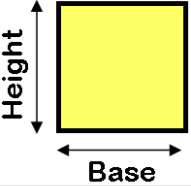
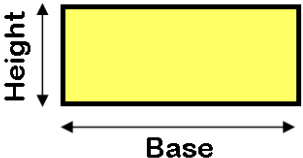
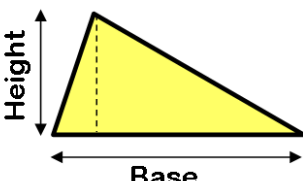
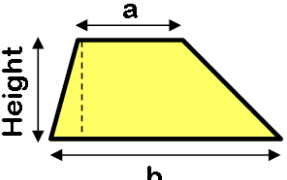
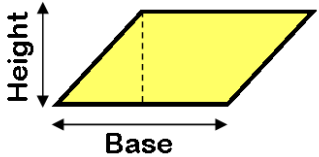
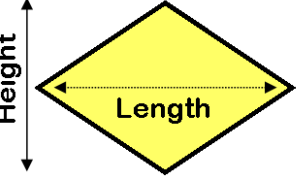
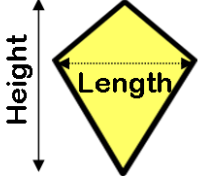


Perimeter, area and volume work book

Common formulae

Shape	Name	Formula for Area
	Square	Base x Height
	Rectangle	Base x Height
	Triangle	Base x Perpendicular Height ÷ 2
	Trapezium	$\frac{(a + b) \times \text{height}}{2}$
	Parallelogram	Base x Perpendicular Height
	Rhombus	Length x Height ÷ 2
	Kite	Length x Height ÷ 2

Read It

perimeter

Define It

The distance around the outside of a shape is the perimeter.

Digging Deeper:

The perimeter of the equator is 24,901 miles. If you are standing at the equator, since the world rotates in 24 hours, you are travelling at just over 1,000 mph.

Draw It

Deconstruct It

From the Latin *perimetros*, *peri* meaning around and *metros*, meaning measure.

Link It

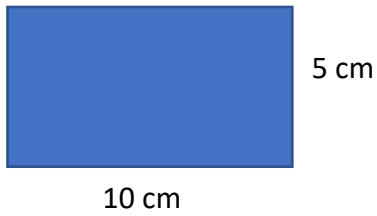
2-dimension, line, scale, measurement.

Use It

Find the perimeter of the garden.

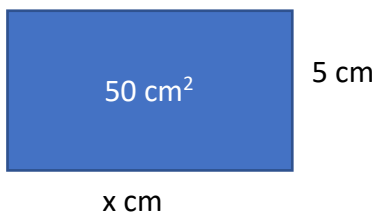
Section 1: Area of a rectangle

Example 1. Calculate the area given the dimensions



$$\begin{aligned}\text{Area} &= \text{length} \times \text{height} \\ &= 10 \text{ cm} \times 5 \text{ cm} \\ &= \mathbf{50 \text{ cm}^2}\end{aligned}$$

Example 2. Calculate a missing dimension given the area



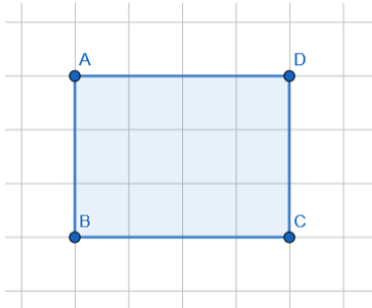
$$\begin{aligned}\text{Area} &= \text{length} \times \text{height} \\ 50 \text{ cm}^2 &= x \text{ cm} \times 5 \text{ cm} \\ x &= 50 \text{ cm}^2 \div 10 \text{ cm} \\ &= \mathbf{5 \text{ cm}}\end{aligned}$$

Worksheet 1 Area of a rectangle

True or false

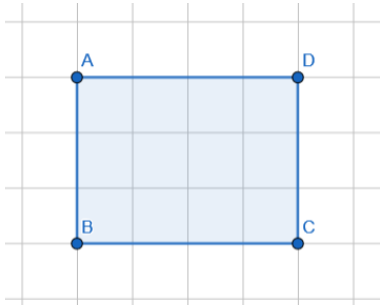
Write either T or F in the box depending on the answer.

1.



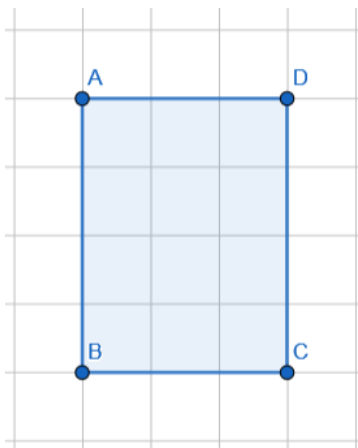
Area of ABCD = 14 cm^2

2.



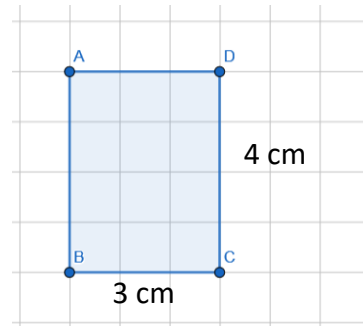
Area of ABCD = 12 cm^2

3.



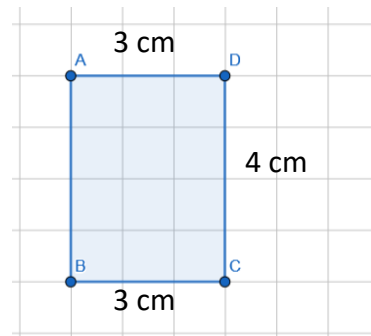
Area of ABCD = 12 cm^2

4.



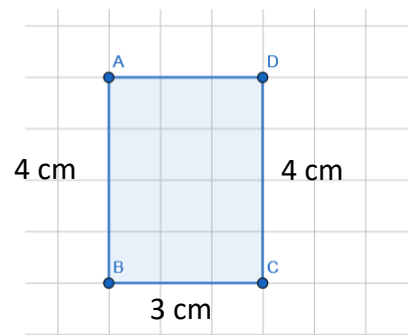
Area of ABCD = 12 cm^2

5.



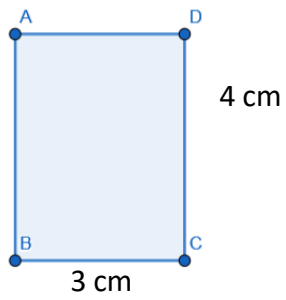
Area of ABCD = 36 cm^2

6.



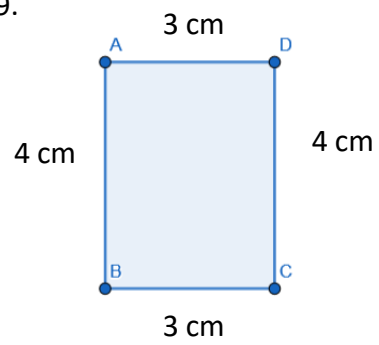
Area of ABCD = 48 cm^2

7.



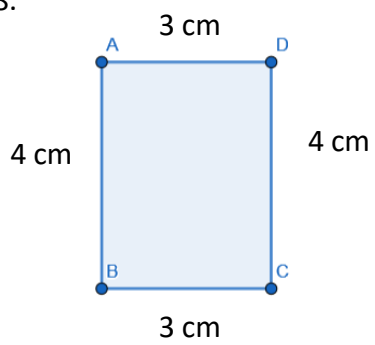
Area of ABCD = 12 cm^2

9.



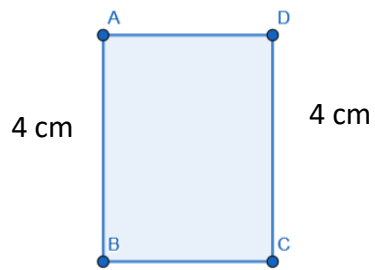
Area of ABCD = 144 cm^2

8.



Area of ABCD = 14 cm^2

10

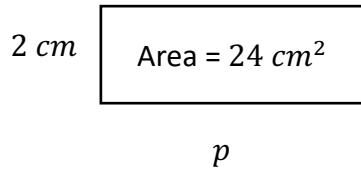


Area of ABCD = 16 cm^2

Worksheet 2 Area of a rectangle

Calculate the missing length given the area

Q1



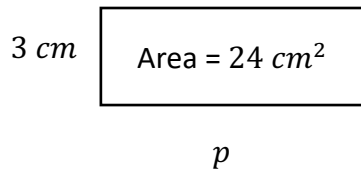
Area = length \times width

$$24 \text{ cm}^2 = 2 \times p$$

$$\frac{24}{2} = p$$

$$p = \quad \text{cm}$$

Q2



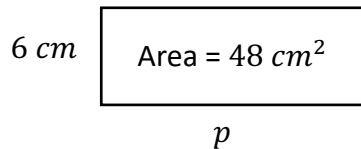
Area = length \times width

$$24 \text{ cm}^2 = 3 \times p$$

$$\frac{24}{3} = p$$

$$p = \quad \text{cm}$$

Q3



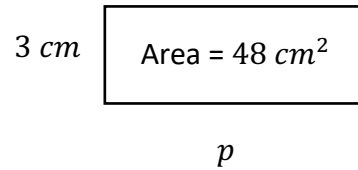
Area = length \times width

$$48 \text{ cm}^2 = \quad \times p$$

$$\frac{48}{\quad} = p$$

$$p = \quad \text{cm}$$

Q4



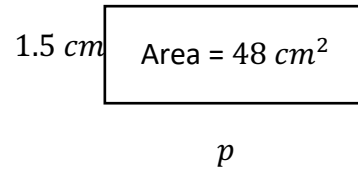
Area = length \times width

$$\text{cm}^2 = \quad \times p$$

$$\text{---} = p$$

$$p = \quad \text{cm}$$

Q5



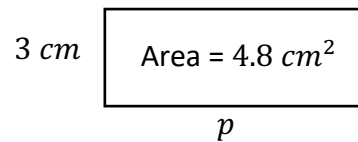
Area = length \times width

$$\text{cm}^2 = \quad \times p$$

$$\text{---} = p$$

$$p = \quad \text{cm}$$

Q6



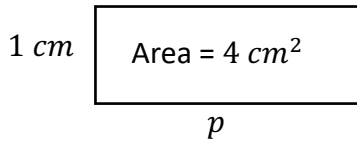
Area = length \times width

$$\text{cm}^2 = \quad \times p$$

$$\text{---} = p$$

$$p = \quad \text{cm}$$

Q7



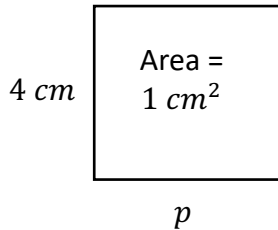
Area = length \times width

$$\text{cm}^2 = \quad \times p$$

$$\text{————} = p$$

$$p = \quad \text{cm}$$

Q8



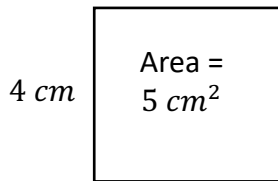
Area = length \times width

$$\text{cm}^2 = \quad \times p$$

$$\text{————} = p$$

$$p = \quad \text{cm}$$

Q9



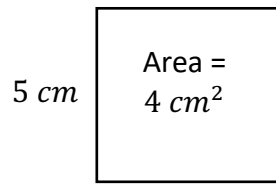
Area = length \times width

$$\text{cm}^2 = \quad \times p$$

$$\text{————} = p$$

$$p = \quad \text{cm}$$

Q10



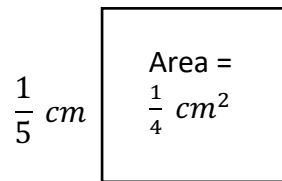
Area = length \times width

$$\text{cm}^2 = \quad \times p$$

$$\text{————} = p$$

$$p = \quad \text{cm}$$

Q11



Area = length \times width

$$\text{———— cm}^2 = \text{————} \times p$$

$$\text{————} = p$$

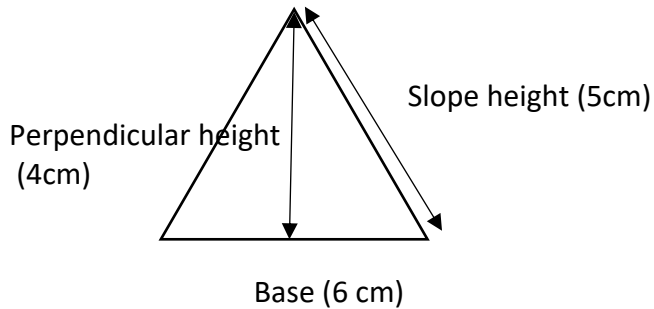
$$p = \text{———— cm}$$

Section 3: Area of a triangle

Area of a triangle = $\frac{1}{2}$ (base \times perpendicular height).

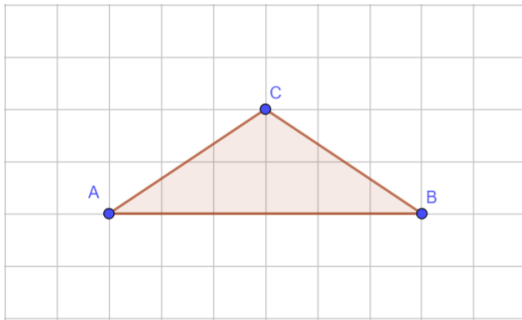
Note the words “perpendicular height”. This is the height that is at right angles to the base. This is important.

A common trick that examiners use is to give you the slope height, NOT the perpendicular height



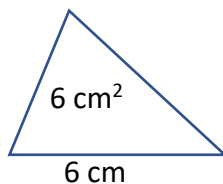
$$\begin{aligned}\text{Area} &= \frac{1}{2} (\text{base} \times \text{perpendicular height}). \\ &= \frac{1}{2} (6 \text{ cm} \times 4 \text{ cm}) \text{ NOT } = \frac{1}{2} (6 \text{ cm} \times 5 \text{ cm}).\end{aligned}$$

Example 1: Find the area given the dimensions
Area of a triangle = $\frac{1}{2}$ (base \times perpendicular height).



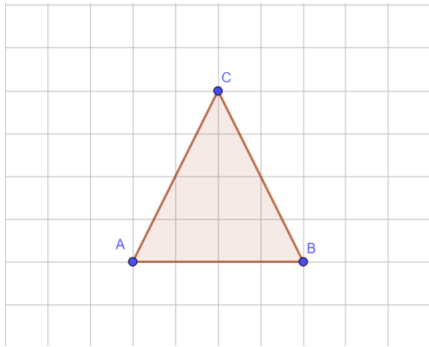
$$\begin{aligned}\text{Area} &= \frac{1}{2} (\text{base} \times \text{perpendicular height}). \\ &= \frac{1}{2} (6 \text{ cm} \times 2 \text{ cm}). \\ &= \frac{1}{2} (12 \text{ cm}^2). \\ &= \mathbf{6 \text{ cm}^2}\end{aligned}$$

Example 2: Find a dimension given the area.
Area of a triangle = $\frac{1}{2}$ (base \times perpendicular height).
Find the perpendicular height



$$\begin{aligned}\text{Area} &= \frac{1}{2} (\text{base} \times \text{perpendicular height}). \\ 6 \text{ cm}^2 &= \frac{1}{2} (6 \text{ cm} \times \text{height}). \\ 12 \text{ cm}^2 &= (6 \text{ cm} \times \text{height}). \\ 12 \text{ cm}^2 \div 6 \text{ cm} &= \text{height} \\ \mathbf{\text{Height} = 2 \text{ cm}}\end{aligned}$$

Q1.

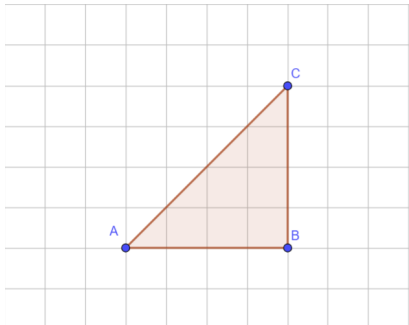


Area = $\frac{1}{2}$ (base \times perpendicular height).

$$= \frac{1}{2}(4 \times 4)$$

$$= \text{cm}^2$$

Q2

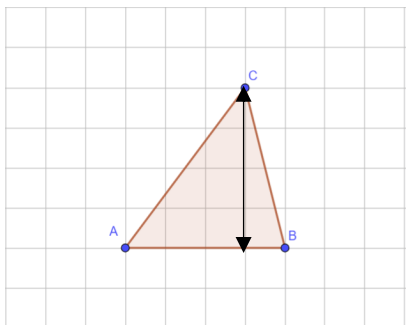


Area = $\frac{1}{2}$ (base \times perpendicular height).

$$= \frac{1}{2}(\quad \times \quad)$$

$$= \text{cm}^2$$

Q3

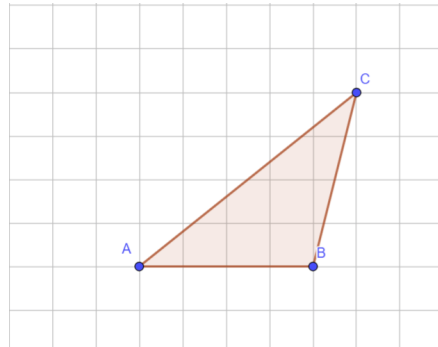


Area = $\frac{1}{2}$ (base \times perpendicular height).

$$= \frac{1}{2}(\quad \times \quad)$$

$$= \text{cm}^2$$

Q4

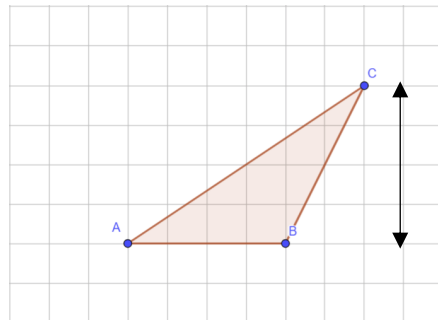


Area = $\frac{1}{2}$ (base \times perpendicular height).

$$= \frac{1}{2}(\quad \times \quad)$$

$$= \text{cm}^2$$

Q5

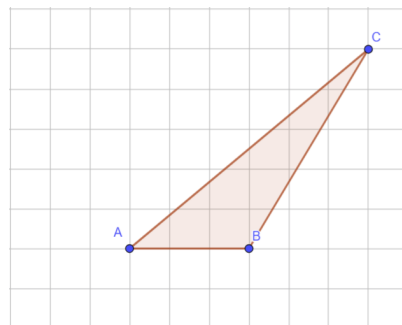


Area = $\frac{1}{2}$ (base \times perpendicular height).

$$= \frac{1}{2}(\quad \times \quad)$$

$$= \text{cm}^2$$

Q6

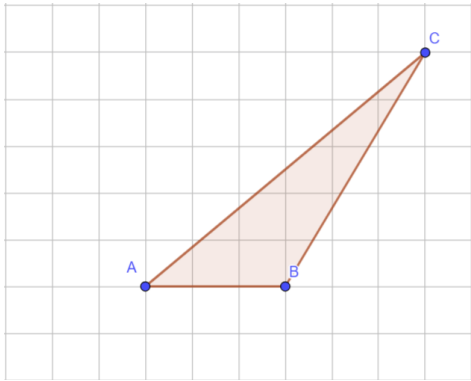


Area = $\frac{1}{2}$ (base \times perpendicular height).

$$= \frac{1}{2}(\quad \times \quad)$$

$$= \text{cm}^2$$

Q7

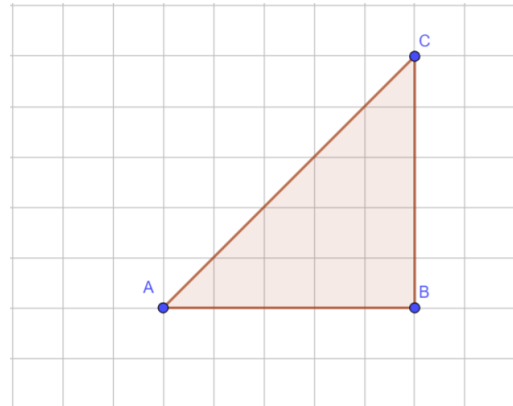


Area = $\frac{1}{2}$ (base \times perpendicular height).

= $\frac{1}{2}$ (\times)

= cm^2

Q9

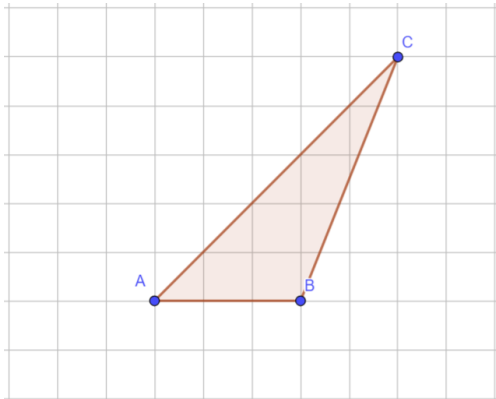


Area = $\frac{1}{2}$ (base \times perpendicular height).

= $\frac{1}{2}$ (\times)

= cm^2

Q8



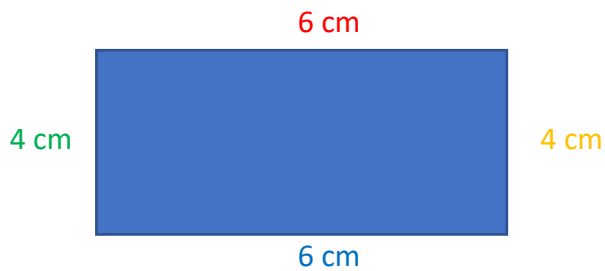
Area = $\frac{1}{2}$ (base \times perpendicular height).

= $\frac{1}{2}$ (\times)

= cm^2

Section 4: Perimeter of a rectangle

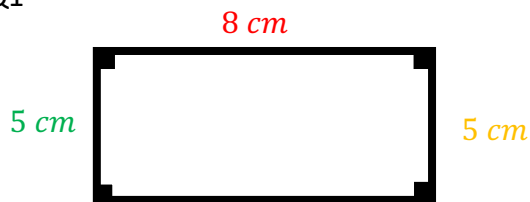
Perimeter = distance around a shape. Think of it as taking a journey around the outside of the shape.



$$\begin{aligned} \text{Perimeter} &= 6 \text{ cm} + 4 \text{ cm} + 6 \text{ cm} + 4 \text{ cm} \\ &= 20 \text{ cm (note unit – perimeter is a length so mm, cm, m etc)}. \end{aligned}$$

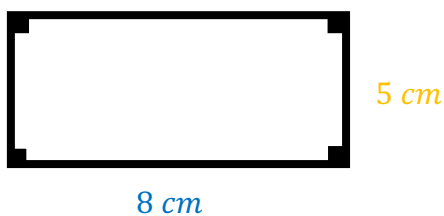
Worksheet 3: Perimeter of a rectangle

Q1



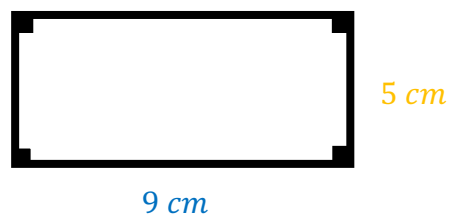
$$\begin{aligned} \text{Perimeter} &= 8 \text{ cm} + 5 \text{ cm} + 8 \text{ cm} + 5 \text{ cm} \\ &= \text{ cm} \end{aligned}$$

Q2



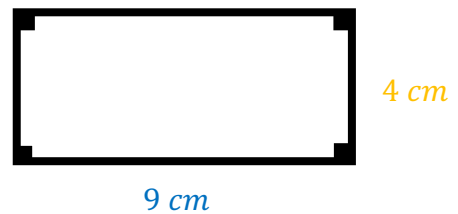
$$\begin{aligned} \text{Perimeter} &= \text{ cm} + \text{ cm} + 8 \text{ cm} \\ &+ 5 \text{ cm} \\ &= \text{ cm} \end{aligned}$$

Q3



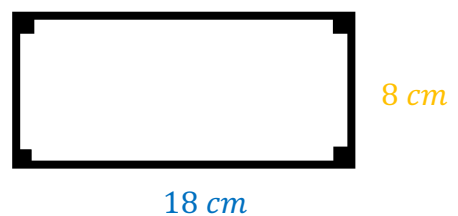
$$\begin{aligned} \text{Perimeter} &= \text{ cm} + \text{ cm} + \\ &\text{ cm} + \text{ cm} \\ &= \text{ cm} \end{aligned}$$

Q4



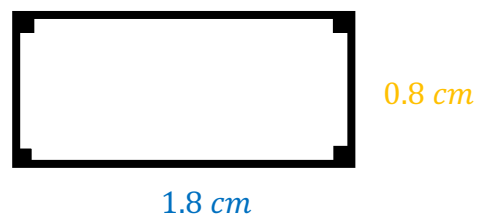
$$\begin{aligned} \text{Perimeter} &= \text{ cm} + \text{ cm} + \\ &\text{ cm} + \text{ cm} \\ &= \text{ cm} \end{aligned}$$

Q5



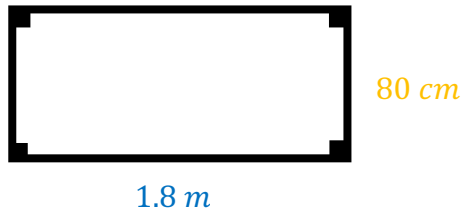
$$\begin{aligned} \text{Perimeter} &= 2 \times (\text{ cm} + \text{ cm}) \\ &= \text{ cm} \end{aligned}$$

Q6



$$\begin{aligned} \text{Perimeter} &= 2 \times (\text{ cm} + \text{ cm}) \\ &= \text{ cm} \end{aligned}$$

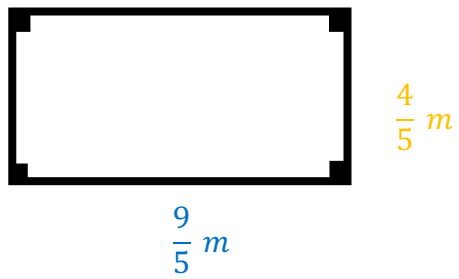
Q7



$$\text{Perimeter} = 2 \times (\quad + \quad)$$

=

Q8

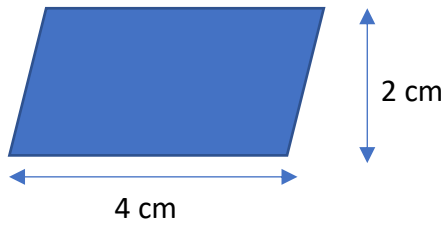


$$\text{Perimeter} = 2 \times (\text{--- m} + \text{--- m})$$

= ---

= m

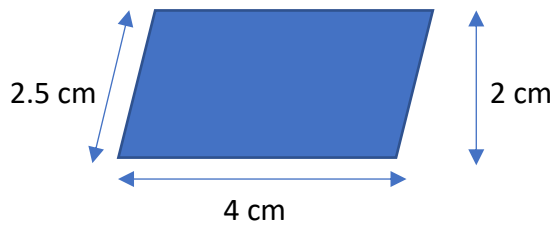
Section 5: Area of a parallelogram



$$\begin{aligned}\text{Area} &= \text{base} \times \text{perpendicular height} \\ &= 4 \text{ cm} \times 2 \text{ cm} \\ &= 8 \text{ cm}^2\end{aligned}$$

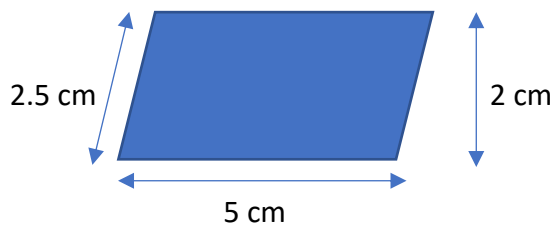
Once again, take care with questions trying to trick you. It is the perpendicular height, NOT the slope height

Ignore the 2.5 cm. It is a red-herring.



Worksheet 5: Area of a parallelogram

Q1.



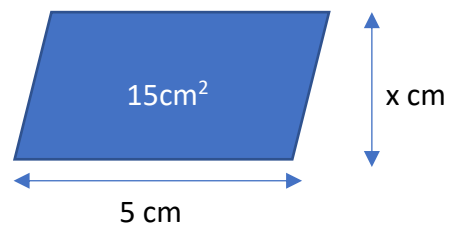
$$\begin{aligned}\text{Area} &= \text{base} \times \text{perpendicular height} \\ &= 5 \text{ cm} \times 2 \text{ cm} \\ &= \text{cm}^2\end{aligned}$$

Q2.



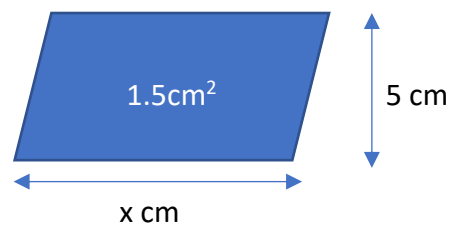
$$\begin{aligned}\text{Area} &= \text{base} \times \text{perpendicular height} \\ &= \text{cm} \times \text{cm} \\ &= \text{cm}^2\end{aligned}$$

Q3.



$$\begin{aligned}\text{Area} &= \text{base} \times \text{perpendicular height} \\ 15 \text{ cm}^2 &= 5 \text{ cm} \times x \text{ cm} \\ x &= \text{cm}\end{aligned}$$

Q4.

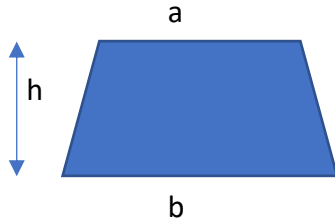


$$\begin{aligned}\text{Area} &= \text{base} \times \text{perpendicular height} \\ 1.5 \text{ cm}^2 &= 5 \text{ cm} \times x \text{ cm} \\ x &= \text{cm}\end{aligned}$$

Section 6: Area of a trapezium

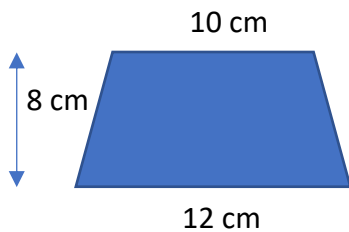
$$\text{Area} = \frac{h(a+b)}{2}$$

Where a, b are the two parallel sides, and h is the *perpendicular* height



Once again, don't be fooled by questions that give you the slant height. It is the perpendicular height that you need.

Example 1



Calculate the area of this trapezium

$$\text{Area} = \frac{h(a+b)}{2}$$

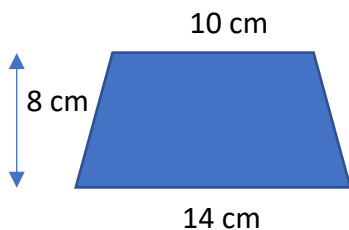
$$\text{Area} = \frac{8 \times (10 + 12)}{2}$$

$$\text{Area} = \frac{8 \times 22}{2}$$

$$= 88 \text{ cm}^2$$

Worksheet 6: Area of a trapezium

Q1



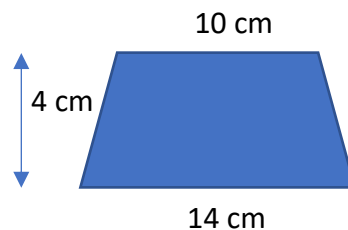
$$\text{Area} = \frac{h(a+b)}{2}$$

$$\text{Area} = \frac{8 \times (10 + 14)}{2}$$

$$\text{Area} = \frac{8 \times 24}{2}$$

$$= \quad \text{cm}^2$$

Q2



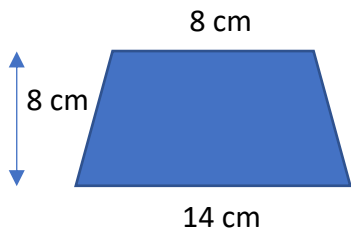
$$\text{Area} = \frac{h(a+b)}{2}$$

$$\text{Area} = \frac{\quad \times (10 + 14)}{2}$$

$$\text{Area} = \frac{\quad \times 24}{2}$$

$$= \quad \text{cm}^2$$

Q3



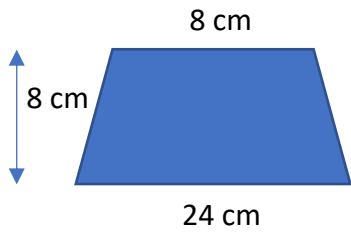
$$Area = \frac{h(a+b)}{2}$$

$$Area = \frac{\quad \times (\quad + 14)}{2}$$

$$Area = \frac{\quad \times \quad}{2}$$

$$= \quad \text{cm}^2$$

Q4



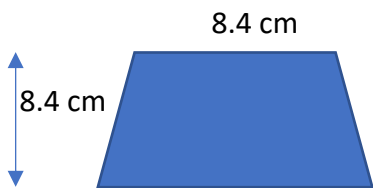
$$Area = \frac{h(a+b)}{2}$$

$$Area = \frac{\quad \times (\quad + \quad)}{2}$$

$$Area = \frac{\quad \times \quad}{2}$$

$$= \quad \text{cm}^2$$

Q5



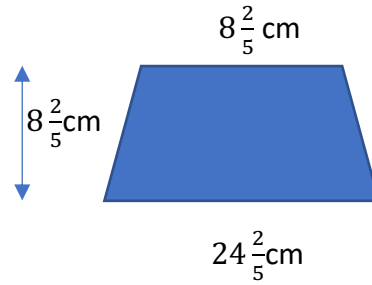
$$Area = \frac{h(a+b)}{2}$$

$$Area = \frac{\quad \times (\quad + \quad)}{2}$$

$$Area = \frac{\quad \times \quad}{2}$$

$$= \quad \text{cm}^2$$

Q6



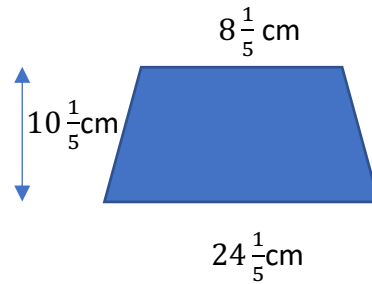
$$Area = \frac{h(a+b)}{2}$$

$$Area = \frac{\quad \times (\quad + \quad)}{2}$$

$$Area = \frac{\quad \times \quad}{2}$$

$$= \quad \text{cm}^2$$

Q7



$$Area = \frac{h(a+b)}{2}$$

$$Area = \frac{\quad \times (\quad + \quad)}{2}$$

$$Area = \frac{\quad \times \quad}{2}$$

$$= \quad \text{cm}^2$$

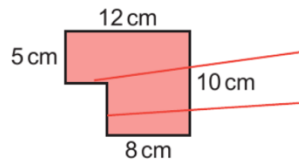
Section 7: Area of a compound shapes

Key point 6

A **compound shape** is made up of simple shapes.
To find the area of a compound shape, split it into simple shapes like rectangles and triangles.
Find the area of each shape and then add them all together.

Example 3

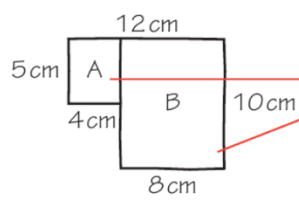
Calculate the perimeter and area of this compound shape.



Sketch the shape. Work out the missing lengths.
 $12\text{ cm} - 8\text{ cm} = 4\text{ cm}$
 $10\text{ cm} - 5\text{ cm} = 5\text{ cm}$

Add all the lengths around the shape to work out the perimeter.

Perimeter = $12 + 10 + 8 + 5 + 4 + 5 = 44\text{ cm}^2$



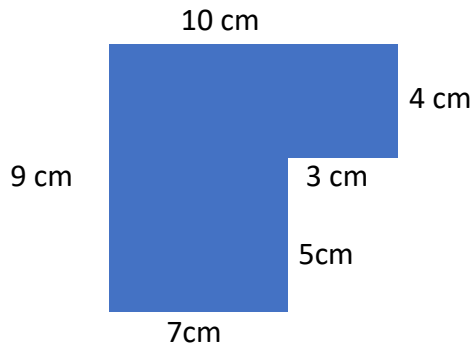
Divide the shape into two rectangles A and B.

Work out the area of each.

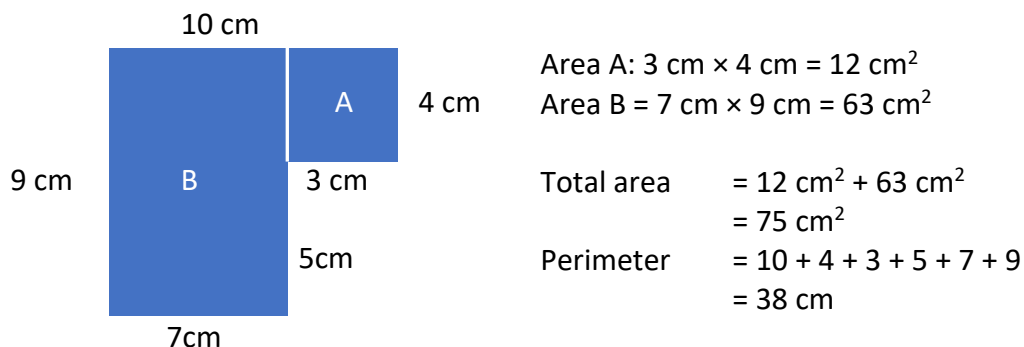
Area of A = $5 \times 4 = 20\text{ cm}^2$
 Area of B = $8 \times 10 = 80\text{ cm}^2$
 Total area = 100 cm^2

Example 1:

Calculate the area and perimeter of this shape

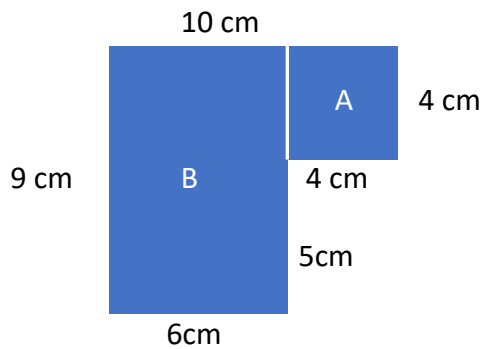


Divide the shape into two rectangles, A and B. Calculate their areas. Add them.



Worksheet 7: Area of a compound shapes

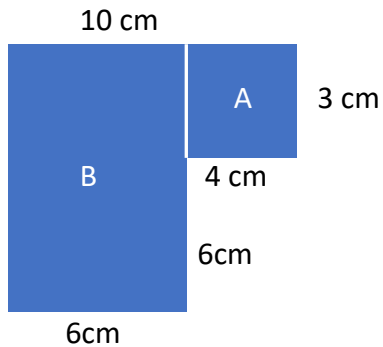
Q1



Area A: $4\text{ cm} \times 4\text{ cm} = 16\text{ cm}^2$
 Area B: $6\text{ cm} \times 9\text{ cm} = 54\text{ cm}^2$

Total area = $16\text{ cm}^2 + 54\text{ cm}^2$
 = cm^2

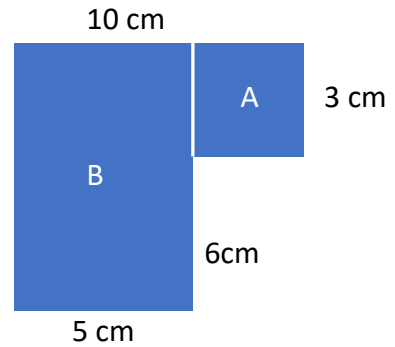
Q2



Area A: $3\text{ cm} \times 4\text{ cm} = 12\text{ cm}^2$
 Area B: $6\text{ cm} \times \text{cm} = \text{cm}^2$

Total area = $12\text{ cm}^2 + \text{cm}^2$
 = cm^2

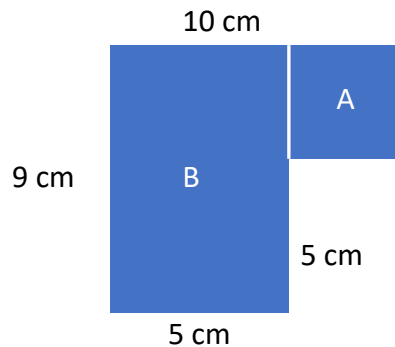
Q3



Area A: $3\text{ cm} \times \text{cm} = \text{cm}^2$
 Area B: $5\text{ cm} \times \text{cm} = \text{cm}^2$

Total area = $\text{cm}^2 + \text{cm}^2$
 = cm^2

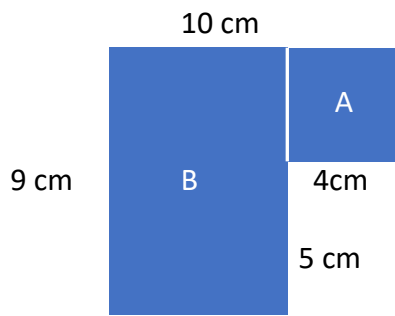
Q4



Area A: $\text{cm} \times \text{cm} = \text{cm}^2$
 Area B: $5\text{ cm} \times \text{cm} = \text{cm}^2$

Total area = $\text{cm}^2 + \text{cm}^2$
 = cm^2

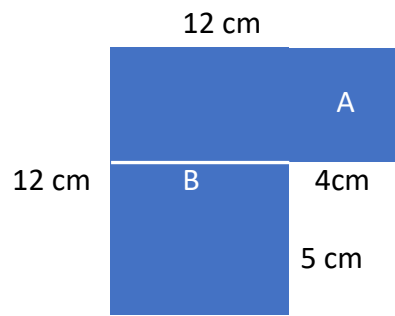
Q5



Area A: $1 \text{ cm} \times 9 \text{ cm} = 9 \text{ cm}^2$
 Area B: $9 \text{ cm} \times 9 \text{ cm} = 81 \text{ cm}^2$

Total area = $9 \text{ cm}^2 + 81 \text{ cm}^2$
 = 90 cm^2

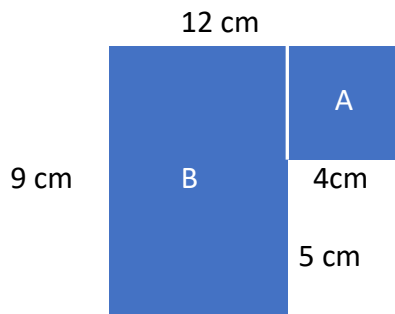
Q8



Area A: $8 \text{ cm} \times 4 \text{ cm} = 32 \text{ cm}^2$
 Area B: $4 \text{ cm} \times 4 \text{ cm} = 16 \text{ cm}^2$

Total area = $32 \text{ cm}^2 + 16 \text{ cm}^2$
 = 48 cm^2

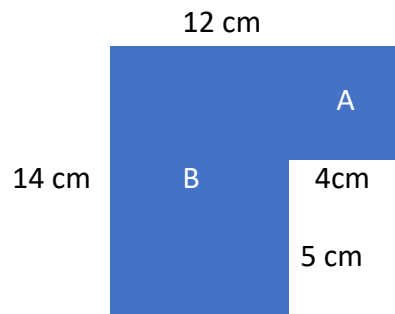
Q6



Area A: $3 \text{ cm} \times 9 \text{ cm} = 27 \text{ cm}^2$
 Area B: $9 \text{ cm} \times 9 \text{ cm} = 81 \text{ cm}^2$

Total area = $27 \text{ cm}^2 + 81 \text{ cm}^2$
 = 108 cm^2

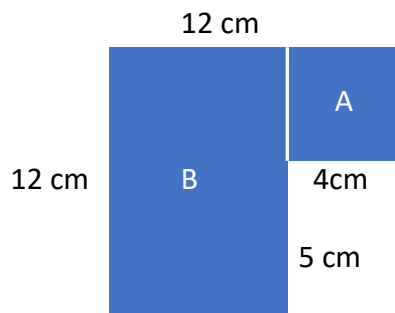
Q9



Area A: $2 \text{ cm} \times 4 \text{ cm} = 8 \text{ cm}^2$
 Area B: $10 \text{ cm} \times 10 \text{ cm} = 100 \text{ cm}^2$

Total area = $8 \text{ cm}^2 + 100 \text{ cm}^2$
 = 108 cm^2

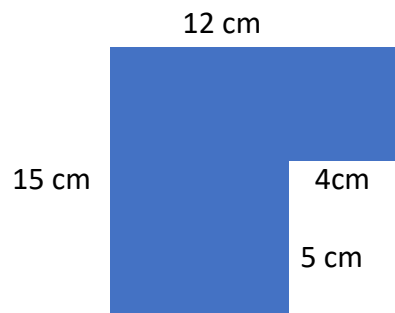
Q7



Area A: $1 \text{ cm} \times 12 \text{ cm} = 12 \text{ cm}^2$
 Area B: $12 \text{ cm} \times 12 \text{ cm} = 144 \text{ cm}^2$

Total area = $12 \text{ cm}^2 + 144 \text{ cm}^2$
 = 156 cm^2

Q10



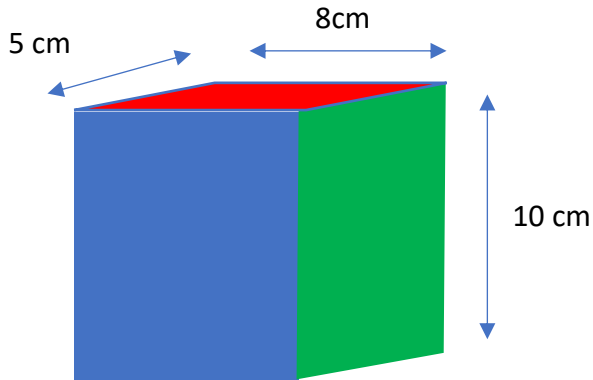
Area A: $2 \text{ cm} \times 5 \text{ cm} = 10 \text{ cm}^2$
 Area B: $10 \text{ cm} \times 10 \text{ cm} = 100 \text{ cm}^2$

Total area = $10 \text{ cm}^2 + 100 \text{ cm}^2$
 = 110 cm^2

Section 8: Surface area of 3D solids (cuboids/cubes)

When we talk about the surface area of a shape, we are referring to the total area of all of its faces.


A reminder, a face is the surface of a shape. A cube or a cuboid, has six faces.

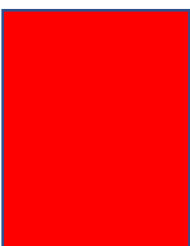


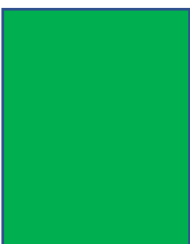
In this diagram you can see three of them, but there will be two blue, two green and two red surfaces.

Surface area = area of all the surfaces of a shape.

Surface area of cuboid = $2 \times$ area blue rectangle (one front, one back) + $2 \times$ area red rectangle (one top, one bottom) + $2 \times$ area green rectangle (one left, one right)


$$= 10 \times 8 = 80\text{cm}^2$$

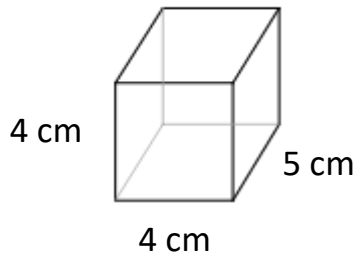

$$= 8 \times 5 = 40\text{cm}^2$$


$$= 10 \times 5 = 50\text{cm}^2$$

$$\begin{aligned}\text{Area} &= (2 \times 80\text{cm}^2) + (2 \times 40\text{cm}^2) + (2 \times 50\text{cm}^2) \\ &= 160\text{cm}^2 + 80\text{cm}^2 + 100\text{cm}^2 \\ &= \mathbf{340\text{cm}^2}\end{aligned}$$

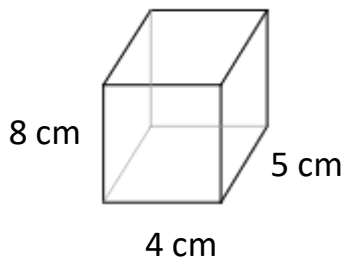
Worksheet 8: Surface area of 3D solids

Q1



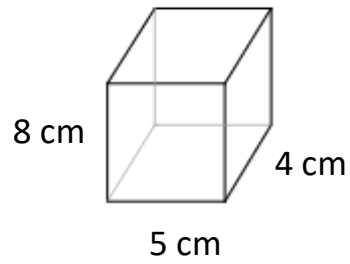
Front and back	$2 \times 4 \times 4 \text{ cm}^2$ $= 32 \text{ cm}^2$
Left and right side	$2 \times 5 \times 4 \text{ cm}^2$ $= 40 \text{ cm}^2$
Top and bottom	$2 \times 4 \times 5 \text{ cm}^2$ $= 40 \text{ cm}^2$
Total Surface Area	$32 + 40 + 40 \text{ cm}^2$ $= \text{ cm}^2$

Q2



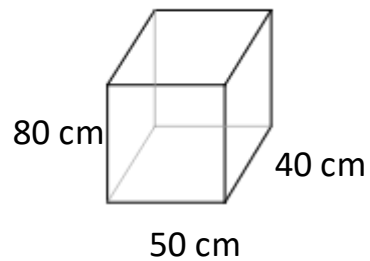
Front and back	$2 \times 8 \times 4 \text{ cm}^2$ $= \text{ cm}^2$
Left and right side	$2 \times 5 \times 4 \text{ cm}^2$ $= \text{ cm}^2$
Top and bottom	$2 \times 8 \times 4 \text{ cm}^2$ $= \text{ cm}^2$
Total Surface Area	$+ \quad +$ $\text{ cm}^2 \quad \text{ cm}^2$ $= \text{ cm}^2$

Q3



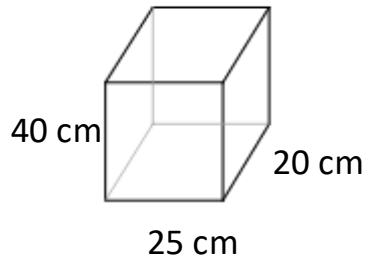
Front and back	$2 \times 8 \times \text{ cm}^2$ $= \text{ cm}^2$
Left and right side	$2 \times 8 \times \text{ cm}^2$ $= \text{ cm}^2$
Top and bottom	$2 \times 5 \times \text{ cm}^2$ $= \text{ cm}^2$
Total Surface Area	$+ \quad +$ $\text{ cm}^2 \quad \text{ cm}^2$ $= \text{ cm}^2$

Q4



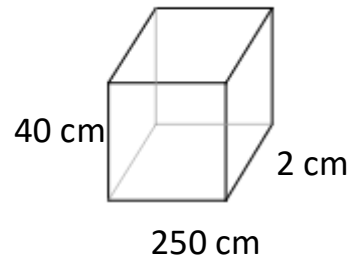
Front and back	$2 \times \times \text{ cm}^2$ $= \text{ cm}^2$
Left and right side	$2 \times \times \text{ cm}^2$ $= \text{ cm}^2$
Top and bottom	$2 \times \times \text{ cm}^2$ $= \text{ cm}^2$
Total Surface Area	$+ \quad +$ $\text{ cm}^2 \quad \text{ cm}^2$ $= \text{ cm}^2$

Q5



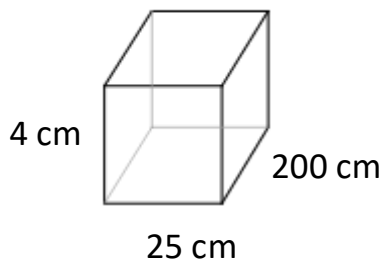
Front and back	\times cm^2 \times = cm^2
Left and right side	\times cm^2 \times = cm^2
Top and bottom	\times cm^2 \times = cm^2
Total Surface Area	$+$ cm^2 $+$ = cm^2

Q7



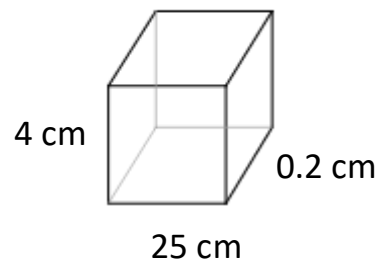
Front and back	\times cm^2 \times = cm^2
Left and right side	\times cm^2 \times = cm^2
Top and bottom	\times cm^2 \times = cm^2
Total Surface Area	$+$ cm^2 $+$ = cm^2

Q6



Front and back	\times cm^2 \times = cm^2
Left and right side	\times cm^2 \times = cm^2
Top and bottom	\times cm^2 \times = cm^2
Total Surface Area	$+$ cm^2 $+$ = cm^2

Q8



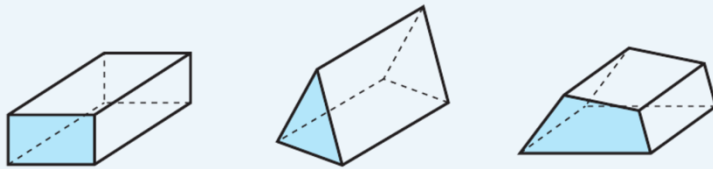
Front and back	\times cm^2 \times = cm^2
Left and right side	\times cm^2 \times = cm^2
Top and bottom	\times cm^2 \times = cm^2
Total Surface Area	$+$ cm^2 $+$ = cm^2

Section 9: Surface area of 3D solids (prisms)

You can calculate the surface area of any 3D prism

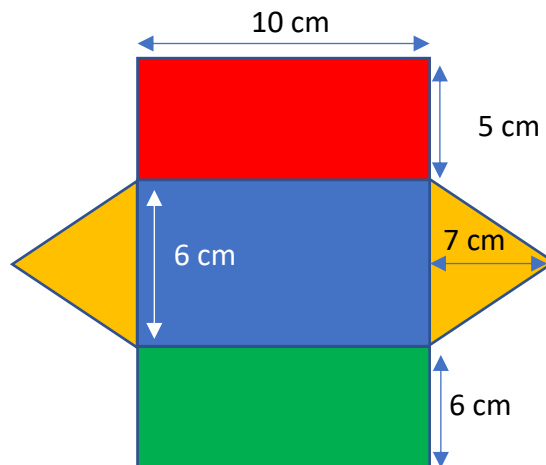
Key point 7

A prism is a 3D solid that has the same cross-section all through its length.



In exactly the same way that you calculated the surface area of a cuboid, so you can calculate the surface area of a prism

One way of thinking about it is to think about the net that would make the shape.



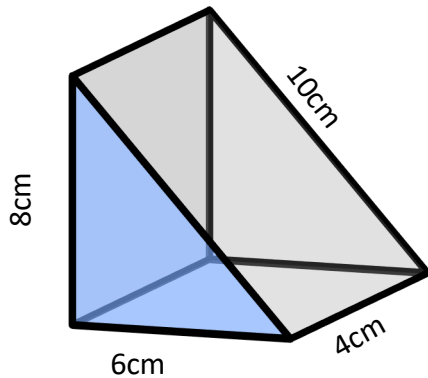
Finding areas of rectangles should not be a problem. The area of the two orange triangles you will have to think about

$$\begin{aligned}\text{Area} &= \frac{1}{2} (\text{base} \times \text{height}) \\ &= \frac{1}{2} (6\text{cm} \times 7\text{cm}) \\ &= \frac{1}{2} (42\text{cm}^2) \\ &= 21\text{cm}^2\end{aligned}$$

$$\begin{aligned}\text{Total area} &= (10\text{cm} \times 5\text{cm}) + (10\text{cm} \times 6\text{cm}) + (10\text{cm} \times 6\text{cm}) + (2 \times 21\text{cm}^2) \\ &= 50\text{cm}^2 + 60\text{cm}^2 + 60\text{cm}^2 + 42\text{cm}^2 \\ &= 212\text{cm}^2\end{aligned}$$

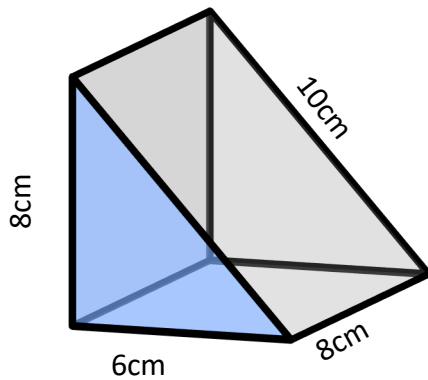
Worksheet 9: Surface area of 3D solids (prisms)

Q1



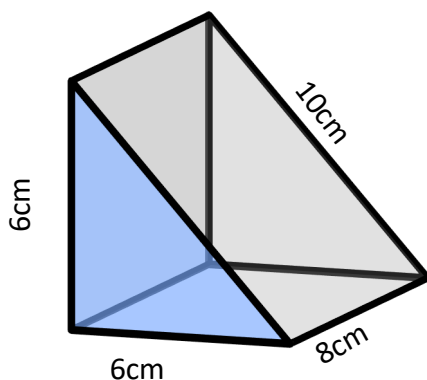
Area of triangle	$\frac{1}{2} (\text{base} \times \text{height})$ $\frac{1}{2} (6 \times 8)$ $= 24 \text{ cm}^2$
Area of base	$4 \text{ cm} \times 6 \text{ cm}$ $= 24 \text{ cm}^2$
Area of top	$4 \text{ cm} \times 10 \text{ cm}$ $= 40 \text{ cm}^2$
Area of back	$8 \text{ cm} \times 4 \text{ cm}$ $= 32 \text{ cm}^2$
Total	$(2 \times 24) + 24 + 40$ $+ 32$ $= \text{ cm}^2$

Q2



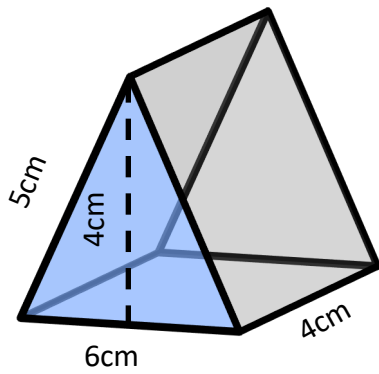
Area of triangle	$\frac{1}{2} (\text{base} \times \text{height})$ $\frac{1}{2} (6 \times 8)$ $= \text{ cm}^2$
Area of base	$6 \text{ cm} \times \text{ cm}$ $= \text{ cm}^2$
Area of top	$10 \text{ cm} \times 8 \text{ cm}$ $= 80 \text{ cm}^2$
Area of back	$8 \text{ cm} \times 8 \text{ cm}$ $= 64 \text{ cm}^2$
Total	$(2 \times \text{ }) +$ $+ 80 + 64$ $= \text{ cm}^2$

Q3



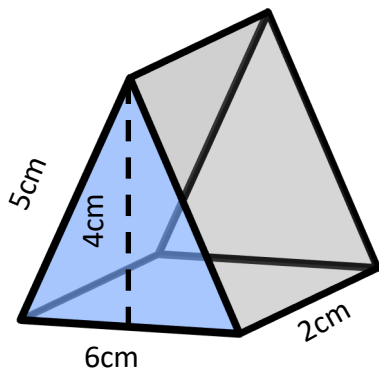
Area of triangle	$\frac{1}{2} (\text{base} \times \text{height})$ $\frac{1}{2} (\times)$ $= \text{ cm}^2$
Area of base	$\text{ cm} \times$ cm $= \text{ cm}^2$
Area of top	$\text{ cm} \times 8 \text{ cm}$ $= \text{ cm}^2$
Area of back	$6 \text{ cm} \times 8 \text{ cm}$ $= 48 \text{ cm}^2$
Total	$(2 \times \text{ }) +$ $+ \text{ } +$ 48 $= \text{ cm}^2$

Q4



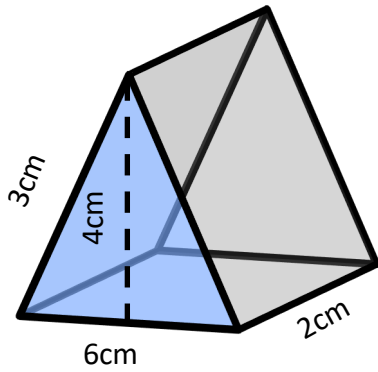
Area of triangle	$\frac{1}{2} (\text{base} \times \text{height})$ $\frac{1}{2} (6 \times 4)$ $= \text{cm}^2$
Area of base	$\text{cm} \times$ cm $= \text{cm}^2$
Area of Left top	$5 \text{ cm} \times 4 \text{ cm}$ $= 20 \text{ cm}^2$
Area of right top	$\text{cm} \times$ cm $= \text{cm}^2$
Total	$(2 \times \text{cm}^2) +$ $+ 20 +$ $= \text{cm}^2$

Q5



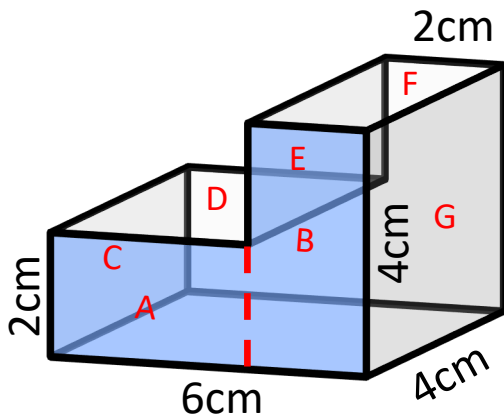
Area of triangle	$\frac{1}{2} (\text{base} \times \text{height})$ $\frac{1}{2} (\quad \times \quad)$ $= \text{cm}^2$
Area of base	$\text{cm} \times$ cm $= \text{cm}^2$
Area of Left top	$\text{cm} \times 2 \text{ cm}$ $= \text{cm}^2$
Area of right top	$5 \text{ cm} \times \quad \text{cm}$ $= \text{cm}^2$
Total	$(2 \times \text{cm}^2) +$ $+ \quad +$ $= \text{cm}^2$

Q6



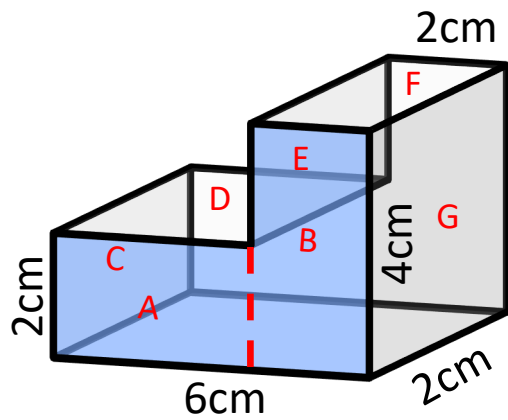
Area of triangle	$\frac{1}{2} (\text{base} \times \text{height})$ $\frac{1}{2} (\quad \times \quad)$ = cm^2
Area of base	$\text{cm} \times \text{cm}$ = cm^2
Area of Left top	$\text{cm} \times \text{cm}$ = cm^2
Area of right top	$\text{cm} \times \text{cm}$ = cm^2
Total	$(2 \times \quad) + \quad + \quad + \quad$ = cm^2

Q7



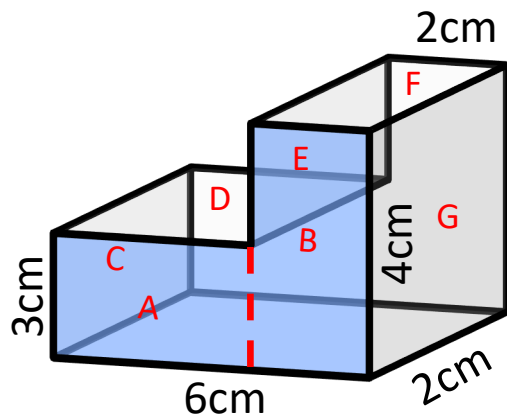
Area of rectangle A (front)	$2 \text{ cm} \times 4 \text{ cm}$ = cm^2
Area of rectangle B (front)	$2 \text{ cm} \times 4 \text{ cm}$ = cm^2
Total area of front	$+ =$ cm^2
Area of base	$6 \text{ cm} \times 4 \text{ cm}$ = cm^2
Area of rectangle C (Left hand side)	$2 \text{ cm} \times 4 \text{ cm}$ = cm^2
Area of rectangle D (Top surface)	$4 \text{ cm} \times 4 \text{ cm}$ = cm^2
Area of rectangle E (Left hand side)	$2 \text{ cm} \times 4 \text{ cm}$ = cm^2
Area of rectangle F (Top surface)	$2 \text{ cm} \times 4 \text{ cm}$ = cm^2
Area of rectangle G (Right hand side)	$4 \text{ cm} \times 4 \text{ cm}$ = cm^2
Total (2 × Front) + base + C + D + E + F + G	$(2 \times \quad) + \quad + \quad + \quad + \quad + \quad$ = cm^2

Q8



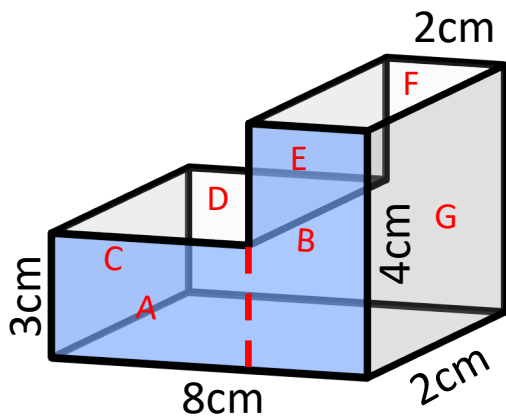
Area of rectangle A (front)	$= 6 \text{ cm} \times 2 \text{ cm}$ $= 12 \text{ cm}^2$
Area of rectangle B (front)	$= 2 \text{ cm} \times 4 \text{ cm}$ $= 8 \text{ cm}^2$
Total area of front	$12 \text{ cm}^2 + 8 \text{ cm}^2 = 20 \text{ cm}^2$
Area of base	$6 \text{ cm} \times 2 \text{ cm} = 12 \text{ cm}^2$
Area of rectangle C (Left hand side)	$2 \text{ cm} \times 6 \text{ cm} = 12 \text{ cm}^2$
Area of rectangle D (Top surface)	$6 \text{ cm} \times 2 \text{ cm} = 12 \text{ cm}^2$
Area of rectangle E (Left hand side)	$2 \text{ cm} \times 2 \text{ cm} = 4 \text{ cm}^2$
Area of rectangle F (Top surface)	$2 \text{ cm} \times 2 \text{ cm} = 4 \text{ cm}^2$
Area of rectangle G (Right hand side)	$4 \text{ cm} \times 2 \text{ cm} = 8 \text{ cm}^2$
Total (2 × Front) + base + C + D + E + F + G	$(2 \times 20) + 12 + 12 + 4 + 4 + 8 = 60 \text{ cm}^2$

Q9



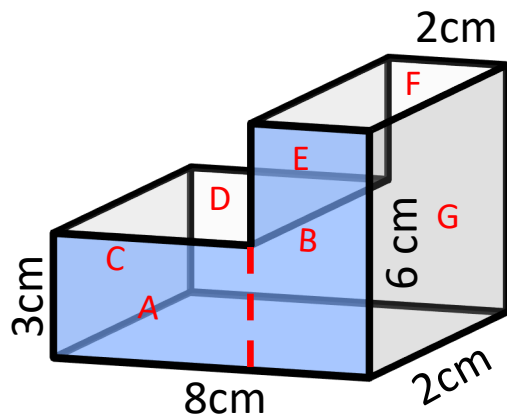
Area of rectangle A (front)	$= \text{cm} \times 4 \text{ cm}$ $= \text{cm}^2$
Area of rectangle B (front)	$\text{cm} \times$ $= \text{cm}^2$
Total area of front	$+ \quad =$ cm^2
Area of base	$\text{cm} \times$ cm $= \text{cm}^2$
Area of rectangle C (Left hand side)	$3 \text{ cm} \times \quad \text{cm}$ $= \text{cm}^2$
Area of rectangle D (Top surface)	$\text{cm} \times$ cm $= \text{cm}^2$
Area of rectangle E (Left hand side)	$2 \text{ cm} \times \quad \text{cm}$ $= \text{cm}^2$
Area of rectangle F (Top surface)	$\text{cm} \times$ cm $= \text{cm}^2$
Area of rectangle G (Right hand side)	$4 \text{ cm} \times \quad \text{cm}$ $= \text{cm}^2$
Total (2 × Front) + base + C + D + E + F + G	$(2 \times \quad) +$ $+ \quad +$ $+ \quad +$ $+ \quad +$ $= \text{cm}^2$

Q10



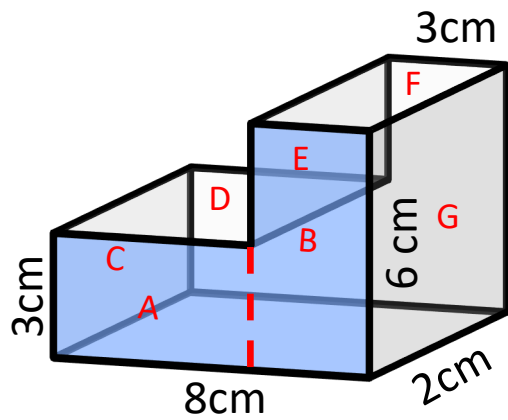
Area of rectangle A (front)	$\text{cm} \times \text{cm} = \text{cm}^2$
Area of rectangle B (front)	$\text{cm} \times \text{cm} = \text{cm}^2$
Total area of front	$+ = \text{cm}^2$
Area of base	$\text{cm} \times \text{cm} = \text{cm}^2$
Area of rectangle C (Left hand side)	$\text{cm} \times \text{cm} = \text{cm}^2$
Area of rectangle D (Top surface)	$\text{cm} \times \text{cm} = \text{cm}^2$
Area of rectangle E (Left hand side)	$\text{cm} \times \text{cm} = \text{cm}^2$
Area of rectangle F (Top surface)	$\text{cm} \times \text{cm} = \text{cm}^2$
Area of rectangle G (Right hand side)	$\text{cm} \times \text{cm} = \text{cm}^2$
Total (2 × Front) + base + C + D + E + F + G	$(2 \times) + + + = \text{cm}^2$

Q11



Area of rectangle A (front)	$\text{cm} \times \text{cm} = \text{cm}^2$
Area of rectangle B (front)	$\text{cm} \times \text{cm} = \text{cm}^2$
Total area of front	$+ = \text{cm}^2$
Area of base	$\text{cm} \times \text{cm} = \text{cm}^2$
Area of rectangle C (Left hand side)	$\text{cm} \times \text{cm} = \text{cm}^2$
Area of rectangle D (Top surface)	$\text{cm} \times \text{cm} = \text{cm}^2$
Area of rectangle E (Left hand side)	$\text{cm} \times \text{cm} = \text{cm}^2$
Area of rectangle F (Top surface)	$\text{cm} \times \text{cm} = \text{cm}^2$
Area of rectangle G (Right hand side)	$\text{cm} \times \text{cm} = \text{cm}^2$
Total (2 × Front) + base + C + D + E + F + G	$(2 \times) + + + = \text{cm}^2$

Q12



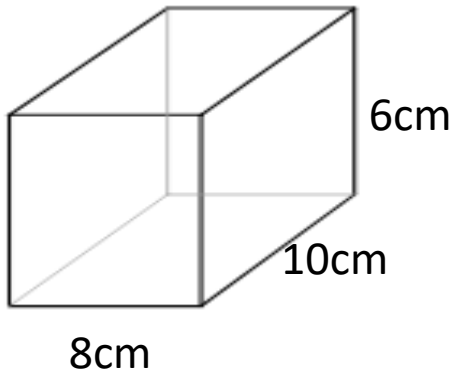
Area of rectangle A (front)	cm × cm = cm ²
Area of rectangle B (front)	cm × cm = cm ²
Total area of front	+ = cm ²
Area of base	cm × cm = cm ²
Area of rectangle C (Left hand side)	cm × cm = cm ²
Area of rectangle D (Top surface)	cm × cm = cm ²
Area of rectangle E (Left hand side)	cm × cm = cm ²
Area of rectangle F (Top surface)	cm × cm = cm ²
Area of rectangle G (Right hand side)	cm × cm = cm ²
Total (2 × Front) + base + C + D + E + F + G	(2 ×) + + + + + + = cm ²

Section 10: Volume of cubes and cuboids

Volume = length × width × height

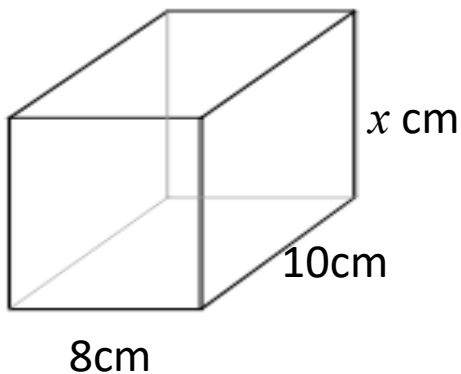
The unit of volume is mm^3 , cm^3 , or m^3 or, if it was something massive, km^3 .

Example 1: Calculate the volume given the dimensions



$$\begin{aligned}\text{Volume} &= \text{length} \times \text{width} \times \text{height} \\ &= 8 \text{ cm} \times 10 \text{ cm} \times 6 \text{ cm} \\ &= 480 \text{ cm}^3\end{aligned}$$

Example 2: Calculate a missing dimension given volume

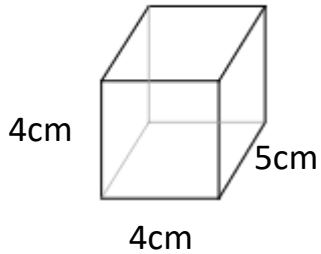


$$\text{Volume} = 240 \text{ cm}^3$$

$$\begin{aligned}\text{Volume} &= \text{length} \times \text{width} \times \text{height} \\ 240 &= 8 \text{ cm} \times 10 \text{ cm} \times x \text{ cm} \\ 240 &= 80 \times x \text{ cm} \\ 240 / 80 &= x \text{ cm} \\ x &= \mathbf{3 \text{ cm}}\end{aligned}$$

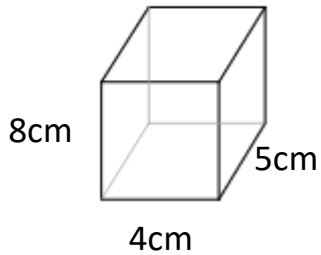
Worksheet 10: Volume of cubes and cuboids

Q1



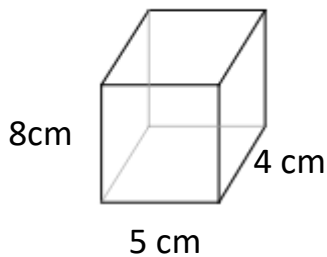
Volume = length × width × height
 = 4 cm × 5 cm × 4 cm
 = cm³

Q2



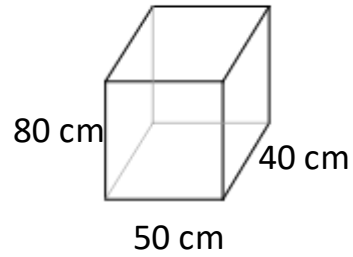
Volume = length × width × height
 = 4 cm × 5 cm × cm
 = cm³

Q3



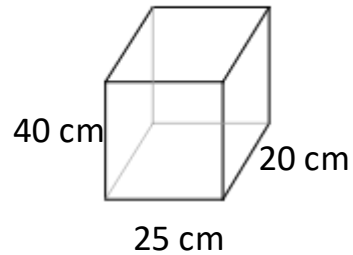
Volume = length × width × height
 = cm × cm ×
 cm
 = cm³

Q4



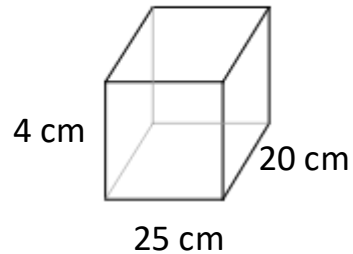
Volume = length × width × height
 = cm × cm ×
 cm
 = cm³

Q5



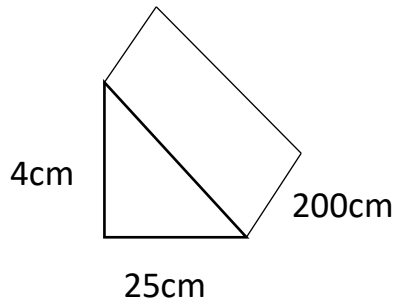
Volume = length × width × height
 = cm × cm ×
 cm
 = cm³

Q6



Volume = length × width × height
 = cm × cm ×
 cm
 = cm³

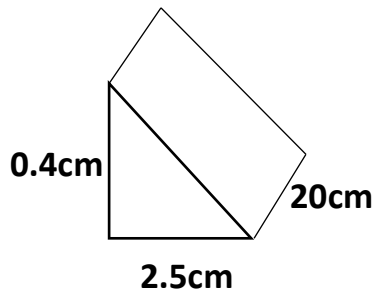
Q7



Think about this one. If you calculated the volume in Q6, then this is half of the shape. If it is half the size of Q6, then what will its volume be?

Volume = $\frac{1}{2}$ (length \times width \times height)
 \times cm) = $\frac{1}{2}$ (cm \times cm
= cm³

Q8.



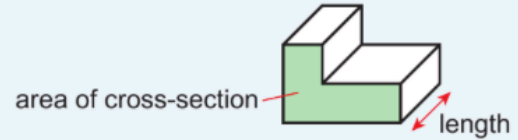
Volume = $\frac{1}{2}$ (length \times width \times height)
 \times cm) = $\frac{1}{2}$ (cm \times cm
= cm³

Section 11: Volume of prisms

Cross sectional area means the area of the base.

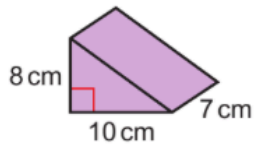
Key point 12

Volume of a prism = area of cross-section \times length



Example 5

Work out the volume of this prism.



Volume = area of cross-section \times length

$$\begin{aligned} \text{Area of } \triangle &= \frac{1}{2} \times 10 \times 8 \\ &= 5 \times 8 \\ &= 40 \end{aligned}$$

$$\text{Volume} = 40 \times 7$$

$$= 280 \text{ cm}^3$$

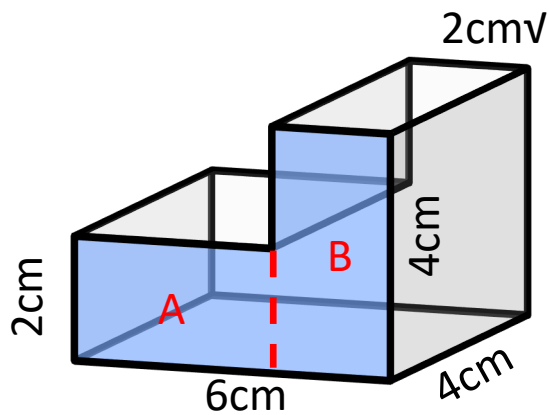
Write down the formula.

Work out the area of the cross-section.

Substitute the area of the cross-section and the length into the formula.

Write the units.

Example 2. More complex shape



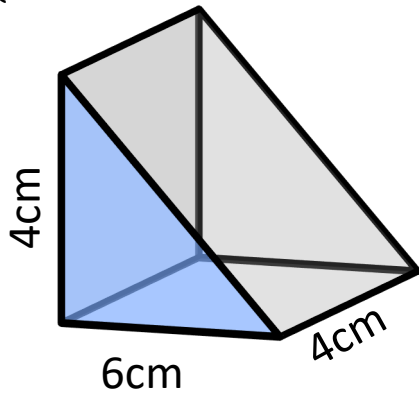
Volume = cross sectional area \times length

$$\begin{aligned} \text{Cross sectional area} &= \text{area A} + \text{area B} \\ &= (4 \times 2) + (2 \times 4) \\ &= 8 \text{ cm}^2 + 8 \text{ cm}^2 \\ &= 16 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Volume} &= \text{cross sectional area} \times \text{length} \\ &= 16 \text{ cm}^2 \times 4 \text{ cm} \\ &= 64 \text{ cm}^3 \end{aligned}$$

Worksheet 11: Volume of prisms

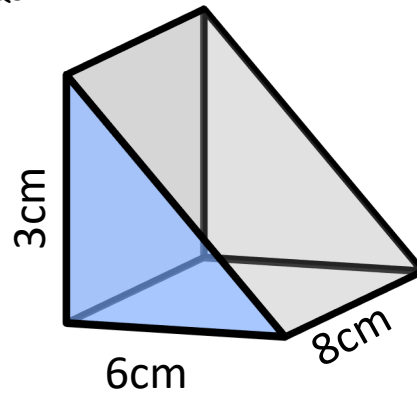
Q1



$$\begin{aligned} \text{Volume} &= \text{cross sectional area} \times \text{length} \\ \text{cross sectional area} &= \frac{1}{2} (\text{base} \times \text{height}) \\ &= \frac{1}{2} (6 \text{ cm} \times 4 \text{ cm}) \\ &= 12 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Volume} &= \text{cross sectional area} \times \text{length} \\ &= 12 \text{ cm}^2 \times 4 \text{ cm} \\ &= 48 \text{ cm}^3 \end{aligned}$$

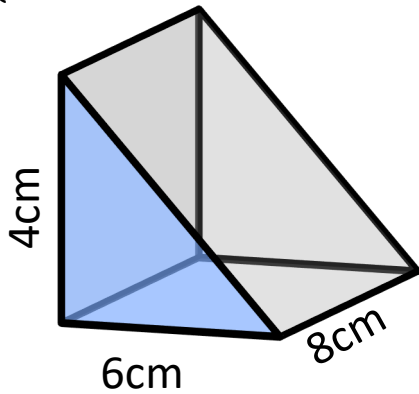
Q3



$$\begin{aligned} \text{Volume} &= \text{cross sectional area} \times \text{length} \\ \text{cross sectional area} &= \frac{1}{2} (\text{base} \times \text{height}) \\ &= \frac{1}{2} (6 \text{ cm} \times 3 \end{aligned}$$

$$\begin{aligned} &= 9 \text{ cm}^2 \\ \text{Volume} &= \text{cross sectional area} \times \text{length} \\ &= 9 \text{ cm}^2 \times 8 \text{ cm} \\ &= 72 \text{ cm}^3 \end{aligned}$$

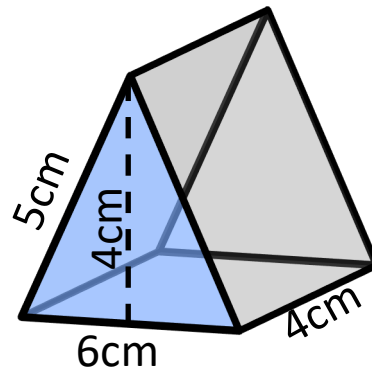
Q2



$$\begin{aligned} \text{Volume} &= \text{cross sectional area} \times \text{length} \\ \text{cross sectional area} &= \frac{1}{2} (\text{base} \times \text{height}) \\ &= \frac{1}{2} (6 \text{ cm} \times 4 \end{aligned}$$

$$\begin{aligned} &= 12 \text{ cm}^2 \\ \text{Volume} &= \text{cross sectional area} \times \text{length} \\ &= 12 \text{ cm}^2 \times 8 \text{ cm} \\ &= 96 \text{ cm}^3 \end{aligned}$$

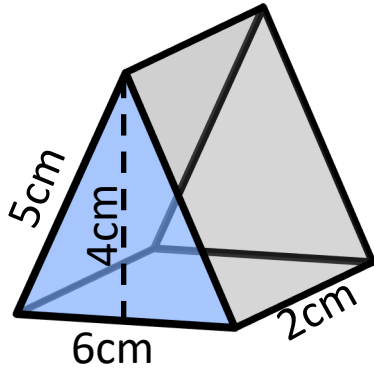
Q4



$$\begin{aligned} \text{Volume} &= \text{cross sectional area} \times \text{length} \\ \text{cross sectional area} &= \frac{1}{2} (\text{base} \times \text{height}) \\ &= \frac{1}{2} (6 \text{ cm} \times 4 \text{ cm}) \\ &= 12 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Volume} &= \text{cross sectional area} \times \text{length} \\ &= 12 \text{ cm}^2 \times 4 \text{ cm} \\ &= 48 \text{ cm}^3 \end{aligned}$$

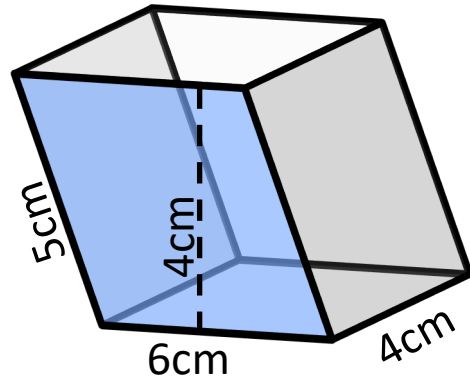
Q5



$$\begin{aligned} \text{Volume} &= \text{cross sectional area} \times \text{length} \\ \text{cross sectional area} &= \frac{1}{2} (\text{base} \times \text{height}) \\ &= \frac{1}{2} (6 \text{ cm} \times 4 \text{ cm}) \\ &= 12 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Volume} &= \text{cross sectional area} \times \text{length} \\ &= 12 \text{ cm}^2 \times 2 \text{ cm} \\ &= 24 \text{ cm}^3 \end{aligned}$$

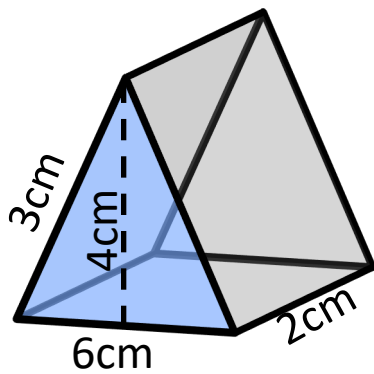
Q7



$$\begin{aligned} \text{Volume} &= \text{cross sectional area} \times \text{length} \\ \text{cross sectional area} &= (\text{base} \times \text{perpendicular height}) \\ &= (6 \text{ cm} \times 4 \text{ cm}) \\ &= 24 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Volume} &= \text{cross sectional area} \times \text{length} \\ &= 24 \text{ cm}^2 \times 5 \text{ cm} \\ &= 120 \text{ cm}^3 \end{aligned}$$

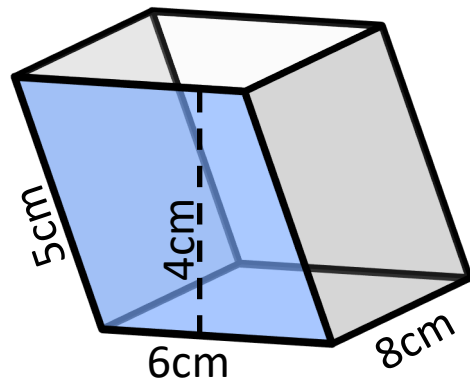
Q6



$$\begin{aligned} \text{Volume} &= \text{cross sectional area} \times \text{length} \\ \text{cross sectional area} &= \frac{1}{2} (\text{base} \times \text{height}) \\ &= \frac{1}{2} (6 \text{ cm} \times 4 \text{ cm}) \\ &= 12 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Volume} &= \text{cross sectional area} \times \text{length} \\ &= 12 \text{ cm}^2 \times 2 \text{ cm} \\ &= 24 \text{ cm}^3 \end{aligned}$$

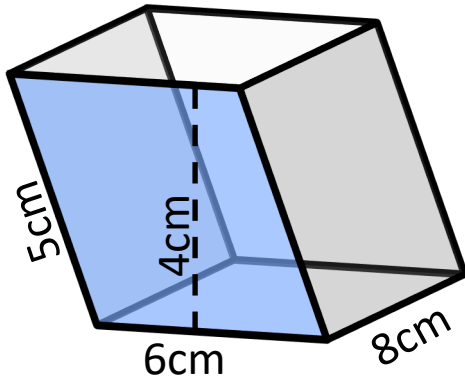
Q8



$$\begin{aligned} \text{Volume} &= \text{cross sectional area} \times \text{length} \\ \text{cross sectional area} &= (\text{base} \times \text{perpendicular height}) \\ &= (6 \text{ cm} \times 4 \text{ cm}) \\ &= 24 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Volume} &= \text{cross sectional area} \times \text{length} \\ &= 24 \text{ cm}^2 \times 5 \text{ cm} \\ &= 120 \text{ cm}^3 \end{aligned}$$

Q9



Volume = cross sectional area × length
cross sectional area

$$= (\text{base} \times \text{perpendicular height})$$

$$= (\quad \text{cm} \times \quad \text{cm})$$

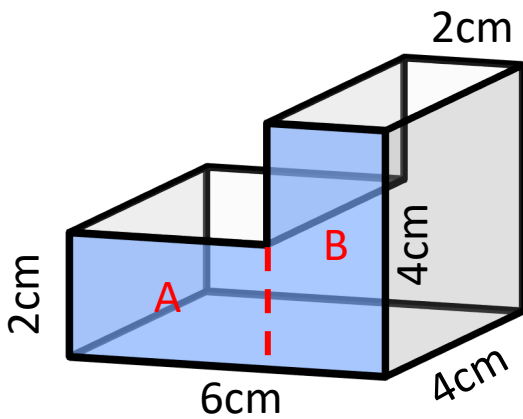
$$= \quad \text{cm}^2$$

Volume = cross sectional area × length

$$= \quad \text{cm}^2 \times \quad \text{cm}$$

$$= \quad \text{cm}^3$$

Q10



Volume = cross sectional area × length

Cross sectional area = area A + area B

$$= (4 \times 2) + (2 \times 4)$$

$$= 8 \text{ cm}^2 + 8 \text{ cm}^2$$

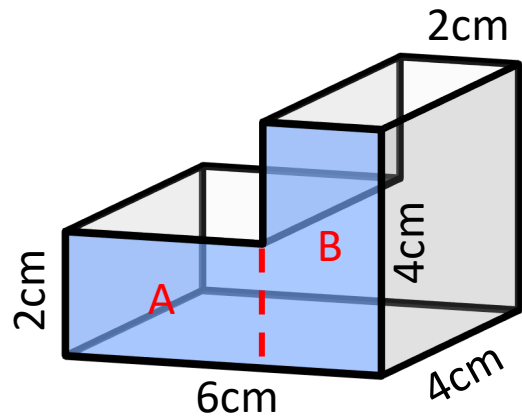
$$= \quad \text{cm}^2$$

Volume = cross sectional area × length

$$= \quad \text{cm}^2 \times \quad \text{cm}$$

$$= \quad \text{cm}^3$$

Q11



Volume = cross sectional area × length

Cross sectional area = area A + area B

$$= (\quad \times \quad) +$$

$$(\quad \times \quad)$$

$$= \quad \text{cm}^2 +$$

$$\quad \text{cm}^2$$

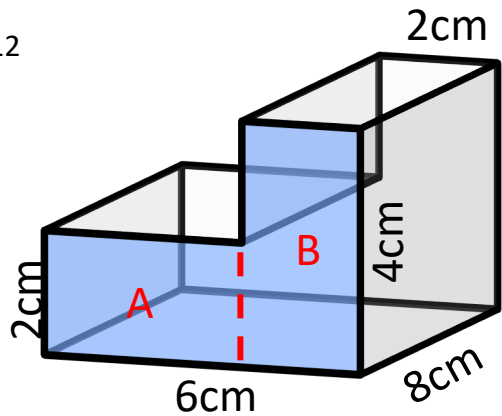
$$= \quad \text{cm}^2$$

Volume = cross sectional area × length

$$= \quad \text{cm}^2 \times \quad \text{cm}$$

$$= \quad \text{cm}^3$$

Q12



Volume = cross sectional area × length

Cross sectional area = area A + area B

$$= (\quad \times \quad) +$$

$$(\quad \times \quad)$$

$$= \quad \text{cm}^2 +$$

$$\quad \text{cm}^2$$

$$= \quad \text{cm}^2$$

Volume = cross sectional area × length

$$= \quad \text{cm}^2 \times \quad \text{cm}$$

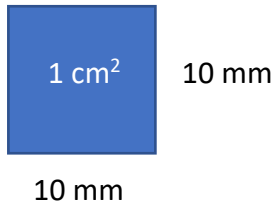
$$= \quad \text{cm}^3$$

Section 12: Converting area and cubic units

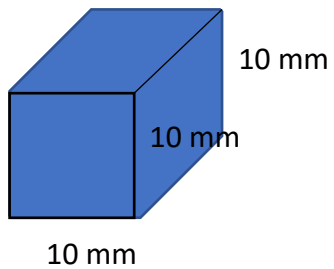
$$1 \text{ cm} = 10 \text{ mm}$$

$$1 \text{ m} = 100 \text{ cm}$$

$$\begin{aligned} \text{So } 1 \text{ cm}^2 &= 10 \text{ mm} \times 10 \text{ mm} \\ &= 100 \text{ mm}^2 \end{aligned}$$

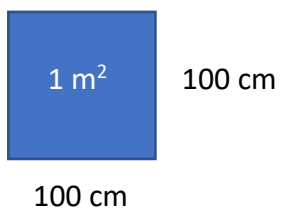


$$\begin{aligned} \text{And } 1 \text{ cm}^3 &= 10 \text{ mm} \times 10 \text{ mm} \times 10 \text{ mm} \\ &= 1000 \text{ mm}^3 \end{aligned}$$

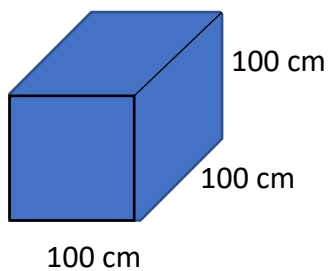


Likewise

$$\begin{aligned} 1 \text{ m}^2 &= 100 \text{ cm} \times 100 \text{ cm} \\ &= 10,000 \text{ cm}^2 \end{aligned}$$



$$\begin{aligned} \text{And } 1 \text{ m}^3 &= 100 \text{ cm} \times 100 \text{ cm} \times 100 \text{ cm} \\ &= 1,000,000 \text{ cm}^3 \end{aligned}$$



Worksheet 12: Converting area and cubic units

Q1

Convert 7cm^2 into mm^2

$$\begin{aligned} 1\text{ cm}^2 &= 100\text{ mm}^2 \\ 7\text{ cm}^2 &= 7 \times 100\text{ mm}^2 \\ &= \quad \text{mm}^2 \end{aligned}$$

Q2

Convert 70cm^2 into mm^2

$$\begin{aligned} 1\text{ cm}^2 &= 100\text{ mm}^2 \\ 70\text{ cm}^2 &= \quad \times 100\text{ mm}^2 \\ &= \quad \text{mm}^2 \end{aligned}$$

Q3

Convert 0.70cm^2 into mm^2

$$\begin{aligned} 1\text{ cm}^2 &= 100\text{ mm}^2 \\ 0.70\text{ cm}^2 &= \quad \times \quad \text{mm}^2 \\ &= \quad \text{mm}^2 \end{aligned}$$

Q4

Convert 0.7cm^2 into mm^2

$$\begin{aligned} 1\text{ cm}^2 &= 100\text{ mm}^2 \\ 0.7\text{ cm}^2 &= \quad \times \quad \text{mm}^2 \\ &= \quad \text{mm}^2 \end{aligned}$$

Q5

Convert 0.07cm^2 into mm^2

$$\begin{aligned} 1\text{ cm}^2 &= 100\text{ mm}^2 \\ 0.07\text{ cm}^2 &= \quad \times \quad \text{mm}^2 \\ &= \quad \text{mm}^2 \end{aligned}$$

Q7

Convert 3.07cm^3 into mm^3

$$\begin{aligned} 1\text{ cm}^3 &= 1\,000\text{ mm}^3 \\ 3.07\text{ cm}^3 &= \quad \times \quad \text{mm}^3 \\ &= \quad \text{mm}^3 \end{aligned}$$

Q8

Convert 3.7cm^3 into mm^3

$$\begin{aligned} 1\text{ cm}^3 &= 1\,000\text{ mm}^3 \\ 3.7\text{ cm}^3 &= \quad \times \quad \text{mm}^3 \\ &= \quad \text{mm}^3 \end{aligned}$$

Q9

Convert 3.7m^3 into cm^3

$$\begin{aligned} 1\text{ m}^3 &= 1\,000\,000\text{ cm}^3 \\ 3.7\text{ m}^3 &= \quad \times \quad \text{cm}^3 \\ &= \quad \text{cm}^3 \end{aligned}$$

Q10

Convert 0.37m^3 into cm^3

$$\begin{aligned} 1\text{ m}^3 &= 1\,000\,000\text{ cm}^3 \\ 0.37\text{ m}^3 &= \quad \times \quad \text{cm}^3 \\ &= \quad \text{cm}^3 \end{aligned}$$

Q11

Convert 0.37m^3 into mm^3

$$\begin{aligned} 1\text{ m}^3 &= 1\,000\,000\text{ cm}^3 \\ 1\text{ cm}^2 &= 100\text{ mm}^2 \\ 0.37\text{ cm}^3 &= \quad \times \quad \text{cm}^3 \\ &= \quad \text{cm}^3 \\ \text{cm}^3 &= \quad \text{mm}^3 \end{aligned}$$

Q12

Convert 37m^3 into mm^3

$$\begin{aligned} 1\text{ m}^3 &= 1\,000\,000\text{ cm}^3 \\ 1\text{ cm}^2 &= 100\text{ mm}^2 \\ 37\text{ cm}^3 &= \quad \times \quad \text{cm}^3 \\ &= \quad \text{cm}^3 \\ \text{cm}^3 &= \quad \text{mm}^3 \end{aligned}$$

Q13

Convert 137m^3 into mm^3

$$\begin{aligned} 1\text{ m}^3 &= 1\,000\,000\text{ cm}^3 \\ 1\text{ cm}^2 &= 100\text{ mm}^2 \\ 137\text{ cm}^3 &= \quad \times \quad \text{cm}^3 \\ &= \quad \text{cm}^3 \\ \text{cm}^3 &= \quad \text{mm}^3 \end{aligned}$$