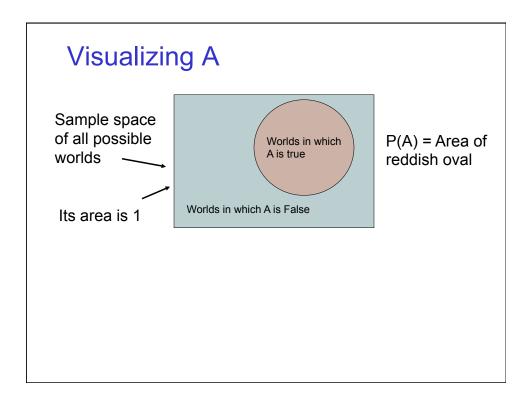
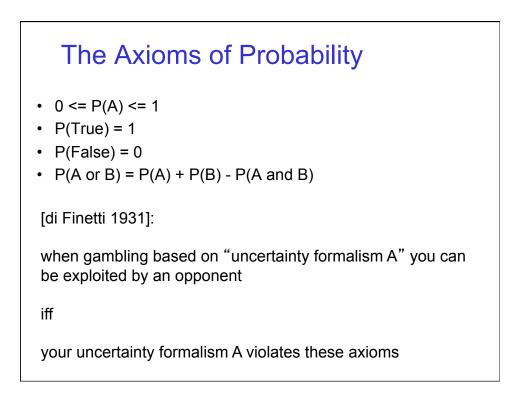
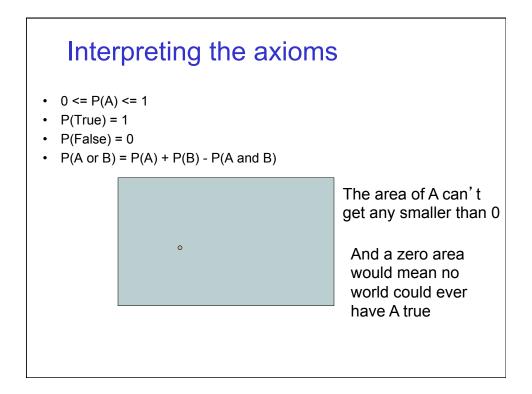


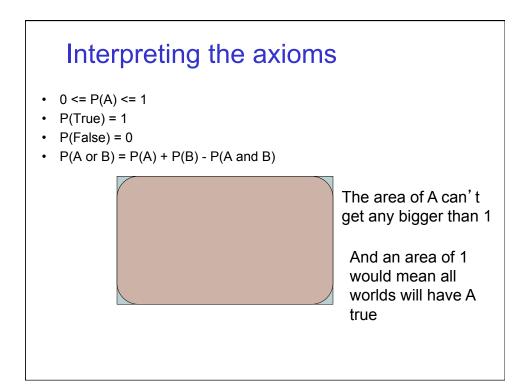
A little formalism

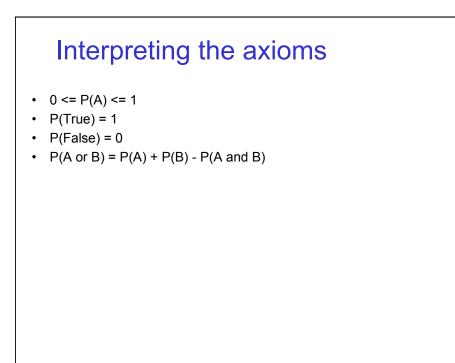
- a <u>sample space S</u> (e.g., set of students in our class)
 aka the set of possible worlds
- a <u>random variable</u> is a function defined over the sample space
 - Gender: S → { m, f }
 - Height: S → Reals
- an event is a subset of S
 - e.g., the subset of S for which Gender=f
 - e.g., the subset of S for which (Gender=m) AND (eyeColor=blue)
- · we're often interested in probabilities of specific events
- · and of specific events conditioned on other specific events

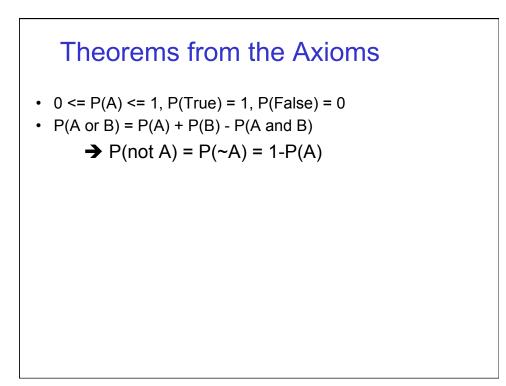


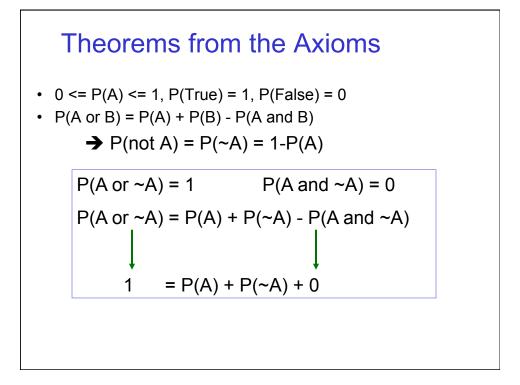


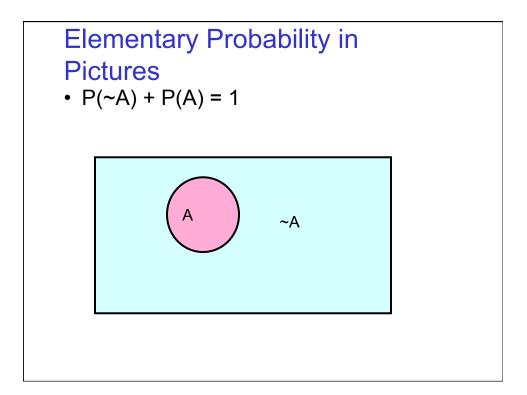


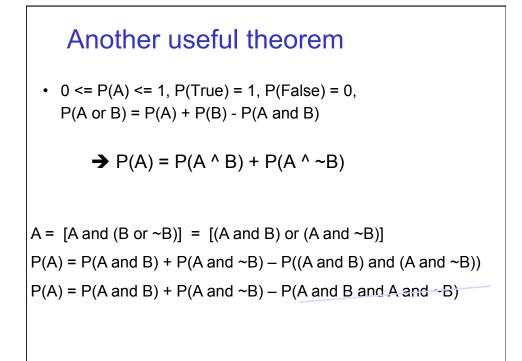


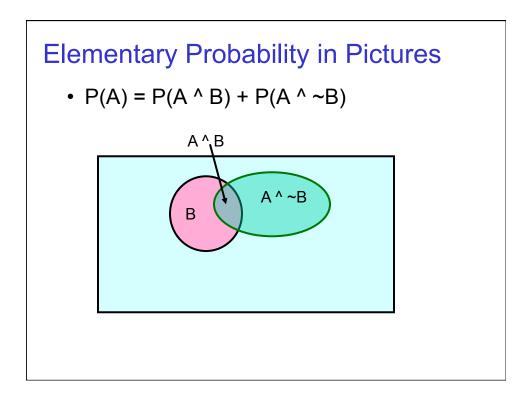












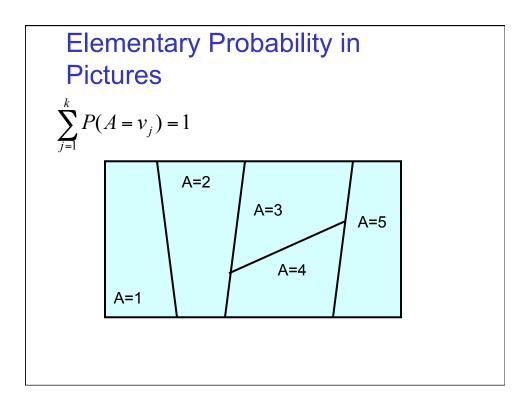
Multivalued Discrete Random Variables

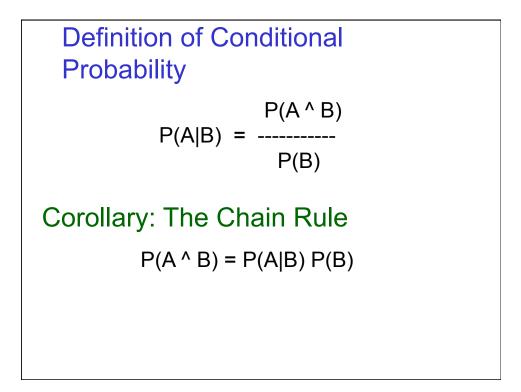
- Suppose A can take on more than 2 values
- A is a <u>random variable with arity k</u> if it can take on exactly one value out of {v₁, v₂, ... v_k}

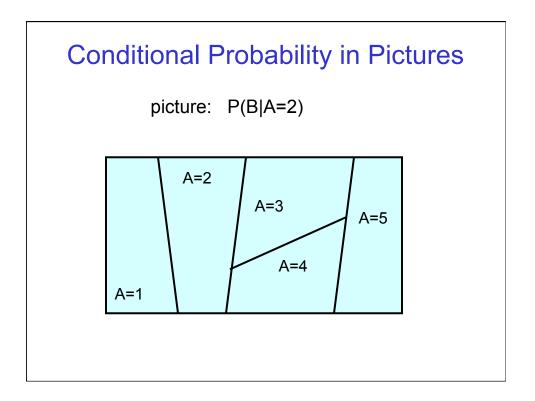
• Thus...

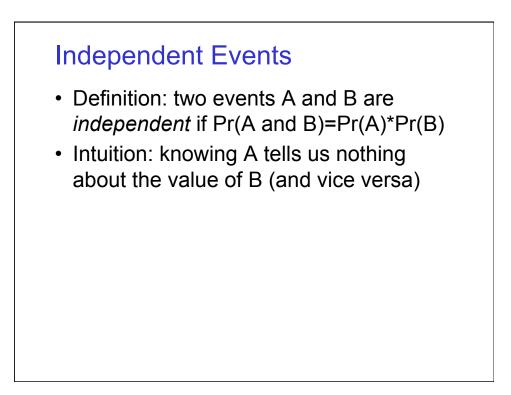
$$P(A = v_i \land A = v_j) = 0 \text{ if } i \neq j$$

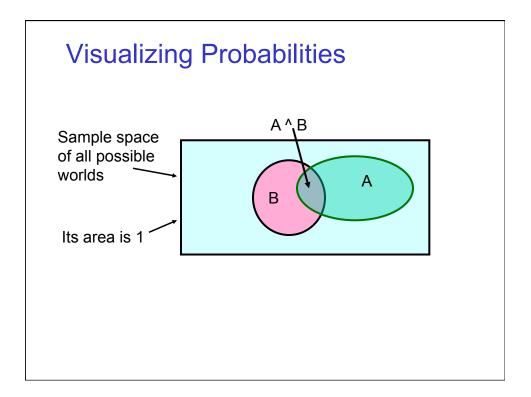
$$P(A = v_1 \lor A = v_2 \lor \dots \lor A = v_k) = 1$$

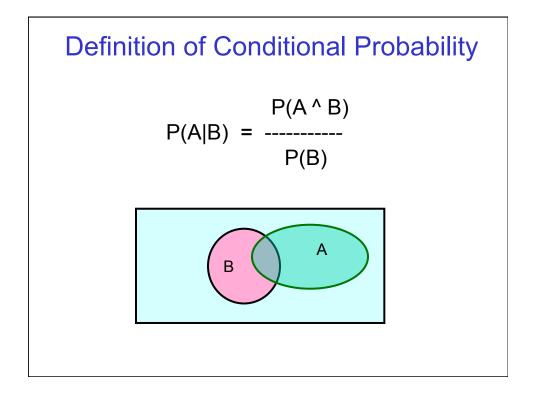


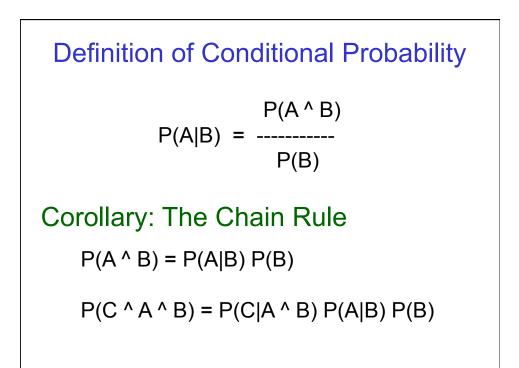


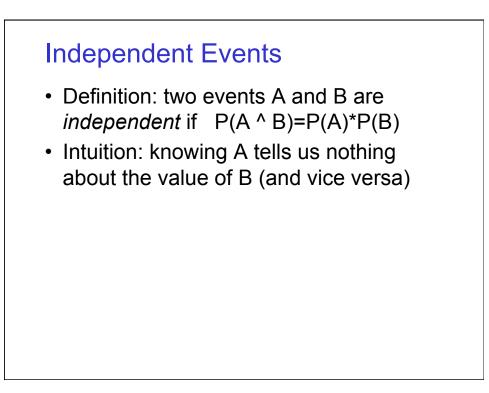


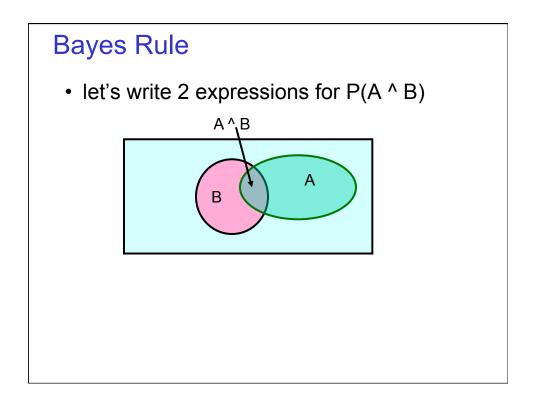


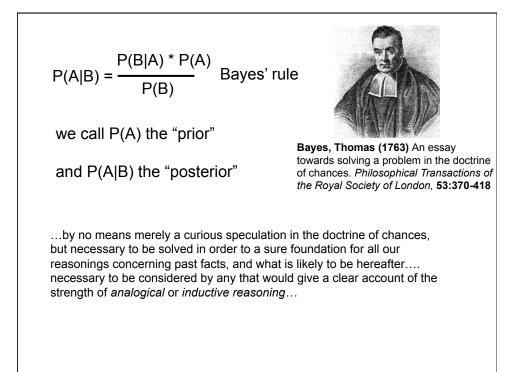


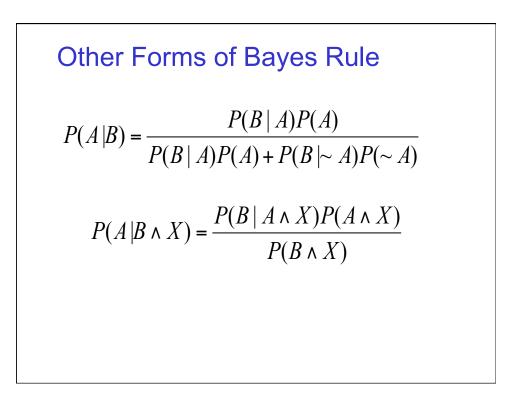


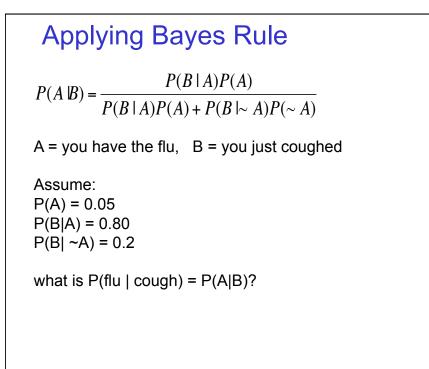


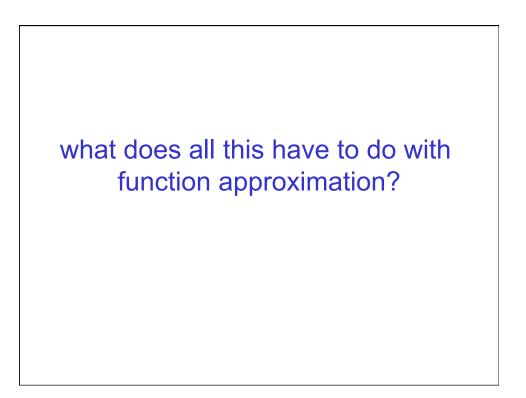


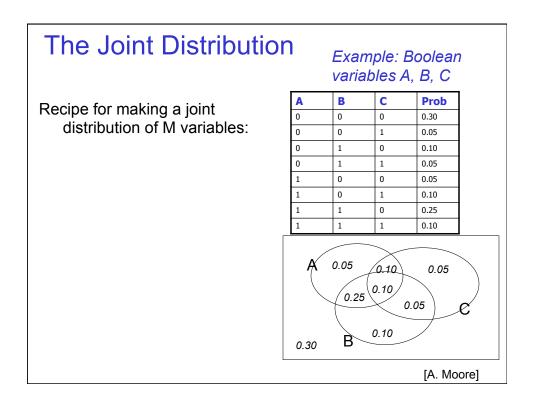


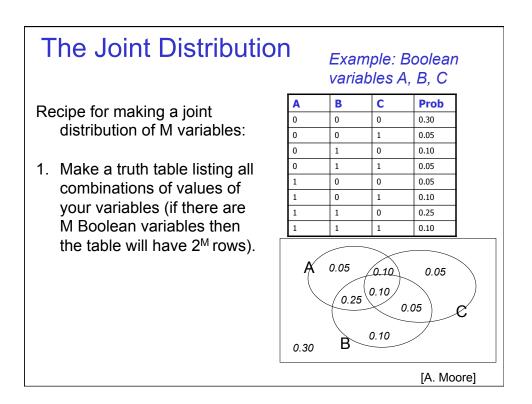


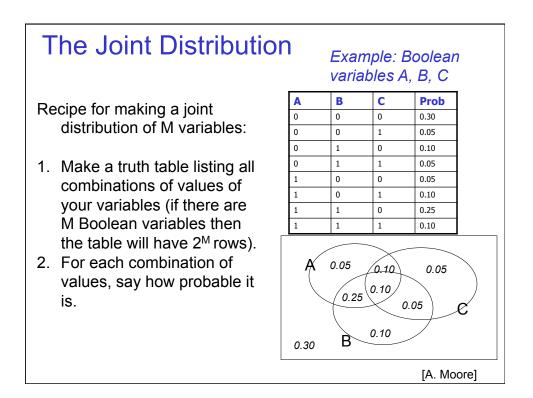


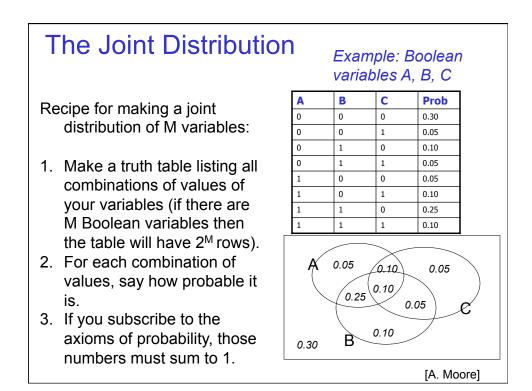


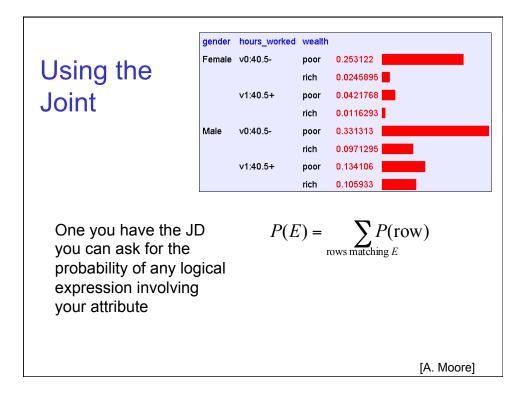


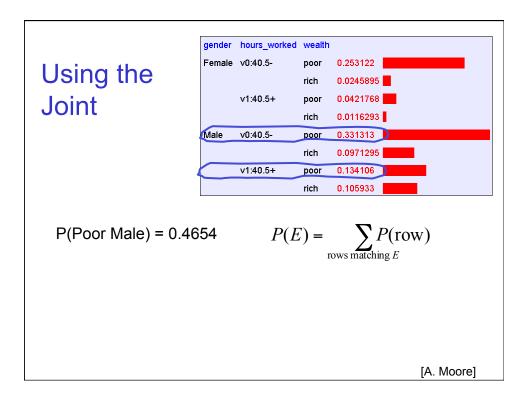


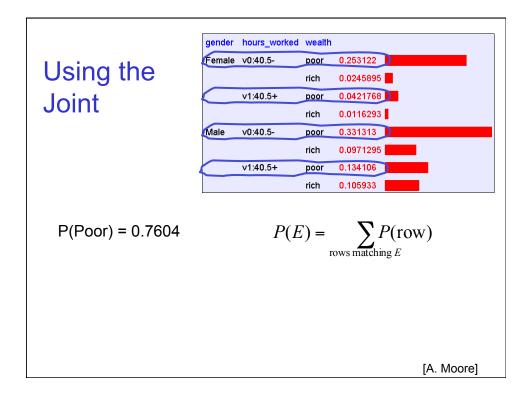


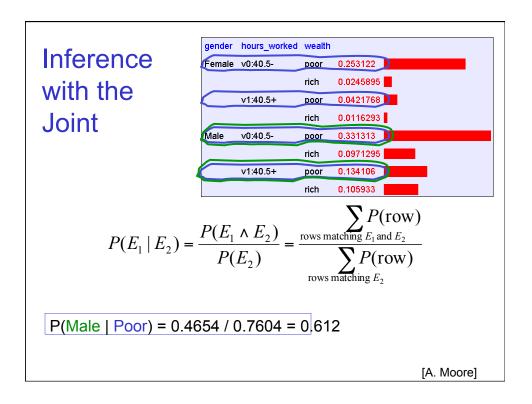


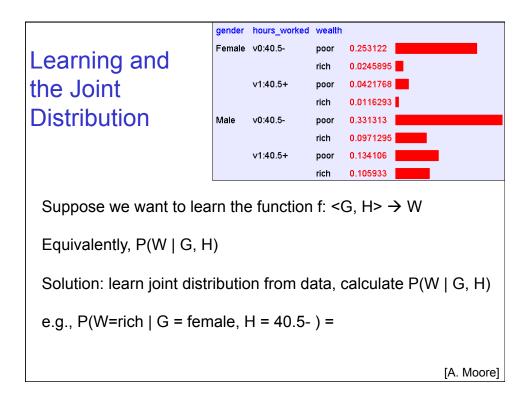


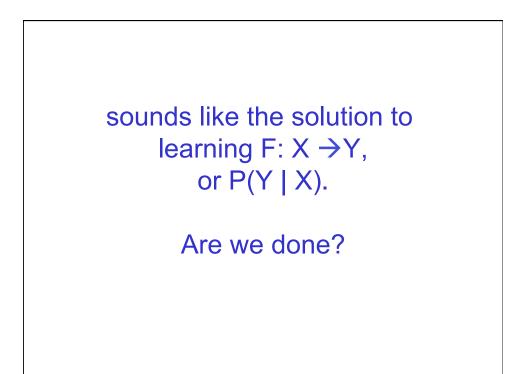


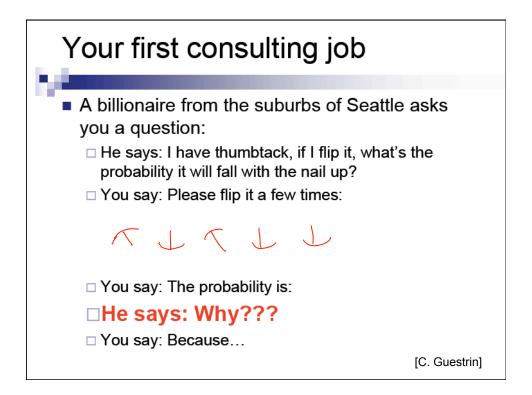


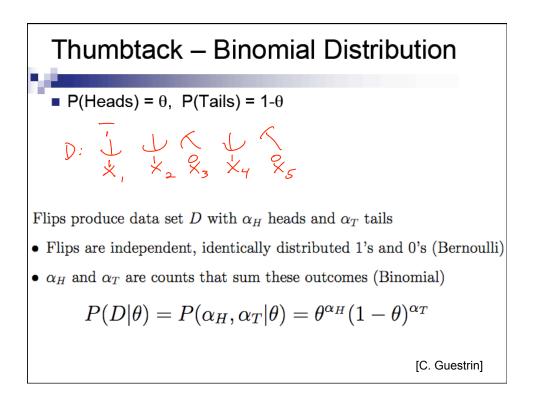


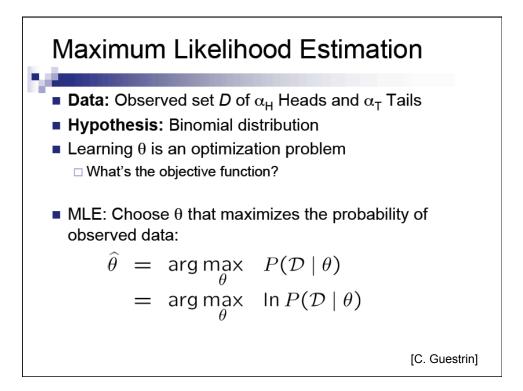


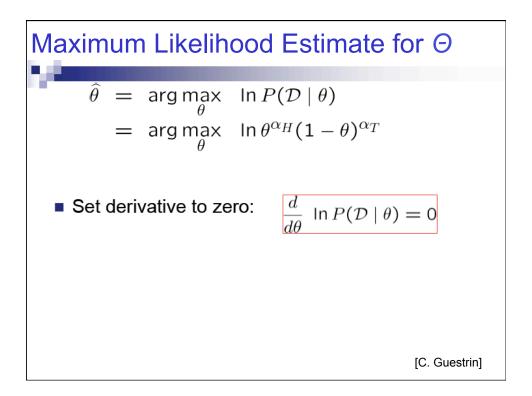


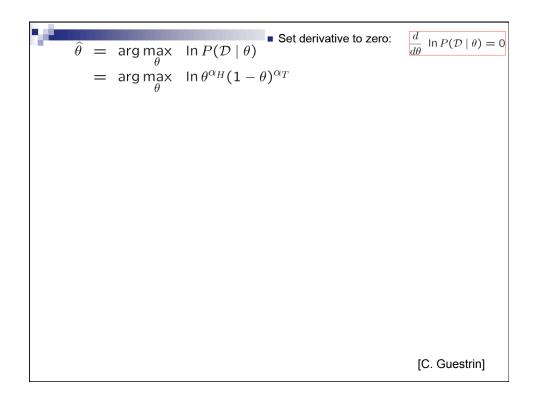


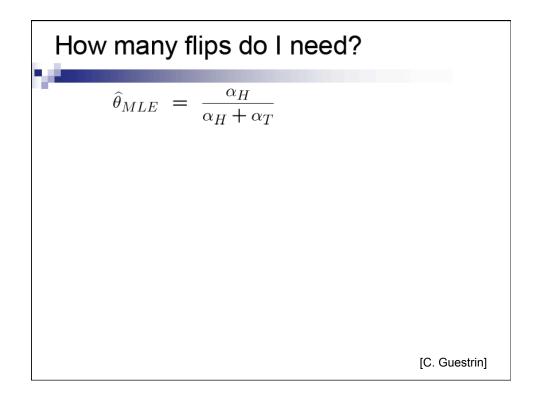


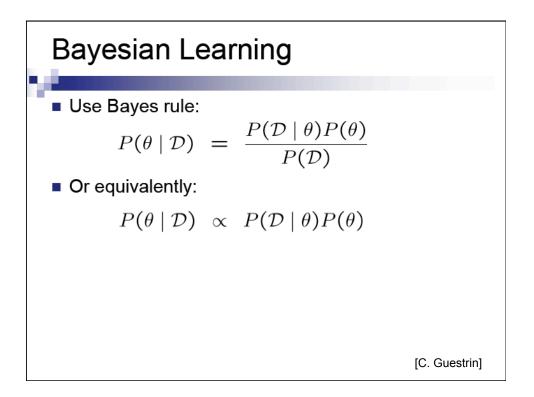


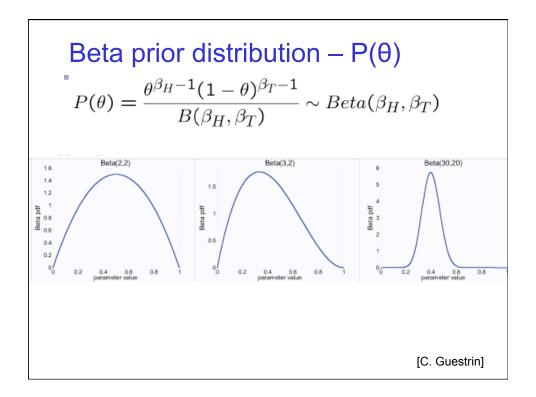


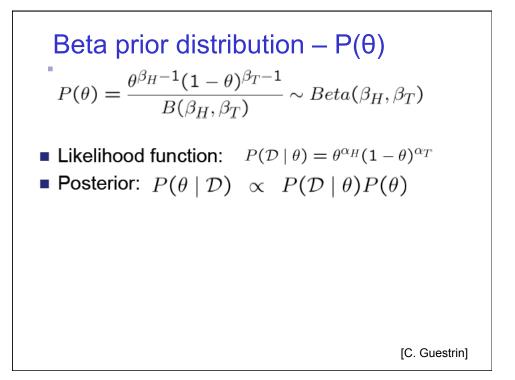


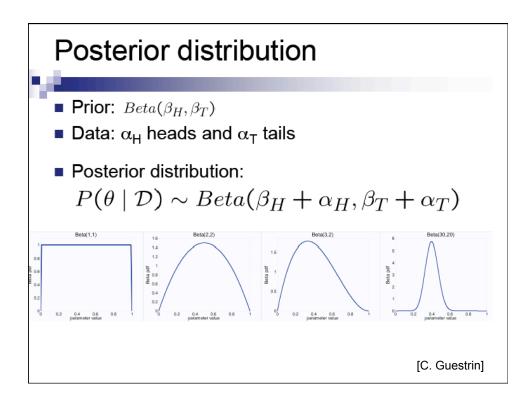


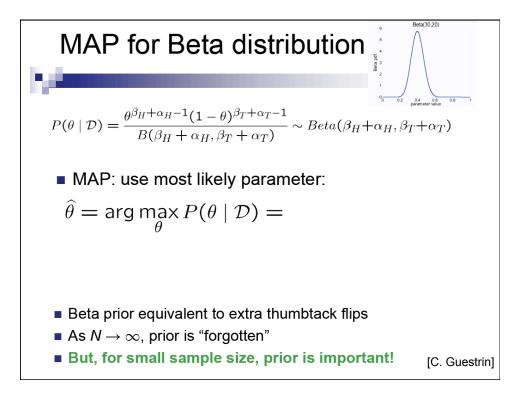


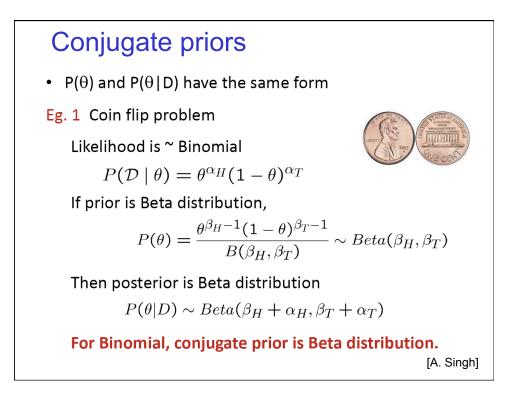


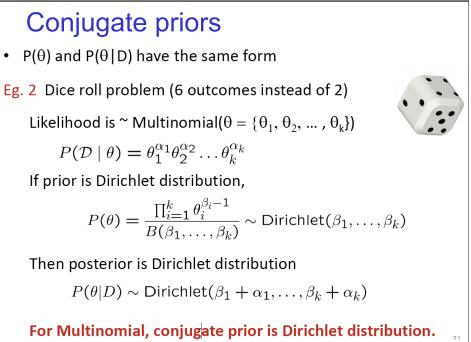




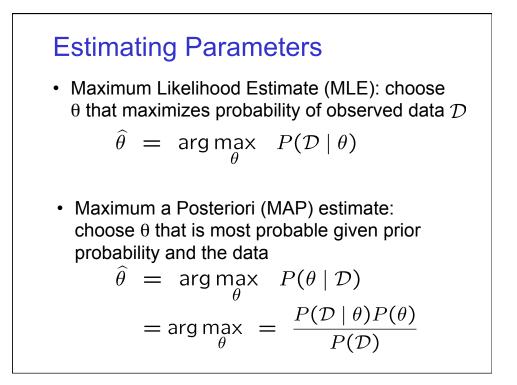


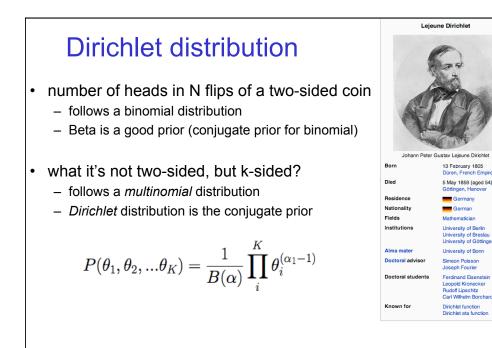






[A. Singh]





You should know

- Probability basics
 - random variables, events, sample space, conditional probs, ...
 - independence of random variables
 - Bayes rule
 - Joint probability distributions
 - calculating probabilities from the joint distribution
- Estimating parameters from data
 - maximum likelihood estimates (MLE)
 - maximum a posteriori estimates (MAP)
 - distributions binomial, Beta, Dirichlet, ...
 - conjugate priors



Expected values

Given discrete random variable X, the expected value of X, written E[X] is

$$E[X] = \sum_{x \in \mathcal{X}} x P(X = x)$$

We also can talk about the expected value of functions of \boldsymbol{X}

$$E[f(X)] = \sum_{x \in \mathcal{X}} f(x) P(X = x)$$

