## Polygon Practice

In 1-11, write the number of sides and the number of angles that each polygon has. Then match each description to one of the polygons drawn below. Label the polygon with the exercise number of the description that matches the polygon.

1. regular decagon

## 10 sides and angles

3. regular hexagon

## 6 sides and angles

5. regular octagon

## 8 sides and angles

7. regular pentagon

## 5 sides and angles

9. regular quadrilateral

## 4 sides and angles

11. regular triangle

## 3 sides and angles




## A Triangular Challenge

Classify each triangle as isosceles, scalene, or equilateral and as acute, right, or obtuse. The sum of the angle measures in a triangle is always $180^{\circ}$. You can use a protractor to help you draw the triangle in the space provided.

## Drawings may vary.

Who Am I?

1. I have two congruent sides. I also have two congruent angles that measure $45^{\circ}$ each.
I am a(n) right, isosceles triangle.

2. I have three congruent sides. I also have three congruent angles.
I am a(n) acute, equilateral triangle.

3. I have no congruent sides. One of my angles has a measure of $100^{\circ}$.


I am a(n) obtuse, scalene triangle.
4. Two of my angles measure $30^{\circ}$ each. My two shorter sides are congruent.
 I am a(n) obtuse, isosceles triangle.
5. My 3 angles have measures of $38^{\circ}, 52^{\circ}$, and $90^{\circ}$. My 3 sides are all different lengths.


I am a $\qquad$ triangle.

## A Quadrilateral Challenge

The sum of the angle measures in a quadrilateral is always $360^{\circ}$. You can use subtraction to find unknown angle measures. Each set of angle measures below represents three known angle measures in a quadrilateral. Write and solve an equation to find the unknown measure of the fourth angle.


Known Angle Measures

1. $90^{\circ}$
$90^{\circ}$
$90^{\circ}$

## Unknown Angle Measure

Add the given angle measures.

$$
90^{\circ}+90^{\circ}+90^{\circ}=270^{\circ}
$$

Subtract the sum from $360^{\circ}$.

$$
360^{\circ}-270^{\circ}=90^{\circ}
$$

2. $112^{\circ}$
$56^{\circ}$
$84^{\circ}$

$$
\frac{112^{\circ}+56^{\circ}+84^{\circ}=252^{\circ}}{360^{\circ}-252^{\circ}=108^{\circ}}
$$

3. 

$120^{\circ}$
$90^{\circ}$
$90^{\circ}$

$$
\begin{gathered}
120^{\circ}+90^{\circ}+90^{\circ}=300^{\circ} \\
360^{\circ}-300^{\circ}=60^{\circ}
\end{gathered}
$$

4. 

$55^{\circ}$
$55^{\circ}$
$125^{\circ}$

$$
\frac{55^{\circ}+55^{\circ}+125^{\circ}=235^{\circ}}{360^{\circ}-235^{\circ}=125^{\circ}}
$$

5. 

$135^{\circ}$

$$
\begin{gathered}
135^{\circ}+45^{\circ}+135^{\circ}=315^{\circ} \\
360^{\circ}-315^{\circ}=45^{\circ} \\
\hline
\end{gathered}
$$

6. 

$90^{\circ}$
$55^{\circ}$
$135^{\circ}$

$$
\frac{90^{\circ}+55^{\circ}+135^{\circ}=280^{\circ}}{360^{\circ}-280^{\circ}=80^{\circ}}
$$

7. 

$85^{\circ}$
$90^{\circ}$
$130^{\circ}$

## Triangle Quick Draw Match-Up

Divide each regular polygon into the given number of congruent triangles. The first one has been done for you.
Check students' drawings.
1.

2.


8 congruent triangles
4.


6 congruent triangles

5. Write Math How can you determine whether the triangles you drew inside each figure above are congruent?
Possible answer: I act it out by cutting out the shapes and folding them to see if the triangles
match each other.
6. Stretch Your Thinking Is it possible to divide the triangle
in Exercise 1 into 16 congruent triangles? Explain.
Yes. I can divide each of the 4 small triangles into
4 smaller triangles, for a total of 16 congruent
triangles.

## In Fit Shape

Complete the crossword puzzle by filling in the correct term for each clue.


## ACROSS

6. A solid figure with faces that are polygons.
7. This solid figure has three pairs of parallel faces, and all faces are congruent.
8. A solid figure that has two congruent polygons as bases and lateral faces that are rectangles.
9. A solid figure without any bases and with only one curved surface.

## DOWN

1. A cube has six congruent faces that are all $\qquad$ _.
2. Polygons that have the same shape and size are $\qquad$ _.
3. A solid figure with one circular base and one curved surface.
4. A solid figure that has two circular bases and one curved surface.
5. A flat surface of a solid figure.

## Unit Cubes

For each solid figure, write the fraction of unit cubes that are shaded. Write each fraction in simplest form. Assume that cubes you cannot see are not shaded.
1.

3.

$\frac{2}{3}$
5.

$\frac{1}{2}$
6.

2.

$\frac{1}{4}$
4.

$\frac{1}{3}$
7. Stretch Your Thinking In the fraction you wrote for Exercise 1, what does the denominator represent?

## Volume of Irregular Figures

Use the unit given. Find the volume.


Each cube $=1 \mathrm{cu} \mathrm{cm}$
Volume $=\underline{84 \mathrm{cu} \mathrm{cm}}$


Each cube $=1 \mathrm{cu} \mathrm{ft}$ Volume $=\underline{176 \mathrm{cu} \mathrm{ft}}$
2.


Each cube $=1 \mathrm{cu}$ in.
Volume $=\underline{68 \text { cu in. }}$
4.


Each cube $=1 \mathrm{cu}$ yd
Volume $=\underline{72 \mathrm{cu} \text { yd }}$
5. Write Math Explain how you found the volume of the figure in Exercise 4.

Possible explanation: I found the volume of a prism that is 8 units long, 3 units wide, and 4 units high. From that volume, I subtracted the volume of a figure that is 4 units long, 3 units wide, and 2 units high. The subtracted volume represents the "hole" in the prism.

## What Will Fit?

A cubic centimeter is 1 cm long on each edge. A cubic decimeter is 10 cm long on each edge. A cubic meter is 1 m long on each edge.

Estimate the smallest unit cube that will hold each object. Choose from a cubic centimeter, a cubic decimeter, and a cubic meter. Possible answers

1. a grain of rice cubic centimeter are given.
2. an orange cubic decimeter
3. a basketball $\qquad$ cubic meter
4. a pebble cubic centimeter
5. a cell phone cubic decimeter
6. a textbook $\qquad$
7. a key cubic decimeter
8. a backpack $\qquad$
9. a paper clip cubic decimeter
10. a raisin cubic centimeter
11. an iron $\qquad$ cubic meter
12. a can of paint cubic meter
13. a crayon cubic decimeter
14. a staple cubic centimeter
15. a stick of gum
cubic decimeter
16. Stretch Your Thinking How many cubic centimeters do you need to fill a cubic decimeter? How many cubic centimeters do you need to fill a cubic meter?

## 1,000 cubic centimeters; $1,000,000$ cubic

 centimeters
## Unknown Dimensions

Find the unknown dimensions. Use whole numbers only.

1. A rectangular prism has a volume of $96 \mathrm{ft}^{3}$. The area of the base is $24 \mathrm{ft}^{2}$. What is the height of the prism?

## 4 ft

3. A rectangular prism has a volume of $175 \mathrm{in}^{3}$. The height of the prism is 7 in . The base is a square. What is the length of a side of the base?

$$
5 \text { in. }
$$

5. A rectangular prism has a volume of $189 \mathrm{~cm}^{3}$. The height of the prism is 3 cm . What are the dimensions of the base? $\begin{array}{ll}\text { length }=\frac{9 \mathrm{~cm}}{7 \mathrm{~cm}} & \text { answers } \\ \text { width }=\underline{\text { are given. }} .\end{array}$
6. A rectangular prism has a volume of $384 \mathrm{~cm}^{3}$. The width is twice the height, and the length is three times the height. What are the dimensions of the prism?

$$
\begin{aligned}
& \text { length }=\frac{12 \mathrm{~cm}}{8 \mathrm{~cm}} \\
& \text { width }=\frac{4 \mathrm{~cm}}{\text { height }=4}
\end{aligned}
$$

2. A rectangular prism has a volume of $729 \mathrm{ft}^{3}$. The length, width, and height are all the same. What is the length of each side of the prism?

## 9 ft

4. A rectangular prism has a volume of $144 \mathrm{~cm}^{3}$. The base is a square with a length of 4 cm . What is the height of the prism?

## 9 cm

6. A rectangular prism has a volume of $160 \mathrm{~cm}^{3}$. The height of the prism is 5 cm . The length is twice the width. What are the dimensions of the base? length $=\frac{8 \mathrm{~cm}}{4 \mathrm{~cm}}$
width
7. A rectangular prism has a volume of $432 \mathrm{in}^{3}$. The height of the prism is 9 in . What are the dimensions of the base? length $=\frac{8 \mathrm{in} .}{6 \mathrm{in} .}$
width $=$ Possible answers are given.
8. Stretch Your Thinking For Exercise 8, what are other possible dimensions for the base?

## Possible answer: 3 in. and 16 in.; 4 in. and

 12 in.; 2 in. and 24 in.
## What Is the Volume?

The dimensions of a rectangular prism are given.
Find the volume of the prism. Possible answers are given.

1. length $=2$ feet, width $=15$ inches, height $=8$ inches

$$
V=\underline{2,880 \text { in. }^{3}}
$$

2. length $=4$ yards, width $=7$ feet, height $=3$ feet

$$
v=252 \mathrm{ft}^{3}
$$

3. length $=9$ centimeters, width $=35$ millimeters, height $=7$ centimeters

$$
v=\underline{220,500 \mathrm{~mm}^{3}}
$$

4. length $=1$ yard, width $=2$ feet, height $=18$ inches

$$
v=\underline{15,552 \text { in. }^{3}}
$$

5. length $=1$ meter, width $=3$ decimeters, height $=8$ centimeters

$$
v=\underline{24,000 \mathrm{~cm}^{3}}
$$

6. length $=9$ feet, width $=2$ yards, height $=36$ inches

$$
V=6 \mathrm{yd}^{3}
$$

7. Stretch Your Thinking What cubic unit did you use in your answer to Exercise 6? Express the volume in a different cubic unit.
Possible answer: cubic yards; $162 \mathrm{ft}^{3}$
or 279,936 in. ${ }^{3}$

## The Gift of Volume

Leah and Wayne are sending presents in the mail. Boxes A, B, and C are shipping boxes. Find the volume of each shipping box. Then solve each problem below.
A.

15 in.
B.

C.


Volume of A : 3,375 in. ${ }^{3}$ Volume of B: 504 in. $^{3}$
1.

2.


7 in.

Volume: 125 in. $^{3}$

How many of these boxes can fit into Box A?

27 boxes


8 in.
5.


Volume: $\qquad$
After Leah packs 10 of these presents in Box B, what is the volume left to pack other presents?
6.
 Volume: $\qquad$ After Wayne packs 3 of these presents in Box C, what is the volume left to pack other presents?

## Finding Unknown Side Lengths

The volume of each composite figure is given. Find the unknown side length.

1. Volume $=378$ in. $^{3}$


3 in.
3. Volume $=768 \mathrm{ft}^{3}$


4 ft
2. Volume $=2,400 \mathrm{ft}^{3}$

4. Volume $=864 \mathrm{~cm}^{3}$


16 cm
5. Write Math Explain how you found the unknown side length of the composite figure in Exercise 3.
Possible answer: I broke apart the composite figure into two rectangular prisms. The dimensions of the larger prism are $18 \mathrm{ft}, 8 \mathrm{ft}$, and 4 ft , so its volume is $18 \times 8 \times 4$, or $576 \mathrm{ft}^{3}$. So, the volume of the smaller prism must be $768-576$, or $192 \mathrm{ft}^{3}$. I know its length is 6 ft , and its width is 8 ft . Its height is $192 \div(6 \times 8)$, or $192 \div 48$. The quotient is 4 . So the height of the smaller prism is 4 ft .

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