## Poll Question \#1

PIPE
FLOTATION

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## Outline

- Why do we care?
-What is buoyancy?
- TWO methods to account for this our designs
- Factors of Safety
- Where the rubber meets the road...example problems!


## Flotation Failure




## U.S. 2019 Billion-Dollar Weather and Climate Disasters



This map denotes the approximate location for each of the 14 separate billion-dollar weather and climate disasters that impacted the United States during 2019.



National Weather Service

NOAA forecasters predict widespread flooding this spring, but do not expect it to be as severe or prolonged overall as the historic floods in 2019. Major to moderate flooding is likely in 23 states from the Northern Plains south to the Gulf Coast, with the most significant flood potential in parts of North Dakota, South Dakota and Minnesota.


Various levels of buoyancy depending on weight of the submerging body
$\stackrel{+}{4}$


## Relative Weights



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## Pipe Weights

$$
\mathrm{V}=18.35 \mathrm{ft}^{3} / \mathrm{ft}
$$

$62.4 \mathrm{lb} / \mathrm{ft} 3$


|


WATER
CONCRETE
HDPE
$\mathrm{W}=1145 \mathrm{lb} / \mathrm{ft}$
$\mathrm{W}=867 \mathrm{lb} / \mathrm{ft}$
$\mathrm{W}=26 \mathrm{lb} / \mathrm{ft}$

STEEL
$\mathrm{W}=48 \mathrm{lb} / \mathrm{ft}$

## 48" PIPE

## Poll Question \#2

## Flotation Calculation



Soil Resistance + Pipe Weight - Buoyancy Force $\geq 0.0$


## Microstructure of Soil



Buoyant Weight of Soil

$$
\gamma_{b}=\gamma_{t}-\gamma_{w}
$$

- $\gamma_{\mathrm{t}}=$ saturated unit weight of soil (pcf)
- $\gamma_{w}=$ unit weight of water (pcf)


## c)

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# Methods of Calculating Soil Resistance for Buoyancy 



## 1 - American Concrete Pipe Association (ACPA) Design Data (DD) 22



There are several installation conditions where there is the possibility that concrete pipe may float even though the density of concrete is approximately 2.4 times that of water. Some of these conditions are: the use of flooding to consolidate backfill; pipelines in areas which will be inundated, such as, a flood plain or under a future man-made lake; subaqueous pipelines; flowable fill installations; and pipelines in areas with a high groundwater table. When such conditions exist, flotation probability should be checked.

## FLOTATION FACTORS

The buoyancy of concrete pipe depends upon the weight of the pipe, the weight of the volume of water displaced by the pipe, the weight of the liquid load carried by the pipe and the weight of the backfill. As a conservative practice in analysis, the line should be considered empty so the weight of any future liquid load is then an additional safety factor.

## Pipe Weights

The average density of concrete is 150 pounds per cubic foot and the approximate weight per linear foot of circular concrete pipe may be calculated by the following equation:

$$
\begin{equation*}
W_{p}=\frac{-}{4}\left(B_{0}^{2}-D^{2}\right) 150 \tag{1}
\end{equation*}
$$

local conditions should be investigated when seeking solutions for specific projects.

## Displaced Water Weight

When water is displaced a buoyant or upward force exists, and, if the buoyant force is greater than the weight of the object displacing the water, flotation will occur. The weight of fresh water displaced per linear foot of circular pipe can be calculated by the following equation:

$$
\begin{equation*}
\mathrm{W}_{\mathrm{w}}=\frac{-}{4}\left(\mathrm{~B}_{\mathrm{c}}^{2}\right) 62.4 \tag{2}
\end{equation*}
$$

where
$\mathrm{W}_{\mathrm{w}}=$ weight of displaced water per linear foot,
pounds,
$\mathrm{B}_{\mathrm{C}}=$ outside pipe diameter, feet.

The average weights of the volume of fresh water displaced per linear foot of C14 and C76 pipe are presented in Tables 3 and 4.

## Backfill Weight

The weight of the backfill directly over the pipe assists in holding the pipe down. The unit weight of compacted backfill material varies with specific gravity, the grain size, and the degree of compaction. For preliminary computations, however, average values for surface dry


## 2 - Watkins/Moser (W/M) <br> Utah State



## Required Information



American Concrete Pipe Assocition

## ACPA DD 22



Equation 4 - Concrete Pipe Design Manual

## Watkins/Moser



$$
\begin{gathered}
\theta=45-\phi / 2 \\
\mathrm{R}_{\mathrm{s}}=\mathrm{PL}+2 \mathrm{X} \\
2 \mathrm{X}=\left[\left(\mathrm{H}+\mathrm{D}_{\mathrm{o}} / 2\right)^{2} \tan (45-\phi / 2)\right] \gamma_{\mathrm{b}} \\
\phi=\text { internal angle of friction }
\end{gathered}
$$



## Watkins/Moser


$\phi=$ internal angle of friction


American Concrete Pipe Association

## www.asce.org/accessengineering/




## Poll Question \#3

Which method accounts for a larger value for the soil resistance?

a. ACPA DD 22/ Column Method b. The Bar Method<br>c. Watkins \& Moser Method d. The Numerical Method



## Factors of Safety Geotechnical Engineering LRFD Bridge Substructures

Slope Stability 1.3 to 1.5
Foundation Bearing Capacity 2 to 3
Foundation Sliding 1.5+
Foundation Overturning 2.0+


## ACPA DD 22 - Factors of Safety -Guidance





- Buoyancy Force
- Soil Resistance
- Factor of Safety





## Is flotation a concern?

RC Pipe Weight =<br>$\mathrm{W}_{\mathrm{p}}=867 \mathrm{lb} / \mathrm{ft}$<br>Weight of Water<br>Displaced =<br>$W_{w}=\pi\left(d_{o} / 2\right)^{2} \gamma_{w}$<br>$\mathrm{W}_{\mathrm{w}}=1,145 \mathrm{lbs} / \mathrm{ft}$

$B F=-278 \mathrm{lb} / \mathrm{ft}$

## ACPA Method Concrete Pipe

## What is the Soil Resistance?

$$
R_{s}=W_{s}=P L=\gamma_{b}\left[H+\frac{D_{0}(4-\pi)}{8}\right] D_{o}
$$

Equation 4 - Concrete Pipe Design Manual

$$
\begin{gathered}
\mathrm{R}_{\mathrm{s}}=(120-62.4)\left[1+\frac{4.833(4-\pi)}{8}\right] 4.833 \\
\mathrm{R}_{\mathrm{s}}=423 \mathrm{lbs} / \mathrm{ft}
\end{gathered}
$$

## Watkins/Moser Method Concrete

 Pipe$$
\begin{aligned}
& \theta=45-\phi / 2 \\
& \mathrm{R}_{\mathrm{s}}=\mathrm{PL}+2 \mathrm{X} \\
& 2 \mathrm{X}=\left[\left(\mathrm{H}+\mathrm{D}_{\mathrm{o}} / 2\right)^{2} \tan (45-\phi / 2)\right] \gamma_{\mathrm{b}} \\
& 2 \mathrm{X}=\left[(1+4.833 / 2)^{2} \tan (45-30 / 2)\right](120-62.4) \\
& \quad \mathrm{R}_{\mathrm{s}}=423+388=811 \mathrm{lbs} / \mathrm{ft}
\end{aligned}
$$

## Results

## ACPA Method

- Net force $=(B F \times F S)+R_{s}$
- $=(-278 \times 1.25)+423=75 \mathrm{lbs}$

Watkins/Moser Method

- Net force $=(B F \times F S)+R_{s}$
- $=(-278 \times 2.0)+811=255 \mathrm{lbs}$



## RCP Results

| Method | Buoyancy <br> Force, BF <br> (lbs/ft) | Soil <br> Resistance <br> $\mathrm{R}_{\mathrm{s}}(\mathrm{lbs} / \mathrm{ft})$ | Factor of <br> Safety, <br> FS | Net <br> Force <br> $(\mathrm{lbs} / \mathrm{ft})$ |
| :---: | :---: | :---: | :---: | :---: |
| ACPA | -278 | 423 | 1.25 | 75 |
| W/M | -278 | 811 | 2.0 | 255 |

## Poll Question \#4



- Buoyancy Force
- Soil Resistance
- Factor of Safety




## Given:

CM Pipe Weight = $\mathrm{W}_{\mathrm{p}}=48 \mathrm{lb} / \mathrm{ft}$
$\gamma_{\mathrm{t}}=120 \mathrm{pcf}$
$\phi=30 \mathrm{deg}$


## Is flotation a concern?

## CM Pipe Weight =

 $\mathrm{W}_{\mathrm{p}}=48 \mathrm{lb} / \mathrm{ft}$Weight of Water
Displaced
$W_{w}=\pi\left(d_{o} / 2\right)^{2} \gamma_{w}$
$\mathrm{W}_{\mathrm{w}}=817 \mathrm{lbs} / \mathrm{ft}$
$B F=-769 \mathrm{lb} / \mathrm{ft}$

## ACPA Method Metal Pipe

What is soil resistance?

$$
R_{s}=W_{s}=P L=\gamma_{b}\left[H+\frac{D_{0}(4-\pi)}{8}\right] D_{o}
$$

Equation 4 - Concrete Pipe Design Manual

$$
\begin{gathered}
\mathrm{R}_{\mathrm{s}}=(120-62.4)\left[1+\frac{4.08(4-\pi)}{8}\right] 4.08 \\
\mathrm{R}_{\mathrm{s}}=338 \mathrm{lbs} / \mathrm{ft}
\end{gathered}
$$

## Watkins/Moser Method Metal Pipe

What is soil resistance?

$$
\begin{gathered}
\theta=45-\phi / 2 \\
\mathrm{R}_{\mathrm{s}}=\mathrm{PL}+2 \mathrm{X} \\
2 \mathrm{X}=\left[\left(\mathrm{H}+\mathrm{D}_{\mathrm{o}} / 2\right)^{2} \tan (45-\phi / 2)\right] \gamma_{\mathrm{b}} \\
2 \mathrm{X}=\left[(1+4.08 / 2)^{2} \tan (45-30 / 2)\right](120-62.4) \\
\mathrm{R}_{\mathrm{s}}=338+307=645 \mathrm{lbs} / \mathrm{ft}
\end{gathered}
$$



Results Metal Pipe

| Method | Buoyancy <br> Force, BF <br> $(\mathrm{lbs} / \mathrm{ft})$ | Soil <br> Resistance <br> $\mathrm{R}_{\mathrm{s}}(\mathrm{lbs} / \mathrm{ft})$ | Factor of <br> Safety, <br> FS | Net <br> Force <br> $(\mathrm{lbs} / \mathrm{ft})$ |
| :---: | :---: | :---: | :---: | :---: |
| ACPA | -769 | 338 | 1.25 | -623 |
| W/M | -769 | 645 | 2.0 | -893 |



- Buoyancy Force
- Soil Resistance
- Factor of Safety




## Given:

> HDPE Pipe Weight = $\mathrm{W}_{\mathrm{p}}=26 \mathrm{lb} / \mathrm{ft}$
> $\gamma_{\mathrm{t}}=120 \mathrm{pcf}$
> $\phi=30 \mathrm{deg}$


## Is flotation a concern?

HDPE Pipe Weight = $W_{p}=26 \mathrm{lb} / \mathrm{ft}$

Weight of Water Displaced $W_{w}=\pi\left(d_{o} / 2\right)^{2} \gamma_{w}$
$\mathrm{W}_{\mathrm{w}}=885 \mathrm{lbs} / \mathrm{ft}$
$B F=-859 \mathrm{lb} / \mathrm{ft}$

## ACPA HDPE Pipe



$$
R_{s}=W_{s}=P L=\gamma_{b}\left[H+\frac{D_{0}(4-\pi)}{8}\right] \quad D_{0}
$$

Equation 4 - Concrete Pipe Design Manual

$$
\begin{gathered}
\mathrm{R}_{\mathrm{s}}=(120-62.4)\left[1+\frac{4.25(4-\pi)}{8}\right] 4.25 \\
\mathrm{R}_{\mathrm{s}}=356 \mathrm{lbs} / \mathrm{ft}
\end{gathered}
$$

## Watkins/Moser HDPE Pipe

$$
\begin{aligned}
& \theta=45-\phi / 2 \\
& 2 \mathrm{X}=\left[\left(\mathrm{H}+\mathrm{D}_{\mathrm{o}} / 2\right)^{2} \tan (45-\phi / 2)\right] \gamma_{\mathrm{b}} \\
& 2 \mathrm{X}= \\
& \\
& \quad\left[(1+4.25 / 2)^{2} \tan (45-30 / 2)\right](120-62.4) \\
& \\
& \mathrm{R}_{\mathrm{s}}=356+325=681 \mathrm{lbs} / \mathrm{ft}
\end{aligned}
$$

## Results HDPE Pipe

| Method | Buoyancy <br> Force, BF <br> $(\mathrm{lbs} / \mathrm{ft})$ | Soil <br> Resistance <br> $\mathrm{R}_{\mathrm{s}}(\mathrm{lbs} / \mathrm{ft})$ | Factor of <br> Safety, <br> FS | Net <br> Force <br> $(\mathrm{lbs} / \mathrm{ft})$ |
| :---: | :---: | :---: | :---: | :---: |
| ACPA | -859 | 356 | 1.25 | -717 |
| W/M | -859 | 681 | 2.0 | -1037 |



## Comparison - ACPA Method

| 48" Pipe <br> Type | Buoyancy <br> Force, BF <br> $(\mathrm{lbs} / \mathrm{ft})$ | Soil <br> Resistance <br> $\mathrm{R}_{\mathrm{s}}(\mathrm{lbs} / \mathrm{ft})$ | Factor of <br> Safety, <br> FS | Net <br> Force <br> $(\mathrm{lbs} / \mathrm{ft})$ |
| :---: | :---: | :---: | :---: | :---: |
| HDPE | -859 | 356 | 1.25 | -717 |
| CMP | -769 | 338 | 1.25 | -623 |
| RCP | -278 | 423 | 1.25 | 75 |

## Comparison - W/M Method

| 48" Pipe <br> Type | Buoyancy <br> Force, BF <br> $(\mathrm{lbs} / \mathrm{ft})$ | Soil <br> Resistance <br> $\mathrm{R}_{\mathrm{s}}(\mathrm{lbs} / \mathrm{ft})$ | Factor of <br> Safety, <br> FS | Net <br> Force <br> $(\mathrm{lbs} / \mathrm{ft})$ |
| :---: | :---: | :---: | :---: | :---: |
| HDPE | -859 | 681 | 2.0 | -1037 |
| CMP | -769 | 645 | 2.0 | -893 |
| RCP | -278 | 811 | 2.0 | 255 |

## How Much Fill For a 48 Inch Pipe?

|  | Pipe Type |  |  |
| :---: | :---: | :---: | :---: |
| Method | RCP | CMP | HDPE |
| ACPA | 0.8 ft. | 3.7 ft. | $4 \mathrm{ft} .^{*}$ |
| M/W | 0.5 ft. | 2.8 ft. | 3.0 ft. |

[^0]
## ACPA Min Fill to Avoid Flotation

| Pipe <br> Size (in) | Min. <br> Fill (ft) | Pipe <br> Size (in) | Min. <br> Fill (ft) | Pipe <br> Size (in) | Min. <br> Fill (ft) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 21 | 0.1 | 42 | 0.6 | 78 | 1.5 |
| 24 | 0.1 | 48 | 0.8 | 84 | 1.7 |
| 27 | 0.2 | 54 | 0.9 | 90 | 1.9 |
| 30 | 0.3 | 60 | 1.1 | 96 | 2.0 |
| 33 | 0.3 | 66 | 1.2 | 102 | 2.2 |
| 36 | 0.4 | 72 | 1.4 | 108 | 2.4 |

## 48" RCP Results

| Shape | Buoyancy <br> Force, BF <br> $(\mathrm{lbs} / \mathrm{ft})$ | Soil <br> Resistance <br> $\mathrm{R}_{\mathrm{s}}(\mathrm{lbs} / \mathrm{ft})$ | Factor of <br> Safety, <br> FS | Net <br> Force <br> $(\mathrm{lbs} / \mathrm{ft})$ |
| :---: | :---: | :---: | :---: | :---: |
| Elliptical | -226 | 471 | 1.25 | 188 |
| Circular | -278 | 423 | 1.25 | 75 |

## Poll Question \#5

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Figure 5.19. Unanchored thin edge projecting.

## Source: FHWA HDS 5

c)

American Concrete Pipe Association






Source: FHWA HDS 5





## Poll Question \#6



# The End 

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## Water Table Not up to the Surface





## Given:




## Is flotation a concern?



HDPE Pipe Weight = $\mathrm{W}_{\mathrm{p}}=62 \mathrm{lb} / \mathrm{ft}$

Weight of Water Displaced
$W_{w}=\pi\left(d_{o} / 2\right)^{2} \gamma_{w}$
$\mathrm{W}_{\mathrm{w}}=1373 \mathrm{lbs} / \mathrm{ft}$
$B F=-1311 \mathrm{lb} / \mathrm{ft}$

## Water Table Not up to the Surface



$$
\begin{aligned}
\text { Net Force } & =(B F \times F S)+R_{s} \\
& =(-1311 \times 1.25)+R_{s}
\end{aligned}
$$

If the water table is above the top of the pipe and at or above the ground surface:

$$
\begin{equation*}
P_{s p}=\frac{\left(H+0.11 \frac{D_{o}}{12}\right) \gamma_{b}}{144} \tag{12.12.3.7-1}
\end{equation*}
$$

- If the water table is above the top of the pipe and below the ground surface:

$$
P_{s p}=\frac{1}{144}\left[\begin{array}{r}
{\left[\left(H_{W}-\frac{D_{o}}{24}\right)+0.11 \frac{D_{o}}{12}\right] \gamma_{b}+}  \tag{12.12.3.7-2}\\
{\left[H-\left(H_{w}-\frac{D_{o}}{24}\right)\right] \gamma_{s}}
\end{array}\right]
$$

- If the water table is below the top of the pipe:

$$
\begin{equation*}
P_{s p}=\frac{\left(H+0.11 \frac{D_{o}}{12}\right) \gamma_{s}}{144} \tag{12.12.3.7-3}
\end{equation*}
$$

## Calculation of Soil Resistance

$$
\begin{gathered}
R_{s}=\left(\gamma_{t}-\gamma_{w}\right)\left[H_{w}+\frac{D_{o}(4-\pi)}{8}\right] D_{o}+\gamma_{d}\left(H-H_{w}\right)\left(D_{o}\right) \\
R_{s}=(130-62.4)\left[1.5+\frac{5.29(4-\pi)}{8}\right] 5.29+110(3-1.5)(5.29) \\
R_{s}=739+873 \\
R_{s}=1612 \mathrm{lbs} / \mathrm{ft}
\end{gathered}
$$

## Results HDPE Pipe

| Method | Buoyancy <br> Force, BF <br> $(\mathrm{lbs} / \mathrm{ft})$ | Soil <br> Resistance <br> $\mathrm{R}_{\mathrm{s}}(\mathrm{lbs} / \mathrm{ft})$ | Factor of <br> Safety, <br> FS | Net <br> Force <br> $(\mathrm{lbs} / \mathrm{ft})$ |
| :---: | :---: | :---: | :---: | :---: |
| ACPA | -1311 | 1612 | 1.25 | -27 |

# Floatation of Horizontal Elliptical Concrete Pipe 







## Illustration 5.3 Dimensions and Approximate Weights of Elliptical Concrete Pipe

| ASTM C 507-Reinforced Concrete Elliptical Culvert, |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Storm Drain and Sewer Pipe |  |  |  |  |  |




1 Ft

## Is Flotation a Concern?

RC Pipe Weight = $\mathrm{W}_{\mathrm{p}}=1000 \mathrm{lb} / \mathrm{ft}$

Area of Water Displaced $=19.64 \mathrm{ft}^{2}$

Weight of Water Displaced = $\mathrm{W}_{\mathrm{w}}=1,226 \mathrm{lbs} / \mathrm{ft}$
$B F=-226 \mathrm{lb} / \mathrm{ft}$

Areas of Elliptical Pipe for Buoyancy Purposes

| Size <br> (in) | Total <br> Area <br> $\left(\mathrm{ft}^{2}\right)$ | Size <br> (in) |  | Total <br> Area <br> $\left(\mathrm{ft}^{2}\right)$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $24 \times 38$ | 8.02 | $63 \times 98$ |  | 50.66 |  |
| $27 \times 42$ |  | 9.55 | $68 \times 106$ |  | 58.14 |
| $29 \times 45$ |  | 11.44 | $72 \times 113$ |  | 66.38 |
| $32 \times 49$ |  | 13.58 | $77 \times 121$ |  | 75.70 |
| $34 \times 53$ |  | 15.58 | $82 \times 128$ |  | 84.09 |
| $38 \times 60$ |  | 19.64 | $87 \times 136$ |  | 93.62 |
| $43 \times 68$ |  | 25.02 | $92 \times 143$ |  | 103.95 |
| $48 \times 76$ | 30.49 | $97 \times 151$ | 114.74 |  |  |
| $53 \times 83$ | 24.8 | 36.5 | $106 \times 166$ |  | 138.81 |
| $58 \times 91$ | 43.05 | $116 \times 180$ |  | 164.76 |  |



What is the Soil Resistance from the Upper Haunch?

Rise $=38$ in $\quad$ Span $=60$ in $\quad$ Wall $=5.5$ in
$Y=38+2(5.5)=49$ in $\quad X=60+2(5.5)=71$ in
Rect. Area $=X^{*} Y=(49 \times 71) / 144=24.16 \mathrm{ft}^{2}$
Pipe Area $=19.64 \mathrm{ft}^{2}$
Upper Haunch Area $=(24.16-19.64) / 2=2.26 \mathrm{ft}^{2}$
Soil Weight from Upper Haunch $=2.26 \mathrm{ft}^{2} \times 1 \mathrm{ft} \times(120-62.4)=130 \mathrm{lbs} / \mathrm{ft}$

## ACPA Method Concrete Pipe

What is the Soil Resistance from the soil prism above the crown?

$$
\begin{aligned}
& \mathrm{R}_{\mathrm{s}}=\text { Upper Haunch }+ \text { Rectangular Soil Prism } \\
& \mathrm{R}_{\mathrm{s}}=130 \mathrm{lbs} / \mathrm{ft}+1 \mathrm{ft} \times(71 / 12) \times(120-62.4) \\
& \mathrm{R}_{\mathrm{s}}=471 \mathrm{lbs} / \mathrm{ft}
\end{aligned}
$$

## 48" RCP Results

| Shape | Buoyancy <br> Force, BF <br> $(\mathrm{lbs} / \mathrm{ft})$ | Soil <br> Resistance <br> $\mathrm{R}_{\mathrm{s}}(\mathrm{lbs} / \mathrm{ft})$ | Factor of <br> Safety, <br> FS | Net <br> Force <br> $(\mathrm{lbs} / \mathrm{ft})$ |
| :---: | :---: | :---: | :---: | :---: |
| Elliptical | -226 | 471 | 1.25 | 188 |
| Circular | -278 | 423 | 1.25 | 75 |

## Areas of Arch Pipe for Buoyancy Purposes

| Size <br> (in) |  | Total Area (ft ${ }^{2}$ ) | Size <br> (in) | $\begin{aligned} & \text { Flow } \\ & \text { Area } \end{aligned}$ | Total Area (ft ${ }^{2}$ ) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $18 \times 28^{1 / 2}$ |  | 4.5 | $54 \times 88$ |  | 37.9 |
| $\begin{gathered} 22^{1 / 2} \mathrm{x} \\ 36^{1 / 4} \\ \hline \end{gathered}$ |  | 7.0 | $62 \times 102$ | 14. | 50.4 |
| $\begin{gathered} 26^{5} / 8 x \\ 43^{3} / 8 \end{gathered}$ |  | 9.8 | $72 \times 115$ |  | 64.5 |
| $\begin{gathered} 31^{5 / 16 x} \\ 51^{1 / 8} \\ \hline \end{gathered}$ |  | 13.2 | $\begin{gathered} 77^{1 / 2 x} \\ 122 \end{gathered}$ |  | 73.5 |
| $36 \times 58^{1 / 2}$ |  | 17.2 | $\begin{gathered} \hline 87^{1 / 8 x} \\ 138 \\ \hline \end{gathered}$ | 36.0 | 93.5 |
| $40 \times 65$ |  | 21.2 | $\begin{gathered} 96^{7} / 8 \mathrm{x} \\ 154 \end{gathered}$ | 81.8 | 115.4 |
| $45 \times 73$ |  | 26.5 | $\begin{gathered} 106^{1 / 2 x} \\ 168^{3} / 4 \end{gathered}$ | 99. | 131.2 |

## Flowable Fill



$$
A=1 / 2 r_{o}^{2}(\theta-\sin \theta)
$$

$\theta=\operatorname{invcos}\left[\left(\mathrm{r}_{\mathrm{o}}-\mathrm{x}\right) / \mathrm{r}_{\mathrm{o}}\right] 2$

## Flowable Fill

- Using $\gamma_{\mathrm{ff}}=130 \mathrm{pcf}$
- Maximum depths of flowable fill
- HDPE pipe - 2 to 3 inches
- CMP pipe - 3 to 4 inches
- RCP pipe - approximately $40 \%$ of $D_{\text {。 }}$


## References

- ACPA Design Data 22, Flotation of Circular Concrete Pipe
- Buried Pipe Design by A.P. Moser, second edition, McGraw hill
- Structural Mechanics of Buried Pipes by R.K. Watkins and L.R. Anderson, CRC press
- Pipeline Installation by A. Howard, relativity publishing
- Soil Engineering by M. Spangler \& R. Handy, Harper \& Row
- Federal Highways Administration


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[^0]:    *For plastic pipe, a good rule of thumb is fill height equal to pipe diameter.

