EL5823/BE6203 Medical Imaging

Projection Radiography

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Based on J. L. Prince and J. M. Links, Medical Imaging Signals and Systems, and lecture notes by Prince. Figures are from the textbook.

Lecture Outline

- Instrumentation
 - X-ray tube configuration
 - Filtration and restriction of x-ray photons
 - Compensation and Scatter control
 - Film screen detector
- Image formation
 - Geometric effect
 - Extended source
 - Detector/film response
- Image quality
 - Contrast and SNR
 - Effect of noise and Compton scattering

Overview

• Systems:

- chest x-rays, mammography
- dental x-rays
- -fluoroscopy, angiography
- Properties
 - high resolution
 - low dose
 - broad coverage
 - short exposure time

Radiographic System



X-ray Tube





X-Ray Tube Components

- <u>Filament</u> controls tube current (mA)
- <u>Cathode</u> and <u>focussing cup</u>
- <u>Anode</u> is switched to high potential

- 30 - 150 kVp

- Made of tungsten
- Bremsstrahlung is 1%
- Heat is 99%
- Spins at 3,200–3,600 rpm
- Glass housing; vaccum

Exposure Control

- kVp applied for short duration
 - fixed timer (SCR), or
 - automatic exposure control (AEC), 5 mm
 thick ionization chamber triggers SCR
- Tube current mA controlled by
 - filament current, and
 - kVp Itube = 1-1000mA
- mA times exposure time yields mAs

mAs measures x-ray exposure

X-Ray Spectra



Bremsstrahlung

- Continuous spectrum of EM radiation is produced by abrupt deceleration of charged particles ("Bremsstrahlung" is German for "braking radiation").
- Deceleration is caused by deflection of electrons in the Coulomb field of the nuclei
- Most of the energy is converted into heat, ~0.5 % is x-ray
- The energy of the generated x-ray photon is given by energy conservation:
- The maximum energy for the produced photon is given by:



$$h\nu = K_e - K'_e$$

$$E_{p,\max} = h\nu = K_e = eV_{tube}$$

[From Graber, Lecture Note for BMI1-FS05]

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Bremsstrahlung intensity

• Overall Bremsstrahlung intensity *I*:

$$I \propto V_{tube}^2 I_{tube}$$

Electrical power consumption of tube: $P_{tube} = I_{tube} \times V_{tube}$ [W]

• The produced x-ray power P_x (in[W]) is given by:

$$P_x = k Z V_{tube}^2 I_{tube} = k Z V_{tube} P_{tube} = \eta P_{tube}$$

 $\eta = P_x / P_{tube} = kZ V_{tube}$: x-ray production efficiency

- Material constant $k = 1.1 \times 10^{-9}$ for Tungsten (Z=74).

[From Graber, Lecture Note for BMI1-FS05]

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Bremsstrahlung spectrum

• Theoretically, bremsstrahlung from a thick target creates a continuous spectrum from E = 0 to E_{max} with intensity I_b :

 $I_b(E) \sim Z(E_{\max} - E)$



- Actual spectrum deviates from ideal form due to
 - Absorption in window / gas envelope material and absorption in anode
 - Multienergetic electron beam



Characteristic radiation

- Narrow lines of intense x-ray at characteristic energies are superimposed on the continuous bremsstrahlung spectrum.
- Caused by removal of inner shell electrons and subsequent filling of hole with electrons from higher shell. The shell-energy difference determines the energy of characteristic rays
- Lines are named after the lower shell involved in the process; the upper shell involved is denoted by Greek letters:

 $\Delta n = 1 \rightarrow \alpha$ -transitions, $\Delta n = 2 \rightarrow \beta$ -transitions, ...



Different types of characteristics rays



From http://hyperphysics.phy-astr.gsu.edu/Hbase/quantum/xterm.html#c1

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X-ray spectra

- X-ray for general diagnostic radiology produced at 40 – 150 kVp
- Maximum photon energy: $E_p[\text{keV}] = hv_{\text{max}} = e \times \text{kVp}$
- Characteristic radiation occurs only for anode voltages



X-ray tube design

- Cathode w/ focusing cup, 2 filaments (different spot sizes)
- Anode
 - Tungsten, $Z_{\rm w} = 74$, $T_{\rm melt} = 2250 \ ^{\circ}{\rm C}$
 - Embedded in copper for heat dissipation
 - Angled (see next slide)
 - Rotating to divert heat





Filtration

- Low energy x-ray will be absorbed by the body, without providing diagnostic information
- Filtration: Process of absorbing low-energy x-ray photons before they enter the patient
 - \bullet Inherent filtration
 - Within anode
 - Glass housing
 - \bullet Added filtration
 - Aluminum
 - Copper/Aluminum
 - Note: Cu has 8keV characteristic xrays
 - Measured in mm Al/Eq

Restriction

• Goal: To direct beam toward desired anatomy



Compensation Filters



Contrast Agents

• Goal: To create contrast where otherwise



When the x-ray energy exceeds the Kedge (binding energy of K-shell), the mu coefficient is much higher, providing high contrast EL5823 Projection Radiography Yao Wang, NYU-Poly

- Iodine:
 - Can be synthesized into soluble compounds that are safely introduced through intravascular injection or ingestion
 - Used for imaging of
 - Blood vessels, heart chambers, tumors, infections
 - Kidneys, bladder
 - Naturally exist in thyroid, and hence X-ray is very good for thyroid imaging
- Barium
 - Administered as a "chalky milkshake"
 - Used in the gastrointestinal tract,
 - Stomach, bowel
- Air
 - Does not absorb x-ray
 - "opposite" type of contrast
 - By Inflating the lungs, air provides contrast for lung tissues

Scatter Control

- Ideal x-ray path: <u>a line!</u>
- Compton scattering causes blurring
- How to reduce scatter?
 - airgap
 - scanning slit
 - grid

Grids



grid ratio
$$=\frac{h}{b}$$

• 6:1 to 16:1 (radiography) or 2:1 (mammo)

Problem with Grids

Radiation is absorbed by grid
 grid conversion factor

$$GCF = \frac{mAs w/grid}{mAs w/o grid}$$

- Typical range 3 < GCF < 8
- Grid visible on x-ray film
 - move grid during exposure
 - linear or circular motion

Film-Screen Detector



- Phosphor = calcium tungstate
- Flash of light lasts 1×10^{-10} second
- ~1,000 light photons per 50 keV x-ray photon

Radiographic Cassette



Digital Radiology

- Replace the intensifying screen/X-ray film by
 - flat panel detectors (FPD) using thin-film transistor (TFT) arrays
 - A scintillator
 - Consisting of many thin, rod-shaped cesium iodide (CsI) crystals
- When an X-ray is absorbed in a CsI rod, the CsI scintillates and produces light
- The light is converted into an electrical signal by a photodiode in the TFT array
- The electrical signal is amplified and converted to a digital value using an A/D converter
- A typical commercial DR system has flat panel dimensions of 41x41 cm, with an TFT array of 2048x2048 elements
- Ref: Webb, Introduction to biomedical imaging, Sec. 1.5.5

Biological effects of ionizing radiation

- Damage depends on deposited (= absorbed) energy (intensity × time) per tissue volume
- Threshold: No minimum level is known, above which damage occurs
- Exposure time: Because of recovery, a given dose is less harmful if divided
- Exposed area: The larger the exposed area the greater the damage (collimators, shields!)
- Variation in Species / Individuals: LD 50/30 (lethal for 50% of a population over 30 days, humans ~450 rads / whole body irradiation)
- Variation in cell sensitivity: Most sensitive are nonspecialized, rapidly dividing cells (Most sensitive: White blood cells, red blood cells, epithelial cells. Less sensitive: Muscle, nerve cells)
- Short/long term effects: Short term effects for unusually large (> 100 rad) doses (nausea, vomiting, fever, shock, death); long term effects (carcinogenic/genetic effects) even for diagnostic levels ⇒ maximum allowable dose 5 R/yr and 0.2 R/working day [Nat. Counc. on Rad. Prot. and Meas.]

Image Formation

- Basic imaging equation
- Geometric effects
- Extended source
- Film blurring
- Impact of noise and scattering

Basic Imaging Equations



Example



1) What is the local contrast of the blood vessel?

2) What is the local contrast of the blood vessel when contrast agent is injected?

2 w/o contrast :

$$I_{b} = I_{\min} = I_{0}e^{-(0.4*2.0)};$$

$$I_{o} = I_{\max} = I_{0}e^{-(0.4*1.5+0.2*0.5)}$$
Local contrast : $C_{1} = \frac{I_{0} - I_{b}}{I_{b}};$
Global contrast : $C = \frac{I_{\max} - I_{\min}}{I_{\max} + I_{\min}}$
w/ contrast :

$$I_{b} = I_{\max} = I_{0}e^{-(0.4*2.0)};$$

$$I_{o} = I_{\min} = I_{0}e^{-(0.4*1.5+20*0.5)}$$
Local contrast : $C_{1} = \frac{|I_{0} - I_{b}|}{I_{b}};$
Global contrast : $C = \frac{I_{\max} - I_{\min}}{I_{\max} + I_{\min}}$

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Geometric Effects

- X-rays are diverging from source
- Undesirable effects:
 - $-\cos^3\theta$ falloff across detector
 - anode heel effect
 - pathlength irregularities
 - magnification
- I_0 is intensity at (0,0)
- r is distance from (x, y) to x-ray origin
- θ is angle between (0,0) and (x,y)

Inverse Square Law

• Net flux of photons decrease as $1/r^2$. Therefore

$$I_0 = \frac{I_S}{4\pi d^2} \qquad I_r = \frac{I_S}{4\pi r^2}$$

• Eliminate source intensity I_S

$$I_r = I_0 \frac{d^2}{r^2}$$

• Since $\cos \theta = d/r$

$$I_r = I_0 \cos^2 \theta$$

I_0 is the detected flux at the origin of the detector plane I_r is the detected flux at an arbitrary point of the detector plane with angle θ w/o considering the oblique effect discussed in the next page

Obliquity



Overall Effect of Beam Divergence

• Inverse square law and obliquity combine

$$I_d(x_d, y_d) = I_0 \cos^3 \theta$$

- <u>Can usually be ignored</u>. Why?
 - Detector is far away
 - Field of view (FOV) is often small

$\neg \theta$ is small

Anode Heel Effect

- Intensity within the x-ray cone
 - Not uniform
 - stronger in the cathode direction
 - 45% variation is typical
- Compensate, use to advantage, or ignoreWe will ignore in math

Imaging of a Uniform Slab

• Uniform slab yields different intensities



• Intensity on detector

$$I_d(x, y) = I_0 \exp\{-\mu L / \cos \theta\}$$

• Including inverse square law and obliquity:

$$I_d(x, y) = I_i \cos^3 \theta \exp\{-\mu L / \cos \theta\}$$

• If $d \approx r$ all effects can be ignored

I_i = I_s/ (4 \pi d^2)

Illustrate the received intensity as function of y or x or \theta

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Received Signal as a Function of Theta



Theta in Degree

This plot assumes mu*L=1, e.g. mu=1/cm, L=1cm.

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- How does it vary as a function of Y when x=0 (vertical axis of the detector plain)?
- cos(q) = d/r=d/sqrt(d^2+y^2)/
- Assuming d=5m, y= -10cm to 10cm (q from 0 to 1.14 degree)
- Vary small relative change in the range of y



intensity as function of y

Example: Image of a prism due to a point source

Consider the x-ray imaging of a cube. Determine the intensity of detected photons along the y axis on the detector plane. Express your solution in terms of the angle q. Sketch this function. You should consider the inverse square law and the oblique effect. Assume the x-ray source is an ideal point source with intensity *I0*, and the object has a constant linear attenuation coefficient m. (Example 5.4 in textbook)



Solution

Sketch over in class. Also see textbook Must consider different regions separately

Objects Magnification

• Size on detector depends on distance from source



Imaging of a Thin Non-Uniform Slab

- Assume a very thin slab at z
 - the linear absorption coefficient at (x',y') is $\mu(x',y')$
 - Detector position (x,y) -> slab position (x',y')



• Let "transmittivity" be $t_z(x, y) = \exp\{-\mu(x, y)\Delta z\}$

• On detector, intensity is

$$I_d(x,y) = I_0 \cos^3 \theta \, t_z \left(\frac{x}{M(z)}, \frac{y}{M(z)}\right)$$

• After substitution

$$I_d(x,y) = I_0 \left(\frac{d}{\sqrt{d^2 + x^2 + y^2}}\right)^3 t_z \left(\frac{xz}{d}, \frac{yz}{d}\right)$$

$$I_0 = I_0 \left(\frac{d}{\sqrt{d^2 + x^2 + y^2}}\right)^3 t_z \left(\frac{xz}{d}, \frac{yz}{d}\right)$$

Blurring Due to Extended Source



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Image of source through a pinhole



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Image of an Arbitrary Slice

- An arbitrary slab at z can be thought of as many pinholes at different locations (x',y'), each with transmittivity t_z(x',y')
 - The received signal due to transmitivity at (x',y') can be written as h(x-x',y-y') t_z(x',y') assuming the system is translation invariant
- The image of the slab is a sum of individual images of the source through all the pinholes multiplied by the respective transmittivity
 - $I_d(x,y) = \inf_{x',y'} h(x-x',y-y') tz(x',y') dx' dy'$
- The overall effect can be captured through linear conv $I_d(x, y) = \frac{\cos^3 \theta}{4\pi d^2 m^2} t_z \left(\frac{x}{M}, \frac{y}{M}\right) * s\left(\frac{x}{m}, \frac{y}{m}\right)$

Note: m depends on z, distance of slab to the source

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Example

- Source is a circular disk with diameter D
- Object is square plane with dimension W at distance z
- Detector plane at distance d from source
- How does the detected image look for d=2Z and d=3Z
- Note that the blurring of the edge depends on z
- What is t_z(x,y) and s(x,y)?
- What is I_d(x,y)?
- How is I_d(x,y) related with t_z(x,y)?
- How does the image of I_d(x,y) look?

Example: solution

Tz(x,y): a square with width W S(x,y): a disk with diameter D. Assuming D << W,

For d=2z, M=d/z=2, m=1-M=-1

Tz(x/M,y/M): a square with width 2W S(x/m,y/m): a disk with diameter D The resulting detector image is a square with width 2W but with a blurred edge with blurring width D

• For d=3z, M=d/Z=3, m=1-M=-2

Tz(x/M,y/M): a square with width 3W S(x/m,y/m): a disk with diameter 2D The resulting detector image is a square with width 3W but with a blurred edge with blurring width 2D



For the previous example, L is very small, but the source has diameter D, blurring is due to the source diameter being non-zero

Film Screen Blurring



A single x-ray photon causes a blurry spot on the film which is effectively the "impulse response" to the x-ray impulse h(x,y)

Typical MTF for a filmscreen detector



Overall Imaging Equation

 Including all effects (geometric, extended source, film-screen blurring), the image corresponding to a slab at z with transmittivity function t_z(x,y) is

$$I_d(x,y) = \cos^3 \theta \frac{1}{4\pi d^2 m^2} s\left(\frac{x}{m}, \frac{y}{m}\right)$$
$$* t_z\left(\frac{x}{M}, \frac{y}{M}\right) * h(x,y)$$

- For an object with a certain thickness, the transmittivity function must be modified to reflect the overall attenuation along the z-axis
- When the source is polyenergetic, integration over photon energy is additionally needed

Example

 In the previous example, how would the image look if the film blurring is a box function of width h?

Film Characteristics

 Film darkening (after development) depends on incident light (which depends on the incident x-ray)

Т

Optical density

$$D = \log_{10} \frac{I_i}{I_t}$$

- \bullet Usable densities 0.25 < D < 2.25
- Best densities 1.0 < D < 1.5

Optical Density vs. Exposure

• X-ray exposure yields optical density

$$D = \Gamma \log_{10} \frac{X}{X_0}$$

- Γ is <u>film gamma</u>
- Typical ranges: $0.5 < \Gamma < 3.0$
- <u>Latitude</u> is range exposures where relationship is linear
- \underline{Speed} is inverse of exposure at which

$$D = 1 + \text{ fog level}$$

The H&D Curve



Effect of Noise

- Source of noise:
 - Detector does not faithfully reproduce the incident intensity
 - X-rays arrive in discrete packets of energy. This discrete nature can lead to fluctuations in the image
 - Local contrast

$$C = \frac{I_t - I_b}{I_b}$$

- Signal is $I_t I_b$
- Noise is due to Poisson behavior
- Variance of noise in background: σ_b^2
- Signal to noise

$$SNR = \frac{I_t - I_b}{\sigma_b} = \frac{CI_b}{\sigma_b}$$



How is noise related to signal?

- Assuming the number of photons in each burst follows the Poisson distribution
 - P(N=k)= (a^k / k!) e^{-a}
 - Variance = mean = a
- Let N_b denotes the average number of photons per burst per area
- Let hv denotes the effective energy for the X-ray source
- The average background intensity is
- The variance of photon intensity is

$$I_b = \frac{N_b h\nu}{A\Delta t}$$
$$\sigma_b^2 = N_b \left(\frac{h\nu}{A\Delta t}\right)^2$$

If X is an RV with mean η_x , variance σ_x^2

Y = aX is a RV with mean $\eta_y = a\eta_x$, variance $\sigma_y^2 = a^2 \sigma_x^2$

• The SNR is $SNR = C\sqrt{N_b}$

- SNR can be improved by
 - Increasing incident photon count
 - Improving contrast

Detective Quantum Efficiency

- How good is a detector?
- Consider:
 - Potential SNR before detection
 - Actual SNR upon detection
- <u>Detective Quantum Efficiency</u>

$$\mathrm{DQE} = \left(\frac{\mathrm{SNR}_{\mathrm{out}}}{\mathrm{SNR}_{\mathrm{in}}}\right)^2$$

• Degradation of SNR during detection

When a x-ray source has mean intensity m=N_b, and variance s^2=N_b, SNR =m/s=\sqrt(N_b)

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Example

- Suppose an X-ray tube is set up to fire bursts of photons each with N=10000 photons and the detector's output (# of detected photons per burst) x has a mean =8000, variance=40000. What is its DQE?
- Solution:

The actual # of photons fired at the x - ray tube follows the Poisson process (mean = variance = 10000) $SNR_{in} = \frac{mean}{\sqrt{variance}} = \sqrt{10000} = 100$ The #of detected photons has mean = 8000, variance = 40000 $SNR_{out} = \frac{mean}{\sqrt{variance}} = \frac{8000}{\sqrt{40000}} = \frac{8000}{200} = 40$ $DQE = \left(\frac{SNR_{out}}{SNR_{in}}\right)^2 = 0.16$

This means that only about 16% of photons are detected correctly

Effect of Compton Scattering

- Compton scattering causes the incident photons to be deflected from their straight line path
 - Add a constant intensity I_s in both target and background intensity ("fog")
 - Decrease in image contrast
 - Decrease in SNR

W/ scattering : target intensity : $I_t + I_s$ background intensity : $I_b + I_s$ contrast $C' = \frac{I_t - I_b}{I_b + I_s} = \frac{I_b}{I_b + I_s} C = \frac{C}{1 + \frac{I_s}{I_b}}$ SNR' = $C \frac{I_b}{\sigma_b} = C \frac{N_b}{\sqrt{N_b + N_s}} = C \frac{\sqrt{N_b}}{\sqrt{1 + N_s / N_b}} = \text{SNR} \frac{1}{\sqrt{1 + I_s / I_b}}$

background intensity :
$$I_b$$

contrast $C = \frac{I_t - I_b}{I_b}$
SNR = $C \frac{I_b}{\sigma_b} = C \sqrt{N_b}$

W/o scattering :

target intensity : I_{t}

Medical Applications

- Orthopedic
- Chest
- Abdomen
- Mammography
- Angiography



Mammography

- Detection and diagnosis (symptomatic and screening) of breast cancer
- Pre-surgical localization of suspicious areas
- Guidance of needle biopsies.
- Breast cancer is detected on the basis of four types of signs on the mammogram:
 - Characteristic morphology of a tumor mass
 - Presentation of mineral deposits called microcalcifications
 - Architectural distortions of normal tissue patterns
 - Asymmetry between corresponding regions of images on the left and right breast
- \Rightarrow Need for good image contrast of various tissue types.
- Simple x-ray shadowgram from a quasi-point source.



Mammography contrast

- Image contrast is due to varying linear attenuation coefficient of different types of tissue in the breast (adipose tissue (fat), fibroglandular, tumor).
- Ideal energy distribution of X-ray should be below 20 for average size breast, slightly higher for denser breast



Mammography source

- Voltage ~ 25-30 kVp
- Anode material Mo (Molybdenum), Rh (Rhodium) (characteristic peaks at 17.9 and 19 for Mo, and slightly higher for Rh)
- Filtering: use Mo or Rh to absorb energy above 20 or 25Kev



Anti-scatter grid

- Significant Compton interaction for low E_p (37-50% of all photons).
- Linear grid: Lead septa + interspace material. Septa focused toward source. Grid ratio ~ 3.5-5:1. Only scatter correction in one dimension. Scatter-toprimary (SPR) reduction factor ~5
- Recently crossed grid introduced
- Grids are moved during exposure
- Longer exposure



X-ray projection angiography

- Imaging the circulatory system. Contrast agent: Iodine (Z=53) compound; maximum iodine concentration ~ 350 mg/cm³
- Monitoring of therapeutic manipulations (angioplasty, atherectomy, intraluminal stents, catheter placement).
- Short intense x-ray pulses to produce clear images of moving vessels. Pulse duration: 5-10 ms for cardiac studies ...100-200 ms for cerebral studies



Summary

- Projection radiography system consists of an x-ray tube, devices for beam filtration and restriction, compensation filters, grids, and a filmscreen detector (or digital detector, filmless)
- The detector reading (or image gray level) is proportional to the number of unabsorbed x-ray photons arriving at the detector, which depends on the overall attenuation in the path from the source to the detector
- The above relation must be modified to take into account of inverse square law, obliquity, anode heel effect, extended source and detector impulse response
- The degree of film darkening is nonlinearly related to the film exposure (detected x-ray) by the H&D curve
- Both detector noise and Compton scattering reduce contrast and SNR of the formed image

Reference

- Prince and Links, Medical Imaging Signals and Systems, Chap 5.
- Webb, Introduction to biomedical imaging, Chap 1.

Homework

- Reading:
 - Prince and Links, Medical Imaging Signals and Systems, Chap 5.
- Note down all the corrections for Ch. 5 on your copy of the textbook based on the provided errata.
- Problems for Chap 5 of the text book:
 - P5.2
 - P5.4
 - P5.5
 - P5.8
 - P5.18
 - P5.19
 - correction: the sentence "Suppose a 5 cm ..." in Part (a) should be moved to the beginning of part (b). Also, intrinsic contrast in part (b)= (μ_t-μ_b)/(μ_t+μ_b), contrast in part (c)= (I_{max}-I_{min})/(I_{max}+I_{min}).
 - P5.22

Homework (added problem)

1. Consider the x-ray imaging of a two-layer slab, illustrated below. Determine the intensity of detected photons along the *y* axis on the detector plane. Express your solution in terms of the y-coordinate Sketch this function. You should consider the inverse square law and the oblique effect. Assume the x-ray source is an ideal point source with intensity *I0*. For simplicity, assume the slab is infinitely long in the *y* direction.

