 1. Which quadrant is the giraffe in? **QUADRANT 3**
- 2. Which quadrant is the zebra in? QUADRANT 1
- 3. Which quadrant is the ostrich in? QUADRANT 2
- 4. Draw a triangle and a rectangle in quadrant four.
- 5. Draw a circle and a square in quadrant three.
- 6. The coordinates of the square in quadrant 2 are (-1, 1).

 What are the coordinates of the circle in quadrant one? (2,4)



Which quadrant does not contain an insect?

QUADRANT 3



Expression vs. Equation

An expression in math is a sentence containing numbers and the operations. Below are examples of expressions:

$$\frac{2}{5} \times \frac{6}{6}$$

An equation is the statement of numbers, expressions, operations that are equal. **Examples:**

$$2 + 3 = 4 + 1$$

$$2+3=4+1$$
 $17-16+2=3$

$$\frac{2}{5} \times \frac{6}{6} = \frac{12}{30}$$

$$6 = 6$$

$$(3 \times 5) - (6 \times 2) = 15 - 12$$

$$y - 20 = 10 + x$$

Look at the statements below. Write "ex" if the statement is an expression. Write "eq" if the statement is an equation.

$$\frac{eq}{7} = 5$$

eq
$$(6 \times 4) = (3 \times 8)$$

eq
$$\frac{9}{2} \times \frac{4}{3} = 6$$

Challenge

Complete the equation by writing the expression on the other side of equation. See the example.

$$60 + 4 = 8 \times 8$$

$$25 - 15 = 2 \times 5$$

$$4 \times 2 = 4 + 4$$

$$\frac{12}{4} = \frac{1+2}{1}$$



Writing Expressions With Variables #1



An expression in math is a sentence containing numbers and the operations. Below are examples of expressions:

$$\frac{2}{5} \times \frac{6}{6}$$

$$(3 \times 5) - (6 \times 2)$$

A variable represents the unknown number in the expression or equation. For example, $4 \times t = 12$. The letter "t" represents the number which multiplies by 4 to equal 12.

Read the sentences below and write an expression. See the example.

Robin has 10 chocolates and Martin has *m* chocolates. Write an expression of chocolates that Martin and Robin have together.

> Robin has 10 Martin has *m*

The expression is 10 + m



Bobby grows 20 carrots and Tommy grows k carrots. Write the expression of carrots that both Bobby and Tommy have.



Bobby has 20 Tommy has K

The expression is 20 + k

Julie has 7 jelly beans. She gave y jelly beans to Susie. Write the expression of jelly beans that she has left. Julie has 7



Susie has y

The expression is 7 - y



Sally ate 2 pieces of cake in the morning and *n* pieces in the evening. Write the expression for the amount of cake she had today.

Sally ate 2 in the morning Sally ate n in the evening

The expression is 2 + n

Ronny had 12 paper clips. He lost **p** of them. Write the expression of paper clips Ronny has left.



Ronny has 12 Ronny lost p

The expression is 12 - p



More worksheets at www.education.com/worksheets



Writing Expressions With Variables

An expression in math is a sentence containing numbers and the operations. Below are examples of expressions:

$$(3x) - (6x + 2)$$

A variable is a letter (x, y, t, etc.) that represents the unknown number in an expression or equation. When a variable is next to a number, it means multiply. For example: 4t = 12 means 4 multiplied by t equals 12.

Read the sentences below and write an expression. See the example.

There are y letters in the bag. They are divided into 4 equal groups. Write an expression of the letters after dividing.

Number of letters is **y**Divided into 4

The expression of division is

There are 20 people in the room. They are divided into *m* equal groups. Write the division expression of the number of people in each group.





Ashley has 25 flowers. The number of flowers Sam has is **z** times more than what Ashley has. Write a multiplication expression of flowers that Sam has.

A piece of wood is 20 feet long. It was cut into k equal pieces to make a track. Write a division expression of the length of each piece of wood.



Mary has p handbags. Lynn has 2 times more than Mary. Write the multiplication expression of the handbags that Lynn has.



Algebraic Expressions

(answer sheet)

Simplify the following expressions.

1.)
$$5a + 6a = 11a$$

2.)
$$3a + a = 4a$$

3.)
$$8a - 3a = 5a$$

4.)
$$10a - 2a = 8a$$

$$5.) 9a + 4a = 13a$$

6.)
$$11a - 7a = 4a$$

7.)
$$4b + 3b = 7b$$

8.)
$$12b - 6b = 6b$$

9.)
$$5b + 9b = 14b$$

Complete the following expressions.

1.)
$$12 \times 3 - 5 + 4 = 35$$

 $36 - 5 + 4$
 $31 + 4$

2.)
$$4 + 7 \times 2 - 8 = 10$$

 $4 + 14 - 8$
 $18 - 8$

3.)
$$5-7+2 \times 10 = 18$$

 $5-7+20$
 $20-2$

4.)
$$15 \div 3 + 8 \times 5 = 45$$

 $5 + 8 \times 5$
 $5 + 40$

5.)
$$11 \times 3 - 12 \div 4 = 30$$

 $33 - 12 \div 4$
 $33 - 3$

6.)
$$5 + 9 - 16 \div 2 = 6$$

 $5 + 9 - 8$
 $14 - 8$

Combine like terms to simplify the following expressions.

1.)
$$3a(a + 4) - 2a + 7 = 3a^2 + 10a + 7$$

 $3a^2 + 12a - 2a + 7$

2.)
$$5a + 3a - 15 \div 3 = 8a - 5$$

 $5a + 3a - 5$

3.)
$$4(3+9) + 10a - 4a = 48 + 6a$$

 $4(12) + 10a - 4a$
 $48 + 10a - 4a$

4.)
$$(21 \div 7)(4a + a) - 12 = 15a - 12$$

 $3(4a + a) - 12$
 $3(5a) - 12$

5.)
$$17 + 4(3 + a) - a = 29 + 3a$$

 $17 + 12 + 4a - a$
 $29 + 4a - a$

6.)
$$10a - 4a + 27 \div 3 = 6a + 9$$

 $10a - 4a + 9$



Algebra Action! ANSWER SHEET Value of The Expression

A variable represents the unknown number in the expression or equation. For example, $4 \times t = 12$. The letter "t" represents the number which multiplies by 4 to equal 12.

An expression in math is a sentence containing numbers and the operations. Below are examples of expressions:

We can find the value of the expression 7 + y by placing the variable with the number. For example: if y = 5

1. Put 5 in the place of y

2. Calculate it

$$7 + 5 = 12$$

Find the value of the expressions below. Show your work.

17 - h

$$4 + y + 7$$

(12 - b) + 5

If h = 4

$$17 - 4 = 13$$

If
$$y = 8$$

$$4 + y + 7$$

$$4 + 8 + 7 = 19$$

If b = 3

$$(12 - b) + 5$$

$$(12 - 3) + 5 = 14$$

 $20 + (6 \times w)$

(5 x m) + 1

If
$$m = 6$$

$$(5 x m) + 1$$

$$(5 \times 6) + 1 = 31$$

If p = 10

$$(4 \times p) \times 2$$

$$(4 \times 10) \times 2 = 80$$

 $(4 \times p) \times 2$

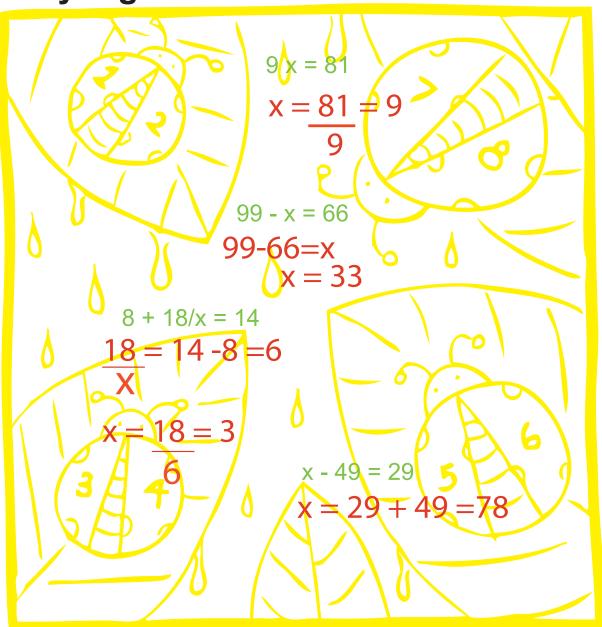
If w = 3

$$20 + (6 \times w)$$

$$20 + (6 \times 3) = 38$$

ANSWER SHEET

Ladybug Math



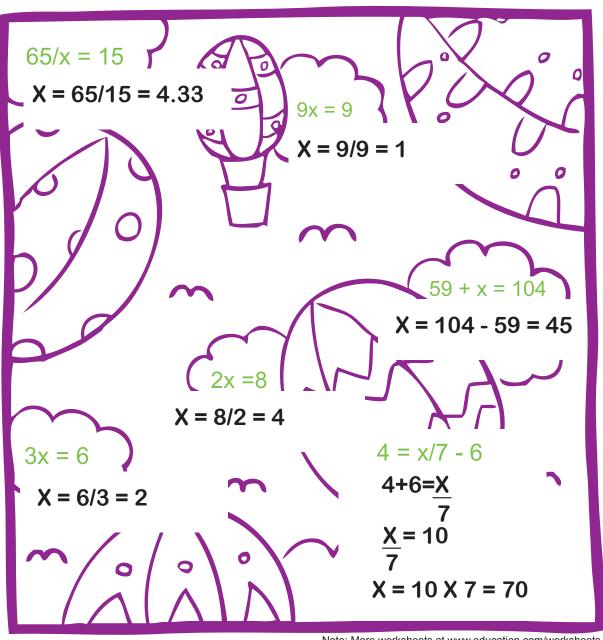
Note: More worksheets at www.education.com/worksheets

Instructions:



ANSWER SHEET

Air Balloon Math



Note: More worksheets at www.education.com/worksheets

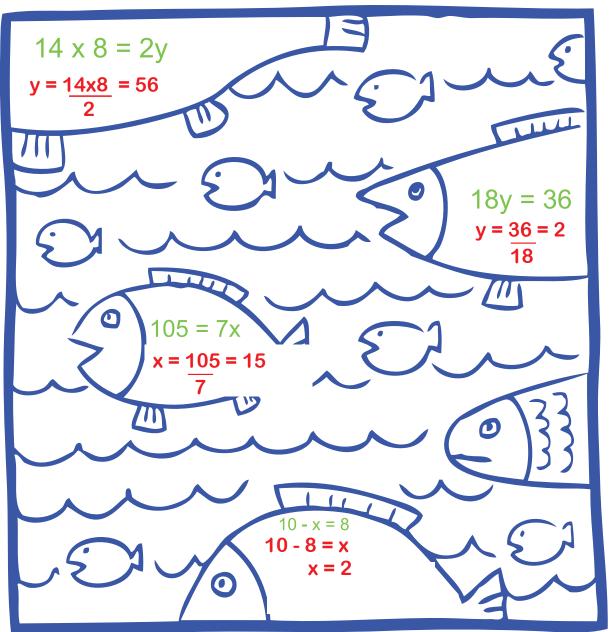
Instructions:

Complete each math problem and color the page!

created by: education.com www.education.com/worksheets

ANSWER SHEET

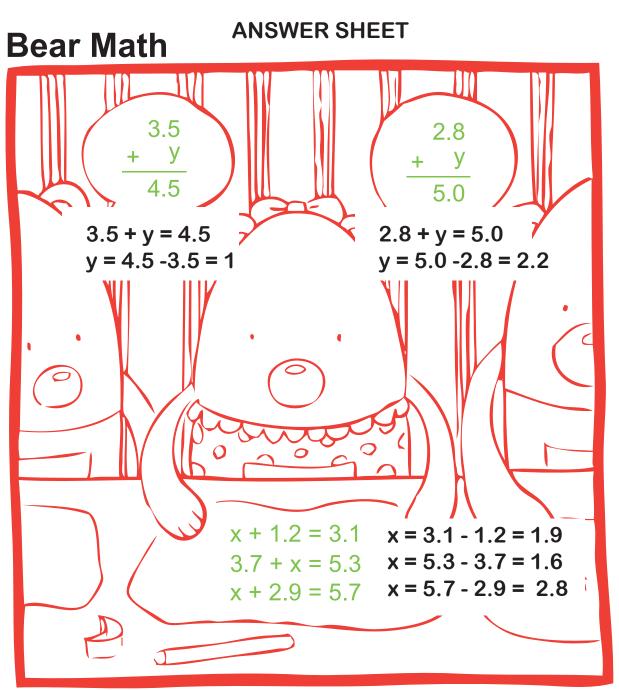
Fish Math



Note: More worksheets at www.education.com/worksheets

Instructions:



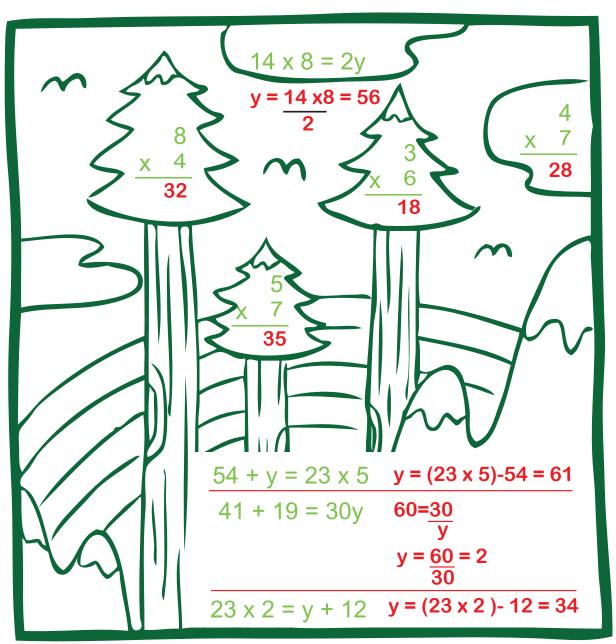


Note: More worksheets at www.education.com/worksheets

Instructions:

ANSWER SHEET

Forest Math



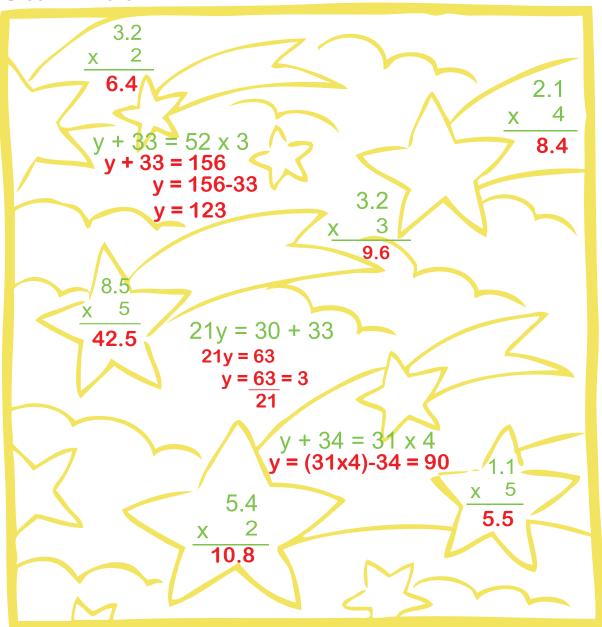
Note: More worksheets at www.education.com/worksheets

Instructions:



ANSWER SHEET

Star Math



Note: More worksheets at www.education.com/worksheets

Instructions: