- How does Sunlight heat a planet with no atmosphere? This is similar to our dust grain heating problem
- First pass: Consider a planet of radius a at a distance R from a star of luminosity L\*. The energy received by the planet per time per area is,

$$\frac{L_*}{4\pi R^2}\pi a^2$$

 The planet is heated to a temperature, *T*, & re-emits radiation in thermal infrared. The amount of radiation released is

$$4\pi a^2 \sigma T^4$$

• By equating both of these expressions,

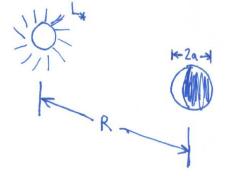
$$\frac{L_*}{4\pi R^2}\pi a^2 = 4\pi a^2\sigma T^4$$

• And solving for *T*,

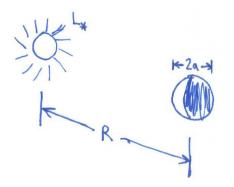
$$T = \frac{1}{2} \left( \frac{L_*}{\pi R^2 \sigma} \right)^{1/4}$$

• So, plugging in the appropriate numbers for Earth,

$$T = \frac{1}{2} \left( \frac{L_*}{\pi R^2 \sigma} \right)^{1/4} = \frac{1}{2} \left[ \frac{3.83 \times 10^{26} \text{ W}}{\pi (1.5 \times 10^{11} \text{ m})^2 \times 5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}} \right]^{1/4} = 278 \text{ K}^{-1}$$



Second pass: But, of course, planets reflect a certain fraction of the light that strikes then. The albedo, A, is defined as the fraction of light incident on an object that is reflected back into space. So, in actuality, the energy absorbed by the planet time<sup>-1</sup> area<sup>-1</sup> is,



$$\frac{L_*}{4\pi R^2}\pi a^2(1-A)$$

• And thus, the temperature expression becomes,

$$T = \frac{1}{2} \left( \frac{L_* [1 - A]}{\pi R^2 \sigma} \right)^{1/4}$$

• In terms of albedo, the general breakdown is -

Albedo = 0 (no reflection) Albedo = 1 (all reflected) Albedo = 0.7 (cloud, snow, ice) Albedo = 0.1-0.25 (rocks)

 The Earth has an albedo across all wavelengths (I.e., a Bond albedo) of 0.306. So, the T of the Earth is,

$$T = \frac{1}{2} \left( \frac{L_*(1-A)}{\pi R^2 \sigma} \right)^{1/4} = \frac{1}{2} \left[ \frac{3.83 \times 10^{26} \text{ W} \times (1-0.306)}{\pi (1.5 \times 10^{11} \text{ m})^2 \times 5.67 \times 10^{-8} \text{ W} \text{ m}^{-2} \text{ K}^{-4}} \right]^{1/4} = 253 \text{ K}$$

Planet	Visual albedo	Bond albedo	
Mercury	0.106	0.119	
Venus	0.650	0.750	
Earth	0.367	0.306	
Mars	0.150	0.250	
Jupiter	0.520	0.343	
Saturn	0.470	0.342	
Uranus	0.510	0.300	
Neptune	0.410	0.290	
Pluto	0.300	0.367	

Table X.1. The visual and Bond albedoes of the planets.

• The table below shows the results of the calculation for the terrestrial planets & the moon -

#### Table 10.2 Temperatures of the Terrestrial Worlds

World	Distance to Sun (AU)	Albedo ( $0 = black$ , 1 = white)	Length of Day (Earth days)	"No Greenhouse" Temperature*	Observed Average Surface Temperature
Mercury	0.38	0.11	176	440 K	700 K (day), 100 K (night)
Venus	0.72	0.72	117	230 K	740 K
Earth	1.00	0.36	1	250 K	288 K
Moon	1.00	0.07	28	273 K	400 K (day), 100 K (night)
Mars	1.52	0.25	≈l	218 K	223 K

$$T = \frac{1}{2} \left( \frac{L_*(1-A)}{\pi R^2 \sigma} \right)^{1/4} = \frac{1}{2} \left[ \frac{3.83 \times 10^{26} \text{ W} \times (1-0.306)}{\pi (1.5 \times 10^{11} \text{ m})^2 \times 5.67 \times 10^{-8} \text{ W} \text{ m}^{-2} \text{ K}^{-4}} \right]^{1/4} = 253 \text{ K}$$

- We have, of course, ignored a couple of things:
- First, planets rotate, & the speed of the rotation affects whether the planet has a nearly uniform temperature, or if it has a "day" & "night"-side temperatures. For no, rotation, only half of the planet is illuminated, thus,

$$\frac{L_*(1-A)}{4\pi R^2}\pi a^2 = 2\pi a^2 \sigma T^4 \quad \to \quad T = \left[\frac{L_*(1-A)}{8\pi \sigma R^2}\right]^{1/4}$$

Table 10.2 Ter	mperatures of the	<b>Terrestrial Worlds</b>
----------------	-------------------	---------------------------

World	Distance to Sun (AU)	Albedo ( $0 = black$ , 1 = white)	Length of Day (Earth days)	"No Greenhouse" Temperature*	Observed Average Surface Temperature
Mercury	0.38	0.11	176	440 K	700 K (day), 100 K (night)
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Moon	1.00	0.07	28	273 K	400 K (day), 100 K (night)
Mars	1.52	0.25	≈l	218 K	223 K

• For a non-rotating Mercury,

$$T = \left(\frac{L_*(1-A)}{8\pi R^2 \sigma}\right)^{1/4} = \frac{1}{2} \left[\frac{3.83 \times 10^{26} \text{ W} \times (1-0.119)}{8\pi (0.38 \text{ AU} \times 1.5 \times 10^{11} \text{ m AU}^{-1})^2 \times 5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}}\right]^{1/4} = 520 \text{ K}^{-1}$$

 I.e., lower than 700 K, but higher by 2<sup>1/4</sup> than the rapid rotation approximation.

World	Distance to Sun (AU)	Albedo (0 = black, 1 = white)	Length of Day (Earth days)	"No Greenhouse" Temperature*	Observed Average Surface Temperature
Mercury	0.38	0.11	176	440 K	700 K (day), 100 K (night)
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Mars	1.52	0.25	≈l	218 K	223 K

Table 10.2 Temperatures of the Terrestrial Worlds

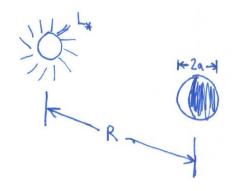
 Second, planets have atmospheres, the composition of which will affect the planet's surface temperature. We'll talk about the Greenhouse effect momentarily

Table 10.2	<b>Temperatures of t</b>	the Terrestrial	Worlds
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World	Distance to Sun (AU)	Albedo (0 = black, I = white)	Length of Day (Earth days)	"No Greenhouse" Temperature*	Observed Average Surface Temperature
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Moon	1.00	0.07	28	273 K	400 K (day), 100 K (night)
Mars	1.52	0.25	≈]	218 K	223 K

 Third pass: we can include an emissivity, ε, which is the fraction on incident radiation which is emitted by the planet. Typically, ε ~ 0.8 - 0.9.

$$\frac{L_*}{4\pi R^2}\pi a^2(1-A) = 4\pi a^2\sigma\epsilon T^4$$



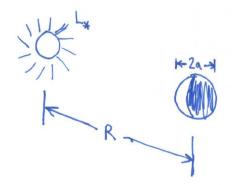
• And thus, the temperature expression becomes,

$$T = \frac{1}{2} \left[ \frac{L_*(1-A)}{\sigma \epsilon \pi R^2} \right]^{1/4}$$

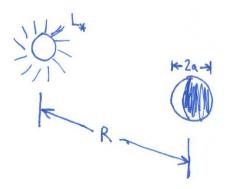
• The *T* is higher by a factor of 1.03 - 1.06 because of  $\varepsilon$ .

 Note that atmospheres affect A & ε because of clouds, surface volatiles (ocean, polar caps), gaseous molecular absorption, & Rayleigh scattering.

$$T = \frac{1}{2} \left[ \frac{L_*(1-A)}{\sigma \epsilon \pi R^2} \right]^{1/4}$$



• Fourth pass: planets can have internal heat sources. If the internal heat source is  $L_p$ , then,  $\frac{L_*}{4\pi R^2}\pi a^2(1-A) + L_p = 4\pi a^2\sigma\epsilon T^4$ 



- Observations of the giant planets show that L<sub>p</sub> is significant.
- But where does *L*<sub>p</sub> come from? Maybe heat of formation. Consider,

$$t_K = \frac{\text{total gravitational binding energy}}{\text{rate of energy loss}} \sim \frac{GM^2}{R} \frac{1}{L}$$

$t_K = \frac{\mathrm{to}}{-}$			l binding ergy loss	$\frac{\text{energy}}{\sim} \sim \frac{0}{2}$	$\frac{GM^2}{R} \frac{1}{L}$
	<i>M</i> (kg)	<i>R</i> (m)	<i>L</i> (W)	$t_{K}(s)$	$t_{\kappa}$ (yr)
Jupiter	2x10 <sup>27</sup>	7x10 <sup>7</sup>	3x10 <sup>17</sup>	1.3x10 <sup>19</sup>	4x10 <sup>11</sup>
Saturn	6x10 <sup>26</sup>	6x10 <sup>7</sup>	8x10 <sup>16</sup>	5x10 <sup>18</sup>	1x10 <sup>11</sup>
Uranus	9x10 <sup>25</sup>	2x10 <sup>7</sup>	<2x10 <sup>15</sup>	>1.3x10 <sup>19</sup>	>4x10 <sup>11</sup>
Neptune	1x10 <sup>26</sup>	2x10 <sup>7</sup>	2x10 <sup>15</sup>	1.7x10 <sup>19</sup>	6x10 <sup>11</sup>

• For  $t_{\kappa}$  > age of planets, the observed heat loss may be heat of formation

• For Saturn,  $t_{\kappa}$  < age of Saturn. Detailed calculations verify this.

	<i>M</i> (kg)	<i>R</i> (m)	<i>L</i> (W)	$t_{K}(s)$	$t_{\kappa}$ (yr)
Jupiter	2x10 <sup>27</sup>	7x10 <sup>7</sup>	3x10 <sup>17</sup>	1.3x10 <sup>19</sup>	4x10 <sup>11</sup>
Saturn	6x10 <sup>26</sup>	6x10 <sup>7</sup>	8x10 <sup>16</sup>	5x10 <sup>18</sup>	1x10 <sup>11</sup>
Uranus	9x10 <sup>25</sup>	2x10 <sup>7</sup>	<2x10 <sup>15</sup>	>1.3x10 <sup>19</sup>	>4x10 <sup>11</sup>
Neptune	1x10 <sup>26</sup>	2x10 <sup>7</sup>	2x10 <sup>15</sup>	1.7x10 <sup>19</sup>	6x10 <sup>11</sup>

• For Saturn, **helium rain** is responsible for heat loss. At low temperature and pressure, liquid helium does not dissolve with liquid hydrogen. A deficit of helium is observed in the outer atmosphere of Saturn.

• Energy is produced through friction with atmosphere

# Atmospheres: Pressure vs. Height

Consider again the equation of hydrostatic equilibrium

$$rac{dp}{dh} = -
ho(h)g(h)$$

 Where g(h) is the acceleration due to gravity & ρ(h) is the density. Consider also the ideal gas law

$$p = \frac{\rho kT}{\mu m_H}$$

Assume further that g(h) = g, T = constant, & μ = constant.

$$\frac{dp}{dh} = -\left(\frac{p\mu m_H}{kT}\right)g$$

## Atmospheres: Pressure vs. Height

• Taking

$$rac{dp}{dh} = -\left(rac{p\mu m_H}{kT}
ight)g$$

• and integrating both sides,

$$\int_{P(0)}^{P} \frac{dp}{p} = -\left(\frac{\mu m_H g}{kT}\right) \int_{h=0}^{h} dh$$
$$\ln\left[\frac{P}{P(0)}\right] = -\left(\frac{\mu m_H g}{kT}\right) h$$
$$P(h) = P(0)e^{-\left(\frac{\mu m_H g}{kT}\right)h} = P(0)e^{-\left(\frac{h}{H}\right)h}$$

• The quantity *H* is called the scale height.

#### Atmospheres: Pressure vs. Height

• For the Earth,

 $H = \frac{kT}{\mu m_H g} = \frac{1.38 \times 10^{23} \text{ J K}^{-1} \times 290 \text{ K}}{29 \times 1.67 \times 10^{27} \text{ kg} \times 9.8 \text{ m s}^{-2}} \sim 8.4 \times 10^3 \text{m}$ 

• or,

$$8.4 \times 10^3 \mathrm{m} \left( \frac{R_{\mathrm{earth}}}{6.4 \times 10^6 \mathrm{m}} \right) = 0.0013 R_{\mathrm{earth}}$$

• I.e., *H* << *R*<sub>planet</sub>

### Mass of Atmosphere

 Because the atmosphere is so thin, the mass of the atmosphere can be estimated via,

$$P = \frac{mg}{\text{area}} = \frac{mg}{4\pi R^2}$$

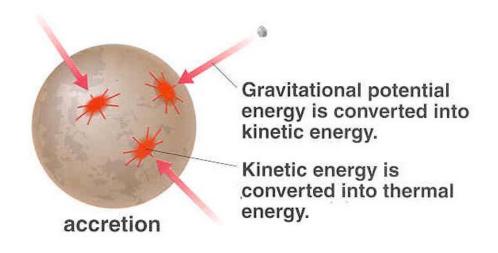
Rearranging the terms & plugging in numbers for the Earth,

$$\begin{split} m &= \frac{4\pi R^2 P}{g} = \frac{4\pi \times (6.4 \times 10^6 \text{ m})^2 \times 10^5 \text{ N m}^{-2}}{9.8 \text{ m s}^{-2}} \sim 5 \times 10^{18} \text{ kg} \\ \bullet \quad \text{Or,} \end{split}$$

$$5 \times 10^{18} \text{ kg} \left(\frac{M_{\text{earth}}}{6.0 \times 10^{24} \text{kg}}\right) = 9 \times 10^{-7} M_{\text{earth}}$$

# How does a planet obtain an atmosphere?

- Capture/Primordial: it forms with one. This is applicable to the gas giants
- **Outgassing**: it produces one from the material in which the planet is made. This is applicable to the terrestrial planets. They produced their atmosphere as the result of volcanism.



# How does a planet hold an atmosphere?

- First, define the exosphere as the height, h<sub>atm</sub>, at which the atmosphere is so thin that a gas molecular has a mean-free-path of infinity.
- For the Earth, h<sub>atm</sub> ~ 500 km, which is,

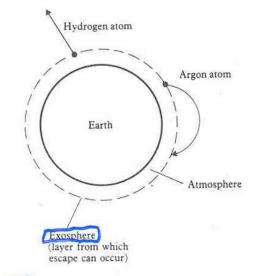


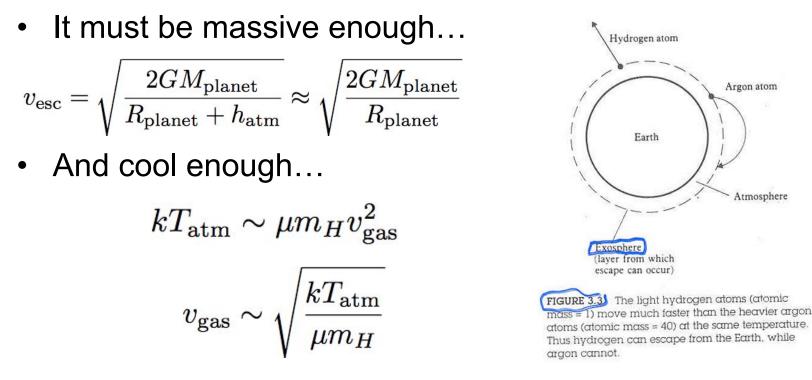
FIGURE 3.3) The light hydrogen atoms (atomic mass = 1) move much faster than the heavier argon atoms (atomic mass = 40) at the same temperature. Thus hydrogen can escape from the Earth, while argon cannot.

$$500 \times 10^3 \text{ m} \left( \frac{R_{\text{earth}}}{6.4 \times 10^6 \text{ m}} \right) = 0.078 R_{\text{earth}}$$

# How does a planet hold an atmosphere?

Argon atom

Atmosphere



- ... or the gas will escape.
- For a fixed T, lighter atoms escape more readily than heavier atoms because they have higher velocities

# How does a planet hold an atmosphere?

 For a gas of mass µm<sub>H</sub> in equilibrium at *T*, the probability distribution of speeds is described by th Maxwell-Boltzmann distribution.

$$p(v) = \left(\frac{2\mu^3 m_H^3}{\pi k^3 T^3}\right)^{1/2} v^2 e^{-\frac{\mu m_H v^2}{2kT}}$$

 Given this, the proportion of molecules with speeds exceeding the escape velocity at any time is

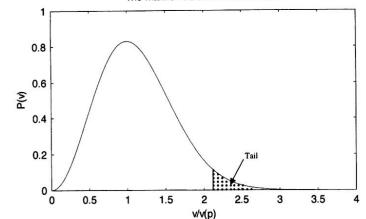
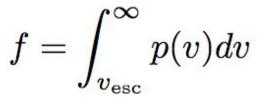
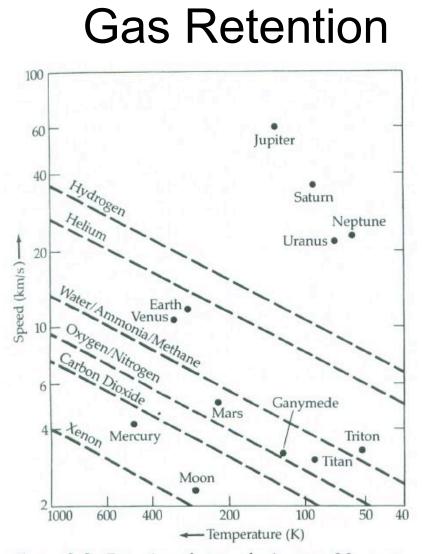


Figure 0.4. The Maxwell-Boltzmann distribution showing the tail which extends to infinity. The velocity is made non-dimensional by dividing by  $v(p) = \sqrt{2kT/\mu}$ .





**Figure 2–8** Retention of atmospheric gases. Mean molecular speeds are given as a function of temperature, along with the escape speeds for the indicated bodies. The dashed lines show ten times the mean molecular speeds, which defines an essentially infinite lifetime for that component in the atmosphere.

Photo	Planet	Average Distance from Sun (AU)	Temperature <sup>†</sup>	Relative Size	Average Radius (km)	Average Density (g/cm <sup>3</sup> )	Composition	Moons	Rings?
	Mercury	0.387	700 K	×	2,440	5.43	Rocks, metals	0	No
	Venus	0.723	740 K		6,051	5.24	Rocks, metals	0	No
	Earth	1.00	290 K		6,378	5.52	Rocks, metals	1	No
	Mars	1.52	240 K		3,397	3.93	Rocks, metals	2 (tiny)	No
-	Most asteroids	2–3	170 K	×	≤500	1.5–3	Rocks, metals	?	No
	Jupiter	5.20	125 K		71,492	1.33	H, He, hydrogen compounds <sup>‡</sup>	16	Yes
ø	Saturn	9.53	95 K		60,268	0.70 .	H, He, hydrogen compounds‡	18	Yes
	Uranus	19.2	60 K	•	25,559	1.32	H, He, hydrogen compounds‡	17	Yes
	Neptune	30.1	60 K	•	24,764	1.64	H, He, hydrogen compounds‡	8	Yes
	Pluto	39.5	40 K	×	1,160	2.0	lces, rock	1	No
à	Most comets	0-50,000	a few K <sup>s</sup>	8	a few km?	<1?	lces, dust	?	No

\*Appendix C gives a more complete list of planetary properties. \*Surface temperatures for all objects except Jupiter, Saturn, Uranus, and Nepturne, for which cloud-fog temperatures are listed. \*Includes water (H<sub>2</sub>O), methane (CH<sub>4</sub>), and ammonia (NH<sub>3</sub>). \*Comets passing close to the Sun warm considerably, especially their outer layers.



#### Contents

# Why does the atmospheric content of terrestrial & jovian planets differ?

- **Small planets**: formation via outgassing + planets have low masses & are hot
- Large planets: formation via capture/primordial + planets are massive & cold

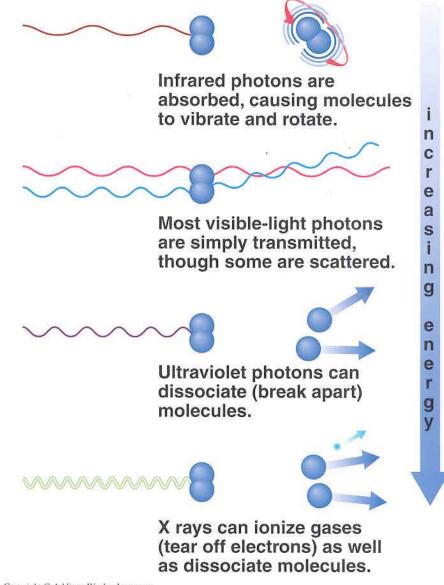
# The Generic Atmosphere

- Two Key Points
  - 1) Interaction between the gas & sunlight warms atmosphere
  - 2) Different wavelengths of light are absorbed in different layers of the atmosphere
- Processes

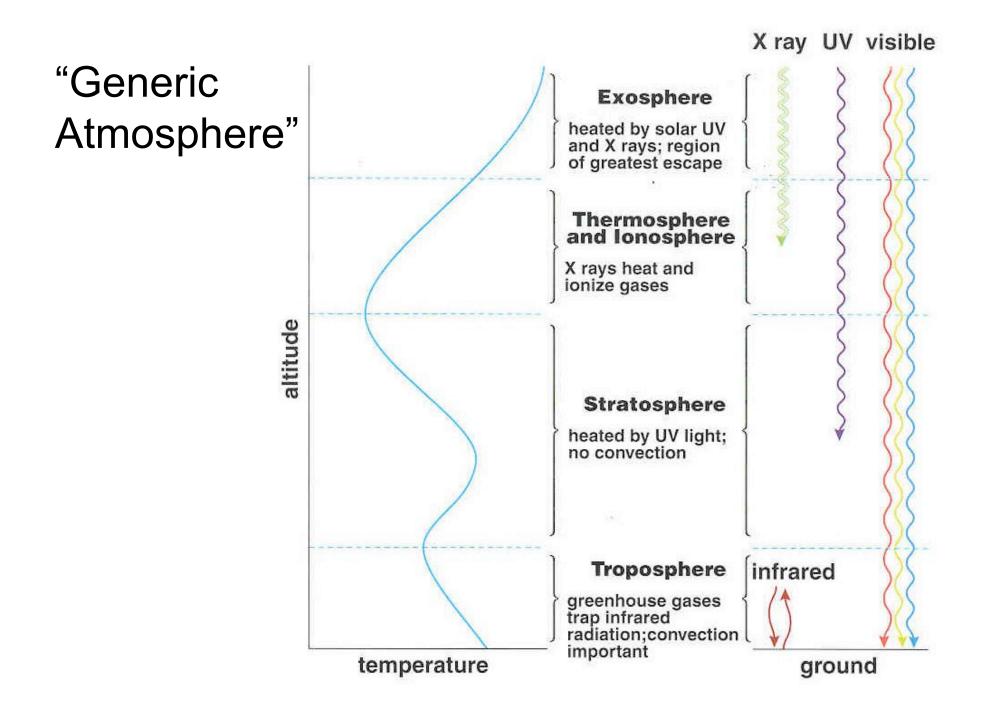
1) Some gases (greenhouse gases) absorb infrared light very efficiently

2) Atmosphere is generally transparent to visible light, but can scatter a fraction of visible light

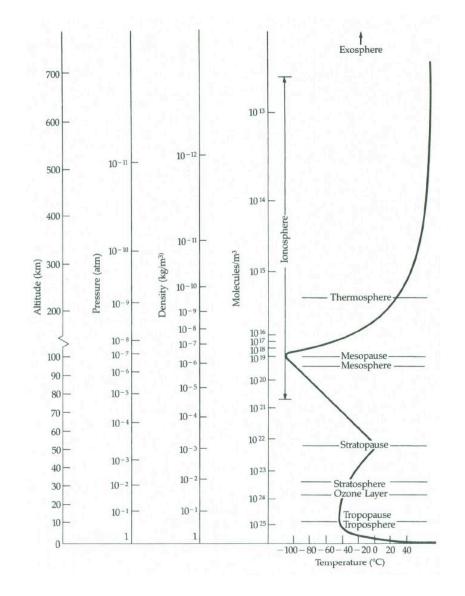
- 3) UV photons can break molecules such as Ozone apart
- 4) X-rays have enough energy to ionize atoms



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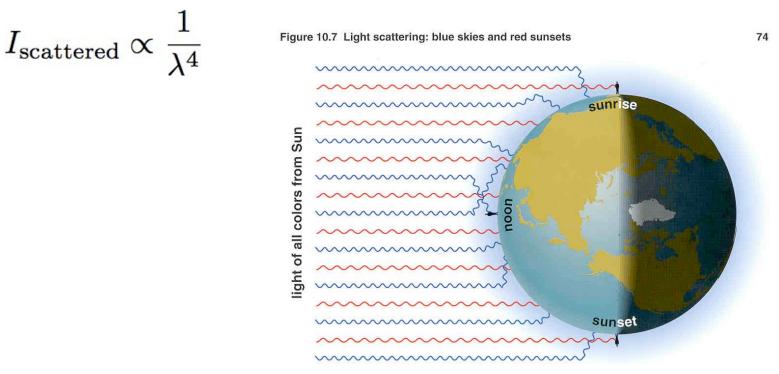


#### Earth: Altitude vs. Temperature



# Visible Light

- Absorbed by the Surface
- Shorter wavelength light is easier to scatter than longer wavelength light. The intensity of scattered radiation obeys the Rayleigh scattering law,



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# The Greenhouse Effect

- Greenhouse Effect: The process by which greenhouse gases in an atmosphere make a planet's surface temperature warmer than it would be in the absence of an atmosphere
  - 1) Visible light is absorbed by the surface of a planet
  - 2) Ground reradiates infrared photons
  - 3) The infrared photons are absorbed by greenhouse gases (carbon dioxide, water vapor)
  - 4) Greenhouse gases reradiate infrared photons isotropically
- Where is this important: Troposphere, where the atmosphere is thick
- This warming process causes convection

Figure 10.8 The greenhouse effect

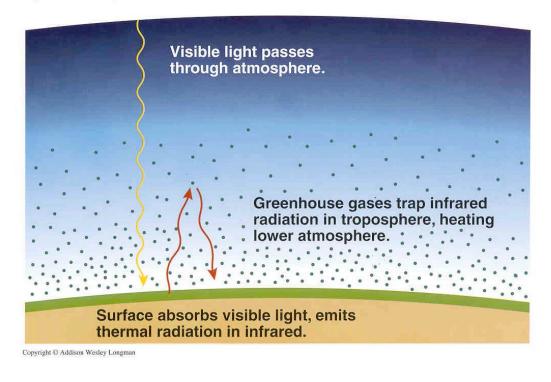
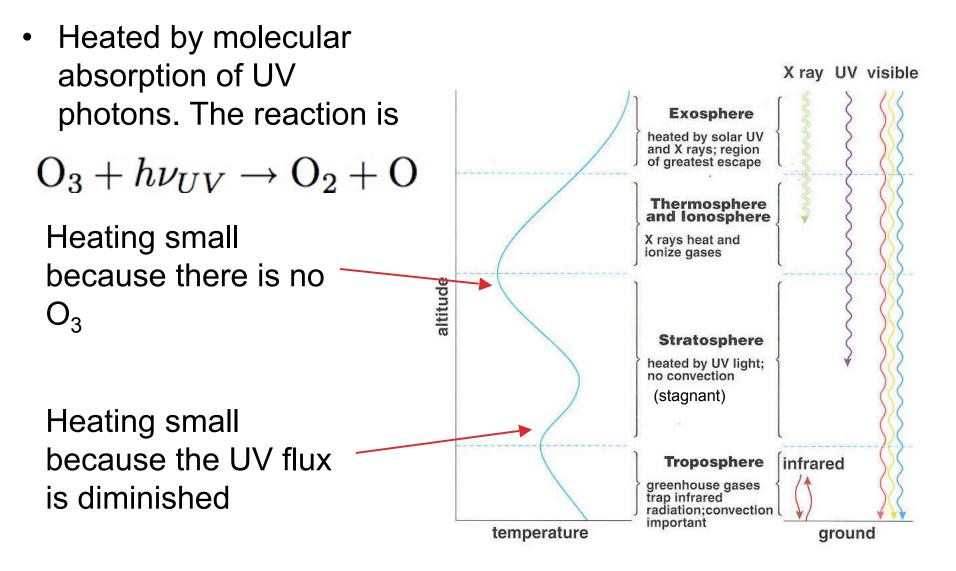


Table 10.2 Temperatures of the Terrestrial Worlds

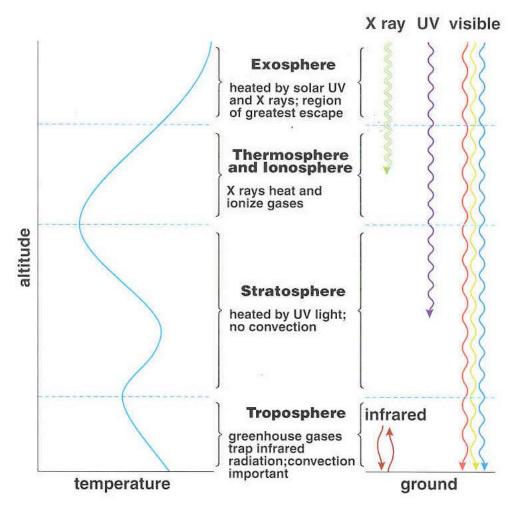
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Mars	1.52	0.25	≈l	218 K	223 K

# UV & Stratosphere



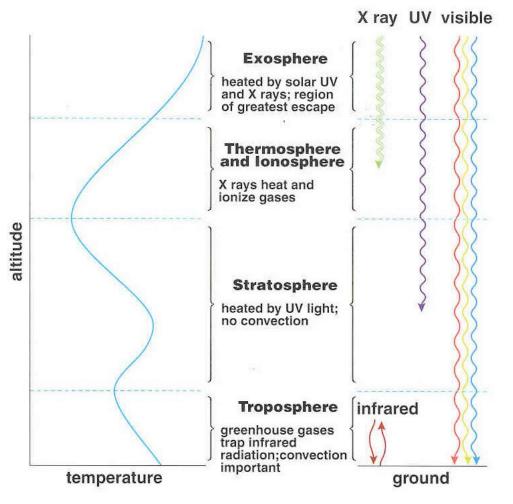
# X-rays & Thermosphere

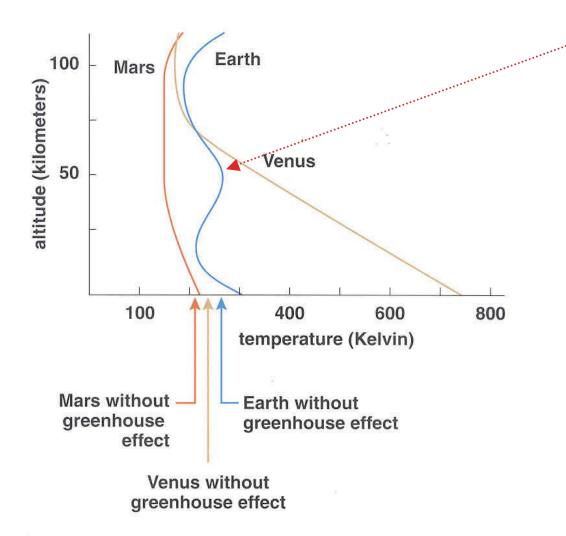
- Origin is similar to the stratosphere, but the heating source is  $O_2 + h\nu_X \rightarrow O + O$
- Gas is primarily ions & free electrons
- Because the mass in the thermosphere is small, the resulting temperatures are high (~ 1000-1200 K)



# Exosphere

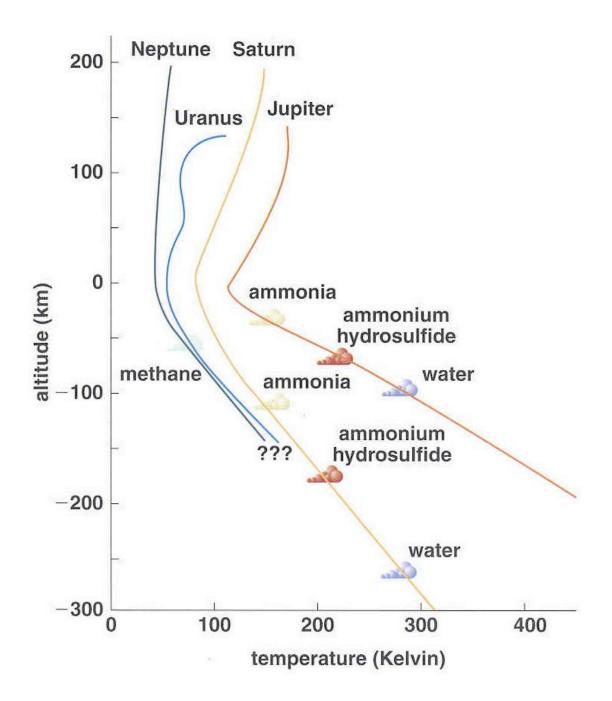
- High temperature, low density gas
- Space Shuttle & artificial satellites orbit the Earth in the exospheric layer
- Drag effects minor but important





Ozone - note that oxygen readily combines with Si, Al, Mg, etc. to make rocks. The presence of Oxygen our atmosphere indicates that biological processes are producing it.

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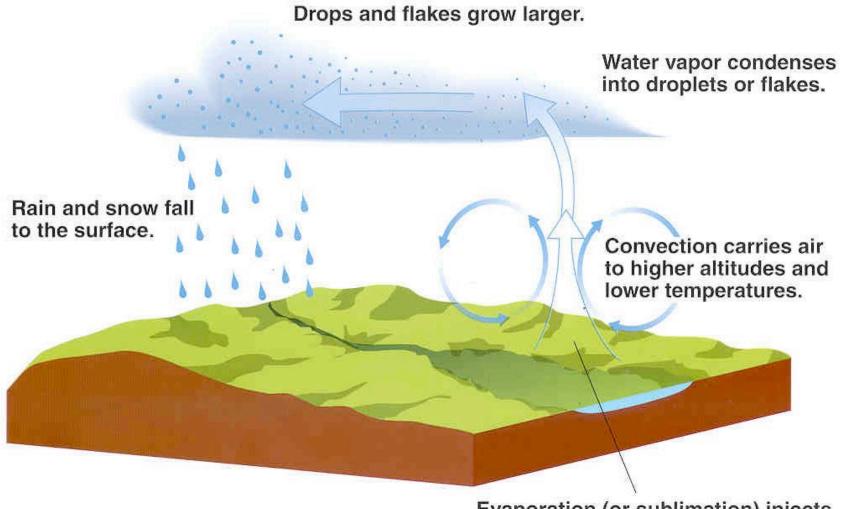


# Clouds

- Forms when one of the gases in the air condenses into liquid/solid form as a result of convection of air ascending a mountainside
- Once droplets grow so large that convection cannot hold them up against gravity, precipitation occurs
- Thus, strong convection → more clouds & precipitation
- Clouds on Different Planets

→ Earth: water

 $\rightarrow$  Venus: Sulfuric Acid (H<sub>2</sub>SO<sub>4</sub>) & water droplets

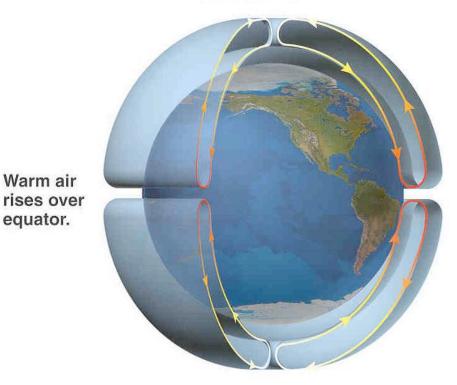


Evaporation (or sublimation) injects water vapor into lower atmosphere.

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#### **Atmosphere Heating & Wind Patterns**

 Equator heated more than poles, creating convective circulation cells Cool air descends over poles.



## Wind Patterns & Rotation

Rotation causes air moving on a planet to deviate from a straight line trajectory (coriolis effect)

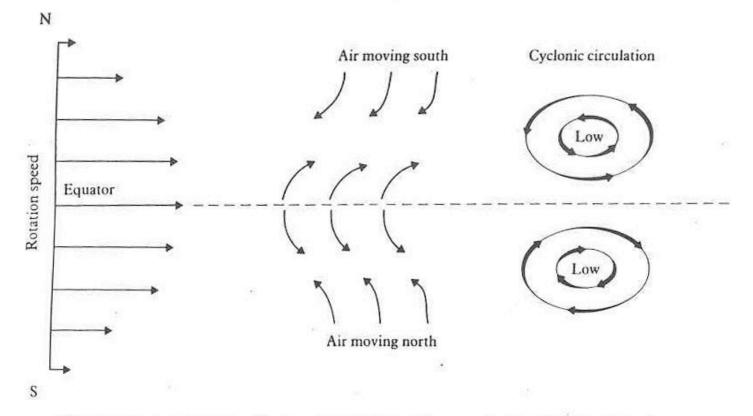
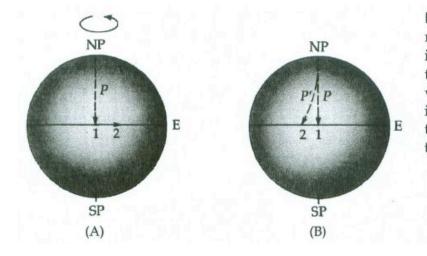


FIGURE 9.17 The Coriolis effect on air moving north or south on a rotating planet. You can experience this same force by trying to walk toward or away from the center of a spinning carousel.

## **Coriolis Effect**

 Rotation causes air moving on a planet to deviate from a straight line trajectory



**Figure 3–6** Projectile trajectories on the Earth. (A) On a rotating Earth, a rocket launched from the north pole (NP) is aimed at a target located at point 1. During the flight time, the Earth (and the target) rotate from 1 to 2. (B) The view from the Earth's surface shows the rocket's trajectory if the Earth did not rotate (P) and the actual one (P'). Note that the path curves to the right as seen by an observer at the north pole.

## **Coriolis Effect**

Consider a turntable rotating with speed ω and a body moving above the table with radial velocity ν. At time, t, the body moves a distance dr from A to B within a time dt. Thus,

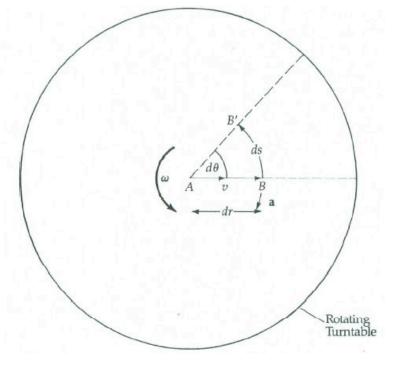
$$dr = vdt$$

 In *dt*, point B has moved to B'. The angle swept out by this motion is *dθ*. So,

$$d\theta = \omega dt$$

Note, also that,

$$d heta = {ds \over dr} ~~
ightarrow ~~ ds = dr d heta$$



## **Coriolis Effect**

• Thus,

$$ds = (dr)(d\theta) = (vdt)(\omega dt) = v\omega(dt)^2$$

- We know that, in general,  $d = \frac{1}{2}at^2$
- So, applying this to our turntable,

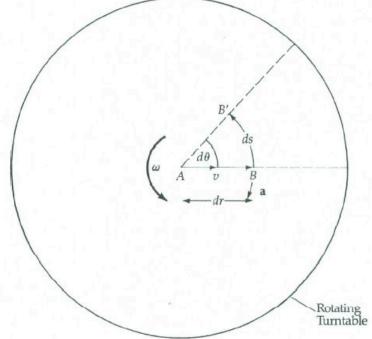
$$ds = \frac{1}{2}a(dt)^2$$

• So,

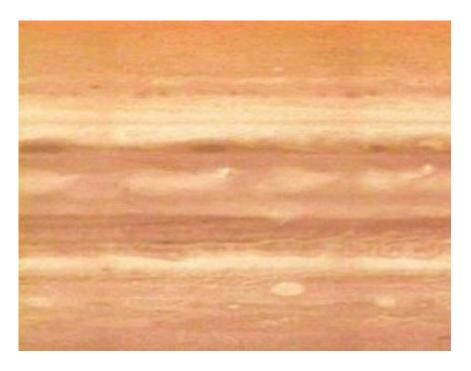
$$a=2ds\frac{1}{(dt)^2}=2v\omega(dt)^2\frac{1}{(dt)^2}=2v\omega$$

In terms of vectors (the vector ω is towards you),

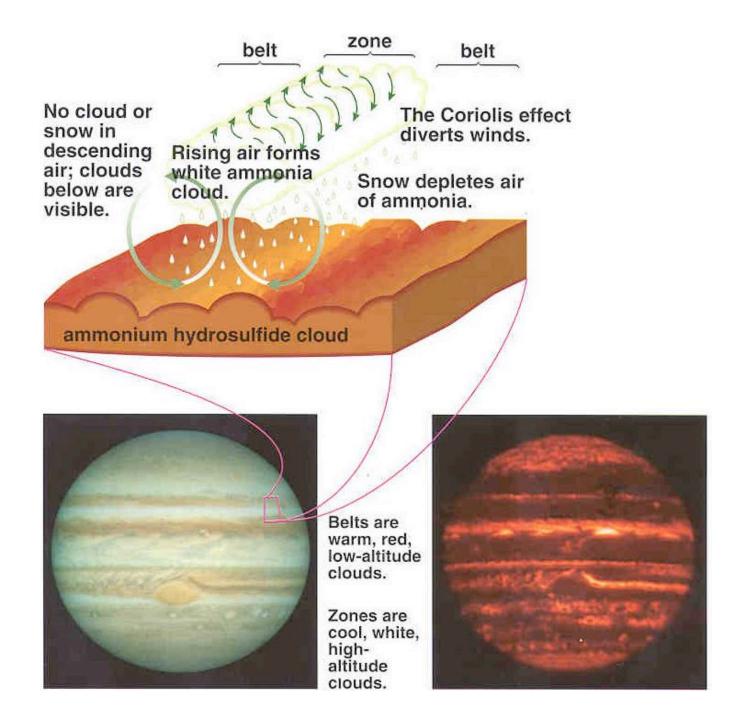
$$a_{\rm coriolis} = 2\vec{v} \times \vec{\omega}$$



## Gas Giants Have Strong Coriolis

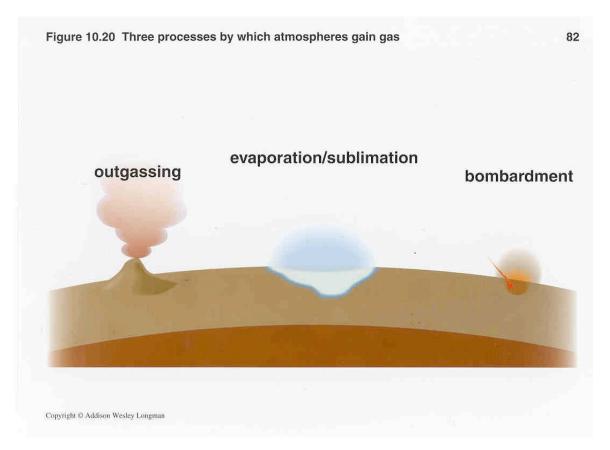


- ... which divide circulation cells into bands
- Convection results in bands
- For Jupiter -
- → Zones: rising, cooling air out of which ammonia condenses into clouds
- → Belts: falling air depleted in clouds; allows clouds below to be seen



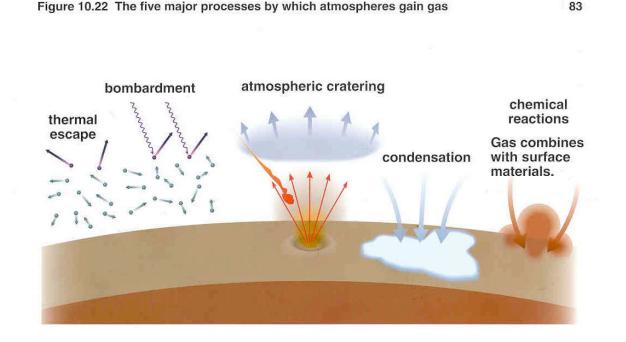
## Origin & Evolution of Atmosphere

- **Outgassing** volcanoes expel water, carbon dioxide, molecular nitrogen, hydrogen sulfide, sulfur dioxide
- Evaporation/Sublimation important for Mars
- **Bombardment** important for Mercury & the Moon



#### How are gases lost?

- 1) Thermal Escape atoms/ molecules moving fast enough to escape the pull of gravity
- 2) Bombardment: gives kinetic energy (speed) to atmospheric atoms & molecules & breaks heavier molecules into lighter atoms



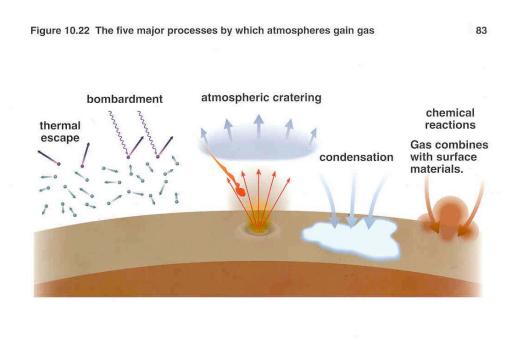
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#### Losing gases, cont.

#### 3) Atmospheric cratering –

via large impacts is important on small worlds

- 4) **Condensation** via cooling is important for Mars & polar craters of the Moon and Mercury
- 5) **Chemical Reactions**: air combining with rocks



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