RADIATION PHYSICS FOR PERSONNEL AND ENVIRONMENTAL PROTECTION

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J. Donald Cossairt Fermi National Accelerator Laboratory



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PREFACE

The advancement of particle accelerators is now well into its ninth decade, or second century if Röntgen's x-ray tube is properly considered to be a particle accelerator. This field of human endeavor has achieved maturity but not stagnation. Accelerators now pervade nearly every facet of both modern scientific research and everyday life. They are utilized in virtually all branches of science ranging from the frontiers of particle and nuclear physics to engineering, chemistry, biology, geology, and the environmental sciences. Very important practical applications of accelerators are now found in many industrial applications and even in agriculture. The prominent and longstanding contribution to medicine is well-known as community hospitals of moderate size now utilize accelerators extensively. Indeed, particle accelerators are by far the type of "radiological" installation most commonly encountered by members of the public. The historical development of accelerator radiation physics has accompanied that of the machines themselves and has been well described by Patterson and Thomas (Pa94). A stated goal of the U.S. Particle Accelerator School (USPAS) is to provide "quality education in beam physics and associated accelerator technology". It is therefore quite proper that the USPAS continues to include a course on accelerator radiation physics in its curriculum. Those who develop, operate, and utilize the accelerators of the future will be able to do this far more effectively if the associated radiological hazards are better understood and mitigated. To that end, the content of this textbook has been selected and developed. The intent is to address the major elements of radiation physics issues that are encountered at accelerators of all particle types and energies. To do this, some topics not commonly thought to be within the domain of "health physics" such as charged particle optics, synchrotron radiation, hydrogeology, and meteorology are included along with the more familiar subjects that might be anticipated by the readers. The problem sets supplied with most of the chapters were developed to promote better understanding of the contents.

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1.1 Introduction

In this chapter, our discussion begins by reviewing the standard terminology of radiation physics. The most important physical and radiological quantities and the system of units by which they are measured are introduced. Due to its importance at most accelerators, the results of the special theory of relativity are reviewed. The energy loss by ionization and the multiple Coulomb scattering of charged particles is also summarized.

1.2 Review of Units, Terminology, Physical Constants, and Material Properties

1.2.1 Radiation Physics Terminology and Units

In order to develop an understanding of accelerator radiation physics, it is necessary to introduce the prominent quantities of importance and the units by which they are measured that are commonly used in accelerator radiation protection. Over the years various systems of units have been employed. Presently, there is a slow migration toward the use of the *Système Internationale* (SI) units. However, the practitioner needs to understand the interconnections of all of the units, both "customary" and SI, due to the diversity of usage found in the scientific literature and in government regulations, particularly in the U.S.

- **energy:** The unit of energy in common use when dealing with energetic particles is the **electron volt** (eV). 1 eV is equal to 1.602 x 10⁻¹² ergs or 1.602 x 10⁻¹⁹ Joules. Multiples of these units in common use at accelerators are the keV (10³ eV), MeV (10⁶ eV), GeV (10⁹ eV), and TeV (10¹² eV). In the scientific literature, particle energies are almost always measured in these energy units rather than in the SI equivalent (i.e., Joules). Also, nearly always, the "energy" of an accelerated particle refers to the **kinetic energy** (see section 1.3).
- **absorbed dose:** Absorbed dose is the energy absorbed per unit mass of material. It is usually denoted by the symbol *D*. The customary unit of absorbed dose is the **rad** while the *Système Internationale* (SI) unit of absorbed dose is the **Gray**. 1 rad is defined to be 100 ergs gram⁻¹ or 6.24×10^{13} eV g⁻¹. One Gray (Gy) is defined to be 1 J kg⁻¹ and is thus 100 rads. A Gray, then, is equal to 6.24×10^{15} eV g⁻¹. The concept of absorbed dose can be applied to any material. Thus it is commonly used to quantify both radiation exposures to human beings and the delivery of energy to materials and accelerator components where radiation damage is a consideration.
- **dose equivalent:** This quantity has the same physical dimensions as absorbed dose. It is used to take into account the fact that different particle types have biological effects which are enhanced, per given absorbed dose, over those due to the standard reference particles which are 200 keV photons. It is usually denoted by the symbol *H*. The customary unit is the **rem** while the SI unit is the **Sievert** (Sv). One Sievert is equal to 100 rem. The concept of dose equivalent is relevant only to radiation exposures received by human beings. In recent years, variants of this quantity have been introduced such as "dose equivalent index" and "equivalent dose". For the most part this text will ignore such subtleties.

quality factor: This factor takes into account the relative enhancement in biological effects of various types of ionizing radiation. It is usually denoted by Q, and is used to connect H with D through the following equation:

$$H = QD. \tag{1.1}$$

Thus, H (rem) = QD (rads) or H (Sv) = QD (Gy). Q is dependent on both particle type and energy and, thus, for any radiation field its value is an average over all components. It is formally defined to have a value of unity for 200 keV photons. Qranges from unity for photons, electrons of most energies, and high energy muons to a value as large as 20 for α -particles (i.e.,⁴He nuclei) of a few MeV in kinetic energy. For neutrons, Q ranges from 2 to greater than 10. Although recent guidance by the International Council on Radiation Protection (ICRP) has recommended increased values of Q for neutrons (IC91), these increased values have yet to be adopted by regulatory authorities in the United States. Q is presently defined to be a function of **linear energy transfer** (LET), *L*. LET, approximately, is equivalent to **stopping power**, or rate of energy loss for charged particles and is conventionally expressed in units of keV μ m⁻¹ (see Section 1.4). All ionizing radiation ultimately manifests itself through charged particles so LET is, plausibly, a good measure of localized radiation damage.

The value of Q commonly used is an average over the spectrum of LET present, weighted by the absorbed dose as a function of LET, D(L);

$$\left\langle Q\right\rangle = \frac{\int_0^\infty dL Q(L) D(L)}{\int_0^\infty dL D(L)}.$$
(1.2)

Figures 1.1, 1.2, and 1.3 give the relationships between Q and LET and Q as a function of particle energy for a variety of particles and energies. The results shown in Fig. 1.2 are based upon ionization due to the *primary* particles only. For particles subject to the strong (or nuclear) interaction, the inclusion of *secondary* particles produced at higher energies will result in increased values of Q as a function of energy. For example for protons Q rises to a value of 1.6 at 400 MeV and a value of 2.2 at 2000 MeV (Pa73) with secondary particles included. The subject of relating operationally useful values of Q to the existing knowledge of radiobiological effects is a complex one, discussed at length elsewhere (NC90). In general, it is preferred to use the dose equivalent per fluence conversion factors discussed below.



Fig. 1.1 Quality Factor, *Q*, of charged particles as a function of collision stopping power (LET) in water as recommended by the ICRP in Publication 21 (IC73) and later as revised in Report 60 (IC91).



Fig. 1.2 Quality factors, Q, of several types of charged particles as a function of energy, as recommended by the ICRP. [Adapted from (IC73)].



Fig. 1.3 Effective quality factor, Q, for neutrons as a function of neutron kinetic energy. This is the maximum dose equivalent divided by the absorbed dose where the maximum dose equivalent occurs (IC73) in human tissue. [Adapted from (Pa73).]

flux density: The number of particles that traverse a unit area in unit time. This quantity is generally denoted by the symbol ϕ ;

$$\phi = \frac{d^2 n}{dAdt},\tag{1.3}$$

where d^2n is the differential number of particles traversing surface area element dA during time dt. For radiation fields where the constituent particles move in a multitude of directions, ϕ is the number of transversals of a sphere having a cross-sectional area dA per unit area per unit time. The units of flux density are commonly cm⁻²s⁻¹ (customary) and m⁻²s⁻¹ (SI).

fluence: This quantity, denoted by Φ , is simply the integral over some time interval, $t_i < t < t_f$, of the flux density;

$$\Phi = \int_{t_i}^{t_f} dt \phi(t) \tag{1.4}$$

The units of fluence are, of course, inverse area. The reader is cautioned that other units of time such as hours, minutes, days, years, etc. are commonly found in the scientific literature. As always, unit analysis is recommended.

dose equivalent per fluence conversion factors: These factors, here generally denoted by P, include effects due to the finite thicknesses of the tissue and include effects due to secondary particles. Figures 1.4 and 1.5, adapted from the tabulations of Schopper et al. (Sc90) for many particles commonly encountered provide these factors. Muons, as will be seen later, are of particular importance at high energy accelerators. For these particles, the dose equivalent per fluence, P, has been found by Stevenson (St83) to be about 40 fSv m² (i.e., 400 pSv cm²), equivalent to 25,000 muons cm⁻² mrem⁻¹, for 100 MeV < E_{μ} < 200 GeV. At lower energies range-out of muons in the human body with consequential higher energy deposition gives a conversion factor of 260 fSv m² (3850 muons cm⁻² per mrem). In principle, these values can be calculated for any particle. As an example for more "exotic" particles possibly of importance for future accelerators, Fig. 1.6 gives values of P for muon neutrinos, v_{μ} 's (Co97 and Mo99). For a radiation field containing a mixture of n different components (e.g., different particle types), one determines the dose equivalent, H, from

$$H = \sum_{i=1}^{n} \int_{E_{\min}}^{E_{\max}} dE P_i(E) \Phi_i(E), \qquad (1.5)$$

where $\Phi_i(E)$ is the fluence of particles of type *i* with energy between *E* and *dE* and $P_i(E)$ is the dose equivalent per unit fluence in appropriate units.

cross section: This quantity is an extremely important physical concept in describing particle interactions. The cross section represents the effective "size" of the atom or nucleus for some particular interaction. Consider a beam of particles of fluence Φ (particles cm⁻²) incident on a thin slab of absorber of thickness dx. The absorbing medium has N atoms cm⁻³. The number of incident particles that interact and are "lost" from the original fluence, $-d\Phi$, is given by

$$-d\Phi = \sigma N \Phi dx, \tag{1.6}$$

where σ is the cross section (cm²). But, $N = \rho N_A / A$, where ρ is the material density (g cm⁻³), N_A is Avogadro's number (6.02 x 10²³ mol⁻¹, see Table 1.1), and A is the atomic weight. Cross sections are often tabulated in units of **barns** where 1 barn is 10⁻²⁴ cm². Submultiples such as the mb (10⁻³ barn, 10⁻²⁷ cm²) are commonly used. If only one physical process is present with no others operative and if one starts with an initial fluence Φ_0 , this integrates, after some distance x (cm), to

$$\Phi(x) = \Phi_o e^{-N\sigma x}.$$
(1.7)

linear absorption coefficient: This quantity, μ , and its reciprocal, the **attenuation length**, λ , are given by

$$\mu = N\sigma(\text{cm}^{-1}) \text{ and } \lambda = 1/N\sigma \text{ (cm)}.$$
 (1.8)

Sometimes the **mass attenuation length**, $\lambda_m = \rho / N \sigma$ (g cm⁻²), is used where ρ is the density in g cm⁻³. Unfortunately, in the literature λ is often used for λ_m so that one has to take care to understand the context to be sure to use the correct units. For particles subject to the **nuclear interaction**, λ commonly denotes the **nuclear interaction length**.



Fig. 1.4 Dose equivalent per fluence for various charged particles, *P*, as a function of energy. The curve for muons is valid for both negative and positively-charged muons. [Adapted from (Sc90).]



Fig. 1.5 Dose equivalent per fluence for photons and neutrons, *P*, as a function of energy. [Adapted from (Sc90).]



Fig. 1.6 Dose equivalent per fluence for muon neutrinos (v_{μ}) , *P*, as a function of energy. [Adapted from (Co97).]

1.2.2 Physical Constants and Atomic and Nuclear Properties

Tables 1.1 and 1.2 give physical constants and atomic and nuclear properties as tabulated by the Particle Data Group $(PDG04)^1$. These tables are updated regularly and are republished every two years. A number of these constants and properties will be used throughout the rest of this text and in the solutions to the problems. Most of these quantities will be discussed subsequently and more details will be provided in subsequent chapters.

¹ The Particle Data Group based at the Lawrence Berkeley National laboratory maintains many tabulations on its website which are regularly updated. The reference list entry for (PDG04) provides the web link to this important source of information and, in some cases, provides more details.

Quantity	Symbol, Equation	Value ^{a,b}
speed of light	С	$2.99792458 \times 10^8 \text{ m s}^{-1}$
Planck constant	h	6.6260693(11) x 10 ⁻³⁴ J s
Planck constant, reduced	$\hbar = h/2\pi$	1.05457168(18) x 10 ⁻³⁴ J s
		$= 6.58211915(56) \times 10^{-22}$ MeV s
electron charge	e	1.60217653(14) x 10 ⁻¹⁹ C
		$= 4.80320441(41) \times 10^{-10} \text{ esu}$
useful constant	$\hbar c$	197.326968(17) MeV fm
useful constant	$(\hbar c)^2$	0.389379323(67) GeV ² mbarn
electron mass	m_e	$0.510998918(44) \text{ MeV/c}^2$
		$= 9.1093826(16) \times 10^{-31} \text{ kg}$
proton mass	m_p	938.272029(80) MeV/c ²
		$= 1.67262171(29) \times 10^{-27} \text{ kg}$
		= 1.00727646688(13) u
		$= 1836.15267261(85) m_e$
neutron mass	m_n	939.565360(81) MeV/c ²
		= 1.00866491560(55) u
Neutron mean -life	τ_n	885.70(80) s
deuteron mass	m_d	1875.61282(16) MeV/c ²
unified atomic mass unit (u)	$(mass ^{12}C atom)/12$	931.494043(80) MeV/c ²
	$= (1 g)/N_A$	$=1.66053886(28) \times 10^{27} \text{ kg}$
permittivity of free space	ε _o	8.854187817 x 10 ¹² F m ¹
permeability of free space	$\mu_{0,} [\varepsilon_0 \mu_0 = 1/c^2]$	$4\pi \times 10^{-7} \text{ N A}^{-2}$
fine structure constant	$\alpha = e^2 / 4\pi \varepsilon_0 \hbar c$	1/137.03599911(46)
classical electron radius	$r_e = e^2 / 4\pi \varepsilon_0 m_e c^2$	2.817940325(28) x 10 ⁻¹⁵ m
electron compton wavelength	$\lambda = \hbar / m_e c = r_e / \alpha$	3.86159678(26) x 10 ⁻¹³ m
wavelength of 1 eV/c particle	hc/e	1.23984191(11) x 10 ⁻⁶ m
Thomson cross section	$\sigma_T = 8\pi r_e^2/3$	0.665245873(13) barn
Newtonian gravitational	G_N	$6.6742(10) \times 10^{-11} \text{ m}^3 \text{ kg}^{-1} \text{ s}^{-2}$
constant		$= 6.7087(10) \hbar c (\text{GeV/c}^2)^{-2}$
std. gravitational accel.	8	9.80665 m s ⁻²
Avogadro number	N _A	$6.0221415(10) \ge 10^{23} \text{ mol}^{-1}$
Boltzmann constant	k	$1.3806505(24) \ge 10^{-23} \text{ J K}^{-1}$
		$= 8.617343(15) \times 10^{-5} \text{ eV K}^{-1}$
	1 barn	$10^{-28} \text{ m}^2 = 10^{-24} \text{ cm}^2$
	1 eV	1.60217653(14) x 10 ⁻¹⁹ J
	1 Gauss	10 ⁻⁴ Tesla
	1 erg	10 ⁻⁷ J
	1 fm	10 ⁻¹⁵ m
	1 atmosphere	760 torr = $1.01325 \times 10^5 \text{ N m}^{-2}$ (Pa)
	$0^{\circ} C$	273.15 °K

Table 1 1	Physical constants	[Adapted from	(PDG04) and (NI (04) 1
1 avic 1.1	I hysical constants.	[Auapieu II 0III	(1 DOV4) anu (191 9	J#J.]

^a The one-standard deviation uncertainties in the last digits are given in parentheses. ^b N = Newton, F = Farad, A = Ampere, C = Coulomb, J = Joule, esu = electrostatic unit, u = atomic mass unit

Table 1.2 Atomic and nuclear properties of materials. [Adapted from (1D604).]									
Material	Ζ	A^{b}	Nuclear	Nuclear	Nuclear	Nuclear	Minimum	Radiation	Density
			total	inelastic	collision	inter-	stopping	Length	ρ
			cross	cross	length	action	Power	X_{o}	$\{g/cm^{\circ}\}$
			sect.	sect.	λ_T	length	dE/dx	{g/cm}}	(g/1) or [g/1] for
			<i>σ</i> _T ∫harn ∖	<i>σ_{in}</i> ∫harn ∖	{g/cm }	Λ_{in}	$\{\text{Nev}\}$		gas
H_2^a	1	1.00794	0.0387	0.033	43.3	50.8	(4.103)	63.047	(0.0838)[0.0899]
D_2^a	1	2.014	0.073	0.061	45.7	54.7	(2.052)	122.4	0.169[0.179]
He ^a	2	4.00260	0.133	0.102	49.9	65.1	(1.937)	94.32	0.1249[0.1786]
Li	3	6.941	0.211	0.157	54.6	73.4	1.693	82.76	0.534
Be	4	9.01218	0.268	0.199	55.8	75.2	1.594	65.19	1.848
С	6	12.011	0.331	0.231	60.2	86.3	1.745	42.70	2.265^{f}
N_2^{a}	7	14.0067	0.379	0.265	61.4	87.8	(1.825)	37.99	0.8073[1.250]
O_2^{a}	8	15.9994	0.420	0.292	63.2	91.0	(1.675)	34.24	1.141[1.428]
Al	13	26.9815	0.634	0.421	70.6	106.4	1.615	24.01	2.70
Si	14	28.0855	0.660	0.440	70.6	106.0	1.664	21.82	2.33
Ar ^a	18	39.948	0.868	0.566	76.4	117.2	(1.519)	19.55	1.396[1.782]
Fe	26	55.845	1.120	0.703	82.8	131.9	1.451	13.84	7.87
Cu	29	63.546	1.232`	0.782	85.6	134.9	1.403	12.86	8.96
Ge	32	72.61	1.365	0.858	88.3	140.5	1.371	12.25	5.323
W	74	183.84	2.767	1.65	110.3	185	1.145	6.76	19.3
Pb	82	207.2	2.960	1.77	116.2	194	1.123	6.37	11.35
U	92	238.029	3.378	1.98	117.0	199	1.082	6.00	18.95
Air ^a					62.0	90.0	(1.815)	36.66	(1.205)[1.2931]
H ₂ O					60.1	83.6	1.991	36.08	1.00
Shielding	concr	ete ^g			67.4	99.9	1.711	26.7	2.5
SiO ₂ (qua	rtz)				66.5	97.4	1.699	27.05	2.64
NaI					94.6	151	1.305	9.49	3.67
Polystyre	ne, sci	ntillator (CI	H)		58.5	81.9	1.936	43.72	1.032
Polyethylene (CH ₂)					57.0	78.4	2.076	44.6	0.92-0.95
Mylar ($C_5H_4O_2$)					60.2	85.7	1.848	39.95	1.39
CO_2^a					62.4	89.7	(1.819)	36.2	[1.977]
Methane ^a (CH ₄)					54.8	73.4	(2.417)	46.22	0.4224[0.717]
Ethane ^a (C	$C_2H_6)$				55.8	75.7	(2.304)	45.45	0.509(1.356)
NaF					66.9	98.3	1.69	29.87	2.558
LiF					62.2	88.2	1.614	39.25	2.632

Table 1.2 Atomic and nuclear properties of materials. [Adapted from (PDG04).]

^aParameters for materials that are gases at NTP are evaluated at 20 °C and 1 atm (*value*) or at STP [*value*] or as cryogenic liquids at their 1 atmosphere boiling point if the *value* is given without parentheses.

^bAveraged over naturally occurring isotopes.

^cThese are energy dependent. The values tabulated are for the high energy limit. The inelastic cross section is obtained by subtracting the elastic and quasi-elastic cross sections from the total cross section.

^dThese quantities are the mean free path between all collisions (λ_T) or inelastic interactions (λ_{in}) and are also energy dependent. The values quoted are for the high energy limit.

^eThis is the minimum value of the ionization stopping power for heavy particles. It is calculated specifically for pions and the results are slightly different for other particles.

^fThe tabulated values are for pure graphite; industrial graphite may vary between 2.1-2.3 g cm⁻³.

^gThis is for standard shielding blocks, typical composition of O_2 (52%), Si (32.5%), Ca (6%), Na (1.5%), Fe (2%), Al (4%), plus reinforcing iron bars.

1.3 Summary of Relativistic Relationships

The results of the special theory of relativity are quite evident at most accelerators. In this section, the important conclusions are reviewed. The **rest energy**, W_o , of a particle of rest mass m_o is given by

$$W_o = m_o c^2 \,, \tag{1.9}$$

where c is the velocity of light. The **total energy** in free space, W, is given by

$$W = mc^{2} = \frac{m_{o}c^{2}}{\sqrt{1-\beta^{2}}} = \gamma m_{o}c^{2}, \text{ with } \gamma = \frac{W}{W_{o}} = \frac{1}{\sqrt{1-\beta^{2}}},$$
(1.10)

where $\beta = v/c$ and v is the velocity of the particle in a given frame of reference. The relationship between the quantities β and γ is obvious. Similarly, the **relativistic mass**, m, of a particle moving at velocity β is given by

$$m = \frac{m_o}{\sqrt{1 - \beta^2}} = \gamma m_o \,. \tag{1.11}$$

The **kinetic energy**, *E*, is $E = W - W_o = (m - m_o)c^2$ and (1.12)

$$\beta = \sqrt{1 - \left(\frac{W_0}{W}\right)^2} \,. \tag{1.13}$$

The **momentum**, *p*, of a particle in terms of its relativistic mass, *m*, and velocity, *v*, is;

$$p = mv = \gamma m_o \beta c = \frac{W m_o}{m_o c^2} \left[\sqrt{1 - \left(\frac{W_o}{W}\right)^2} \right] c = \frac{1}{c} \left[\sqrt{W^2 - W_o^2} \right] = \frac{1}{c} \sqrt{E(E + 2W_o)} , \qquad (1.14)$$

so that at high energies, $p \approx E/c \approx W/c$ while at low energies ($E \ll W_o$) one has the familiar nonrelativistic $p^2 \approx 2(W_o/c^2)E = 2m_oE$.

It is usually most convenient to work in a system of units where energy is in units of eV, MeV, etc. Velocities are then expressed in units of the speed of light (β), momenta are expressed as energy divided by *c* (e.g., MeV/c, etc.), and masses are expressed as energy divided by c^2 (e.g., MeV/c², etc.). In these units, the total energy, *W*, and the relativistic mass, *m*, are equivalent. One thus avoids the explicit inclusion of numerical values for *c*, or c^2 .

The **decay length** at a given velocity of a particle with a finite meanlife (at rest), τ , is given by $\gamma \beta c \tau$, where relativistic time dilation is taken into account by inclusion of the factor γ .

The product of the speed of light and the meanlife, $c\tau$, is often tabulated. The decay length is the mean distance traveled by a particle in vacuum prior to its decay. This length must be distinguished from that called the **decay path**. The decay path represents a distance in space in which a given particle is allowed to decay with no or minimal competition from other effects such as scattering or absorption. Thus, the decay length is determined by the basic physics of the decay process while the decay path is defined by the physical configuration of the accelerator components present.

1.4 Energy Loss by Ionization and Multiple Coulomb Scattering

1.4.1 Energy Loss by Ionization

For moderately relativistic particles, the mean rate of energy loss, the **stopping power**, is given approximately by

$$-\frac{dE}{dx} = 4\pi N_A r_e^2 m_e c^2 z^2 \frac{Z}{A} \frac{1}{\beta^2} \left[\ln\left\{\frac{2m_e c^2 \gamma^2 \beta^2}{I}\right\} - \beta^2 - \frac{\delta}{2} \right]$$
(MeV cm²g⁻¹), (1.15)

where N_A is Avogadro's number (atoms mol⁻¹), Z and A are the atomic number and weight of the material traversed, z is the charge state of the projectile in units of electron charge, m_e and r_e are the rest mass and "classical radius" of the electron (see Table 1.1), and I is the ionization constant. For Z > 1, $I \approx 16Z^{0.9}$ eV while for diatomic hydrogen (H₂), I = 19 eV. β and γ are as defined in Section 1.3. δ is a small correction factor that can be approximated by $2 \ln \gamma$. Substituting constants, for I in eV;

$$-\frac{dE}{dx} = 0.3071 \, z^2 \frac{Z}{A} \frac{1}{\beta^2} \left[\ln\left\{\frac{1.022 \times 10^6 \, \gamma^2 \beta^2}{I}\right\} - \beta^2 - \frac{\delta}{2} \right] \, (\text{MeV cm}^2 \text{g}^{-1}). \quad (1.16)$$

This is the stopping power² due to ionization, the process in which a charged particle transfers its energy to atomic electrons in the absorbing medium. In these units, the dependence upon the absorbing material is slowly-varying given the fact that *I* appears only in the logarithmic term and the ratio Z/A ranges between 0.4 to 0.5 over most of the periodic table for stable nuclides. Thus, for a given projectile charge *z* the value of the stopping power, dE/dx, is most strongly dependent on β . A broad minimum is found at a value of $\gamma = 3.2$. At this value of γ , the particles are said to be **minimum ionizing** and the corresponding minimum stopping powers are listed in Table 1.2.

The absorption of the energy of charged particles by ionization is characterized by a parameter called the **range**, R, in material. The range is the length of the path followed by the particle while it is losing its energy. Simplistically one might think that one could

² The argument of the logarithmic term of Eqs (1.15) and (1.16) must be dimensionless. Hence, the rest energy of the electron, m_ec^2 , and *I* must be in the same units (e.g., both in eV). These equations are found in Phys Rev. <u>D45</u> (1992) S1, the 1992 edition of reference (PDG04). This version of these equations is somewhat simpler than, but equivalent to, that found in (PDG04) and thus is adopted for use here.

calculate the value of R by a numerical integration of the reciprocal of the stopping power. However, as the particles lose energy by ionization and thus slow down, other effects at very low energies become important that are not included in Eq. (1.15). It is prudent, therefore, to consult explicit tabulations to determine the particle ranges. For charged particles much more massive than electrons, the trajectory through the material to first approximation is a straight line modified only by multiple Coulomb scattering (see Section 1.4.2) since the mass of the moving particle is so much larger than the mass of the atomic electrons. For a moving electron, the range is the sum of many divergent line segments through the material since its mass is identical to that of the atomic electrons encountered with the consequence that the individual angular deflections are much larger. As shall be seen in Section 3.2.2, for electrons the loss of energy in matter due to the radiation of photons increases rapidly with electron kinetic energy and becomes much more important than the ionization stopping power or the range at relatively low energies. The situation is also different for particles such as protons that participate in the nuclear interaction. For these particles, as the kinetic energy of the particle increases, the absorption of the particles through strong interaction processes has a high probability of absorbing the particles prior to their depositing all of their energy by ionization. This will be discussed further in Section 4.2.1. Figures 1.7 and 1.8 give stopping power and range values as a function of momentum or energy for common high energy particles and for some light ions, respectively. Detailed tables of the values of stopping power and ranges for many heavy ions have been given by Northcliffe and Schilling (No70). Also, the Monte Carlo computer code SRIM is currently easily obtained and may be used to generate similar tables as well as do simulations of protons or heavy charged ions interacting with elemental or compound materials (Zi96).

For muons (μ 's) the situation is rather unique. The muon rest energy is 105.66 MeV, its meanlife $\tau = 2.1970 \times 10^{-6}$ s, and the meanlife times the speed of light is $c\tau = 658.65$ m. Due to their large rest mass compared to that of the electron and the fact that these particles, to first order, do not participate in the strong (nuclear) interaction, muons tend to penetrate long distances in matter without being absorbed by other mechanisms. Muons, due to their heavier masses, are also far less susceptible to radiative effects. Thus, over a very large energy domain, the principal energy loss mechanism is that of ionization. This, as shall be seen later, makes the shielding of muons matter of considerable importance at high energy accelerators. The range-energy relation of muons is given in Fig. 1.9. At high energies ($E_{\mu} > 100$ GeV), the distribution of the ranges of individual muons about the mean range, called the **range straggling**, becomes severe (Va87). Also, above a muon energy of several hundred GeV, radiative losses begin to dominate such that the stopping power, dE/dx, is given by (PDG 04)

$$-\frac{dE}{dx} = a(E) + b(E)E, \qquad (1.17)$$

where a(E) is the collisional ionization energy loss [from Eq. (1.16), approximately 0.002 GeV cm²g⁻¹], and b(E) is the radiative coefficient for *E* in GeV. The latter parameter separated into contributions from the important physical mechanisms is plotted in Fig. 1.10.



Fig. 1.7 **A.** Mean ionization stopping power in various media as a function of particle momenta. Radiative effects are not included. **B.** Ionization range of heavy charged particles in various media. The abscissa of these plots are scaled to the ratio of particle momenta, *p*, to particle rest mass, *M*. [Reproduced from (PDG04).]



Fig. 1.8 Stopping power (top) and ranges (bottom) for protons in three different materials. These curves can be used for other incident particles by taking their atomic number, *z*, and mass, *m* (in atomic mass units), into account. The incident energy is thus expressed as the specific kinetic energy, *E/m*. The curves are approximately correct except at the very lowest energies where charge exchange effects can be important. The results are most valid for projectile mass, $m \le 4$ [Adapted from (En66).]



Fig. 1.9 Range-energy curves for muons in various materials. On the curve labeled "Earth", the gray boxes are indicative the approximate spread in the range due to range straggling at one standard deviation at the indicated muon energy. The density of "earth" was taken to be 2.0 g cm⁻². [Adapted from (Sc90).]



Fig. 1.10 Contributions to the fractional energy loss by muons in iron due to e^+e^- pair production, bremsstrahlung, and photonuclear interactions. See Eq (1.17). [Adapted from (PDG04).]

The mean range, R_{μ} , of a muon of kinetic energy E (GeV), is approximated by

$$R_{\mu}(E) = \frac{1}{b(E)} \ln \left[1 + \frac{b(E)}{a(E)} E \right] \text{ (g cm}^{-2}).$$
(1.18)

Muon range straggling (Va87) is chiefly due to the fact that, for muon kinetic energies greater than about 100 GeV, electron-positron pair production, bremsstrahlung, and deep inelastic nuclear reactions become the dominant energy loss mechanisms. Although these processes have low probabilities, when they do occur they involve large energy losses and thus have quite significant effects. Tables 1.3 and 1.4 give fractional energy loss and comparisons of muon ranges at high energies for different physical mechanisms. Here, the straggling is very important since shielding calculations based upon using the mean range values can lead to significant *underestimates* of the fluence of muons which can penetrate the shield.

Table 1.3 Fractional energy loss of muons in soil ($\rho = 2.0 \text{ g cm}^{-3}$). The fractions of the total energy loss due to the four dominant energy loss mechanisms are given. [Adapted from (Va87) and (Sc90).]

Energy (GeV)	Ionization	Bremsstrahlung	Pair production	Deep inelastic nuclear scattering
10	0.972	0.037	8.8 x 10 ⁻⁴	9.7 x 10 ⁻⁴
100	0.888	0.086	0.020	0.0093
1000	0.580	0.193	0.168	0.055
10,000	0.167	0.335	0.388	0.110

Table 1.4 Comparison of muon ranges (meters) in heavy soil ($\rho = 2.24$ g cm³). [Adapted from (Va87) and (Sc90).]

Energy	Mean Ranges from <i>dE/dx</i> in Heavy Soil (meters)					
(GeV)	Mean Range (meters)	Standard Deviation (meters)	All Processes	Coulomb Losses Only	Coulomb & Pair Production Losses	
10	22.8	1.6	21.4	21.5	21.5	
30	63.0	5.6	60.3	61.1	60.8	
100	188	23	183	193	188	
300	481	78	474	558	574	
1000	1140	250	1140	1790	1390	
3000	1970	550	2060	5170	2930	
10,000	3080	890	3240	16,700	5340	
20,000	3730	1070				

1.4.2 Multiple Coulomb Scattering

Multiple Coulomb scattering from nuclei is an important effect in the transport of charged particles through matter. A charged particle traversing a medium is deflected by many small-angle scattering events and only occasionally by ones involving large-angle scattering. The small-angle scattering events are largely due to Coulomb scattering from nuclei so that the effect is called multiple Coulomb scattering. This simplification is not quite correct for hadrons since it ignores the contribution of strong interactions to multiple scattering. For purposes of discussion here, a Gaussian approximation adequately describes the distribution of deflection angles of the final trajectory compared with the incident trajectory for all charged particles. The distribution as a function of deflection angle, θ , is as follows:

$$f(\theta)d\theta = \left(\frac{d\theta}{\theta_0\sqrt{2\pi}}\right) \exp\left(-\frac{\theta^2}{2\theta_0^2}\right).$$
 (1.19)

The mean width of the projected angular distribution, θ_o , on a particular plane is approximated by

$$\theta_o = \frac{13.6z}{pc\beta} \sqrt{\frac{x}{X_o}} \left\{ 1 + 0.038 \ln\left(\frac{x}{X_o}\right) \right\} \text{ (radians)}$$
(1.20)

where z is the charge of the projectile in units of the charge of the electron, p is the particle momentum in MeV/c and x is the absorber thickness in the same units as the quantity X_o (PDG04). X_o is a material-dependent parameter, to be discussed further in Section 3.2.2 called the **radiation length**. This description of multiple Coulomb scattering has been validated for particles having momenta up to 200 GeV/c by Shen et al. (Sh79). The best values of the radiation length are probably those of Tsai (Ts74), the values tabulated in Table 1.2. A compact, approximate formula for calculating the value of X_o as a function of atomic number, Z, and atomic weight, A, of the material medium (PDG04) is

$$X_o = \frac{716.4A}{Z(Z+1)\ln(287/\sqrt{Z})} \text{ (g cm}^{-2}).$$
(1.21)

Results obtained using this formula agree to those of Tsai within about 2.5 % for all elements except helium, where the result is about 5 % low. An alternative method of calculating X_o using different atomic wave functions is given by Seltzer and Berger (Se85). It provides results similar to those given by Eq. (1.21).

1.5 Radiological Standards

While the discussion of radiological standards is not a topic of great emphasis in this text, some mention of it seems to be appropriate. Standards or limits on occupational and environmental exposure to ionizing radiation are now instituted worldwide. In general, individual nations, or sub-national entities, incorporate guidance provided by international or national bodies into their laws and regulations. The main international body that develops radiological standards is the International Commission on Radiation Protection (ICRP). Another international institution, the International Commission on Radiation Units and Measurements (ICRU), also is an important standards-setting institution. In the United States, the major national body chartered by the U.S. Congress is the National Council on Standards developed by these Radiation Protection and Measurements (NCRP). organizations are referenced in other chapters of this text. Of particular interest are the following References: (IC71), (IC73), (IC78), (IC87), (IC91), (NC77), (NC90), and (NC03). In the U.S. the U.S. Environmental Protection Agency (EPA) is the primary federal agency for establishing basic radiological requirements. These are further implemented by the U.S. Department of Energy (DOE) for its facilities, and by individual states. At present the U.S. Nuclear Regulatory Commission (NRC) does not regulate However, certain aspects of state regulations pertaining to particle accelerators. accelerators are reflective of general NRC requirements for radiation protection. The regulation of accelerator facilities varies considerably between individual states and some local jurisdictions, the authority having jurisdiction should be consulted to obtain an accurate understanding of applicable regulatory requirements.

Problems

- 1. a) Express 1 kilowatt (1 kW) of beam power in GeV s^{-1} .
 - b) To how many singly charged particles per second does 1 ampere of beam current correspond?
 - c) Express an absorbed dose of 1 Gy in GeV kg⁻¹ of energy deposition.
- 2. Which has the higher quality factor, a 10 MeV (kinetic energy) α -particle or a 1 MeV neutron? Write down the quality factors for each particle.
- 3. Calculate the number of ${}^{12}C$ and ${}^{238}U$ atoms in a cubic centimeter of solid material.
- 4. Calculate the velocity and momenta of a 200 MeV electron, proton, iron ion, π^+ , and μ^+ . The 200 MeV is kinetic energy and the answers should be expressed in units of the speed of light (velocity) and MeV/c (momenta). Iron ions have an isotope-averaged mass of 52021 MeV ($A = 55.847 \times 931.5$ MeV/amu). The π^+ mass is 140 MeV and the μ^+ mass = 106 MeV. Do the same calculation for 20 GeV protons, iron ions, and muons. It is suggested that these results be presented in tabular form. Make general comments on the velocity and momenta of the particles at the two energies. (The table may help you notice any algebraic errors that you may have made.)
- 5. Calculate the mass stopping power of a 20 MeV electron (ionization only) and a 200 MeV proton in ²⁸Si.
- 6. Calculate the fluence of minimum ionizing muons necessary to produce a dose equivalent of 1 mrem assuming a quality factor = 1 and that <u>tissue</u> is equivalent to <u>water</u> for minimum ionizing muons. (Hint: use Table 1.2.) Compare with the results given in Fig. 1.4 for high energies.

CHAPTER 2 GENERAL CONSIDERATIONS OF RADIATION FIELDS AT ACCELERATORS

2.1 Introduction

In this chapter general properties of the radiation fields at accelerators will be discussed. To do this, the concept of particle yield and solid angle will be introduced. Following that, a theoretical approach to particle transport will be introduced. The Monte Carlo technique will be described and illustrated by simple examples. The manipulation of charged particles using electromagnetic fields will be reviewed due to its importance in understanding the handling of the charged particle beams.

2.2 Primary Radiation Fields at Accelerators-General Considerations

Accelerated charged particles, except in the singular phenomenon of synchrotron radiation (discussed in Section 3.2.3), do not produce radiation unless there is some interaction with matter. The charged particles directly accelerated, and otherwise manipulated by the electromagnetic fields within the accelerator, are referred to as the **primary particles** or beam. All other particles that are produced from this beam are either due to the interactions of these primary particles in matter or due to synchrotron radiation are referred to as **secondary particles**. In some instances, one finds references to **tertiary particles** that result from the interactions in matter of the secondary particles or are emitted in their radioactive decay. Confusion at many high energy accelerators sometimes arises from the fact that secondary and tertiary particles and ions can be collected into beams of their own and even accelerated. In these instances, when the secondary or tertiary particles are employed at some location separated from the place where they were initially produced, they can obviously play the role of primary particles.

If one considers primary particles incident upon a physical object such as a target, the **yield**, *Y*, of secondary particles is a crucial parameter. For a given type of secondary particle, the yield is typically a function of both angle and particle energy and is defined according to Fig. 2.1. Scattered reaction products are found at a "point of interest" located at radius, *r*, and polar angle, θ , relative to the direction of the incident particle along the positive *z* -axis. In general, particle **differential yields** are expressed in terms of particles per unit solid angle at the point of interest and are commonly normalized to the number of incident particles or to the beam current or total delivered charge. Such particle yields, dependent upon both target material and thickness, are reported in terms of particle type, energy, and angular distribution. The rate of production of the desired reaction products and their energy spectra is, in general, a strong function of both θ and the incident particle energy E_{ρ} . There is usually no dependence on the azimuthal angle in a spherical coordinate system.³

³The most common exception is the situation in which the spins of the target nuclei and/or the incident particles are oriented along some chosen direction in a so-called polarization experiment. Interactions of colliding beams that include spin-polarized particles likewise may have azimuthal dependencies. Secondary particles resulting from multipole emission/deexcitation processes from excited atomic or nuclear states will also have a dependence on azimuthal angle.



Fig. 2.1 Conceptual interaction of incident beam with material (target) which produces radiation at the point of interest located at polar coordinates (r, θ) .

In principle, the particle yield could be obtained directly from differential cross sections for given incident particle kinetic energy *E*;

$$\frac{d\sigma(E,\theta)}{d\Omega},$$

where $\sigma(E, \theta)$ is the cross section as a function of energy and angle and Ω is the solid angle into which the secondary particles are directed. For example, *Y* could, in principle be obtained from an integration of this cross section as it varies with energy while the incident particle loses energy in passing through the target material.

Calculations of the radiation field that directly use the cross sections are often not practical because targets hit by beam are not really "thin". Thus one cannot ignore energy loss or secondary interactions in the target. Furthermore, the knowledge of cross sections at all energies is often incomplete with the unfortunate result that one cannot always integrate over θ and *E* to get the total yield.

For many applications, the details of the angular distributions of total secondary particle yield, $dY(\theta)/d\Omega$, and the angular dependence of the emitted particle energy spectrum, $d^2Y(E, \theta)/dEd\Omega$, are very important.

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Often, the particle fluence is needed at a particular location at coordinates (r, θ) from a known point source of beam loss while the angular distributions of $dY/d\Omega$ are generally expressed in units of particles/(steradian-incident particle). To obtain the total fluence $\Phi(\theta)$ [e.g., particles/(cm²·incident particle)], or differential fluence $d\Phi(E, \theta)/dE$ [e.g., particles/(cm²·MeV·incident particle)] at a given distance r (cm) at a specified angle θ from such a **point source**⁴, one must simply multiply the yield values by r^{-2} :

$$\Phi(\theta) = \frac{1}{r^2} \frac{dY(\theta)}{d\Omega} \quad \text{and} \quad \frac{d\Phi(E,\theta)}{dE} = \frac{1}{r^2} \frac{d^2 Y(E,\theta)}{dE d\Omega}.$$
 (2.1)

Given the fact that secondary, as well as primary, particles can create radiation fields, it is quite obvious that the transport of particles through space and matter can become a very complex matter. In the following section, the advanced techniques for handling these issues are described.

2.3 Theory of Radiation Transport

The theoretical material in this section is largely due to the work of O'Brien (OB80). It is included to show clearly the mathematical basis of the contents of shielding codes, especially those that use the Monte Carlo method. Vector notation is used in this section.

2.3.1 General Considerations of Radiation Transport

Stray and direct radiations at any location are distributed in particle type, direction, and energy. To determine the amount of radiation present for radiation protection purposes one must assign a magnitude to this multidimensional quantity. This is done by forming a double integral over energy and direction of the product of the flux density and an approximate dose equivalent per unit fluence conversion factor, summed over particle type;

$$\frac{dH(\vec{x},t)}{dt} = \sum_{i} \int_{4\pi} d\vec{\Omega} \int_0^\infty dE f_i(\vec{x}, E, \vec{\Omega}, t) P_i(E) , \qquad (2.2)$$

where the summation index *i* is over the various particle types, $\overline{\Omega}$ is the direction <u>vector</u> of particle travel, \overline{x} is the coordinate <u>vector</u> of the point in space where the dose or dose equivalent is to be calculated, *E* is the particle energy, *t* is time, and *i* is the particle type. $P_i(E)$ is the dose equivalent per fluence conversion factor expressed as a function of energy and particle type for the *i*th particle. The inner integral is over all energies while the outer integral is over all spatial directions from which contributions to the radiation field at the location specified by \overline{x} originate. The result of the integration is $dH(\overline{x},t)/dt$, the dose equivalent rate at location \overline{x} and time *t*. Values of $P_i(E)$ are given in Figs. 1.4,

⁴ A point source is one in which the dimensions of the source are small compared with the distance to some other location of interest.

1.5, and 1.6. The **angular flux density**, $f_i(\vec{x}, E, \vec{\Omega}, t)$, the number of particles of type *i* per unit area, per unit energy, per unit solid angle, per unit time at location \vec{x} , with a energy *E*, at a time *t*, and traveling in a direction $\vec{\Omega}$ is related to the total flux density, $\phi(\vec{x}, t)$, by integrating over direction and particle energy;

$$\phi(\vec{x},t) = \sum_{i} \int_{4\pi} d\vec{\Omega} \int_{0}^{\infty} dE f_{i}(\vec{x},E,\vec{\Omega},t) \,.$$
(2.3)

The angular flux density, $f_i(\vec{x}, E, \vec{\Omega}, t)$, is connected to the total fluence $\Phi(\vec{x})$ by integrating over a relevant interval of time (t_i to t_f), as well as direction and energy;

$$\Phi(\vec{x}) = \sum_{i} \int_{4\pi} d\vec{\Omega} \int_{0}^{\infty} dE \int_{t_{i}}^{t_{f}} dt f_{i}(\vec{x}, E, \vec{\Omega}, t), \qquad (2.4)$$

and to the energy spectrum expressed as a flux density for particle type *i* at point \vec{x} at time *t*, $\phi_i(\vec{x}, t, E)$, by

$$\phi_i(\vec{x}, t, E) = \int_{4\pi} d\vec{\Omega} f_i(\vec{x}, E, \vec{\Omega}, t) \,.$$
(2.5)

To determine the proper dimensions and composition of a shield, the amount of radiation, expressed in terms of the dose or dose equivalent, which penetrates the shield and reaches locations of interest must be calculated. This quantity must be compared with the maximum permissible dose equivalent. If the calculated dose equivalent is too large, either the conditions associated with the source of the radiation or the physical properties of the shield must be changed. The latter could be a change in shield materials, dimensions, or both. If the shield cannot be adjusted, then the amount of beam loss allowed by the beam control instrumentation, the amount of residual gas in the vacuum system, or the amount of beam accelerated may have to be reduced. It is difficult and expensive, especially in the case of the larger accelerators, to alter permanent shielding or operating conditions if the determination of shielding dimensions and composition has not been done correctly. The methods for determining these quantities have been investigated by a number of workers. The next section only summarizes the basics of this important work.

2.3.2 The Boltzmann Equation

The primary tool for determining the amount of radiation reaching a given location is the *stationary form* of the **Boltzmann equation** (henceforth, simply the Boltzmann equation) which, when solved, yields the angular flux density, f_i , the distribution in energy and angle for each particle type as a function of position and time. The angular flux density is then converted to dose equivalent rate by means of Eq. (2.2). This section describes the

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theory that yields the distribution of radiation in matter, and discusses some of the methods for extracting detailed numerical values for elements of this distribution such as particle flux, or related quantities, such as dose, activation or instrument response. The Boltzmann equation is a statement of all the processes that the particles of various types, including photons, that comprise the radiation field can undergo. A much more complete derivation and discussion has been given by O'Brien (OB80).

This equation is an integral-differential equation describing the behavior of a dilute assemblage of corpuscles. It was derived by Ludwig Boltzmann in 1872 to study the properties of gases but applies equally to the behavior of those "corpuscles" which comprise ionizing radiation. This equation is a continuity equation of the angular flux density, f_i , in phase space which is made up of the three space coordinates of Euclidian geometry, the three corresponding direction cosines, the kinetic energy, and the time. The density of radiation in a volume of phase space may change in the following five ways:

- **uniform translation**; where the spatial coordinates change, but the energy-angle coordinates remain unchanged;
- **collisions**; as a result of which the energy-angle coordinates change, but the spatial coordinates remain unchanged, or the particle may be absorbed and disappear altogether;
- **continuous slowing down**; in which uniform translation is combined with continuous energy loss;
- **decay**; where particles are changed through radioactive transmutation into particles of another kind; and
- **introduction**; involving the direct emission of a particle from a source into the volume of phase space of interest: electrons or photons from radioactive materials, neutrons from an α -n emitter, the "appearance" of beam particles, or particles emitted from a collision at another (usually higher) energy.

Combining these five elements yields

$$\tilde{\mathbf{B}}_i f_i(\vec{x}, E, \vec{\Omega}, t) = Q_{ij} + Y_i, \qquad (2.6)$$

where the mixed differential and integral **Boltzmann operator** for particles of type i, \tilde{B}_i , is given by

$$\tilde{\mathbf{B}}_{i} = \vec{\Omega} \cdot \nabla + \sigma_{i} + d_{i} - \frac{\partial S_{i}}{\partial E}, \qquad (2.7)$$

$$Q_{ij} = \sum_{j} \int_{4\pi} d\vec{\Omega}' \int_{0}^{E_{\text{max}}} dE_{B} \sigma_{ij} \left(E_{B} \to E, \vec{\Omega}' \to \vec{\Omega} \right) f_{j}(\vec{x}, E, \vec{\Omega}', t), \qquad (2.8)$$

and

 $d_i = \frac{\sqrt{1 - \beta_i^2}}{\tau_i \beta_i c} \,. \tag{2.9}$

In Eq. (2.7):

 Y_i is the number of particles of type *i* introduced by a source per unit area, time, energy, and solid angle;

 σ_i is the absorption cross section for particles of type *i*. To be dimensionally correct, this is actually the *macroscopic* cross section or linear absorption coefficient $\mu = N\sigma$ as defined in Eq. (1.8);

 d_i is the decay probability per unit flight path of radioactive particles (such as muons or pions) of type i;

 S_i is the stopping power for charged particles of type *i* (assumed to be zero for uncharged particles);

 Q_{ij} is the "scattering-down" integral; the production rate of particles of type *i* with a direction $\vec{\Omega}$, an energy *E* at a location \vec{x} , by collisions with nuclei or decay of *j*-type particles having a direction $\vec{\Omega}'$ at a higher energy E_B ;

 σ_{ij} is the doubly-differential inclusive cross section for the production of *i*-type particles with energy *E* and a direction $\vec{\Omega}$ from nuclear collisions or decay of *j*-type particles with a direction E_B and a direction $\vec{\Omega}'$; and

 β_i is the velocity of a particle of type *i* divided by the speed of light *c*; and τ_i is the mean-life of a radioactive particle of type *i* in the rest frame.

This equation is obviously quite difficult to solve in general and special techniques have been devised to yield useful results. The Monte Carlo method is the most common method of approximate solution used in the field of radiation shielding.

2.4 The Monte Carlo Method

2.4.1 General Principles of the Monte Carlo Technique

The Monte Carlo method is based on the use of random sampling to obtain the solution of the Boltzmann equation. It is one of the most useful methods for evaluating radiation

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hazards for realistic geometries that are generally quite difficult to characterize using analytic techniques (i.e., with equations in closed form). The calculation proceeds by constructing a series of trajectories, each segment of which is chosen at random from a distribution of applicable processes. In the simplest and most widely used form of the Monte Carlo technique, the so-called **inverse transform method**, a **history** is obtained by calculating travel distances between collisions and then sampling from distributions in energy and angle made up from the cross sections,

$$\sigma_{ij}(E_B \to E, \vec{\Omega}' \to \vec{\Omega}). \tag{2.10}$$

The result of the interaction may be a number of particles of varying types, energies, and directions each of which will be followed in turn. The results of many histories will be tabulated, leading typically to some sort of mean and standard deviation.

If p(x)dx is the **differential probability** of an occurrence at $x \pm 1/2 dx$ in the interval, [a,b], then the integration

$$P(x) = \int_{a}^{x} dx' p(x')$$
 (2.11)

gives P(x), the **cumulative probability** that the event will occur in the interval [a, x]. The cumulative probability function is monotonically increasing with x and always satisfies the conditions P(a) = 0, P(b) = 1. If a random number R uniform on the interval [0, 1] is chosen, for example from a computer routine, the equation

$$R = P(x) \tag{2.12}$$

corresponds to a random choice of the value of x, since the distribution function for the event P(x) can, in principle, be inverted as a unique one-to-one mapping;

$$x = P^{-1}(R). (2.13)$$

As a simple illustration, to determine when an uncharged particle undergoes a reaction in a one-dimensional system with no decays (d = 0), no competing processes (S = 0), and no "in-scattering" (Q = 0), one recognizes from Eqs. (1.6), (2.6), and (2.7) that a simple application of the Boltzmann equation is applicable;

$$\tilde{\mathbf{B}}\Phi = \left\{\vec{\Omega}\cdot\nabla + \sigma_i\right\}\Phi \ . \tag{2.14}$$

This simple situation reduces to the following, taking in this discussion σ_i to be the *macroscopic* cross section otherwise denoted by $N\sigma$ in this text;

$$\tilde{B}\Phi = \frac{d\Phi}{dx} + N\sigma\Phi = 0. \qquad (2.15)$$

The solution to this equation is the familiar

$$\Phi = \Phi_0 \exp(-x/\lambda), \qquad (2.16)$$

where $\lambda = 1/N\sigma$ as in Eq. (1.8). One can replace x/λ with *r*, the number of mean-freepaths the particle travels in the medium. The differential probability per unit mean-freepath for an interaction is given by

$$p(r) = \exp(-r)$$
, (2.17)

with
$$P(r) = \int_0^r dr' \exp(-r') = -\exp(-r') \Big]_0^r = 1 - \exp(-r) = R$$
. (2.18)

Selecting a random number, R, then determines a depth r that has the proper distribution. Of course, mathematically identical results apply to other processes described by an exponential function such as radioactive decay. In this simple situation, it is clear that one can solve the above for r as a function of R and thus obtain individual values of r from a corresponding set of random numbers. For many processes, an inversion this simple is not possible analytically. In those situations, other techniques exemplified by successive approximations and table look-up procedures must be employed.

In a Monte Carlo calculation, the next sampling process might select which of several physical processes would occur. Another sampling might choose, for instance, the scattering of the particle being followed. Deflections by magnetic fields might be included as well as further particle production and/or decay.

The Monte Carlo result is the number of times the event of interest occurred for the random steps through the relevant processes. As a counting process it has a counting uncertainty and the variance will tend to decrease as the square root of the number of calculations run on the computer. Thus high probability processes can be more accurately simulated than low probability processes such as passage through a thick shield in which the radiation levels are attenuated over many orders of magnitude. In modern calculations, sophisticated techniques are often employed which temporarily give enhanced probabilities to the low-probability events during the calculation in order to study them. The normal probabilities are restored at the end of the calculation by removing these so-called "weights" to obtain realistic results. It is by no means clear that the distributions obtained using the Monte Carlo method will be distributed according to the normal, or Gaussian distribution, so that a statistical test of the adequacy of the mean and standard deviation may be required.

2.4.2 Monte Carlo Example; A Sinusoidal Angular Distribution of Beam Particles

Suppose one has a distribution of beam particles such as exhibited in Fig 2.2.


Fig. 2.2 Hypothetical angular distribution of particles obeying a distribution proportional to $\cos \theta$.

For this distribution, $p(\theta) = A \cos \theta$ for $0 < \theta < \pi/2$. Then, the fact that the integral of $p(\theta)$ over the relevant interval $0 \le \theta \le \pi/2$ to get the cumulative probability $P(\theta = \pi/2)$ must be unity implies A = 1 since

$$P(\pi/2) = \int_0^{\pi/2} d\theta A \cos \theta = A \sin \theta \,\Big|_0^{\pi/2} \stackrel{\text{def}}{=} 1.$$
(2.19)

Thus, $p(\theta) = \cos \theta$. The cumulative probability, $P(\theta)$, is then given by

$$P(\theta) = \int_{0}^{\theta} d\theta' p(\theta') = \int_{0}^{\theta} d\theta' \cos \theta' = \sin \theta' \Big|_{0}^{\theta} = \sin \theta .$$
 (2.20)

If *R* is a random number, then $R = P(\theta)$ determines a unique value of θ ; hence

$$\theta = \sin^{-1}(R). \tag{2.21}$$

One can perform a simple Monte Carlo calculation using, for example, 50 random numbers. To do this one should set up a table such as Table 2.1 that was generated using a particular set of such random numbers. One can set up a set of bins of successive ranges of θ -values. The second column is a "tally sheet" for collecting "events" in which a random number *R* results in a value of θ within the associated range of θ -values. θ_{mid} is the midpoint of the bin (0.1, 0.3,...). Column 4 is the normalized number in radians found from the following:

N = Number found in Monte Carlo bin	
$TV = \frac{1}{(\text{Total number of events})(\text{bin width})}$	
_ Number found in bin in Monte Carlo	
= (50)(0.2 radians).	(2.22)

Table 2.1 Tally sheet for Monte Carlo ex	xample.
--	---------

θ (radians)	R (random #)	Total <i>R</i> 's in Bin	N (norm. #)	$\cos \theta_{mid}$
0.0 - 0.199	1111 1111 1	11	1.1	0.995
0.2 - 0.399	1111 1111 111	13	1.3	0.955
0.4 - 0.599	1111 1111 1	11	1.1	0.877
0.6 - 0.799	1111	4	0.4	0.765
0.8 - 0.999	1111 11	7	0.7	0.621
1.0 - 1.199	1111	4	0.4	0.453
1.2 - 1.399				0.267
1.4 - 1.57				0.086

One can calculate exactly the mean value of θ for the specified distribution:

$$\langle \theta \rangle = \frac{\int_0^{\pi/2} \theta p(\theta) d\theta}{\int_0^{\pi/2} p(\theta) d\theta} = \frac{\int_0^{\pi/2} \theta \cos(\theta) d\theta}{1} = \left[\cos \theta + \theta \sin \theta \right]_0^{\pi/2}$$

$$\langle \theta \rangle = \left[0 - 1 + \frac{\pi}{2} - 0 \right] = 0.57.$$

$$(2.23)$$

To calculate the same quantity from the Monte Carlo result, one proceeds first by multiplying the frequency of Monte Carlo events for each eight angular bins from the table by the midpoint value of the bins. Then one sums over the 8 bins and divides by the number of incident particles (50 in this example). Thus one can determine the average value of θ , $< \theta >_{MC}$, calculated by the Monte Carlo technique:

$$<\Theta_{MC} = [(11)(0.1) + (13)(0.3) + (11)(0.5) + (4)(0.7) + (7)(0.9) + (4)(1.1)]/50 = 0.48.$$
(2.24)

It is easy to see from this simple example involving very coarse bins and a very small number of histories that the agreement is quite good in spite of the rather poor "statistics". This example also illustrates that the statistical errors are generally larger for the more rare events here represented by large values of θ (i.e., $\theta > 1$ radian). The choice of bin sizes is also crucial.

Practical Monte Carlo calculations generally involve the need to follow a huge number of histories. Early calculations of this type, such as the one reported by Wilson (Wi52), were made using devices such as "wheels of chance" and hand-tallying. The advent of digital computers has rendered this technique much more powerful. As the speed of computer processors has increased, the ability to model the physical effects in more detail and with ever improving statistical accuracy has resulted. In later chapters, results obtained using specific codes will be presented. Descriptions of the codes themselves, accurate as of this writing, are presented in Appendix A. The reader should be cautioned that most of these codes are being constantly improved and updated. The wisest practice in using them is to consult with the authors of the codes directly.

2.5 Review of Magnetic Deflection and Focussing of Charged Particles

2.5.1 Magnetic Deflection of Charged Particles

Particle accelerators of all types operate by utilizing electromagnetic forces to accelerate deflect, and focus charged particles. These forces have been well described in detail by other authors such as Edwards and Syphers (Ed93), Carey (Ca87), and Chao and Tigner (Ch99). In accelerator radiation protection, an understanding of these forces is motivated by the need to be able to determine the deflection of particles by electric or magnetic fields. Clearly, one needs to be able to assure that particles in a deflected particle beam either interact with material where such interactions are desired or avoid such points of beam loss. The answers to such questions are interconnected with the design of the accelerator and, for those purposes advanced texts such as those cited above should be consulted. This is especially true for situations involving the application of radiofrequency (RF) electromagnetic fields to the particle beams where a full treatment using electrodynamics is needed⁵. However, some of the issues are quite simple and are discussed in this section for static, or slowly varying electric and magnetic fields.

The force, \overline{F} (Newtons) on a given charge, q (Coulombs), at any point in space is given, in SI units, by

$$\vec{F} = q(\vec{v} \times \vec{B} + \vec{E}) = \frac{d\vec{p}}{dt},$$
(2.25)

where the electric field, \vec{E} , is in Volts meter⁻¹, the magnetic field \vec{B} is in Tesla (1 Tesla = 10^4 Gauss), and \vec{v} is the velocity of the charged particle in m sec⁻¹, \vec{p} is the momentum of the particle in SI units, and *t* is the time (sec). The direction of the force due to the cross product in Eq (2.25) is, of course, determined by the usual **right-hand** rule. Static electric fields (i.e., $d\vec{E}/dt = 0$), if present, serve to accelerate or decelerate the charged

⁵ As the reader should recall, Maxwell's Equations interconnect the electric and magnetic fields when they vary with time.

particles. In a uniform magnetic field without the presence of an electric field, due to the cross product in this equation, any component of \vec{p} which is parallel to \vec{B} will not be altered by the magnetic field. Typically, charged particles are deflected by dipole magnets in which the magnetic field is, to high order, spatially uniform and constant in time, or slowly-varying compared with the time during which the particle is present. For this situation, if there is no component of \vec{p} which is parallel to \vec{B} , the motion is circular and the magnetic force serves to supply the requisite centripetal acceleration. The presence of a component of \vec{p} which is parallel to \vec{B} results in a trajectory that is a spiral rather than a circle. Figure 2.3 illustrates the condition of circular motion. Equating the centripetal force to the magnetic force and recognizing that \vec{p} is perpendicular to \vec{B} leads to

$$\frac{mv^2}{R} = qvB, \qquad (2.26)$$

where *m* is the *relativistic* mass (see Eq. 1.11). Solving for the radius of the circle, *R* (meters), recognizing that p = mv, and changing the units of measure for momentum, one gets

$$R(\text{meters}) = \frac{p}{qB} \text{ (SI units)} = \frac{p(\text{GeV/c})}{0.29979qB},$$
 (2.27)

where q in the denominator of the right hand side is now the *number* of electronic charges carried by the particle and B remains expressed in Tesla. The numerical factor in the denominator is just the mantissa of the numerical value of the speed of light in SI units.

In practice, at large accelerators, one is often interested in the angular deflection of a magnet of length, L, which provides such a uniform field orthogonal to the particle trajectory. Such a situation is also shown in Fig. 2.3. If L is only a small piece of the complete circle (i.e., $L \ll R$), one can consider the circular path over such a length to be two straight line segments. Doing this, one finds that the change in direction, $\Delta\theta$, is given by

$$\Delta \theta = \frac{L}{R} = \frac{0.29979 \, qBL}{p} \text{ (radians)}, \tag{2.28}$$

where the product, BL (Tesla-meters) is commonly referred to the **field integral** of the magnet system and p remains in GeV/c. It is evident that BL could just as well be obtained by integrating a non-uniform field over the length of the magnet system. This angle of deflection can be used to deduce if the particle beam will, or will not, interact with some solid object near its path, a matter of practical importance for radiation protection.



B is perpendicular to the paper and directed toward the reader

Fig. 2.3 A particle of positive charge q having momentum \vec{p} follows a circular path when directed perpendicular to a static, uniform magnetic field \vec{B} . The figure on the left illustrates this for a complete circle. On the right, a particle of momentum \vec{p} enters a magnet of length L that has field integral value of *BL*. For this example, $L \ll R$ and the particle experiences a small angular deflection $\Delta \theta$. The angular deflection is exaggerated in this figure for clarity.

2.5.2 Magnetic Focussing of Charged Particles

Now we consider, in a simplified way, how the focussing of charged particle beams can be accomplished using of quadrupole magnets. Edwards and Syphers (Ed93) and Carey (Ca87) describe in much more detail the magnetic deflections in general electromagnetic systems, including quadrupole magnets, and those of higher order which focus particle beams. Mathematical methods analogous to those found in the study of geometrical optics are often used to describe the optics of charged particles. Where time-varying electric and magnetic fields are involved, the full complement of Maxwell's equations must, of course, be used to describe the motion of charged particles. The application of higher order multipole fields and the employment of radiofrequency ("RF") electromagnetic fields to accelerate, decelerate, and otherwise manipulate charged particle beams is left to the specialized texts.

An idealized quadrupole magnet has the transverse cross section shown in Fig. 2.4, which also defines the Cartesian coordinate system to be used in the remainder of this section. As one can see, the polarities of the pole pieces alternate. Following the usual convention, the longitudinal coordinate, *z*, is taken to be directed along the beam and, in this case, "into the paper" along the **optic axis** of the quadrupole. Positive values of the *y*-coordinate measure upward deviations from the optic axis while positive values of the *x*-coordinate measure deviations from the optic axis to "beam left", to maintain consistency with the familiar **right-hand rule**.



Fig. 2.4 Cross section of a typical quadrupole magnet. The pole pieces are of opposite magnetic polarities, denoted "N" and "S", and are of hyperbolic shapes. A Cartesian coordinate system is used in which x and y denote transverse coordinates while z is along the desired beam trajectory, the optic axis of the beam optical system. In this figure, the beam enters the quadrupole <u>into</u> the paper along the positive z axis. The curves with arrows denote magnetic field lines. [Adapted from (Ca87).]

Often in the accelerator magnets themselves and nearly always in beam lines transmitting extracted particles, the electromagnetic fields vary only slowly with time or are static compared with the particle transit times. Under these conditions, it is shown in other texts that if the shape of the pole pieces are hyperbolae described by equations of form $xy = \pm k$, where k is a constant, and if the pole pieces are uniformly magnetized, then the components of the magnetic field within the gap containing the beam are given by

$$B_x = -\frac{B_o}{a} y = -gy \text{, and}$$
(2.29a)

$$B_y = -\frac{B_o}{a}x = -gx.$$
 (2.29b)

Here, *a* is the gap dimension as defined in Fig. 2.4 and B_o is the magnitude of the magnetic field strength at the pole pieces. The parameter *g* is, quite naturally, called the **gradient** of the quadrupole and in this scheme has units of Tesla meter⁻¹. This configuration defines an ideal quadrupole, which is of length, *L*.

Now examine qualitatively what happens to a particle having positive charge that enters this magnet parallel to the *z*-axis. If the particle trajectory is along the optic axis, then it

will not be deflected at all since $B_x = B_y = 0$. If, however, the particles enter the magnet parallel to the optic axis but with some finite *positive* value of y, it will receive a deflection toward *smaller* values of y in accordance with the right hand rule and Eq. (2.25). Likewise, if it enters with a finite *negative* value of y, it will receive a deflection toward *less negative* values of y. Thus, a beam of such particles is said to be **focussed** in the yz plane. However, if the particle enters with a finite positive value of x, it will be deflected toward a *larger* value of x, away from the optic axis. Finally, a particle incident with a finite negative value of x will similarly be deflected away from the optic axis. Thus, a beam of such particles is said to be **defocussed** in the xz plane. From this qualitative discussion it should be evident that more than one quadrupole is needed to achieve a net focussing effect.

Considering just the situation in the yz plane, it is easy to see that the analogy with geometrical optics is instructive even in mathematical detail. For a particle entering with coordinate y, one can substitute into Eq (2.28) and find that the angular deflection, if within the aperture of the magnet, is given by

$$\Delta \theta = \frac{0.29979qLgy}{p} \text{ (radians)}, \tag{2.30}$$

where the same units as Eq. (2.28) have been employed, with g (Tesla meter⁻¹) and y (meters) inserted. If the incident particle trajectory is parallel with the z-axis, the situation is schematically shown in Fig. 2.5a. It should be pointed out that in schematic drawings of beam optics, it is customary to show convex lenses to denote focussing elements and concave lenses to represent defocussing elements pertinent to a given plane. Bending magnets are correspondingly represented by prisms in such drawings.

Applying simple trigonometry, one finds that after deflection in this situation, the particle trajectory will intercept the *z*-axis at a distance, f, given as follows:

$$f = \frac{y}{\tan \Delta \theta} \approx \frac{y}{\Delta \theta} = \frac{p}{0.29979qLg},$$
(2.31)

since the deflection, $\Delta \theta$, is small. This approximation is called the **thin lens** approximation. In recognition of the fact that *f* is independent of the *y* coordinate, it is called the **focal length** of the quadrupole. By analogy with optical thin lenses, one can write down **the thin lens equation** which gives the relationship between the image distance, z_i , and the object distance, z_o , for other rays as follows:

$$\frac{1}{z_o} + \frac{1}{z_i} = \frac{1}{f}.$$
(2.32)



Figure 2.5 Configurations of quadrupole lenses are shown with the symbolism explained in the text: **a**) Representation of focusing in the yz plane of a beam trajectory incident from the left parallel to the *z*-axis. A *real* image is formed at the focal length, *f*, from the lens. **b**) Representation of defocusing in the yz plane. The parallel beam is deflected so that it appears to emerge from a point a distance *f* before the lens, thus, forming a *virtual* image. **c**) Representation of a particle trajectory in the yz plane of a quadrupole doublet. The particle enters a quadrupole doublet parallel to the *z*-axis from the left. First a focusing quadrupole (quad 1) is encountered and then a defocusing quadrupole (quad 2) follows. **d**) Representation of a particle trajectory in the *xz* plane of the same doublet. The particle enters the doublet parallel to the *z*-axis. In this plane, the defocusing quadrupole is encountered first.

In this equation, z_o and z_i are > 0 if the object is to the left of the lens and the image is to the right of the lens, forming a *real* image, for a focussing lens with f > 0. The situation for the defocussing plane, here the xz plane, is shown in Fig. 2.5b as a concave lens. For that plane, the equations are still workable if one applies a negative sign to the value of f and understands that a value of $z_i < 0$ describes a *virtual* image.

The simplest configuration of quadrupole magnets is in the form of a pair of two such magnets. In a given plane, say the yz, the first would be focussing while the second would be defocussing. In the orthogonal plane, here the xz, the defocussing quadrupole would thus be encountered first. Generally, these magnets will be of identical dimensions and have gradients of similar magnitudes. Such a **quadrupole doublet** is shown in Figs 2.5c and 2.5d for the yz and xz planes, respectively.

Eq. (2.32) can now be employed to explore how a quadrupole doublet can focus a parallel beam in both the xz and yz planes in a simple example. For the sake of this discussion, the quadrupoles, quad 1 and quad 2, have different focal lengths, f_1 and f_2 , respectively, and are separated by distance d. Quad 1 is focussing in the yz plane. As one would do in geometrical optics, for an incoming parallel beam, the object distance relative to quad 1 is $z_{yol} \rightarrow \infty$. Thus, the image distance from quad 1 is at $z_{yil} = f_1$. The object distance of this image from quad 2 is thus $z_{yo2} = d - f_1$. Relative to quad 2, the location of the final image will be at z_{yi2} by means of the thin lens equation;

$$\frac{1}{z_{\gamma i2}} = \frac{1}{-f_2} - \frac{1}{d - f_1},$$
(2.33)

where the negative coefficient of f_2 explicitly incorporates the fact that lens 2 is *defocussing* in the *yz* plane. Solving,

$$z_{yi2} = \frac{f_2(f_1 - d)}{f_2 - f_1 + d}.$$
(2.34a)

If the quadrupoles are identical $(f = f_1 = f_2)$, then,

$$z_{yi2} = \frac{f(f-d)}{d}.$$
 (2.34b)

It is simple to follow the same procedure for the xz plane to obtain the corresponding image distance, z_{xi2} ,

$$z_{xi2} = \frac{f_2(f_1 + d)}{f_1 - f_2 + d}.$$
(2.35a)

With identical quadrupoles, this becomes

$$z_{xi2} = \frac{f(f+d)}{d}.$$
 (2.35b)

One should notice that with identical quadrupoles,

$$z_{xi2} - z_{yi2} = 2f , \qquad (2.36)$$

a result that should not be surprising given that particles in xz plane are first subject to *defocussing*, and thus become *more* divergent, prior to their being focussed. The average focal length of the system for both the xz and yz planes is thus f^2/d . More sophisticated schemes such as quadrupole triplets and non-identical magnets can be used, where needed, to obtain a specialized beam envelope. These advanced methods are discussed in great detail, for example, by Carey (Ca87).

In this simple exposition, a number of significant effects have been ignored. First, a typical particle beam will contain some spread in particle momenta. The derivation given above ignores the fact that **dispersion** will occur in the magnetic fields in the same way that prism disperses a visible beam of "white" light into the various colors. There also may be **aberrations** or distortions of an image. One such aberration is called **chromatic aberration**, analogous to its namesake encountered in geometrical optics. For particle beams chromatic aberration is due to the dependence of focal length on particle momentum evident from Eq. (2.31). Also, the fact that no particle beam is ever completely parallel or completely emergent from a geometrical point has also been ignored.

All particle beams possess a property called **transverse emittance**. This quantity is expressed in units of angular divergence times physical size, typically in units of π mmmradian. The explicit display of the factor π is a matter of custom. The emittance concept is used to describe both longitudinal and transverse phenomena and is discussed by Carey (Ca87) and by Edwards and Syphers (Ed93). The discussion here is limited to transverse emittance. During the process of accelerating particles, the beam emittance in general becomes smaller because the normalized transverse emittance [the emittance when multiplied by the relativistic factors $\gamma\beta$ from Eqs. (1.10) and (1.11)] is an *invariant*. Thus, as velocity increases, the unnormalized emittance must decrease since the product $\gamma\beta$ increases with particle momentum. There are exceptions to this generalization beyond the scope of this discussion. Once a beam is no longer subject to accelerating electromagnetic fields (e.g. by RF waves) in an accelerator, the emittance can generally no longer be made smaller and can only increase due to processes such as multiple Coulomb scattering, space charge effects, etc.⁶ Under conditions in which the emittance

⁶ Under some conditions not discussed further in this text, synchrotron radiation can, in fact, reduce the transverse emittance.

is constant, the product of the angular divergence of the beam envelope and the transverse size of the beam envelope is conserved.⁷ This means that efforts made to focus the beam tightly into a smaller cross-sectional size will unavoidably result in a beam with a correspondingly larger angular spread. Likewise, attempts to create a parallel beam (one with essentially no angular spread) will result in a correspondingly larger beam size.

As a final word, one should be aware of the fact that the above discussion of quadrupoles depends upon the beam axis coinciding with the optic axis. Should the beam enter a quadrupole with its center far off-axis, it should be obvious that the entire beam will be deflected nearly as if a quadrupole were a dipole magnet of equivalent field strength and length (see Fig. 2.4). Beams that are deflected in this manner by a quadrupole are said to have suffered **steering**. The steering of beams can constitute significant loss points in the beam transport system.

⁷ This is a consequence of **Liouville's theorem** of classical dynamics as applied to the coordinate system defined here which requires that the volume of the phase space defined by the transverse spatial coordinates; *x* and *y*, and their corresponding "conjugate" momentum components, p_x and p_y ; is conserved. Since in this Cartesian coordinate system, the momentum components p_x and p_y are, in small angle approximation, directly proportional to the angles (in radians) between the momentum vector and the *x* and *y* coordinate axes, respectively, the assertion made above directly follows. Other texts address this point in more detail (e.g., Ca87).

Problems

- 1. This problem gives two elementary examples of Monte Carlo techniques that are almost "trivial". In this problem, obtaining random numbers from a standard table or from a hand calculator should be helpful.
 - a) First, use a random number table or random number function on a calculator along with the facts given about the cumulative probability distribution for exponential attenuation to demonstrate that, even for a sample size as small as, say, 15, the mean value of paths traveled is "within expectations" if random numbers are used to select those path lengths from the cumulative distribution. Do this, for example, by calculating the mean and standard deviation of your distribution.
 - b) An incident beam is subjected to a position measurement in the coordinate *x*. It is desirable to "recreate" incident beam particles for a shielding study using Monte Carlo. The *x* distribution as measured is as follows:

x	#
0	0
1	1
2	2
3	3
4	4
5	5
6	4
7	3
8	2
9	1
10	0

Determine, crudely, p(x), P(x) and then use 50 random numbers to "create" particles intended to represent this distribution. Then compare with the original one which was measured in terms of the average value of x and its standard deviation. Do <u>not</u> take the time to use interpolated values of x, simply round off to integer values of x for this demonstration.

2. A beam of protons having a kinetic energy of 100 GeV is traveling down a beam line. The beam is entirely contained within a circle of diameter 1 cm. All of the beam particles have the same kinetic energy. An enclosure further downstream must be protected from the beam or secondary particles produced by the beam by shielding it with a large diameter iron block that is 20 cm in radius centered on the beam line. The beam passes by this block by being deflected by a uniform field magnet that is 3 meters long, the longitudinal center of which is located 30 meters upstream of the iron block. Calculate the magnetic field, *B*, that is needed to accomplish this objective.

3.1 Introduction

In this chapter the major features of the prompt radiation fields produced by electrons are described. An extensive discussion of the electromagnetic cascade and of the shielding of photoneutrons and high energy particles that result from these interactions is given. The utilization of Monte Carlo calculations in electron shielding problems is also addressed. The material presented in this chapter is useful for understanding electron, photon, and photoneutron radiation from electron accelerators used in medicine and in high energy physics research. As has been pointed out by Silari et al. (Si99), some of the content discussed in this chapter is also useful in understanding the radiation that may be produced by certain accelerator components, such as RF cavities (including superconducting ones), even when operated apart from the main accelerator.

3.2 Unshielded Radiation Produced by Electron Beams

At all energies photons produced by **bremsstrahlung** dominate the unshielded radiation field aside from the hazard of the direct beam. As the energy increases, neutrons become a significant problem. For electrons having kinetic energy E_o approaching 100 MeV, the **electromagnetic cascade** is of great importance. A useful rule of thumb is that electrons have a finite ionization range, R, in any material that monotonically increases with the initial kinetic energy, E_o , (MeV). For $2 < E_o < 10$ MeV,

$$R = 0.6E_o \,(\mathrm{g}\,\mathrm{cm}^{-2}). \tag{3.1}$$

In air at standard temperature and pressure (STP) over this energy domain, R (meters) $\approx 5 E_o$ (MeV). Above an energy of 10 MeV or so, a threshold that we will see is dependent upon the absorbing medium, the loss of energy begins to be dominated by **radiative processes**, whereby photons that are emitted begin to dominate over those losses of energy due to collisions. This transition will be discussed further in Section 3.2.2.

3.2.1 Dose Equivalent Rate in a Direct Beam of Electrons

At any accelerator, the dose equivalent rate in the direct particle beam is generally larger than in any purely secondary radiation field. This is certainly true at electron accelerators. Swanson (Sw79a) has given a rule of thumb, said to be "conservative", for electrons in the energy domain of $1 < E_o < 100$ MeV;

$$\frac{dH}{dt} = 1.6 \times 10^{-4} \phi \,, \tag{3.2}$$

where dH/dt is the dose equivalent rate (rem h⁻¹) and ϕ is the flux density (cm⁻² s⁻¹) in the electron beam. One of the problems at the end of this chapter examines the domain of validity of this approximation. The coefficient is 1.6 x 10⁻⁶ if dH/dt is to be in Sv h⁻¹ with ϕ remaining in units of cm⁻² s⁻¹.

3.2.2 Bremsstrahlung

Bremsstrahlung is the radiative energy loss of charged particles, especially electrons, as they interact with materials. It appears in the form of photons. An important parameter when considering the radiative energy loss of *electrons* in matter is the **critical energy**, E_c . The critical energy is the energy above which the radiative loss of energy exceeds that due to ionization. There are several formulae used to calculate E_c , representative ones are given here. For electrons, the value of E_c is a smooth function of atomic number, approximated by

$$E_c = \frac{800 \text{ (MeV)}}{Z+1.2},$$
 (3.3a)

where Z is the atomic number of the material. For *muons* in solid materials (see Section 1.4.1) the corresponding critical energy, $E_{c,muon}$, is much larger and differs for solid and gaseous media (PDG04);

$$E_{c,muon} = \frac{5700 \text{ GeV}}{(Z+1.47)^{0.838}} \text{ (solids), and } E_{c,muon} = \frac{7980 \text{ GeV}}{(Z+2.03)^{0.879}} \text{ (gases).}$$
(3.3b)

The transition from dominance by ionization to dominance by radiation is a smooth one. The total stopping power for electrons or muons may be written as the sum of collisional and radiative components, respectively;

$$\left(\frac{dE}{dx}\right)_{tot} = \left(\frac{dE}{dx}\right)_{coll} + \left(\frac{dE}{dx}\right)_{rad}.$$
(3.4)

Another parameter of significant importance is the **radiation length**, X_o , which is the mean thickness of material over which a high energy electron loses all but 1/e of its energy by bremsstrahlung. This parameter is the approximate scale length for describing high energy electromagnetic cascades, supplanting the ionization range for even moderate electron energies. It also plays a role in the "scaling" of multiple Coulomb scattering for all charged particles and was discussed in that context in Section 1.4.2. The radiation length is approximated by Eq. (1.21). For energetic electrons, the fractional energy loss is equal to the fraction of a radiation length it penetrates;

$$\frac{dE_{rad}}{E} = -\frac{dx}{X_0}, \text{ thus } \left(\frac{dE}{dx}\right)_{rad} = -\frac{E}{X_0}, \quad (3.5)$$

so that under these conditions (i.e., where loss by ionization can be neglected), the energy of the electron, E, as a function of thickness of shield penetrated, x, is given by

$$E(x) = E_o \exp(-x/X_o),$$
 (3.6)

where the energy of the incident particle is E_o and x and X_o are in the same units.



Fig. 3.1 Bremsstrahlung efficiency for electrons stopped in various materials. This is the fraction (in per cent) of the kinetic energy of incident electrons converted to radiation as a function of incident energy E_o . The remainder of the kinetic energy is transferred to the medium by ionization. [Adapted from (Sw79a).]

Figure 3.1 gives the percentage of energy E_o that appears as radiation for various materials as a function of energy. External bremsstrahlung develops as a function of target thickness and is described by a **transition curve**. As the thickness increases, the intensity of the radiation increases until re-absorption begins to take effect. Then, self-shielding begins to take over. One talks about conditions at the maximum as being a "thick-target" bremsstrahlung spectrum. This phenomenon becomes dominant above energies of about 100 MeV for low atomic number ("low-Z") materials and above 10 MeV for high atomic number ("high-Z") materials.

The energy spectrum of the radiated photons ranges from zero to the energy of the incident electron and the number of photons in a given energy interval is approximately inversely proportional to the photon energy. The amount of energy radiated per energy interval is practically constant according to Schopper et al. (Sc90). Detailed spectral information for bremsstrahlung photons has been provided by various workers. Figures 3.2 and 3.3 are provided as examples of such spectra at moderate electron beam energies. Bremsstrahlung spectra are noticeably more energetic (i.e., "harder") at forward angles.

For thin targets of thickness x ($x \ll X_o$), the spectrum of photons of energy k per energy interval dk, dN/dk, can be approximated by

$$\frac{dN}{dk} \approx \frac{x}{X_o k} \,. \tag{3.7}$$

Thick targets may require consideration of the electromagnetic cascade. In general, the spectra fall as $1/k^2$ at $\theta = 0$ and even faster at larger angles (Sw79a).

A more detailed parameterization of the normalized total photon differential yield per incident electron, $dN/d\Omega$, for photons of all energies has been reported by Swanson and Thomas (Sw90), with improvements suggested by Nelson (Ne97);

$$\frac{1}{E_o} \frac{dN}{d\Omega} = 4.76E_o \exp(-\theta^{0.6}) + 1.08 \exp(-\theta/72) \text{ (photons sr}^{-1} \text{ GeV}^{-1} \text{ electron}^{-1}\text{).}$$
(3.8)

This expression is normalized to results involving iron and copper targets of thicknesses of about 17 X_o at $E_o = 15$ GeV. In Eq. (3.8), E_o is in GeV and θ is in degrees. As will be shown below, this formalism is especially useful as a source term in thick shields and is particular valid for scattering angles around 90 degrees.



Fig. 3.2 Bremsstrahlung spectra measured at zero degrees from intermediate thickness $(0.2 X_o)$ targets of high atomic number (Z) material. The data points are measurements of O'Dell et al. (OD68) [adapted by Swanson (Sw79a)].



Fig. 3.3 Spectra of bremsstrahlung photons emerging in various directions from thick tungsten targets irradiated by normally incident monoenergetic electron beams at two different energies. The target thickness at both energies (z) is twice the mean electron ionization range, r_o , given by the continuous slowing down approximation. The arrows indicate the abundant positron annihilation radiation at 0.511 MeV. **a**) Kinetic energy 30 MeV, thickness = 24 g cm⁻² (3.6 X_o); **b**) 60 MeV, thickness = 33 g cm⁻² (4.9 X_o). [Adapted from Berger and Seltzer (Be70) by Swanson (Sw79a).]

The three **Swanson's Rules of Thumb** parameterize this behavior for the absorbed dose rates, dD/dt, normalized to one kW of incident beam power for E_o in MeV, expected at one meter from a point "target" of high atomic number, Z (Sw79a):

Swanson's Rule of Thumb 1; $\frac{dD}{dt} \approx 20E_o^2 \text{ (Gy m}^2)(\text{kW}^{-1}\text{h}^{-1}) \text{ at } \theta = 0^\circ, E_o < 15 \text{ MeV}. \tag{3.9}$

Swanson's Rule of Thumb 2;

$$\frac{dD}{dt} \approx 300E_o \text{ (Gy m}^2)(\text{kW}^{-1}\text{h}^{-1}) \text{ at } \theta = 0^\circ, E_o > 15 \text{ MeV}.$$
(3.10)

Swanson's Rule of Thumb 3;

$$\frac{dD}{dt} \approx 50 \quad (\text{Gy m}^2)(\text{kW}^{-1}\text{h}^{-1}) \text{ at } \theta = 90^{\circ}, E_o > 100 \text{ MeV}.$$
(3.11)

It should be noted that higher absorbed dose rates at 90° can arise in certain circumstances due to the presence of softer radiation components. In Eq. (3.11), the value of 50 is sometimes increased to a value of 100 to better describe measurements (Fa84). For point-like sources, one can scale these results to other distances (in meters) by using the inverse square law. Figure 3.4 shows the behavior for a high-Z target. The forward intensity is a slowly varying function of target material except at very low values of Z.



Fig. 3.4 Thick target bremsstrahlung from a high atomic number target. Absorbed dose rates at 1 meter per unit incident electron beam power (kW) are given as a function of incident electron energy E_0 . The dashed lines represent a reasonable extrapolation of the measured values. The dose rates measured in the sideward direction (smoothed for this figure) depend strongly on target and detector geometry and can vary by more than a factor of two. The dashed line at 90° represents the more penetrating radiation component to be considered in room shielding. [Adapted from (Sw79a).]

The value of θ where the intensity in the forward lobe has half of its maximum intensity, $\theta_{1/2}$, is approximately given by a relation due to Swanson (Sw79a);

$$E_0 \theta_{1/2} = 100 \text{ (MeV degrees).} \tag{3.12}$$

Alternatively, according to Schopper et al. (Sc90) the average angle of emission is of the order of m_e/E_o (radians) where m_e is the rest mass (in energy units, e.g., MeV) of the electron.

At higher energies (E_o greater than approximately 100 MeV), the electromagnetic cascade development in accelerator components is very important and can result in a forward "spike" of photons with a characteristic angle of $\theta_c = 29.28/E_o$ (degrees, if E_o is in MeV). At $\theta = \theta_c$ the intensity of the spike has fallen to 1/e of its value at $\theta = 0$.

A formula for the unshielded bremsstrahlung dose equivalent at one meter, H_{brem} , that works reasonably well for all angles that approximates the results of Eqs. (3.10) and (3.11) and which incorporates Eq. (3.12) for values of $E_0 \ge 100$ MeV is

$$H_{brem} = E_0 [1.33E_0 \exp(-E_0 \theta / 2.51) + 133 \exp(-\theta / 0.159) + 3 \exp(-\theta / 0.834)]$$
 [(Sv m² electron⁻¹) x 10⁻¹⁷], (3.12a)

where E_o is in MeV and θ is, here, in radians (NC03). In this formula, the "doubling" suggested by (Fa84) for Eq. (3.11) is been included.

3.2.3 Synchrotron Radiation

Swanson (Sw90) presents a summary discussion of this important phenomenon restated in this section. A more complete discussion of this phenomenon and its radiation protection ramifications is provided in Appendix B. The movement of electrons in a circular orbit results in their centripetal acceleration. This gives rise to emission of photons. At nonrelativistic energies, this radiation is largely isotropic. However, for relativistic energies, a condition readily achievable for accelerated electrons, the photons emerge in a tight bundle along a tangent to any point on a circular orbit. Figure 3.5 shows this bundle. The characteristic angle (i.e., the angle of 1/e of the zero degree intensity) of this "lobe" is

$$\theta_c = \frac{1}{\gamma} = \sqrt{1 - \beta^2} \text{ radians.}$$
(3.13)

The median energy of the power spectrum, sometimes called the characteristic energy, ε_c , is given in terms of the total energy, W (GeV), and bending radius, R (meters)

by
$$\mathcal{E}_{c} = \frac{2.218W^{3}}{R}$$
 (keV). (3.14)

For singly-charged particles of other masses, m_x , the characteristic energy is obtained by multiplying this result by a factor of $(m_e/m_x)^3$.

The radiated power, P, for a circulating electron current, I (milliamperes), is

$$P = \frac{88.46W^4 I}{R} \text{ (watts).}$$
(3.15)

For singly-charged particles of other masses, m_x , the radiated power is obtained by multiplying this result by a factor of $(m_e/m_x)^4$. More details on this subject, including those related to the angular distributions and spectra of the emitted photons, have been given in various texts with a good summary provided by the Particle Data Group (PDG04). Fig. 3.6 gives the universal radiation spectrum for high energies.



Fig. 3.5 Synchrotron radiation pattern for relativistic particles at the instantaneous location denoted by "electrons". Twice the opening angle, θ_c , is shown as the shaded region.



Fig. 3.6 Universal synchrotron radiation spectrum. The graph gives the relative power as a function of photon energy in units of the characteristic energy, ε_c . This spectrum yields unity if integrated over all energies. [Adapted from (Sw90).]

3.2.4 Neutrons

3.2.4.1 Giant Photonuclear Resonance Neutrons

Neutron production can be expected to occur in any material irradiated by electrons in which bremsstrahlung photons above the material-dependent threshold are produced. This threshold varies from 10 to 19 MeV for light nuclei and 4 to 6 MeV for heavy Thresholds of 2.23 MeV for deuterium and 1.67 MeV for beryllium are nuclei. noteworthy exceptions. Between this threshold and approximately 30 MeV, a production mechanism known as the giant photonuclear resonance is the most important source of neutron emission from material. Swanson (Sw79a) has given a detailed description of this process that is summarized here. A simple picture of this phenomenon is that the electric field of the photon produced by bremsstrahlung transfers its energy to the nucleus by inducing an oscillation in which the protons as a group move oppositely to the neutrons as a group. This process has a broad maximum cross section at photon energies, k_{o} , between about 20-23 MeV for light nuclei for materials having mass numbers A less than about 40. For heavier targets, the peak is at an energy of approximately $k_o = 80A^{-1/3}$ MeV. Schopper et al. (Sc90) have provided a great deal of data on the relevant cross sections. It turns out that the yield, Y, of giant resonance neutrons at energies above approximately $2k_o$ is nearly independent of energy and nearly proportional to the beam power.

This process may be thought of as one in which the target nucleus is excited by the electron and then decays somewhat later by means of neutron emission. It is a (γ, n) nuclear reaction, written in the scheme of notation in which the first symbol in the parentheses represents the incoming particle in a reaction while the second represents the outgoing particle. In this process the directionality of the incident electron or photon is lost so that these emissions are **isotropic**. Because of this isotropicity, the inverse square law may be used to estimate the flux density at any given distance r. The spectrum of neutrons of energy E_n is similar to that seen in a fission neutron spectrum and can be described as a **Maxwellian** distribution;

$$\frac{dN}{dE_n} = \frac{E_n}{T^2} \exp(-E_n / T), \qquad (3.16)$$

where *T* is a **nuclear "temperature"** characteristic of the target nucleus and its excitation energy, *T*, in energy units, is generally in the range 0.5 < T < 1.5 MeV. For this distribution, the most probable value of $E_n = T$ and the average value of $E_n = 2T$. This process generally is the dominant one for incident photon kinetic energies $E_o < 150$ MeV. The excitation functions of total neutron yields in various materials are plotted in

Fig. 3.7. Table 3.1 gives the high energy limits for total yield, Y_n , of giant resonance neutrons per watt of beam power (s⁻¹W⁻¹), the isotropic differential neutron yield, $dY_n/d\Omega$ (GeV⁻¹ sr⁻¹) per unit of beam energy per electron, and a recommended dose equivalent source term, S_n , (Sv cm² GeV⁻¹) per unit beam energy per electron to be used as follows:

$$H = \frac{S_n}{r^2} E_0 I , \qquad (3.17)$$

where *H* is the dose equivalent in Sieverts, *r* is the radial distance from the target in cm, E_o is in GeV, and *I* is the total number of beam particles incident (e.g., during some time interval). For electron energies below 500 MeV, appropriate values can be obtained by scaling the Table 3.1 entries according to the Fig. 3.7 curves. The agreement with various experiments is quite good according to Schopper et al. (Sc90). The use of these "saturation" values can support reasonable, but conservative, estimates.



Fig. 3.7 Neutron yields from infinitely thick targets per kW of electron beam power as a function of electron beam energy E_o , ignoring target self-shielding. [Adapted from (Sw79b).]

Table 3.1 Total neutron yield rate per unit beam power (s⁻¹ watt⁻¹), differential yield per unit electron energy (GeV⁻¹ sr⁻¹) per electron, and source term per unit electron energy (Sv cm² GeV⁻¹) per electron for giant resonance neutrons in an optimum target. No energy dependence "near threshold" is assumed. The neutrons are distributed uniformly over all directions (4π steradians). These results are best used for $E_0 > 0.5$ GeV. [Adapted from (Sw79b) and (Sc90).]

Material	Total Neutron	Differential Neutron	Recommended Source Terms",	
	Production	Yield	S_n	
	Y_n	$dY_n/d\boldsymbol{\Omega}$		
	$(s^{-1}W^{-1})$	(GeV ⁻¹ sr ⁻¹) per electron	(Sv cm ² GeV ⁻¹) per electron	
С	4.4×10^8	5.61 x 10 ⁻³	4.3×10^{-12}	
Al^b	6.2×10^8	7.90 x 10 ⁻³	$6.0 \ge 10^{-12}$	
Fe	$8.18 \ge 10^8$	1.04 x 10 ⁻²	7.7×10^{-12}	
Ni	$7.36 \ge 10^8$	9.38 x 10 ⁻³	$6.9 \ge 10^{-12}$	
Cu	1.18 x 10 ⁹	1.50 x 10 ⁻²	$1.1 \ge 10^{-11}$	
Ag	1.68 x 10 ⁹	2.14 x 10 ⁻²	$1.5 \ge 10^{-11}$	
Ba	1.94 x 10 ⁹	2.47 x 10 ⁻²	$1.8 \ge 10^{-11}$	
Та	2.08×10^9	2.65 x 10 ⁻²	$1.8 \ge 10^{-11}$	
W	2.36 x 10 ⁹	3.01 x 10 ⁻²	2.0×10^{-11}	
Au	2.02×10^9	2.58 x 10 ⁻²	$1.8 \ge 10^{-11}$	
Pb	2.14 x 10 ⁹	2.73 x 10 ⁻²	$1.9 \ge 10^{-11}$	
U	3.48 x 10 ⁹	4.44 x 10 ⁻²	3.0×10^{-11}	

^aTo get Sv cm² h⁻¹kW⁻¹, multiply this column by 2.25 x 10^{16} .

^bThe value for aluminum is also recommended for concrete.

3.2.4.2 Quasi-Deuteron Neutrons

At energies above the giant resonance, the dominant neutron production mechanism is one in which the photon interacts with a neutron-proton pair within the nucleus rather than with the whole nucleus. The **quasi-deuteron effect** is so-named because for $E_o \approx 30$ MeV the photon wavelength is near resonance with the average inter-nucleon distance so that the photon interactions tend to occur with "pairs" of nucleons. Only neutron-proton pairs have a nonzero electric dipole moment, which makes interactions of photons with such pairs (pseudo-deuterons) favorable. This mechanism is important for $30 < E_o < 300$ MeV and has been described by Swanson (Sw79b). An important general effect due to this mechanism is to add a tail of higher-energy neutrons to the giant resonance spectrum. For $5 < E_n < E_o/2$ (MeV), the nearly isotropic spectrum of quasi-deuteron neutrons is given by

$$\frac{dN}{dE_n} = E_n^{-\alpha} \text{ where, approximately, } 1.7 < \alpha < 3.6.$$
(3.18)

The slope becomes steeper as E_o , the kinetic energy of the incident electron, is approached. Eq. (3.18) is for *thin* targets. For *thick* target situations, the fall-off with E_n is generally steeper. Since the mechanism is the (γ , np) reaction and the neutron and the proton are nearly identical in mass, they share the available energy equally so that the yield of neutrons due this mechanism is essentially zero for neutrons having kinetic

energy $E_n > E_0/2$. In general, the quasi-deuteron neutrons are fewer in number and generally less important than are the giant resonance neutrons. Shielding against the latter will usually provide adequate protection against the former for shielding purposes, but should not be neglected for questions where the fluences of particularly energetic neutrons may be important.

3.2.4.3 Neutrons Associated with the Production of Other Particles

There are interactions in which the production of other elementary particles, perhaps best typified by pions, becomes energetically possible at still higher energies (say, $E_o > 300$ MeV). These particles can then produce neutrons through secondary interactions as will be discussed in Chapter 4. The neutrons from this source tend to dominate the lateral shielding requirements in the GeV region. DeStaebler (De65) has parameterized the measured yields of high energy particles per incident electron;

$$\frac{d^2 Y_n}{dEd\Omega} = \frac{7.5 \times 10^{-4}}{(1 - 0.75 \cos \theta)^2 A^{0.4}} \quad (\text{GeV}^{-1} \text{sr}^{-1}), \qquad (3.19)$$

where A is the atomic mass (g mole⁻¹) of the target material. It is reasonable to use a dose equivalent per fluence conversion factor of approximately 1×10^{-13} Sv m² ($10^{-3} \mu$ Sv cm²) for these neutrons (see Fig. 1.5). Obviously, these neutrons are forward-peaked, not isotropically distributed.

In general photons are produced more copiously, but the neutrons can be more difficult to shield.

3.2.5 Muons

With electron beams, muons become of significance above an electron energy of approximately 211 MeV, the threshold of the process in which a μ^{\pm} pair is produced in a **pair production** process quite analogous to the more familiar one in which an electron-positron pair results from photon interactions. They can be produced, with much smaller yields, at electron accelerators by the decay of π^{\pm} and K[±] which are, in turn, due to secondary production processes exemplified by photo-pion creation. Such **decay muons**, which are more prominent at hadron accelerators, will be discussed in Section 4.2.4. A detailed theoretical treatment of muon production by incident electrons is given by Nelson (Ne68 and Ne74). Figure 3.8 gives the muon flux density as a function of electron energy at $\theta = 0^{\circ}$ while Fig. 3.9 shows an example of the angular dependence of these yields at $E_o = 20$ GeV. The reasonableness of scaling with energy to larger values of E_o is well demonstrated.

Obviously, the range-energy relation of muons and considerations related to their energy loss mechanisms discussed in Section 1.4.1 is relevant to shielding against muons regardless of their origin.



Fig. 3.8 Muon production at $\theta = 0^{\circ}$ from an unshielded thick iron target at one meter, as a function of electron energy, E_{0} . [Adapted from (Ne68a) and (Ne74).]



Fig. 3.9 Integrated muon flux density at 1 meter per kW of electron beam power as a function of muon energy for 20 GeV electrons incident on a thick iron target at several values of θ . The integral of the flux density over energy includes all muons that have energies that exceed the value of the abscissa at the specified value of θ . [Adapted from (Ne68a) and (Ne74).]

3.2.6 Summary of Unshielded Radiation Produced by Electron Beams

Swanson (Sw79a) has illustrated the broad features of the radiation field due to the unshielded initial interactions of electrons that is given in Fig. 3.10. This figure is useful for making crude estimates of the resultant radiation field. As one can see, at large angles, from the standpoint of dose equivalent, the unshielded field is always dominated by photons. At small angles, the field is dominated by photons at the lower energies with muons increasing in importance as the energy increases to large values. The production of induced radioactivity will be discussed in Chapters 7 and 8.



Fig. 3.10 Dose-equivalent rates per unit primary electron beam power at one meter produced by various types of "secondary" radiations from a high-Z target as a function of primary beam energy, if no shielding were present (qualitative). The width of the bands suggests the degree of variation found, depending on such factors as target material and thickness. The angles at which the various processes are most important are indicated. [Adapted from (Sw79a).]

3.3 The Electromagnetic Cascade-Introduction

As a prelude to discussing the electromagnetic cascade process, one must look a bit more at the dose equivalent due to thick target bremsstrahlung dose at large values of θ for targets surrounded by cylindrical shields. The situation is given in Fig. 3.11.



Fig. 3.11 Target and shielding geometry for the estimation of dose equivalent due to electron beam interactions with a target surrounded by a cylindrical shielding. L is the length of the target and the other parameters specify the geometry.

Returning to Eq. (3.8), the results of Swanson and Thomas (Sw90) as improved by Nelson (Ne97) give the photon absorbed dose per incident electron, *D*, external to such a shield as;

$$D(\theta) = (1 \times 10^{-11}) \left\{ 10.2E_o \exp(-\theta^{0.6}) + 2.3\exp(-\theta/72) \right\} E_o \left(\frac{\sin \theta}{a+d} \right)^2 \exp\left(-\frac{\mu}{\rho} \frac{\rho d}{\sin \theta} \right)$$

(Gy/electron). (3.20)

As was the case for Eq. (3.8), this expression is normalized to results involving thick iron and copper targets at $E_0 = 15$ GeV. Here, E_0 is the electron energy in GeV, θ is in degrees, *a* is the target-to-shield distance (cm), *d* is the shield thickness (cm), ρ is the shielding material density (g cm⁻³), and μ/ρ is the attenuation coefficient equal to the value at the so-called **Compton minimum** which for concrete is 2.4 x 10⁻² cm²g⁻¹. The "Compton minimum" is the energy where the total photon cross section is at a minimum and the **photon mean free path**, λ_{γ} , is thus a maximum. The use of this term is somewhat inaccurate since the Compton scattering cross section *monotonically* decreases with energy. The minimum value of the total photon cross section always occurs at energies less than E_c and is typically a few MeV. Figures 3.12 and 3.13 give values of the photon mean free path for a variety of materials as a function of energy. Values for more materials, energies, and mixtures, are available from the National Institute of Standards and Technology.⁸

The major feature that needs to be considered in the shielding design at electron accelerators is the **electromagnetic cascade**. One should recall the definitions of **critical energy**, E_c and **radiation length**, X_o , that were given in Eqs. (3.3a), (3.3b), and (1.21),

⁸ Specifically, these data are found on a website at: http://physics.nist.gov/PhysRefData.



Fig. 3.12 Photon mean free path as a function of photon energy in various materials for low energies. [Adapted from (PDG04).]



Fig. 3.13 Photon mean free path as a function of photon energy in various materials for high energies. [Adapted from (PDG04).]

respectively. A related parameter of importance for describing the electromagnetic cascade is the **Molière radius**, X_m ;

$$X_m = X_o E_s / E_c, \tag{3.21}$$

in which

$$E_s = \left(\sqrt{\frac{4\pi}{\alpha}}\right) m_e c^2 = 21.2 \text{ MeV}, \qquad (3.22)$$

where α is the fine structure constant of atomic physics (see Table 1.1), and m_e is the mass of the electron. X_m is a good characteristic length for describing radial distributions in electromagnetic showers. Two additional dimensionless scaling variables are commonly introduced to describe electromagnetic shower behavior;

$$t = x/X_o$$
 (for longitudinal distance scaling) (3.23)

and
$$y = E/E_c$$
 (for energy scaling). (3.24)

For mixtures of *n* elements these quantities and also for the stopping power dE/dx scale according to the elemental fractions by weight, f_i , as follows:

$$\frac{dE}{dx} = \sum_{i=1}^{n} f_i \left(\frac{dE}{dx}\right)_i,$$
(3.25)

where all stopping powers are expressed as energy loss per unit areal density (e.g., MeV $cm^2 g^{-1}$) (PDG04).

For high energy photons ($E_o > 1$ GeV), the total e⁺e⁻ **pair production** cross section, σ_{pair} , is approximately given, for a single element, by

$$\sigma_{pair} = \frac{7}{9} \left(\frac{A}{X_0 N_A} \right) \quad (\text{cm}^2), \tag{3.26}$$

where A is the atomic weight, N_A , is Avogadro's number, and X_o is the radiation length expressed in units of g cm⁻². For energies larger than a few MeV, the pair production process dominates the total photon attenuation. The mean free path length for pair production, λ_{pair} , is thus given by

$$\lambda_{pair} = \frac{\rho}{N\sigma} (\text{g cm}^2) = \frac{\rho}{\frac{\rho N_A 7}{A 9} \left(\frac{A}{X_0 N_A}\right)} = \frac{9}{7} X_0.$$
(3.27)

The energy-independence and near-equality of λ_{pair} and X_o leads to the most important fact about the electromagnetic cascade:

The electrons radiatively produce photons with almost the same characteristic length for which the photons produce more $e^+ e^-$ pairs.

This is so important because as a first order approximation it means that the "size" in physical space is independent of energy. For **hadronic cascades**, we will later see that the results are considerably different and, one may daresay, more complicated.

3.4 The Electromagnetic Cascade Process





Fig. 3.14 Conceptual view of the development of an electromagnetic cascade in a semi-infinite medium. The solid lines represent electrons or positrons, the dashed lines represent photons, and the dotted lines represent neutrons. The shower is initiated by an electron or positron of energy E_o incident on the medium from the left. The spreading in the transverse direction is greatly exaggerated for clarity. Bremsstrahlung and pair production events are denoted by **B** and **P**, respectively. Compton scattering and ionization are both not shown but also play a roles in the dispersal of energy. Photonuclear reactions, as illustrated by the (γ , n) reaction at point N also play a role, albeit much more infrequently than inferred from this illustration. The process could just as well be initiated by a photon. [Adapted from (Sw79a).]

In the simplest terms, the electromagnetic cascade at an electron accelerator proceeds qualitatively according to the following steps:

- 1. A high energy electron $(E_o >> m_e c^2)$ produces a high energy photon by means of bremsstrahlung after traveling an average distance of X_o .
- 2. This photon produces an e⁺ e⁻ pair after traveling, on average, a distance of $\frac{9}{7}X_o$. Each member of the pair will have, on average, half the energy of the photon.
- 3. After traveling an average distance of X_{o} , each member of the e⁺ e⁻ pair will produce yet another bremsstrahlung photon.
- 4. Each electron or positron may continue on to interact again and release yet more photons before its energy is totally absorbed.

This chain of events can equally well be initiated by a high energy photon, even one produced in secondary interactions at a *hadron* accelerator. Eventually, after a number of generations, the individual energies of the electrons and positrons will be degraded to values below E_c so that ionization processes then begin to dominate and terminate the shower. Likewise, the photon energies eventually are degraded so that Compton scattering and the photoelectric effect compete with the further e⁺ e⁻ pair production.

Of course, there are subtleties representing many different physical processes, such as the production of other particles, which must be taken into account and are best handled by Monte Carlo calculations. A general discussion of the use of Monte Carlo techniques for such problems has been given by Rogers and Bielajew (Ro90). The most widely-used code incorporating the Monte Carlo method applied to electromagnetic cascades is **EGS** (electron gamma shower), which was written by W. R. Nelson and described by Nelson et al. (Ne85, Ne90) (see Appendix A). Van Ginneken developed the Monte Carlo program called **AEGIS** (Va78), which is very effective for calculating the propagation of such cascades through thick shields. Analytical approximations have been developed and are summarized elsewhere [e.g., (Sw79a), (Sc90)]. The results of published calculations are used in the following discussion to aid in improving the reader's understanding of electromagnetic cascades.

3.4.1 Longitudinal Shower Development

The dosimetric properties of the calculations of an electromagnetic cascade may be summarized in curves that give fluence, dose, or other quantities of interest as functions of shower depth or distance from the axis. Figure 3.15 shows the fraction of total energy deposited (integrated over all radii about the shower axis) versus longitudinal depth calculated by Van Ginneken and Awschalom (Va75). They introduced a longitudinal scaling parameter, ζ , given by

$$\zeta = 325(\ln Z)^{-1.73} \ln E_0 \quad (\text{g cm}^{-2}), \tag{3.28}$$

where E_o is in MeV and Z is the atomic number of the absorber. When the longitudinal coordinate is expressed in units of ζ , all curves approximately merge into this universal

one and are rather independent of target material.



Fig. 3.15 Fraction of total energy deposited by an electromagnetic cascade versus depth, *X*, integrated over all radii about the shower axis. See Eq. (3.28). [Adapted from (Va75).]

In their epic development of analytical shower theory, Rossi and Griesen (Ro41) using their so-called **Approximation B**, a more advanced formalism than their Approximation A, predicted for an *electron-initiated* shower that the total number of electrons and positrons at the shower maximum, N_{show} , are proportional to the primary energy as follows:

$$N_{show} = \frac{0.31 E_o / E_c}{\sqrt{\ln(E_o / E_c) - 0.37}} \,. \tag{3.29}$$

For a *photon-initiated* shower, a value of 0.18 should replace that of 0.37 in the denominator of Eq. (3.29). This distinction related to the initiator of the shower (electron/positron or photon), and others, reflect the deeper penetration of an initiating photon implied by the 9/7 factor in Eq. (3.27). The result embodied in the mathematical language of this equation is intuitively sensible since the final outcome of the shower is to divide the energy at the shower maximum among a number of particles with energies near E_c . One can obtain the maximum energy deposited per radiation length from Eq. (3.29) as the product $E_c N_{show}$ (Sc90).

Also from the Rossi-Griesen Approximation B, the location of the **shower maximum** t_{max} , [along the longitudinal coordinate in units of radiation length, see Eq. (3.23)] should be given by

$$t_{\max} = 1.01 \ln\left(\frac{E_o}{E_c}\right) - C_{show}, \text{ with } C_{show} = 1.$$
(3.30)

Experimentally, Bathow et al. (Ba67) found that values of $C_{show} = 0.77$ for copper and $C_{show} = 0.47$ for lead fit data better. Not surprisingly, photon-initiated showers penetrate about 0.8 radiation lengths deeper than do the electron-initiated showers. Schopper et al. (Sc90) simply give values of $C_{show} = 1$ and $C_{show} = 0.5$ for electron- and photon-initiated showers, respectively.

The longitudinal center of gravity, \overline{t} , of all the shower electrons is given by

$$\overline{t} = 1.009 \ln\left(\frac{E_o}{E_c}\right) + 0.4$$
 (electron-induced shower), and (3.31)

$$\overline{t} = 1.012 \ln\left(\frac{E_o}{E_c}\right) + 1.2$$
 (photon-induced shower). (3.32)

Schopper et al (Sc90) gives the mean squared *longitudinal* spread, τ^2 , (squared standard deviation) about \overline{t} ;

$$\tau^2 = 1.61 \ln\left(\frac{E_o}{E_c}\right) - 0.2$$
 (electron-induced shower), and (3.33)

$$\tau^2 = 1.61 \ln\left(\frac{E_o}{E_c}\right) + 0.9$$
 (photon-induced shower). (3.34)

There are other differences between photon and electron-induced showers but these can normally be neglected. EGS4 results tabulated by Schopper et al. (Sc90) have been parameterized to determine **source terms**, S_i , for longitudinal distributions of absorbed dose in various materials and for the associated dose equivalent within shields comprised of these materials over the energy region of 1 GeV $< E_o < 1$ TeV. This has been done for the dose on the z-axis (subscripts "a") and for the dose averaged over a 15 cm radius about the z-axis (subscripts "15"). Table 3.2 gives parameters for calculating dose equivalent, H_{long} (Sv per electron), at the end of a beam absorber of length, L (cm), of density ρ (g cm⁻³), and gives fitted values of the various "attenuation lengths", λ_i (g cm⁻²) to be used with the corresponding tabulated values of S_i . For absorbed dose calculations, the factor C, which is the ratio of dose equivalent in tissue (Sv) to absorbed dose in the material (not tissue) (Gy), should be set to unity. The formula in which these parameters from Table 3.2 are to be used is as follows:

$$H_{long} = CS_i \exp(-\rho L / \lambda_i).$$
(3.35)

This equation is valid in the longitudinal region beyond the shower maximum.

Table 3.2 Source terms S_a and S_{15} , and corresponding recommended longitudinal attenuation lengths, λ_a and λ_{15} , for doses on the axis, and averaged over a radius of 15 cm in the forward direction for beam absorbers and end-stops, respectively. These results are most valid in the region of incident electron energy, E_o , from 1 GeV to 1 TeV. Conversion factors *C* from absorbed dose in the shielding material to dose equivalent within the shield are given. E_o is the beam kinetic energy in GeV. These parameters are to be used with Eq. (3.35). [Adapted from (Sc90).]

Material	C (Sv/Gv)	S _a (Gv/electron)	λ_a	S ₁₅ (Gv/electron)	λ_{15}
Water	0.95	$1.0 \times 10^{-10} \text{E} 2.0$	<u>(g cm)</u> 58	1 5×10-11E 2.0	59.9
Concrete	1.2	$1.9 \times 10^{-9} \times 18^{-9}$	44	$1.5 \times 10^{-11} \text{E}_0^{-11}$	45.6
Concrete	1.2	$1.9 \times 10^{-9} E_0^{-1.0}$	44	$2.2 \times 10^{-11} E_0^{-1.0}$	45.0
Aluminum	1.2	$2.3 \times 10^{-9} E_0^{1.7}$	46	$3.4 \times 10^{-11} E_0^{-1.7}$	46.3
Iron	1.3	2.9x10 ⁻⁸ E ₀ ^{1.7}	30	1.8x10 ⁻¹⁰ E ₀ ^{1.7}	33.6
Lead	1.8	$1.9 \times 10^{-7} E_0^{-1.4}$	18	$4.6 \times 10^{-10} E_0^{1.4}$	24.2

3.4.2 Lateral Shower Development

Figure 3.16 shows the fraction U/E_o of the incident electron energy that escapes laterally from an infinitely long cylinder as a function of cylinder radius, R, for showers caused by electrons of various energies that bombard the front face of the cylinder. On this graph R is in units of X_m . According to Neal et al. (Ne68b), a function that fits data between 100 MeV and 20 GeV for electrons incident on targets ranging from aluminum to lead is given by

$$\frac{U(R / X_m)}{E_0} = 0.8 \exp[-3.45(R / X_m)] + 0.2 \exp[-0.889(R / X_m)].$$
(3.36)

Results similar to this universal curve have been obtained using EGS4 (Sc90). For values of R/X_m greater than about four, a material-dependent phenomenon emerges in which the photons having the largest mean free paths determined by the photon cross section at the Compton minimum for the absorber material will dominate the slopes of these curves. These extrapolations, normalized to X_m , are also included in this figure. As was done for the longitudinal situation, EGS4 (Sc90) has been similarly used to give the maximum energy deposition (and by extension, the maximum absorbed dose and dose equivalent) as a function of radius R. Over the energy range 1 GeV $< E_o < 1$ TeV, there is direct scaling with energy in the formula for maximum dose equivalent at $\theta \approx 90^{\circ}$;

$$H_{lat} = CE_0 S_{lat} \frac{\exp(-\rho d / \lambda_{lat})}{r^2} , \qquad (3.37)$$

- - -

where H_{lat} is the maximum dose equivalent laterally (Sv per electron), C is the same as in Eq. (3.35), E_o is the electron kinetic energy in GeV, S_{lat} is the source term from the EGS4 calculations, d is the lateral dimension of the shield (shield thickness) in cm, ρ is the density (g cm⁻³), λ_{lat} is the attenuation length (g cm⁻²), and r is the distance from the axis, in cm, where the dose equivalent is desired (see Fig. 3.11). Table 3.3 gives the parameters needed for Eq (3.37).



Fig. 3.16 Fraction of total energy deposited beyond a cylindrical radius, R/X_m , as a function of radius, R, for showers caused by 0.1 to 20 GeV electrons incident on various materials. The curve labeled "Equation" refers to Eq. (3.36). [Adapted from (Ne68b).]

Table 3.3 Conversion factors *C* from absorbed dose in shielding material to dose equivalent, source terms S_{lat} for the maximum of the electromagnetic component, and recommended lateral attenuation lengths λ_{lat} for the electron energy range, E_o , from 1 GeV to 1 TeV laterally for beam absorbers or end-stops. These parameters are to be used with Eq. (3.37). [Adapted from (Sc90).]

Material	С	S _{lat}	λ_{lat}
	(Sv/Gy)	(Gy cm ² GeV ⁻¹ per electron)	(g cm ⁻²)
Water	0.95	2.5x10 ⁻¹²	26
Concrete	1.2	3.6x10 ⁻¹²	27
Aluminum	1.2	3.4×10^{-12}	29
Iron	1.3	4.7x10 ⁻¹¹	33
Lead	1.8	1.3x10 ⁻¹⁰	26

3.5. Shielding of Hadrons Produced by the Electromagnetic Cascade

3.5.1 Neutrons

As discussed before, neutrons are produced by high energy electrons and photons. These neutrons must be taken into account to properly shield electron accelerators. Tesch has summarized shielding against these neutrons by developing simple analytical relations for cases where thick targets are struck by the electron beam (Te88). Figure 3.11 defines the shielding geometry. For lateral concrete shielding, the maximum dose equivalent outside of shield thickness (implying $\theta \approx 90^{\circ}$ as defined in Fig. 3.11), d (cm), which begins at radius a (cm) from a thick iron or copper target struck by electrons having primary energy E_o (GeV) is, per incident electron,

$$H(d,a) = \frac{4 \times 10^{-13}}{\left[(a+d)\right]^2} E_o \exp\left(-\rho d / 100\right)$$
 (Sv). (3.38)

This equation is valid for $E_o > 0.4$ GeV and $\rho d > 200$ g cm⁻². For other target materials one can scale this equation in the following way. The neutron production is proportional to the photoproduction cross section, the track length in cm, and the atom number density (atoms cm⁻³). The interaction cross section is generally proportional to the atomic weight, A. Since the track length is proportional to X_o , the production becomes proportional to the radiation length in units of g cm⁻². Thus one can, for rough estimates of dose equivalent in the environs of targets of materials other than iron, obtain results by scaling this value for iron by the factor f;

$$f = \frac{X_o (\text{material})}{X_o (\text{iron})}.$$
(3.39)
For shields comprised of other materials, one can simply adjust the implicit attenuation length (i.e., the value of 100 g cm^{-2} in the exponential function) to that appropriate to the material.

Schopper et al. (Sc90) give a somewhat more detailed treatment separately handling the giant resonance neutrons and high energy particle components of dose equivalent while deriving "source terms" and appropriate formulae. The formula for the dose equivalent H_n due to the giant resonance neutrons given below is held to be valid for 1 GeV < E_o < 1 TeV and for 30 < θ < 120 degrees. For the giant resonance neutrons, per incident electron;

$$H_n = \eta_n S_n E_o \left(\frac{\sin\theta}{a+d}\right)^2 \exp\left(-\frac{\rho d}{\lambda_n \sin\theta}\right), \qquad (Sv) \qquad (3.40)$$

where E_o is the beam energy (GeV), ρ (g cm⁻³) is the density, and the quantities *a* (cm) and *d* (cm) are defined in Fig. 3.11. S_n (Sv cm² GeV⁻¹) is the source term from Table 3.1 and λ_n (g cm⁻²) is the attenuation length recommended for giant resonance neutrons listed in Table 3.4. Values of λ_n are given as follows for representative materials. This formula is regarded as being valid for $30 < \theta < 120$ degrees.

л	I (SC30)•]	
	Material	$\lambda_n (\mathrm{g \ cm}^{-2})$
	water	9
	concrete	42
	iron	130
	lead	235

Table 3.4 Recommended attenuation lengths for use in Eq. (3.40) for various materials. [Adapted from (Sc90).]

The factor η_n ($\eta_n \leq 1$) is dimensionless and gives an estimate of the efficiency for the production of neutrons by the target. For "conservative" calculations, it can be taken to have a value of unity. It smoothly increases from very small values to unity as the target thickness approaches X_o .

3.5.2 High Energy Particles

In this situation no correction for target thickness is generally employed. These particles tend to drive the shielding requirements of large electron accelerators. The following formula uses the same source term as Eq (3.19), per incident electron with the geometry as defined in Fig. 3.11;

$$H_h = \frac{7.5 \times 10^{-13} E_o}{(1 - 0.75 \cos \theta)^2 A^{0.4}} \left[\frac{\sin \theta}{a + d}\right]^2 \exp\left[-\frac{\rho d}{\lambda_h \sin \theta}\right]$$
(Sv). (3.41)

In this formula H_h is the dose equivalent due to these particles (Sv), E_o is the beam energy (GeV), A is the atomic weight of the target, and λ_h (g cm⁻²) is the attenuation length typical of these particles. The tunnel dimensions a (cm) and d (cm) are defined as before. Table 3.5 gives values of λ_h for representative materials. Schopper et al. (Sc90) go further and describes a variety of special cases. The neutrons from this source tend to dominate the lateral shielding requirements in the GeV region.

Material	Energy Limit > 14 MeV or > 25 MeV (g cm ⁻²)	Energy Limit > 100 MeV	Nuclear Interaction Length (g cm ⁻²)	Recommended λ_h [Eq. (3.41)] (g cm ⁻²)
Water Aluminum			84.9 106.4	86 128
Soil (sand)	101104^*	117	99.2	117
Concrete	102105+ 101105* 91 82_100+	96 120 105	99.9	117
Iron	139+	100	131.9	164
Lead	244+		194	253

Table 3.5 Attenuation lengths λ_h in g cm⁻² for the high energy particle component. [Adapted from (Sc90).]

Attenuation lengths for the indicated values are slightly dependent on angle with the higher value at $\theta = 0^{\circ}$ and the smaller value in the backward direction for E > 15 MeV.

+Same remark but for E > 25 MeV.

Problems

- 1. An electron accelerator has a beam profile in the form of a 2 mm diameter circle uniformly illuminated by the beam. Make a crude plot of the value of the dose equivalent rate in the beam as the energy increases from 1 MeV to 10 GeV. The average beam current is 1 microamp (1 μ A). Assume the beam profile is unchanged during acceleration. Compare the results with Swanson's simple formula, said to be a "conservative" value. Is his formula "conservative" above 100 MeV? (Hint: use Fig. 1.4.)
- 2. Calculate for electrons the critical energy and length of material that corresponds to the radiation length for carbon and for lead. What does this say about the effectiveness of low-*Z* versus high-*Z* shielding materials for electrons?
- 3. A 100 MeV electron accelerator produces a 1.0 μ A beam incident on a high-Z (thick) target. Estimate the bremsstrahlung absorbed dose rates at $\theta = 0^{\circ}$ and 90° at r = 2 m from the target using Swanson's rules of thumb. Compare the 0° result with the "in-the-beam dose equivalent rate" found in Problem 1. How do the bremsstrahlung and in-beam dose rates compare?
- 4. Suppose the Tevatron enclosure at Fermilab is converted into an enclosure for an electron synchrotron. The radius of the synchrotron is 1000 m. If the circulating beam is 10^{12} electrons, calculate the median energy of the synchrotron radiation photons for E₀ = 100 GeV. Also find θ_c of the "lobe."
- 5. For the accelerator of Problem 3, calculate the neutron flux density at r = 2 m from giant resonance neutrons at large angles using the values in Table 3.1 for a high-Z (tungsten) target. Also use Table 3.1 to estimate the dose equivalent r = 2 m. Check this result by "guessing" the average neutron energy is between 1 and 10 MeV and use the curve in Fig. 1.5. Compare this neutron dose with the bremsstrahlung dose at large angles obtained in Problem 3.
- 6. For a 20 GeV electron accelerator operating at 1 kW, the electron beam strikes a beam stop made of aluminum or iron. How <u>long</u> (in *z*) does the beam stop have to be to range out all of the muons for either aluminum or iron based on the mean range? Compare the dose equivalent rates at the immediate downstream ends of each material if 10 % of the muons leak through due to straggling and multiple Coulomb scattering can be neglected. (Assume the production of muons from Fe is approximately equal to that from Al. Recall the inverse square law.)

- 7. In the discussion of the longitudinal development of electromagnetic showers, there are two different formulations (Rossi-Griesen, Bathow, and Van Ginneken). Using Van Ginneken's scaling method, calculate the value of ζ (g cm⁻²) for $E_o = 1000$ MeV, 10 GeV, and 100 GeV for copper and lead. Determine the number of radiation lengths to which ζ , corresponds for each material at each energy.
- 8. Compare the results of Van Ginneken for the location of the longitudinal shower maximum with Bathow's result for copper and lead at the three energies given in Problem 7 for incident electrons. Is the agreement better or worse as the energy increases?
- 9. A hypothetical electron accelerator operates at either 100 MeV or 10 GeV and delivers a beam current of 1 µA. Using Table 3.2, calculate the dose equivalent rates in both Sv/sec and rem/h at the end of a 300 cm long aluminum beam stop; averaged over a 15 cm radius that are due to bremsstrahlung. (The beam stop is a cylinder much larger than 15 cm in radius.) Then assume that, in order to save space, a high-Z beam stop is substituted. How long of a high-Z beam stop is needed to achieve the same dose rates? (Assume lead is a suitable high-Z material.) Why is the length of high-Z shield different for the 2 energies? In this problem, assume the values in Table 3.2 are valid for energies as low as 0.1 GeV.
- 10. In the accelerator and beam stop of Problem 9, if the radius of the beam stop is 30 cm, what is the maximum dose equivalent rate (Sv s⁻¹ and rem h⁻¹) on the lateral surface (at contact at r = 30 cm) of the beam stop for both energies, 100 MeV and 10 GeV, and both materials? Again assume approximate validity at 100 MeV of the results.
- 11. Calculate the dose equivalent rate due to neutrons outside a 1 meter thick concrete shield surrounding a cylindrical tunnel (inner radius 1 meter) in which is located a copper target stuck by 1 μ A beam of 100 GeV electrons. The geometry should be assumed to be optimized for producing giant resonance photoneutrons and the calculations should be performed at $\theta = 30$, 60 and 90° (Concrete has $\rho = 2.5$ g cm⁻³). Express the result as Sv s⁻¹ and rem h⁻¹. For $\theta = 90^{\circ}$, use Eq. (3.38) as a check.

4.1 Introduction

In this chapter the major features of development of prompt radiation fields and the shielding of these fields as they are produced at proton and ion accelerators are addressed. Particular emphasis is placed on the shielding of neutrons in view of their general dominance of the radiation fields. The shielding of muons at such accelerators is also described. Methods for utilizing the results of both semi-empirical and Monte Carlo methods in the solution of practical shielding problems are presented.

4.2 Radiation Production by Proton Accelerators

4.2.1 The Direct Beam; Radiation Hazards and Nuclear Interactions

Direct beams at proton accelerators, from the dosimetric standpoint, nearly always dominate over any type of secondary phenomena in terms of the level of hazard since the beam current is generally confined to small dimensions. Figure 1.4 gives the dose equivalent per fluence as a function of proton energy. The physical reason that the conversation factor shows such a prominent transition at about 200 MeV is that below that energy the proton range in tissue is less than the typical thickness of the human body. At these lower energies, a high fraction of the proton's energy is absorbed in tissue. However, as the energy is increased above 200 MeV, an increasing fraction of the proton's energy escapes from the body so that it requires a far larger fluence of protons to deliver the same absorbed dose or dose equivalent.

The ionization range of a proton increases monotonically with energy. Since the mass of the proton is so much larger than that of the electron, the radiative processes of bremsstrahlung and synchrotron radiation are negligible at energies found at current accelerators, but not at future ones that reach ultra-high energies. As will be discussed in Section 4.5, the cross sections for inelastic interactions become nearly independent of energy and have approximately the values tabulated in Table 1.2. Thus, as an individual proton passes through a material medium, the probability of it participating in an inelastic nuclear reaction before it loses its remaining energy to ionization becomes significant and, as the energy increases, the dominant means by which protons are absorbed. Tesch has summarized this effect and the results are shown in Fig. 4.1 for various materials and energies (Te85).

4.2.2 Neutrons (and Other Hadrons at High Energies)

The production and behavior of neutrons at proton and ion accelerators have different characteristics as the energy of the beam particles, E_0 , is increased. The interactions of protons in a sequence of energy domains of proton energy will be discussed separately.



Fig. 4.1 Range of protons (**curves on right and right hand scale**) and probability of inelastic nuclear interaction within the range (**curves on left and left hand scale**) for various materials [Adapted from (Te85).]

$4.2.2.1 E_o < 10 \, MeV$

For a nuclear reaction, the **Q-value**, Q_v , is the energy released by the reaction and is defined in terms of the rest masses, m_i , of the participant particles as

$$Q_{v} = [(m_{1} + m_{2}) - (m_{3} + m_{4})]c^{2}, \qquad (4.1)$$

for the nuclear reaction $m_1 + m_2 \rightarrow m_3 + m_4$.⁹ Conventionally, the projectile is represented by m_1 while generally the less massive emitted particle is represented by m_3 . A value of $Q_v > 0$ implies an **exothermic** nuclear reaction. **Endothermic** $(Q_v \le 0)$ reactions are characterized by a **threshold energy**, E_{th} , given by

$$E_{th} = \frac{m_1 + m_2}{m_2} |Q_v| \,. \tag{4.2}$$

Below a kinetic energy of about 10 MeV, (p, n) reactions are important for some materials because these reactions commonly have very low threshold energies ($E_{th} < 5$ MeV). For example, the reaction ⁷Li(p, n)⁷Be has a threshold energy of 1.9 MeV and a reaction cross section, σ , that quickly rises as a function of energy to a value of about 300 mb. Many features of low energy nuclear reactions are highly dependent upon the details of the structure of the target nuclei and are often sensitive to the target element, angle, and energy. There are also many resonances attributable to nuclear excited states that greatly affect the reaction cross sections.

$$4.2.2.2 10 < E_o < 200 \, MeV$$

For protons having energies of this magnitude and higher, neutrons are usually the dominant feature of the radiation field that results from their interactions. In this region of energy, the neutron yields are smoother functions of energy due to the lack of resonances, but are also more forward-peaked. For energies in this regime and higher, Tesch (Te85) has summarized the total neutron yields, *Y*, per incident proton for different materials as a function of energy in Fig. 4.2. In this figure the smooth curves agree with the original primary data obtained from a myriad of experiments performed over several decades to within about a factor of two. An important feature is that for $50 < E_o < 500$ MeV, $Y \propto E_o^2$ while for $E_o > 1$ GeV, $Y \propto E_o$. Especially at the lower energies, some of the neutrons produced are so-called **evaporation neutrons** that have an isotropic distribution due to the physical mechanism with which they are produced. Evaporation neutrons can be viewed as "boiling" off of a nucleus that has been "heated" by absorption of energy from the incident particle. Other neutrons that are produced are **cascade neutrons** that result directly from individual nuclear reactions. The latter are likely to have a directionality that can usually be described as at least mildly "forward-peaked". In

⁹ A more compact notation commonly used for the same nuclear reaction is $m_2(m_1, m_3)m_4$.

this region there are extensive angular distribution data, products of of nuclear physics research that are quite useful for applied purposes. Representative examples of angular distributions of neutrons are given in Figs. 4.3 and 4.4 for 52 and 200 MeV protons, respectively. Additional examples of neutron yields from proton interactions are found in (NC03).



Fig. 4.2 Total neutron yield per proton for different target materials as a function of incident proton energy, E_o. These values apply to relatively thick targets and include some degree of shower development. [Adapted from (Te85).]



Fig. 4.3 Measured angular distributions of total neutron yield above 5 MeV for carbon, iron, copper, and lead bombarded by 52 MeV protons. The measurements were normalized at $\theta = 15^{\circ}$. The curves are drawn to guide the eye. [Adapted from (Na78).]



Fig. 4.4 Calculated energy spectra of neutrons emitted by iron and aluminum targets bombarded by 200 MeV protons for four ranges of θ . The results for iron are from (Ha88) while those for aluminum are from (Al75). [Adapted from (Ha88).]

4.2.2.3 $200 \text{ MeV} < E_o < 1 \text{ GeV}; ("Intermediate" Energy)$

In this region, many more reaction channels become open and the number of protons emitted gradually becomes approximately equal to the number of neutrons. In fact, at the highest energies the radiation effects of protons and neutrons are essentially identical and both must be taken into account. Thus reliance on the values shown in Fig. 4.2 could underestimate radiation effects by as much as a factor of two. Also, at these energies, cascade neutrons become much more important than evaporation neutrons and thus the radiation field is more sharply forward-peaked with increasing primary particle energy.

4.2.2.4 $E_o > 1 \text{ GeV}$ ("High" Energy Region)

In this region, both the calculations and measurements become much more difficult. Figures 4.5, 4.6, 4.7, and 4.8 show representative data at 14, 26, 22, and 225 GeV.¹⁰ These results should be regarded as **thin target** values. "Thin" target in this context means a target shorter than the **mean free path** for **removal** of the high energy protons. Table 4.1 summarizes common removal mean free paths based upon the nuclear collision lengths of Table 1.2. Considerable efforts have been made to semi-empirically fit the distributions of the yields of secondary particles produced by proton interactions. These efforts are needed to supply the needs of the particle physics community as well as to address radiation safety issues. They began in the early days of radiation protection and continue to the present and are embodied in the continual development of Monte Carlo programs designed to calculate the properties of hadronic cascades as discussed in Section 4.6. An example of a particularly successful early model is one developed by Ranft (Ra67) expressed as the following formula for the yield of protons (or neutrons):

$$\frac{d^{2}Y}{d\Omega dp} = \left\{\frac{A}{p_{o}} + \frac{Bp}{p_{o}^{2}}\left[1 + f(p_{o})\left\{1 - \frac{p_{o}}{p}\right\}\right]\right\} \times \left\{1 + f(p_{o})\left[1 - \frac{pp_{o}}{m_{p}^{2}}\right]\right\} p^{2} \exp(-Cp^{2}\theta)$$
(protons or neutrons sr⁻¹ GeV⁻¹ per interacting proton), (4.3)

where

 p_o is the primary proton momentum (GeV/c), m_p is the proton rest energy (GeV/c²), $f(p_0) = \{1 + (p_o/m_p)^2\}^{1/2}$, and θ is the production angle (radians).

The parameters A, B, and C of the Ranft model are material dependent and are given in Table 4.2.

According to Patterson and Thomas (Pa73), when this formula is numerically integrated above the indicated particle threshold, it describes well the experimental data presented in Figs. 4.7 and 4.8.

¹⁰ Much of the experimental data presented in this and other sections related to high energy interactions were obtained using activation "threshold" detectors. This technique will be discussed at greater length in Section 9.5.3.



Fig. 4.5 Measurements of the angular distribution, $dY/d\Omega$, of neutrons above 20 MeV produced by 14 and 26 GeV protons incident on a thin beryllium target. The yield is per interacting proton. The lines are drawn to guide the eye. [Adapted from (Gi68).]



Fig. 4.6 Measurements of the angular distribution, $dY/d\Omega$, of neutrons above 600 MeV produced by 14 and 26 GeV protons incident on a thin beryllium target. The yield is per interacting proton. The lines are drawn to guide the eye [Adapted from (Gi68).]



Fig. 4.7 Measured angular distributions of hadron fluence (particles cm⁻²) at 1 meter from a copper target bombarded by 22 GeV protons. Several choices of hadron energy thresholds are shown. [Adapted from (Ra72).]



Fig. 4.8 Measurements of hadron yields above different energy thresholds as a function of production angle θ around a 15 cm long copper target bombarded by 225 GeV protons. The data have been multiplied by the indicated powers of 10 prior to plotting. The lines are intended to guide the eye. [Adapted from (St85).]

Material	Density	Removal Mean	Removal Mean	
		Free Path	Free Path	
	(grams cm ⁻³)	(grams cm ⁻²)	(cm)	
hydrogen gas @ STP	9.00 x 10 ⁻⁵	43.3	4.81×10^5	
beryllium	1.85	55.8	30.16	
carbon	2.27	60.2	26.58	
aluminum	2.70	70.6	26.15	
iron	7.87	82.8	10.52	
copper	8.96	85.6	9.55	
lead	11.35	116.2	10.24	
uranium	18.95	117.0	6.17	
air @ STP	1.29 x 10 ⁻³	62.0	4.81×10^4	
water	1.00	60.1	60.10	
concrete (typical)	2.50	67.4	26.96	
silicon dioxide (quartz)	2.64	66.5	25.19	
plastics (polyethylene)	0.93	56.9	61.29	

Table 4.1 Summary of removal mean free paths for high energy protons. [Adaptedfrom Table 1.2.]

 Table 4.2 Material-dependent parameters to be used in Eq. 4.3. [From (Ra67).]

Target	A	В	С
H ₂	0.55	-0.30	2.68
Be	0.68	-0.39	3.12
Fe	0.92	-0.75	2.90
Pb	1.14	-1.06	2.73

4.2.3 Sullivan's Formula

For simple radiation protection calculations, Sullivan (Su89) has developed a formula for the fluence, $\Phi(\theta)$, of hadrons with $E_o > 40$ MeV that will be produced at one meter from a copper target struck by protons in the energy region $5 < E_o < 500$ GeV per interacting proton;

$$\Phi(\theta) = \frac{1}{2\left[\theta + \left(35/\sqrt{E_0}\right)\right]^2} \quad (\text{cm}^{-2} \text{ per interacting proton}), \tag{4.4}$$

where E_o is in GeV and θ is in degrees.

At proton energies between about 0.05 and 5 GeV, this formula also approximately

accounts for the distributions of *neutrons* per incident proton. This equation is plotted in Fig. 4.9, for "lateral" ($\theta \approx 90^{\circ}$) and "forward" ($\theta \approx 0^{\circ}$) directions.



Fig. 4.9 Plot of Eq. (4.4) for two different values of θ . The proton is interacting in a copper target. [According to (Su89).]

Of course, the dose equivalent is more directly germane to radiation protection concerns than is the "raw" fluence. In principle, the dose equivalent can be obtained by integrating over the spectrum the product of the fluence and the dose equivalent per unit fluence, P(E), defined in Section 1.2.1;

$$H = \int_0^{E_{\text{max}}} dEP(E)\Phi(E), \qquad (4.5)$$

or by summation, taking into account the "coarseness" of available data and/or calculations;

$$H = \sum_{j=1}^{m} \Delta_j(E) P_j(E) \Phi_j(E)$$
(4.6)

Tesch (Te85) has done this to obtain the dose equivalent at $\theta = 90^{\circ}$ at a distance of one meter from a copper target bombarded by protons of various energies. The result is plotted in Fig. 4.10. Above about 1 GeV, the dose equivalent is approximately proportional to E_{\circ} . Levine (Le72) has measured the angular distribution of absorbed dose for 8 and 24 GeV/c protons incident on a Cu target. The results are in approximate agreement with those found by Tesch.



Fig. 4.10 Dose equivalent per proton due to neutrons at $\theta = 90^{\circ}$ having energies higher than 8 MeV at a distance of 1 meter from a copper target. The curve is an interpolation between the normalized experimental measurements denoted by the open symbols. [Adapted from (Te85).]

4.2.4 Muons

Muons at proton accelerators arise from two principal mechanisms; from pion and kaon decay and from so-called "direct" production. Production by means of pion and kaon decay proceed as follows where mass of the parent particles, the branching fraction (the percentage of time the parent particle decays by the reaction given), the mean-life, τ , and the value of $c\tau$ are also given (PDG04):

$$\pi^{\pm} \to \mu^{\pm} + \nu_{\mu}; m_{\pi} = 139.570 \text{ MeV}, \quad \tau = 2.6033 \text{ x } 10^{-8} \text{ s}, \quad (99.99 \% \text{ branch}),$$

 $c \tau = 7.8045 \text{ m}, \text{ and}$
 $K^{\pm} \to \mu^{\pm} + \nu_{\mu}; \quad m_{K} = 493.677 \text{ MeV}, \quad \tau = 1.2384 \text{ x } 10^{-8} \text{ s}, \quad (63.51 \% \text{ branch})$
 $c \tau = 3.713 \text{ m}.$

"Direct" muon production, important only at very high energy hadron accelerators, is discussed in more detail in Section 4.7.3.

Muon fields are forward-peaked and, normally, dominated by those from pion decay, except, perhaps at the highest energies. Usually, Monte Carlo techniques are needed to accurately estimate muon intensities. This is because of the need to:

- calculate the production of pions from the proton interactions,
- follow the pions until they decay or interact,
- adequately account for the range-energy relation and range straggling, and
- track the muons to the point of interest, for example, through magnetic fields.

4.3 Primary Radiation Fields at Ion Accelerators

Large portions of Section 4.2 have discussed general considerations that are appropriate the primary radiation fields generated by accelerated ions as well as to protons. In this section, special issues found in radiation fields produced by ions other than protons are described. Because the ionization range for ions of a given kinetic energy decreases as a function of ion mass, targets become effectively "thicker" as the ion mass increases. A comprehensive recent reference on this topic is that of Nakamura and Heilbronn (Na05)

4.3.1 Light Ions (Ion Mass Number A < 5)

For such ions there are exothermic reactions that should be treated as special cases. Noteworthy examples (followed by their reaction Q-values, Q_{ν} , in parentheses) are;

$D(d, n)^3$ He	$(Q_v = 3.266 \text{ MeV}),$
$^{9}\text{Be}(\alpha, n)^{12}\text{C}$	$(Q_v = 5.708 \text{ MeV})$, and
3 H(d, n) 4 He	$(Q_v = 17.586 \text{ MeV}).$

In some cases monoenergetic beams of neutrons can be produced using these or the following slightly endothermic reactions:

$^{12}C(d, n)^{13}N$	$(Q_v = -0.281 \text{ MeV}),$
$T(p, n)^3$ He	$(Q_v = -0.764 \text{ MeV})$, and
$^{7}\text{Li}(p, n)^{7}\text{Be}$	$(Q_v = -1.646 \text{ MeV}).$

The energies of such neutrons can range from 0 to 24 MeV for bombarding energies up to 10 MeV.

In general, deuteron stripping and breakup reactions, (d, n), have the highest yields

because the binding energy of the deuteron is only 2.225 MeV. In effect, one gets an extra neutron "for free". Furthermore, the neutrons due to deuteron stripping reactions typically have a kinetic energy of about half that of the incident deuteron if the latter has a kinetic energy that is large compared with the binding energy of the target nucleus. This phenomenon is especially pronounced at the lower energies. In the low energy region, and especially with light ions, one should carefully consider all possible reactions given the materials present in conjunction with the ions that are being accelerated. Patterson and Thomas (Pa73) have summarized total neutron yields for light ions. In general, the yields for the various light ions behave similarly to those due to protons. That is, the yield is within, typically, a factor of three of that expected for proton beams. A good measurement of neutron yields due to 40 MeV α -particles has been provided by Cecil et al. (Ce80).

4.3.2 Heavy Ions (Ions with A > 4)

At higher energies and especially at higher masses, neutron yield and dose equivalent data and calculations are very sparse. The data is usually normalized in terms of kinetic energy per atomic mass unit, the **specific energy**, expressed in units of MeV/amu, or kinetic energy per nucleon because reaction parameters generally scale to that parameter. In the literature the technical distinction between energy/amu and energy/nucleon is often ignored. In the range up to 20 MeV/amu, Ohnesorge et al. (Oh80) have measured dose equivalent rates at one meter at $\theta = 90^{\circ}$ from thick targets of iron, nickel, or copper bombarded by ⁴He, ¹²C, ¹⁴N, ¹⁶O, and ²⁰Ne beams. The dose equivalent was found to be essentially independent of ion type as a function of specific energy. At 10 MeV/amu, a value of 6.3 x 10⁻¹⁸ Sv/incident ion was measured while at 20 MeV/amu, a value of 3.6 x 10⁻¹⁷ Sv/incident ion was found. Other data relevant to this general energy region are exemplified by those of Hubbard et al. (Hu60), Aleinikov et al. (Al85), and especially Nakamura (Na85).

Tuyn et al. (Tu84) reported studies done with 86 MeV/amu ¹²C ions incident on Fe targets slightly thicker (longer) than an interaction length. The measurements are shown in Fig. 4.11. At a specific energy of 155 MeV/amu, Britvitch et al. (Br99) have measured energy spectra and total neutron yields and angular distributions for ⁴He, ¹²C, and ¹⁶O ions stopping in a thick target of an alloy of tungsten, nickel, and copper commonly known as "Hevimet". The differential yields, $dY/d\Omega$, were fit by the form

$$\frac{dY}{d\Omega} = C \exp(-\beta\theta), \qquad (4.7)$$

with the total yields being found by the integration,

$$Y_{total} = 2\pi \int_0^{\pi} d\theta \sin \theta \frac{dY(\theta)}{d\Omega} = 2\pi C \frac{\left[\exp(-\beta\pi) + 1\right]}{(\beta^2 + 1)}.$$
 (4.8)

The results are presented in Fig. 4.12. The total neutron yields for ⁴He, ¹²C, and ¹⁶O were found to be 4.90, 1.56, and 1.74 neutrons per incident ion, respectively.



Fig. 4.11 Measured neutron yields for 86 MeV/amu ¹²C ions incident on an iron target. Activation detectors (see Section 9.5.3) with the following sensitive regions in neutron energy, E_n , were used: moderated indium foils ("Mod. In") ($0.4 < E_n < 107 \text{ eV}$), ³³S(n, p)³²P ($E_n > 3 \text{ MeV}$), ²⁷Al(n, α)²⁴Na ($E_n > 7 \text{ MeV}$), and ¹²C(n,2n)¹¹C ($E_n > 20 \text{ MeV}$). The lines are intended to guide the eye. [Adapted from (Tu84).]



Fig. 4.12 Neutron yields per incident ion for 155 MeV/amu ions reported by Britvich et al. (Br99). The diamonds are measurements for ⁴He which were fitted by parameters (*C*{neutrons/incident ion) and β {radian⁻¹}) of (0.8, 0.49) as defined by Eqs. (4.7) and (4.8). The results for ¹²C are denoted by triangles and were fit by (*C*, β) values of (0.26, 0.51). The results for ¹⁶O are denoted by crosses and were fit by (*C*, β) values of (0.29, 0.51).

Clapier and Zaidins (Cl83) have surveyed a sample of ion data from 3 to 86 MeV/amu and have been able to approximate the total neutron yields an angular distributions over that domain. They found the total yield per ion, Y, to be given by

$$Y(W,Z) = C(Z)W^{\eta(Z)} \text{ (neutrons ion}^{-1)} \text{ with } (4.9a)$$

$$\eta(Z) = 1.22\sqrt{Z} \qquad \text{and} \qquad (4.9b)$$

$$C(Z) = \frac{1.96 \times 10^{-4}}{Z^{2.75}} \exp\left\{-0.475 \left(\ln Z\right)^2\right\},$$
(4.9c)

where Z is the atomic number of the projectile and W is the specific energy (MeV/amu). They found essentially no dependence on the atomic number of the target material and assert that an average neutron energy of 6-7 MeV is appropriate. To fit the angular distribution, $dY/d\Omega$, the "form factor" $F(\theta, \xi)$ defined as follows was found to be useful:

$$F(\theta,\xi) = \frac{1}{4\pi} \left(\frac{1}{\ln\{1 + 1/\xi\}} \right) \left(\frac{1}{\xi + \sin^2(\theta/2)} \right),$$
(4.10)

where θ is defined as usual and the fitting parameter ξ is related to the ratio of fluences, Φ , at $\theta = 0$ and 90 degrees, and thus related to "forward-peakedness". In a subsequent paper, Aleinikov et al. (Al85) developed the following parameterization for ξ :

$$\xi = \frac{\Phi(90^{\circ})}{\Phi(0^{\circ}) - \Phi(90^{\circ})} = \frac{1}{\Phi(0^{\circ}) / \Phi(90^{\circ}) - 1} \qquad (4.11)$$

In this scheme,

$$\frac{dY(\theta)}{d\Omega} = Y(W,Z)F(\theta,\xi).$$
(4.12)

Values of the parameters C(Z) and $\eta(Z)$ for specific circumstances are given in Table 4.3.

Atomic Number Element C(Z) $\eta(Z)$ 1 hydrogen 1.5 1.7 x 10⁻⁴ 3.9 x 10⁻⁶ 2 helium 2.6 2.5 x 10⁻⁶ 6 carbon 1.7 3.6×10^{-7} 8 3.6 oxygen 2.7×10^{-10} 10 neon 7.0 5.1×10^{-11} 18 7.0 argon $6.0 \ge 10^{-12}$ 36 7.9 krypton 1.7 x 10⁻¹³ 82 lead 11.0

Table 4.3 Values of the parameters $\eta(Z)$ and C(Z) as expressed in Eqs (4.9). [Adapted from (Cl83).]

They also give a few examples of the values of their parameter, ξ ; 0.07 for uranium incident on uranium at 9 MeV/amu, 0.025 for neutrons of energy $E_n < 20$ MeV produced by 86 MeV/amu ¹²C incident on iron, and 3 x 10⁻⁴ for neutrons of energy $E_n > 20$ MeV produced by 86 MeV/amu ¹²C incident on iron (based on an analysis of the data presented in Fig. 4.11). One, in principle, could use values given in Table 4.3 or the direct calculation using Eqs. (4.9b) and (4.9c) and obtain some idea of the uncertainties inherent in this fit of such a broad range of data. However, the uncertainties in this type of fit are quite large due to the functional forms that were used.

McCaslin et al. (McC85) measured the angular distribution of yields of 670 MeV/amu Ne and Si ions stopped in a copper target. The distributions for the two different projectiles were similar with fits to the data provided for the 670 MeV/amu ²⁰Ne ions. For the ²⁰Ne ions, including all neutrons above 6.5 MeV at a radius of one meter, McCaslin found

$$\Phi(\theta) = 372 \frac{1}{\theta}$$
 neutrons m⁻² per ion for 2° < θ < 180°, θ in degrees (4.13)

and for the same ions, including all neutrons above 20 MeV;

$$\Phi(\theta) = 248e^{-0.2\theta}$$
 neutrons m⁻² per ion for $0^{\circ} < \theta < 20^{\circ}$, θ in degrees, and (4.14)

$$\Phi(\theta) = 10e^{-0.038\theta} \text{ neutrons } \text{m}^{-2} \text{ per ion for } 20^{\circ} < \theta < 120^{\circ}, \theta \text{ in degrees.}$$
(4.15)

The neutron yields at this high specific energy for heavy ions turn out to be quite large. By integrating the above over all angles, one finds a total yield of 74.1 neutrons/incident ion for $E_n > 6.5$ MeV for ²⁰Ne incident ions (see Problem 4).

It is clear that a more complete picture of neutron yields from heavy ion interactions is desirable especially in the intermediate to high energy ranges. The systematic studies of Kurosawa et al. (Ku99), Heilbronn et al. (He99), and Kurosawa et al. (Ku00) that span the periodic table document major advances on this topic. Along with a good parameterizeration of measured neutron angular distributions not discussed in detail here, (Ku00) presents a useful simple formula based upon geometrical considerations that describes total yield, *Y*, of neutrons having energies above 5 MeV emitted into the hemisphere $0 < \theta < 90^{\circ}$. This heavy ion neutron yield formula is

$$Y = \frac{1.5 \times 10^{-6}}{N_T^{1/3}} W_P^2 \left(A_P^{1/3} + A_T^{1/3} \right)^2 N_P \frac{A_P}{Z_P^2} \text{ (neutrons particle}^{-1)}, \tag{4.16}$$

where the subscripts P and T denote properties of the projectile ion and the target, respectively, and Z, N, and A have their usual meanings of atomic number, neutron number, and mass number. W_P is the projectile specific energy in MeV amu⁻¹. This

formula describes data generally within factors of 2 or 3 for ions from He to Xe incident ions fully stopped in targets ranging from C to Pb over the specific energy domain $100 < E_P < 800$ MeV amu⁻¹. Fig. 4.13 shows representative total neutron yields for heavy ions from some measurements and calculations using Eq. (4.16) compared with the yields found for protons as a function of specific energy.



Fig. 4.13 Neutron yields as a function of specific energy for selected projectiles and targets as reported by the cited references along with results obtained using Eq. (4.16).¹¹

4.4 Hadron (Neutron) Shielding for Low Energy Incident Protons ($E_o < 15$ MeV)

Neutron shielding in this region is especially complex because it is the region of significant nuclear structure effects. There are many resonances associated with compound nucleus that can be excited and there are also many nuclear reaction channels leading to a large number of nuclear excited states up to 20 MeV in excitation energy which have a wide variety of nuclear structure quantum numbers and very narrow widths in energy.

¹¹ A comment should be made here that measurements of neutron yields using heavy ions are rather difficult to perform. This leads to results from different laboratories that sometimes appear to be in only "qualitative" agreement. For example, for the conditions of the measurement reported by McCaslin (McC85), using Eq. (4.16) a yield of only 18.6 neutrons ion⁻¹ is calculated. The discrepancy of a factor of four is not likely attributable to the somewhat smaller angular range covered by Eq. (4.16). "Systematic" variables such as target sizes and neutron detection techniques may be quite important. At the higher energies, the escape of mesons produced by interactions in target volume may also be important.

Clark (Cl71) has expressed some general rules of attack on the neutron shielding problem. **Clark's principles** are:

- "The shield must be sufficiently thick and the neutrons so distributed in energy that only a narrow band of the most penetrating source neutrons give any appreciable ultimate contribution to the dose outside the shield."
- "There must be sufficient hydrogen in the shield, intimately mixed or in the final shield region, to assure a very short characteristic transport length from about one MeV to absorption at or near thermal energy."
- "The source energy distribution and shield material (non-hydrogeneous) properties must be such as to assure a short transport distance for slowing down from the most penetrating energies to one MeV."

An elementary method used to calculate shielding thicknesses in this energy domain is that of **removal cross section theory**. It has been found that the dose equivalent, H, as a function of shield thickness, t, is approximately given for these neutrons by

$$H(t) = \Phi_o PG \exp(-\Sigma_r t), \qquad (4.17)$$

where Φ_0 is the fluence before the shielding (calculated from neutron yield information), P is the dose equivalent per fluence conversion factor (obtained by performing any needed integration over the energy spectrum), G is a "geometry factor", t (cm) is the thickness of the shield. For parallel beams, G = 1 while for an isotropic point source, $G = 1/r^2$. Σ_r is the **macroscopic removal cross section**;

$$\Sigma_r = \frac{0.602\sigma_r \rho}{A} \ (\text{cm}^{-1}),$$
 (4.18)

where σ_r is the **microscopic removal cross section** in barns, ρ is the density (g cm⁻³) and *A* is the mass number. For mixtures of *n* materials,

$$\sum_{r} = \sum_{i}^{n} \frac{\rho_{i}}{\rho} \sum_{ri}$$
(4.19)

where the right-most quantity is the **removal cross section per unit mass** of the *i*th constituent and ρ_i is the **partial density** of the *i*th material. In this formulation the overall density is equal to the sum of the partial densities. For A > 8,

$$\sigma_r \approx 0.21 \, A^{-0.58}$$
 (barns) (4.20)

for neutrons of approximately 8 MeV.

Figure 4.14 taken from (Pa73) shows the values of σ_r as a function of mass number at this energy. Table 4.4 gives representative values for σ_r for some energies where this approach is applicable.



Fig. 4.14 Removal cross sections per unit atomic mass number for fission neutrons as a function of mass number at a neutron energy of 8 MeV. Over the range $8 \le A \le 240$, the values are well fit by Eq. (4.20). [Adapted from (Pa73)].

Table 4.4 Removal cross sections, σ_r (barns), for low energy neutrons. The typical accuracy is quoted to be ± 5 %. [Adapted from (Pa73).]

Element	1 MeV	Fission	2.9 MeV	4 MeV	6.7 MeV	14.9 MeV
		Spectrum				
Carbon		0.9	1.58	1.05	0.83	0.50
Aluminum		1.31				
Iron	1.1	1.96	1.94	1.98	2.26	1.60
Copper		2.04				
Lead		3.28	2.70	3.44	3.77	2.95

The use of removal cross sections describe attenuation data rather effectively despite the fact that as more shielding is penetrated, neutrons of lower energy tend to dominate the spectrum over those found in the few MeV region.

4.5 Limiting Attenuation at High Energy

The most important feature of neutron shielding at higher energy accelerators is the fact that the attenuation length becomes an approximate constant at high energy. As the energy increases, the neutron inelastic cross sections increase rapidly until about 25 MeV where they generally level off and then fall rapidly with energy in the region $25 < E_n < 100$ MeV to a value which becomes independent of energy, aside from a slight, gradual *increase* at the very highest energies. Lindenbaum was the first to make this observation (Li61). The result is that high energy neutron beams attenuate approximately exponentially with an attenuation length, λ_{atten} , that is rather insensitive to energy. Thus, in units of length,

$$\lambda_{atten} = \frac{1}{N\sigma_{in}} \quad (\text{cm}), \tag{4.21}$$

where σ_{in} is the inelastic cross section, roughly equivalent to the so-called "absorption cross section" and *N*, as before, is the number of absorber nuclei per unit volume. This cross section specifically does not include elastic scattering and so is always smaller than the total cross section. In a simple-minded approach, this cross section can be taken approximately to be the geometrical cross section with the nucleon radius assumed to be 1.2 x 10⁻¹³ cm. It then follows (see Problem 5) that in the high energy limit, one can multiply by the density to get

$$\rho \lambda_{atten} = 36.7 A^{1/3}$$
 (g cm⁻²). (4.22)

Fig. 4.15 illustrates the neutron inelastic cross sections for several materials up to a kinetic energy of 1.4 GeV beyond which the value is, for our present purposes, essentially constant.



Fig. 4.15 Inelastic neutron cross sections as a function of energy in the range 1 to 1000 MeV. [Adapted from (Li61).]

The high energy asymptotes were first verified by historic cosmic ray data and are wellrepresented by

$$\sigma_{in} = 43A^{0.69}$$
 (mb). (4.23).

In the high energy limit, the **interaction length**, λ_{inel} , is thus given by

$$\lambda_{inel} = \frac{\rho}{N\sigma_{in}} = 38.5 A^{0.31} \text{ (g cm}^{-2}\text{)}.$$
(4.24)

This **geometric approximation** is thus reasonably accurate. Values of the high energy interaction lengths are available for many different materials and representative examples are found in Table 1.2. Figure 4.16 shows the results for absorption cross sections based upon these values. Schopper et al. (Sc90) have provided extensive tabulations of the value of σ_{in} (mb) for a variety of particles, energies, and materials in the high energy region as functions of particle momenta up to 10 TeV/c.



Fig. 4.16 Inelastic mean free path and cross section as a function of mass number, *A*. [Adapted from (Pa73).]

The saturation of attenuation length for concrete as a function of particle energy is especially important, due to the widespread utilization of concrete shielding for hadrons. Figure 4.17 gives the results for both neutrons and protons. An important feature of these

results is the equivalence of the attenuation lengths for protons and neutrons at high energies. Due to the similarities of chemical composition, results for soil shielding in this energy regime can be taken to be the same as those for concrete when λ is expressed in units of areal density, e.g. in g cm⁻².



Fig. 4.17 The variation of the attenuation length λ for monoenergetic neutrons and protons in concrete shielding as a function of neutron energy. The high energy limit is 117 g cm⁻². [Adapted from (Th88).]

4.6 Intermediate and High Energy Shielding-The Hadronic Cascade

4.6.1 The Hadronic Cascade from a Conceptual Standpoint

The **hadronic cascade** is initiated at proton accelerators when the beam interacts with targets, beam absorbers, and accelerator components to produce neutrons and other particles. Such cascades can also arise at electron accelerators since (see Chapter 3) high energy secondary hadrons can also result from electromagnetic interactions.

The collision of a high energy nucleon with a nucleus produces a large number of particles; pions, kaons, and other nucleons as well as fragments of the struck nucleus. According to Thomas and Stevenson, above 1 GeV and at forward angles, the pions, protons, and neutrons, can be nearly equal in number (Th88). The neutrons may be classified as either **evaporation neutrons** or **cascade neutrons**, as discussed in Section 4.2.2.2. To review, evaporation neutrons originate as decays from excited states of residual nuclei and average a few MeV in energy. These neutrons tend to be isotropically distributed. Cascade neutrons are emitted by direct impact and their spectrum extends in energy up to the incident energy with diminishing probability following a spectrum roughly characterized as having an energy dependence proportional to 1/E.

As the proton kinetic energy increases, other particles, notably π^{\pm} , π° , and K^{\pm} , play roles in the cascade when their production becomes energetically possible. They are absorbed with absorption lengths comparable in magnitude to, but not identical, with those of protons. These particles also decay into muons. Because of their long ionization ranges and lack of nuclear interactions, muons provide a pathway for energy to escape the cascade.

Hadrons, principally neutrons with $E_n > 150$ MeV, propagate the cascade. This is clear from the attenuation lengths shown in Figs. 4.15 and 4.17. Nucleons in the range $20 < E_n$ < 150 MeV also deposit their energy predominantly by nuclear interactions but their energy gets distributed over many particles of all types energetically possible. The charged particles produced in such cascades are generally "ranged-out" by ionization in material or create yet other particles in the cascade. The role played by the energy of approximately 150 MeV for hadronic cascade propagation is qualitatively somewhat analogous to that of the critical energy for electromagnetic cascades.

Neutral pions (π^{0}) are produced when the kinetic energy of the incident proton significantly exceeds the π^{0} rest energy of 135.0 MeV. The π^{0} mean-life, $\tau = (8.4 \pm 0.6)$ x 10⁻¹⁷ s is very short so that for the π^{0} , $c\tau = 25.1$ nm. Hence, π^{0} 's do not travel very far at all before decaying. The principal decay (99 % branching ratio) is into two γ -rays. An energetic π^{0} thus appears as two forward-peaked photons each with half of the π^{0} 's total energy. The decay photons from π^{0} decay readily initiate electromagnetic cascades along with the hadronic one. It is possible for the electromagnetic channel to feed back into the hadronic cascade because it, too, produces high energy hadrons. However this effect is generally of little importance and, for most shielding calculations, the electromagnetic component of a hadronic cascade can be ignored. The principal exception involves energy deposition calculations at forward angles (small values of θ). In fact, at hundreds of GeV, electromagnetic cascades dominate the energy deposition at very forward angles (i.e., at very small values of θ). This feature can have important ramifications if one needs to consider radiation damage to equipment, the heat load on cryogenic systems, and the ability of targets to survive bombardment.

In general, the neutrons are the principal drivers of the cascade because of the ionization energy loss for pions and for protons below 450 MeV where the ionization range becomes roughly equal to the interaction length. Also, any magnetic fields that are present which can deflect and disperse charged particles present will not, of course, affect the neutrons. Furthermore, neutrons are produced in large quantities at large values of θ compared with the forward-peaked pions. These phenomena, in general, apply also to ions heavier than the proton with suitable corrections (especially at low energies) for nuclear structure effects. Scaling of proton results for heavier ions will, in general, roughly be according to the specific energy (MeV/amu). Figure 4.18 is a schematic flow chart of the hadronic cascade process (IC78).

	Most Numerous Participants	Time Scale s (seconds)	Typical Energy per Particle (MeV)	Per Cent of Energy Deposition
$\qquad \qquad $	π, Κ -> μ	10 ⁻⁸	any	10
n^{ρ} n^{-} Electro- magnetic n^{-} Cascade	π ⁰ -> e,γ	- 16 10	any	20
Intra-Nuclear Cascade	p, n, π, K	10 ⁻²²	<200	30
Hadron A Extranuclear Cascade	p, n, π, K	- 23 10	>200	30
Evaporation of Nucleons and Fragments	p, n, d, α	- 1 9 10	<30	10
β Induced Activity	α, β, γ	seconds to years	<10	<1

Fig. 4.18 Schematic representation of the development of the hadronic cascade and the major participants in any given path. The approximate time scales, the typical energies, and the fraction of the total energy deposition due to these participants are also shown. [Adapted from (IC78).]

4.6.2 A Simple One-Dimensional Cascade Model

A simple one-dimensional model of the hadronic cascade was first proposed by Lindenbaum (Li61). This approach provides some "intuition" into the nature of the hadronic cascade. Figure 4.19 defines the geometry of Lindenbaum's approximation.



Fig. 4.19 **a)** Single collision geometry for the Lindenbaum approximation. **b)** Two collision geometry for the Lindenbaum one-dimensional model. [Adapted from (Th88).]

Suppose one initially has N_o incident high energy nucleons. After an individual collision, one of them continues in its original direction at a reduced energy but with the same attenuation length, λ , or will generate one or more secondary particles also with the same value of λ . The value of λ is approximately constant due to the limiting attenuation at high energy. This process continues until a number of collisions, *n*, have occurred which are sufficient to degrade the particle energies to approximately 150 MeV, below which energy the inelastic cross sections greatly increase (see Fig. 4.15). At this point a given particle is said to be removed from the cascade. For the present discussion, it is assumed that *n* is an integer, an approximation when in reality it has a statistical distribution. Following these assumptions, the number v_i that reach x = z having made no collisions is

$$v_1 = N_a \exp(-z/\lambda). \tag{4.25}$$

Now suppose that there is one collision between 0 and z. The number, v_2 , that reach z is given by the product of the number that reach elemental coordinate dr and the probability

of subsequently reaching z, times the probability of interacting in dr, dr/λ , times the **multiplicity**, m_1 , of particles produced in the first interaction. Integrating over dr;

$$\int_{0}^{z} dr \frac{m_{1}}{\lambda} \left[N_{0} \exp(-r/\lambda) \right] \left[\exp\{-(z-r)/\lambda\} \right] = \left(N_{0} m_{1} \frac{z}{\lambda} \right) \exp(-z/\lambda) = v_{2}.$$
(4.26)

Continuing, we further suppose there two collisions occur. The number, v_3 , that reach z is the product of those that reach s having made one collision, multiplied by the probability of subsequently reaching z, times the multiplicity in the second interaction $m_{2,}$ times the probability of interacting in ds;

$$\int_{0}^{z} ds \frac{m_{2}}{\lambda} \left[N_{0}m_{1} \frac{s}{\lambda} \exp(-s/\lambda) \right] \left[\exp\{-(z-s)/\lambda\} \right] = \left\{ N_{0}m_{1}m_{2} \frac{z}{\lambda^{2}} \exp(-z/\lambda) \right\} \int_{0}^{z} s ds = \left\{ N_{0}m_{1}m_{2} \frac{z^{2}}{2\lambda^{2}} \exp(-z/\lambda) \right\} = V_{3}.$$
(4.27)

Therefore, with *n* defined as above, one can write:

$$N_n(x) = N_0 \beta_n(z/\lambda) \exp(-z/\lambda), \qquad (4.28)$$

where β is a **buildup factor**:

for
$$n = 1$$
; $N_1 = v_1$ and $\beta_1 = 1$,
for $n = 2$; $N_2 = v_1 + v_2$ and $\beta_2 = 1 + (m_1 z/\lambda)$, while
for $n = 3$; $N_2 = v_1 + v_2 + v_3$ and $\beta_3 = 1 + (m_1 z/\lambda) + (m_1 m_2 z^2/2\lambda^2)$.

For arbitrary *n*,
$$\beta_n = 1 + \frac{m_1 z}{\lambda} + \frac{m_1 m_2 z^2}{2\lambda^2} + \dots + \frac{1}{(n-1)!} \left(\frac{z^{n-1}}{\lambda^{n-1}}\right) \prod_{i=1}^{n-1} m_i.$$
 (4.29)

Thus, this buildup factor is a monotonically increasing function of z. If $m_1 = m_2 = ...= m$ (i.e., assuming that the multiplicity stays the same for all interactions in this simple model) and n is large, comparison with the series expansion of the exponential function reveals that β_n approximates an exponential dependence on z. The condition on n implies that the shield must be quite thick. The general result is that the **attenuation length of the cascade**, λ_{cas} , is somewhat larger than the value of the interaction length, λ , for a single interaction. The upper frame of Fig. 4.20 is a plot of the results of Lindenbaum's approximation for several values of m and n as a function of z/λ while the lower frame is a plot for a specific case (n = 3 and m = 2). The exponential region is not completely achieved until $z/\lambda \approx 5$. In concrete this represents a depth of approximately 600 g cm⁻². In the lower frame, these calculations are also compared with the results of data from the

experiment of Citron et al. (Ci65) with 19.2 GeV/c protons incident on an iron slab taken under experimental conditions which approximated these values of m and n.



Fig. 4.20 **Upper frame:** Development of a one-dimensional cascade in Lindenbaum's approximation with n = 1 to 4 and m = 1, 2, and 5. Lower frame: The same approximation with n = 3 and m = 2 from Thomas and Stevenson (Th88) labeled "Curve" compared with the laterally integrated star density in nuclear emulsions produced by a 19.2 GeV/c proton beam incident on an iron slab measured by Citron et al. (Ci65) which is labeled "Data".

Analytical approaches such as this one are constructive qualitatively but have severe limitations, among which are;

- the restriction to one dimension,
- the neglect of ionization energy losses and escape of energy carried by muons,
- the neglect of elastic and multiple Coulomb scattering,
- the assumption that <u>all</u> secondary particles go forward,
- the assumption that multiplicities are <u>not</u> dependent on energy and particle type,
- the assumption that λ is a constant for all particles at all energies, and
- the neglect of radiative and electromagnetic cascade effects.

4.6.3 A Semiempirical method, the Moyer Model for a Point Source

A number of references (Pa73, IC78, Sc90, Ro76, St82, Th84, McC87, Te83, Te85, McC85, Co82a, and Co85a) bear on the development of this model that is predominantly based on an exponential approximation with constants fitted to actual data spanning the range of proton beam energies from 7.4 to 800 GeV. The summary of this method here is largely taken from Patterson and Thomas (Pa73) and Schopper et al. (Sc90). This so-called **Moyer Model** was first developed by B. J. Moyer to solve particular shielding problems related to the Bevatron at the Lawrence Radiation Laboratory. The model predates the development of large, fast computers and advanced Monte Carlo techniques but remains useful as means of checking more sophisticated calculations.

This model will be discussed for the situation shown in Fig. 4.21 for a "point" target source.



Fig. 4.21 Sketch of the geometry for the empirical Moyer Model. A beam of N_p protons impinges on the target of length *L*. The shield materials represented by the layers x_i , could be, for example, iron, concrete, earth, and air (i.e., vacuum) respectively. *a* is the inner radius of the tunnel. The observer is situated at a radial thickness of *d* equal to the sum of the thicknesses of the four layers and is at a distance $r' = r \csc \theta$ from the beam-target interaction point.

The number of neutrons, dN/dE, which are emitted into a given element of solid angle $d\Omega$ at angle θ relative to a target struck by N_p protons in an energy interval E + dE is given for a single shield material of thickness d by

$$\frac{dN}{dE} = N_p B(E) \left(\frac{d^2 Y}{dE d\Omega} \right) d\Omega \exp\left(-\frac{d \csc \theta}{\lambda(E)} \right), \tag{4.30}$$

where B(E) is a buildup factor and the exponential function accounts for the attenuation of the radiation field by shielding of thickness, d, at the angle θ . The energy-dependent interaction length is denoted by $\lambda(E)$. The role of the double differential of the yield is obvious. In the above, the flux density at coordinates (r, θ) can be obtained at distance r' from the target by including the factor

$$\frac{d\Omega}{dA} = \frac{1}{(a+d)^2 \csc^2 \theta} = \frac{1}{r^2 \csc^2 \theta} = \frac{1}{r'^2}.$$
(4.31)

The total fluence, Φ , at the point where the ray emerges from the shield is given by

$$\Phi = \frac{N_p}{r'^2} \int_{E_{\min}}^{E_{\max}} dE \ \frac{d^2 Y}{dE d\Omega} B(E) \exp\left(-\frac{d \csc \theta}{\lambda(E)}\right).$$
(4.32)

The following are Moyer's simplifying assumptions:

A. $\lambda(E) = \lambda = \text{constant}$ for $E \ge 150$ MeV and $\lambda(E) = 0$ for E < 150 MeV. This is a simplified rendering of the leveling-off of the inelastic cross section at high energy. Thus,

$$\Phi(E_n > 150 \text{ MeV}) = \frac{N_p}{r'^2} \exp\left(-\frac{d \csc \theta}{\lambda}\right) \int_{150 \text{ MeV}}^{E_{\text{max}}} dE \frac{d^2 Y}{dE d\Omega} B(E) .$$
(4.33)

B. The neutrons emitted at angle θ can be represented by a simple function $f(\theta)$ multiplied by a multiplicity factor $M(E_{max})$ that depends only on the incident energy, thus;

$$\Phi(E_n > 150 \text{ MeV}) = \frac{N_p}{r'^2} \exp\left(-\frac{d \csc \theta}{\lambda}\right) M(E_{\max}) f(\theta) = \frac{N_p}{r'^2} \exp\left(-\frac{d \csc \theta}{\lambda}\right) g(E_{\max}, \theta)$$
(4.34)

where $g(E_{\text{max}}, \theta)$ is an angular distribution function that is constant for a given value of E_{max} and for a particular target.

C. The dose equivalent per fluence, P, for neutrons is not strongly dependent on energy over a rather wide energy range near $E \approx 150$ MeV (see Fig. 1.5). Thus the dose equivalent just outside of the shield due to neutrons with E > 150 MeV can be taken to be $H_{150} \approx P_{150} \Phi$ ($E_n > 150$ MeV), where P_{150} is the value of this conversion factor at 150 MeV.

The total dose equivalent, *H*, is then given by

$$H = kH_{150}$$
 where $k \ge 1$. (4.35)

This implicitly assumes that the low-energy neutrons are in equilibrium with those having E > 150 MeV so that the spectrum no longer changes with depth. This is a valid assumption for a shield more than a few mean free paths thick. Thus, Moyer's assumptions lead to

$$H = \frac{kP_{150}N_pg(E_{\max},\theta)}{\left(a+d\right)^2\csc^2\theta}\exp\left(-\frac{d\csc\theta}{\lambda}\right).$$
(4.36)

One can generalize the results for the geometry shown in Fig. 4.21 with multiple materials in the shield. The parameter ζ , which replaces the ratio d/λ in the argument of the exponential function in Eq. (4.36), is introduced to take care of the *n* shielding components;

$$\zeta = \sum_{i=1}^{n} \frac{x_i}{\lambda_i},\tag{4.37}$$

where the sum is over the *n* layers of shielding.

Moyer model parameters have been determined by experiment. Stevenson (St82) and Thomas and Thomas (Th84) have determined from global fits to data over a wide domain of energy that $f(\theta)$ is well described by

$$f(\theta) = \exp(-\beta\theta), \qquad (4.38)$$

where θ is in radians, β is in radians⁻¹, and, in fact, $\beta \approx 2.3 \text{ rad}^{-1}$ (for $E_n > 150 \text{ MeV}$) for proton kinetic energies above a few GeV. Thus,

$$H = \frac{H_o(E_p)\exp(-\beta\theta)\exp(-\zeta\csc\theta)}{\left(r\csc\theta\right)^2}$$
(4.39)

in which
$$r = a + \sum_{i=1}^{n} x_i$$
 (4.40)

and where the value of $H_o(E_p)\exp(-\beta\theta)$ is determined from the yield data and empirical measurements. $H_o(E_p)$ is best fit as a power law; $H_o(E_p) = kE^n$. From such results, per incident proton;

$$H_o(E_p) = [(2.84 \pm 0.14) \ge 10^{-13}] E_p^{(0.80 \pm 0.10)}$$
(Sv m²)
= 2.84 \x 10^{-8} E_p^{0.8} (mrem m²) = 2.8 \x 10^{-4} E_p^{0.8} (mrem cm²), (4.41)

with E_p in GeV. These results are derived for relatively "thick" targets (like accelerator magnets) in tunnel configurations. Schopper et al. (Sc90), based on Monte Carlo results gave values for "thin" targets of $k = 2.0 \times 10^{-14}$ (Sv m²) and n = 0.5. A thin-walled beam pipe would be an example of a "thin" target. The variations thus reflect buildup in the shower. For thick lateral shields close to the beam where the cascade immediately becomes fully developed and self-shielding arises, $k = (6.9 \pm 0.1) \times 10^{-15}$ (Sv m²) and n = 0.8 independent of target material (Sc90 and St87). The value of n = 0.8 for thick shields has also been verified by Torres (To96) and rigorously discussed by Gabriel et al. (Ga94).

Similarly, recommended values of λ for concrete and other materials as a function of mass number A are;

concrete:
$$1170 \pm 20 \text{ kg m}^{-2} = 117 \text{ g cm}^{-2}$$

others: $428A^{1/3} \text{ kg m}^{-2} = 42.8A^{1/3} \text{ g cm}^{-2}$

These values are 15-30% larger than the high energy nuclear interaction lengths (Table 1.2), a result consistent with that of Lindenbaum's approximation concerning the values of λ_{cas} relative to those of λ .

If one sets the partial derivative, $\partial H / \partial \theta$, equal to zero, one can derive an equation for determining the value of $\theta = \theta'$ at which the maximum dose equivalent occurs;

$$\zeta \cos \theta' - \beta \sin^2 \theta' + 2 \cos \theta' \sin \theta' = 0. \qquad (4.42)$$

Generally this equation can be solved by successive approximation methods. One can substitute into the above equation to get the maximum dose equivalent at a given radial depth. According to McCaslin (McC87), with r in meters and over a wide range of values of ζ , the following holds:

$$H_{\text{max}} = 1.66 \times 10^{-14} E_p^{0.8} \exp(-\zeta) \frac{\zeta^{0.245}}{r^2}$$
 (Sv per incident proton). (4.43)

For values of $\zeta > 2$, the following is an equally accurate approximation;

$$H_{\text{max}} = 1.26 \times 10^{-14} E_p^{0.8} \frac{\exp(-1.023\zeta)}{r^2} \quad (\text{Sv per incident proton}). \tag{4.44}$$

4.6.4 The Moyer Model for a Line Source

The Moyer model can be extended to a line source. Assume a uniform source of one proton interacting per unit length. Then, the dose equivalent from the individual increments along the line source contribute to the total at any given point, P, external to the shield. Fig. 4.22 shows the integration variables.



Secondary Particles

Figure 4.22 Variables of integration of Moyer point source result needed to obtain Moyer line source results. As in Fig. 4.21, the shielding of thickness d could be comprised of multiple layers of thickness ζ mean free paths.

One can integrate contributions of the elements $d\ell$ of a line source at given perpendicular distance *r* as follows. Making the change of variable of integration from the line integral to an integral over angle θ , $(d\ell = r \csc^2 \theta \ d\theta)$;

$$H = H_0 \left(E_p \right) \int_{-\infty}^{\infty} d\ell \frac{\exp(-\beta\theta) \exp(-\zeta \csc \theta)}{r^2 \csc^2 \theta} = H_0 \left(E_p \right) \int_0^{\pi} d\theta r \csc^2 \theta \frac{\exp(-\beta\theta) \exp(-\zeta \csc \theta)}{r^2 \csc^2 \theta} = \frac{H_0 \left(E_p \right)}{r} \int_0^{\pi} d\theta \exp(-\beta\theta) \exp(-\zeta \csc \theta) = \frac{H_0 \left(E_p \right)}{r} M(\beta, \zeta)$$
(per interacting proton per unit length). (4.45)

The integral in the above, $M(\beta,\zeta)$, is known as the **Moyer integral**. The values of this integral have been tabulated by Routti and Thomas (Ro76). In view of the results found
empirically for point sources, $M(2.3,\zeta)$ has obvious special significance and is tabulated extensively by, among others, Schopper et al. (Sc90). Tesch (Te83) made an important contribution in that he determined an approximation to this integral that has become known as the **Tesch approximation**:

$$M_T(2.3,\zeta) = 0.065 \exp(-1.09\zeta). \tag{4.46}$$

For "intermediate" values of ζ , $M_T(2.3,\zeta)$ can be used instead of $M(2.3,\zeta)$ to simplify calculations. Table 4.5 gives the ratio $M_T(2.3, \zeta) / M(2.3, \zeta)$ as a function of ζ . Of course, few so-called "line sources" are actually *infinite* in length. Thus, the integration can be limited to a finite angular range. Likewise, only a limited angular range (and hence length) contributes significantly to the Moyer integral. Tables 4.6 and 4.7 give angular integration limits corresponding to 90 % of the value of $M(2.3,\zeta)$ as a function of ζ (Table 4.6) and the distances along the z-axis corresponding to 90 % or more of the value of $M(2.3,\zeta)$ as a function of the radial distance and ζ (Table 4.7). These calculations were done for concrete shields. McCaslin (McC85) demonstrated that the Mover Model approach is also effective for moderately energetic heavy ions. It has also been found that the Moyer Model approach works well even in the intermediate energy region of $200 < E_o < 1000$ MeV. This may be interpreted as due to the relatively smooth dependence of neutron yield upon incident proton kinetic energy. The Moyer Model generally does not provide sufficiently accurate results at forward angles. For these situations, the Boltzmann equation must be solved. Monte Carlo calculations are often the best approximation to such solutions.

<u>[]</u>			
ζ	$M_T(2.3, \zeta)/M(2.3/\zeta)$	ζ	$M_T(2.3, \zeta)/M(2.3/\zeta)$
0.2	0.27	11	1.02
1	0.53	12	0.99
2	0.75	13	0.95
3	0.90	14	0.91
4	1.00	15	0.86
5	1.06	16	0.82
6	1.09	17	0.78
7	1.10	18	0.73
8	1.10	19	0.69
9	1.08	20	0.65
10	1.06		

Table 4.5 Values of the Ratio $M_T(2.3,\zeta)/M(2.3,\zeta)$ as a function of ζ . [Adapted from (Sc90).]

ζ	Lower Limit	Upper Limit	ζ	Lower Limit	Upper Limit
2.5	31.52	106.58	12	57.25	106.29
3	24.35	107.15	13	58.45	106.04
4	39.00	107.64	14	59.74	105.78
5	42.67	107.73	15	60.66	105.54
6	45.77	107.66	16	61.49	105.29
7	48.51	107.48	17	62.34	105.04
8	50.69	107.28	18	63.22	104.80
9	52.7	107.04	19	64.08	104.54
10	54.34	106.79	20	64.63	104.30
11	56.07	106.54			

Table 4.6 Angular integration limits in θ (degrees) which contain 90% of the Moyer Integral $M(2.3,\zeta)$. [Adapted from (Sc90).]

Table 4.7 Distances corresponding to 90% limits in Moyer Integrals. [Adapted from (Sc90).]

Radial Distance (m)	Thickness (concrete) (meters)	Thickness (concrete) ζ	Upstream Limit, z ₁ (meters)	Downstream Limit, z ₂ (meters)	Total Length z_2 - z_1 (meters)
1.5	0.5	1.0	-4.2	0.3	4.5
2.0	1.0.	2.0	-3.7	0.6	4.3
3.5	2.5	5.0	-3.8	1.1	4.9
6.0	5.0	10.0	-4.3	1.8	6.1
8.5	7.5	15.0	-4.8	2.4	7.2
11.0	10.0	20.0	-5.2	2.8	8.0

4.7 The Use of Monte Carlo Shielding Codes for Hadronic Cascades

4.7.1 Examples of Results of Monte Carlo Calculations

It should be quite obvious by now an approach based upon the Moyer Model is of diminished utility for beamline and shielding figures of significant complexity. Geometrical complexity presents severe limitations. The inclusion of magnetic fields is not possible. Further, the model is not valid at forward angles and for kinetic energies lower than a few hundred MeV. It is also incapable of handling the production of other types of particles aside from neutrons that can often be copiously produced at forward angles. The treatment of labyrinth penetrations by this means is also severely limited. It also does not readily allow for calculating residual activities. Thus, the Monte Carlo technique has become a very vital tool to use in such work. Appendix A describes a number of Monte Carlo programs that have been developed at various laboratories for a variety of purposes. In this section, methods of using results from such computations are reviewed.

The code HETC remains a sort of benchmark on all of the others. A simple example of the results of a calculation performed using this code is shown in Fig. 4.23 taken from Alsmiller's results (AL75) for 200 MeV protons incident on "thin" and "thick" aluminum

targets. It is a plot of r^2H as a function of angle for several intervals of θ in a *spherical* concrete shield with the beam incident on a target at the center of the sphere.



Fig. 4.23 HETC calculations of r^2H as a function of CONCRETE shield thickness, *d*, averaged over several intervals of θ for 200 MeV protons incident on an aluminum target centered in a spherical shield. [Adapted from (Al75).]

For higher energies, CASIM and FLUKA have also served the role as benchmark programs while MARS is probably now the most versatile. CASIM was developed as a very "fast" code in terms of computational speed while FLUKA and MARS include the details of more physical effects. Representative results for solid iron and concrete cylinders bombarded by protons of various energies are provided in Figs. 4.24, 4.25, and 4.26. These values allow one to estimate the dose equivalent per incident proton at various locations and for various proton beam energies. They are also useful for obtaining a quick understanding of the effects of a beam absorber. Detailed calculations should be performed to assure adequately accurate designs.



Fig. 4.24 Variation of the dose equivalent per proton at the position of the longitudinal maximum multiplied by the square of the radius, Hr^2 , versus radius, r, for proton-induced cascades in IRON of density 7.2 g cm⁻³. The coordinate r is defined as in Fig. 4.22. The results are fits to calculations obtained using FLUKA and MARS. [Adapted from (Sc90).]



Fig. 4.25 Dose equivalent per proton, H, on the longitudinal axis, Z, as a function of depth Z in the shield for proton-induced cascades in IRON of density 7.2 g cm⁻³. The curves are the result of CASIM calculations for incident proton momenta of 100 GeV/c, 1 TeV/c, and 10 TeV/c and FLUKA results for 10 GeV/c. [Adapted from (Sc90).]



Fig. 4.26 Dose equivalent per proton, *H*, on the longitudinal axis, *Z*, as a function of depth, *Z*, in the shield for proton-induced cascades in CONCRETE of density 2.4 g cm⁻³. The curves are the result of CASIM calculations for incident proton momenta of 100 GeV/c, 1 TeV/c, and 10 TeV/c and FLUKA results for 10 GeV/c. [Adapted from (Sc90).]

4.7.2 General Comments on Monte Carlo Star-to-Dose Conversions

Several of these codes calculate the **star density** as their most basic output quantity. This quantity, generally denoted by S, is more correctly called the density of inelastic interactions (stars cm⁻³) and is relatively easy to tabulate as the calculation proceeds since only a simple counting process is involved. The term "star" comes from historic cosmic ray experiments in which the high energy interaction events, with their large multiplicities, appeared as tracks originating from a point. In a shield comprised of more

than one material, the star density may change dramatically from one material boundary to the other, reflective of differing material densities and atomic numbers. A related quantity is the **star fluence**, denoted by Φ_S , that is the product of the star density and the nuclear interaction length. The star fluence roughly corresponds to the fluence of hadrons having energies above that where the cross section "levels off" and is, furthermore, reflective of any "artificial" thresholds in the calculation. In contrast to the situation found with star density, due to the property of continuity the star fluence is conserved across material boundaries.

The **dose equivalent per star density** conversion factor is a rather important ingredient of radiation protection calculations. Perhaps the best results have been provided by Stevenson (St86). While this conversion factor is somewhat dependent upon the position in the shield, after a shield thickness sufficient to establish "equilibrium" spectra, a constant value may be used for high energy protons (i.e., $E_{proton} > 1$ GeV), and other hadrons, within a given material. In other words, the energy and spatial dependences are rather weak. These values for these quantities, as well as the related **dose equivalent per star fluence conversion factors**, are given in Table 4.8.

Table 4.8 Coefficients to convert star densities, S, and star fluence, Φ_S , into dose equivalent. A star density is transformed into the corresponding star fluence by the relation $\Phi_S = S\lambda$ where λ is the nuclear interaction length. [Adapted from (St86).]

Proton Energy	Absorber Material	Dose Equivalent/Star	λ (cm)	Dose Equivalent/Star
(GeV)		Density (Sv cm ³ /star)		Fluence (Sv cm ² /star)
		$(\mathbf{x} 10^{-6})$		$(x \ 10^{-3})$
10	Iron ^a	2.04 <u>+</u> 0.06	17.1	1.19 <u>+</u> 0.04
100	Iron ^a	2.15 <u>+</u> 0.08	17.8	1.21 <u>+</u> 0.05
1000	Iron ^a	2.12 <u>+</u> 0.08	17.2	1.23 <u>+</u> 0.05
Mean	Iron ^a	2.10 <u>+</u> 0.04		1.21 <u>+</u> 0.02
100	Aluminum	4.62 <u>+</u> 0.17	38.6	1.20 <u>+</u> 0.04
100	Tungsten	1.19 <u>+</u> 0.05	9.25	1.29 <u>+</u> 0.05
	Concrete	4.9	40.0	1.22
Mean	All			1.22 <u>+</u> 0.02

^aAs discussed in detail in Section 6.3.5, iron shielding presents a unique problem due to the copious emission of low energy neutrons in shields of modest thickness. The values reported here are for relatively thin iron shields of only one or two mean free paths. If a thick iron shield is encountered that is not "finished" with at least 50 cm, or so, of concrete as the outermost layer, one should multiply these conversion factors by a factor of approximately 5.

Compilations of such calculations have been given by Van Ginneken (Va75 and Va87) and by Cossairt (Co82b). Schopper et al. (Sc90) have also compiled a comprehensive set of Monte Carlo results. A convenient way to display these results is to provide contour plots of star density as function of longitudinal coordinate, Z, and radial coordinate, R,

assuming cylindrical symmetry. Appendix C provides examples of the results of such hadronic Monte Carlo calculations that are meant to illustrate a number of situations commonly encountered. One of the salient advantages of the Monte Carlo method is the ability to handle configurations of arbitrary complexity and results for both solid cylinders and more complicated example configurations are provided in Appendix C.

4.7.3 Shielding Against Muons at Proton Accelerators

The production of muons has been discussed previously in Section 4.2.4. At the higher energies, there are significant complications in that muon creation mechanisms, in addition to the production of pions and kaons and their subsequent decays, are possible. However, the muons from pion decay and kaon decay generally, but not universally, represent the most important consideration in practical shielding calculations. In Monte Carlo calculations, it is straightforward to "create" muons and follow them through the shielding medium. Muon transport is well understood, as discussed in the preceding chapters.

The particle energy downgrades quickly in hadronic showers so the most penetrating muons must originate in the first few generations of the cascade process. These energetic muons are not distributed over a large volume of space as are the neutrons. However, geometric effects or deflections by magnetic fields encountered near the point of production can affect the muon fluence at large distances. Thus, the presence of large "empty" spaces, that is, decay paths (vacuum or air), near the point of interaction provide opportunity for the pions or kaons to decay into muons before they can be removed by nuclear interactions in solid materials. This is particularly important for the typical situation of a target used to produce secondary beams followed (downstream) by an air or vacuum gap (the space for decay into muons) and then a beam absorber. If magnetic fields are present, the muon fluence generally peaks in the bend plane. Multiple Coulomb scattering from nuclei is an important effect in muon transport.

Generally the most copious sources of muons are those due to the decay of pions and kaons. There are several important facts about such muons that are summarized below:

A. The decay length (mean length for π or K to decay), Λ , is given by

 $\Lambda_{\pi} = 55.9p$ (meters), where *p* is the pion momentum in GeV/c, and $\Lambda_{K} = 7.51p$ (meters), where *p* is the kaon momentum in GeV/c.

The available decay path in conjunction with the decay length can be used to estimate the total number of muons present. For example, a beam of 10^7 pions at 20 GeV/c will decay in a distance of 50 meters into 10^7 x [50 meters]/[(56 x 20) meters decay length] = 4.5 x 10^5 muons. This uses the fact that the decay path (50 meters) is small compared with the mean decay length of 1120 meters. If the decay path, *x*, was comparable to the decay length, Λ , the final intensity would need to be multiplied by the exponential factor {1 - exp(x/Λ)}.

B. If $\beta \approx 1$, relativistic kinematics determines that the ratio, k_i , of the *minimum* momentum of the daughter muon (p_{\min}) to the momentum of the parent pion or kaon (p_i) is given by

$$k_i = p_{\min}/p_{\text{parent}} = (m_{\mu}/m_{parent})^2 . \qquad (4.47)$$

The result is that k_i has a value of 0.57 for muons with pion parents and 0.046 for muons with kaon parents. Thus if, say, a beam transport system restricts the momentum of pions to some minimum value, then the momentum of the decay muons has a minimum value given by the above.

C. Since in the frame of reference of the kaon or pion parent the decay is isotropic, and there is a one-to-one relationship between the muon momentum, p, and the angle of emission, for $p >> m_{parent}$ (in units where c = 1) the momentum spectrum of the muons can be expressed as

$$\frac{dN}{dp} = \frac{1}{p_{parent}(1-k_i)} \quad . \tag{4.48}$$

This means that the spectrum of daughter muons uniformly extends from the momentum of the parent down to the minimum established in Eq. (4.47).

D. Relativistic kinematics also gives the result that the maximum angle, θ_{max} , in the laboratory frame of reference, between the momentum vector of the muon and that of the parent particle is given by

$$\tan \theta_{\max} = \frac{(m_{parent}^2 - m_{\mu}^2)}{2p_{parent}m_{\mu}}.$$
(4.49)

For muons originating from pion decay, θ_{max} is at most several milliradians. However, for muons originating from, say, the decay of 5 GeV kaons, θ_{max} is a relatively large 12°. Thus $\pi - > \mu$ decays can be assumed to be approximately collinear while K $- > \mu$ decays have significant divergence at the lower energies.

Monte Carlo calculations are needed to adequately describe the production and transport of muons because of the sensitivity to details of the geometry that determine the pion and kaon flight paths and influence the muon populations. Schopper et al, (Sc90) has presented some useful information about the yield of muons that one can use to make approximate estimates by giving calculated values of angular distributions of muon spectra with an absolute normalization from pion and kaon decays for one meter decay paths. Neither the effects of absorbers nor magnetic fields are included in these results. For other decay paths that are short compared with the decay length, one can simply scale by the length of the actual decay path in meters. The results are displayed in Fig. 4.27.



Fig. 4.27 Yield of muons from the decay of pions and kaons of both charges produced in proton-Fe collisions at several energies of the incident proton. The distance available for decay (the decay path) is taken to be 1 meter. The abscissa, E_{μ}/E_p , is the muon energy expressed as a fraction of the incident proton energy. The ordinate, $dY/d\Omega$, is the number of muons per unit solid angle (sr⁻¹) per incident proton having an energy greater than E_{μ} . All values are for $\theta = 0$. [Adapted from (Sc90).]

Decays of other particles can be important sources of muons at higher energies, especially those found in hadron-hadron collisions at high energy colliders. Especially notable are those from charm (D) and bottom (B) meson decays (Sc90). The muons from these sources are often called **direct muons** due to the short lifetimes and decay lengths

involved. The masses of these parent particles and their mean-lives, τ , are as follows (PDG04):

$$m(D^{\pm}) = 1869.4 \pm 0.5 \text{ MeV}, \ \tau = (1.040 \pm 0.007) \text{ x } 10^{-12} \text{ s}, \ c\tau = 311.8 \ \mu\text{m} \text{ and} \ m(B^{\pm}) = 5279.0 \pm 0.5 \ \text{MeV}, \ \tau = (1.671 \pm 0.018) \text{ x } 10^{-12} \text{ s}, \ c\tau = 501 \ \mu\text{m}.$$

Figures 4.28 and 4.29 give results for muons originating from these decays in the same format as used in Fig. 4.27. The length of the decay path is irrelevant for these small values of $c\tau$.



Fig. 4.28 Yield of muons from the decay of D-mesons produced in proton-proton collisions at four incident proton energies and at $\theta = 0$. The abscissa, E_{μ}/E_p , is the muon energy expressed as a fraction of the incident proton energy. The ordinate, $dY/d\Omega$, is the number of muons per unit solid angle (sr⁻¹) per incident proton having an energy greater than E_{μ} . [Adapted from (Sc90).]



Fig. 4.29 Yield of muons from the decay of B-mesons produced in proton-proton collisions at various energies of the incident proton and at $\theta = 0$. The abscissa, E_{μ}/E_p , is the muon energy expressed as a fraction of the incident proton energy. The ordinate, $dY/d\Omega$, is the number of muons per unit solid angle (sr⁻¹) per incident proton having an energy greater than E_{μ} . [Adapted from (Sc90).]

Sullivan's approximation for muons is a method of estimating muon flux densities at proton accelerators based upon a semi-empirical fit to existing muon production data (Su92). Sullivan gives an equation for the flux density of muons per meter of decay path as a function of shield thickness found along the proton beam axis (that is, on the straight-ahead maximum of the muons);

$$\Phi = 0.085 \frac{Ez}{Z^2} \exp\left\{-\frac{\alpha t}{E}\right\},\tag{4.50}$$

where Φ is the fluence (muons m⁻²) per interacting proton, *E* is the proton beam energy (GeV), *Z* is the distance of the point of concern to the point of production of the pions and kaons (meters), *z* is the average path length (i.e., the decay path) of the pions and kaons in air, gases, or vacuum prior to their absorption by solids or liquids, and α is an effective average energy loss rate (GeV meter⁻¹) for the muons in a shield of thickness *t* (meters). Values of α for typical shielding materials are provided in Table 4.9. *z* can be taken to be the actual physical length of the decay path, or according to Sullivan, for a solid beam absorber, *z* can reasonably be taken to be 1.8 times the hadron nuclear interaction mean free path for the material comprising the beam absorber. It is obvious that the argument of the exponential in Eq. (4.50) can be expanded as the sum over the materials comprising a composite shield. Sullivan has also given a prescription for calculating the full width at half maximum, FWHM, of the muon distribution at the boundary of such a shield. This is given by

$$FWHM = 4.6 \frac{Z}{\sqrt{E\alpha t}} \text{ (meters).}$$
(4.51)

Table 4.9	Values of	α for	typical	shielding	materials	for	use	in	Eqs.
(4.50) and (4	4.51) accor	rding to	o Sulliv	an (Su92).					

Material	α (GeV m ⁻¹)	Density, ρ (g cm ⁻³)
Concrete ^a	9.0	2.35
Water	4.0	1.0
Iron	23.0	7.4
Lead	29.0	11.3

^aThe value for concrete can be used for earth if one adjusts it to the correct density.

Problems

- 1. One can use measurement results to check Sullivan's formula, Eq. (4.4), for hadron fluence above 40 MeV for high-energy proton interactions. Check the agreement for the 22 and 225 GeV/c data in Figs. 4.7 and 4.8 for 3 representative angles at one meter. (Ignore the fact that the formula is for hadrons > 40 MeV while the only data provided is for hadrons >35 MeV and > 50 MeV, but do <u>not</u> ignore the difference between normalizing to <u>incident</u> versus <u>interacting</u> protons.) (It is valid to make the comparison on yield <u>per interacting</u> proton since the results in Fig. 4.8 is for targets approximately 1 interaction length long.) Comment on the quality of the agreement.
- 2. Calculations can also be used to check the Tesch curve for dose equivalent at $\theta = 90^{\circ}$ (Fig. 4.10). Use the 200 MeV calculations in Fig. 4.4 to do this by crudely numerically integrating the $60^{\circ} < \theta < 90^{\circ}$ yields to determine the average energy of the neutrons and the total fluence at $\theta = 90^{\circ}$ and at 1 meter. Use the results along with dose equivalent per fluence curves to obtain the dose equivalent per proton to compare with Tesch's result. (Iron is considered equivalent to copper for this problem.)
- 3. A copper target at an accelerator is struck by $1 \mu A$ of 100 MeV protons.
 - a) Use Tesch's curve in Fig. 4.10 to calculate the dose equivalent rate at 2 m and $\theta = 90^{\circ}$ relative to this target.
 - b) Compare this result with the neutron dose equivalent rate calculated in Chapter 3, Problem 5 for an <u>electron</u> accelerator having the same intensity and beam energy and discuss. (Scale the relevant result of Chapter 3, Problem 5 by the appropriate yield for copper versus tungsten.)
- 4. It is often necessary to work from fragmentary data to determine other quantities.
 - a) Use McCaslin's results, Eqs. (4.13, 4.14, and 4.15), and the appropriate dose equivalent/fluence to calculate the dose equivalent rate at 1 meter and at $\theta = 30^{\circ}$ for a target struck by 10^{8} 670 MeV/amu ²⁰Ne ions per sec. (Hint: Use all available spectrum information.)
 - b) Use McCaslin's results to obtain the total yield of neutrons per ion with $E_n > 6.5$ MeV. Assuming the target to be iron or copper, how does this yield correspond to that due to 700 MeV protons? Do this for both $E_n > 6.5$ MeV and $E_n > 20$ MeV to understand the overall composition. Hint: Integrate over the unit sphere (double integral over spherical coordinates $\theta \& \phi$) and convert all quantities associated with angles from degrees to radians.

The following indefinite integrals are needed:

$$\int \frac{dx \sin x}{x} = x - \frac{x^3}{3 \cdot 3!} + \frac{x^5}{5 \cdot 5!} - \frac{x^7}{7 \cdot 7!} + \dots$$
$$\int dx e^{ax} \sin bx = \frac{e^{ax} [a \sin bx - b \cos bx]}{a^2 + b^2}$$

The elemental area on the sphere of radius r is $dA = r^2 \sin \theta d\theta d\phi$, where ϕ is the standard azimuthal coordinate in a spherical coordinate system.

- 5. It is asserted that if the assumption is made that the limiting attenuation is simply geometric, with the nucleon radius equal to 1.2 x 10⁻¹³ cm, then $\rho\lambda_{atten} = 36.7A^{1/3}$ (g cm⁻²). Show this to be the case using the volume of a nucleus and nucleons along with the cross section.
- 6. a) Use the Moyer Model to calculate the dose equivalent rate (mrem/hr) lateral ($\theta = 90^{\circ}$) to a magnet centered in a 1.5 m radius tunnel. The magnet is struck by 10^{12} protons at 100 GeV (per sec). The tunnel walls consist of 1/3 m concrete followed by soil having the same composition [ρ (concrete) = 2.5 g cm⁻³, ρ (soil) = 2.0 g cm⁻³]. Perform the same calculation for several thicknesses of soil out to 6 meters of soil radially. Do this for increments of 1 meter from 1 meter to 6 meters of soil.
 - b) Calculate the result if the same beam loss occurs uniformly over a string of such magnets 100 meters long in the same tunnel at the same soil thicknesses as above. Use the Tesch approximation. Approximately how many meters of beam loss does it take to cause 90% of the calculated dose equivalent rate at 6 m of lateral soil shield?
 - c) For the point loss in part a), at what value of θ does the maximum dose equivalent rate occur and what is its magnitude outside of 6 meters of soil shield? (Use successive approximations to solve.)
- 7. An accelerator delivers 10^{12} 1 TeV protons per second head-on on the inner edge of a magnet. Use the CASIM calculations found in Appendix C to determine the approximate dose equivalent rate at R = 400 centimeters and compare with a result using the Moyer equation for point loss. Both calculations should be at the location of the maximum dose equivalent. Assume ρ (concrete) = 2.5 g cm⁻³ and ρ (soil) = 2.25 g cm⁻³. Why might there be an explainable disagreement between the two results?

- 8. Using the results of Monte Carlo hadron calculations (FLUKA/MARS), calculate, for solid shields of iron (cylinders), what longitudinal thickness of iron is needed to achieve the same <u>hadron</u> dose equivalent per proton on the beam axis as found at R = 50 cm at 10 GeV/c, 100 GeV/c, 1000 GeV/c and 10 TeV/c. Use the maximum value of H (r = 50 cm).
- 9. In Fig. 4.4, we have calculations of neutron energy spectra for 200 MeV protons incident on various targets, including aluminum. In Fig. 4.23, calculations of dose equivalent values for spherical concrete shielding surrounding aluminum targets at $E_p = 200$ MeV are given. At shielding thicknesses approaching zero and at forward angles, are the two results in "sensible" (that is, approximate, agreement)? (Hint: "Integrate" crudely over the forward spectrum to obtain the fluence/proton and convert this fluence to dose equivalent.)
 - a) Make the comparison for zero shield thickness and in the angular range $0 < \theta < 30^{\circ}$.
 - b) Now use the shielding calculations to obtain the dose equivalent rate (rem h⁻¹) due to a 1 μ A beam incident at 200 MeV on such a thick target at a distance of 4 m from the target with 0, 1, 2, & 3 m of intervening concrete shielding ($\rho = 2.5$ g cm⁻³) for $\theta = 15^{\circ}$ and $\theta = 75^{\circ}$. (Hint: Use the center of the angular bins.)
- 10. Assume that a target is struck by 100 GeV protons and that a 10 m long decay space exists for π and K decay. Use the curves in Fig. 4.27 to crudely estimate the muon flux density and dose equivalent rates (mrem/h) at 1 km away and at $\theta = 0^{\circ}$ if 10^{12} protons/second are targeted in this manner if the following additional assumptions are made:
 - a) Assume that there is no shielding present and neglect air scattering and inscattering from the ground. (Hint: The muon yield for this decay space will scale with the length of the decay space.)
 - b) Assume there is 100 meters of intervening shielding of earth ($\rho = 2 \text{ g cm}^{-3}$) (Hint: use Fig. 1.9 range-energy curves to determine the mean energy of muons which will penetrate this much shielding). Neglect multiple scattering and range-straggling.
 - c) If the beam operates for 4000 h yr⁻¹, is 100 mrem yr⁻¹ exceeded? Will multiple scattering increase or decrease this dose equivalent? (Answer both questions for the soil-shielded case only.)
 - d) Repeat Part b) of the same calculation using Sullivan's semi-empirical approach. If the disagreement between the results obtained using the two methods is large, suggest an explanation of a possible cause of the difference.

5.1 Introduction

In this chapter two phenomena are discussed that involve low-energy neutrons. These processes are the transmission of photons and neutrons through penetrations and the control of neutron "skyshine". They arise at all accelerators that operate at energies above the threshold for producing neutrons. The general behavior of both of these phenomena is qualitatively independent of incident particle type and energy.

5.2 Transmission of Photons and Neutrons Through Penetrations

All accelerators evidence the need to control the transmission of neutrons by penetrations since all have accessways to permit entry of personnel and equipment as well as penetrations for cables and for radio-frequency (RF) waveguides. Personnel access penetrations will typically have cross-sectional dimensions of about 1 meter by 2 meters (door-sized) while utility ducts will generally be much smaller, typically no larger than 0.2 by 0.2 m. Often the utility penetrations are partially filled with cables and other items, and even cooling water in pipes.

Two general rules are advised for all penetrations of accelerator shielding:

- A penetration should not be arranged so that a particle or photon beam is aimed directly toward it. This is needed to assure that the penetrations are transmitting primarily neutrons that result from large angle scattering rather than those arising from the forward peaked neutron radiation fields or from the direct beam.
- For any labyrinth, the sum of the wall thickness between the source and the "outside" should be equivalent to that which would be required if the labyrinth were not present.

5.2.1 Albedo Coefficients

Before describing the details of penetration design, one should review some simple parameterizations of the reflections of photons and neutrons. These reflections can be treated through the use of **reflection** or **albedo coefficients**. Such coefficients account for the reflection of particles analogous to the reflection of visible light by various kinds of surfaces. They take into account the appropriate *microscopic* cross sections in a *macroscopic* way. These have applications more general than merely the design of penetrations. Figures 5.1 and 5.2 give the albedo coefficients α_x and α_n for monoenergetic photons and neutrons, respectively, incident on flat surfaces of infinite dimensions of concrete plotted as functions of neutrons is typically larger and somewhat less strongly dependent on energy than is that of photons. Chilton et al. have given more detailed results for concrete and for other materials (Ch63, Ch64, Ch65a, Ch65b, and Ch84). A good summary is provided in (NC03).



Fig. 5.1 Reflection coefficients, α_{χ} , for monoenergetic PHOTONS incident on ordinary concrete as a function of incident photon energy for several angles of reflection assuming normal incidence (**top frame**) and for equal angles of incidence and reflection ($\theta_{I} = \theta_{R}$) (**bottom frame**). For photon energies higher than 10 MeV, the use of the 10 MeV values of α_{χ} is expected to be conservative. [Adapted from (NC03) and references cited therein.]



Fig. 5.2 Reflection coefficients, α_n , for monoenergetic NEUTRONS incident on ordinary concrete as a function of incident neutron energy for several angles of reflection assuming normal incidence (**top frame**) and for equal angles of incidence and reflection ($\theta_1 = \theta_R$) (**bottom frame**). [Adapted from (NC03) and references cited therein.]

5.2.1.1 Usage of Photon Albedo Coefficients

A particular application of these coefficients to the design of labyrinths is given here as an illustration. Figure 5.3 shows an example of a labyrinth providing access to a collimated photon source of some known dose equivalent (or dose equivalent rate, with inclusion of units of inverse time), H_0 , determined at some reference distance, d_0 . To use these coefficients correctly, some knowledge of the photon energy spectrum at this location is also needed. Such a photon "beam" is relevant to the subject of this text since, for example, such a beam can arise from the forward-peaked photons due to the targetry of a beam from an electron accelerator. With the reflection coefficients α_x , one can use the following formula to obtain a conservative estimate of the dose equivalent (or dose equivalent rate), H_{rj} , after *j* sections (not counting the initial path length to the wall, d_i) of the maze:

$$H_{r_{j}} = H_{0} \left(\frac{d_{0}^{2}}{d_{i}^{2}} \right) \left(\frac{\alpha_{1}A_{1}}{d_{r_{1}}^{2}} \right) \prod_{k=2}^{k=j} \left(\frac{\alpha_{k}A_{k}}{d_{r_{k}}^{2}} \right), \ j > 1.$$
(5.1)

In this formula, the coefficient α_1 is selected to be representative of that expected at the *initial* photon energy while A_1 estimates the cross sectional area of the wall struck by the initial photons evaluated by projecting the beam profile to the wall. A_k , for k > 1, is the cross-sectional area of the k^{th} leg of the maze, not including the first. The first parenthetical factor is just inverse square propagation of the beam to the wall, the second models "reflection" into the first leg, and the product factor models reflection into the remaining legs. For right angle labyrinths such as this one, it is reasonable to use the values plotted for normal incidence ($\theta_I = 90^0$), $\theta_R = 75^\circ$. For successive legs after the first, taking the value of α_k to be that appropriate for 0.5 MeV photons is often considered to be a conservative approach. This is logical because if E_0 is the initial photon energy in MeV, the energy of the scattered photon, E_{scatt} (MeV), following Compton scattering is given by

$$E_{scatt} = \frac{E_0}{1 + (E_0 / 0.511)(1 - \cos\theta)}.$$
 (5.2)

Thus, E_{scatt} has a maximum value of 0.511 MeV after a scatter of 90° for $E_0 >> 0.511$ MeV, the rest energy of the scattered electron. If the maze is of uniform cross section, A, and has j legs, then the product in the numerator is simply αA raised to the $(j-1)^{\text{th}}$ power, $(\alpha A)^{j-1}$, where $\alpha = \alpha_k$ for all legs after the first. In the denominator, the distances are just those defined in Fig. 5.3 and, of course, represent the inverse-square law dependence. This formula is "conservative" for photon energies exceeding 10 MeV, but at the higher energies the uncertainties are larger. The above formula is probably most accurate if the ratios $d_{rk}/(A_k)^{1/2}$ lie between 2 and 6 (NC03).



Fig. 5.3 Generalized labyrinth design illustrating successive reflections of photons from a collimated source through the maze. The source could just as well originate from an electron beam originating from the right side of the figure incident on a target located at the point in space labeled "collimated x-ray source". The various path lengths can be approximated by a sequence of centerline distances, as shown in the diagram. [Reproduced from (NC03).]

5.2.2 Neutron Attenuation in Labyrinths-General Considerations

Unfortunately, the more complex physics of the transport of neutrons discourages the use of a similar formula similar to that employed above using photon albedo coefficients. The radiation source, or potential radiation source for situations of concern from the standpoint of accidental beam losses, should be evaluated according to the methods described previously. Typical methods for addressing the attenuation of radiation by penetrations involve the use of the results of calculations performed using Monte Carlo codes. These can be used for both rectilinear and curved labyrinths with the primary practical experience being with the former. In this section, the results of such work will be presented in order to give the reader useful information in the evaluation of such penetrations. A typical rectilinear personnel access labyrinth is shown in Fig. 5.4.



Fig. 5.4 Schematic plan view of a typical personnel access labyrinth of three "legs" at a large accelerator facility that defines the coordinate system and terminology associated with labyrinth calculations. The (*) denotes the location of a loss of beam at a point adjacent to the "mouth" of the labyrinth. The lengths of legs after the first are measured between <u>centers</u> of turns.

An overwhelming conclusion drawn from existing body of data is that the bombarding particle energy, or even particle type, has very little effect upon the attenuation by a labyrinth viewing a source of beam loss other than the fact that the total yield of "source" neutrons increases as a function of incident energy and ion type. One can thus estimate the dose, dose equivalent, or neutron fluence at the exit of a labyrinth by using attenuation estimates in the **legs** multiplied by an estimate of the neutron fluence or dose

equivalent found at the entrance, or **mouth**, of the penetration into the beam enclosure. The validity of this **factorization approximation** allows attenuation measurements and calculations obtained at proton accelerators to be of rather general utility.

5.2.3 Attenuation in First Leg of Rectilinear Penetrations or in Straight Penetrations

For penetrations exposed to targets struck by hadrons, we first consider the straight penetration studied by Gilbert et al. (Gi69) who measured the transmission of an exceptionally long straight tunnel of dimensions 2.8 m high by 1.8 m wide and 100 m long. 14 GeV protons were incident on a target providing a good "point source" 3.2 m from the tunnel mouth. The use of a set of activation detectors having different energy thresholds made it possible to obtain some information about the neutron energy spectrum as well. The measurement technique employed will be discussed in somewhat more detail in Chapter 9. An absolute normalization to beam loss was not reported. Table 5.1 gives the thresholds, or approximate sensitive domains, of nuclear reactions used in this particular measurement (see Section 9.5.3). The dosimeters used to detect photons are also sensitive to gamma rays produced by the capture of neutrons by the nuclei in the air and in the tunnel walls.

Table 5.1 Detectors and their characteristics as used in the measurements summarized in Fig. 5.5. The sensitive energy ranges are approximate. [Adapted from (Gi69).]

Detector	Nuclear Reaction	Energy Range (MeV)
βy Dosimeters	photons and charged particles	all
Gold (Au)	$^{197}Au(n, \gamma)^{198}Au$	Thermal Energies
Aluminum (Al)	27 Al(n, α) 24 Na	E > 6 MeV
Carbon (C)	$^{12}C(n, 2n)^{11}C$	E > 20 MeV

The results of the measurements are presented in Fig. 5.5. The "fits" to the relative response, R, as a function of depth in the penetration, d, shown in this figure were arbitrarily normalized to the measurements at a depth of 20 meters in the tunnel and fit by an exponential attenuation multiplied by an inverse square-law dependence;

$$R(d) = R_{20} \left(\frac{20}{d_1}\right)^2 \exp[-d_1 / \lambda(E)], \qquad (5.3)$$

where R_{20} is the response measured at $d_1 = 20$ meters and $\lambda(E)$ is an energy-dependent attenuation length.

The responses as a function of depth d_1 are quite revealing. For short tunnels (< 20 m long) the "attenuation" of the fast neutrons is almost entirely accounted for by inverse-square law considerations. For larger depths, the responses clearly illustrate that neutrons of lower energy (i.e., as illustrated by the response for gold) attenuate more rapidly by

air and wall-scattering than do the higher energy neutrons. Taking into account the inverse-square dependence for this long tunnel, the attenuation is well-described by exponential absorption functions having effective mean free paths, $\lambda(E)$, corresponding to energy-dependent removal cross sections. The $\lambda(E)$ values determined by fitting these data are given in Table 5.2. The effective removal cross sections determined by this measurement are about a factor of 1.5 to 2 smaller than those that would be inferred from the known absorption cross sections of the constituents of air. This is taken as evidence of "in-scattering" by the concrete walls since more neutrons than expected were observed at the larger distances into the tunnel.



Fig. 5.5 The relative transmission of neutron flux density and gamma dose rate along a large straight tunnel described in the text. The measurement results are shown as the symbols while the solid lines represent the fits described in the text arbitrarily normalized at a depth of 20 meters. [Adapted from (Gi69).]

Table 5.2	Mean	free	paths	and	removal	cross	sections	s for	tunnel	transmi	ssion	as
exhibited k	by the r	neası	iremei	its si	ımmarize	ed in F	ig. 5.5.	[Ada	pted fr	om (Gi69).]	

Detector	Mean Free Path	Inferred Removal Cross
	(meters)	Section (barns)
βy Dosimeters	55	3.3
Gold (Au)	30	6.2
Aluminum (Al)	60	3.2
Carbon (C)	100	1.9

An important principle is the **labyrinth scaling** rule. That is, the attenuation of neutrons in the legs of labyrinths generally scale with a unit length equal to the square root of its cross-sectional area, provided that the height to width ratio does not vary greatly outside of the range 0.5 to 2.0 (Th88). Of course, details of the source geometry are very important in such a straight penetration. Goebel [(Go75) and summarized in (Sc90)] has calculated universal attenuation curves for "first" legs of labyrinths (i.e., those sections first encountered as one moves outward from the beam). Goebel compared results from the codes SAM-CE (Co73), AMC (Ma67), and ZEUS (D'H68). Gollon and Awschalom (Go71) have generated similar curves using the ZEUS code for a variety of geometries. The three situations of point source, line source, and plane or point source off-axis for a straight tunnel displayed as universal dose attenuation curves as calculated by Goebel are given in Fig. 5.6. An off-axis point source is one that is not centered in front of the labyrinth mouth. The distance down the passageway is expressed in units of the square root of the cross-sectional area of the passageway. It is obvious that extended or off-axis sources are more readily attenuated because the tunnel aperture provides a smaller solid angle for acceptance.

It has been found by Cossairt (Co95) that Goebel's point source dependence in a tunnel of cross sectional area A can be approximated by the following expression, where $\delta_1 = (d_1 - R)/A^{1/2}$ and r_o is a fitting parameter;

$$H_1(\delta_1) = \left[\frac{r_o}{\delta_1 + r_o}\right]^2 H_o(R)$$
(5.4)

with
$$r_o = 1.4$$
. (5.5)

 $H_1(\delta_1)$ is the dose equivalent at distance δ_1 in the first leg as measured from the mouth of the passageway in "**units**" of the square root of the cross-sectional area of the first leg (see Fig. 5.4). $H_0(R)$ is the dose equivalent at the mouth the determination of which will be discussed later. The result of this fit is included in Fig. 5.6. Over the domain of $0 < \delta_1 < 9$ the expression fits the Goebel curve within ± 10 per cent, certainly sufficiently accurate for radiation protection purposes. The domain in δ_1 is an appropriate one given the fact that most "personnel" labyrinths are of cross-sectional area of about 1 x 2 m². Hence, a typical unit length is approximately 1.4 meters. A 10 "unit" long first leg is, typically, about 14 meters (or about 46 feet), a distance quite long compared with typical labyrinth legs.

Tesch (Te82) has developed a very simple approach to the problem of dose equivalent rate attenuation by multi-legged labyrinths at proton accelerators that are typical of personnel passageways of approximately 2 m² cross section. For the first leg the expression is an inverse-square law dependence with a simple factor of two included to allow for "in-scattering";

$$H_1(d_1) = 2H_0(R) \left(\frac{R}{d_1}\right)^2.$$
 (5.6)

In Eq (5.6), the distance into the labyrinth, d_1 (defined as in Fig. 5.4), is <u>not</u> scaled by the cross-sectional area of the passageway and, presumably, is valid only for personnel tunnels of approximately 2 m² cross section.



Fig. 5.6 Universal transmission curves for the first leg of a labyrinth as a function of normalized distance, δ_1 from the mouth. The fit for the point source curve represented by Eq. (5.4) is also included. The curve for a plane source is also suitable to use with an off-axis point source. [Adapted from (Go75) and (Co95).]

5.2.4 Attenuation in Second and Successive Legs of Rectilinear Penetrations

Stevenson and Squier reported the results of measurements in a two-legged penetration at the NIMROD synchrotron (St73). This penetration was of cross section 2.3 x 2.3 m² and the walls were made of concrete. The target at the mouth of the labyrinth was bombarded by 7 GeV protons. Figure 5.7 is a plot of the transmission of particle flux density along this tunnel using different nuclear reactions, again employed because of their thresholds. One can see that, proceeding from the target outward in the passageway, beyond the abrupt jump that arises as the corner hides the target from view, the fast neutron components are attenuated more readily than is the thermal one. This phenomena associated with "turning the corner" was also verified by Cossairt et al. (Co85b).



Fig. 5.7 Relative transmission of particle flux density along a two-legged labyrinth using threshold detectors. The curve labeled "**thermal**" corresponds to the measured attenuation of thermal neutrons, the curve labeled "**intermediate**" corresponds to neutrons having energies between approximately 6 and 25 MeV while the curve labeled "**high**" corresponds to neutron energies above 20 MeV. [Adapted from (St73).]

Second and successive legs of such "rectilinear" penetrations thus change the situation dramatically, principally by modifying the spectrum of the transmitted neutrons. Fig. 5.8 displays a universal curve for second and succeeding legs that can serve as a companion to that given for the first leg in Fig. 5.6. The distance from the center of the preceding turn normalized to the square root of the cross sectional area of the i^{th} leg, A_{ib} the so-called "unit length", is $\delta_i = d_i / A^{1/2}$, for second and succeeding legs.





It was found by Cossairt (Co95) that the following recursive expression adequately describes this curve, where δ_i is the distance in the *i*th leg measured in "units" of the square root of the cross-sectional area of the *i*th leg:

$$H_{i}(\delta_{i}) = \left\{ \frac{\exp(-\delta_{i}/a) + A\exp(-\delta_{i}/b) + B\exp(-\delta_{i}/c)}{1 + A + B} \right\} H_{i-1}(\delta_{i-1}) \quad i^{th} \log (i > 1),$$
(5.7)

where the fitting parameters are;

$$a = 0.17,$$
 $A = 0.21,$
 $b = 1.17,$ and $B = 0.00147.$
 $c = 5.25,$

The results of this fit are included in Fig. 5.8.

Tesch (Te82) also has developed a formula for the transmission of the second and successive legs which is

$$H_i(d_i) = \left\{ \frac{\exp(-d_i / 0.45) + 0.022A_i^{1.3}\exp(-d_i / 2.35)}{1 + 0.022A_i^{1.3}} \right\} H_{i-1} \ (i^{th} \log, i > 1)$$
(5.8)

Here A_i is the cross sectional area of the i^{th} leg in units of square meters. As was the case with respect to Eq. (5.6), this formula uses the distances, d_i (meters), along the labyrinth directly and does <u>not</u> scale them against the square root of the cross sectional area. As was the case for Eq. (5.6), the results are valid for "door-sized" labyrinths having cross sectional areas of approximately 2 m².

Figure 5.9 shows a four-legged labyrinth providing entrance to a tunnel above a target struck by 400 GeV protons accelerated by the Tevatron at Fermilab. Figure 5.10 compares experimental measurements (Co85b) of absorbed dose throughout this labyrinth with several methods of calculation. As one can see, all methods of calculating the attenuation discussed here are approximately valid even for this four-legged labyrinth. Even the first leg, while not quite having a truly "open view" of the target is handled well by these methods. Thus, the assumption that succeeding legs can be considered the same as the second leg is verified.¹²

For this labyrinth, a recombination chamber technique (see Section 9.5.7) was used to measure the neutron quality factor, Q, at two locations, one at the end of the first leg and one in the middle of the short second leg. These locations are denoted by R in Fig. 5.9. The results were $Q = 5.5 \pm 0.6$ (first leg) and $Q = 3.4 \pm 0.1$ (second leg). This indicates a reduction of the average neutron energy in the second leg which was further verified by a

¹²In the labyrinth shown in Fig. 5.9, the shielding blocks were, in fact, aligned as indicated. This is contrary to good design practice as the blocks should have been overlapped to prevent "streaming". This condition may well explain the excess of measurement over calculation at the end of the third leg.

measurement of the neutron energy spectrum (see Fig. 6.7) using a multisphere technique (see Section 9.5.2.1) that resulted in $Q = 3.1 \pm 0.7$. This spectrum was measured at the location denoted by S, in Fig. 5.9. The spectrum measured in the second leg exhibited domination by thermal, or near-thermal, neutrons. It is clear that several approaches to the design of labyrinths are equally effective for practical radiation protection work.



Fig. 5.9 Labyrinth enclosure in which 400 GeV protons interacted with an aluminum target located beneath the floor as shown. The neutron energy spectrum was measured at the location denoted "S" and the quality factor of the radiation field was measured at the locations denoted "**R**". [Adapted from (Co88).]



Fig. 5.10 Measurements and predictions of transmission in a tunnel at Fermilab. The results of Tesch (Te82), Goebel et al. (Go75), and Gollon and Awschalom (Go71) are compared with measurements of absorbed dose conducted at the position shown in the four-legged labyrinth displayed in Fig. 5.9. Fortuitously, the "Transmission Factor" plotted as the ordinate is also the absolute scale of the absorbed dose measurement in units of mrad/10¹⁰ incident 400 GeV protons (fGy proton⁻¹). [Reproduced from (Th88) and (Co85b).]

5.2.5 Attenuation in Curved Tunnels

Curved tunnels are principally used to provide access for large equipment items that cannot negotiate right-angle bends. These have not been treated in nearly the same detail as have the rectilinear passageways. It appears that the attenuation is described by an exponential function having an attenuation length, λ , that is only a function of the radius, R, of the tunnel. Patterson and Thomas (Pa73) determined that

$$\lambda = 0.7\sqrt{R} \,, \tag{5.9}$$

where *R* is in meters and 4 < R < 40 meters. Thus, the dose equivalent, H(r), or fluence at any circumferential distance through the tunnel, *x*, is given by

$$H(x) = H_o \exp(-x/\lambda), \tag{5.10}$$

where x and λ are expressed in mutually consistent units.

5.2.6 Attenuation Beyond the Exit

A final piece of information that is sometimes needed in practical labyrinth calculations is the answer to the question; "What happens to the neutrons beyond the "exit" to the passageway?" Direct observational evidence is that beyond the exit, the neutrons "disappear" rather rapidly. This phenomenon is probably due to the fact that the neutron energy spectrum is heavily dominated by thermal and near-thermal neutrons in all "legs" after the first. Such neutrons, therefore, having suffered many scatters would not be collimated in any particular direction, being a thermalized "gas". Elwyn (El91) has quantified this phenomenon by assuming that the exit of the labyrinth is a circular disk of area A, equivalent in area to that of the exit opening. Further, it is assumed that the neutrons emerge from this disk at all random directions with source strength (neutrons/unit area, during some time interval) S_A . Fig. 5.11 illustrates the geometry. It is also assumed that there is only emission into the 2π steradian hemisphere outside the exit. Then the differential flux density at P on the axis of the disk is

$$d\phi = \frac{S_A \cos \alpha \, dA}{2\pi\rho^2},\tag{5.11}$$

where $dA = rdrd\theta$, $\rho^2 = h^2 + r^2$, and angle α is defined in Fig. 5.11 (cos $\alpha = h/\rho$). The cos α factor is present to take into account the solid angle of the source elemental area subtended at point *P*.



Fig. 5.11 Diagram of labyrinth exit neutron calculation. The coordinates are explained in the text.

Thus,

$$d\phi = \frac{S_A hr}{2\pi\rho^3} dr d\theta \,. \tag{5.12}$$

Integrating,

$$\phi(h) = \frac{S_A h}{2\pi} \int_0^R dr \int_0^{2\pi} d\theta \frac{r}{\left(r^2 + h^2\right)^{3/2}} = S_A h \int_0^R dr \frac{r}{\left(r^2 + h^2\right)^{3/2}}$$

where attenuation by the air is neglected. Thus one can use this by approximating the area of the exit opening by the area of a disk have an equivalent area. At large distances, one can apply a "point source" approximation due to the fact that

$$\phi(h) \approx \frac{S_A}{2} \left(\frac{R}{h}\right)^2 \quad \text{for } h >> R.$$
 (5.14)

For h = 0, $\phi(0) = S_A$ as expected. This calculation neglects neutron absorption by the intervening air.

The rapidity of the decrease of fluence is illustrated by the tabulation of a few values in Table 5.3.

	¥	
h/R	$\phi(h)/S_A$	
0.5	0.55	
1.0	0.29	
2.0	0.11	
4.0	0.03	
10.0	0.005	

 Table 5.3 Estimates of relative neutron flux or dose equivalent as a function of scaled distance from the exit of a labyrinth.

To summarize thus far; one can use a calculation or measurement of the neutron flux density or dose equivalent at mouth of the labyrinth in conjunction with one of the above methods of calculating the attenuation of the neutrons by the passageway to get an estimate of the dose equivalent or fluence at the exit of the passageway.

5.2.7 Determination of the Source Factor

Generally, the dose at the mouth of a labyrinth can be obtained using Monte Carlo techniques or by directly using the information about neutron yields. For protons, approximations that use Moyer Model parameters discussed in Chapter 4 are likely to overestimate the dose equivalent at the entrance. This is because the Moyer parameters implicitly assumes development of the shower (intrinsically a "buildup" mechanism, as seen in Chapter 4) in the enclosure shielding. This buildup does not happen in the passageway.

For high energy proton accelerators, a rule of thumb for the source term which has been found to be very successful for the degree of accuracy generally required for personnel protection purposes has been developed by Ruffin and Moore (Ru76). It was improved by inclusion of Moyer energy scaling by Rameika (Ra91). In this model, it is seen that about one fast neutron GeV^{-1} of proton beam energy is produced with an isotropic distribution in addition to the much higher multiplicity in the forward direction. The neutrons that will dominate the spectrum and determine the dose equivalent at the entrance to the labyrinth have kinetic energies between 1 to 10 MeV. From the dose equivalent per fluence factors, P(E), in Fig. 1.5, one rem of 10 MeV neutrons represents a fluence of approximately 3 x 10^7 cm⁻² for neutrons over this energy domain.

Thus, at distance R (cm) from the source, one obtains

$$H(rem) = \frac{E_0^{0.8} N_p}{4\pi R^2 (3 \times 10^7)} = 2.65 \times 10^{-9} \frac{E_0^{0.8} N_p}{R^2},$$
(5.15)

where E_0 is in GeV, and N_p is the number of incident protons. The constant, 2.65 x 10⁻⁹ (rem cm²), turns out to be approximately one-third the value obtained by using the Moyer source parameter along with high energy value of the Moyer angular factor at $\theta = \pi/2$ [Eqs. (4.38) and (4.41)];

$$(2.8 \times 10^{-7} \text{ rem cm}^2)\exp(-2.3\pi/2) = 7.6 \times 10^{-9} \text{ rem cm}^2.$$
 (5.16)

To obtain the source factor for neutrons produced by electrons, the neutron yields discussed in Section 3.2.4 can be utilized.

5.3 Skyshine

Thin roof shielding represents a serious problem that has plagued a number of accelerators such as the Cosmotron (at Brookhaven National Laboratory), the Bevatron (at the Lawrence Berkeley National Laboratory), the Fermilab experimental areas, and likely elsewhere. The phenomenon, known as skyshine, is the situation in which the roof of some portion of the accelerator or an associated experimental facility is shielded more thinly than are the sides of the same enclosure that directly view the radiation source. The first attempt to calculate the skyshine radiation field was made by Lindenbaum (Li61). Schopper et al. (Sc90) give a rather complete description of the phenomena and Patterson and Thomas (Pa73), Rindi and Thomas (Ri75), Stevenson and Thomas (St84a), and Cossairt and Coulson (Co85c) present some specific results. Neutron skyshine, while it is usually "preventable" through the application of sufficient roof shielding, has been encountered at nearly all major accelerators. This has resulted either from lack of consideration of it at the design stage or from the need to accommodate other constraints such as the need to minimize the weight of shielding borne by the roofs of large experimental halls. Also, due to the creative efforts of many physicists and engineers the beam intensities eventually available at accelerators have often greatly exceeded those credible at the time at the initial design.

5.3.1 Simple Parameterizations

When addressing the skyshine question, it is generally customary to plot the neutron fluence, or even the dose equivalent, as a function of distance from the source by multiplying it by the square of the distance from the source, i.e. as $r^2 \Phi(r)$. Stevenson and Thomas (St84a) included plots of a number of measurements of neutron skyshine obtained at proton accelerators producing protons of energies ranging from 30 MeV to 30 GeV, and also at high energy electron accelerators having energies of 7.5 and 12 GeV. In general, the quantity $r^2 \Phi(r)$ is characterized by a buildup followed by an exponential falloff. Most skyshine distributions are isotropic at ground level (i.e., independent direction with respect to the beam axis). As exhibited by the typical skyshine data, λ , the effective attenuation length, has been found to vary between a minimum value of about 200 meters and much larger values which approach one kilometer. We shall shortly see how this quantity is dependent upon the energy spectrum of the neutron radiation field that is the source of the skyshine.

Patterson and Thomas (Pa73) give a formula that describes such behavior for r greater than about 20 meters;

$$\Phi(r) = \frac{aQ}{4\pi r^2} \left(1 - e^{-r/\mu} \right) e^{-r/\lambda} .$$
 (5.17)

In this equation, a = 2.8 and represents an empirical **buildup factor**, while μ is the corresponding buildup relaxation length and λ is the effective interaction length. Nearly all of existing measurements are well described by taking μ to be 56 meters. Q is the source strength that dimensionally must be consistent with $\Phi(r)$. Thus, for the standard meaning of $\Phi(r)$ as the fluence, Q, is the number of neutrons emitted by the source. A plot of $r^2 \Phi(r)$ for a variety of choices of the value of λ in Eq. (5.17) is given in Fig. 5.12.



Fig. 5.12 Plot of skyshine distributions according to Eq. (5.17) for a variety of values of λ . The ordinate is the quantity $r^2 \phi(r)$ in that equation for a value of Q = 1.

Values of $\lambda > 830$ meters are possible if very high energy neutrons (E >> 150 MeV) are present. A value of 830 m (100 g cm⁻² of air at standard temperature and pressure) corresponds to the interaction length of the neutrons of approximately 100 MeV likely to control the propagation of hadronic cascades in air. Thus, λ is determined by the neutron energy spectrum present at the thinly shielded location. Larger values of λ are more plausibly due to multiple sources or an extended source. In such circumstances, the radiation field may also not necessarily be isotropic. Cossairt and Coulson (Co85c) present an example of a non-isotropic, complex skyshine source involving high energies, an extended source, and an extremely thin shield that resulted in a value of $\lambda \approx 1200$ meters.

The procedure, then, for using Eq. (5.17) is to do the following:

- A. Estimate the total emission rate of neutrons from the source. This can be done by using information about the neutron spectrum at the source to choose an "average" energy and intensity. The dose equivalent per fluence conversion factor at that energy can then be used in conjunction with a dose equivalent rate survey over the thinly shielded region to determine the total neutron emission rate, Q, by numerically integrating over the area of the top of the shield.
- B. Estimate the value of λ from the neutron energy spectrum information.
- C. Apply Eq. (5.17) to determine the radial dependence.

5.3.2 A Somewhat More Rigorous Treatment

A somewhat more rigorous treatment has been reported by Stevenson and Thomas (St84a) that is based on the work of Alsmiller, Barish, and Childs (Al81) and Nakamura and Kosako (Na81). These groups have independently performed extensive calculations of the neutrons emitted into cones of small vertex angle. Alsmiller, Barish, and Childs used the Discrete Ordinates Transport (DOT) Code while Nakamura and Kosako used the Monte Carlo code MORSE. For selected distances from the skyshine source, these workers have calculated the dose equivalent as a function of both the source neutron energy and the emission cone's semivertical angle (that is, the half-angle the rotation of which defines the cone into which the neutrons are emitted). The authors define this quantity, the so-called **neutron importance**, as the dose equivalent per emitted neutron as a function of the energy of the emitted neutron and of the distance from the source. This quantity is a measure of how "important" a given emitted neutron is in delivering radiation dose equivalent to a point in space located at a given distance from the skyshine source. The results of the Alsmiller calculation for small semivertical angles are given in Fig. 5.13. Numerical tabulations of neutron importance functions according to (Al81) are provided in references (NC03) and (Th88). The corresponding, but somewhat lessdetailed results of Nakamura, are in good agreement with these results.


Fig. 5.13 **Top frame**: The definition of the semivertical cone angle used in skyshine calculations of Alsmiller et al. (Al81). **Bottom frame**: Neutron skyshine importance functions for a semivertical cone angle of 37° at three different values of the distance from a point source. [Adapted from Alsmiller et al. (Al81)].

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Stevenson and Thomas (St84a) were able to derive an alternative "recipe" for skyshine neutron calculations to that expressed in Eq. (5.17) by making two assumptions:

- A. The neutron energy spectrum has the 1/E form up to the proton energy and zero at higher energies. This likely overestimates the contribution of the higher energy neutrons.
- B. The neutrons are emitted into a cone whose semivertical angle is about 35 to 40°. This may overestimate the doses by up to a factor of three for sources of smaller semivertical angles.

Stevenson and Thomas parameterized the skyshine phenomena using the following equation:

$$\Phi(r) = \frac{Q'}{4\pi r^2} e^{-r/\lambda}.$$
(5.18)

In this equation, the buildup exponential factor has been suppressed so the formula is valid only at large distances (i.e., r >> 56 meters). In addition, the source strength denoted by Q' implicitly includes the buildup factor of 2.8.

Further, they used the Alsmiller importance functions to estimate the value of λ based upon the upper energy (i.e., cutoff energy) of the 1/*E* spectrum. Fig. 5.14 displays the results of doing this for several choices of upper energies at three distances in a plot in which the inverse-square dependence is suppressed. A comparison with a measurement conducted at Brookhaven National Laboratory is also provided.



Fig. 5.14 Variation of dose equivalent with distance r for 1/E neutron spectra with different upper energies. The ordinate is dose equivalent H times r^2 . The curve labeled "BNL" is the result of a measurement at the Brookhaven National Laboratory Alternating Gradient Synchrotron, a 30 GeV proton accelerator. [Adapted from (St84a).]

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The slopes, then, were used to obtain theoretical values of λ as a function of "upper energy" which are plotted in Fig. 5.15.



Fig. 5.15 Effective absorption length λ as a function of upper neutron energy *E* for 1/*E* spectra. [Adapted from (St84a).]

To determine the source term, the straight lines in Fig. 5.14 (on the semi-logarithmic plot) were extrapolated to zero and used to determine intercepts at r = 0 ranging from 1.5 x 10⁻¹⁵ to 3 x 10⁻¹⁵ Sv m²/neutron (1.5 x 10⁻¹³ to 3 x 10⁻¹³ rem m²/neutron). Hence, conservatively, Stevenson and Thomas found that, over a rather large range of incident proton energies spatial dependence of the dose equivalent, H(r) can be described by

$$H(r) = \frac{3 \times 10^{-13}}{r^2} e^{-r/\lambda}$$
 (rem/emitted neutron, *r* in meters). (5.19)

Again, one has to determine the total number of neutrons emitted. This can be done as before by measuring the integral of dose equivalent times the area over the thinly shielded location and using the reciprocal of the dose equivalent per fluence conversion factor appropriate for the neutron energy spectrum at hand to get the total number of neutrons emitted. The use of Eq. (5.19) will lead to an overestimate of neutrons for values of r less than approximately 100 meters because the extrapolation ignores the observed exponential buildup of the skyshine.

Stevenson and Thomas (St84a) give a convenient table, useful for general purposes, of dose equivalent per fluence conversion factors derived from data in ICRP Publication 21 (IC73) integrated over such 1/E spectra which is provided here as Table 5.4.

Upper Energy Spectrum Averaged De			
	Equivalent Conversion		
(MeV)	(10 ⁻⁹ rem cm ² /neutron)		
1.6	3.9		
2.5	4.8		
4.0	5.6		
6.3	6.4		
10	7.2		
16	7.9		
25	8.6		
40	9.4		
63	10.1		
100	10.9		
160	11.7		
250	12.5		
400	13.4		
630	14.6		
1000	16.2		
1600	18.4		
2500	21.2		
4000	25.0		
6300	30.0		
10000	36.5		

Table 5.4 Dose equivalent per neutron/ cm^2 for 1/E neutron spectra of different upper energies. [Adapted from (St84a).]

5.3.3 Examples of Experimental Verifications

Measurements at Fermilab (Co85c) have confirmed the validity of these methods for a "source" involving the targetry of 400 GeV protons. Figure 5.16 shows two measured and fitted radial distributions made using Eq. (5.17). In Fig. 5.16 "Survey 2" corresponds to a shielding configuration where the neutron energy spectrum was inferred to be of very high energy while "Survey 4" was likely to involve a much less energetic spectrum. Survey 4 was made for the same beam and target after the concrete shield thickness around the source was greatly increased compared with the shield present when "Survey 2" was obtained. The normalization to "COUNTS-M² HR⁻¹" refers to an integration of an instrumental response over the surface area of the source and should be approximately proportional to the emitted neutron fluence. The instrument calibration of "COUNTS/HR" made possible an estimate of the dose equivalent at r = 200 meters for the two surveys. In view of details of the conditions not described in detail here, one can make an educated guess that the spectrum of emitted neutrons of "Survey 2" had an upper energy of ≈ 1 GeV, while the spectrum of emitted neutrons of "Survey 4" had an upper energy of ≈ 100 MeV.



Fig. 5.16 Skyshine data from two different surveys plotted as $r^2 \phi$ as a function of distance from the source *r*. The solid curves are from the least squares fit of Eq. (5.17) to the data points while the dashed curve is the fit if λ is constrained to have a value of 830 m. Error bars represent one standard deviation counting statistics. [Reproduced from (Co85c).]

Using the appropriate dose equivalent per fluence conversion factor, the value of Q for the Survey 2 conditions was determined experimentally to be 2.5 x 10⁵ mrem m² hr⁻¹. This was obtained from the measured absorbed dose surface integral of 5 x 10⁴ mrad m²hr⁻¹ and assumed a quality factor of 5. For the Survey 4 conditions, Q was found to be 4.0 x 10⁴ mrem m² hr⁻¹. Again, this was obtained from the measured absorbed dose surface integral of 8.1 x 10³ mrad m² hr⁻¹ and assumed a quality factor of 5. Table 5.5 makes a comparison with the prescription of (St84a) for these data. In this table *H* is the dose equivalent in one hour at 200 meters. The prescription of Stevenson and Thomas (St84a) is used to calculate the dose equivalent in one hour at 200 meters. The agreement is well within all uncertainties involved.

Table 5.5 Comparisons of Fermilab skyshine data with results of parameterizations of surveys shown in Fig. 5.16, assuming 1/E spectra with inferred upper energies. The quantities are all for a one hour time period.

Survey	λ	Emax	Dose	<i>Q</i> measured	<i>H</i> (200 m)	<i>H</i> (200 m)
	(meters) (Co85c)	(inferred) (MeV)	Equiv. per Fluence (mrem/ n cm ⁻²) (St84a)	(mrem m ²) (Co85c)	(mrem)- calculated	(mrem)- measured (Co85c)
Survey 2	1200	1000	16.2×10^{-6}	2.5×10^5	1.0	1.6
Survey 4	340	100	10.9 x 10 ⁻⁶	$4.0 \ge 10^4$	0.15	0.15

Another illustration is provided by Elwyn and Cossairt (El86) in connection with neutron radiation field emerging from an iron shield that is more fully described in Section 6.3.5. Fig. 5.17 taken from (El86) shows the measured radial dependence of neutron flux as a function of distance from that iron shield.



Fig. 5.17 The product of r^2 and the neutron fluence ϕ (r) per 10¹² protons incident on a target as a function of the distance from the source r. The source is that described in connection with Fig. 6.8. The smooth curve is a fit to Eq. (5.17) with parameters $\lambda = 184.4$ m and Q = 1.74 x 10^{10} neutrons per 10^{12} protons. [Reproduced from (E186).]

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From other considerations pertaining to an iron shield discussed in Section 6.3.5, it is known that the radiation field is dominated by neutrons of energies near 847 keV. Using the measured data, normalized to 10^{12} incident protons the parameters $Q = 1.75 \times 10^{10}$ and $\lambda = 184.4$ meters were determined by fitting the skyshine data using Eq. (5.17). Evaluating Φ at r = 200 meters,

$$\Phi(200) = \frac{2.8(1.75 \times 10^{10})}{4\pi (200)^2} \left[1 - \exp(200/56)\right] \exp(-200/184.4) = 3.20 \times 10^4 \text{ neutrons m}^{-2}.$$
(5.20)

Thus, taking the measured neutron flux at r = 200 meters and applying a dose equivalent per fluence value of 3.0 x 10⁻⁵ mrem cm⁻² appropriate for 847 keV neutrons (see Fig. 1.5) gives a dose equivalent per 10¹² incident protons of 9.6 x 10⁻⁵ mrem at r = 200 meters. The value of λ that fitted the skyshine data is also consistent with the neutron energy spectrum, which was known to be dominated by neutrons of about 1 MeV kinetic energy.

Elwyn and Cossairt also estimated a value of $(3.4 \pm 2.0) \times 10^{10}$ per 10^{12} incident protons for the total neutron emission of the source by performing a numerical integration over the surface area of the source, separate from the result determined using the skyshine measurement. Applying the prescription of Stevenson and Thomas (St84a) found in Eq. (5.18);

$$H(200) = \frac{(3 \times 10^{-13})[(3.4 \pm 2.0) \times 10^{10}]}{(200)^2} \exp(-200/184.4) =$$

= (8.6 ± 5.1) x 10⁻⁵ mrem per 10¹² protons (5.21)

at this same location. This result is very consistent with that found using Eq. (5.20).

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Problems

- 1. A 1 μ A 100 MeV electron beam is incident on an "optimized bremsstrahlung" target in a shielding configuration and labyrinth like that in Fig. 5.3. Using the facts given in Chapter 3 (Swanson's Rules of Thumb, etc.) about bremsstrahlung, calculate the dose equivalent rate at the exit of a labyrinth having 2 legs. Set all distances d_i , d_1 , and $d_2 = 3$ meters. If the goal is to get the dose equivalent rate at the exit to be < 1 mrem/hr, is this a sensible design? The 2 legs are 1 x 2 meter² in cross section and, since no other information is available, use $\alpha = 10^{-2}$ as a "conservative" value. For purposes of this problem, photons constitute the only component of radiation present. [Hint: One needs to calculate the projected diameter of the beam at the wall where the first scatter occurs. This can be done using Eq. (3.12).]
- 2. A 500 GeV proton beam of 10^{11} protons/second strikes a magnet 2 m from the mouth of a 3-legged labyrinth. Each of the 3 legs is 4 meters long and 1 x 2 m² in cross section. The length of leg 1 is measured from the mouth of the labyrinth to the center of the first turn, all other lengths are measured between centers of turns. Assume the source is an on-axis "point source". Using Goebel's "universal" curves and Rameika's source term, what is the dose equivalent rate at the exit expressed in rem hr⁻¹. How far away from the exit does the value of *dH/dt* fall to 10 mrem hr⁻¹.
- 3. A high energy accelerator has a section of beamline which was poorly designed. Beam losses and insufficient shielding have resulted in a region of roof 10 meters wide and 50 meters long where a neutron dose equivalent rate averaging 100 mrem/hour (averaged over the surface of the weak shield) is found. A spectrum measurement indicates the spectrum to be approximately 1/E with an upper end point of approximately 500 MeV. Calculate the dose equivalent rate due to skyshine at distance r = 50, 100, 200, 500, & 1000 m using both formulae presented here.

6.1 Introduction

After all of this discussion of the production of prompt radiation at accelerators, it is now advisable to review in one place the relevant properties of the most common materials used in radiation shielding. Since many shielding problems are driven by the nature of the energy spectrum of the neutrons, such spectra are also discussed here in some detail and examples of neutron energy spectra measured external to shielding at various types of accelerator facilities are presented.

6.2 Discussion of Shielding Materials Commonly Used at Accelerators

Given the size of many modern accelerators, economic considerations commonly dominate shielding designs; requiring the use of relatively relatively inexpensive, but often less than optimally efficient shields. Aside from the need to accomplish the identified goals in radiation safety, in all situations good engineering practices concerning structural properties, appropriate floor loading allowances, and fire protection must be taken into account to provide an acceptable level of occupational and public safety. In general, low atomic number materials are best used for targets, collimators, and beam stops at electron accelerators to reduce photon production, while high atomic number materials are preferred at proton and heavy ion accelerators for these components to reduce neutron production. From the previous chapters, it should be clear that at beam energies above 5 MeV neutrons are produced in most materials. Some materials have superior heat transfer characteristics that enhance durability and reliability and thus can reduce personnel exposures incurred in maintenance activities.

6.2.1 Earth

Earth has many admirable qualities as a shield material besides its low cost. Especially important is the fact that the water it contains enhances the effectiveness of the neutron attenuation. This is because the mass of a proton is essentially equal to that of a neutron, a fact that facilitates the transfer of energy from the particle to the shielding medium. As a result of conservation of energy and momentum, in an elastic collision the energy ΔE that can be transferred from a neutron having kinetic energy E_o to a target nucleus as a function of scattering angle θ is given by

$$\frac{\Delta E}{E_o} = \frac{4\frac{M}{m_n}\cos^2\theta}{\left(1 + \frac{M}{m_n}\right)^2},$$
(6.1)

where *M* is the mass of the recoiling nucleus and m_n is the mass of the incident neutron. Thus, at small scattering angles (i.e., $\theta \approx 0$), nearly all of the neutron kinetic energy can be transferred to the protons in the water. For comparison, ¹²C nuclei are capable of absorbing only 28 per cent of the incident neutron energy. The proton energy, then, can

be dissipated in the medium by means of ionization and nuclear interactions. Representative ranges of soil water content (per cent of dry weight) for different soil types are; sand (0-10), sandy loam (5-20), loam (8-25), silty loam (10-30), dry loam (14-30), and clay (15-30).

Additionally, earth is also composed of sufficiently high atomic number elements to be effective against photons. Dry earth has a typical elemental composition as given in Table 6.1. Earth is generally a "crackless" shield, not prone to neutron leakage by "streaming". The density of earth varies widely, from as low as 1.7 g cm⁻³ to as much as 2.25 g cm⁻³, depending upon soil type and water content. In general, sandy soils will have lower values of density than heavy clays found in glacial till. Extrusive volcanic soils, on the other hand, can have very low densities. Given this variation, specific knowledge of soil characteristics at the accelerator site are needed to do effective shielding designs. Definitive measurements of the soil water content are also most useful if the shielding of neutrons is the intent and no safety factors are being used.

Element	Global Average (%)
0	43.77
Si	28.1
Al	8.24
Fe	5.09
Mn	0.07 <u>+</u> 0.06
Ti	0.45 <u>+</u> 0.43
Ca	3.65
Mg	2.11
Κ	2.64
Na	2.84

Table 6.1Elemental composition, dry-weightper cent, of representative soils. [Adapted from
(Ch84).]

6.2.2 Concrete

Concrete has obvious advantages in that it can either be poured in place permanently or be cast into modular blocks. It has considerable structural strength and steel reinforcement has essentially no effect on the shielding properties. Sometimes concrete blocks are used to shield targets, beam stops, etc. in a manner that allows their ready access if the need for maintenance arises. The use of concrete blocks generally requires their overlapping to avoid **streaming** through the cracks. It is sometimes efficient to use a heavy material as part of the aggregate in the concrete recipe. This can increase the concrete density as well as its average atomic number. The latter, of course, increases the effectiveness against photons. Table 6.2 due to Chilton (Ch84) gives some partial densities of various concretes used in shielding, thus illustrating the elemental variability found in the composition. When shielding neutrons, the concrete water content is quite important because it incorporates almost all of the hydrogen. Under conditions of

extremely low humidity, the water content of concrete can decrease with time, to as little as 50 % of the initial value over a 20 year period. The density of concrete is locally variable. Heating due to the energy deposition of the beam can also drive out the water. This can also be sufficient to require passive or active heating of adjacent iron shielding.

Type:	Ordinary	Magnetite	Barytes	Magnetite & Fe
Additive:		(FeO, Fe ₂ O ₃)	BaSO ₄	
Density $(g \ cm^{-3})$:	2.34	3.53	3.35	4.64
Н	0.013	0.011	0.012	0.011
0	1.165	1.168	1.043	0.638
Si	0.737	0.091	0.035	0.073
Ca	0.194	0.251	0.168	0.258
Na	0.040			
Mg	0.006	0.033	0.004	0.017
Al	0.107	0.083	0.014	0.048
S	0.003	0.005	0.361	
Κ	0.045		0.159	
Fe	0.029	1.676		3.512
Ti		0.192		0.074
Cr		0.006		
Mn		0.007		
V		0.011		0.003
Ba			1.551	

 Table 6.2 Partial densities of representative concretes after curing. [Adapted from (Ch84).]

6.2.3 Other Hydrogenous Materials

6.2.3.1 Polyethylene and Other Materials That Can Be Borated

Polyethylene, (CH₂)_n, is a very effective neutron shield because of its hydrogen content (14% by weight) and its density (≈ 0.92 g cm⁻³). It can thus attenuate so-called "fast" neutrons. In many circumstances, it provides very adequate shielding and is highly efficient due to the high hydrogen content. Thermal neutrons can be captured through the ${}^{1}H(n, \gamma)^{2}H$ reaction which has a cross section of 0.33 barn for neutrons in thermal equilibrium at room temperature ($E_n = 0.027 \text{ eV}$). The emitted γ -ray has an energy of 2.2 MeV that provides a somewhat troublesome source of radiation exposure in some situations. The addition of boron can reduce the buildup of 2.2 MeV photons released in the thermal neutron capture by hydrogen by instead capturing the thermal neutrons in the boron, by means of the ${}^{10}B(n, \alpha)^7Li$ reaction. The latter has a cross section for room temperature thermal neutrons of 3837 barns. In 94 per cent of these captures, the emitted α -particle is accompanied by a 0.48 MeV γ -ray. The α -particle is readily absorbed by ionization while the γ -ray has a much shorter attenuation length than does a 2.2 MeV γ ray. Commercially, polyethylene is available that includes additives of boron (up to 32%), lithium (up to 10 %), and lead (up to 80 %) in various forms such as planer sheets, spheres, and cylinders. Polyethylene also becomes brittle after receiving a high absorbed dose.

These materials can be useful, if it is necessary, to economize on space and also to accomplish shielding of photons and neutrons simultaneously. Pure polyethylene is flammable, but some of the commercial products available contain self-extinguishing additives. Some of these materials are available in powder form, for molding into a desired shape by the user. Besides polyethylene, boron has been added to other materials to form effective thermal neutron shields. These include other plastics, putties, clays, glasses, and even water to accomplish specific shielding objectives. Plastic materials such as polyethylene can also be subject to significant radiation damage at relative low levels of integrated absorbed dose (Sc90). The effects upon the structural integrity must be carefully considered in such circumstances.

6.2.3.2 Water, Wood, and Paraffin

These materials are superficially attractive neutron shields because of their very high hydrogen contents.

Water, of course, tends to rust out its containers and there is the omnipresent question as to whether the shield material has flowed away. Exposed to thermal neutrons, it also emits the 2.2 MeV capture γ -ray from hydrogen. The addition of boron is more difficult because of the relative insolubility of boron salts in water. However, potassium tetraborate is relatively soluble in water.

Wood was found in the early years of operation at the Bevatron at the Lawrence Radiation Laboratory (now the Lawrence Berkeley National Labortory) to be as effective per unit length as concrete for shielding intermediate energy neutrons. Thus, it is essential that the neutron energy spectrum to be attenuated is known. In the past wood has been discouraged as a shielding material because of its flammability. Chemically treated wood that is nearly completely fireproof has become available, but it is not clear that the flammability problem has been solved with complete satisfaction. Also, questions have been raised by reports of a reduction in structural strength of such treated wood products.

Paraffin historically has been used for neutron shielding but has been spurned because of the fire hazard. Under some conditions it can be used if it is packaged in metal containers. Recently, paraffin treated with fire retardant additives has become available. This material is also subject to "plastic" flow problems.

6.2.4 Iron

A relatively high density, in conjunction with its low cost, makes iron an attractive shielding material. Caution is required because the density of iron can vary widely from a low of 7.0 for low-grade cast iron to a high value of 7.8 g cm⁻³ for some steels. The "textbook" value of 7.87 g cm⁻³ given in Table 1.2 is almost never attained in the bulk quantities necessary for radiation shielding. Because of its nonmagnetic properties and resistance to corrosion, stainless steel is often used as part of accelerator components.

Because of concerns about radioactivation (see Chapter 7), knowledge of the elemental composition of various alloys can sometimes be useful. For example, long-lived ⁶⁰Co can be produced in stainless steel but not in pure iron. While tempting, the use of steel wool to fill cracks in a large shield is undesirable due to the contamination hazard presented by the resulting rust. Iron has a very important deficiency as a neutron shield; this will be discussed in Section 6.3.5.

6.2.5 High Atomic Number Materials (Lead, Tungsten, and Uranium)

The materials in this category are valuable because of their high atomic number, especially where the shielding of photons is important. The most obvious material in this category is *lead*. It has a high density (11.3 g cm⁻³) and is resistant to corrosion. Pure lead, as is well known, has major drawbacks because of its poor structural characteristics and low melting point (327.4 °C). It is usually best used when it can be laminated to some other more structurally stable material. Some alloys represent improvements on the structural properties. It is often available as an additive to other materials in order to improve their capacity for shielding photons. Fabric blankets containing shredded lead can be effectively used to shield radioactivated components to minimize exposures associated with accelerator maintenance activities during operational shutdowns. The high chemical toxicity of lead requires care in its fabrication and handling to properly protect personnel. The use of lead wool to fill cracks is discouraged due to the chemical toxicity hazard. Bismuth, having a density of 9.7 g cm⁻³, is sometimes used as a lower-toxicity substitute for shielding against photons.

Tungsten is an excellent, but relatively expensive, shielding material. Its high density (19.3 g·cm⁻³) and high melting temperature (3410 °C) make it extremely useful as a component in photon shields, beam absorbers, and beam collimators. It is difficult to machine, so alloys such as Hevimet are commonly used. Hevimet was developed by the General Electric CompanyTM. It consists of tungsten (90%), nickel (7.5%) and copper (2.5%) and has a typical density ranging from 16.9 to 17.2 g cm⁻³ (Ma68). It is currently commercially available from several sources and in various forms exemplified by HD18¹³. HD18 is 95% tungsten, 3.5% nickel, and 1.5% copper, and has a density of 18 g cm⁻³.

Uranium is a superficially attractive shielding material, most often in its "depleted" form in which the concentraton of ²³⁵U compared with the dominant ²³⁸U has been reduced to a value, usually ≤ 0.2 %, lower than the natural value of 0.72 %. Its high density (19.0 g cm⁻³) and relatively high melting point (1133 °C) are positive attributes, especially in places where space efficiency is a concern. It is obviously not a good choice of material in environments having a high neutron flux density due to its susceptibility to fission induced by fast neutrons. Depleted uranium is relatively safe, but if is combined with hydrogenous materials, nuclear fission criticality should be considered for the specific material and geometric arrangement to be employed. Even in the absence of hydrogen

¹³ Mi-Tech Metals, Inc., 4701 Massachusetts Ave., Indianapolis, Indiana 46218

thermal neutrons under certain conditions can result in the possibility of criticality if insufficiently depleted of ²³⁵U (Bo87). Major drawbacks are its material properties. It has a large anisotropic thermal expansion coefficient and also readily oxidizes when exposed to air especially under conditions of significant humidity. The oxide is readily removable and presents a significant internal exposure hazard. Prevention of oxidation by sealing it with epoxy or paint meets with only limited success due eventual embrittlement and chipping accelerated by radiation damage. Sealed containers filled with dry air or with noble gases or liquefied noble gases such as argon seem to represent the best storage solution to limit oxide formation. Small chips of this element are also pyrophoric, complicating machining-type processes by posing yet another safety hazard. Uranium in any form, as classified as a "nuclear material", is subject to stringent accountability requirements established internationally by treaty.

6.2.6 Miscellaneous Materials (Beryllium, Aluminum, and Zirconium)

These three materials find considerable usage as accelerator components because of various properties. *Beryllium* is often used as a target material in intense beams because of its resistance to thermal effects and consequent ability to endure large values of energy deposition density, especially when in the form of the oxide, BeO. It has been used at high energy accelerators in relatively large quantities as a "filter" to enrich one particle type at the expense of another taking advantage of particle-specific variations in absorption cross sections. A serious concern is the extreme chemical toxicity of the metal and its compounds, which makes it difficult to fabricate. *Aluminum* is used in accelerator components because of its nonmagnetic properties and its resistance to corrosion. It is not an effective shield against neutrons. *Zirconium* has a very small thermal neutron capture cross section and very good thermal properties. It is therefore not a good neutron absorber but has been found to be useful in beam-handling component material in some situations.

6.3 Neutron Energy Spectra Outside of Shields

As has been discussed in the previous chapters, at most accelerators, except perhaps for forward shielding at high energy accelerators capable of producing muons, the shielding is largely designed largely to attenuate neutrons emitted in all directions. In this section, examples of neutron energy spectra commonly found at accelerators external to shielding are presented and discussed. While individual spectra may vary a great deal from these examples, which are not intended to be comprehensive, the general principles are of interest.

6.3.1 General Considerations

In the most simple approximation, outside of thick shields of soil or concrete that contain some hydrogen content (usually as water), accelerator neutron shields can most generally said in first order to be proportional to inverse energy. Such "**1**/*E* spectra" can span

energies extending from those of thermal neutrons ($\langle E_n \rangle \approx 0.025 \text{ eV}$) up to the energy of the incident particles, but are commonly effectively cut off at some upper energy that is less then the incident particle energy. Thus, at this level of approximation, the spectrum is given as

$$\frac{d\phi(E)}{dE} = k\frac{1}{E},\tag{6.2}$$

where k is a normalizing constant. Rohrig (Ro83) observed from this that it often is more convenient to plot such spectra as flux per *logarithmic* energy interval by simply plotting $E\phi(E);$

$$\frac{d\phi(E)}{d\ln E} = E\phi(E) \,. \tag{6.3}$$

In the terminology of textbooks on neutron physics, this is also called a "lethargy" plot that, in effect, suppresses the 1/E dependence seen in typical neutron energy spectra. Most, but not all, of the example spectra discussed further are presented as lethargy plots.

6.3.2 Examples of Neutron Spectra Due to Incident Electrons

ilmenite

iron

when 400 MeV electrons are incident on a thick copper target (Al73). Predictions of the neutron yields over several ranges of production angle θ also resulted from these calculations. They considered four different shielding materials; soil, concrete, ilmenite Calculations of neutron energy spectra and the fractional (FeTiO₃), and iron. contributions to the total dose equivalent from neutrons with energies less than a given energy E for the same spectrum for the angular region $0 < \theta < 30^{\circ}$ are presented in Fig. 6.1. These results are for a radial depth in the shield of 7 mean free paths of the highest energy neutrons found in this source spectrum within this angular range. Table 6.3 gives the densities and the neutron mean free paths used for the four materials.

Table 6.3 N	laterial proper	ties used in the
calculations	of Alsmiller	and Barish.
[Adapted from	n (Al73).]	
Material	Density	Mean Free
	(g cm ⁻³)	Path
	-	$(g \text{ cm}^{-2})$
soil	1.8	103.6
concrete	2.3	105.3

3.8

7.8

120.6

138.6

T-11. (2 M-4------.. 1 • 41



Fig. 6.1 Neutron spectral information from 400 MeV electrons incident on a thick Cu target. The **upper frame** shows the omnidirectional neutron fluence per unit energy multiplied by the square of the radial depth in the shield as a function of energy for the various shield materials studied by Alsmiller and Barish. The **lower frame** shows the fractional contribution to the total dose equivalent from neutrons with energies less than *E* as a function of *E* for the illustrated shielding materials. [Reproduced from (AI73).]

In this figure, the inverse square dependence was removed to eliminate the effect of "geometrical" attenuation within the shield. It should be clear that the neutron spectra in the iron shield is markedly different from that found in the soil and concrete shields. The characteristics of the spectra found in the ilmenite are intermediate, perhaps related to the presence of iron in this material. The same kinds of phenomena associated with iron shielding are found in neutron energy spectra measured at high energy proton accelerators. Special considerations pertaining to neutron energy spectra emerging from iron shielding will be discussed in Section 6.3.5.

6.3.3 Examples of Neutron Spectra Due to Low and Intermediate Energy Protons

Calculations and measurements of neutron energy spectra at various depths in shielding due to 52 MeV protons have been reported by Uwamino et al. (Uw82). These results are presented in Fig. 6.2.

Alsmiller et al. (Al75) have provided predictions of neutron energy spectra averaged over specific angular intervals for 200 MeV protons stopped in a thick water target. The results are given for large angles are presented in Fig. 6.3.

6.3.4 Examples of Neutron Spectra Due to High Energy Protons

In the regime of proton energies well above one GeV the details of the spectra are far more sensitive to geometrical considerations than they are dependent upon the incident proton energy. O'Brien carried out a calculation of a generalized neutron spectrum that could be found external to a high energy accelerator (OB71). These were compared with measurements and alternative calculations performed by Höfert and Stevenson (Hö84a). The results are provided in Fig. 6.4 for both "lateral" and "forward" angular regions. The results for forward angles also include the spectra of charged pions and protons. It is clear that at the forward angles, the total fluence of hadrons at high energies is likely to be a mixture of charged particles and neutrons.

Detailed features of the geometry involved can produce peaks in the neutron energy spectrum. Examples of such spectra have been provided by various workers (Pa73, Th88, El86, McC88, and Co88). These peaks are typically encountered in the few MeV region. Figures 6.5, 6.6, 6.7, and 6.8 are plots of neutron spectra and sketches of the corresponding shielding geometry taken from Cossairt et al. (Co88). These spectra were obtained (i.e., "unfolded") using the Bonner sphere technique discussed in more detail in Section 9.5.2.1. In these four figures, "spheres" denote the locations where the neutron energy spectra were measured. These are typical of the spectra found at high energy proton accelerators. Figure 6.5 is rather typical of the spectra found external to earth and concrete shields lateral to high energy proton accelerators. The neutron energy spectrum displayed in Fig. 6.6 is particular interesting because its shape was demonstrated to be essentially independent of proton energy over the range of 150 to 900 GeV (McC88). Fig. 6.7 is typical of the results obtained in the second and succeeding sections ("legs") of a labyrinth penetration.



Fig. 6.2 Forward neutron energy spectra and attenuations measured and calculated by Uwamino et al. for 52 MeV protons. The protons interacted with the material being studied. Following a distance, t, the spectra were determined at $\theta = 0$. Frame **A** displays spectra for water at two different values of t, frame **B** displays spectra for ordinary concrete at three different values of t, and frame **C** provides data on the attenuation profiles for various materials. [Adapted from (Uw82).]



Fig. 6.3 Energy distribution of neutrons averaged over particular angular intervals, produced when 200 MeV protons are stopped in a thick water target. The protons are incident at $\theta = 0^{\circ}$. [Adapted from (Al75).]



Fig. 6.4 Neutron energy spectra outside of a concrete shield at a high energy proton accelerator at forward angles (**upper frame**) and at large angles (**lower frame**). The open circles represent the calculations of O'Brien (OB71) while the other symbols represent the calculations of Höfert and Stevenson. [Adapted from (Hö84a).]



Fig. 6.5 Neutron energy spectrum (**lower frame**) obtained external to a beam enclosure (**upper frame**) in which 8 GeV protons struck the yoke of a magnet. The site was the Fermilab Debuncher Ring. The normalization of the spectrum is arbitrary. [Adapted from (Co88).]



Fig. 6.6 Neutron energy spectrum (**lower frame**) obtained internally in a beam enclosure (**upper frame**) in which 800 GeV protons interacted with residual gas in the Tevatron vacuum chamber during circulating beam conditions. The site was the Fermilab Tevatron Ring. The normalization of the spectrum is arbitrary. [Adapted from (McC88).]



Fig. 6.7 Neutron energy spectrum (lower frame) obtained within a labyrinth enclosure (upper frame) in which 400 GeV protons interacted with an aluminum target located beneath the floor of the enclosure shown. The spectrum was measured in the second leg at the location denoted "S". A quality factor measurement was made at the locations denoted "R" (see Sections 5.2.4 and 9.5.7). The normalization of the spectrum is arbitrary. [Adapted from (Co88).]

6.3.5 Leakage of Low Energy Neutrons Through Iron Shielding

One peak commonly found in such spectra is of particular importance. As discovered by Alsmiller and Barish (Al73) (see Section 6.2.4), iron has a major deficiency as a shield for fast neutrons. An important mechanism by which fast neutrons lose energy is inelastic scattering. At energies below the first excited state of any nucleus, inelastic scattering becomes impossible and elastic scattering becomes the only removal process aside from nuclear reactions. As evident from Eq. (6.1), elastic scattering is a very inefficient mechanism for energy transfer from neutrons scattering off a much massive nucleus such as iron. The scattering of billiard balls from bowling balls provides a picture. Consistent with experimental observation, the scattering of billiard balls off other billiard balls of equal mass provides much more efficient transfer of energy. Similarly, the scattering of neutrons by the "free" protons in hydrogenous materials transfers energy much better than does elastic scattering of neutrons from iron nuclei. The first excited state of ⁵⁶Fe, the dominant isotope in natural iron (92% abundance), is at 847 keV. Due to the inefficiency of the transfer of energy by means of elastic scattering, neutrons having kinetic energies above 847 keV in a given spectrum will be slowed by inelastic scattering to $E_n \approx 847$ keV only to build up at energies just below this value. Amplifying this effect, when one considers the dose equivalent external to such shields, is the fact that the quality factor for neutrons as a function of energy also has its maximum value at about 500 keV (see Fig. 1.3). Thus, pure iron shields are rather ineffective in attenuating neutrons in this energy region.

This phenomenon is illustrated by the geometry and spectra shown in Figs. 6.8, supporting calculations such as those provided, for example, in Fig. 6.1. Both spectra in Fig. 6.8 shown were measured at about $\theta = 90^{\circ}$ from a beam absorber struck by secondary particles due to 800 GeV proton interactions far upstream of the beam absorber (E186). The secondary particles were chiefly a multitude of hadrons of several hundred GeV. The beam absorber was shielded by the yoke of a large iron magnet as shown in Fig. 6.8a. Originally, the neutron energy spectra was measured directly adjacent to this iron shield. This spectrum is shown in Fig. 6.8b. Later, in order to reduce the intensity of the neutron radiation, additional concrete shielding blocks 91.4 cm thick were placed between the neutron detectors and the beam absorber up to a height of about 0.5 meters above the beam line as indicated in Fig. 6.8a. The neutron energy spectrum was measured again with the result displayed in Fig. 6.8c. For the bare iron situation the normalized dose equivalent rate external to the shield was over 40 times that measured after the concrete was installed. This factor is far in excess of the approximate factor of 10 expected from simple attenuation of the equilibrium cascade neutron spectrum and indicates both the importance of the leakage neutrons and the maximization of their quality factor. The additional concrete also reduced the measured value of the average quality factor from 5.4 to 2.8.

In general, an iron shield "capped" or "backed" by such a concrete shield will be an efficient use of space. It has been determined that about 60 cm of concrete is the most efficient thickness to use for this purpose [(Yu83) and (Za87)]. Shielding properties of other elements near iron in the periodic table (e.g., copper and nickel) are comparable.





Fig. 6.8a Situation for the measurements shown in Figs. 6.8b and 6.8c. A target far upstream (to the left) of the apparatus shown in the figure was struck by 800 GeV protons. The beam axis was horizontal and 1.8 m above the floor. Secondary particles, largely hadrons, produced by these interactions were intercepted by the beam absorber shown in the Figure. The plain shielding blocks are of ordinary concrete. During initial operations, the cross-hatched blocks, also of ordinary concrete, were not in place between this beam absorber and the location of measurements and the result was the measured spectrum in Fig. 6.8b. Later, those blocks were added and the spectrum shown in Fig. 6.8c was measured. [Reproduced from (E186).]



c)

Fig. 6.8 b&c Neutron energy spectra obtained external to the shielding configuration shown in Fig. 6.8a for the two different situations discussed above. The normalization of the spectra is arbitrary. [Adapted from (El86).]

6.3.6 Neutron Spectra Due to Ions

Measurements of neutron energy spectra external to shielding obtained with ions are rare. Britvich et al. (Br99) have provided such spectra for ¹²C ions incident on a Hevimet target at 155 MeV nucleon⁻¹. The spectrum of neutrons due to ¹²C ions was measured at $\theta = 94^{\circ}$ without shielding at a distance of 121 cm from the target. The result is shown in Fig. 6.9. Qualitatively similar spectra were obtained at this location with ⁴He and ¹⁶O ions at 155 MeV nucleon⁻¹. The spectrum of neutrons due to the ¹²C ions was measured, also at $\theta = 94^{\circ}$, at a distance of 403 cm from the target which was shielded by 308 g cm⁻² of ordinary concrete. The result is shown in Fig. 6.10. One can see that the shielding effectively attenuates many of the neutrons below about 0.3 MeV.



Fig. 6.9 Neutron energy spectrum $F(E) \ge E$ at 121 cm and $\theta = 94^{\circ}$ from a thick Hevimet target bombarded by 155 MeV/nucleon ¹²C ions where F denotes the normalized neutron fluence. The solid line is a fit to these data using a parameterization suggested by Nakamura (Na85). [Reproduced from (Br99).]

Intuitively, especially for ions of high atomic number, one might expect more copious production of neutrons. This matter was studied in measurements conducted by Aroura et al. (Ar97) for lead ions having a specific energy of 160 GeV nucleon⁻¹. Comparisons of neutron energy spectra on top of a concrete shield surrounding a lead target were made with those obtained with 205 GeV protons. The results are given in Fig. 6.11.



Fig. 6.10 Neutron energy spectrum $F(E) \ge E$ at 403 cm and $\theta = 94^{\circ}$, and external to 128.3 cm of concrete shielding, from a thick Hevimet target bombarded by 155 MeV/nucleon ¹²C ions [Reproduced from (Br99)].



Fig. 6.11 Neutron fluence spectra around a lead ion beam of 160 GeV/nucleon shielded by concrete compared with that obtained with of a 205 GeV proton beam. The units used for the ordinate are arbitrary. For further discussion, consult the original reference of Aroua et al. [Reproduced from (Ar97).]

6.3.7 Neutron Fluence and Dosimetry

As was seen with electrons in Section 6.3.1, one must be concerned with the relative amounts of fluence and dose equivalent due to specific spectral regions. This can affect the potential to produce radioactivity and also guides the designer of shielding. Tables 6.4 and 6.5 give these properties for the spectra displayed in Figs. 6.5, 6.6, 6.7, and 6.8. Fig. 6.12 is a plot of cumulative values of the same quantities calculated for 1000 GeV protons incident on the face of a thick cylindrical concrete shield. As determined by Van Ginneken and Awschalom (Va75), the dependence upon incident proton energy of the distributions of fluence and dose equivalent is slight.

Table 6.4 Per cent fluence in specific energy bins for neutron energy spectra.[Adapted from (Co88).]

Energy Range	Fig. 6.5	Fig. 6.6	Fig. 6.7	Fig. 6.8b	Fig. 6.8c
< 1.5 eV	31.5	19.5	71	28	55
0.0015 - 100 keV	12.5	36	24	46	43
0.1 - 2 MeV	8.5	36	2	17.5	2
2 - 25 MeV	40.5	7	1	4.5	0.1
> 25 MeV	7	1.5	1.5	4	0

Table 6.5 Per cent of dose equivalent in specific energy bins for neutron energyspectra along with average quality factor. [Adapted from (Co88).]

Energy Range	Fig. 6.5	Fig. 6.6	Fig. 6.7	Fig. 6.8b	Fig. 6.8c
< 1.5 eV	1.5	2	32	4	41.5
0.0015 - 100 keV	0.5	6	16	11.5	37
0.1 - 2 MeV	9	58.5	9	35	17
2 - 25 MeV	75	26	13	24	3.5
> 25 MeV	14	7.5	30	25	1
Average Quality	5.8	6.9	3.1	5.4	2.5
Factor					



Fig. 6.12 Fraction of the omnidirectional flux, entrance absorbed dose, and maximum dose equivalent below a given hadron kinetic energy as a function of hadron energy for the region between zero and 450 cm depth and between 300 cm and 750 cm radius calculated for 1000 GeV/c protons incident on the face of a solid concrete cylinder. [Adapted from (Va75).]

7.1 Introduction

In this chapter the production of induced radioactivity at accelerators is described. This discussion begins with a review of the basic principles of the production of radioactivity. It proceeds with a discussion of the activation of accelerator components including some generalizations that may be used for practical health physics applications.

7.2 Fundamental Principles of Induced Radioactivity

In principle, induced radioactivity can be produced at all accelerators capable of liberating neutrons and other hadrons. When the accelerated beam strikes a nucleus, the resultant nuclear reactions can convert it into a different nuclide, which may or may not be radioactive. The **activity** of a given radionuclide refers to the number of atoms that decay per unit time. The customary unit of activity is the **Curie** (Ci), and its submultiples. One Curie was historically defined to be the activity of one gram of natural radium. It is now precisely defined as 3.7×10^{10} decays per second. The SI unit of activity is the **Becquerel** (Bq), which is defined to be 1 decay per second, with "multiples" such as Gbq commonly used. A related quantity of considerable importance is the **specific activity** that is defined to be the activity per unit volume (e.g., Bq cm⁻³) or, alternatively, the activity per unit mass (e.g., Bq g⁻¹).

Radioactive decay is a random process characterized by a **mean-life** (units of time) denoted by τ , and its reciprocal (units of inverse time), the **decay constant**¹⁴ λ , [$\lambda = 1/\tau$]. If a total of $N_{tot}(t)$ atoms of a radionuclide are present at time *t*, the total activity $A_{tot}(t)$ is determined by the random nature of radioactive decay to be

$$A_{tot}(t) = -\frac{dN_{tot}(t)}{dt} = \frac{1}{\tau}N_{tot}(t) = \lambda N_{tot}(t).$$
(7.1)

If at time t = 0, $N_{tot}(0)$ atoms are present, then this simple differential equation has the solution at some later time t = T, [with T > 0];

$$A_{tot}(T) = \lambda N_{tot}(0) \exp(-\lambda T) = A_{tot}(0) \exp(-\lambda T).$$
(7.2)

Often, the time required to decay to half of the original activity, the **half-life**, $t_{1/2}$, is tabulated and is related to the mean-life by the following:

$$\tau = \frac{1}{\ln 2} t_{1/2} = \frac{1}{0.693} t_{1/2} = 1.442 t_{1/2}.$$
(7.3)

In this text values of half-lives listed are from the National Nuclear Data Center (Tu05).

¹⁴Care needs to be taken with respect to the usage of the symbol λ . In the literature and in this text it is, at different points, used for both the attenuation length and for the decay constant. The reader needs to take note of the context to apply the correct meaning.

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The most simple activation situation at accelerators is that of the steady irradiation of some material by a spatially uniform flux density of particles that begins at time t = 0 and continues at a constant rate for an **irradiation period** that ends at $t = t_i$. This is followed by a decay period called the **cooling time** that is denoted t_c , a period of time that begins at $t = t_i$ and ends at $t = t_i + t_c$. For this simple situation, self-absorption of the hadrons by the target is ignored, as is the fact that a whole spectrum of particles might be incident. Thus the process of producing the radioactivity is characterized by a single average cross section, σ . In the more complicated generalized situations the value of this cross section must be obtained from averaging over the energy spectra of the particles incident.

The number of atoms of the radionuclide of interest per unit volume will thus be governed by the following equation during the period of the irradiation:

$$\frac{dn(t)}{dt} = -\lambda n(t) + N\sigma\phi, \qquad (7.4)$$

where n(t) is the number density of atoms of the radionuclide of interest at time t (cm⁻³), N is the number density of "target" atoms (cm⁻³), σ is the production cross section (cm², and ϕ is the flux density (cm⁻² sec⁻¹) of incident particles. On the right hand side of the above equation, the first term represents the loss of radionuclides through decay during the irradiation while the second term represents the gain of radionuclides through the production reaction under consideration. The equation has the following solution for $0 < t < t_i$:

$$n(t) = \frac{N\sigma\phi}{\lambda} \left(1 - e^{-\lambda t}\right).$$
(7.5)

Thus the specific activity induced in the material as a function of time during the irradiation is given by $a(t) = \lambda n(t)$, hence

$$a(t) = N\sigma\phi(1 - e^{-\lambda t}) \text{ (Bq cm}^{-3)} \quad \text{for } 0 < t < t_i.$$
(7.6)

To obtain specific activity in units of Curies cm⁻³, one must simply divide the resulting value by the conversion factor 3.7 x 10^{10} Bq Curie⁻¹. At the instant of completion of the irradiation ($t = t_i$), the specific activity will be given by

$$a(t_i) = N\sigma\phi \left\{1 - \exp(-\lambda t_i)\right\} \text{ (Bq cm}^{-3}\text{)}, \tag{7.7}$$

so that the specific activity as a function of time is characterized by a buildup from zero to the **saturation concentration** value of $N\sigma\phi$ for infinitely long irradiations. After the irradiation has ceased $(t > t_i)$, the specific activity as a function of the cooling time, t_c ,

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will obviously decay exponentially and be given by the activation equation;

$$a(t_c) = N\sigma\phi\{1 - \exp(-\lambda t_i)\}\{\exp(-\lambda t_c)\} \text{ (Bq/cm^3)},$$
(7.8)

where t_c is the cooling time and $t_c = t - t_i$. (7.9)

To obtain total activities in some object in situations where uniform flux densities of particles of constant energy are incident on a homogeneous "target", one can simply multiply by the volume of the "target". Or, in more complex cases involving non-uniform flux densities, one can integrate the above over the sub-volumes of the target.

For γ -ray emitters typical of those emitted by accelerator-produced radionuclides in the range of from about 100 keV to 10 MeV, many textbooks in health physics demonstrate that the absorbed dose rate, dD/dt (rad h⁻¹), at a distance *r* (meters) from a "point" source is approximately given in terms of the source strength, *S*, (Ci), and the photon energies present, $E_{\gamma i}$ (MeV) by

$$\frac{dD}{dt} = 0.4 \frac{S}{r^2} \sum_{i} E_{\gamma i} . \qquad (7.10)$$

The summation is over all γ -rays present, including appropriate branching fractions if multiple photons are emitted in the course of decay. If dD/dt is desired as an approximate absorbed dose rate in Gy h⁻¹ at a distance, r (meters), from a source strength S in gigaBecquerels¹⁵ (GBq), the constant 0.4 becomes 1.08 x 10⁻⁴. One can use the above to determine the absorbed dose rate from a given activated object if it is a point source. For non-point sources, an appropriate spatial integration must be performed.

7.3 Activation of Components at Electron Accelerators

7.3.1 General Phenomena

At electron accelerators, as was described in Chapter 3, the direct interactions of electrons in material results in the copious production of photons. Through various nuclear reaction channels, these photons then proceed to produce charged particles and neutrons that then interact further with material to produce radioactivity. In general, if the facility is properly shielded against prompt radiation, the radioactivity hazard will be confined to accelerator components and the interior of the accelerator enclosure. The experience at most accelerators bears this out. The vast majority of the radiation exposure incurred by the workers is due to maintenance activities on radioactivated components, handling and moving of activated items, radiation surveys, and radioactive waste handling rather than to exposure to the prompt radiation fields. An understanding of the production of radionuclides can help reduce personnel exposures through the selection of more appropriate machine component materials and the optimization of

¹⁵The GBq (10⁹Bq) or MBq (10⁶) are often better units of activity for practical work than is the tiny Bq.

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decay ("cool-down") times recommended after the beam has been turned off. Some familiarity with the relevant cross sections is extremely useful. "Global" data (i.e., data spanning the periodic table) have been compiled by Barbier (Ba69). The results are given Figs. 7.1, 7.2, and 7.3.



Fig. 7.1 Contours of equal cross section for photon-induced nuclear reactions (γ, n) , (γ, p) , $(\gamma, 2n)$, and (γ, α) as a function of photon energy, E_{γ} , and target material mass number, A_T . The coutour labeled "0" indicates the approximate boundary of the region of insignificant cross sections. The results have been smoothed in these plots. [Adapted from (Ba69).]



Fig. 7.2 Excitation functions for important photon-induced reactions (**upper frame**) and for photopion reactions (**lower frame**) at intermediate energies. [Adapted from (Ba69).]



Fig. 7.3 Excitation functions for photofission (γ , f) and photoneutron (γ , n) reactions at intermediate and high energies for photons incident on a variety of materials. [Adapted from (Ba69).]

Fig. 7.1 presents data in the form of contour plots of the cross sections $\sigma(E_{\gamma}, A_T)$ where E_{γ} is the photon energy and A_T is the atomic mass number of the target material. Figs. 7.2 and 7.3 provide the cross sections for specific processes as a function of energy. These figures are intended to illustrate the importance of various processes at different energies. Specific data should be obtained for precise, accurate calculations.

7.3.2 Results for Electrons at Low Energies

Results such as those presented in Section 7.3.1 form the basis of detailed activation calculations. Swanson (Sw79a) utilized the methodology of "Approximation B" of the analytical shower theory of Rossi and Griesen (Ro41), mentioned in Section 3.4.1, to estimate saturation activities rates in various materials. Since the energy domain below about 35 MeV is characterized by rapidly varying cross sections, Swanson provided energy-dependent results. Here only reactions of the type (γ , n), (γ , p), (γ , np), and (γ , 2n) were considered. Other reactions were ignored due to higher energy thresholds and small cross sections. Swanson points out that the dependence of the induced activity as a function of energy will generally follow that of the neutron yields (see Fig. 3.7). In Swanson's calculations, the material in question absorbs *all* of the beam power and has been irradiated for an *infinite* time with no cooldown [$t_i = \infty$, $t_c = 0$ in Eq. (7.8)]. Thus, so-called **saturation activities** are calculated, normalized to the incident electron beam
power (kW). Results of these calculations, taking into account the natural isotopic abundances and reaction thresholds, are provided in Table 7.1. The results are probably accurate to about + 30 per cent. At these low energies, the distribution of the radioactivity can often approximately be taken to be that of a point source for calculating the residual absorbed dose rates using, for example, Eq. (7.10), taking the summation over all of the γ -ray emitters presented at a given time. Table 7.1 provides the specific gamma-ray constant, Γ , for each tabulated radionuclide. These constants connect activity with the absorbed dose rates at a distance of one meter for point source conditions accounting for all the photons emitted by the decaying radionuclide and including those emitted secondarily such as internal bremsstrahlung and annihilation radiation due to β^+ emission manifested in the form of a pair of 0.511 MeV photons. For point sources, absorbed dose rates at other distances can be calculated by incorporating the inverse square law. In this context, absorbed dose rate is "loosely" connected with a somewhat obsolete unit, the exposure rate ($R h^{-1}$). Exposure rate is tied to the rate of liberation of ions in air by photons and is only defined for photon radiation fields. The quantity one R h^{-1} is the hourly liberation of one electrostatic unit of charge cm⁻³ of air at STP [1 R = 2.58 x 10⁻⁴ Coulomb kg⁻¹]. An exposure rate of 1.0 R h⁻¹ is approximately equal to 0.95 rad h⁻¹ of absorbed dose rate in tissue placed in the radiation field under consideration.

Table 7.1 Examples of saturation activities and saturation absorbed dose rates at one meter for electrons of energy E_o incident on various target materials of naturally-occurring isotopic abundances normalized to the beam power. [Adapted from Swanson (1979a).]

Target Material	Nuclide	Half-life	Threshold	Specific Gammy Ray Constant,		Saturation activity per uni	
Wateriai			(MeV)	[(mGy h ⁻¹) x(GBq m ⁻²) ⁻¹]	[(rad h ⁻¹) x (Ci m ⁻²) ⁻¹]	(GBq kW ⁻¹)	(Ci kW ⁻¹)
Al	²⁴ Na	14.95 h	23.7	0.52	1.9	1.1	0.03
	^{26m} Al	6.34s	13.0	0.17	0.62	330	8.8
Fe	⁵⁴ Mn	312.2 d	20.4	0.34	1.3	22.0	0.29
	⁵⁶ Mn	2.58h	10.6	0.24	0.9	1.12	0.032
	⁵³ Fe	8.51 min	13.6	0.19	0.7	27.0	0.74
Ni	⁵⁶ Ni	6.08 d	22.5	0.45	1.7		
	⁵⁶ Co ^a	77.23 d		0.65	2.4	2.4 ^b	0.07^{b}
	⁵⁷ Ni	35.6 h	12.2	0.38	1.42		
	⁵⁷ Co ^a	217.78 d		0.37	1.36	155 ^b	4.2 ^b
Cu	⁶¹ Cu	3.33 h	19.7	0.2	0.75	32.2	0.87
	⁶² Cu	9.67 min	10.8	0.17	0.63	407	11
	⁶⁴ Cu	12.7 h	9.91	0.11	0.40	185	5
W	^{182m} Ta	15.84 min	7.15	0.04	0.16		
	¹⁸² Ta ^a	114.4 d		0.17	0.64	13.3	0.36
	¹⁸³ Ta	5.1 d	7.71	0.04	0.16	23.3	0.63
	^{181}W	121.2 d	7.99	0.03	0.09	340	9.1
	^{185m}W	1.67 min	7.27	0.05	0.19		
	$^{185}W^{a}$	75.1 d		no γ-ray	no γ-ray	300 ^b	8.1 ^b
Au	^{195m} Au	30.5 s	14.8	0.04	0.16		
	$^{195}Au^{a}$	186.1 d		0.02	0.07	204 ^b	5.5
	^{196m} Au	9.6 h	8.07	0.03	0.12		
	¹⁹⁶ Au ^a	6.17 d		0.08	0.30	1520 ^b	41 ^b
Pb	²⁰³ Pb	6.21 s	8.38	0.05	0.19	17.4	0.47
	^{204m} Pb	1.14 h	14.8	0.32	1.20	44	1.2

^aThis radionuclide is the progeny of the radionuclide above it. ^bActivity of the progeny radionuclide

7.3.3 Results for Electrons at High Energies

For higher energy electrons, more reaction channels become available but the energy dependence is diminished. Swanson has also performed calculations of the production of radionuclides in this energy domain and the results are provided here in Table 7.2 (Sw79a). The results are valid to within an approximate factor of two for any beam energy E_o that is somewhat above the nuclide production threshold. Specific gamma-ray constants for point source conditions, Γ , reaction thresholds, and **integral radionuclide** production cross sections summed over parent isotopes per MeV of electron beam energy, denoted by the somewhat esoteric symbol $\Sigma f \sigma_{-2}$, are provided along with saturation activities and exposures rates. This quantity is a useful one because of the dominance, and lack of energy dependence, of the photoneutron production process, as was discussed in Section 3.2. The electrons are assumed to be totally absorbed in the material and no self-shielding effects are taken into account. The distribution of radioactivity within the material is not taken into account. The results are, again, presented for saturation conditions, i.e. $t_i = \infty$, $t_c = 0$ in Eq. (7.8), for the compositions of materials described in the footnotes to the table.

Cooling curves have been reported by Barbier (Ba69) for high energy electrons incident on various materials for an infinite irradiation at the rate of one electron per second. The results are given in Fig. 7.4, again per MeV of incident electron energy, for an infinite irradiation time, t_i . In this figure, results are given for the absorbed dose rates (mGy hr⁻¹) per electron s⁻¹ assuming the applicability of point source conditions. As discussed in Chapter 3, the lack of strong energy dependence (i.e., the scaling with incident beam power) and the simplicity of the photoneutron spectra make possible these rather uncomplicated results. Table 7.2 Estimations of saturation activities and absorbed rates at one meter in various materials, assuming "point source" conditions for high energy electrons. Results have been summed over the naturally-occurring isotopic composition of the materials. Radionuclides contributing <0.1 (mGy h⁻¹)(kW m⁻²)⁻¹ or with $t_{1/2}$ <1 minute have been excluded as have products of thermal neutron capture reactions. Adapted from Swanson (1979a).]

Material: Natural Aluminum							
Proc	luced Radio	nuclide	Saturation A	ctivity per	Saturation Absorbed		
			Unit Bear	n Power	Dose per Unit Beam		
					Power ^a		
	Half-life	Half-life Threshold		$(Ci kW^{-1})$	$(mGy h^{-1})x$	$(rad h^{-1})x$	
		(MeV)			$(kW m^{-2})^{-1}$	$(kW m^{-2})^{-1}$	
⁷ Be	53.22 d	33.0	4.8	0.13	0.04	0.004	
¹¹ C	20.33 min	33.5	1.9	0.051	0.3	0.03	
^{15}O	2.04 min	33.4	2.5	0.07	0.4	0.04	
18 F	1.83 h	34.4	5.2	0.14	0.8	0.08	
²² Na	2.60 y	22.5	9.2	0.25	3.0	0.3	
²⁴ Na	14.95 h	23.7	10.4	0.28	5.0	0.5	
^{26m} Al	6.34 s	13.0	320	8.8	60.0	6.0	
Material	: Natural Iro	n					
⁴⁶ Sc	83.79 d	37.4	7.4	0.2	2.0	0.2	
^{48}V	15.97 d	25.9	15.0	0.4	8.0	0.8	
⁵¹ Cr	27.70 d	19.7	15.0	0.4	3.0	0.3	
⁵² Mn	5.59 h	20.9	1.5	0.04	0.4	0.04	
^{52m} Mn	21.1 min	20.9	1.5	0.04	0.4	0.04	
⁵⁴ Mn	312.1 d	20.4	22.0	0.59	7.0	0.7	
⁵⁶ Mn	2.58 h	10.6	1.1	0.03	0.3	0.03	
⁵² Fe	8.28 h	24.1	2.2	0.06	0.4	0.04	
⁵³ Fe	8.51 min	13.6	27.4	0.74	4.9	0.49	
⁵⁵ Fe	2.74 y	11.2	490	13.3	90	9	

^a"no γ -rays" is applied to radionuclides having no, or very rare, emission of photons in their decay.

Table 7.2-continued

Material: Natural Copper							
Proc	luced Radio	nuclide	Saturation A	ctivity per	Saturation Absorbed		
			Unit Bean	n Power	Dose per l	U nit Beam	
					Pov	ver ^a	
^{58m} Co	9.04 h	41.8	24.4	0.66	4.0	0.4	
⁵⁸ Co	70.9 d	41.8	240=.4	0.66	2.0	0.2	
⁶⁰ Co	5.27 y	18.9	24.0	0.65	8.0	0.8	
⁶³ Ni	100 y	17.1	16.6	0.45	no γ-rays	no γ-rays	
⁶¹ Cu	3.33 h	19.7	32.2	0.87	6.0	0.6	
⁶² Cu	9.64 min	10.8	407	11	65	6.5	
⁶⁴ Cu	12.7 h	9.9	180	5	19	1.9	
Material	: Natural Tu	ngsten					
	Half-life	Threshol	(GBq kW ⁻¹)	(Ci kW ⁻¹)	$(\mathbf{mGy} \mathbf{h}^{-1})\mathbf{x}$	(rad h ⁻¹)x	
		d (MeV)			$(kW m^{-2})^{-1}$	$(kW m^{-2})^{-1}$	
^{182m} Ta	15.84 min	7.15	13.3	0.36	0.3	0.03	
¹⁸² Ta	114.4 d	7.15	13.3	0.36	1.1	0.11	
¹⁸³ Ta	5.1d	7371	22.9	0.62	0.9	0.09	
¹⁸⁴ Ta	8.7 h	14.9	1.78	0.048	0.4	0.04	
¹⁸⁵ Ta	49.4 min	8.39	20.7	0.56	0.6	0.06	
^{181}W	121.2 d	8.00	330	8.9	8.0	0.8	
^{185m} W	1.67 min	7.27	300	8.1	7.3	0.73	
¹⁸⁵ W	75.1 d	7.27	300	8.1	no γ-rays	no γ-rays	

^a"no γ -rays" is applied to radionuclides having no, or very rare, emission of photons in their decay.

Table 7.2-continued

Material: Natural Lead								
Produced Radionuclide			Saturation A	Activity per	Saturation Absorbed			
			Unit Bear	n Power	Dose per	U nit Beam		
					Pov	ver ^a		
²⁰⁴ Tl	3.78 y	14.83	0.92	0.025	no γ-rays	no γ-rays		
²⁰⁶ Tl	4.20 min	7.46	37	1.0	no γ-rays	no γ-rays		
^{207m} Tl	1.33 s	8.04	93	2.5	9.1	0.91		
²⁰⁷ Tl	4.77 min	8.04	93	2.5	no γ-rays	no γ-rays		
^{202m} Pb	3.53 h	15.3	0.13	0.06	0.3	0.03		
²⁰² Pb	$5.25 \times 10^4 \text{ y}$	15.3	0.13	0.06	no γ-rays	no γ-rays		
^{203m} Pb	6.21 s	8.38	31	0.83	1.3	0.13		
²⁰³ Pb	2.16 d	8.38	31	0.83	0.7	0.07		
^{204m} Pb	1.14 h	14.8	89	2.4	14	1.4		
Material: Typical Concrete ^b								
15 O	2.04 min	15.7	96	2.6	15	1.5		
²² Na	2.60 y	12.4	3.7	0.1	1.2	0.12		
²⁷ Si	4.16	17.2	74	2.0	12	1.2		
³⁸ K	7.64 min	13.1	3.7	0.1	15	0.15		

^a"no γ -rays" is applied to radionuclides having no, or very rare, emission of photons in their decay.

^bBy weight per cent, the isotopic composition of concrete was taken to be: ${}^{12}C(0.10)$, ${}^{16}O(53.0)$, ${}^{23}Na(1.6)$, ${}^{24}Mg(0.16)$, ${}^{27}Al(3.4)$, ${}^{28}Si(31.0)$, ${}^{39}K(1.2)$, ${}^{54}Fe(0.08)$, all others (9.5).



Fig. 7.4 Examples of total photon absorbed dose rates due to radioactive nuclei produced in large targets of various materials irradiated by an electron current of one electron sec⁻¹ per MeV of incident electron energy as a function of time since the cessation of the irradiation. The irradiation was assumed to have occurred for an **infinitely** long period of time. The absorbed dose rates are those found at one meter from a point source containing all of the radioactive nuclei. [Adapted from Barbier (1969).]

7.4 Activation of Components at Proton and Ion Accelerators

7.4.1 General Phenomena

Protons having energies above about 10 MeV, or sometimes less, will produce radioactivity upon interacting with matter. This will also occur for other ions above a specific energy of about 10 MeV/nucleon. In some special cases radioactivity can be produced at much lower energies due to exothermic nuclear reactions that either produce radionuclides directly or emit neutrons capable of inducing radioactivity through their secondary interactions. As with electron accelerators, if a given accelerator is properly designed with respect to the shielding against prompt radiation and has proper access controls to avoid direct beam-on exposure to people, the induced radioactivity is very likely to be the dominant source of occupational radiation exposure.

For the lower incident energies, below about 30 MeV, one is first concerned with production of radionuclides by such processes as (p, γ) and single- and multi-nucleon transfer reactions. While the details of the total cross sections for such reactions are complex, the systematics and approximate energy dependencies are globally well understood. In general, one has endothermic nuclear reactions that have a threshold, E_{th} , below which the process is forbidden by conservation of energy. For nuclear reactions induced by ions, E_{th} is related to the reaction Q-value [see Eq. (4.1)], Q_v , by

$$E_{th} = \frac{m+M}{M} |Q_v|, \qquad (7.11)$$

where Q_v is negative in an endothermic reaction that thus has a positive value of E_{th} . In this equation, *m* is the mass of the incident projectile while *M* is the mass of the target atom, assumed to stationary in the laboratory frame of reference. The treatise by Barbier (Ba69) has addressed activation by many types of particles. As was the case with electrons, some of these results are in the form of contour plots of the cross sections $\sigma(E_{\gamma},A_T)$ where E_{γ} is the photon energy and A_T is the mass number of the target material. These data are intended to convey the general idea of the importance of various processes at different energies. Samples of other data have also been provided concerning specific reaction processes at a variety of energies. These results are provided in Figs. 7.5, 7.6, 7.7, 7.8, 7.9, and 7.10. The results for the light elements (Fig. 7.9) are especially important for environmental radiation considerations while those for iron and copper targets (Fig. 7.10) are of great importance due to the universal presence of those elements in accelerator components.



Fig. 7.5 Contours of equal cross section for proton-induced nuclear reactions (p, n), (p, 2n), (p, pn), and (p, α) as a function of particle energy, E_p , and target material mass number, A_T . The results have been smoothed in these plots. [Adapted from (Ba69).]



Fig. 7.6 Contours of equal cross section for neutron-induced nuclear reactions (n, p), (n, 2n), and (n, α) as a function of particle energy, E_n , and target material mass number, A_T . The results have been smoothed in these plots. [Adapted from (Ba69).]



Fig. 7.7 Contours of equal cross section for deuteron-induced nuclear reactions (d, n), (d, 2n), (d, p), and (d, α) as a function of particle energy, E_d , and target material mass number, A_T . The results have been smoothed in these plots. [Adapted from (Ba69).]



Fig. 7.8 Contours of equal cross section for α -particle-induced nuclear reactions (α , n), (α , 2n), (α , p), and (α , pn) as a function of particle energy, E_{α} , and target material mass number, A_T . The results have been smoothed in these plots. [Adapted from (Ba69).]



Fig. 7.9 Excitation functions for the production of various radionuclides by protons incident on some light targets. [Reproduced from (Ba69).]



Fig. 7.10 Excitation functions for the production of various radionuclides by protons incident on iron and copper targets. [Reproduced from (Ba69).]

Thick target yields of radionuclides for targets having a range of atomic numbers have been systematically studied by Cohen for a number of nuclear processes spanning the periodic table (Co78). Fig. 7.11 is a representative plot of the general features of such excitation functions of such nuclear reactions. Specific processes may vary considerably from this behavior since "resonances" at specific nuclear excited states have been ignored. Table 7.3 lists a variety of such nuclear reactions along with the range of values of energy above threshold at which the radioactivity production rate has risen to 0.1% of the saturation value and also the range of saturation values for the production of radioactivity. It is assumed that the target thickness comfortably exceeds the range of the incident ion and that the irradiation period greatly exceeds the half-life of the radionuclide of interest. For shorter bombarding periods, t_i , one needs to multiply by the factor [1 - exp(- λt_i)]. Over the energy range of these curves, the importance of activation by secondary particles is small compared to that encountered at higher energies.



Fig. 7.11 Typical behavior of radionuclide production by (p, γ) or few-nucleon transfer reactions for energies not far above the reaction threshold, E_{th} . This behavior is typical of the nuclear reactions tabulated in Table 7.3. For detailed calculations, data related to specific reactions on specific target materials should be used. [Adapted from (Co78).]

Table 7.3 Tabulation of generalized parameters for the production of radionuclides by means of low energy nuclear reactions which span the periodic table. The ranges of energies are listed at which the production yields are at approximately 0.1 per cent of the tabulated saturation values. The "high/low" values for the saturated activity are also given. [Adapted from (Co78).]

Reaction	0.1% Yield- low	0.1% Yield- high	Sat. Yield- low	Sat. Yield- high	Reaction	0.1% Yield- low	0.1% Yield- high	Sat. Yield- low	Sat. Yield- high
	$(\mathbf{E}-\mathbf{E}_{\mathbf{th}})$	$(\mathbf{E}-\mathbf{E}_{\mathrm{th}})$	(µCi/	(µCi/		$(\mathbf{E}-\mathbf{E}_{\mathrm{th}})$	$(\mathbf{E}-\mathbf{E}_{\mathbf{th}})$	(µCi/	(µCi/
	(MeV)	(MeV)	μA)	μ <u>Α</u>)		(MeV)	(MeV)	μA)	μA)
(p,γ)	4	9	3×10^{2}	103	(³ He,γ)	4	6	1	2
(p,n)	0	6	3×10^{5}	8×10^{3}	([°] He,n)	3	12	102	3×10^{2}
(p,2n)	1	4	3×10^{5}	10%	$(^{\circ}He,2n)$	2	7	3×10^{2}	4×10^{3}
(p,3n)	1	6	3×10^{5}	10°	$(^{\circ}He, 3n)$	2	5	$2 \times 10^{\circ}$	3×10^4
(p,4n)	5	8	2×10^{3}	10°	([°] He,2p)	4	12	2×10^{2}	104
(p,5n)	5	10	10 ³	$2 \times 10^{\circ}$	$(^{3}\text{He},\alpha)$	6	14	2×10^{2}	10°
(p,pn)	2	5	2×10^{5}	2×10^{6}	('He,p3n)	10	15	10^{4}	4×10^{5}
(p,p2n)	3	8	3×10^{5}	2×10^{6}	(α,γ)	10	13	3	20
(d,γ)	5	7	30	100	(α,n)	1	9	3×10^2	10^{4}
(d,n)	2	7	$4 \ge 10^3$	3×10^5	(α ,2n)	1	4	5×10^3	4×10^4
(d,2n)	2	5	$2 \ge 10^5$	6 x 10 ⁶	(α,3n)	1	6	3×10^3	$7 \ge 10^5$
(d,3n)	1	4	$3 \ge 10^5$	10^{6}	(α,4n)	5	8	3×10^3	$4 \ge 10^4$
(d,4n)	4	8	$2 \ge 10^5$	$6 \ge 10^5$	(α,5n)	5	8	10^{4}	3×10^5
(d,5n)	6	10	10^{5}	10^{6}	(α,p)	5	8	$6 \ge 10^2$	2×10^4
(d,p)	2	7	$4 \ge 10^4$	$3 \ge 10^5$	(a,pn)	3	12	3×10^3	8 x 10 ⁴
(d,p2n)	2	10	10^{5}	2×10^{6}	$(\alpha, p2n)$	5	15	3×10^3	$7 \text{ x } 10^4$
(d,p3n)	8	15	10^{5}	2×10^{6}	$(\alpha, p3n)$	7	15	10^{4}	3×10^4
(d,2p)	5	15	3×10^3	4×10^4	(α,2p)	5	10	10^{2}	3×10^3
(d,α)	4	7	10^{4}	3×10^4	$(\alpha, \alpha n)$	6	16	3×10^3	3×10^4
(d,\alpha n)	5	15	2 x 10 ⁴	10^{5}					

7.4.2 Methods of Systematizing Activation Due to High Energy Hadrons

For proton and ion accelerators of higher energy, the neglect of secondary reactions and the restriction to few- and multi-nucleon transfer reactions can become a serious deficiency in the accuracy of estimation of induced radioactivity because of the rise in importance of such processes as spallation. Below a kinetic energy of about 40 MeV only few-nucleon transfer reactions are available. The variety of radionuclides that can be produced increases as one increases the bombarding energy because more thresholds are exceeded. As a general rule, at high energies ($E_0 \approx 1$ GeV or greater), one must consider that all radionuclides in the periodic table that have mass numbers less than that of the material exposed to the flux of hadrons may be produced. Of course, many of these are of little significance due to short lifetimes and small production cross sections. In fact, the cross sections for producing specific radionuclides often are nearly independent of the target element.

Table 7.4 gives a list radionuclides typically encountered in high energy proton accelerator installations and their half-lives. In this table only nuclides with half-lives between 10 minutes and 5 years are listed. Also, all "pure" β^- (electron) emitters are ignored. Pure β^- emitters are those radionuclides that emit no γ -rays in their decays. Pure β^- emitters generally present minimal exposure hazards at accelerators as compared with γ -ray emitters in routine maintenance activities since the radionuclides are produced throughout the materials comprising accelerator components, with resultant self-shielding of most of the electrons compared with the less effective shielding of the more penetrating γ -rays. In contrast, β^+ (positron) emitters are included in this table due to the generation of the pairs of 0.511 MeV photons that result from annihilation of the positrons with electrons in matter. Approximate thresholds and high energy cross sections for production of these radionuclides by protons, generally taken from the treatise by Barbier (Ba69), are also provided where available.

A systematic way of addressing the great multiplicity of radionuclides produced in accelerator components by high energy particles is highly desirable since it is often not practical to handle them all separately. Global properties of the distribution of radionuclides are found to be useful. Sullivan and Overton (Su65) have treated this problem in an elegant manner that is restated here. The initial starting point is a modification of Eq. (7.8) describing the dose rate as a function of irradiation and cooling times, t_i , and t_c , respectively;

$$\delta(t_i, t_c) = G\phi \Big[1 - \exp(-\lambda t_i) \Big] \exp(-\lambda t_c) , \qquad (7.12)$$

where $\delta(t_i, t_c)$ is the absorbed dose rate, ϕ is the flux density, and G is a collection of many contributing factors including the production cross section, the energy of the beam, the types of secondary particles produced, the isotopic composition of the irradiated component, the geometry, the energy of the γ -rays produced, and the attenuation coefficients for the γ -rays produced.

Table 7.4 Summary of radionuclides commonly identified in materials irradiated around accelerators. Approximate cross sections for their production at the high energy limit and approximate thresholds are given for selected radionuclides. [Adapted from (NC03) and (Ba69).]

Target	Radionuclides	Approximate	Half-life	Production Cross
Material		Threshold		Section
		(MeV)		(High Energy Limit)
	2			(mb)
Plastics & Oils	³ H	11	12.33 y	10
	Be	2	53.22 d	10
	¹¹ C	20	20.33 min	20
Al, Concrete	As above, plus			
	18 F	40	1.83 h	6
	²² Na	30	2.60 y	10
	²⁴ Na	5	14.95 h	10
Fe	As above, plus			
	⁴² K		12.32 h	
	⁴³ K		22.3 h	
	⁴⁴ Sc		3.97 h	
	^{44m} Sc		2.44 d	
	⁴⁶ Sc		83.8 d	
	⁴⁷ Sc		3.35 d	
	⁴⁸ Sc		1.82 d	
	48 V	20	15.97 d	6
	⁵¹ Cr	30	27.7 d	30
	⁵² Mn	20	5.59 d	30
	^{52m} Mn		21.1 min	
	⁵⁴ Mn	30	312.1 d	30
	⁵² Fe	30	8.28 h	4
	⁵⁵ Fe		2.74 v	
	⁵⁹ Fe		44.5 d	
	⁵⁶ Co	5	77.2 d	30
	⁵⁷ Co	30	271.7 d	30
	⁵⁸ Co	30	70.9 d	25
Cu	As above, plus			
	⁵⁷ Ni	40	35.6 h	2
	⁶⁵ Ni		2.52 h	
	⁶⁰ Co	30	5.27 y	15
	⁶⁰ Cu		23.7 min	
	⁶¹ Cu	20	3.33 h	100
	⁶² Cu		9.67 min	-
	⁶⁴ Cu		12.70 h	
	^{62}Zn	15	9.19 h	60
	⁶⁵ Zn	0	243.7 d	100

If the number of radionuclides produced by the irradiation which have decay constants in the interval between λ and $\lambda + d\lambda$ is represented by the differential, dm, then the corresponding increment in absorbed dose rate due to them, $d\delta(t_i, t_c)$, is given by

$$d\delta(t_i, t_c) = dm G\phi \Big[1 - \exp(-\lambda t_i) \Big] \exp(-\lambda t_c) \,. \tag{7.13}$$

If it is assumed that the value of G is independent of λ , or its dependence on λ is small compared to other factors, then one can integrate;¹⁶

$$\delta(t_i, t_c) = G\phi \int_{\lambda_0}^{\infty} d\lambda \frac{dm}{d\lambda} \left[1 - \exp(-\lambda t_i) \right] \exp(-\lambda t_c) \,. \tag{7.14}$$

Here, λ_o is the shortest decay constant, corresponding to the longest mean-life, to be considered. Fig 7.12 is a plot of the number of radionuclides as a function of half-life, $t_{1/2}$, that have half-lives less than that particular half-life for several choices of atomic mass number, A. This corresponds to the distribution of radionuclides that could be produced in a target of mass number A irradiated by high energy hadrons. As one can see, these cumulative distributions are well-described for values of half-life between about 10⁻³ and 10³ days by a function of the following form:

$$N(t_{1/2}) = a + b \ln(t_{1/2}), \tag{7.15}$$

where $N(t_{1/2})$ is the number of radionuclides with half-lives less than the value of $t_{1/2}$ and a and b are fitting parameters. Because of the one-to-one correspondence between values of $t_{1/2}$, τ , and λ , in this **Sullivan-Overton approximation** one can just as well write

$$m(\lambda) = a + b \ln \lambda , \qquad (7.16)$$

where $m(\lambda)$ is the number of radionuclides with decay constants greater than λ for the material of concern. Thus,

$$\frac{dm(\lambda)}{d\lambda} = \frac{b}{\lambda} . \tag{7.17}$$

Substituting into Eq. (7.14), one gets

$$\delta(t_i, t_c) = Gb\phi \int_{\lambda_0}^{\infty} \frac{d\lambda}{\lambda} [1 - \exp(-\lambda t_i)] \exp(-\lambda t_c) = Gb\phi \left\{ \int_{\lambda_0}^{\infty} \frac{d\lambda}{\lambda} \exp(-\lambda t_c) - \int_{\lambda_0}^{\infty} \frac{d\lambda}{\lambda} \exp\left[-\lambda (t_i + t_c)\right] \right\}.$$
(7.18)

¹⁶Taking this step implies the assumption that, on average, the radionuclide production cross sections under consideration are independent of both the half-lives and the particle energies. Somewhat remarkably, this approximation is a sufficiently accurate one for the present purpose.



Fig. 7.12 Total number of radionuclides having half-lives up to a given half-life as a function of half-life for target mass numbers less than those indicated. [Adapted from (Ba69).]

The changes of variables $\alpha = \lambda t_c$ [first term] and $\alpha' = \lambda (t_i + t_c)$ [second term] are helpful;

$$\delta(t_i, t_c) = Gb\phi \left\{ \int_{\lambda_o t_c}^{\infty} d\alpha \frac{e^{-\alpha}}{\alpha} - \int_{\lambda_o(t_i + t_c)}^{\infty} d\alpha' \frac{e^{-\alpha'}}{\alpha'} \right\}.$$
(7.19)

Recognizing that the integrands are identical and simplifying by rearranging the limits of integration, we have

$$\delta(t_i, t_c) = Gb\phi \int_{\lambda_o t_c}^{\lambda_o(t_i + t_c)} d\alpha \frac{e^{-\alpha}}{\alpha} .$$
(7.20)

The integration results in a series expansion found in standard tables of integrals;

$$\int_{x_1}^{x_2} \frac{e^{ax} dx}{x} = \left[\ln x + \frac{ax}{1!} + \frac{a^2 x^2}{2 \times 2!} + \frac{a^3 x^3}{3 \times 3!} + \dots \right]_{x_1}^{x_2}.$$
 (7.21)

Substituting,

$$\int_{\lambda_o t_c}^{\lambda_o(t_i+t_c)} \frac{e^{-\alpha} d\alpha}{\alpha} = \left[\ln \alpha - \alpha + \frac{\alpha^2}{4} - \frac{\alpha^3}{18} + \dots \right]_{\lambda_o t_c}^{\lambda_o(t_i+t_c)}.$$
(7.22)

Evaluating, one obtains

$$\delta(t_i, t_c) = Gb\phi \left[\ln \left(\frac{t_i + t_c}{t_c} \right) - \lambda_0 t_i + \dots \right].$$
(7.23)

Since λ_o approaches zero (corresponding to large mean-lives), the following is obtained:

$$\delta(t_i, t_c) \approx B\phi \ln\left(\frac{t_i + t_c}{t_c}\right), \tag{7.24}$$

where several constants are merged in the new parameter *B*.

7.4.2.1 Gollon's Rules of Thumb

Gollon (Go76) has further elaborated on these principles and determined four very useful "rules of thumb" for high energy hadron accelerators at which the extranuclear hadron cascade process produces the major fraction of the induced activity. These are extremely useful for approximate radioactivity estimates.

Rule 1: This is equivalent to Eq. (7.10), repeated here for convenience;

$$\frac{dD}{dt} = 0.4 \frac{S}{r^2} \sum_{i} E_{\gamma i} , \qquad (7.25)$$

where the summation is over all γ -rays present, including appropriate branching fractions if more than one photon is emitted per decay. [See comment about alternative units related to Eq. (7.10).]

- *Rule 2:* In many common materials, about 50 % of the nuclear interactions produce a nuclide with a half-life longer than a few minutes. Further, about 50 % of these have a half-life longer than one day. Thus, approximately 25 % of the nuclear interactions (e.g., the "stars" discussed in Section 4.7.2) produce a radionuclide having a half-life exceeding approximately one day.
- *Rule 3:* For most common shielding materials, the approximate dose rate dD/dt due to a constant irradiation is [see Eq. (7.24)] given by

$$\frac{dD}{dt} = B\phi \ln\left(\frac{t_i + t_c}{t_c}\right). \tag{7.26}$$

In the above, the geometry and material dependent factor *B* can often be determined empirically, or estimated by using *Rule 2*, while ϕ is the incident flux density. This expression appears to be valid also for intermediate energy heavy ion beams, for example at 86 MeV/nucleon (Tu84).

Rule 4: In a hadronic cascade, each proton or neutron produces about four inelastic interactions for each GeV of energy.

Some examples can illustrate the use of these rules of thumb. As one illustration, in a short target of 1/10 of an interaction length, approximately 10 % of an incident beam of 10^{11} protons s⁻¹ will interact. Assume this has been occurring for several months (long enough to reach saturation production for many radionuclides) at this constant rate. Using *Rule 2* in conjunction with the above rate, one determines that the decay rate after one day of the shutdown is 2.5 x 10⁹ Bq (68 mCi). If each of these decays produces a one MeV γ -ray, then *Rule 1* will indicate an absorbed dose rate of 27 mrad h⁻¹ (≈ 0.27 mGy h⁻¹) at one meter away.

Rule 3 can be used in such a calculation to predict the absorbed dose rate from a point source at some future time after beam shutdown. Furthermore, this rule is not restricted to "point" sources but can be used for more massive ones, with suitable adjustments to

the geometry factors. Sometimes one can estimate the product $B\phi$ or use a measurement of the exposure or absorbed dose rate early in a shutdown period to determine it empirically in order to to predict the "cooldown" for later times using Eq. (7.26) as a tool in planning radiological work. *Rule 3* also clearly works for extended shields irradiated by secondary particles from a well-developed cascade.

Rule 4 can be used to crudely estimate the activation of a beam absorber by incident high energy particles when it is coupled with *Rule 2*. For example, a beam of $10^{12} 400$ GeV protons s⁻¹ (= 0.16 µA or 64 kW) produces a total of 4 x 400 x 10^{12} stars s⁻¹ in a beam absorber. If 25 % of these produce a radionuclide with a half-life > 1 day (*Rule 2*), then the total amount of the moderately long-lived radioactivity (at saturation) is

$$\frac{(0.25 \text{ atoms/star})(1.6 \times 10^{15} \text{ stars/sec})}{3.7 \times 10^{10} \text{ sec}^{-1} Ci^{-1}} = 10.8 \text{ kCi}.$$
(7.27)

At sufficiently large distance (say 10 meters), *Rule 1* could be used to calculate an absorbed dose rate from a point source assuming all decays are 1 MeV γ -rays;

$$\frac{dD}{dt} = 0.4(1 \text{ MeV}) \left(\frac{1.08 \times 10^4 \text{ Curies}}{10^2 \text{ meter}^2} \right) = 43 \text{ rads / hour}.$$
 (7.28)

A valuable quantity used to quantify the absorbed dose rate, dD/dt, at the surface of a thick target is the **danger parameter**, **D**, as developed by Barbier (Ba69) for a thick object irradiated by beam having a uniform flux density ϕ . If this source of radioactivity subtends solid angle Ω at the point of concern, then

$$\frac{dD}{dt} = \frac{\Omega}{4\pi} \phi \,\mathbf{D}\,. \tag{7.29}$$

For contact with a semi-infinite slab of uniformly irradiated material, the fractional solid angle factor ($\Omega/4\pi$) has the intuitively obvious value of 1/2. The danger parameter has the physical interpretation as the absorbed dose rate found inside a cavity of arbitrary form embedded in an infinite volume of a material which has been uniformly irradiated by a unit flux density (one particle per second per square centimeter). Figures 7.13 give representative examples of plots of **D** for several elements and a few compounds. These curves thus can be used to predict cooling of various components around accelerators. Gollon (Go76) has also provided "cooling curves" for iron struck by high energy protons. These are given in Fig. 7.14 and include both calculations by Armstrong and Alsmiller (Ar69a) and empirical measurements at the Brookhaven National Laboratory AGS, the Fermilab Main Ring Accelerator, and the Fermilab Neutrino Experimental Area target station.

Of course, situations arise where the determination of ϕ in the danger parameter equation is not at all simple. For example, one can have activation in a large object where the hadronic cascade is contributing numerous hadrons at a variety of energies from a multitude of directions. Fortunately, important features of activation phenomena have little or no correlation with energy. The chief of these is evidenced by the excitation functions of various reactions. As seen in Figs. 7.9, 7.10, and 7.11, the cross sections rise just above the threshold and then, somewhere in the region of tens of MeV above the threshold, a leveling-off occurs. Furthermore, in general the cross sections for production of radionuclides by neutrons and protons (and even other ions and particles) do not differ greatly from each other (i.e., within one to two orders of magnitiude) at the higher energies.



Fig. 7.13 Values of the Barbier danger parameter, **D**, for selected materials at a proton irradiation energy of 500 MeV. [Adapted from (Ba69).]



Fig. 7.13-continued.



Fig. 7.14 Cooling curves for various irradiation times for iron struck by high energy protons as calculated by Armstrong and Alsmiller (Ar69s). Also shown are the results of measurements. The one labeled "Main Ring", is the measured average cooling curve for the Fermilab Main Ring synchrotron after its initial three years of operation at energies of 200 or 400 GeV. The curve labeled "Neutrino" is for a neutrino target station at Fermilab after eight months of operation at 400 GeV. The curve labeled "AGS" is for an extraction splitter in use for many years at the BNL AGS at energies up to 30 GeV. [Adapted from (Go76).]

7.4.3 The Utilization of Monte Carlo Star Densities in Activation Calculations

The "leveling-off" of the cross section as a function of energy has some very important implications. An important one is the fact that for estimating activation, one can perform approximate calculations without performing integration over energy if one has some reasonable estimate of the hadron flux density above the reaction threshold of interest. An average effective cross section can then be used. Another feature of these excitation functions is the fact that the leveling off occurs in the region from a few 10's to a few 100's of MeV, precisely where relatively fast Monte Carlo hadron shielding calculations are available from several different codes (e.g., CASIM, FLUKA, HETC, and MARS).

It is often possible to relate the flux density of high energy hadrons (i.e., those with energies above the leveling off) to the star density, S, calculated from such Monte Carlo calculations through the relationship

$$\phi(\vec{r}) = \frac{\lambda}{\rho} \frac{dS(\vec{r})}{dt} , \qquad (7.30)$$

where $\phi(\vec{r})$, the flux density (cm⁻² s⁻¹) at position vector at \vec{r} , is related to the rate of star density production $\frac{dS(\vec{r})}{dt}$ (stars cm⁻³ s⁻¹) at the same location¹⁷. ρ (g cm⁻³) is the density and λ (g cm⁻²) is the interaction length¹⁸. The value of $\phi(\vec{r})$ so determined could, in principle, be substituted into Eq. (7.29) for calculating absorbed dose rate due to residual activity using the Barbier danger parameter, **D**, if one were to make suitable adjustments in the solid angle. However, the limitation of this approach is the fact that the Monte Carlo cutoffs may introduce an energy (or momentum) cutoff (e.g., typically 300 MeV/c was used in CASIM) not necessarily matched to the reaction threshold. In order to calculate dose equivalent rates, Gollon (Go76) made detailed calculations and obtained the following formula:

$$\frac{dD(\vec{r})}{dt} = \frac{\Omega}{4\pi} \frac{dS(\vec{r})}{dt} \omega(t_i, t_c), \qquad (7.31)$$

where the so-called "omega factor" (ω -factor) $\omega(t_i, t_c)$ is related to the Barbier danger parameter, **D**. For iron, Gollon gives the following values for two useful situations:

 $\omega(\infty, 0) = 9 \ge 10^{-6} \operatorname{rad} h^{-1}/(\operatorname{star} \operatorname{cm}^{-3} \operatorname{s}^{-1}) = 9 \ge 10^{-2} \,\mu\text{Gy} \,h^{-1}/(\operatorname{star} \operatorname{cm}^{-3} \operatorname{s}^{-1})$ (7.32a) (infinite irradiation, zero cooling time), and

 ω (30d, 1d) = 2.5 x 10⁻⁶ rad h⁻¹/(star cm⁻³ s⁻¹) =2.5 x 10⁻² µGy h⁻¹/(star cm⁻³ s⁻¹)(7.32b) (30 days irradiation, 1 day cooling time).

¹⁷ This flux density is the delivery rate of the "star fluence" discussed in Section 4.7.2.

¹⁸ Once again, the adherence to traditional notation requires that care must be taken not to confuse interaction length with activity constant since they both are customarily denoted by the <u>same</u> symbol, λ .

Estimates of other ω -factor values can be made, for example, by scaling results obtained by Armstrong and Alsmiller (Ar69a) and Gabriel and Santoro (Ga73) for selected values of t_i and t_c . This has been done for three choices of values of t_i , and the results are shown in Fig. 7.15 for irradiated iron (Co98). Curves of this type should be used with some degree of caution. They can readily be used to predict the relative "cooling" rates of various components around accelerators with a fair degree of accuracy. Their use in the prediction of absolute dose equivalent rates due to activated accelerator components required additional care. To do this, the geometric configuration should be simple and well-defined, the flux density of thermal neutrons should be a small component of the prompt radiation field, and the activation of other materials in proximity such as the enclosure walls should be taken into account. Cracks through the shielding materials can sometimes result in higher dose equivalent rates that are difficult to model. The interactions of thermal neutrons in concrete shielding can make a significant contribution to the dose equivalent rate. This phenomenon has been discussed by Armstrong and Alsmiller (Ar69b) and by Cossairt (Co96) and will be summarized in Section 7.4.4.

More generally, Gollon derived a simple relationship between dose rates involving cooling times different from "standard" ones for which values of **D** and ω are available. As stated previously, the dose rate after irradiation time t_i and cooldown time t_c is

$$\delta(t_i, t_c) = \sum_{\mu} A_{\mu} \Big[1 - \exp(-\lambda_{\mu} t_i) \Big] \exp(-\lambda_{\mu} t_c) , \qquad (7.33)$$

where the summation over index μ includes all relevant radionuclides with the product of flux density and geometry factors being absorbed (and allowed to vary with radionuclide) in the quantity A_{μ} .

Rearranging, Gollon obtained

$$\delta(t_i, t_c) = \sum_{\mu} A_{\mu} \Big[\exp\{-\lambda_{\mu} t_c\} - \exp\{-\lambda_{\mu} (t_i + t_c)\} \Big] = \delta(\infty, t_c) - \delta(\infty, t_i + t_c).$$
(7.34)

Thus, the infinite irradiation curve can be used to determine any other combination of the times t_i and t_c . In fact, this formula may be used also with empirical results such as, for example, radiation survey data, in order to predict future radiological conditions.



Fig. 7.15 Extrapolations of the cooling factor $\omega(t_i, t_c)$ from the work of Armstrong and Alsmiller (Ar69a) and Gabriel and Santoro (Ga73) compared with those of Gollon (Go76) for irradiated iron. [Reproduced from (Co98).]

A reliable method for connecting the production of "stars" in material (e.g., as calculated by a Monte Carlo code) to the production of atoms of some radionuclide is by the ratios of cross sections. Thus, at some point in space, \vec{r} , the rate of production of atoms per cm³, $n_i(\vec{r})$, of some radionuclide, *i*, is approximately given by

$$\frac{dn_i(\vec{r})}{dt} \approx \frac{\sigma_i}{\sigma_{in}} \frac{dS(\vec{r})}{dt} = \frac{\Sigma_i}{\Sigma_{in}} \frac{dS(\vec{r})}{dt}, \qquad (7.35)$$

where one essentially scales the star density production rate (e.g., stars cm⁻³ s⁻¹) by the ratio of the production (reaction) cross section for the nuclide of interest, σ_i , to the total inelastic cross section σ_{in} or, equivalently, by the ratio of the macroscopic cross sections, (Σ_i/Σ_{in}) . The phenomena will obey the usual activation equation. The reason this is *approximate* is due to the standard concerns about constancy of cross sections with energy, the lack of perfect "matching" of effective reaction thresholds, etc.

7.4.4 Uniform Irradiation of the Walls of an Accelerator Enclosure

Somewhat special considerations may apply to the concrete shielding surrounding accelerators. As was seen before in Table 6.2, ordinary concrete typically contains a partial density of about 0.04 g cm⁻³ of sodium. This "typical" value varies a great deal due to the variety of minerals that might be present in local concrete. The significance of this seemingly small additive is that the naturally dominant isotope present is ²³Na. This nucleus has the relatively large thermal neutron capture cross section of 535 mb. Patterson (Pa58) determined that average thermal neutron flux density, ϕ_{th} , in a concrete room is approximately given as follows:

$$\phi_{th} = \frac{1.25Q}{S} \ (\text{cm}^{-2}\text{s}^{-1}), \tag{7.36}$$

where Q is the number of fast neutrons produced per second in the enclosure and S is the inside surface area of the enclosure (cm²). Thus, a substantial flux density of thermal neutrons can be present in an accelerator room and this flux can produce significant amount of ²⁴Na with its 15-hour half-life. The pair of relatively high energy photons emitted in its decay (1.37 and 2.75 MeV) further enhances the residual radioactivity hazard. Furthermore, while the dose due to activated components falls off radially with distance, if absorption by the air is not significant the photon flux density due to activation of the walls of an empty room uniformly irradiated by such thermal neutrons is a constant. Thus, the absorbed dose rate due to the walls anywhere inside the enclosure will be equal to the absorbed dose rate at the wall. This has been explicitly demonstrated for cylinders by Armstrong and Barish (Ar69b) and is also true for the interior of all mathematically "well-behaved" closed surfaces (Co96). This fact can readily be demonstrated by analogy to the Gauss Law in electrostatics¹⁹ as follows by examining the situation in Fig. 7.16.

¹⁹ The Gauss law of electrostatics has been treated in detail by others; e.g., Jackson (Ja75) and Konopinski (Ko81).



Fig. 7.16 Geometry for deriving the relationship between a surface of uniform emission and the flux density at any point within it. [Reproduced from (Co96).]

Consider a simple, closed surface that emits an omnidirectional flux density of some particle ϕ_0 (e.g., particles cm⁻²s⁻¹) that is constant over the surface. One wants to calculate the flux density at some arbitrary point in space *P* within the surface. *P* is located at radius vector \vec{r} . Consider further the contributions of the particles emitted by some elemental area $d\vec{A}$ at *P* where $d\vec{A}$ is perpendicular to the surface at coordinate vector \vec{r} . The solid angle subtended at *P* by $d\vec{A}$ is

$$d\Omega = \frac{d\dot{A} \bullet \hat{n}}{\left|\vec{r}' - \vec{r}\right|^2},\tag{7.37}$$

where the unit vector \hat{n} is given by

$$\hat{n} = \frac{\vec{r}' - \vec{r}}{|\vec{r}' - \vec{r}|} \ . \tag{7.38}$$

But the increment of flux at point P due to elemental area $d\vec{A}$ is given by

$$d\phi = \frac{\phi_o}{4\pi} \frac{d\vec{A} \bullet \hat{n}}{\left|\vec{r}' - \vec{r}\right|^2}$$

Thus,

$$d\phi = \frac{\phi_o}{4\pi} d\Omega$$
 and $\int_{4\pi} \frac{\phi_o}{4\pi} d\Omega = \phi_o$. (7.39)

In some situations it is important to minimize the amount of sodium in the concrete ingredients in order to reduce exposures to individuals conducting maintenance on the accelerator. In fact, the phenomena described above has been noticed at accelerators and sometimes leads to "disappointment" in how little gamma-ray exposure rates are reduced when activated accelerator components are removed from enclosures with equally activated walls. For example, Armstrong and Barish (Ar69b) have calculated residual dose rates inside a cylindrical accelerator tunnel due to both the magnets and the concrete walls for 3 GeV protons incident on iron. These authors also included some other reactions due to higher energy neutrons, such as spallation, that are capable of also producing ²⁴Na from common ingredients of concrete. The results are shown in Fig. 7.17 for the surface at the tunnel wall.

The discussion of the production of radioactivity continues in Chapter 8 with specific emphasis on environmental radiation protection.



Fig. 7.17 Photon dose rate at surface of tunnel wall after infinite irradiation time for concrete containing one per cent sodium by weight. [Adapted from (Ar69b).]

Problems

- 1. A 1 mA beam of 30 MeV electrons is absorbed by an aluminum target. Calculate the saturation activities of all major radionuclides produced in the target. Assuming no self-absorption and an infinitely long irradiation period, what will the absorbed dose rate at a distance of 2 meters away immediately after beam shutdown and one hour later? The target can be assumed to be a point source for this estimate.
- 2. A copper beam stop has been bombarded with high energy hadrons for 30 days and exhibits a dose rate of 100 mrem hr⁻¹ at 1 meter away 1 day after the beam is turned off. Maintenance work needs to be scheduled in the vicinity within the next 6 months. Using both Gollon's Rule No. 3 and the Barbier Danger parameter curves, predict the cooling curve and determine when the dose rate is less than a 20 mrem hr⁻¹ maintenance work criteria. Make a table of dose rate versus cooling time in days for both methods. How well do the two methods agree? (Hint: Use the initial value of the dose rate to scale values of **D**.)
- 3. A 100 GeV beam (10^{12} protons s⁻¹) strikes the center of a large solid <u>iron</u> cylinder 30 cm in radius for 30 days. Use the star density curves from the Appendix C and the " ω " factors calculated by Gollon to estimate the residual dose rate after 1 day cooldown at contact with the side of the cylinder in the "hottest" spot. Using Gollon's third rule, how long must the repair crew wait to service this item in a contact radiation field of absorbed dose rate < 10 rad hr⁻¹?
- 4. A copper target is bombarded with high energy protons such that 10 stars per incident proton are produced. If the incident beam is 10¹¹ protons s⁻¹, what is the specific activity (average) of ⁵⁴Mn that is produced after two years of operation? ⁵⁴Mn has a high energy spallation production cross section of about 20 mb in Cu. The target is a cylinder, 10 cm radius by 15 cm long. The half-life of ⁵⁴Mn is 312 days. Express the answer in both Bq cm⁻³ and Ci cm⁻³. (Hint: This problem is best if the calculation is done at saturation and then corrected for the non-infinite irradiation time. Also, one needs to use the inelastic cross section given, for example, in Chapter 4.)

8.1 Introduction

Chapter 7 provided the tools needed to address the subject of induced radioactivity. In this chapter, the discussion of induced radioactivity at accelerators is continued to address its production and propagation in environmental media such as air, soil, rock, and water. Aspects pertinent to both occupational radiation safety and environmental protection are covered. The chapter includes introductory material connecting meteorology and hydrogeology with the production of this radioactivity.

8.2 Airborne Radioactivity

8.2.1 Production

Thomas and Stevenson have presented a very useful synopsis, largely followed here, of the production of radioactivity in air (Th88). This discussion was reprised by Swanson and Thomas (Sw90). The principal source of radioactivity in air at accelerators is due to the interaction of primary and secondary particles directly with the constituent target nuclei in the air in accelerator enclosures. Activated dust and gaseous emission from activated liquids are of much less importance. Table 8.1 gives the abundances and number densities of atoms of the most common stable isotopes found in the atmosphere both by volume percentage and in terms of the atomic density, N_j .

Table 8.1	Abundances of the most prominent stable nuclides in the atmosphere at
sea level.	

Isotope	Percentage by volume in the atmosphere (atoms)	N_j (atoms cm ⁻³) at room temperature
^{14}N	78.16	4.199 x 10 ¹⁹
¹⁶ O	20.00	1.075 x 10 ¹⁹
⁴⁰ Ar	0.467	$1.558 \ge 10^{17}$
¹⁵ N	0.290	$2.149 \ge 10^{16}$
¹⁸ O	0.040	$1.255 \ge 10^{17}$

Patterson and Thomas (Pa73), have expanded the general activation equation, Eq. (7.8), to derive the total specific activity, S (typically in units of Bq cm⁻³), of an enclosed volume of radioactive air;

$$S = C \sum_{i} \left\{ \sum_{j} N_{j} \overline{\sigma}_{ij\gamma} \phi_{\gamma} + \sum_{j} N_{j} \overline{\sigma}_{ijTH} \phi_{TH} + \sum_{j} N_{j} \overline{\sigma}_{ijHE} \phi_{HE} \right\} \left\{ 1 - \exp(-\lambda_{i} t_{irrad}) \right\} \exp(-\lambda_{i} t_{c}) \quad (8.1)$$

where ϕ_{γ} , ϕ_{THP} and ϕ_{HE} , represent the average photon, thermal neutron, and high energy particle flux densities, respectively. To avoid confusion, in this equation t_{irrad} is the irradiation time while t_c represents the decay time. The $\overline{\sigma}_{ijk}$ values are the corresponding cross sections averaged with the energy-dependent flux density over energy,

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$$\overline{\sigma}_{ijk} = \frac{\int_{E_{\min}}^{E_{\max}} dE \sigma_{ijk} (E) \phi_k(E)}{\int_{E_{\min}}^{E_{\max}} dE \phi_k(E)},$$
(8.2)

where the limits of integration correspond to the three broad phenomenological ranges in the summation. The constant *C* is the conversion to specific activity and is equal to unity for activity in Becquerels cm⁻³ if all the units of length implicit in the quantities in Eq. (8.1) are expressed in cm. The outer sum over index *i* includes all possible radionuclides produced and the sum over the index *j* is over the parent atoms found in air. The flux densities are, without further information, the average over some relevant spatial volume.

Table 8.2 lists the radionuclides that can be produced from the principle constituents in air along with the reaction mechanisms associated with their production and an estimate of the average production cross section. The large cross sections for (n, γ) and (n, p) reactions are for captures of neutrons of thermal energies ($\langle E_n \rangle \approx 0.025 \text{ eV}$) while the remaining cross sections are generally the saturation cross sections found in the region above approximately a few 10's of MeV. The γ -induced reactions are present at virtually all accelerators and at most energies. The corresponding cross sections will, of course, be energy-dependent especially at energies just above the reaction thresholds.

8.2.2 Accounting for Ventilation

Adjustments for the presence of ventilation can be quite conveniently made for a given radionuclide by using an effective decay constant, λ' , that includes the physical decay constant, λ , along with a ventilation term, r;

$$\lambda' = \lambda + r$$
, (8.3)
where $r = \frac{D}{V}$,

with D being the ventilation rate in air volume per unit time and V being the enclosure volume. Thus r is the number of air changes per unit time. The applicable differential equation, an extension of Eq. (7.4) with ventilation included, is

$$\frac{dn'}{dt} = -\lambda n'(t) - rn'(t) + N\sigma\phi = -\lambda'n'(t) + N\sigma\phi.$$
(8.4)

After an irradiation time, t_i , with no initial activation, the solution by analogy with Eq. (7.5) is

$$n'(t_i) = \frac{N\sigma\phi}{\lambda + r} \left\{ 1 - \exp\left[-(\lambda + r)t_i \right] \right\}.$$
(8.5)

So the specific activity with mixing, $a'(t_i)$, is given by

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$$a'(t_i) = \lambda n'(t_i) = \frac{\lambda N \sigma \phi}{\lambda + r} \left\{ 1 - \exp\left[-(\lambda + r)t_i \right] \right\}.$$
(8.6)

But $N\sigma\phi$ is just the saturation concentration, a_{sat} , without mixing [see Eq. (7.7)]. Hence, with mixing the saturation concentration, a'_{sat} , is

$$a'_{sat} = \frac{\lambda \, a_{sat}}{\lambda + r}.\tag{8.7}$$

Table 8.2 Rad	lionuclides with half-life > 1 minute that can be produced in a	air at
accelerators.	[Adapted from (Sw90).]	

Radionuclide	Half-life	Emission	Parent	Production	High Energy
			Element	Mechanism	Cross Section
					(mb)
^{3}H	12.32 y	β-	Ν	Spallation	30
		·	0	Spallation	30
⁷ Be	53.22 d	γ, elect. capt.	Ν	Spallation	10
			0	Spallation	5
			Ar	Spallation	0.6
¹¹ C	20.33 min	β^+	Ν	Spallation	10
			0	Spallation	0.7
14			Ar	Spallation	0.7
^{14}C	5700 y	β^-	Ν	(n _{thermal} ,p)	1640
¹³ N	9.96 min	β^+	Ν	Spallation	10
			Ν	(γ,n)	10
			0	Spallation	9
			Ar	Spallation	0.8
¹⁴ O	1.18 min	β+,γ	0	Spallation	1
			Ar	Spallation	0.06
¹⁵ O	2.04 min	β^+	0	Spallation	40
			0	(γ,n)	10
10			Ar	Spallation	
¹⁸ F	1.83 h	β+,	Ar	Spallation	6
²⁴ Ne	3.38 min	β ⁻ ,γ	Ar	Spallation	0.12
²² Na	2.603 y	β^+, γ	Ar	Spallation	10
²⁴ Na	14.95 h	β-	Ar	Spallation	7
²⁷ Mg	9.46 min	β ⁻ ,γ	Ar	Spallation	2.5
^{28}Mg	20.92 h	β ⁻ ,γ	Ar	Spallation	0.4
²⁸ A1	2.24 min	β ⁻ ,γ	Ar	Spallation	13
²⁹ Al	6.56 min	β ⁻ ,γ	Ar	Spallation	4
³¹ Si	2.62 h	β ⁻ ,γ	Ar	Spallation	6
^{30}P	2.50 min	β^+, γ	Ar	Spallation	4.4
32 P	14.26 d	β-	Ar	Spallation	25
³³ P	25.34 d	, β [_]	Ar	Spallation	9
³⁵ S	87.51 d	, β ⁻	Ar	Spallation	23
^{34m} Cl	32.0 min	βγ	Ar	Spallation	0.7
³⁸ Cl	37.24 min	β.γ	Ar	(y.pn)	4
³⁹ Cl	55.6 min	β.γ	Ar	(γ , p)	7
⁴¹ Ar	1.83 h	β-,γ	Ar	$(n_{\text{thermal}}, \gamma)$	660
Since low energy accelerators must, for other reasons, contain their beams in continuous vacuum systems, the activation of air at these machines is greatly minimized. At high energy accelerators, it is quite common to have air gaps at certain interface points to accommodate devices associated with beam targetry or beamline diagnostic instrumentation which render continuous vacuum impractical. These "air gaps" are only found in external beam lines and possibly in linear accelerators. The beam in a circular accelerator or storage ring is, of necessity, contained in continuous vacuum since any air gaps, if traversed multiple times by the beam particles, would result in an unacceptable rate of beam loss. In addition, the large multiplicity of secondary particles produced as a part of cascade processes, either electromagnetic or hadronic, can produce airborne radioactivity external to the beamline vacuum.

If the accelerator enclosures were completely sealed, there would be no releases to the outside world and the hazard of these airborne radionuclides would be entirely restricted to those who might have to enter the enclosures. This would, however, allow the longer-lived radionuclides to build up in accord with Eq. (8.1). Also, ventilation is generally needed to provide cooling of components and fresh breathing air for workers. Typically, the average residence time of air in accelerator enclosures is limited to a range of between approximately 30 minutes and not much longer than one hour²⁰. Thus, the airborne radionuclides in the accelerator environment, in equilibrium, will have half-lives only up to the order of one hour. The residence time of the air in conjunction with the cross sections determines the radionuclides of importance.

8.2.3 Propagation of Airborne Radionuclides in the Environment

The other consideration concerning airborne radioactivity is that associated with the dose delivered to members of the general public when radionuclides are released to the atmosphere external to the accelerator enclosure. The U. S. Environmental Protection Agency (EPA) has placed an annual limit of 10 mrem on dose equivalent to members of the general public due to the operations of DOE facilities, comparable to limits applied to other facilities, and has also placed stringent regulations on how such releases are to be measured (CFR89). An annual dose equivalent of such small value is usually difficult or impossible to measure at distant locations. Thus, the standard practice is to measure the activity released and then use calculational models to estimate the maximum dose equivalent that actual members of the public could receive. The regulations prescribe the specific computer codes that must be used to perform these calculations through the use of a Gaussian plume model that combines input data on the release of radioactivity with meteorological information. The details of such computer modeling will not be described here. Examples of such plume models are given in textbooks and the results depend on details of the meteorological conditions. A short synopsis is given here.

²⁰ However, at some facilities releases of airborne radionuclides to the outdoors are minimized by greatly restricting the release rate of air during accelerator operations. When personnel accesses are made subsequent to operations, the ventilation rate must then be increased to levels consistent with good industrial hygiene practice. The principles described in this chapter can be used to evaluate the magnitude and radionuclide composition of the air released under these more complex operational conditions.

8.2.3.1 Propagation of Airborne Radioactivity - Tall Stacks

Concentrations of radionuclides at distant locations can be estimated analytically using the so-called **Sutton's equation** to be described shortly. Due to the nature of accelerator operations, only "steady-state" conditions are considered since transient accidental releases from accelerators are unlikely. A good description that applies to rather tall (> 25 m) release points has been presented by Cember (Ce69). Such release points are commonly called **stacks**. More details have been provided by Slade (Sl68). The dispersion is mainly characterized by dilution of the radionuclides and their eventual return to ground level breathing zones. The meteorological conditions of major importance to this topic are illustrated in Fig. 8.1. Relevant **stability classes** have been developed that describe the various possibilities. Descriptions of these stability classes are given in Table 8.3.



Fig. 8.1 Effect of atmospheric temperature gradient or lapse rate on a displaced volume of air for various conditions: a) Unstable lapse rate; b) Stable lapse rate; c) Neutral lapse rate [Reproduced from (Sl68).]

Table 8.3 Atmospheric stability classes for use with Sutton's equation. [Adapted from (Sl68).]

<u>stable</u> :	No heat is gained or lost by a parcel of air that rises and expands adiabatically with falling temperature. The adiabatic cooling with rise normally corresponds to a gradient of about 5.4 °F/1000 ft (1 °C/100 meters) for dry air and about 3.5 °F/1000 ft (0.6 °C/100 meters) for moist air. If the atmospheric temperature gradient is less than adiabatic, but still negative, stability is achieved because a rising parcel cools faster than its surroundings and then tends to sink. A sinking parcel is warmer than its surroundings and thus is less dense and tends to rise. This restricts the width of the plume and consequently decreases dilution.
<u>inversion</u> :	If the temperature gradient is such that the temperature increases with height, then an inversion occurs. Rising effluent from a "stack" becomes much denser than its surroundings and thus sinks. The effluent is thus more limited in its ascent and this, too, serves to limit dilution.
<u>superadiabatic</u> :	If the rate of decrease of temperature with elevation is greater than that in adiabatic conditions, an unstable condition results which promotes the vertical dispersion, and hence dilution. A rising parcel does not cool fast enough due to its expansion and therefore remains warmer and continues to rise. Likewise, a falling parcel continues to fall.

Sutton's equation, as adapted here by Cember (Ce69), for determining the concentration of a short-lived radionuclide released by a *tall* stack, is

$$\overline{c}(x,y) = \frac{2Q}{\pi C^2 \overline{u} x^{2-n}} \exp\left\{-\frac{\lambda}{\overline{u}} \sqrt{x^2 + y^2}\right\} \exp\left\{-\frac{h^2 + y^2}{C^2 x^{2-n}}\right\},$$
(8.8)

where the exponential involving the decay constant λ conservatively allows for radioactive decay in transit for a particular radionuclide. The rest of the quantities are as follows:

(x,y,z) are Cartesian coordinates to the point of measurement from the foot of the stack (meters) where

x is along the centerline of the plume as determined by the wind direction (downwind), y is the transverse coordinate, and z is the vertical coordinate;

 $\overline{c}(x, y)$ is the average concentration (activity m⁻³) at ground level (z = 0);

Q is the emission rate of (activity s⁻¹);

 \overline{u} is the mean wind speed (meters s⁻¹);

C is the virtual diffusion constant in lateral and vertical directions (Table 8.4); *n* is a dimensionless parameter related to the atmospheric conditions (Table 8.4); and *h* is the *effective* chimney height (if the gas has significant emission velocity) determined from the actual chimney height h_a by

$$h = h_a + d\left(\frac{v}{\overline{u}}\right)^{1.4} \left(1 + \frac{\Delta T}{T}\right).$$
(8.9)

In Eq. (8.9) *d* is the outlet diameter (meters), *v* is the exit velocity of the gas (meters s⁻¹), and $\Delta T/T$ is the difference between the temperature of the gas and the ambient outdoor temperature divided by the *absolute* temperature of the gas, *T*. Table 8.4 gives values for certain parameters to be used in Eq. (8.8).

Table 8.4 Diffusion (C^2) and Stability (n) parameters for Cember's version of Sutton's Equation, Eq. (8.8). [Adapted from (Ce69).]

Lapse Rate		C^2					
		Effective (Effective Chimney Height, <i>h</i> , (meters)				
	n	25	50	75	100		
Superadiabatic	0.20	0.043	0.030	0.024	0.015		
Stable	0.25	0.014	0.010	0.008	0.005		
Moderate Inversion	0.33	0.006	0.004	0.003	0.002		
Large Inversion	0.5	0.004	0.003	0.002	0.001		

8.2.3.2 Propagation of Airborne Radioactivity - Short Stacks

The above representation of Sutton's equation is a useful one where tall stacks are involved. However, at typical accelerator facilities it is uncommon for stacks to be very tall. Again for purposes of this discussion, only steady state conditions continuous in time are treated here. For such calculations, the concentration as a function of coordinates, $\overline{c}(x,y,z)$, defined as for the tall stacks, is given by a somewhat different formulation of Sutton's equation which uses the same coordinate system (Sl68);

$$\overline{c}(x, y, z) = \frac{Q}{2\pi\sigma_y \sigma_z \overline{u}} \left\{ \exp\left[-\frac{\lambda}{\overline{u}}\sqrt{x^2 + y^2}\right] \right\} \left\{ \exp\left[-\frac{y^2}{2\sigma_y^2}\right] \right\} \left\{ \exp\left[-\frac{(z-h)^2}{2\sigma_z^2}\right] + \exp\left[-\frac{(z+h)^2}{2\sigma_z^2}\right] \right\}.$$
(8.10)

For the common situation of interest where the receptor location of concern is at ground level (z = 0), this simplifies to

$$\overline{c}(x, y, 0) = \frac{Q}{\pi \sigma_y \sigma_z \overline{u}} \left\{ \exp\left[-\frac{\lambda}{\overline{u}} \sqrt{x^2 + y^2}\right] \right\} \left\{ \exp\left[-\left(\frac{y^2}{2\sigma_y^2} + \frac{h^2}{2\sigma_z^2}\right)\right] \right\}, \quad (8.11)$$

where the presence of the ground as a "barrier" to the flux is taken into account. In these equations, the quantity *h* is effective stack height above the ground in meters and $\sigma_y(x)$ and $\sigma_z(x)$, *implicit* functions of downwind coordinate *x*, are dispersion coefficients that have units of length (meters). All other quantities are the same as given above for tall stacks. These variables are, of course, determined from the meteorological conditions. In Eq. (8.10) and Eq. (8.11), the exponential involving the decay constant λ again *conservatively* allows for radioactive decay in transit for a particular radionuclide.

Table 8.5 gives an alternative scheme for classifying the meteorological conditions. The classification may then be used with the curves in Figs. 8.2 and 8.3 to determine the values of σ_y and σ_z as a function of the coordinate *x* for use in Eqs. (8.10) and (8.11).

Table8.5	Relation of	f turbulence	types	to	weather	conditions.	[Adapted	from
(Sl68).]								

A-Extremely uns	table condition	tions	D-neutra	D-neutral conditions ^a		
B-Moderately un	stable cond	itions	E-Slight	ly stable conditions	S	
C-Slightly unstal	ole condition	ns	F-Mode	rately stable condit	ions	
Surface Wind	Da	ytime insolati	on	Nightime c	conditions	
Speed						
(m/sec)	Strong	Moderate	Slight	Thin overcast	<u><</u> 3/8	
				or <u>></u> 4/8	cloudiness	
				cloudiness ^b		
<2	А	A-B	В			
2	A-B	В	С	Е	F	
4	В	B-C	С	D	E	
6	С	C-D	D	D	D	
>6	С	D	D	D	D	

^aApplicable to heavy overcast, day or night

^bThe degree of cloudiness is defined as that fraction of the sky above the local apparent horizon which is covered by clouds.

Airborne radioactivity releases can be minimized by

- limiting the ventilation rates during operations when people are <u>not</u> present in the enclosure (see footnote, this chapter),
- delaying the actual emissions by requiring long pathways to the ventilation "stacks", and
- minimizing air gaps in the beam.

8.2.4 Radiation Protection Standards for Airborne Radioactivity

The airborne radioactivity is of primary concern to workers who might enter the enclosure to perform maintenance activities and thus are classified as "occupational workers". Since the principal radionuclides are of relative short half-life, the hazard is largely due to the "immersion" in a "cloud" of *external* dose rather than a gaseous ingestion hazard such as might be found in operations involving the processing of long-lived radioactive materials. The latter leads to long-term *internal* radiation exposures. Regulatory authorities, guided by recommendations of the International Commission on



Fig. 8.2 Horizontal diffusion constants, σ_y , as a function of downwind distance, *x*, from the source for turbulence types defined in Table 8.5. [Adapted from (Sl68).]



Fig. 8.3 Vertical diffusion constants, σ_z , as a function of downwind distance, *x*, from the source for turbulence types defined in Table 8.5. [Adapted from (Sl68).]

Radiation Protection (ICRP) and National Council on Radiation Protection and Measurements (NCRP), have established **Derived Air Concentrations** (DACs) for These regulatory standards have supplanted the Maximum radiation workers. **Permissible Concentrations** (MPCs) formerly employed for this purpose that reflected methodologies that have subsequently been updated by the ICRP. DACs, as were MPCs, are based upon the receipt of 5000 mrem of dose equivalent if the entire working year (≈ 2000 hours, or 40 hours weekly) is spent working in a concentration corresponding to "1 DAC". A concentration as large as one DAC is rarely encountered in accelerator radiation environments. Similarly, for members of the general public, values of **Derived** Concentration Guides (DCGs) have been tabulated that would result in the receipt of 100 mrem of dose equivalent by an individual who spent all of the time in one year Table 8.6 gives representative values of these circumstancebreathing such air. dependent maximum concentrations, C_{max} , for accelerator-produced radionuclides in air based upon present U. S. Department of Energy Orders (DOE90) and Regulations (CFR93) along with companion values determined for accelerator-produced radionuclides not included in the cited references that have been calculated by Höfert (Hö69). For some radionuclides commonly found at accelerators, DOE regulations (CFR93) gives two values of DAC, one for air inhaled into the lungs and the other for immersion in an infinite cloud of γ -emitting radionuclides.

	DAC- U. S. DOE Radiation Worker							ral Population ^d
	Inhaled A [50 1 (40 b	ir Exposure ^b mSv y ⁻¹		Immersie [50 mSv y ⁻¹	[1 mSv year ⁻¹ (168 h week ⁻¹)]			
	(40 11	week)]	Infinite Radius Cloud ^b 4 m Radius Cloud ^c					
	$(\mu Ci m^{-3})$	(Bq m ⁻³)	$(\mu Ci m^{-3})$	(Bq m ⁻³)	$(\mu Ci m^{-3})$	(Bq m ⁻³)	$(\mu Ci m^{-3})$	(Bq m ⁻³)
^{3}H	20	8 x 10 ⁵	unlisted	unlisted	unlisted	unlisted	0.1	3.7×10^3
⁷ Be	8	3×10^5	unlisted	unlisted	unlisted	unlisted	0.04	1.5×10^3
¹¹ C	200	6 x 10 ⁶	4	$1 \ge 10^5$	59	2.2×10^{6}	0.02	7.4×10^2
^{13}N	unlisted	unlisted	4	$1 \ge 10^5$	41	$1.5 \ge 10^6$	0.02	7.4×10^2
¹⁵ O	unlisted	unlisted	4	$1 \ge 10^5$	27	$1.0 \ge 10^6$	0.02	7.4×10^2
²² Na	0.3	$1 \ge 10^4$	unlisted	unlisted	unlisted	unlisted	0.001	37
²⁴ Na	2	$8 \ge 10^4$	0.9	$3 \ge 10^4$	unlisted	unlisted	0.004	$1.5 \ge 10^2$
⁴¹ Ar	unlisted	unlisted	3	$1 \ge 10^5$	47	$1.8 \ge 10^6$	0.01	3.7×10^2

Table 8.6 DACs and DCGs (Air) for radiation workers and the general population. These represent maximum concentrations for radionuclide *i*, $C_{max,i}$, depending upon the circumstances of exposure (see text).²¹

Immersion conditions are more likely to be the dominant exposure mechanism due to activated air at accelerators. However, for occupational exposures, the sizes of the "clouds" are not likely to be "infinite" but will be determined by the dimensions of the

²¹ The values in Table 8.6 are, essentially, "worst case" values from the references cited. The user must take care to apply the specific values promulgated by the regulatory authority having jurisdiction. Furthermore, given the primacy of "customary" rather than SI units in United States Regulations, the former is generally taken to be limiting quantity. Also, conversion between the two sets of units in regulatory tables is generally only performed to one significant figure, as reflected here. Where choices needed to be made between day, week, or year exposures, the most restrictive value was taken.

accelerator enclosures. While Höfert's calculations are connected with the obsolete MPCs values, they remain of importance because they recognized that "immersion dose" is highly sensitive to the size of the cloud and that clouds of infinite extent are rare inside buildings at accelerators. Höfert calculated the equivalent of DACs for clouds of various sizes. Table 8.6 gives those for clouds of 4 meters radius that might be typical of an accelerator enclosure. For the general population, Höfert postulated an infinite cloud, since such exposure would presumably occur outdoors. Mixtures of radionuclides are commonly encountered. To account for the presence of multiple radionuclides, the set of individual radionuclide concentrations in the air, C_i , must satisfy the following inequality:

$$\sum_{i} \frac{C_i}{C_{\max,i}} \le 1,\tag{8.12}$$

where $C_{max,i}$ is the regulatory standard for the i^{th} radionuclide, dependent upon the circumstances of the exposure.

8.2.5 Production of Airborne Radionuclides at Electron Accelerators

At electron accelerators, significant air activation will not occur without bremsstrahlung because the nuclear cross sections of *electrons* are about two orders of magnitude smaller than those of *photons* $(Sw79a)^{22}$. This airborne radioactivity is generally short-lived and the concentrations, as shall be seen in what follows, are usually quickly reduced to levels where the exposure rates (R h⁻¹), or equivalently the absorbed dose rates (rads h⁻¹) are small compared to those due to the accelerator components. This result is because the radiation length of air is so much longer than that of any solid material (see Table 1.2).

Swanson (Sw79a) has calculated the saturation activities produced in air normalized to the electron beam power with the results provided in Table 8.7. The results of these calculations are normalized to unit path length and to beam power. To use them to determine the volume specific activity (e.g., Ci cm⁻³) in a given accelerator enclosure, one must multiply the tabulated values by the available **bremsstrahlung path length**²³ and divide by the enclosure volume. The results found in this table were calculated in a manner completely analogous to those given in Table 7.2 for other materials. For energies close to the threshold of an individual reaction, the rise of activity with beam energy, E_o , (see Section 7.3.2 and Fig. 3.7) must be considered. ⁴¹Ar is produced in the thermal neutron capture (n, γ) reaction most copiously where there are high fluences of moderated neutrons present, typically near water-cooled targets and in concrete enclosures. ³H, ¹⁴C, and ⁷Be are too long-lived to be at levels anywhere near saturation and usually do not merit further consideration.

²² The reverse is true for toxic gas production, which occurs by a chemical, rather than nuclear, transformation and whose reaction rate is closely proportional to the integral absorbed dose to the air. Such dose is generally higher if the primary electron beam does not strike a target to produce bremsstrahlung but rather is directly delivered to air. The production of such toxic gases, most notably ozone (O₃) is beyond the scope of this text but has been covered adequately by Swanson (Sw79a).

²³ The available path length would either be set by the physical dimensions of the room or, for a large room, by the attenuation length of the bremsstrahlung radiation in air.

Table 8.7 Saturation activities per unit path length and per unit beam power produced in air by an electron beam normalized to the beam power. "Cross section" ($\Sigma f \sigma$) refers to the integral radionuclide production cross section per MeV of beam energy inclusive of the natural isotopic abundance in air (see Sect. 7.3.3). [Adapted from (Sw79a).]

Produced Radionuclide		Pa	Parent Stable Nuclide		Cross Section, Σfσ	Saturation per Unit Lo Beam P	Activity ength and ower ^a
Nuclide	Half-life	Nuclide	Reaction Type	Threshold (MeV)	(µb MeV ⁻¹)	(MBq m ⁻¹ kW ⁻¹)	(µCi m ⁻¹ kW ⁻¹)
³ H	12.32 y	14 N	$(\gamma,^{3}H)$	22.7	3		
		¹⁶ O	$(\gamma,^{3}H)$	25.0	3	5.2	140
⁷ Be	53.22	^{14}N	(y,sp) ^b	37.8	0.6		
		¹⁶ O	$(\gamma, sp)^{b}$	31.9	0.6	1.11	30
¹¹ C	20.33 min	^{12}C	(γ,n)	18.7	0.011		
		14 N	$(\gamma, sp)^{b}$	22.7	6		
		¹⁶ O	$(\gamma, sp)^{b}$	25.9	6	11	300
^{13}N	9.96 min	¹⁴ N	(γ,n)	10.6	310	520	1.4×10^4
¹⁵ O	2.04 min	¹⁶ O	(γ,n)	15.7	32	55.5	1.5×10^3
¹⁶ N	7.13 s	¹⁸ O	(y,np)	21.8	0.01	0.018	0.5
³⁸ Cl	37.24 min	⁴⁰ Ar	(y,np)	20.6	0.13	0.22	6
³⁹ Cl	55.6 min	⁴⁰ Ar	(γ,p)	12.5	0.86	1.5	40
⁴¹ Ar	1.83 h	⁴⁰ Ar	$(n,\gamma)^{c}$	-	-	variable	variable

^aNormalized per bremsstrahlung pathlength in air (m) and electron beam power (kW) incident on a high-Z target, summed over individual contributing reactions.

^bSpallation reaction

^cThermal neutron capture reaction that where high neutron fluences are moderated by water or concrete shielding.

After calculating the production rates, one can then apply the general methodology presented in this chapter determine the concentrations within the accelerator enclosure and to estimate the effective dose equivalent rates at offsite locations as well as the status of compliance with applicable regulations.

8.2.6 Production of Airborne Radionuclides at Proton Accelerators

At proton accelerators, the excitation functions of the possible nuclear reactions listed in Table 8.2 exemplified by those shown in Fig. 7.9 become important. In general, the positron emitters ¹¹C, ¹³N, ¹⁵O, along with ⁴¹Ar (produced by thermal neutron capture), are the nuclides most frequently seen. Work at Fermilab described by Butala et al. (Bu89) and Vaziri et al. (Va93 and Va96) has also confirmed these identifications and, additionally, detected ³⁸Cl and ³⁹Cl. The determination of the relative contributions of the various positron emitters present must principally be done by fitting measured decay curves with a sum of exponential functions, each term of which represents one of the possible radionuclides present. This is a result of the fact that their γ -ray spectra are all dominated by 0.511 MeV photons from positron annihilation. The results of analysis of such decay curves have been discussed in various references (Th88, Sw90, Bu89, Va93, and Va96). In addition, the production of ³H in the molecular form HTO and its impact should be evaluated.

It was concluded by Butala et al. that the geometry of target stations significantly can affect the composition (Bu89). For example, high intensity targets immediately surrounded with large volumes of iron and concrete (in contact with the iron) produced much less ⁴¹Ar than did other targets where the bulk iron shield was located in a open room with a layer of air between the iron and the concrete. Presumably, the open space provided opportunity for the large flux of low energy neutrons expected external to a pure iron shield (see Section 6.3.5) to "thermalize" and thus enhance the production of ⁴¹Ar in the air space. The large cross section for the ⁴⁰Ar(n, γ)⁴¹Ar reaction at thermal neutron energies ($\sigma_{th} = 660$ mb) also may possibly have provided the photons necessary to enhance the (γ , p) and (γ , pn) reactions required to produce significant quantities of ³⁹Cl and ³⁸Cl, respectively. Some typical percentages of the various radionuclides, by activity concentration, released from high energy proton accelerators are given in Table 8.8.

Table 8.8Measured examples of radionuclide compositions of typical airbornereleases at proton accelerators.

Situation		Radio	onuclides (Activity H	Per Cent)	
	¹¹ C	¹³ N	¹⁵ O	³⁸ Cl	³⁹ Cl	⁴¹ Ar
CERN (Th88) 28 GeV protons	31.0	47.0	8.0			14.0
Fermilab (Bu89) 800 GeV protons						
(no gap between iron and concrete walls)	46.0	19.0	35.0			
(gap between iron and concrete walls)	42.0	14.0	0.0	0.0	10.0	34.0
Fermilab (Va93) 120 GeV protons	58.5	37.9		1.0	1.1	1.5
Fermilab (Va96) 120 GeV protons	64.6	30.5				5

After calculating the production rates, one can then apply the general methodology presented in this chapter to estimate the effective dose equivalent rates as well as the status of compliance with applicable regulations.

8.3 Water and Geological Media Activation

The protection of groundwater resources is a significant public concern that includes the need to assure protection of such valuable resources from contamination with radionuclides. Radioactivity can be produced in soil or rock and in the water it contains. Sometimes the radioactivity produced in water is a matter of concern for occupational workers as well. In practice, it is not always a simple matter to separate these two areas of concern. One can, in principle, initiate calculations of groundwater activation at accelerators by starting from "first principles" and by using the activation equation, Eq. (7.8).

8.3.1 Water Activation at Electron Accelerators

As seen before, questions of radioactivation are generally less complex at electron accelerators. As was done for atmospheric activation and exhibited in Table 8.7, Swanson (Sw79a) has provided the results of calculations to address the production of radionuclides in water at electron accelerators. Such activation will principally occur in water used to cool magnets and beam absorbers and can become a radioactive waste issue. The results are, again, in the form of saturation activities normalized to the electron beam power absorbed in the water volume. Such activities, as before, are for infinite irradiation periods with no time allowed for decay. The results are given in Table 8.9, which also includes the point source specific gamma-ray constants, Γ_i , useful for calculating exposure rates near such water as well as the now obsolete maximum permissible concentrations in water (MPC_w's). From these results, it is clear that, aside from short-lived positron emitters, only ³H and ⁷Be are of importance. Table 8.9 gives the results due to interactions with ¹⁶O found in water. Activity concentrations can be obtained by assuming rapid mixing of the saturated activity in the available volume of water. In principal, ³H could be produced from the hydrogen in water by means of two sequential thermal neutron capture reactions, ${}^{1}H(n, \gamma){}^{2}H$ followed by ${}^{2}H(n, \gamma){}^{3}H$. However this is unimportant due to the fact that the cross sections for both thermal capture reactions involved are fractions of a millibarn.

In practice, due to the compactness of the shielding at electron accelerators compared with that found at proton and ion accelerators, soil activation is generally not as severe a problem at such facilities.

Table 8.9 Saturation activities per unit beam power produced in ¹⁶O by an electron beam normalized to the beam power. "Cross section" refers to the integral radionuclide production cross section per MeV of beam energy (see Sect. 7.3.3). [Adapted from (Sw79a).]

Produced Radionuclide			Reaction Para	meters Specific Gammy Ray Constant, Γ		Satura Activity p Beam H	ation per Unit Power	
	Half-life	Reaction	Threshold (MeV)	Cross Section, σ (μb MeV ⁻¹)	(mGy h ⁻¹) x(GBq m ⁻²) ⁻¹	(rad h ⁻¹) x (Ci m ⁻²) ⁻¹	(GBq kW ⁻¹)	(Ci kW ⁻¹)
³ H ^a	12.32 у	$(\gamma,^{3}H)$	25.0	1.5	-	-	7.4	0.2
⁷ Be	53.22 d	(y,5n4p)	31.9	0.3	0.008	0.03	1.5	0.04
^{10}C	19.26 s	(y,4n2p)	38.1	1	0.29	1.06	3.7	0.1
¹¹ C	20.33 min	(y,3n2p)	25.9	3	0.17	0.62	14.8	0.4
^{13}N	9.96 min	(y,2np)	25.0	0.9	0.17	0.62	3.7	0.1
14 O	1.18 min	(y,2n)	28.9	1	0.45	1.7	3.7	0.1
¹⁵ O	2.04 min	(γ,n)	15.7	75	0.17	0.62	330	9

^aDoes not present an external radiation hazard.

8.3.2 Water and Geological Media Activation at Proton Accelerators

8.3.2.1 Water Activation

At proton and ion accelerators, as with electron accelerators, radioactivity can be produced directly in water as a result of both proton and neutron interactions. Values for some of the relevant cross sections were given in Chapter 7. Equipped with knowledge of the beam energy and information about the energy spectra of neutrons that are present, one can proceed to calculate the activity produced. In general, the most important radionuclides, as is the situation with electron accelerators, result from the interactions of the hadrons with the oxygen present in the water. As before, the production of ³H from the hydrogen present in the water is possible, but is rendered sufficiently improbable due to the small cross sections of both of the thermal neutron capture reactions required to occur sequentially. For such calculations, the production of ³H in water from atoms other than hydrogen is of special importance. Published experimental data of ³H production reactions is surprisingly scarce. Konobeyev and Korovin (Ko93) have developed a method of globally fitting the existing cross section data on the production of ³H due to neutron interactions with a variety of target elements found in soils with the results shown in Fig. 8.4. The results for protons are similar.

8.3.2.2 Geological Media Activation

While calculating the production of radionuclides in soil, and in the water it contains, directly from known cross sections has an appeal due to its simplicity, in practice such calculations have been done more frequently by analyzing results obtained using irradiated samples. The work of Borak et al. (Bo72) is of singular importance in this regard. Borak et al. measured the radioactivity produced in soil by high energy hadrons by radiochemical analysis of soil samples irradiated near high energy synchrotrons; the 12 GeV Argonne ZGS and the 28 GeV Brookhaven AGS. The radionuclides ³H, ⁷Be, ²²Na, ⁴⁵Ca, ⁴⁶Sc, ⁴⁸V, ⁵¹Cr, ⁵⁴Mn, ⁵⁵Fe, ⁵⁹Fe, and ⁶⁰Co were identified. Experiments were then performed to determine which radionuclides, and what fractions of them, could be leached by water. This study determined macroscopic production cross sections and ion velocities relative to ground water flow in soil. Of these nuclides, only ³H, ²²Na, ⁴⁵Ca, and ⁵⁴Mn were observed in leach waters. The ³H was assumed to be all leachable and was measured by driving it out of the sample by baking. Radionuclides with half-lives exceeding 15 days were the only ones considered. The results were based upon the elemental composition of soil given in Table 8.10.



Fig. 8.4 Cross sections for the production of ³H due to neutron bombardment of materials commonly found in soil and rock as a function of neutron energy. The calculations have been performed following the method of Konobeyev and Korovin (Ko93). Results for aluminum are quite similar to those found for silicon and the results for sodium are quite similar to those found for magnesium.

	Elemental Composition of So	il [*]
Element	Z, Atomic Number	% by Weight
Silicon	14	14.47
Aluminum	13	2.44
Iron	26	1.11
Calcium	20	7
Magnesium	12	3.79
Carbon	6	5.12
Sodium	11	0.34
Potassium	19	0.814
Oxygen	8	≈ 64

Table 8.10Composition of soils typical of the Fermilab site.[Adapted from(Bo72).]

^{*}The mean moisture percentage was 13.15 ± 4.45 % and the mean pH was 7.6 ± 0.1 .

Borak et al. measured specific activities at saturation, A_i , (Bq g⁻¹) which are related to the microscopic cross sections by means of the following equation:

$$A_i = \phi \sum_j n_j \sigma_{ij} , \qquad (8.13)$$

where ϕ is the flux density (cm⁻² s⁻¹), n_j is the number density of target nuclei of the *j*th nuclide (g⁻¹) of the soil sample, and σ_{ij} (cm²) is the effective cross section for the transformation from target nucleus *j* to radionuclide *i*. The summation is taken over the soil constituents. Borak et al. were able to directly measure the summations on the right hand side of Eq (8.13). These summations are the total **macroscopic cross sections** summed over the soil constituents for each radionuclides of interest. Table 8.11 gives the results of the measurements of the macroscopic cross sections, denoted Σ (cm² g⁻¹), for each of the radionuclides identified in the various types of soils analyzed.

Glacial Till Gray Sandy Clay Red Sandy Clay Grav Clav Nuclide Σ (cm² g⁻¹) Σ (cm² g⁻¹) Σ (cm² g⁻¹) Σ (cm² g⁻¹) 2.9 x 10⁻⁴ 2.7 x 10⁻⁴ ⁷Be 3.7 x 10⁻⁴ 3.2 x 10⁻⁴ ⁵¹Cr 1.7 x 10⁻⁵ 3.7 x 10⁻⁵ 2.8 x 10⁻⁵ 3.1 x 10⁻⁵ ²²Na 2.1 x 10⁻⁴ 2.3 x 10⁻⁴ 2.0×10^{-4} $1.6 \ge 10^{-4}$ ^{54}Mn 5.9 x 10⁻⁵ 4.1×10^{-5} 3.5 x 10⁻⁵ 3.7×10^{-5} ⁴⁶Sc 3.0×10^{-5} 1.3×10^{-5} 9.6 x 10⁻⁶ $1.1 \ge 10^{-5}$ ^{48}V 1.1 x 10⁻⁵ 6.7 x 10⁻⁶ 7.4 x 10⁻⁶ 4.1 x 10⁻⁶ ⁵⁵Fe 1.2 x 10⁻⁴ 7.0 x 10⁻⁵ 2.1 x 10⁻⁴ 9.3 x 10⁻⁵ ⁵⁹Fe 3.2 x 10⁻⁶ 1.7 x 10⁻⁶ 1.3 x 10⁻⁶ 1.6 x 10⁻⁶ ⁶⁰Co 3.3 x 10⁻⁵ 1.4 x 10⁻⁵ 1.1 x 10⁻⁵ 1.3 x 10⁻⁵ ⁴⁵Ca 2.0 x 10⁻⁵ 1.6 x 10⁻⁵ 1.6×10^{-4} $3.0 \ge 10^{-5}$ ^{3}H 8.2 x 10⁻⁴ 1.1 x 10⁻³ 3.3 x 10⁻⁴ 5.2 x 10⁻⁴ 5.9 x 10⁻³ 5.9 x 10⁻³ $^{3}H*$ 4.1 x 10⁻³ 4.4 x 10⁻³

Table 8.11Macroscopic cross section for soil normalized to unit flux of hadronswith kinetic energies greater than 30 MeV. [Adapted from (Bo72).]

*Cross sections per gram of water in soil.

Borak et al. also obtained data related to the **leachabilities** of the various elements from the soils studied. Leachability measures the ability of water to remove a given radionuclide from the soil material. It is not related to nuclear properties but rather is related to chemical properties and processes such as ion exchange. The results were reported by Borak et al. as follows:

- ³H: The leaching process was able to collect all the tritium as measured by a bake-out process. The average value of the macroscopic cross section in soil was found to be 5.1×10^{-3} cm² g⁻¹ of water. An important conclusion is that the tritium will migrate with the same velocity as any other water in the soil.
- ²²Na: Typically 10-20 % of this nuclide was found to be leachable. On average, it appeared that the migration velocity of this nuclide is approximately 40% of that of water through the soil due to ion exchange processes.
- ⁴⁵Ca: At most 5 % of this nuclide was leached from the soil. The migration velocity was determined to be extremely small.
- ⁵⁴Mn: At most 2 % of this nuclide was leached from the soil. It was determined that this nuclide will not migrate significant distances.

Thus, based upon leachability considerations, ³H and ²²Na are thus the most important leachable radionuclides that can be produced in environmental media such as soil.

One can thus calculate the quantities of radionuclides that might pose a risk to groundwater in the environs of an accelerator. This can be done by using the cross sections directly, or, as demonstrated by Gollon (Go78) for high energy protons, by performing, for example, Monte Carlo calculations in which the total stars (i.e. total inelastic nuclear interactions above some threshold) produced in some volume of earth shielding are determined²⁴. As in Eq. (7.35), the total number of atoms, K_i , of the *i*th nuclide that can be produced per star in that same volume is given by

$$K_i = \frac{\Sigma_i}{\Sigma_{in}},\tag{8.14}$$

where Σ_i is, as above, the macroscopic cross section (cm² g⁻¹) for the *i*th radionuclide and Σ_{in} is the total macroscopic inelastic cross section (cm² g⁻¹) for soil. Gollon inferred a value of $\Sigma_{in} = 1.1 \times 10^{-2} \text{ cm}^2 \text{ g}^{-1}$ for soil from the results of Borak et al.

²⁴ Some Monte Carlo codes of more recent development can now calculate these quantities directly from the energy-dependent production cross sections. However, given the limited energy dependence at high energies, working with the total stars remains worthwhile as a means to achieve results rapidly, or as a "quality check" on the more complex computations.

Gollon used the following values of K_i for ³H and ²²Na, respectively, as selected from Borak's paper for soils peculiar to Fermilab (glacial till):

$$K_3 = \frac{8.2 \times 10^{-4}}{1.1 \times 10^{-2}} = 0.075$$
, and (8.15a)

$$K_{22} = \frac{2.1 \times 10^{-4}}{1.1 \times 10^{-2}} = 0.020.$$
(8.15b)

One can then calculate the total number of atoms of radionuclides produced during some time interval in some volume by simply multiplying these factors by the number of stars (or inelastic interactions) in the same volume. The number of atoms then can be converted to activity using the decay constant. The above values of K_i are applicable to soils such as those found at Fermilab. For other soil compositions one may need to use cross sections for producing the radionuclides of interest in various target elements and integrate over the energy spectrum of incident hadrons. Figure 8.5 gives cross sections for producing 22 Na by interactions of hadrons with the various elements comprising soil due to Van Ginneken (Va71). This figure is a companion to Fig 8.4.

8.3.3 Regulatory Standards

The quantity of ultimate concern, of course, is the resultant concentration in water. The water could be an actual or potential drinking water resource that might well be subject to specific regulatory requirements. The regulations may differ between different governing jurisdictions. The requirements, generally not developed for application to the operations of particle accelerators, need to be understood by facility management personnel. The standards can differ for drinking water supplies and surface water discharges. The allowable concentrations for surface waters may be larger due to the likelihood that such discharges will most certainly be diluted significantly prior to the consumption by individuals. However, in some jurisdictions, this may not be the case. For public drinking water supplies, the U. S. Environmental Protection Agency (CFR76, reaffirmed in CFR00) limits such concentrations to those that would produce an annual dose equivalent of 4 mrem and specifically gives a limit of 20 pCi cm⁻³ for tritium. An explicit limit for ²²Na is not specified by USEPA. For surface water discharges, the U. S. Department of Energy (DOE90) has set forth Derived Concentration Guides, values of concentrations which would result in members of the public each receiving no more than 100 mrem yr⁻¹ should they use such water for their household needs. The DOE DCGs are based upon a more up-to-date dosimetry methodology that results in values of 80 pCi cm⁻³ for ³H and 0.4 pCi cm⁻³ for ²²Na in drinking water. However, EPA's explicit limit for ³H in drinking water is considered to be legally preeminent. Table 8.12 lists these concentration limits, $C_{max,i}$. For purposes of this discussion, surface water discharges include those to streams, ponds, etc. while drinking water standards apply to water that could potentially end up in a source of drinking water such as a public, or even private, well. Local jurisdictions can, and in some cases have, applied drinking water standards to all discharges.



Fig. 8.5 Cross sections for the production of ²²Na due to neutron bombardment of materials commonly found in soil and rock as a function of neutron energy. Results for potassium are quite similar to those found for calcium. [Adapted from (Va71).]

Half-Life (years)	Concentration Limit, C _{max,i} (pCi cm ⁻³)				
	Surface Water	Drinking Water			
12.32	2000^{a}	20^{b}			
2.603	10 ^a	0.4^{a}			
	Half-Life (years) 12.32 2.603	Half-Life (years)Concentration Lin Surface Water12.322000°2.60310°			

 Table 8.12 Concentration Limits for ³H and ²²Na in surface water discharges and in drinking water.

^aValue taken from (DOE90)

^bValue taken from (CFR76, CFR00). A value of 80 pCi cm⁻³ is implied by (DOE90).

In exact analogy with the situation found with airborne radioactivity (Eq. 8.12), to account for the presence of multiple radionuclides, the set of radionuclide concentrations in the water, C_i , must satisfy the following inequality, where $C_{max,i}$ is the regulatory standard for the *i*th radionuclide for the particular circumstances of exposure:

$$\sum_{i} \frac{C_i}{C_{\max,i}} \le 1$$
(8.16)

8.3.4 The Propagation of Radionuclides Through Geological Media

The methods for calculating these concentrations in actual environmental media will vary with the regulatory authority and the "conservatism" of the institution. The most conservative assumption is to assume that saturation concentration values of production are reached. This is equivalent to assuming that the accelerator will operate "forever" in a static configuration and that the water in its vicinity never moves. This assumption is an extremely unrealistic one as it is questionable that the "motionless" water in such a medium actually comprises a potential source of useable drinking water. For an irradiation over a finite period of time, the activity concentration C_i of radionuclide *i* in leaching water under such conditions can be calculated by means of following formula:

$$C_{i} = \frac{N_{p}K_{i}L_{i}S_{ave}}{1.17 \times 10^{6} \rho w_{i}} \{1 - \exp(-t_{irrad} / \tau_{i})\} \exp(-t_{c} / \tau_{i}) \text{ (pCi cm}^{-3}), \qquad (8.17)$$

where,

 N_p is the number if incident particles delivered per year,

 K_i is as above,

 L_i is the fraction of the radionuclide of interest that is leachable,

- S_{ave} is the average star density (stars cm⁻³) in the volume of interest per incident particle,
- ρ is the density of the medium (g cm⁻³),
- w_i is the mass (grams) of water per unit mass (grams) of medium required to leach some specified fraction of the leachable radioactivity and is thus linked to the value of L_i .

 t_{irrad} is the irradiation time,

 t_c is the "cooling" time once the irradiation is suspended, and

 τ_i is the mean-life of the *i*th radionuclide.

The constant in the denominator contains the unit conversions needed to yield results in pCi cm⁻³. For a given medium, the ratio L_i/w_i should be determined by measurements specific to the local media. An important quantity is the **effective porosity**, *p*, which represents the volume fraction of the material that is available to water movement. It is given by

$$p = \rho w_i. \tag{8.18}$$

The effective porosity is essentially equal to the pore volume of the material for soils but for consolidated materials (i.e., rock) it does not include sealed pores through which movement does not occur. This provides a means by which "worst case" estimates may be made. For realistic estimates some method of taking into account water movement must be used.

At Fermilab, a simple model allowing for some movement and further dilution of water was employed for many years (Go78). In this model, called the single resident model for reasons that are obvious, the vertical migration of water was assumed to be 2.2 m yr⁻¹. In the standard clays present at Fermilab, this velocity is likely conservative (i.e., large) by at least an order of magnitude. Its use crudely allowed for the presence of cracks and fissures through which more rapid propagation of water might be possible. The tritium vertical velocity was taken to have this value while the results obtained by Borak et al. (Bo72) were used to obtain a lesser value of about 1.0 m yr⁻¹ for ²²Na. Only the leachable fraction of the ²²Na is included. The procedure then allowed for decay during the downward migration of the total inventory of radionuclides produced in one year, integrated over the entire volume of the irradiated material, to the highest aquifer below the location of the irradiation. At that point, it was assumed that the radionuclides were rapidly transported horizontally to a shallow well where it was presumed that the flow of water collecting the radionuclides is entirely used by a single user who consumes a volume of 150 liters per day. This value, a minimal one, was taken from results achieved by municipalities that have needed to ration public water consumption during conditions of severe drought. Thus the annual production, as transported vertically, was diluted into the 5.5 x 10^7 cm³ yr⁻¹ that this represents. This simple model is generally conservative but it does, in fact, neglect that fact that the water movement may not be uniform from year-to-year. It also did not take advantage of the fact that the radionuclides are initially distributed over a considerable volume as they are produced.

It is clear that better methods are warranted and a better model has been developed for use at Fermilab (Ma93). The **concentration model** now in use at Fermilab calculates the production of the radionuclides of concern in accordance with Eq. (8.17). Variations of this approach are used at most large accelerators. The result, then, provides an initial concentration that is available for further migration, decay, and dilution. The concentration after migration is then calculated by using up-to-date modeling techniques to calculate the reduction in the concentration due to dilution, diffusion, and radioactive decay. At the point of concern, usually the location of an aquifer producing water suitable for consumption as a supply of drinking water, the concentrations calculated are then substituted into Eq. (8.16) in order to determine if a shielding design is adequate.

To do these calculations properly requires a detailed knowledge of the media involved. Some principles will be given here but many details are left to the references [(Fe88), (Ba98), and (An07)]. In situations where a definite potential gradient, often called the **hydraulic gradient**, dh/dx, is applied to water in a medium, the rate of flow is said to be **advective**. Under such conditions and in situations where only one dimensional coordinate is important, the average linear velocity (or seepage velocity), *v*, is given by the application of **Darcy's Law** as (Fe88);

$$v = \frac{K}{p} \frac{dh}{dx},\tag{8.19}$$

where p, the effective porosity, is defined as above. More complicated situations involving two and three dimensions are addressable using the mathematical language of vector calculus. The derivative is the gradient of the **hydraulic head** in the material. K in this equation represents the **hydraulic conductivity**. This quantity is a function of the material and its moisture content. All of the factors in this equation can, and generally should, be determined empirically for the medium and location under consideration. Typical values of K are given in Table 8.13 and have been given by Batu (Ba98).

Group	Porous Materials	Range of K values
		$(cm s^{-1})$
Igneous Rocks	Weathered granite	$(3.3 - 52) \ge 10^{-4}$
	Weathered gabbro	$(0.5 - 3.8) \ge 10^{-4}$
	Basalt	$(0.2 - 4250) \ge 10^{-6}$
Sedimentary Materials	Sandstone (fine)	$(0.5 - 2250) \ge 10^{-6}$
	Siltstone	$(0.1 - 142) \ge 10^{-8}$
	Sand (fine)	$(0.2 - 189) \ge 10^{-4}$
	Sand (medium)	(0.9-567) x 10 ⁻⁴
	Sand (coarse)	(0.9-6610) x 10 ⁻⁴
	Limestone and dolomite	$(0.4 - 2000) \ge 10^{-7}$
	Karst limestone	(1-20000) x 10 ⁻⁴
	Gravel	$(0.3 - 31.2) \ge 10^{-1}$
	Silt	$(0.09-7090) \ge 10^{-7}$
	Clay	0.1 - 47) x 10 ⁻⁸
Metamorphic Rocks	Schist	(0.002 - 1130) x 10 ⁻⁶

Table 8.13 Examples of typical values of hydraulic conductivity.[Adapted from (Ba98).]

Darcy's Law can, then, be used to determine the rate of migration of a contaminant, in this case, radioactivity, from one point to another. During the time of migration, the concentration would be *decreased* by radioactive decay while possibly being *increased* by any ongoing radioactivation. One often encounters the problem of calculating the concentration of radionuclides at some location as a function of time during, or after, a period of irradiation comparable to the mean-lives of the radionuclides of concerns. At a given location in such a medium, denoted by the coordinate x, one needs to solve the following continuity equation that can be thought of as an extension of Eq. (7.4), for situations where the velocity of water movement, v, can be thought of as slowly varying or a constant over time and some volume of space:

$$\frac{\partial C_i}{\partial t} + v \frac{\partial C_i}{\partial x} + \lambda_i C_i(x,t) = \frac{L_i}{w'_i} Q_i(x,t), \qquad (8.20)$$

where all variables are as in Eq. (8.17) with the refinements that λ_i is the decay constant of the *i*th radionuclide, *x* is the spatial coordinate, *t* is the time, w'_i is the water content of the media per unit volume of media. The quantity $Q_i(x,t)$ represents the production of the *i*th radionuclide and is equivalent to the factor $N_p S_{ave}/(1.17 \times 10^6 p)$ in Eq. (8.17). It includes any time-dependence in the delivery of beam. The middle term in the left-hand side of the equation takes care of movement from a point of one concentration to another at the seepage velocity *v*. As seen elsewhere in this text, one can commonly describe the spatial dependence of the production factor in a thick shield as an exponential function;

$$Q_i(x,t) = Q_{oi}(t) \exp(-\xi x).$$
 (8.21)

Mokhov (Mo97) has solved this equation for the typical initial conditions of $C_i(x,0)=0$ and $x \ge 0$, $t \ge 0$.

In general, $C_i(x,t) = \frac{L_i}{w_i} \int_0^t dt' Q_i(x - vt', t') \exp(-\lambda t'), \qquad (8.22)$

and for an exponential spatial dependence as in Eq. (8.21) this becomes:

$$C_i(x,t) = Q_{oi}(t) \frac{L_i}{w_i} \frac{1}{\eta_i} \exp(-\xi x) [\exp(\eta_i \tau) - 1],$$

with

$$\eta_i = \xi_v - \lambda_i,$$

$$\tau = t \text{ for } t < x/v, \text{ and}$$

$$\tau = x/v \text{ for } t \ge x/v.$$
(8.23)

 $C_i(x,t)$ has a maximum at $x_{i,\max}$ given by,

$$x_{i,\max} = -\frac{v}{\lambda_i} \frac{\ln\left(\frac{\xi v}{\lambda_i}\right)}{1 - \frac{\xi v}{\lambda_i}}.$$
(8.24)

In using these results, one must take care that the algebraic signs of the coordinates x relative to that of v are properly taken into account. In situations where the seepage velocity is extremely slow, **diffusion** becomes the dominant mechanism for water flow and dilution. Mathematically, a second partial derivative with respect to the spatial coordinate is added to Eq. (8.20). Examples are provided by Fetter (Fe88). Computer software has been written to address this topic such as the one produced by Sudicky et al. (Su88).

As a further example of methodologies that can be employed in solving such problems, Jackson (Ja87) has estimated the dilution for a shallow uncased well in an aquifer a distance, r, from a beam loss point also in the aquifer. The loss point was assumed to be within the drawdown zone of the well. This was performed for a simple geology that involved a single uniform stratum of earth above some level of impervious stratum. Fig. 8.6 shows the situation described by this model. Here, a given well is modeled by using the profile of the depth of water, h(r), as a function of r. h(r) is determined by the depth of a test well at radius, r, from the well under consideration and represents the hydraulic potential. The well is assumed to supply a volume, Q, of water per day. The flux of water is determined by the gradient relation, equivalent to Darcy's Law;

$$S_r = k \frac{dh(r)}{dr} , \qquad (8.25)$$

where S_r is the inward flux at radius r and k is a constant with dimensions of volume per unit time per unit area and is characteristic of the soil. Conservation of water yields the steady-state equation;

$$Q = 2\pi r h(r) S_r = 2\pi r k h \frac{dh}{dr} = \pi k \frac{d(h^2)}{d(\ln r)}.$$
(8.26)

The quantity $2\pi rh \frac{dh}{dr}$ corresponds to the rate of change of volume of the cylindrical shell of height, *h*, (i.e., the hydraulic head) with respect to *r*. This equation has the solution;

$$Q\ln\left(\frac{r}{r_o}\right) = \pi k \left\{h^2(r) - h_o^2\right\},\tag{8.27}$$

where r_o is the radius of the well and h_o is the height of water above the impervious stratum at the well. If *H* is the depth of the impervious layer below the water table in a asymptotic region unperturbed by any wells, the radius of influence *R* of the well can be defined by the relation;

$$\ln\frac{R}{r_o} = \frac{\pi k \left\{ H^2 - h_o^2 \right\}}{Q}.$$
 (8.28)



Fig. 8.6 Hydrogeological model of a shallow well in proximity to an accelerator tunnel where a beam loss occurs. The radioactivated region is represented in cross section by the cross-hatched rectangle to the right. h represents the elevation of the water table above the impervious stratum as a function of r while the water table is a distance H above the impervious stratum where the water table is not perturbed by wells. [Adapted from (Ja87).]

However, the detailed solution is not necessary. Suppose that there is a well a distance r away from the region of deposition of radioactivity near an accelerator. One also assumes that the activation zone lies below the water table and that the deposition region lies within the radius of influence of the well. This assumption leads to higher concentrations than would be obtained if the activation zone were totally, or partially, above the water table. The amount of activity drawn into the well is determined by the rate of pumping Q and the necessary total flow through a cylinder of radius r and height h(r) as we have seen. Let ΔV be the volume of soil yielding Q gallons of water. The cylindrical shell providing this amount of water will be of radial thickness Δr , where $\Delta V = 2\pi rh(r)\Delta r$. The fraction F of the volume of activity included in this shell can be said to be given by:

$$F = \frac{\Delta r}{t} = \frac{2\pi \ rh\Delta r}{2\pi \ rht} = \frac{\Delta V}{2\pi \ rht} , \qquad (8.29)$$

provided that $\Delta r < t$.

If the activated region contains leachable activity, A (either total activity or that of a particular radionuclide of interest), the corresponding specific activity, a, in water drawn from the well is thus given by

$$a = F \frac{A}{Q} = F \frac{A}{p\Delta V} = \left[\frac{\Delta V}{2\pi r h t}\right] \frac{1}{p} \left[\frac{1}{\Delta V}\right] A = \frac{1}{2\pi r t D} \frac{f}{p} A, \qquad (8.30)$$

where f = D/h is the fraction of the total height of the cylindrical shell occupied by the activated region and p is the effective porosity of the soil. The pumping volume Q is implicit in f. Porosity values vary considerably but in general are in the range of

$$0.2$$

Thus, this formula may be used to obtain an estimate of the specific activity as a function of distance from the well, although it is perhaps not too useful for applications to beam losses far from the well. By definition, $f \leq 1$ and the lower value of porosity can be used to obtain upper limit estimates of the concentration. It must be emphasized that this model depends upon uniformity of water conduction by the strata. The presence of cracks, voids, so-called "sand lenses", or more complex geological strata can, of course, provide much more rapid movement that is not well-described by this simple model.

Problems

- 1. A 20 m long air gap has a beam of 10^{12} s⁻¹ of high energy protons passing through it. First, calculate the production rate of ¹¹C in the gap at equilibrium if one approximates air in the gap by nitrogen and assumes σ (¹¹C) = 10 mb. Assume that there are no significant losses of beam by interaction after checking to see that this assumption is, in fact, true. Table 1.2 contains helpful information.
 - a) If the air gap is in a 10 x 10 x 20 meter³ enclosure with <u>no</u> ventilation, calculate the equilibrium concentration of ¹¹C in the room (in units of μ Ci m⁻³) assuming extremely rapid mixing (i.e., no time allowed for decay while mixing occurs) of the enclosed air. Compare the concentration with the derived air concentration values in Table 8.6 and calculate, using simple scaling, the dose equivalent to a worker who spends full time in this room. (This is a purely hypothetical scenario due to the much larger hazards due to such an intense direct beam!)
 - b) Calculate the concentration if two (2) air changes hr^{-1} are provided.
 - c) Assume the exhaust of the ventilation described in part "b" is through a 10 cm radius stack 25 m tall. Calculate the air speed in the stack, and the emission rate in Ci s⁻¹. Then using Cember's version of Sutton's equation for tall stacks to estimate the concentration directly downwind at ground level, and hence the dose equivalent 1 km away with moderately stable meteorological conditions and an average wind speed of 10 km hr⁻¹.
 - d) Perform the same calculation requested in "c" using the more general version of Sutton's equation appropriate to short stacks and assume the stack height to be 3 meters. All other conditions of the problems are the same as in "c".
- 2. In soil conditions similar to those at Fermilab, a volume of soil around a beam absorber approximately 10 m wide by 10 m high by 20 m long is the scene of a star production rate (averaged over the year) of 0.02 stars proton⁻¹ at a beam intensity of 10^{12} protons s⁻¹.
 - a) Calculate the annual production of ³H ($t_{1/2} = 12.3$ years), the saturated activity (in Bq & Ci), and the average saturated specific activity in the above volume's water (assume 10% water content by volume).
 - b) Use the older Fermilab single residence model to calculate the concentration at the nearest well. Assume the activation region (beam loss point) is 50 m above the aquifer and the usual migration velocities.
 - c) "Conservatively" apply the "Jackson Model" to estimate the concentration at a well 100 meters distant from the center of the activation region.

3. The method of accounting for ventilation presented in Section 8.2.2 can readily be generalized to include other mechanisms which "remove" airborne radionuclides such as absorption, filtration, etc. Assume that an arbitrary total number "j" of such mechanisms are present and that the irradiation has gone on sufficiently long to have come to equilibrium between the production of radionuclides and all modes of removal. Following termination of the irradiation, determine the fraction of the total activity that is removed from the air volume by each of the "j" mechanisms. It is safe to assume that all the atoms of the radionuclide produced are removed by one of the processes. The solution of this problem has some importance for the more long-lived radionuclides for it leads to a method of estimating the total activity expected to be found on, say, filter media.

9.1 Introduction

In this chapter instruments and dosimeters currently used in the environment of particle accelerators to measure and characterize the radiation fields are discussed. The emphasis here is on instrumentation that addresses those aspects of accelerator radiation fields that pose special problems that are somewhat unique to this branch of radiation protection. Thomas and Stevenson (Th88) and Swanson and Thomas (Sw90) also discuss these matters. Cember (Ce69) has also described the basics of radiation measurement instrumentation quite well. Knoll (Kn79) has written an excellent detailed treatise on this subject. Virtually all particle detection techniques that have been devised by physicists have to some degree been employed in radiation measurements at accelerators. Furthermore, the specialized instruments used to characterize the accelerator radiation fields are commonly found to be of use to the researcher in the understanding of experiment "backgrounds". The radiation protection practitioner needs to be able to astutely determine which techniques, including those in use in the physics experiments, can be applied to problems of practical interest in radiation protection.

9.2 Counting Statistics

Many of the detection techniques employed to measure radiation fields are directly, or indirectly, dependent upon the counting of individual events such as the passage of charged particles through some medium or the decay of some particle or radionuclide. Cember (Ce69) has given a good summary of **counting statistics** that is largely repeated here. Radioactive decays are randomly occurring events having a sampling distribution that is correctly described by the **binomial distribution** given by the following expansion:

$$(p+q)^{n} = p^{n} + np^{n-1}q + \frac{n(n-1)}{2!}p^{n-2}q^{2} + \frac{n(n-1)(n-2)}{3!}p^{n-3}q^{3} + \dots +, \quad (9.1)$$

where p is the mean probability for occurrence of an event, q is the mean probability of non-occurrence of the event so that p + q = 1, and n is the number of chances of occurrence. The probability of exactly n events occurring is given by the first term, the probability of (n - 1) events is given by the second term, etc. For example, in the throwing of a dice, the probability of throwing a "one" is 1/6 and the probability of throwing a "one" 3 times in a row (n = 3) is

$$p^n = (1/6)^3 = 1/216. (9.2)$$

In three throws, the probabilities of throwing 2 "ones", 1 "one" and no "ones" are given by the 2^{nd} , 3^{rd} , and 4^{th} terms of the expansion; 15/216, 75/216, and 125/216, respectively.

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This distribution becomes essentially equivalent to the **normal or Gaussian distribution** when n has an approximate value of at least 30. The Gaussian distribution is as follows:

$$p(n) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left[-(n-\overline{n})^2 / (2\sigma^2)\right], \qquad (9.3)$$

where p(n) is the probability of finding exactly n, \overline{n} is the mean value, and σ in this context is the standard deviation and not a reaction cross section.

Radioactive decays or particle reactions can often be characterized as highly improbable events. For such "rare" events, the binomial distribution approaches the **Poisson distribution**. In this distribution, the probability of obtaining *n* events if the mean value is \overline{n} , is given by

$$p(n) = \frac{\left(\overline{n}\right)^n \mathrm{e}^{-\overline{n}}}{n!} \,. \tag{9.4}$$

For example consider $10^{-3} \ \mu\text{Ci}$ of activity. For this, $\overline{n} = 37$ decays sec⁻¹. The probability of exactly observing this number of events in any one second is

$$p(37) = \frac{(37)^{37} e^{-37}}{37!}.$$
(9.5)

One can apply Stirling's approximation to evaluate the factorial;

$$n! = \sqrt{2\pi n} \left(\frac{n}{e}\right)^n,\tag{9.6}$$

where *e* is the Naperian base (e = 2.718...). Thus p(37) = 0.066. As in the case of the normal distribution, 68 % of the events would lie within one standard deviation of the mean, 96 % of the events would lie within 2 standard deviations of the mean, etc. For the Poisson distribution, the **standard deviation** is given by

$$\sigma = \sqrt{n} . \tag{9.7}$$

The relative error, σ/n , is thus $\sqrt[n]{n}$.

Often, when dealing with instrumentation, the **counting rate** is involved. For this quantity the following holds:

$$r \pm \sigma_r = \frac{n}{t} \pm \frac{\sqrt{n}}{t}, \qquad (9.8)$$

where r is the counting rate per unit time, σ_r is its standard deviation, and t is the counting time during which the rate is measured. The quantity t, for example, could even be the integration time constant of some instrument. It follows that

$$\sigma_r = \frac{\sqrt{n}}{t} = \sqrt{\frac{n}{t} \cdot \frac{1}{t}} = \sqrt{\frac{r}{t}}.$$
(9.9)

Usually, counts due to various background radiations are present and must be dealt with. The standard deviation of the **net counting rate** is

$$\sigma_n = \sqrt{\sigma_g^2 + \sigma_{bg}^2} = \sqrt{\frac{r_g}{t_g} + \frac{r_{bg}}{t_{bg}}} \quad , \tag{9.10}$$

where the subscripts g refer to the measurement of the **gross counting rate** while the subscripts bg refer to the measurement of the **background counting rate**. The time durations of the measurements of the rates r_g , and r_{bg} are t_g and t_{bg} , respectively. In general, the common statistical tests are valid for Poisson statistics.

Another quantity that sometimes becomes important is the **resolving time**, or **dead time**, of an instrument. This is the time that the detector, following an event, is incapable of measuring a second event. It is a function of both electronic characteristics and the physical process inherent in the detection mechanism. It can be measured by exposure to two different sources of radiation. In such a measurement, a certain detector has a measured background rate of R_{bg} and responds to first source alone with a rate R_1 and to the second source alone with a rate R_2 where both R_1 and R_2 include the background. When exposed to the two sources simultaneously, the measured rate is R_{12} . The resolving time, τ , is given by (Ce69);

$$\tau = \frac{R_1 + R_2 - R_{12} - R_{bg}}{R_{12}^2 - R_1^2 - R_2^2}.$$
(9.11)

In many situations, it is often easier to determine τ from the physical properties of the detection mechanism or from the electronic time constants related to the resolving time in the measurement circuitry. If an instrument has a finite resolving time, τ , and the measured counting rate is R_m , then the "true" counting rate, R, that would be observed with a *perfect* instrument having a resolving time of zero is given by

$$R = \frac{R_m}{1 - R_m \tau}.$$
(9.12)

Knoll (Kn79) has provided a very detailed discussion of count rate considerations and the optimization of the counting statistics.

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9.3 Special Considerations for Accelerator Environments

There are a number of features of accelerator radiation fields which merit attention in choosing instrumentation or measurement techniques. The most important of these are discussed here.

9.3.1 Large Range of Flux Densities, Absorbed Dose Rates, etc.

The dynamic range of quantities to be measured encountered at accelerators may extend from fractional mrem yr⁻¹ found in environmental monitoring and environmental studies to the very large values of absorbed dose, up to megarads (10^6 rads) or so delivered virtually instantaneously of concern in radiation damage situations²⁵.

9.3.2 Possible Large Instantaneous Values of Flux Densities, Absorbed Dose Rates, etc.

Certain accelerators such as linacs, rapid cycle synchrotrons, and "single-turn" extracted beams from synchrotrons can have very low average intensities but have extremely high instantaneous rates. Such circumstances arise at accelerators at high intensities or in situations where the **duty factor**, the fraction of the time the beam is actually present because of accelerator characteristics, of a high intensity radiation field is small. Thus, the dead time considerations described above must be taken into account or the apparent measured values of radiological quantities such as flux densities or dose rates can be misleadingly low. Some instruments can be completely paralyzed by high instantaneous rates. Thus, the effect of dead time on the instantaneous counting rate that is present needs careful consideration.

9.3.3 Large Energy Domain of Neutron Radiation Fields

At any given accelerator capable of producing neutrons, the properties of nuclear interactions make it highly probable that neutrons will be present at all energies from thermal ($\langle E_n \rangle \approx 0.025$ eV) up to nearly the energy of the beam. As will be discussed shortly, the methods of detection of neutrons vary considerably over this energy domain. Thus the choice of instrumentation is crucial to the success of the measurement. For no other particle type is the energy range of the particles encountered in the accelerator environment so large. Also, for no other particles are the types of effective detection techniques so diverse.

9.3.4 Presence of Mixed Radiation Fields

At accelerators, one has to consider that any given radiation field external to shielding is likely to be comprised of a mixture of photons, neutrons, and at high energies and at forward angles, muons and even a multitude of other particles. Interior to shielding, the multiplicity of particle types present can be quite large. Also, virtually all neutron fields

²⁵ It is customary to quantify radiation fields in terms of absorbed dose, rather than dose equivalent, at levels above those encountered in routine personnel protection (≈ 1 rad).

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contain at least some photon component due, at least, to the capture of thermal neutrons by means of (n, γ) reactions. Furthermore, muon fields near proton and ion accelerators commonly contain some neutron component. Thus the choice of instrumentation is somewhat dependent upon what particles are present in addition to the one being measured. In certain situations, the radiation field component that is not of immediate interest can actually mask the one of concern.

9.3.5 Directional Sensitivity

Certain instruments intrinsically exhibit directional sensitivity. This feature can be either beneficial or detrimental, depending upon the situation. In all instances, it must be understood. It can lead to underestimates in radiation fields where all particles are not monodirectional. Directional sensitivity can actually be useful in certain circumstances to identify sources of unwanted radiation.

9.3.6 Sensitivity to Features of the Accelerator Environment Other than Ionizing Radiation

While the focus of this discussion is on ionizing radiation, other features must be taken into account. The most prominent of these is the presence of radiofrequency radiation (RF) at some locations that can perturb instruments which can act, sometimes rather effectively, as "antennas". Environmental effects such as temperature and humidity can also be important. In addition, one must use caution when attempting radiation measurements in the presence of magnetic fields. Induced eddy currents might be interpreted as radiation-induced ionization. Instruments may become magnetized and meter movements may be damaged or "paralyzed". Also, devices based on photomultiplier tubes commonly read "zero" in static magnetic fields of even moderate strength because of severe deflections of the low energy electrons within the tubes.

9.4 Standard Instruments and Dosimeters

This section will review instruments and dosimeters. Some of these are commonly available from commercial sources. However, commercial instruments should be used with care at accelerator facilities to be sure that their properties are adequate for usage in the particular radiological and physical environment at hand.

9.4.1 Ionization Chambers

A basic type of instrument used at accelerators to measure absorbed dose rates is the ionization chamber. Such devices are used at high energy accelerators extensively. They rely on the collection of charge liberated by particles passing through a gas. Some detectors used in physics research now employ liquids, both room temperature and cryogenic, for the ionization medium. A beneficial result from atomic physics is that the **energy loss per ion pair**, *W*, is nearly a constant over a number of gases and rather independent of type of charged particle as exhibited by Table 9.1.

	W (eV/ion pair)				
Gas	Fast Electrons	α- particles			
Ar	27.0	25.9			
He	32.5	31.7			
H_2	38.0	37.0			
N_2	35.8	36.0			
Air	35.0	35.2			
O_2	32.2	32.2			
CH_4	30.2	29.0			

Table 9.1 Values of the energy deposition per ion pair, *W*, for different gases^{*}. [Adapted from (Kn79).]

*The original data was obtained from Curran (Cu55).

Thus in a gas with a certain value of W (eV/ion pair), a charged particle depositing a certain amount of energy, ε (MeV), will liberate an electrical charge, Q_{elect} (Coulombs), according to

$$Q_{elect} = \frac{1.602 \times 10^{-13} \varepsilon}{W}.$$
 (9.13)

The charge Q_{elect} is collected by electrodes held at some voltage, V. The collected charge generates a small change in V, ΔV (volts), in accord with the relation,

$$\Delta V = \frac{\Delta Q_{elect}}{C} , \qquad (9.14)$$

where C is the capacitance of the total circuit (including that of the chamber) in units of Farads. For typical chambers, C is of the order of 10^{-10} Farads. Knoll (Kn79) gives many details of the processes that determine the size and form of the electrical signals that can be generated in a measurement. Such chambers can be operated either in a current mode (also called "DC" [i.e., direct current] or ratemeter mode) or in a integration mode in which the charge is collected (integrated) over some time period, then digitized into pulses that represent some increment of absorbed dose or dose equivalent. In the ion chamber mode of operation the applied voltage is sufficiently small so that **gas multiplication** (charge amplification) does not occur. In the most simple-minded approach, one might believe that for measurements in photon fields one could fill such a chamber with gases that "mimic" tissue and, with suitable calibration, convert the charge collected into absorbed dose. Such tissue equivalent gases range from complex mixtures to simply hydrocarbons, depending upon the accuracy of the representation of biological tissue that is desired. However, since ion chamber gases are in general much less dense than tissue, one must also capture the energy of the secondary electrons, which in the region of a few MeV have ranges of several meters in such gaseous material. It is thus necessary to use compensation techniques in which the solid material of the walls is chosen because of properties that match those of the gas.

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This condition can be readily achieved by the use of any material having an atomic number close to that of the gas. The accuracy is sufficient for most practical purposes. Thus, aluminum and especially plastics are reasonably equivalent to tissue and air, at least for use in photon radiation fields. Such walls should be of sufficient thickness to establish **electronic equilibrium**. In this condition, the flux of secondary electrons leaving the inner surface of the wall is independent of the thickness. Table 9.2 gives the wall thickness needed to establish electronic equilibrium for photons of various energies.

Photon Energy (MeV)	Thickness ^b (g cm ⁻²)	
0.02	0.0008	
0.05	0.0042	
0.1	0.014	
0.2	0.044	
0.5	0.17	
1	0.43	
2	0.96	
5	2.5	
10	4.9	

Table 9.2 Thickness of ionization chamber walls required forestablishment of electronic equilibrium^a. [Adapted from (Kn79).]

^aFrom (IC71).

^bThe thicknesses quoted are based on the range of electrons in water. The values will be substantially correct for tissue-equivalent ionization chamber walls and also for air. Half of the above thickness will give an ionization current within a few per cent of its equilibrium value.

The measurement of absorbed dose is accomplished by application of the **Bragg-Gray principle**, which states that the absorbed dose D_m in a given material can be deduced (with suitable unit conversions) from the ionization produced in a small gas-filled cavity within that material as follows:

$$D_m = WS_m P \,, \tag{9.15}$$

where W is the average energy loss per ion pair in the gas and P is the number of ion pairs per units mass formed. S_m is the ratio of the mass stopping power (i.e., the energy loss per unit density in units of, say, MeV g⁻¹ cm²) of the material of interest to that of the chamber gas. For D_m to be in grays (J kg⁻¹), W must be expressed in Joules per ion pair and P in ion pairs per kg.

For accelerator radiation fields that contain neutrons, or mixtures of neutrons with muons and photons, one is commonly able to use an ideal ion chamber to measure the absorbed dose, D, and determine the dose equivalent, H, by using the average quality factor, Q, as follows [see also Eq (1.1)]:

$$H = QD. \tag{9.16}$$

Ion chambers with tissue equivalent walls have been used in this manner at many accelerators. The value of Q has to be determined by some other means such as those described later in this chapter; usually as a separate measurement. Awschalom described the original use of such instruments at Fermilab (Aw72). Krueger and Larson have discussed their more recent evolution (Kr02). These chambers, and their later versions, are filled with suitable gases and have tissue equivalent plastic walls. They have a net volume of about 3.4 liters. Current versions of these instruments have chambers produced commercially and are made with 4 mm thick walls of phenolic. They are filled with propane gas at atmospheric pressure and contain an electrometer encased in a sealed container. Several different ion chambers commonly used at Fermilab have been studied by Freeman and Krueger (Fr84). Their properties are briefly described in Table 9.3.

Table 9.3 Descriptions of ionization chambers used at Fermilab. The instruments designated "new" were produced after 1980 while those designated "old" were produced earlier. [Adapted from (Fr84).]

produced carner	
"Old" Chipmunk	A high-pressure gas-filled ionization chamber designed by Fermilab
	and built by LND, Inc. with 4 mm thick walls of tissue-equivalent
	plastic. The fill gas is 10 atmospheres of ethane. The chamber is
	enclosed in a protective box that contains a sensitive electrometer and
	associated electronics to measure the current output and convert it to
	the dose equivalent rate. Switch-selectable quality factors of 1, 2.5, or
	5 are available. The instrument is equipped with a visible dose
	equivalent ratemeter and audible alarms. It provides a remote readout
	and capability for interface with radiation safety interlock systems.
"New" Chipmunk	These instruments are similar to the Old Chipmunk except for the use
	of phenolic-lined ionization chamber, filled with propane gas at
	atmosphere pressure and an electrometer encased in a sealed
	container. The reduced gas pressure was chosen for safety and the
	sealed container was provided to improve reliability over a larger
	range of temperature and humidity. The ion chambers were supplied
	by HPI, Inc. The latest versions of this instrument also allow for the
	selection of a quality factor of 10.
"Old" Scarecrow	A high-pressure ionization chamber with bare stainless steel walls
	filled with 10 atmospheres of ethane gas. The instrument is otherwise
	similar to the Old Chipmunk but with a fixed quality factor of 4 and
	capability to measure dose equivalent rates 100 times higher (up to 10
	rem h^{-1}). A visible ratemeter, audible alarm, and remote readout
	capability are present as is the provision for interface to radiation
	safety interlocks.
"New" Scarecrow	The electronics and functionality is similar to that of the Old
	Scarecrow, but the ion chamber of the New Chipmunk is used.

Typically, such chambers are calibrated using photons and have a typical "quality factor" built in to the electronics. Such chambers are available either as line-powered fixed monitors or as hand-held survey instruments. The use of such instruments at accelerators must be done with the assurance that the instrument will respond correctly to the radiation field present. Neutron radiation fields are generally considered to be the most difficult in which to do this successfully. Höfert and Raffnsøe of CERN have made measurements of the response of various instruments, including tissue equivalent ion chambers (Hö80). They were able to test such chambers, along with others (see further
below), in neutron radiation fields having measured neutron energies ranging from thermal to 280 MeV. Table 9.4 provides the results. The neutron fields originated from reactor and radioactive sources, except that at 280 MeV, a neutron beam from the 600 MeV CERN Synchrocyclotron was used.

Table 9.4 Absorbed dose response and measurement errors for tissue equivalent ion chambers as a function of neutron energy. [Adapted from (Hö80).]

Neutron Energy	Absorbed Dose Response	Error
(MeV)	(10 ⁵ Coulombs Gy ⁻¹)	(%)
thermal	0.446	9.8
0.0245	0.404	12.1
0.1	0.622	6.1
0.25	0.806	7.1
0.57	0.885	5.4
1.0	0.885	5.4
2.5	0.993	6.1
5.0	1.179	5.2
15.5	1.370	5.2
19.0	1.664	12.1
280.0	0.389	10.1

The performance is reasonably independent of energy in the energy region that typically dominates the dose equivalent (approximately up to about 5-10 MeV).

Simple tests that have been conducted at Fermilab indicate that absorbed dose measured in muon fields is adequately understood using the γ -ray calibration of such instruments (Co87). These tests have involved comparison with direct measurements of the muon fluence using counter-telescope techniques (see Section 9.5.8), and typically are in agreement within about 10 per cent for the Fermilab-built instruments described previously. This is to be expected since muons at high energies behave as "minimum ionizing particles" whose loss of energy in matter by ionization proceeds, to first order, as does that of electrons.

Practical problems encountered with such ion chambers are mostly those due to radiofrequency interference, pulsed radiation fields, and environmental factors such as temperature and humidity extremes. Cossairt and Elwyn (Co87) determined that airfilled, self-reading pocket ion chambers of the type that are commonly issued to personnel to allow real-time monitoring of exposure to γ -rays, performed very well in *muon* radiation fields (measuring absorbed doses to within about \pm 15 %). This is due to the fact that the ratio of muon stopping power in tissue to that in air for energies between 1 and 800 GeV is 1.07 ± 0.05 (St83).

9.4.2 Geiger-Müller Detectors

These instruments, among the oldest developed for the detection of radiation, are in conspicuous use at particle accelerators primarily with respect to detection and measure-

ment of induced activation and removable induced activity (contamination). In some instances such instruments can be used to identify prompt radiation fields. They are very rugged and remarkably insensitive to environmental effects such as temperature and humidity. However, the typical dead time of 100 μ sec or so renders them to be generally useless in fields having high instantaneous rates.

9.4.3 Thermoluminescent Dosimeters (TLDs)

Swanson and Thomas (Sw90) and Knoll (Kn79) have provided discussions of the properties of TLDs. These dosimeters are an attractive alternative to photographic film particularly to monitor personnel exposures in β and γ radiation fields. They have also been found to be useful in measuring neutron radiation fields when used as a pair of ⁶LiF and ⁷LiF TLDs crystals in the same dosimeter. Such use exploits the fact that the reaction ⁶Li(n, α)³H has a large thermal neutron cross section of 940 barns (see Section 9.5.1.2) while the ⁷Li(n, γ)⁸Li reaction cross section is only 0.037 barns for thermal neutrons. Since a TLD containing either ⁶Li and ⁷Li has a comparable efficiency for photon or muon radiation, measurement of the response of the two detectors can, then, be used to determine the dose equivalent due to thermal neutrons in the presence of photons or muons. These reactions provide tools to use in the detection of fast neutrons if moderation is supplied, as will be discussed later.

TLDs operate on the principal that some of the radiation liberated by the ionizing particle is "trapped" in band gaps in the crystal lattice. The process is well described by Knoll (Kn79). In particular, ionization elevates electrons from the valence to the conduction band where they are then captured by a "trapping center". At room temperatures, there is only a small probability per unit time that such "trapped" electrons will escape back to the conduction band from the valence band. Thus exposure to radiation continuously populates the traps. "Holes" are similarly trapped in the valence band. When readout of the dose is desired, the crystal is heated and this thermally excites the electrons and holes out of the traps. This process is accompanied by the emission of light that can then be measured as a so-called "glow curve". A number of other materials can function as TLDs; notably CaSO₄:Mn, CaF₂, and CaF₂:Mn. These materials have properties that can be optimized for particular applications. CaF₂:Mn is particularly useful for environmental monitoring purposes, where extraordinarily high sensitivity is required. The large numbers of trapped electrons and holes per unit of dose permits sensitivity to absorbed doses as small as 2 x 10⁻⁵ rads. LiF "fades" over time to a lessor degree than most of the other materials at room temperature and its average atomic number is very close to that of tissue, so it is particularly useful for personnel dosimetry.

TLDs can give valid results for fields as high as 100 rads. Higher doses can be measured under certain conditions if one takes care to use crystals calibrated in the intense radiation fields since linearity of the response breaks down in the high dose region. These devices exhibit superlinearity. TLDs are not generally susceptible to dose rate problems. However the readout process is intrinsically "destructive" and usually cannot be repeated.

9.4.4 Nuclear Track Emulsions

This discussion is summarized from that of Swanson and Thomas (Sw90). For many years thin (≈ 25 micron) emulsions (NTA) have been used for personal dosimetry in fast neutron fields. The technique is based upon detection of tracks left by proton recoils in the film. The energy range for which these dosimeters are effective is from roughly 0.5 to 25 MeV because below that range the tracks are too short to be read out, while above it there are too few tracks because the (n, p) cross section (elastic scattering, mostly) decreases with energy. However, this energy range is the one that often results in significant neutron dose equivalents at accelerators. The singular important problem with NTA is that the latent image fades and leads to underestimates of the dose equivalent. The fading time can be a short as two weeks. Extreme efforts to keep out the moisture, and experience in dry climates give some indication that this problem can be overcome.

Höfert (Hö84b), as has Greenhouse et al. (Gr87), has given a good summary of experience with this dosimeter at accelerators. The dose equivalent range from about 10 mrem to a few hundred mrem is that for which this dosimeter can be expected to perform acceptably. Any technique based upon track formation should not be dependent upon dose rate effects.

9.4.5 Track Etch Dosimeters

Swanson and Thomas (Sw90) have discussed the use of such dosimeters. In these detectors, the passage of a charged particle through a dielectric material will result in a trail of damaged molecules in the material. These tracks can be made visible upon etching in a strong acid or base solution. The tracks will be etched at a faster rate than the undamaged portions of the material. As with nuclear emulsions, there is a minimum detectable track length that sets a threshold of about 0.5 MeV on the neutron detection. Such detectors have been reviewed extensively by Griffith and Tommasino (Gr90). Mica, Lexan, and other materials are suitable for this purpose and electronic methods of readout are available. Repeated readouts of the processed tracks are feasible.

9.4.6 CR-39 Dosimeters

Swanson and Thomas (Sw90) have provided a discussion of applications of such dosimeters at accelerators. This material, also a "track detector", has largely replaced NTA as a film dosimeter. It is a casting resin, originally developed for use in eyeglass lenses, that is transparent and is thermoset, rather than thermoplastic. It is the most sensitive of the track detectors and registers recoil protons up to 15 MeV and down to about 0.1 MeV. It is processed either chemically or electrochemically. Repeated readouts of the processed tracks are feasible. The lower limit of detection appears to be superior to that of NTA or Track-Etch (Lexan). There are about 7 x 10^3 tracks cm⁻² rem⁻¹, which is adequate, but the sensitivity may be as much as a factor of two lower in high energy spectra. Fading appears to be insignificant. However, natural radon gas can contribute to background readings and the angle of incidence is important.

9.4.7 Bubble Detectors

The use of these detectors at accelerators has also been discussed by Swanson and Thomas (Sw90). The bubble damage polymer detector is an innovative dosimeter that is similar to a bubble chamber in that a liquid whose normal boiling point is below room temperature is kept under pressure. When the pressure is released bubbles form along the path of a charged particle that has traversed it. To enhance the effect, superheated droplets of a volatile liquid are dispersed in a gelatinous medium. There are two types of these detectors that have been developed; one type by Apfel (Ap79) and the other type by Ing (In84). The polymer or gel is supplied in a clear vial. When a neutron interacts in the sensitive material, a bubble is created that expands to optically visible dimensions and can thus be counted. There is no angular dependence but temperature effects must be considered. The Ing detector was reported to exhibit a constant response over the range 15 °C < T < 35 °C. The material can be tailored to match a chosen neutron energy threshold that can be as low as 10 keV or less. Indeed, sets have been prepared with arbitrary thresholds of 0.010, 0.100, 0.500, 1, 3, and 10 MeV. The range of sensitivity can be adjusted to be between 1 and 30 bubbles per mrem, or larger, in a volume of about 4 cm^3 and the physical mechanism is not readily sensitive to dose rate effects. Disadvantages include a high unit cost, and the fact that once the vial is opened it is only good for limited periods of time of dose integration. The materials have been successfully used at accelerator facilities. These detectors could not be expected to give accurate results in high dose rates.

One can see that no single commercial instrument "solves all problems" simultaneously, especially for neutron fields. The practitioner is encouraged to utilize a variety of instruments, including some of the special techniques discussed below to fully understand the radiation fields.

9.5 Specialized Detectors

9.5.1 Thermal Neutron Detectors

Although thermal neutrons are not commonly the major source of neutron dose equivalent at particle accelerators, they are of considerable importance in accelerator radiation protection because of the ability to moderate the fast neutrons (as we shall see below). Furthermore, because some of the most prominent thermal neutron detectors rely upon radioactivation (by neutron capture) as the detection mechanism, they have the advantage that the response is entirely independent of dose rate effects and hence free of dead time effects. An excellent discussion, summarized here, on thermal neutron detectors is given by Knoll (Kn79).

At the outset, there are some general features concerning thermal neutrons that need to be recalled. The kinetic energies of thermal neutrons have the familiar relationship as a

function of temperature given by the Maxwell-Boltzmann distribution:

$$f(E) = \frac{2}{\sqrt{\pi} \left(kT\right)^{3/2}} E^{1/2} \exp\left\{-\frac{E}{kT}\right\},$$
(9.17)

where f(E) is the fraction of particles, in this case neutrons, of energy E per unit energy interval, the Boltzmann constant $k = 1.38 \times 10^{-23} \text{ J} \text{ oK}^{-1}$ or 8.62 x 10⁻⁵ eV oK⁻¹, and T is the absolute temperature of the gas (oK). The most probable energy, E_{mp} , is given by

$$E_{mp} = kT \,, \tag{9.18}$$

while the average energy at any given temperature, $\langle E \rangle$, is

$$\left\langle E\right\rangle = \frac{3}{2}kT\,.\tag{9.19}$$

At room temperature T = 293 °K, so that the most probable energy is 0.025 eV. Normally, thermal neutron cross sections are tabulated for this value of kinetic energy. Since thermal neutrons are decidedly nonrelativistic, the most probable velocity, v_{mp} , at T = 293 °K is determined from

$$E_{mp} = \frac{1}{2} m v_{mp}^2 = kT$$
, so that $v_{mp} = 2200 \text{ m s}^{-1}$. (9.20)

As the neutron energy increases above the thermal value (up to about 1 keV), unless there are resonances present in the cross section, the absorption cross section, σ , has been found to be approximately described by the relation

$$\sigma \propto \frac{1}{\sqrt{E}} \propto \frac{1}{\nu},\tag{9.21}$$

that is known as the 1/v law. Thus, within the limits of validity of the 1/v law, one can scale from the tabulated "thermal" cross section, σ_{th} , as follows:

$$\sigma(E) = \sigma_{th} \sqrt{\frac{E_{mp}}{E}} .$$
(9.22)

Several different nuclear reactions that are initiated by thermal neutrons are used as the basis of detectors. They all involve particular target nuclei and thus the detector materials sometimes depend upon isotopically separated materials to enhance the effectiveness.

9.5.1.1 Boron-10

The ${}^{10}B(n, \alpha){}^{7}Li$ reaction is exothermic, having a *Q*-value [see Eq. (4.1)], Q_{ν} , of 2.792 MeV, and leads either to the ground state of ${}^{7}Li$ or its first excited state at 0.482 MeV. The latter occurs for about 94 % of the time when thermal neutrons are incident. Thus, for the dominant transition to the excited state, the reaction imparts about 2.31 MeV to the reaction products. This energy is much larger than the kinetic energy of the incoming *thermal* neutron. Since energy and momenta must be conserved, for the dominant excited state branch the kinetic energy of the alpha particle, $E(\alpha)$, is 1.47 MeV and, accordingly, $E({}^{7}Li) = 0.84$ MeV. This is because the following must hold:

$$E(^{7}\text{Li}) + E(\alpha) = 2.31 \text{ MeV},$$
 (9.23)

due to energy conservation for the excited state branch, if one neglects the very small kinetic energy of the incident thermal neutron. Also,

$$[2m(^{7}\text{Li})E(^{7}\text{Li})]^{1/2} = [2m(\alpha)E(\alpha)]^{1/2}.$$
(9.24)

holds due to conservation of momentum since the two reaction products emerge in opposite directions. The very small momentum of the thermal neutron is ignored and one recalls that, nonrelativistically, $p^2 = 2mE$, where *m* denotes the rest mass of the particle.

The excited state subsequently decays by emission of a photon. For this reaction, at 0.025 eV, $\sigma_{th} = 3837$ barns. The relatively large natural abundance of ¹⁰B is 20 % compared with 80 % for the other stable isotope, ¹¹B (Se81). The large natural abundance of the crucial isotope makes this reaction very favorable for thermal neutron detection. In addition, material enriched in ¹⁰B is readily available. Also the reaction products, and thus their deposited energies, being of short range, are contained in "reasonable" detector configurations. Figure 9.1 gives the cross sections as a function of neutron energy for several of the thermal capture reactions described here, including this one. It is useful that the Boron-10 reaction has a rather featureless cross section and obeys the $1/\nu$ law quite well even up to an energy of approximately 0.5 MeV.

This reaction has been used principally in BF₃ gas in proportional tubes. Proportional counters are somewhat similar in concept to ionization chambers except that the applied electric fields are of sufficient strength to accelerate the initial electrons liberated by the ionization to energies above the thresholds for liberating additional secondary electrons. In typical gases at one atmosphere, this threshold is of the order 10^6 volts/meter. Under proper conditions, the number of electrons generated in this process can be kept proportional to the energy loss but the number of electrons released (and hence the size of the signal) can be "amplified" by a "gain" of many thousands. In proportional chambers, the region in which these secondary electrons are released is kept small compared to the chamber volume. If the voltage is raised beyond these conditions, then proportionality is lost and the counter enters the Geiger-Mueller mode. Knoll (Kn79) has given a detailed

exposition on proportional chambers and the gas multiplication process. BF₃ is the best of the boron-containing gases as a proportional counter gas because of its "good" properties as a counter gas and also because of the high concentration of boron in the gas molecule. Typical BF₃ tubes operate at 2000 to 3000 volts potential with gas ionization multiplications ranging from about 100 to 500. An enriched (96%) BF₃ tube can have an absolute detection efficiency of 91 % at 0.025 eV dropping to 3.8 % at 100 eV for neutrons incident upon it. Alternatives with somewhat better gas properties (and cleaner signals) have been achieved by using boron-lined chambers with other gases that have better properties in proportional chambers.

9.5.1.2 Lithium-6

The reaction of interest is ${}^{6}\text{Li}(n, \alpha){}^{3}\text{H}$. For this reaction, $Q_{v} = 4.78$ MeV. The process leads only to the ground state of ${}^{3}\text{H}$. As discussed in connection with the ${}^{10}\text{B}(n, \alpha){}^{7}\text{Li}$ reaction, conservation of energy and momentum can be shown to determine the result that $E({}^{3}\text{H}) = 2.73$ MeV and $E(\alpha) = 2.05$ MeV. For incident thermal neutrons, $\sigma_{th} = 941$ barns (Se81). The natural isotopic abundance of ${}^{6}\text{Li}$ is about 7.5 %. Figure 9.1 includes the cross section of this reaction as function of neutron kinetic energy. The cross section exhibits a significant resonance at about 3 x 10⁵ eV. The apparent disadvantage of the "small" thermal cross section is offset by the higher *Q*-value and resultant larger signals.

For use in gas counters, no fill gas containing lithium having suitable properties analogous to those of BF₃ has been found. Instead, ⁶Li has been successfully added to scintillators. With the addition of a small amount (< 0.1 % of the total atoms) of europium to LiI [LiI(Eu)], the light output is as much as 35 % of that of a comparable size NaI(Tl) crystal. Such scintillators have a decay time of approximately 0.3 μ s. Of course, ⁶LiF is also in prominent use as a TLD and employs the same nuclear reaction. The TLD can be used in high dose rates, since no instantaneous readout is involved.

9.5.1.3 Helium-3

This nuclide, gaseous at room temperature, is used through the reaction ${}^{3}\text{He}(n, p){}^{3}\text{H}$. The Q-value is 0.765 MeV so that, as for the other reactions, E(p) = 0.574 MeV and $E({}^{3}\text{H}) = 0.191$ MeV for incident thermal neutrons. For this reaction, $\sigma_{th} = 5327$ barns (Se81). Although this isotope of helium can be used directly as a detector gas, it has the disadvantages that the natural abundance is only 0.000138 %, which renders enriched ${}^{3}\text{He}$ to be rather costly. Also some of the energy can escape the sensitive volume of a detector of reasonable size because of the relatively long range of the emitted proton. Again, the cross section as a function of energy is given in Fig. 9.1. As seen, the cross section is quite "well-behaved". ${}^{3}\text{He}$ is a reasonable gas for proportional chambers; however no compounds are available since it is a noble gas. In sufficient purity it will work as an acceptable proportional counter gas. Because a proton is the reaction product instead of the short range α -particle, "wall effects" (i.e., effects in which some energy

escapes the counting gas volume) may be somewhat more severe than for BF_3 . However, proportional chambers filled with ³H can be operated at much higher pressures than are possible with BF_3 and can thus have enhanced detection efficiency.



Fig. 9.1 Cross section versus neutron energy for some reactions of interest in neutron detection. [Adapted from (Kn79).]

9.5.1.4 Cadmium

This discussion would be incomplete without discussing cadmium. Averaged over the naturally-occurring isotopes of cadmium, the thermal neutron capture reaction of form ^ACd(n, γ)^{A+1}Cd has a cross section $\sigma_{th} = 2450$ barns. More spectacularly, the reaction ¹¹³Cd(n, γ)¹¹⁴Cd has a value of $\sigma_{th} = 19910$ barns (Se81). ¹¹³Cd has a natural abundance of 12.2 %. Thus, even without using enriched material, the thermal neutron cross section is large. This element is not used directly in the detector medium. Rather, it is used to shield other detectors from thermal neutrons because the large cross section results in the absorption of essentially all neutrons with energies less than about 0.4 eV. Hence, one can do measurements with and without the Cd inside of some moderator (see Section 9.5.2) and have a very clear understanding of the thermal component.

9.5.1.5 Silver

Awschalom et al. was able to use thermal neutron capture on silver as a basis of a moderated detector (Aw72). As it occurs in nature, silver has two stable isotopes which both capture thermal neutrons via the (n, γ) process; ¹⁰⁷Ag (51.8 % natural abundance, $\sigma_{th} = 40$ barns) and ¹⁰⁹Ag (48.2 % natural abundance, $\sigma_{th} = 93.5$ barns). The average value of σ_{th} is 63.6 barns (Se81). While the cross sections are not as large as those of some of the other reactions discussed, the material is readily available and enrichment is not needed. The detector which utilized these capture reactions was a moderated one (see below) in which the output of a Geiger-Mueller tube wrapped with silver that sensed the capture γ -rays was compared with an identical tube wrapped with tin (average mass number = 118.7). Tin has an average value of $\sigma_{th} = 0.63$ barns and is thus comparatively insensitive to thermal neutrons. The tin-wrapped tube was then used to subtract background due to muons, photons, etc.

9.5.2 Moderated Neutron Detectors

As seen above, many neutron reactions tend to have much smaller cross sections in the MeV region than they have in the "thermal" region. Historically, shortly after the discovery of the neutron, it was observed that surrounding a thermal neutron detector with hydrogenous material enhance detection rates exhibited by a "bare" thermal neutron detector placed in the same radiation field. The reason this occurs with hydrogenous materials is because in nonrelativistic elastic scattering, as we have seen before, the fraction of the incident energy, E_o , that can be transferred to the target nucleus after a collision where the target nucleus recoils at angle θ is determined by conservation of momentum and energy to be given by

$$\left(\frac{\Delta E}{E_o}\right) = \frac{4M\cos^2\theta}{\left(1+M\right)^2},\tag{9.25}$$

where M is the mass of the target nucleus in units where the mass of the neutron is unity.

The energy that can be transferred in the reaction is maximized in the head-on collision $(\theta = 0)$ and has its maximum value (1) when $M \approx 1$ (hydrogen). Even for a nucleus as light as ¹²C, the quantity $(\Delta E/E_o)_{\text{max}}$ has a value of only 0.28.

One might, naively, expect that the detection efficiency to improve with the thickness of the moderator. However as the moderator thickness increases, the probability that a given *moderated* neutron will actually ever reach the detector *decreases*. Fig. 9.2 illustrates these tradeoffs qualitatively. In general, the optimum thickness will, for moderators such as polyethylene, range from a few centimeters for keV neutrons to several tens of centimeters for MeV neutrons. Furthermore, for any given thickness, the overall counting efficiency as a function of energy will tend to show a peak at some energy determined by the thickness.

9.5.2.1 Spherical Moderators, Bonner Spheres, and Related Detectors

Bramblett, Ewing, and Bonner employed spherical moderators to obtain low resolution neutron spectra (Br60) using a method that has become known as the **Bonner sphere** technique. In this technique moderating spheres of different diameters surrounding a thermal neutron detector of some type are placed in a given radiation field. The normalized relative (or absolute) responses are, then, indicative of the neutron energy spectra. As one might expect, the determination of the efficiency of each sphere as a function of energy is a rather complicated matter, and such response functions have been calculated, using techniques such as the Monte Carlo method, by a number of authors over the years since this method was invented. Hertel and Davidson (He85) have calculated the response functions for spheres that possess the "standard" set of diameters. Other response functions, perhaps more accurate in neutron fields of higher energies, have been reported by Awschalom and Sanna (Aw85). The response functions are dependent upon detector size as well as upon moderator thickness and density. The density is typically 0.95 g cm⁻³ for polyethylene. The results of Awschalom and Sanna are given in Fig. 9.3 for cylindrical LiI(Eu) detectors of lengths equal to their diameters which are each 1.27 cm (0.5 inch) in polyethylene spheres of this density. As one might expect, larger detectors readily give a higher efficiency response in accordance with the size of their sensitive volumes.

Most of the efficiency calculations have been made for ${}^{6}\text{LiI}(\text{Eu})$ scintillators, but also can be used for ${}^{6}\text{LiF}$ TLD dosimeters. They cannot, in general, be used for other thermal neutron capture reactions used to detect thermal neutrons as the neutron cross sections needed for the calculation of the responses will differ. There are other sets of response functions extant. Experimental verifications of the details of these response functions are rare because of the difficulty of the measurements. Kosako et al. (Ko85) have successfully verified some of the important response functions using a neutron time-offlight technique in the especially difficult keV energy region of neutron energy. A Bonner sphere determination of the neutron spectrum is comprised of a set of measurements of the responses for the different spheres of radius r, C_r , where r has the



Fig. 9.2 Schematic representation of neutron tracks in moderated detectors. The small thermal neutron detector at the center is shown surrounded by two different thicknesses of moderator material. The track labeled 1 represents incident fast neutrons that are successfully moderated and detected. The track labeled 2 represents those neutrons partially or fully moderated, but escape without reaching the detector. Track 3 represents those neutrons that are parasitically captured by the moderator. Larger moderators will tend to enhance process 3 while reducing process 2. [Reproduced from (Kn79).]



Fig. 9.3 The calculated responses for the bare 12.7 mm diameter LiI detector and for the same detector inside 5.08, 7.62, 12.7, 20.32, 25.4, 30.48, 38.1, and 45.72 cm diameter spheres as a function of neutron energy. The detector is a cylinder having a length equal to its diameter. The "normalization" is that needed to provide the correct responses according to Eq. (9.26). [Adapted from (Aw85), which contains tables of numerical values of these functions.]

discrete values based on the available set. Such responses, ideally, are given by

$$C_r = \int_0^\infty dE \frac{dN}{dE} R_r(E), \qquad (9.26)$$

where dN/dE is the differential neutron flux density (the neutron spectrum) and $R_r(E)$ is the energy-dependent response function for the sphere of radius r. One measures C_r and knows $R_r(E)$ with the objective of determining dN/dE by **unfolding** the spectrum. In practice, one works with a discrete approximation to the integral;

$$C_r = \sum_i \frac{dN}{dE_i} R_r(E_i) \Delta E_i, \qquad (9.27)$$

where the index *i* labels each member of the set of "energy groups" used. The unfolding procedure is a difficult mathematical problem that, unfortunately, suffers from being underdetermined and mathematically ill-conditioned. One has as many "unknowns" as one has energy groups, with typically only 8 or 9 measurements to determine the response. Commonly 31 energy groups are used in an attempt to achieve "reasonable" energy resolution in the results. A variety of numerical techniques have been developed to do the unfolding.

Prominent codes in use at accelerators include BUNKI (Lo84), LOUHI (Ro80), and SWIFT (OB81). The first uses an iterative recursion method and the second uses a least squares fitting procedure with user-controlled constraints. One essentially starts with an "educated guess" at the spectrum and iterates to fit the responses. As we have seen, a 1/*E* spectrum is a good starting point for an accelerator spectrum. SWIFT is based upon a somewhat different principle; it is a Monte Carlo program that makes no *a priori* assumptions on the spectrum and can thus provide a "reality check" on results using the other two. It has the disadvantage in that it is known to sometimes produce nonphysical peaks in the unfolded spectrum. In general, the codes agree best with each other for those properties that are determined by integrating over the spectrum such as the average quality factor, total fluence, and total absorbed dose and dose equivalent. Typical spectra obtained from such unfolding procedures have been reported at a number of laboratories. Fermilab results have been summarized by Cossairt et al. (Co88) and are, in general, similar to those obtained at other laboratories. Further discussion of examples of neutron spectrum measurements is provided in Chapter 6.

It is sometimes important to verify the reasonableness of the unfolded spectrum. Comparisons can be made with known spectra from radioactive sources such PuBe or AmBe and such comparisons have been made (e.g., Co88). The normalized responses, C_r , can be directly used to check the qualitative "reasonableness" of the unfolded spectrum. For example, this was done for measurement in the labyrinth discussed in connection with Fig. 6.7 and for the iron leakage measurements described in connection with Fig. 6.8. The results are shown in Fig. 9.4 and Fig. 9.5. In Fig. 9.4 the labyrinth responses are compared with the sphere responses for a pure thermal neutron spectrum. The enhanced responses for the intermediate-sized spheres indicate the somewhat more energetic unfolded neutron spectrum that was observed. For the iron leakage spectrum (Fig. 9.5), one can see evidence for the "softening" of the spectrum after the concrete was added. Other verifications, of course can be obtained using entirely independent measurement techniques.

In the use of ${}^{6}\text{LiI(Eu)}$ scintillators for such detectors in mixed fields, there are situations in which the signals from photons and/or muons can overwhelm the neutron signal. Awschalom and Coulson (Aw73) developed a technique in which the ${}^{6}\text{LiI(Eu)}$ is surrounded by plastic scintillator. The physical configuration of such a phoswich detector, and a typical pulse height spectrum obtained by use of this detector in a long exposure to environmental neutrons are given in Figs. 9.6 and 9.7. The same detector



Fig. 9.4 Normalized response from the detector as a function of spherical moderator diameter. The solid circles are the measurements within the second leg of the labyrinth shown in Fig. 6.7. The open circles represent calculated results assuming a purely thermal spectrum while the crosses are the results for the neutron energy spectrum unfolded using the program SWIFT. The solid and dashed curves are drawn to guide the eye. The inset shows a typical gated spectrum of the pulse heights in the ⁶LiI(Eu) phoswich detector described in the text. [Reproduced from (Co85b).]

was used to produce the pulse-height spectrum shown in the inset in Fig. 9.4. In this technique, a "fast" discriminator is set to respond to the 2-3 nanosecond decay time of the plastic scintillation signal while a "slow" discriminator is set to respond to the 1.4 μ sec decay time of the crystal. Selecting the slow counts <u>not</u> accompanied by fast counts clearly gives superior discrimination against non-neutron events from environmental radiation (e.g., cosmic ray muons) which produces coincident pulses in <u>both</u> the crystal and the plastic scintillator (see Fig. 9.7).

In performing Bonner sphere measurements in neutron fields that are suspected of being spatially nonuniform in space, it may be necessary to measure C_r over the set of spheres individually because arranging them in an array may result not only in undesired "cross-talk" between the moderators but also in the need to make corrections for the non-uniformities of the radiation field.



Fig. 9.5 Normalized detector response as a function of spherical moderator diameter for the situation presented in Fig. 6.8. The open circles are the measurements **before**, and the X's are the measurements **after** the placement of the additional concrete shielding. [Reproduced from (El86).]



Fig. 9.6 Cross section of 8 mm x 8 mm cylindrical phoswich. [Reproduced from (Aw73).]



Fig. 9.7 Pulse height spectra obtained using the phoswich shown in Fig. 9.6 in a natural background radiation field. The **upper curve** (filled circles) is a spectrum of all slow pulses (slow with fast and slow without fast). The **lower curve** (open circles) is a spectrum of slow pulses not accompanied by fast pulses, interpreted to be due to neutrons. [Reproduced from (Aw73).]

Since accelerator neutron fields are often quite similar to each other, it was noticed that the choice of a single moderator size might well offer the opportunity to construct a remmeter. Such an instrument uses a given sphere response function particularly well matched to energy dependence of the fluence per dose equivalent conversion factor. The standard implementation of this is in the development of the Andersson-Braun detector (An62), which uses a BF₃ detector. The usage of such counters was reviewed by Thomas and Stevenson (Th88). Generally, the 25.4 cm (10 inch) diameter polyethylene sphere has been selected because its response curve provides the best match to the dose equivalent per fluence function. Höfert and Raffnsøe (Hö80) have measured the dose equivalent response of such an instrument as a function of neutron energy. Their results are given in Table 9.5. Generally, commercial versions of this instrument operate in the proportional counter mode. This renders them somewhat suspect in accelerator fields with high instantaneous dose rates that arise because of the small duty factor due to pulsed beams. A similar detector has been developed by Hankins and employed $^{6}LiI(Eu)$ as the detector (Ha62). Hankins obtained the response shown in Fig. 9.8 that includes a comparison with the "Inverse of the Radiation Protection Guide (RPG)" curve that embodies the relative dose equivalent delivered per neutron as a function of neutron energy. In the keV region, comparisons are difficult and there is some evidence that this

detector overresponds considerably. However, the matching was verified at thermal neutron energies. Leake (Le68) developed an alternative detector of this general type. In this detector a ³He proportional counter is used in a 20.8 diameter sphere to reduce background due to photons along with a cadmium filter against thermal neutrons. It is claimed that this detector is effective in photon fields as intense as 20 rads h^{-1} . There are concerns that above 10 MeV this type of instrument seriously underestimates neutron dose equivalent rates.

Neutron Energy	Dose Equivalent Response	Error
(MeV)	(10 ⁵ Coulombs Sv ⁻¹)	(%)
thermal	0.349	10.0
0.0245	3.209	12.1
0.1	1.335	6.8
0.25	1.082	6.1
0.57	0.923	5.2
1.0	0.745	5.2
2.5	0.784	6.1
5.0	0.653	5.2
15.5	0.348	5.2
19.0	0.445	12.2
280.0	0.157	10.1

Table 9.5 Dose equivalent response and measurement errors for a 25.4
cm diameter polyethylene moderating sphere as a function of neutron
energy, [Adapted from (Hö80)]



Fig. 9.8 Sensitivity of detector comprised of a 25.4 cm (10 in.) diameter moderating sphere surrounding a 4 x 4 mm² cylindrical LiI scintillator in counts s⁻¹ at 40 cm distance from a source of 10⁶ neutrons s⁻¹. Also shown is the relative dose equivalent per neutron labeled as "Inverse RPG". At thermal energies, the response was measured to be 0.227 compared with a value of 0.225 for the "Inverse RPG" curve (see text). [Adapted from (Ha62).]

It is not necessary, for radiation protection purposes, that a "spherical" moderator be an exact sphere. Awschalom et al. (Aw72) measured the responses of three polyethylene moderators; a sphere, an octagon of revolution (a "pseudosphere"), and a cylinder. The sphere had a diameter of 25.4 cm and the sizes of the other moderators were chosen to have the same volume as the sphere. It was found that the alternative moderators have a response almost indistinguishable from that of the sphere as a function of polar angle of the detector with respect to the axis of revolution. Such pseudospheres and cylinders are desirable because they are cheaper to machine than are spheres. They can also be set on a flat surface without rolling about. The results of the measurements of Awschalom et al. are shown in Fig. 9.9. The "polar axis" is defined by the light pipe used to read out the scintillator placed in the center of each moderator.



Fig. 9.9 Relative neutron detection efficiency of three different moderators with a 4 x 4 mm² cylindrical ⁶LiI(Eu) detector at the center. The efficiencies are plotted as a function of the polar angle. The polar angle is measured from the axis of the light pipe. [Adapted from (Aw72).]

9.5.2.2 Long Counters

Another type of moderated neutron detector that has been used extensively is the **long counter.** The idea is to adjust the configuration of moderators around some thermal neutron detector in such a manner as to assure that the detection efficiency is approximately independent of energy over as "long" of an energy domain as practical. It has been found empirically that the best detector is a cylinder of moderating materials surrounding a thermal neutron detector (also cylindrical) on the axis. Since a cylindrical detector is desired, the BF₃ proportional counter is the most popular. One end of the cylinder "views" the neutron source for best results. Hanson and McKibben (Ha47) were the pioneers of the technique. An improved version, which has rather widespread use, is

that developed by DePangher and Nichols (DeP66). Figure 9.10 shows the layout of this detector. The length and diameter are both approximately 41 cm and the mass is about 45 kg. It is designed and calibrated for use with the neutrons incident on the "front" face.

Perhaps the best calibration data on this device is that of Slaughter and Rueppel (S177). They used filtered beams from a reactor ($E_n \approx \text{keV}$) as well as monoenergetic neutron beams from (p, n) and (d, n) reactions at accelerators to cover the energy range from 10 keV to 19 MeV. An average of about 3.5 counts/(n cm⁻²) sensitivity was reported over this energy domain, with deviations of from 5 to 30 per cent from absolute independence of neutron energy. A similar detector has been used to conduct studies of skyshine at Fermilab [(Co85c) and (El86)]. The large peak in the pulse-height spectrum of the BF₃ tube from thermal neutron capture ($Q_v = 2.79$ MeV) renders the detector essentially insensitive, with the application of a suitable pulse-height discriminator, to all other radiations. Knoll (Kn79) summarizes results with modified long counters that achieve better uniformity and higher levels of sensitivity over more restricted energy domains.

9.5.3 Activation Detectors

As we have seen, certain nuclear reactions have relatively sharp thresholds which can be used to determine portions of a hadron spectrum that exceed it since the "leveling off" of the cross sections are generally well-behaved. In addition to information on reaction thresholds provided in Chapter 7, where referral was made to activation threshold techniques, Table 9.6 summarizes some of the useful reactions along with some pertinent information about threshold detectors that have been found to be useful in practical work. Some of these reactions will be discussed further below. Thomas and Stevenson (Th85 and Th88) provide a list of other reactions that might have useful thresholds.

Detector	Reaction	Energy	Half-Life	Typical	Cross	Cross Section-	Particle
		Range		Detector Size	Section-	High	Detected
		(MeV)			Peak (mb)	Energy(mb)	
sulfur	$^{32}S(n,p)^{32}P$	> 3	14.26 d	4 g disk	500 ^a	$10^{\rm a}$	β⁻
aluminum	$^{27}\text{Al}(n,\alpha)^{24}\text{Na}$	> 6	14.95 h	16 - 6600 g	11 ^b	9 ^b	γ
aluminum	$^{27}Al(n,x)^{22}Na$	> 25	2.603 y	17 g	30 ^b	10 ^b	γ
plastic	$^{12}C \rightarrow ^{11}C$	> 20	20.33 min	13-2700 g	90 ^b	30 ^b	β⁺, γ
scintillator							
plastic	$^{12}\text{C} ->^{7}\text{Be}$	> 30	53.22 d	17 g	18 ^b	10 ^b	γ
scintillator							-
mercury	¹⁹⁸ Hg-> ¹⁴⁹ Tb	> 600	4.12 h	up to 500 g	2 ^b	1 ^b	α,γ
gold	197 Au-> 149 Tb	> 600	4.12 h	0.5 g	1.6 ^b	0.7 ^b	α,γ
copper	Cu-> ²⁴ Na	> 600	14.95 h	580 g	4 ^c	3.9 ^c	γ
copper	Cu-> ⁵² Mn	> 70	5.59 d	580 g	5 [°]	4.6 ^c	γ
copper	Cu-> ⁵⁴ Mn	> 80	312.1 d	580 g	11 ^c	11 ^c	γ

 Table 9.6 Important characteristics of various activation detector nuclear reactions.

^aSwanson and Thomas (Sw90)

^bBarbier (Ba69)

^cBaker et al. (Ba84 and Ba91).



Fig. 9.10 Schematic diagram of a DePangher Long Counter. This version contains a built-in PuBe source, which is optional. The source would not be desirable in an instrument to be used in radiation fields near natural background. The dimensions and mass of this instrument are given in the text. [Reproduced from (DeP66).]

The family of reactions which produce ¹¹C from ¹²C are of special interest because of the fact that plastic scintillators can themselves become activated by hadrons (especially neutrons and protons) exceeding 20 MeV. This technique was first developed by McCaslin (McC60). The cross sections for production of ¹¹C, as initiated by several different types of incident particles, are shown in Fig. 9.11. Stevenson (St84b) has determined that a value of 28 fSv m² is an appropriate factor to apply to the conversion of the measured fluence of neutrons with $E_n > 20$ MeV to the dose equivalent due to those energetic neutrons. This assumes a typical accelerator spectrum found within thick shields of earth or concrete where neutrons clearly dominate. Such measurements can be useful to determine the contribution of the high energy ($E_n > 20$ MeV) neutrons to the total neutron dose equivalent.

Moritz (Mo89) has found that the use of NE102A scintillators activated by the reaction ${}^{12}C(n, 2n){}^{11}C$ can be included as an additional high energy detector in a Bonner sphere measurement in order to extend the energy range. Moritz, following Stevenson, used an average cross section of 22 mb for the ${}^{12}C(n, 2n){}^{11}C$ reaction. NE102A, a common and typical plastic scintillator, has a carbon content of 4.92 x 10²² atoms g⁻¹ and a density of 1.032 g cm⁻³ according to Knoll (Kn79). Moritz used a cylindrical detector 5 cm in diameter by 5 cm long and achieved an efficiency of 93 % in detecting the 0.511 annihilation γ -rays produced as a result of the ${}^{11}C$ decay. In effect, the addition of this reaction reduced the degeneracy of the spectrum unfolding process using the code LOUHI.



Fig. 9.11 Excitation functions for the reactions ${}^{12}C \rightarrow {}^{11}C$ induced by neutrons, pions, and protons. The arithmetic mean of the positive and negative pions cross sections is shown as the pion curve. [Adapted from (Sw90).]

Figure 9.12 provides the excitation functions of some other useful reactions with very high thresholds. The Hg -> 149 Tb reaction is a suitable monitor for very high energy particles and is commonly used as a beam calibrator. However, it has been found by Baker et al. (Ba84 and Ba91) that there are three reactions involving copper targets that are more useful for this purpose because they have longer half-lives than the 4.1 hr half-life of 149 Tb. These cross sections have been measured for energies from 30 to 800 GeV and are included in Table 9.6.



Fig. 9.12 Excitation functions of several threshold reactions. [Adapted from (Th88).]

9.5.4 Fission Counters

²³³U, ²³⁵U, and ²³⁹Pu all have relatively large fission cross sections at low neutron energies. The *Q*-values are very large (approximately 200 MeV) so that huge output signals are possible. For higher energy "fast" neutrons, fission reactions become possible for other, lighter nuclei such as bismuth. The cross sections for fast neutrons of these reactions are shown in Fig. 9.13. Fission reactions have been exploited as neutron (or hadron) detectors at accelerators. The fission of ²⁰⁹Bi is especially interesting since this reaction has a threshold of about 50 MeV and also exhibits strong evidence that the neutron and proton-induced fission cross sections are approximately equal. Bismuth has been employed in ionization chambers where the large energy deposited by the fission fragments gives a clear "signature" of this process. Like the use of ¹¹C, it can provide further information about high energy neutrons and resolve ambiguities in the unfolding of spectra from Bonner sphere data. McCaslin et.al. have summarized some interesting results obtained using this process (McC68).



Fig. 9.13 Fission cross sections of some common target nuclides used in fission chambers for fast neutrons. The cross sections for fission of ²³⁵U are much larger at lower energies not shown. [Adapted partially from (Kn79) and from (Sw90).]

9.5.5 Proton Recoil Counters

Knoll (Kn79) describes a variety of techniques for detecting neutrons based upon measuring the energy of recoil particles. The 3 He(n, p) 3 H reaction has a reasonable cross section even into the MeV region but suffers from competition with (n, d) processes and elastic scattering. Elastic scattering of neutrons in which the energy of the recoil particle is measured and correlated with the neutron energy has received a great deal of attention. The most obvious recoil particle to measure is the proton because hydrogenous detector materials (e.g., plastic scintillator) are readily available and also because the proton can receive the most energy in the recoil process. Detector designers have been able to exploit the fact that scattering from hydrogen in the region $E_n < 10$ MeV is *isotropic* in the center of mass frame. Knoll has shown that the probability, $P(E_r)$, of creating a recoil proton having energy E_r is also independent of angle in the laboratory frame within this energy domain (Kn79). Thus the recoil energy is only a function of the incident neutron However, complexities enter the picture because in scintillators, carbon is energy. present along with the hydrogen and can contribute recoil protons. Furthermore, the magnitude of the cross section is a function of neutron energy as is the efficiency of neutron detection in the scintillator. These effects, along with that of finite pulse height

resolution, can lead to the need to resort to unfolding techniques in which the pulse height, indicative of the energy of the recoil proton, is correlated with the average neutron energy which could produce such a pulse. The technique has exhibited some promise in measuring the energy spectra of neutron radiation fields. A good summary is that of Griffith and Thorngate (Gr85) who were able to determine neutron energy spectra in the region between 2 and 20 MeV.

9.5.6 TEPCs and LET Spectrometry

In mixed field dosimetry, a promising technique, now reaching commercial potential is that of the **tissue-equivalent proportional chamber** (TEPC) sometimes referred to as the "Rossi counter" after its inventor, H. Rossi (Ro55). The technique has been described by Brackenbush et al. (Br78). In this instrument tissue equivalent walls are employed to apply the Bragg-Gray principle. In such chambers, the pressure is maintained at low values, only a few torr (a few hundred pascals), so that the energy deposited is kept small. Thus, the energy so deposited will be equal to the linear energy transfer of the particle multiplied by the path length. At these low pressures, the gas-filled cavity has the same energy loss as does a sphere of tissue of diameter about 1 μ m-hence an "equivalent diameter of 1 μ m". In principle, determining the absorbed dose from events in such chambers is a straightforward unit conversion from a measured pulse height spectrum (calibrated in energy) to absorbed dose (in tissue) irrespective of the radiation field;

$$D(\text{rad}) = 1.602 \times 10^{-8} \frac{C}{\rho V} \sum_{i=i_{\text{min}}}^{i=i_{\text{max}}} iN(i) , \qquad (9.28)$$

where the summation is over channels $i (i_{min} \le i \le i_{max})$, see below) corresponding to the radiation type of interest, *V* is the sensitive volume (cm³), ρ is the density (g cm⁻³), *C* converts the channel number to energy in MeV, and *N*(*i*) is the number of counts in channel number *i*.

In such chambers, the transition between photon and neutron-induced events occurs at a pulse height of about 15 keV μ m⁻¹. It is possible to determine the quality factor, Q, from a single TEPC measurement. Under the conditions stated above, one can unfold from the pulse height spectrum the distribution of absorbed dose as a function of LET, D(L), using a formula derived by Rossi (Ro68). The formula is complicated by the fact that one must average over mean chord lengths in the chamber. Such a distribution is used to calculate quality factor, and hence the dose equivalent. The advent of microprocessors has made such instruments available as portable instruments. Fig. 9.14 shows a typical pulse height spectrum for such an instrument. In higher energy fields, dose distributions due to other particles with the same characteristic shapes but larger pulse sizes appear as the ²H, ³H, ³He, ⁴He and even ⁷Li "drop points". This obviously will add complexities to the unfolding procedures in the determination of LET spectra. A good discussion of the application of this technique is given by Vasilik et al. (Va85).



Fig. 9.14 Pulse-height spectra from a tissue-equivalent proportional counter exposed to 1.4 MeV neutrons and ⁶⁰Co γ-rays. [Adapted from (Br78).]

9.5.7 The Recombination Chamber Technique

An adaptation of the ion chamber that has shown considerable potential for usefulness as a dose equivalent meter in a mixed field of radiation is based on the exploitation of recombination phenomena in such chambers. As charged particles interact in such a chamber the gas is ionized. The electrodes will collect only those ions that do not recombine before they reach the cathode. The extent of such **columnar recombination** is dependent upon the average distance between the ions as well as upon the applied voltage. The biasing voltage sets the speed at which the ions migrate to the cathode. For a given voltage, a chamber should exhibit more severe recombination for the radiations having high LET (e.g., neutrons, heavy ions, etc.) than for those having low LET (electrons, photons, and muons). In the high LET situation, the slow moving positive ions are surrounded by a higher density of electrons than they would be in under conditions of low LET. Zielcyznski (Zi62) did the initial work on this topic.

Baarli and Sullivan reported similar results over a somewhat larger range of values of quality factor Q (2 < Q < 20) and further refined the technique (Ba65). It turns out that the current, *i* (or charge if integrated over time), measured in a given radiation field, is related to the applied voltage *V* by the following approximate expression:

$$i = kV^n. (9.29)$$

The power parameter, *n*, is approximately proportional to the quality factor *Q* and *k* is a constant proportional to the intensity of the radiation field. Cossairt et al. (Co84) have measured this effect using a mixed field of γ -rays and neutrons from a Pu-Be source. The results are shown in Fig. 9.15 over the range $1 \le Q < 7$. The relationship between *Q* and *n* determined in (Co84) for one particular chamber was fit linearly by

$$n = 0.00762 + 0.016Q, \tag{9.30a}$$

or by using a power law,

$$n = 0.019Q^{0.95}$$
. (9.30b)

Patterson and Thomas (Pa73) have reported similar results over a somewhat larger range of Q (2 < Q < 20). Typically, the response of such a chamber is measured as a function of applied voltage for the special chamber provided for the purpose over some voltage range, say, $20 \le V \le 1200$ volts. In fields that are not steady with time, the response



Fig. 9.15 Response of a recombination chamber as a function of quality factor Q obtained in mixed fields using radioactive sources. Two different fits to the data are presented [Reproduced from (Co84) and (Co85b).]

typically needs to be normalized against some instrument that accurately measures the intensity of the radiation field. The method of least squares is then applied to determine n by taking advantage of the fact that Eq. (9.29) can be rewritten as

$$\ln i = \ln k + n \ln V \,. \tag{9.31}$$

In typical measurement, such a log-log fit to the data is of moderately good quality. The quality factor, Q, then, can be determined directly from n using a version of Eq. (9.30) determined for the particular recombination chamber used. Fig. 9.16 shows the response measured in a field known to be dominated by high energy muons (Q = 1). Data taken in the iron leakage spectrum described in connection with Fig. 6.8 are shown in Fig. 9.17. Measurements of this type have been used to check the quality factors obtained in the unfolding of Bonner sphere data. Table 9.7 illustrates the typical agreement between these entirely different techniques for diverse radiation fields.

Zel'chinskij and Zharnovetskij (Ze67) proposed using two chambers placed in the radiation field of interest; one operated at a low voltage and other at a high voltage. The differences in responses read out by the two chambers would then be proportional to the dose equivalent rate. It turns out that measuring differences in ion chamber currents found in practical chambers is difficult due to the small currents and electrical leakage problems associated with electrical feed-throughs and cable connectors.



Fig. 9.16 Recombination chamber response as a function of chamber potential in a radiation field nearly completely consisting of high energy muons. [Reproduced from (Co87).]



Fig. 9.17 Recombination chamber response functions measured both before (**top**) and after (**bottom**) the placement of additional shielding in the radiation field described in Fig. 6.8. [Reproduced from (E186).]

Table 9.7Average quality factors obtained for various neutron energy spectrameasurements at Fermilab. [Adapted from (Co88).]

Description of Radiation Field	Technique	
	Unfolding	Recombination
Mixed field of neutrons and muons (Co 87)	1.4 <u>+</u> 0.2	1.1 <u>+</u> 0.3
Iron leakage spectra before shielding was added (Fig. 6.8b) (El86)	5.4 <u>+</u> 0.2	6.0 <u>+</u> 0.6
Iron leakage spectra after shielding was added (Fig. 6.8c) (El86)	2.5 <u>+</u> 0.3	3.0 <u>+</u> 0.3
Spectrum in a labyrinth (Fig. 6.7) (Co85b)	3.1 <u>+</u> 0.7	3.4 <u>+</u> 0.1

Höfert and Raffnsøe (Hö80) have measured the dose equivalent response of such an instrument as a function of neutron energy and obtained the results in Table 9.8.

Neutron Energy (MeV)	Dose Equivalent Response (10 ⁵ Coulombs Sv ⁻¹)	Error (%)
thermal	0.830	10.0
0.0245	2.579	12.1
0.1	1.451	6.2
0.25	1.585	6.1
0.57	1.215	5.2
1.0	1.215	5.2
2.5	1.112	6.1
5.0	0.840	5.2
15.5	0.728	5.2
19.0	0.998	12.1
280.0	0.782	10.1

 Table 9.8 Dose equivalent response and measurement errors for recombination chamber as a function of neutron energy. [Adapted from (Hö80).]

9.5.8 Counter Telescopes

Since the dose equivalent per fluence for muons varies so little over a wide range (see Fig. 1.4), scintillation telescopes provide an attractive method for assessing pure muon fields. At suitable distances and at forward angles, muons will dominate the radiation fields and the result is that little or no discrimination against other particles is necessary.

At Fermilab a pair of 20.32 cm square by 0.635 cm thick plastic scintillators has been used routinely (Co83). The separation distance between these "paddles" provides moderate directional sensitivity when a coincidence is required between the two scintillator paddles in a relatively parallel beam of muons. An aluminum plate, 2.54 cm thick, is employed in the gap between the two scintillators to reduce false coincidences due to recoil electrons (so-called " δ -rays") produced in collisions occurring in the first scintillator that might reach the second if the aluminum were absent. These plates are mounted in an all-terrain vehicle, called the Mobile Environmental Radiation Laboratory (MERL), and are powered by an on-board electrical generator. (The MERL is also used for neutron measurements with a DePangher long counter and other detectors.) A microwave telemetry system provides gating pulses and proton beam intensity information so that normalized beam-on and beam-off (background) measurements can be taken simultaneously. The paddles were chosen to provide sufficient sensitivity to obtain statistical errors at the 20 per cent level in remote locations receiving annual dose equivalents in the fractional mrem range in a scan lasting an hour or two. In such a scan, the detectors are moved across a region of elevated muon flux density, stopping at several loations to acquire data. In these detectors, a muon beam perpendicular to the detectors yields 1.72×10^5 counts per minute per mrem/hour (or 1.03×10^7 counts mrem⁻¹). The normal singles background (i.e., the background of an individual scintillator not counted in coincidence with the other member of the pair) due to cosmic rays at Fermilab is approximately 400 counts per minute.

Smaller, more portable systems can be useful in conducting muon surveys. Fermilab has built such a system, called a **muon finder**, consisting of a pair of small plastic scintillators mounted in a compact package which is battery powered and can be carried by one person. It is read out by scalers and can record both singles and coincidence rates. The ratio of the two can be used to "find" unknown muon sources; hence the name of the detector. Also, the separation distance can be adjusted to enhance or reduce the directional sensitivity. This system has been described by Vaziri, et al. (Va04).

The parameters of this system are given in Table 9.9. Of course, the use of such scintillators, especially in the "singles" mode, in mixed fields of muons and neutrons requires that one must be aware of the fact that the plastic scintillators have nonzero detection efficiency for the neutrons. Vylet has used the values of total cross sections to calculate the neutron detection efficiency of the detectors described above for neutrons over a range of energies (Vy91). The results are given in Fig. 9.18. In this figure, effects due to the first and successive collisions (labeled "Total") as well as those due to just the first collisions (labeled "1^{st»}) with hydrogen atoms are given. The total efficiencies at the upper end of the energy region measured were an efficiency of 0.058 for the MERL paddles and 0.0235 for the muon finders.

Table 7.7 Tarameters of the muon mu	ter used at rerinnab.
Scintillator diameter	2.1 cm
Scintillator thickness	0.635 cm
Scintillator area	3.6 cm^2
Scintillator spacing	0.5 to 8.9 cm
Half-angle cone of sensitivity	0.9 to 0.2 radians (51 to 11.5 deg. half-angle)
Dose equivalent calibration (muons \perp dete	ectors) 90 muons/µrem
Dose equivalent rate calibration (muons \perp	detectors) 25 muons/sec per mrem/hour

 Table 9.9 Parameters of the "muon finder" used at Fermilab.



Fig. 9.18 Calculated neutron efficiencies of scintillation counters used in the "singles" mode at Fermilab as a function of neutron energy as described in the text. [Adapted from (Vy91).]

Problems

- 1. A cylindrical ion chamber is 5 cm in radius and 20 cm long. It is filled with methane (CH₄) at 1 one atmosphere absolute pressure. It is bombarded by a uniform flux density of high energy (minimum-ionizing) muons incident perpendicularly to one of the ends. One can safely make the assumption that the passage of the muons through the entire length of the chamber represents insignificant degradation of the muon energy or direction. The dose equivalent rate in the radiation field is 0.1 mrem hour⁻¹.
 - a) Calculate the electric current that will be drawn from this chamber that represents the "signal" to be measured and correlated with the dose equivalent rate. One could use Table 1.2 to obtain values of $(dE/dx)_{min}$ and to obtain the density of CH₄.
 - b) If the charge liberated in the chamber is collected (i.e., integrated electronically) for 1 second and the chamber and circuit represent a capacitance of 10^{-10} Farads, calculate the size of the signal pulse in volts if one neglects any "pulse-shaping" of the readout electronics.
- 2. Consider the detector based on the 25.4 cm moderating sphere for which the corresponding response curve is displayed in Fig. 9.8.
 - a) Calculate the approximate absolute intrinsic detection efficiency for neutrons. This is to be done for the $2 < E_n < 8$ MeV energy domain and the sharp peaks in the detector response curve are to be ignored (i.e., averaged out). In this problem, 100 % efficiency is defined to be 1 count generated for every neutron that strikes the sphere. Assume the incident neutrons to be aimed at the detector originating from a "point" source" despite the fact that this is not quite true.
 - b) Since the LiI detector only responds to thermal neutrons, calculate the efficiency with which the moderator transforms fast neutrons incident upon it into thermal neutrons present at the LiI. For this calculation, neglect any "dopants" in the LiI, assume that the Li is "natural" lithium with respect to isotopic abundance and use the fact that the atomic weight of iodine is 127. The density of LiI is 3.5 g cm⁻³. Assume that the detector is 100% efficient in detecting thermal neutron captures within its volume.

- 3. A BF₃ proportional chamber is used in a DePangher long counter. This detector, when placed in a certain neutron field that is known to be dominated by neutrons of approximately 5 MeV kinetic energy, has a response due to neutrons of 1 count/minute. The detector sensitivity is that discussed in the text. The counter operates at one atmosphere absolute pressure, the atomic weight of boron is 10.8 while the atomic weight of fluorine is 19. At STP the density of BF₃ is 2.99 grams liter⁻¹.
 - a) What is the dose equivalent rate of this radiation field?
 - b) If the radiation field persists full time, is this detector sufficiently sensitive to detect a dose rate of 10 mrem year⁻¹?
 - c) In this radiation field, high energy minimum ionizing muons pass through this detector, including the proportional counter. The largest muon signals in the proportional counter will obviously result when the muons pass lengthwise through the tube. If the tube is 40 cm long, what will be the size of the largest muon-induced signal relative to the neutron-induced signal? Is it likely that a simple discriminator circuit can be used to eliminate the muon-induced signals? It is quite permissible to estimate the value of $(dE/dx)_{min}$ by roughly interpolating among the values tabulated in Table 1.2.
- 4. One needs to understand the sensitivity of the technique of using the nuclear reaction ${}^{12}C(n, 2n){}^{11}C$ in plastic scintillator to measure dose equivalent rate external to thick concrete or earth shielding near a high energy accelerator. The detector discussed in the text used by Moritz has a sensitive volume of approximately 100 cm³ (a 5 cm diameter by 5 cm long cylinder). The NE102A scintillator, from Knoll (Kn79), has a density of 1.032 g cm⁻³. This detector is nearly 100 % efficient at sensing the 0.511 MeV annihilation photons produced in the course of the ${}^{11}C$ decay.
 - a) This detector is irradiated in a particular radiation field external to such accelerator shielding. The irradiation, which is steady in time, is of sufficient length in time to result in saturation of the production of ¹¹C in the scintillator. After the beam is turned off, the detector counts at a rate of 10 counts per minute (including appropriate decay-correction to the instant of beam shutdown). Calculate the flux density of neutrons with $E_n > 20$ MeV during the irradiation and use the result along with Stevenson's conclusion concerning the conversion from the flux density of neutrons with $E_n > 20$ MeV to dose equivalent to determine the dose equivalent rate.
 - b) Assuming this count rate is the smallest that can be reliably detected, how much smaller in volume can the detector be for it to barely be sensitive to a dose equivalent rate of 2 mrem hour⁻¹?

This appendix provides brief summary descriptions of some of the more prominent Monte Carlo codes used at modern particle accelerators. The reader should be cautioned that most of these codes are being constantly improved and updated. The wisest practice in using them is to consult with the authors of the codes directly who can provide detailed, current in formation.

CASIM

A. Van Ginneken developed this "Cascade Simulation" program (Va75). It was designed to simulate the average behavior of hadrons in the region 10 to 1000 GeV and has been extended to 20 TeV (Va87). It uses inclusive production distributions directly in order to obtain the particles to follow. The particle production algorithm is based upon the Hagedorn-Ranft thermodynamic model. Only one or two high energy particles are created in each collision and these carry a weight related to the probability of their production and the energy carried with them. Path length stretching and particle splitting have been introduced. Electromagnetic showers resulting from π^{o} production are calculated using the companion code AEGIS. Simple "standardized" geometries are available. However, the user generally writes a FORTRAN subroutine to set up the geometry of interest. This subroutine consists of "logical" (i.e., "IF", etc.) statements used to deduce the material or magnetic field in which a particle being tracked is found at a given "time" in the calculation from the particle's spatial and directional coordinates. The program readily allows magnetic fields to be used. A muon version called CASIMU (now MUSIM) has been written (Va87). The accuracy of the hadron version has been verified for energies up to 800 GeV (Co82a and Co85a). The muon version has also been verified for energies up to 800 GeV for production and transport of muons in real-life, complicated shields (Co89a and Co89b). Normally, CASIM is not set up to follow particles with momenta less than 300 MeV/c, which corresponds to a kinetic energy of 47 MeV for nucleons. All low energy phenomena, then, is obtained by matching energy spectra and fluence at this energy with results of codes capable of tracking lower energy particles (e.g., HETC, FLUKA, and MARS). At Fermilab, CASIM has been replaced by MARS as the code of choice. Results obtained using CASIM continue to serve as useful benchmarks.

EGS

EGS, the "Electron Gamma Shower" code is a powerful code for calculating electromagnetic cascades. A recent version is EGS4. A complete description of this code system has been written by Nelson et al. (Ne85, Ne90). This program provides a Monte Carlo analysis of electron and photon scattering including shower generation. In its standard usage, it does not calculate hadron or muon production directly. The lower limit of its validity is about 10 keV while the upper limit of its validity is at least 1 TeV. Possible target materials span the periodic table. As the electron encounters target atoms, it is scattered randomly to mimic the known mechanisms of electron scattering. When secondary particles arise, they are loaded into a stack from which EGS4 selects sequentially the lowest energy particle and then traces out its further path until it leaves the target or until its energy falls below a selected cut-off value. The final kinematical

and charge properties of all the particles are noted and summed for all particles in the shower concluding with a "history" of all of them. Improvements with the code are continuously being made. The code is a fundamental tool at many laboratories that have electron accelerators. The code has been found to be extremely useful in applications in medicine and also in modeling the performance of high energy physics apparatus. The EGS code system is available from the Stanford Linear Accelerator Center.

FLUKA

FLUKA is an integrated, versatile multi-particle Monte Carlo program, capable of handling a wide variety of radiation transport problems. Its energy range extends from one keV (for neutrons, thermal energies) to thousands of TeV. FLUKA can simulate with a similar level of accuracy the propagation of hadronic and electromagnetic cascades, cosmic muons, slowing-down neutrons and synchrotron radiation in the keV region. An original treatment of multiple Coulomb scattering allows the code to handle accurately some challenging problems such as electron backscattering and energy deposition in thin layers. In a fully analog mode, FLUKA can be used in detector studies to predict fluctuations, coincidences and anti-coincidences. On the other hand, a rich supply of biasing options makes it well suited for studies of rare events, deep penetration and shielding in general. This code originated as high-energy particle transport code developed by a CERN-Helsinki-Leipzig collaboration, principally by J. Ranft as discussed by Aarnio et al. (Aa86). More recently, it has been completely rewritten and extended to low energies as discussed by Fassò et al. (Fa93). It handles more than 30 different particles, including neutrons from thermal energies to about 20 TeV and photons from 1 keV to thousands of TeV. Several biasing techniques are available. Recoil protons and protons from N(n,p) reactions are transported explicitly. This code is currently available from the Stanford Linear Accelerator Center.

HETC and LAHET

This code, developed over many years under the leadership of R. G. Alsmiller at the Oak Ridge National Laboratory, is considered by some to be the benchmark hadron shielding code of choice. It has been upgraded many times and can, in suitably augmented versions, follow particles from the 20 TeV region down to thermal energies. It is an extremely flexible code but has the important disadvantage that the individual events are written to mass storage. It is the responsibility of the user to write a program to analyze the results. In terms of CPU-time HETC is also relatively slow so that calculations to be done should be carefully selected. It is seen to be preferable to use selected HETC runs to calibrate other faster, but less accurate codes. It has been described by Armstrong (Ar80) and Gabriel (Ga85). It now uses the same event generator used for FLUKA. A modified version of this code, developed at the Los Alamos National Laboratory (LANL) as LAHET, has been described by Prael and Lichtenstein (Pr89). It is available from the Los Alamos National Laboratory. This variant permits the transport of neutrons, photons, and light nuclei up to ⁴He and employs the geometric capabilities of the MCNP code.

MARS

The MARS Monte Carlo code system has been under continuous development over a number of years by N. Mokhov et al. (Ka89, Mo95, Kr97, Mo04). Early results were compared by Mokhov and Cossairt (Mo86) with those obtained using then-current versions of CASIM and FLUKA with good agreement. The code allows exclusive and fast inclusive simulation of three-dimensional hadronic and electromagnetic cascades for shielding, accelerator, and detector components in the energy range from a fraction of an electron volt up to 100 TeV. The current version, MARS15, uses the phenomenological model for inclusive hadron- and photon-nucleus interactions for E > 5 GeV, exclusive cascade-exciton model at 1 MeV < E < 5 GeV, and, by using the LAQGSM event generator, full theoetically consistent modeling of exclusive distributions of secondary particles, spallation, fission, and fragmentation products for hadron and heavy-ion beams of any energy. MARS15 includes photo- and electro-production of hadrons and muons, advanced algorithms for the 3-body decays, precise particle tracking in magnetic fields, synchrotron radiation by electrons and muons, extended histogramming capabilities and improved material description and computational performance. Along with direct energy deposition calculations, a set of dose conversion per fluence factors for all particles including neutrinos is incorporated. The code includes links to the MCNP4C code for neutron and photon transport below 20 MeV, to the ANSYS code for thermal and stress analyses, and to the MAD and STRUCT codes for lattice description for multi-turn particle tracking in large synchrotrons and collider rings. The geometry module allows the use of a set of the pre-defined shapes, arbitrary user-defined 3-D descriptions, the object-oriented engine coupled with VRML/2.0 (an approved standard web-oriented three dimensional geometry description), or direct use of MCNP and FLUKA geometry input desks. The code is provided with a user-friendly graphical-use interface for geometry and calculated results visualization and debugging. A parallelized version of the code can run in a multi-processor mode. The developments were induced by numerous challenging applications - Fermilab accelerator, detector and shielding upgrades, Large Hadron Collider machine and detector studies, muon and electron-positron colliders etc as well as by a continuous desire to increase code reliability, flexibility and user friendliness. This code is continously updated and improved and is can be obtained from Fermilab. It is likely the most advanced high energy code available.

MCNP

MCNP is a general-purpose Monte Carlo N-particle code that can be used for neutron, photon, electron, or coupled neutron/photon/electron transport, including the capability to handle situations involving nuclear criticality. This code has been developed at the Los Alamos National Laboratory and is well documented in LANL reports (e.g., Br97). The code treats an arbitrary three-dimensional configuration of materials in geometric cells bounded by first- and second-degree surfaces and fourth-degree elliptical tori. The neutron energy regime is from 10⁻¹¹ MeV to 150 MeV, and the photon and electron energy regimes are from 1 keV to 1000 MeV. For neutrons, all reactions given in a particular cross-section evaluation (such as ENDF/B-VI cross section database) are accounted for. Thermal neutrons are described by both the free gas and thermal particle

scattering models. For photons, the code takes account of incoherent and coherent scattering, the possibility of fluorescent emission after photoelectric absorption, absorption in pair production with local emission of annihilation radiation, and bremsstrahlung. A continuous slowing down model is used for electron transport that includes positrons, x-rays, and bremsstrahlung but does not include external or self-induced fields. Important standard features that make MCNP very versatile and easy to use include a powerful general source, criticality source, and surface source; both geometry and output tally plotters; a rich collection of variance reduction techniques; a flexible tally structure (including a pulse-height tally); and an extensive collection of cross-section data. The current version is available from the Los Alamos National Laboratory.
This appendix is intended to supplement Section 3.2.3 to provide more detailed information about synchrotron radiation and its ramifications, especially at modern light sources. The texts of Wiedemann (Wi03) and Margaritondo (Ma88) provide much detailed information on both the synchrotron radiation itself and the modern "light source" facilities that have been built to advantageously utilize it. An important review of radiation protection considerations at synchrotron radiation facilities has been provided by Liu and Vylet (Li01) in addition to that due to Swanson (Sw90). In this section, the figures and equation numbers of the main text are given in small square brackets [].

B.1 General Discussion of the Phenomenon

The movement of electrons in a curved orbit results in their centripetal acceleration. This gives rise to emission of photons. At nonrelativistic energies, this radiation is largely isotropic. However, for relativistic energies, a condition readily achieved by accelerated electrons, the photons emerge in a tight bundle along a tangent to any point on a circular orbit. For a single electron, or a small bunch of electrons orbiting together, the photon beam will sweep around like a searchlight. Figure B.1 [Fig. 3.5] shows this bundle.



Fig. B.1[3.5] Synchrotron radiation pattern for relativistic particles at the instantaneous location denoted by "electrons". Twice the characteristic opening angle, θ_c , is shown as the shaded region.

While the exact shape of this bundle is a somewhat complicated function of the energy of the radiation emitted and the electron energy, it is reasonable to take the **characteristic angle**, θ_c , (i.e., the angle of 1/e of the zero degree intensity) of this "lobe" to be:

$$\theta_c = \frac{1}{\gamma} = \sqrt{1 - \beta^2} \text{ radians,}$$
(B.1)[3.13]

with γ being the relativistic parameter defined in Eq. (1.10). The energy spectrum of the photons emitted by electrons captured in such a circular orbit turns out to be a standardized function the shape of which is independent of the electron beam energy. It is given by an integral of a modified Bessel function of the third kind and thus numerical

tabulations of it are available, but the mathematical details are not further needed in the present discussion. Fig. B.2 [Fig. 3.6] shows this function. The resultant photon spectrum is called a **bending magnet spectrum**.



Fig. B.2 [3.6] Universal synchrotron radiation spectrum. The graph gives the relative power as a function of photon energy in units of characteristic energy, ε_c . This spectrum yields unity if integrated over all energies. [Adapted from (Sw90).]

The median energy of the power spectrum, sometimes called the characteristic energy or critical energy, \mathcal{E}_c , is given in terms of the total energy, W (GeV), and bending radius, R (meters) by

$$\varepsilon_c = \frac{2.218W^3}{R}$$
 (keV). (B.2) [3.14]

For singly-charged particles of other masses, m_X , the characteristic energy is obtained by multiplying this result by a factor of $(m_e/m_X)^3$. One can see that the characteristic energy for synchrotron radiation for *protons* having the same total energy as electrons is far, far lower. As may be obvious later, sometimes it is convenient to specify these and other quantities as functions of the magnetic field *B* (Tesla) which creates the circular orbit of radius *R* for particles of momentum *p* (GeV/c) by recalling Eq. (2.27):

$$R = \frac{p}{0.29979qB} \text{ (meters).} \tag{B.3} [2.27]$$

If one substitutes for R; recalls that q = 1 for electrons; ignores the distinctions between

kinetic energy, momentum, and total energy for *relativistic* electrons; and combines constants;

$$\mathcal{E}_c = 0.6649 W^2 B \text{ (keV)} \tag{B.4}$$

For relativistic conditions, $\gamma >> 1$, the mean number of photons emitted per complete revolution is

$$N_{\gamma} = \frac{5\pi}{\sqrt{3}} \alpha \gamma, \qquad (B.5)$$

where α is the fine structure constant of atomic physics ($\approx 1/137$, see Table 1.1). Since this distribution has considerable "skewness", again for $\gamma >> 1$, the **mean energy per photon**, $\langle \varepsilon \rangle$, is

$$\langle \varepsilon \rangle = \frac{8}{15\sqrt{3}} \varepsilon_c.$$
 (B.6)

As an electron circulates in this circular orbit, the **energy loss per revolution** is given by

$$\delta E = \frac{0.08846}{R} W^4 \text{ (MeV)}, \tag{B.7}$$

with W in GeV and R in meters. An alternative form that is, again, useful arises from substituting for R employing Eq. (B.3);

$$\delta E = 0.02652W^3 B$$
 (MeV), (B.8)

with *B* in Tesla.

If the orbit is a circle with continuous, uniform bending around the circumference and with straight sections of "negligible" length, it should be clear that a circulating current, I (milliamperes) can be connected with the **radiated power**, P (watts). First, determine the number of electrons/sec per milliampere current;

$$I(\text{milliamperes}) = I\left(\frac{10^{-3}\text{Coulombs}}{\text{sec}}\right) \times \left(\frac{1 \text{ electron}}{1.602 \times 10^{-19} \text{ Coulombs}}\right)$$
$$= I\left(\frac{\text{electrons}}{\text{sec} \times \left\{1.602 \times 10^{-16}\right\}}\right).$$

Then one can derive the radiated power from Eq. (B.7);

$$P = \frac{0.08846W^{4}}{R} \frac{\text{MeV}}{\text{electron}} I \left(\frac{\text{electrons}}{\text{secx} \{ 1.602 \times 10^{-16} \}} \right) \times \frac{1.602 \times 10^{-13} \text{ Joule}}{\text{MeV}}$$

$$= \frac{88.46W^{4}I}{R} \frac{\text{Joules}}{\text{sec}} = \frac{88.46W^{4}I}{R} \text{ watts.}$$
(B.9) [3.15]

Again using Eq. (B.3), this can be expressed in terms of the magnetic field;

$$P = 26.52W^3BI$$
 watts. (B.10)

For singly-charged particles of other masses, m_X , the radiated power is obtained by multiplying this result by a factor of $(m_e/m_X)^4$. Again, one can see why all synchrotron radiation facilities (i.e., "light" sources) are based upon circulating electrons, not protons or heavier particles. However for ultra high energy proton accelerators (e.g., the Large Hadron Collider at CERN), the need to replenish the energy lost through synchrotron radiation constitutes a significant electrical power demand.

Synchrotron radiation possesses an additional property not further discussed in detail here; the fact that the photons are polarized to rather high degree, greater than 80 % is typical, in the plane of the ring in which they orbit. These large polarizations can be further manipulated and are extremely beneficial to the users of light sources. They also can result in asymmetries in the radiation production by these accelerators.

B.2 Insertion Devices

The researchers who use the modern light sources are not limited to the broad band of photons obtained from the general bending of the electron beam around its circular orbit. It was realized at an early stage in the development of this technology that if one were to insert a set of bending magnets of alternating polarities into a straight section of a ring, *smaller* bending radii over short distances could be produced that would result in radiation of *higher* energy photons according to Eqs. (B.2) or (B.4). Fig. B.3 shows such a **wavelength shifter** in a schematic way:



Fig. B.3 Schematic of a wavelength shifter showing the three magnets involved; the magnetic field strength, B(z), as a function of longitudinal coordinate z; and the electron trajectory. λ_p is the length of a **period** of group of such magnets, here consisting of a pair. Since the pole pieces are typically short, the magnetic field strength may have an approximate sinusoidal dependence on z as depicted here. [Adapted from (Wi03).]

It is clear while more energetic photons would be emitted, their intensity would be limited by the short fraction of the time of each orbit the individual beam electrons are deflected by this higher magnetic field. It was discovered that if one were to line up a series of such magnets of alternating polarities in a row, the intensity could be increased. If there are N_m such pairs of magnet poles (i.e., "**periods**") in the system, then one will get $2N_m$ times the photons provided by one of them, neglecting end effects. These magnets could be dipoles of alternating polarities lined up in any plane. In practice they are generally set to bend charged particles in the bending plane of the storage ring. This avoids some complications for accelerator operations since it limits the coupling between horizontal and vertical betatron oscillations in the storage ring.

The magnetic field strength in these three magnets can be of any strength so long as there is no net deviation of the overall orbit of the electrons, aside from corrections that might be needed to compensate for additional dispersion and aberrations introduced by this "device". Components of this type introduced into storage rings to create desired, specialized photon energy spectra are called **insertion devices**. A typical modern light source will contain a number of such devices designed to create particular photon beam properties. Some employ permanent magnets while others utilize superconducting magnet technology to achieve high magnetic fields. Sophisticated, improved versions have been developed that are not discussed here. Figure B.4 is a conceptual picture of such a device.



Fig. B.4 Sketch of a ypical insertion device. [Provided by courtesy of J. Liu and V. Vylet.]

A special parameter is useful in this discussion. Consider a device consisting of a large number of alternating magnet poles. The spacing of each *pair* of poles, λ_p (as defined in Fig. B.3), constitutes the length of the period. Because the individual pole pieces are often short compared with the dimensions of the field gaps, truly "uniform" dipole field conditions are generally not achieved. Instead, the magnetic field component perpendicular to the bending plane, here denoted B_y , is often approximated by a sinusoidal dependence on the longitudinal coordinate, *z*;

$$B_{y} = B_{o} \sin \frac{2\pi z}{\lambda_{p}}.$$
 (B.11)

Now one can calculate the angle α_m , the maximum deflection of the electrons away from the central axis as they proceed along the insertion device using Eq. (B.3) by performing an integration over the longitudinal coordinate z. Given the size of practical insertion device pole pieces, it is useful to work with z and λ_p in centimeters. Performing the integration;

$$\alpha_{m} = \frac{2.9979 \times 10^{-3} B_{o}}{p (\text{GeV/c})} \int_{o}^{\lambda_{p}/4} dz \sin \frac{2\pi z}{\lambda_{p}} = \frac{\lambda_{p}}{2\pi} \frac{2.9979 \times 10^{-3} B_{o}}{p (\text{GeV/c})} \left[-\cos \frac{2\pi z}{\lambda_{p}} \right]_{0}^{\lambda_{p}/4}$$
(B.12)
= $\left(4.771 \times 10^{-4} \right) \frac{B_{o} \lambda_{p}}{p}$ (radians).

One multiplies this by the relativistic parameter of the electron beam, γ , to define a new dimensionless parameter, *K*. Since the electrons that produce useful synchrotron radiation are highly relativistic;

$$\gamma = \frac{W}{m_o c^2} \approx \frac{pc}{m_o c^2}$$
, and $K = \gamma \alpha_m = (4.771 \times 10^{-4}) \frac{B_o \lambda_p}{m_o c^2} = 0.934 B_o \lambda_p$, (B.13)

with B_o in Tesla, λ_p in cm, and the rest energy of the electron $(m_o c^2)$ in GeV. *K* is called the **wiggler strength parameter** or **deflection parameter**. Its role can be better understood with the help of Fig. B.5. If one recalls that the cone of emission of the synchrotron radiation has an approximate half-width of $1/\gamma$, for K > 1, the maximum deflection α_m is thus larger than the cone of emission (as illustrated in the bottom frame of Fig. B.5. In such circumstances the insertion device is called a **wiggler** and the synchrotron radiation produced has a bending magnet energy spectrum shape.



Fig. B.5 **Top**: Definition of the angle θ at which radiation is emitted by an undulator inserted in a straight section of a storage ring. **Bottom**: Angular amplitude of the half-angle of the cone of emission of radiation, $\approx \gamma^{-1}$, and maximum deflection angle of the electron trajectory caused by an insertion device, α_m [Adapted from (Ma88).]

For K < 1, the divergence due to the magnetic deflections is *smaller* than the intrinsic cone of emission and the device is then called an **undulator**. In an undulator, since the deflections occur *within* the cone of emission, interference effects can occur. In fact, these are exploited to provide approximately monochromatic photons or spectra with other desired properties. While wigglers are useful for hardening the energy spectrum of the photons, undulators can be used to create very "bright" beams of nearly monoenergetic photons or a spectrum of photons delivered in a few narrow bands. The increased brightness is due to the smaller dispersion due to the bending magnet deflections. Avoiding the details of a somewhat complicated derivation, the **undulator frequency**, v_1 , of the photons produced is given by (Wi03)

$$\nu_{1} \approx \frac{2c\gamma^{2}}{\lambda_{p}} \frac{1}{\left(1 + K^{2}/2 + \gamma^{2}\theta^{2}\right)}$$
(B.14)

for small, but not negligible, values of K and angles of emission, θ , in radians. Since K is a function of magnetic field strength and magnet pole spacing, this frequency can be adjusted to some degree by altering those parameters. At "intermediate" values of K, other spectral peaks at harmonics of the above frequencies become possible. It is of course easy to obtain the photon energy with λ_p in cm by applying Planck's constant;

$$E_{1} = h\nu_{1} \approx \frac{(2.480 \times 10^{-7})\gamma^{2}}{\lambda_{p}} \frac{1}{\left(1 + \frac{K^{2}}{2} + \gamma^{2}\theta^{2}\right)}$$
(keV). (B.15)

One should consider the power that can be emitted in the tightly focused undulator beam. For an undulator of N_m periods, the power emitted (Ma88) is given by:

$$P_{tot} = \frac{(1.9 \times 10^{-12}) N_m \gamma^2 K^2 I(\text{mA})}{\lambda_p(\text{cm})} \qquad (\text{kW}). \tag{B.16}$$

Unlike for the bending magnet situation, this power would be emitted into a very small $1/\gamma$ cone, not in the "pancake-shaped" distribution around the entire circumference representative of the bending magnet situation.

Fig. B.6 shows some examples of spectra emitted by different types of insertion devices. Obviously, these devices continue to evolve and more complicated ones are being developed to address specific research needs. Collimation is often used to select desired portions of these spectra, optimized for their intended use.



Fig. B.6 Different examples of insertion device emission, compared to bending magnet radiation.
Case a is the line emission from an undulator, seen through a pinhole which limits the angular acceptance. Case b is a strong field device (not described in this note), again seen through a pinhole so as to limit the angular acceptance. Upon broadening, due to a small number of periods, this line spectrum becomes similar to the bending magnet spectrum (Cases c and d). [Adapted from (Ma88).]

B.3 Radiation Protection Issues Specific to Synchrotron Radiation Facilities

Obviously, all the radiation protection concerns discussed elsewhere in this text pertinent to electron accelerators of the same energies and intensities apply to synchrotron radiation facilities as well. These include the production of bremsstrahlung photons, the production of neutrons and high energy particles, the development of electromagnetic cascades, and the production of induced radioactivity. However, there are some unique phenomena prominent at these facilities that will be reviewed here. These and related topics have been studied extensively; see references (Ri82), (Ba89), (Tr90), (Ip94), (Li95), and (Li05).

B.3.1 Operating Modes

Synchrotron radiation sources largely operate as storage rings. To accommodate insertion devices and experimental apparatus, these storage rings often have relatively long straight sections. Operating modes need to be considered. Typically, the electron beam is produced by an injector accelerator of some type and injected into the main storage ring in an injection event. Following injection the beam is typically smoothed out for several thousand turns before being added to the stored beam. Electrons are typically lost during the injection process on limiting apertures designed to "clean-up" the beam for storage or lost around the ring (e.g., by turning off the RF). Then, the beam is used for the intended research purposes for long periods of time. Upon conclusion of a given

period of storage ring operations (i.e, at the end of a "store"), the beam is generally disposed of in a beam absorber, and the cycle is repeated. A relatively recent advancement made to improve the quality of operations is the capability to *replenish* the beam by delivering electrons from the injector to the storage ring in a so-called **top-off mode**.

Often the personnel protection requirements and beamline access restrictions imposed on the researchers are considerably different during injection events and storage ring operations due to the differences in the levels and types of radiological hazards presented. Typically, radiological problems are most prominent during the injection events because at that time, errors of beam tuning may result in point losses and the rate of beam delivery can be large and is intrinsically limited only by the output of the injector. Beam loss "accidents" may occur. Obviously this applies also to the top-off mode of operation. During pure storage ring operations, since accelerator orbits have been established to achieve a useful beam lifetime, inductive time constants render sudden, large losses due to mistuning or collapse of the magnetic field (e.g., during a power failure) much less probable. Point losses can, however, occur due to other types of events such as the sudden closure of vacuum valves or some other unintended movement of material into the beam. However, while the stored beam *current* may be significant, during the storage ring mode (i.e., not during injection or topping-off), the total number of stored electrons is limited, and may serve to apply an upper limit to the radiological consequences of beam loss events. At some facilities devices called beam stops, shutters, or injection stoppers are inserted into the front end of each beamline and used to protect personnel and equipment from the consequences of beam losses during injection events. Obviously it is imperative to fully understand the beam loss characteristics at every stage of operation. Fig. B.7 shows the layout of a portion of a typical synchrotron radiation facility showing the installation of some types of safety equipment used in various operational modes.



Fig. B.7 Typical synchrotron radiation facility experimental installation. The storage ring is at the bottom of the frame. So called "ratchet-walls" separate the experimental installations from the main storage ring. [Adapted from (NC03).]

B.3.2 Gas Bremsstrahlung – Straight Ahead

At these facilities, the decay of the stored beam will be dominated by scattering from the residual gas particles. Though the vacuum can be made to be very good, the path lengths of the electrons in a storage ring mode are extremely long, when huge numbers of orbits are taken into account. Also, the synchrotron radiation photons themselves can induce outgassing in certain materials that may *increase* residual pressures within the "vacuum". The process of beam interaction in the residual gas is obviously a "thin target" phenomena, otherwise the electron beam could not be stored! Under some circumstances, equipment damage concerns are important. Following scattering events the electrons will spiral radially inward and be lost. Workers at various laboratories have developed computational methods using both analytical and Monte Carlo techniques to address these matters. In the discussion which follows here, analytical methods will be used to illustrate the results.

It has been found that **gas bremsstrahlung** has a nearly 1/k energy spectrum (with k denoted as the photon energy to distinguish against the electron beam energy). The spectrum extends essentially from zero up to the kinetic energy of the stored electrons. The angular distribution is highly forward peaked and generally has a characteristic angle (i.e., a "1/e" angle) of 0.511/E in radians for electron beam energy E (MeV). The dose is approximately proportional to $E^{2.5}$ and, of course, the mass thickness of the air column in the ring section through which the electrons pass. Given this discussion, it should be obvious that the photons from the gas bremsstrahlung are far more energetic and hence more difficult to shield than are the synchrotron radiation photons which are largely low energy x-rays. To better understand this, Tromba and Rindi (Tr90) have performed Monte Carlo calculations with the code EGS4 for the geometry shown in Fig. B.8.



Fig. B.8 Geometry considered by Tromba and Rindi in their Monte Carlo calculations of gas bremsstrahlung. An electron pencil beam crosses an air target. The bremsstrahlung photons are attenuated in lead. The number of photons and the relative dose are scored on a small surface (about 1 cm²), smaller than the photon-beam angular opening at different depths in the lead. [Adapted from (Tr90).]

As a result of their calculations, these authors propose the following expression for the dose rate, $dD/dt_{10 \text{ meters}}$ (Gyh⁻¹), at 10 meters "on axis" from the end of the straight section ("air target" in Fig. B.8):

$$\frac{dD}{dt}_{10 \text{ meters}} = 3.32 \times 10^{-9} E^{2.43} \frac{p}{p_{atm}} \frac{dN}{dt} L \text{ (Gy h}^{-1}\text{)}, \tag{B.17}$$

where *E* is the electron energy (GeV), dN/dt is the number of electrons s⁻¹ passing through the straight section, p/p_{atm} is the ratio of the residual pressure to atmosphere pressure, and *L* is the length of the straight section in meters. In perhaps more convenient units of beam current, *I* (milliamperes), and residual pressure, *P* (here, in units of mm of Hg, or torr), this is equivalent to:

$$\frac{dD}{dt}_{10 \text{ meters}} = 2.72 \times 10^4 E^{2.43} PIL \text{ (Gy h}^{-1}\text{)}. \tag{B.18}$$

For other distances, r (meters), measured from the center of the straight section, inside of this narrow radiation cone, one should scale this result by the inverse square factor,

$$\frac{dD(r)}{dt} = \frac{dD}{dt}_{10 \text{ meters}} \left\{ \frac{10 + L/2}{r} \right\}^2, \tag{B.19}$$

valid as long as one is within the radiation emission cone and r > L/2.

Of course one will need to calculate the thickness of shielding needed to attenuate this source of radiation to some desired level. Fortunately, as exhibited in Fig. 3.13, the photon mean free path is only very weakly dependent upon energy over several orders of magnitude in the energy domain of interest. In the calculation of Tromba and Rindi, it was found that for lead shielding, the attenuation, after some initial buildup region of a few centimeters can be characterized as an exponential one, with an attenuation coefficient of ≈ 0.6 cm⁻¹, a parameter that is only very weakly dependent upon beam energy.

B.3.3 Gas Bremsstrahlung – Secondary Photons

Another manifestation of gas bremsstrahlung is due to secondary photons produced by interactions of the gas bremssstrahlung photons with materials. This applies when the bremsstrahlung photons are incident on some sort of absorber or beam "shutter" in the absence of the electrons which have been deflected somewhere else by bending magnets. To estimate this a useful "prescription" has been presented by Liu and Vylet (Li01). For a thin piece of material, the lateral photon dose is largest at somewhat forward angles. For more massive objects, the maximum in the lateral photon dose is at more backward angles. From Eq. (3.5), the fractional energy transferred from an electron to the photons, dE/E, is equal to the ratio of the mass thickness, t, of the column of residual gas to its radiation length, X_o . Thus, the fractional energy or power (with units of time included) transferred to gas bremsstrahlung photons from the circulating electrons is t/X_o , where the radiation length of air can be taken to be 36.66 g cm^{-2} . One can multiply this ratio by the stored power of the electron beam to determine the **bremsstrahlung power**; that is, the power that is delivered to the bremsstrahlung photons. To illustrate how this can be used, consider an example for a 3 GeV storage ring that confines 500 mA of electron beam current. Assume that L = 5 meters and the residual gas pressure is 1 x 10⁻⁹ torr (1 torr =

1 mm of Hg = 1/760 of an atmosphere = 133.3 Pa). For this, applying the atmospheric density of NTP (Table 1.2),

$$t = 500 \text{ cm} \times \frac{10^{-9} \text{torr} \times \text{atmosphere}}{760 \text{ torr}} \frac{1.205 \text{ g}}{1000 \text{ cm}^3 \text{ atmosphere}} = 7.928 \times 10^{-13} \text{ (g cm}^{-2}\text{)}.$$

Thus the fraction of the total beam power diverted into gas bremsstrahlung by interactions in the residual gas of this particular straight section is

$$F_{brem} = \frac{t}{X_o} = \frac{7.928 \times 10^{-13}}{36.66} = 2.162 \times 10^{-14}.$$
 (B.20)

At this machine the stored beam power is 1.5×10^9 watts. Applying this factor, 3.24×10^{-5} watts is transferred into bremsstrahlung at this particular location. When this bremsstrahlung bombards a solid object in a beamline an electromagnetic cascade is initiated. For simplicity, this "object" will be taken to be a cylinder several radiation lengths long characterized by a Molière radius, X_m , as defined in Eq. (3.21). Eq. (3.36) (see also Fig. 3.16) gives the fraction of the incident bremsstrahlung beam power that escapes a thickness R of this shield *laterally*, F_{esc} ($0 \le F_{esc} \le 1$);

$$F_{esc} = \frac{U(R/X_m)}{E_o} = 0.8 \exp\left[-3.45 \binom{R}{X_m}\right] + 0.2 \exp\left[-0.889 \binom{R}{X_m}\right]. \quad (B.21) [3.36]$$

Thus, in our example $(3.24 \times 10^{-5})F_{esc}$ watts will escape laterally. Making a simple unit conversion it is easy to see that this is equivalent to $2.022 \times 10^8 F_{esc}$ (MeV s⁻¹). For these laterally-produced photons it is reasonable to take their average energy to be 1 MeV. Thus, this configuration represents a finite, uniform *line source* of strength $S_L = 4.044 \times 10^5 F_{esc}$ photons cm⁻¹s⁻¹. It has been shown by others [e.g., Jaeger et al. (Ja68)], that the flux density at a distance *a* away from a line source length *L* on the perpendicular bisector is given by

$$\phi(a) = \frac{S_L}{2\pi a} \operatorname{Tan}^{-1} \left(\frac{L}{2a} \right), \tag{B.22}$$

with the result of evaluating $Tan^{-1}(L/2a)$ taken to be in radians. Evaluating this at a distance of 1 meter,

$$\phi(100 \text{ cm}) = \frac{4.045 \times 10^5}{2\pi (100 \text{ cm})} \left(\frac{\text{photons}}{\text{cm s}}\right) F_{esc} \text{Tan}^{-1} \left(\frac{500}{200}\right) = 766.3 F_{esc} (\text{photons cm}^{-2} \text{s}^{-1}).$$
 (B.23)

Multiplying by an appropriate dose equivalent per fluence conversion factor of 5 x 10^{-6} µSv cm², this turns out to be a dose equivalent rate of $dH/dt = 3.83 \times 10^{-3} F_{esc} \mu Sv s^{-1} = 13.8 F_{esc} \mu Sv h^{-1}$, a measurable value even with the extremely good vacuum postulated if F_{esc} is finite. Liu and Vylet report that estimations of this type agree with measurements to within a factor of two or three. This methodology is a bit simplistic, it ignores some

amount of forward-peaking. However, for large targets, the dose equivalent rate will be larger at *backward* angles. For small objects struck by the beam, a point source approximation may be an easier, and better choice.

Liu et al. (Li95) have performed a more sophisticated calculation of such photon dose rates using the EGS4 code. The results are provided in Fig. B.9. These results for backward angles (i.e., "upstream" of the beam shutter) are for targets of various materials.



Fig. B.9 Secondary photon dose rate at 1 m lateral to large targets of various materials as a function of electron beam energy. The values are normalized to a beam current of 1 Ampere, per GeV beam energy, and an air path of 1 meter with a pressure of 1 μ Pa (= 7.50 x 10⁻⁹ torr). [Adapted from (Li95).]

These curves exhibit an energy dependence due to the fact that for the higher energies, the location of the shower maximum is located *deeper* in the absorber. Thus, at higher energies the photons will be more attenuated as they move backwards out of the target. The following representations of the energy dependences of H_s , the photon surface dose rate (μ Sv h⁻¹A⁻¹ GeV⁻¹ μ Pa⁻¹m⁻¹) at 1 meter lateral distance from the beam line were determined:

$$H_{s} = 0.35E^{-0.33} \text{ (tungsten)},$$

$$H_{s} = 0.32E^{-0.36} \text{ (lead)},$$

$$H_{s} = 0.23E^{-0.49} \text{ (copper)}, \text{ and}$$

$$H_{s} = 0.11E^{-0.69} \text{ (silicon and aluminum)}.$$

(B.24)

B.3.4 Gas Bremsstrahlung Neutron Production Rates

The prodigious production of photons, as otherwise with electron beams, can lead to photoneutron production. Using a methodology similar to that employed above, Eq. (B.20) can be used to calculate the bremsstrahlung power at the end of a given straight section. These photons may then be incident on some device such as a beam shutter and produce neutrons. For example the straight section discussed above is operational, then

3.24 x 10^{-5} watts goes into the bremsstrahlung at that location. One might assume the beam shutter is made of tungsten. For this material Fig. 3.7 and Table 3.1 give a total photoneutron yield of 2.36 x 10^9 neutrons s⁻¹ W⁻¹, so 7.65 x 10^4 neutrons s⁻¹ will be emitted if this bremsstrahlung power is incident on this device. Since the photoneutrons are isotropic and "point source" conditions are a good approximation, a flux density of 0.61 neutrons cm⁻² s⁻¹ is found at a distance of 1 meter without including the effects of any intervening shielding. For these giant resonance neutrons a conservative dose equivalent per fluence conversion factor is $3.2 \times 10^{-4} \,\mu\text{Sv cm}^2$. When applied here, a dose equivalent rate of $dH/dt = 1.95 \times 10^{-4} \,\mu\text{Sv s}^{-1} = 0.70 \,\mu\text{Sv h}^{-1}$ is realized. Neutrons from quasi-deuteron and photopion reactions are ignored in this estimate. Again, according to Liu and Vylet (Li01), these values are in reasonable agreement with measurement and more sophisticated calculations.

Liu et al. (Li95) have given more detailed results for neutron production by gas bremsstrahlung incident on various materials provided here. Fig. B.10 provides these results. The left frame of this figure presents both the normalized neutron dose rates at 1 meter from the target and the neutron yield with the target as a function of target atomic number. These results are for targets with sufficient size ($\approx 30 X_o$ long and $30 X_m$ in diameter) to generate maximal neutron yields. The right frame of this figure can be used to estimate results for shorter targets made of lead.



Fig. B.10 Left frame: Neutron dose rate at 1 meter away from a beamline device struck by gas bremsstrahlung and the neutron yield within the device as a function of the atomic number of the device. The values are normalized to a beam current of 1 A, per GeV beam energy, and an air path of 1 meter with a pressure of 1 μ PA. Right frame: Relative neutron yield as a function of the target length in units of radiation length for a cylindrical lead target 15 Molière units in radius struck by gas bremsstrahlung for 4 electron beam energies. [Adapted from (Li95).]

B.3.5 Importance of Ray Tracing

As a final word, given the plethora of beamlines, penetrations, and devices mounted both within a light source storage ring and associated with its beam lines and experiments, it is generally important to do careful ray tracing studies for both the ring shielding and beamline shielding design to be sure that secondary radiation from electron losses in the ring (normal and abnormal) as well as synchrotron radiation, gas bremsstrahlung "beams", and photoneutrons in beamlines are effectively prevented from reaching undesired locations. All operational modes including injection events, top-offs, and storage ring runs need to be considered. One must be sure that no "holes" are available that could result in significant radiation exposures. Fig. B.11 shows the complexity of a typical configuration, clearly illustrating why such ray tracing should be done. It is evident that all three spatial dimensions must be considered.



Fig. B.11 Example of the importance of ray tracing in a ring front end. [J. Liu and V. Vylet, private communication]

APPENDIX C EXAMPLES OF RESULTS OF STAR DENSITY CALCULATIONS USING CASIM

As was discussed in Section 4.7.2, a convenient way to exhibit the "raw" output of Monte Carlo high energy hadronic cascade calculations is in the form of contour plots of star density as a function of longitudinal coordinate, Z, and radial coordinate, R. This appendix contains representative samples of such plots obtained using CASIM (Va75, Va87, and Co82b). This collection is illustrative in nature; it is not intended to address all situations. The main text refers to more complete compilations of calculations. Individual calculations should be done for definitive results.

The examples provided here are of three general classes:

Figures C1.a-C1.d present results for protons incident along the axis of a solid CONCRETE cylinder perpendicular to one face of the cylinder. The concrete is of "standard" composition" and is taken to have a density of 2.4 g cm^{-3} .

Figures C2.a-C2.d present results for protons incident along the axis of a solid IRON cylinder perpendicular to one face of the cylinder. The iron is taken to have a density of 7.87 g cm^{-3} .

Figures C3.a-C3.d present results for 1 TeV protons incident on various beamline components that might be found in a typical beam enclosure consisting of a cylindrical tunnel with CONCRETE walls surrounded by a concentric cylindrical SOIL shield. For the components, the standard densities found in Table 1.2 were used. The density of concrete was taken to be 2.4 g cm⁻³ and the density of soil was taken to be 2.25 g cm⁻³. Beam pipes were assumed taken to be at vacuum. The captions describe the details of the beam loss scenarios used in the calculations.



C.1 Results for Solid CONCRETE Cylinders

Fig. C1.a Monte Carlo results for 30 GeV/c protons incident on a CONCRETE cylinder. Contours of equal star density (stars cm⁻³) per incident proton are plotted. The beam of 0.3 x 0.3 cm cross section is centered on the cylinder axis and starts to interact at zero depth. The star density includes only those due to hadrons above 0.3 GeV/c momentum. Contours of higher star density are not shown for clarity while those of lower star density are not included due to statistical uncertainty. [Adapted from (Va75).]



Fig. C1.b Monte Carlo results for 100 GeV/c protons incident on a CONCRETE cylinder. Contours of equal star density (stars cm⁻³) per incident proton are plotted. The beam of 0.3 x 0.3 cm cross section is centered on the cylinder axis and starts to interact at zero depth. The star density includes only those due to hadrons above 0.3 GeV/c momentum. Contours of higher star density are not shown for clarity while those of lower star density are not included due to statistical uncertainty. [Adapted from (Va75).]



Fig. C1.c Monte Carlo results for 1 TeV/c protons incident on a CONCRETE cylinder. Contours of equal star density (stars cm⁻³) per incident proton are plotted. The beam of 0.3 x 0.3 cm cross section is centered on the cylinder axis and starts to interact at zero depth. The star density includes only those due to hadrons above 0.3 GeV/c momentum. Contours of higher star density are not shown for clarity while those of lower star density are not included due to statistical uncertainty. [Adapted from (Va75).]



Fig. C1.d Monte Carlo results for 10 TeV/c protons incident on a CONCRETE cylinder. Contours of equal star density (stars cm⁻³) per incident proton are plotted. The beam of 0.3 x 0.3 cm cross section is centered on the cylinder axis and starts to interact at zero depth. The star density includes only those due to hadrons above 0.3 GeV/c momentum. Contours of higher star density are not shown for clarity while those of lower star density are not included due to statistical uncertainty. [Adapted from (Va87).]

C.2 Results for Solid IRON Cylinders



Fig. C2.a Monte Carlo results for 30 GeV/c protons incident on an IRON cylinder. Contours of equal star density (stars cm⁻³) per incident proton are plotted. The beam of 0.3 x 0.3 cm cross section is centered on the cylinder axis and starts to interact at zero depth. The star density includes only those due to hadrons above 0.3 GeV/c momentum. Contours of higher star density are not shown for clarity while those of lower star density are not included due to statistical uncertainty. [Adapted from (Va75).]



Fig. C2.b Monte Carlo results for 100 GeV/c protons incident on an IRON cylinder. Contours of equal star density (stars cm⁻³) per incident proton are plotted. The beam of 0.3 x 0.3 cm cross section is centered on the cylinder axis and starts to interact at zero depth. The star density includes only those due to hadrons above 0.3 GeV/c momentum. Contours of higher star density are not shown for clarity while those of lower star density are not included due to statistical uncertainty. [Adapted from (Va75).]



Fig. C2.c Monte Carlo results for 1 TeV/c protons incident on an IRON cylinder. Contours of equal star density (stars cm⁻³) per incident proton are plotted. The beam of 0.3 x 0.3 cm cross section is centered on the cylinder axis and starts to interact at zero depth. The star density includes only those due to hadrons above 0.3 GeV/c momentum. Contours of higher star density are not shown for clarity while those of lower star density are not included due to statistical uncertainty. [Adapted from (Va75).]



Fig. C2.d Monte Carlo results for 10 TeV/c protons incident on an IRON cylinder. Contours of equal star density (stars cm⁻³) per incident proton are plotted. The beam of 0.3 x 0.3 cm cross section is centered on the cylinder axis and starts to interact at zero depth. The star density includes only those due to hadrons above 0.3 GeV/c momentum. Contours of higher star density are not shown for clarity while those of lower star density are not included due to statistical uncertainty. [Adapted from (Va87).]

APPENDIX C EXAMPLES OF RESULTS OF STAR DENSITY CALCULATIONS USING CASIM



C.3 Results for 1 TeV Protons Incident on Pipes and Magnets





Fig. C3.b Contour plots of equal star density (stars cm⁻³) per incident proton calculated using CASIM for a 1 TeV proton beam incident "head on" on a thin cylindrical aluminum pipe of 10.16 cm outside diameter with 0.318 cm thick walls. The results were averaged over azimuth and the pipe was centered in a cylindrical tunnel 182 cm in radius. The concrete wall was 30.48 cm thick and was surrounded by soil. [Adapted from (Co82b).]



Fig. C3.c Contour plots of equal star density (stars cm⁻³) per incident proton calculated using CASIM for a 1 TeV proton beam incident "head on" on a thick cylindrical iron pipe of 30.48 cm outside diameter with 1.27 cm thick walls. The results were averaged over azimuth and the pipe was centered in a cylindrical tunnel 182 cm in radius. The concrete wall was 30.48 cm thick and was surrounded by soil. [Adapted from (Co82b).]



Fig. C3.d Contour plots of equal star density (stars cm⁻³) per incident proton calculated using CASIM for a 1 TeV proton beam incident "head on" on a thick cylindrical iron pipe of 30.48 cm outside diameter with 1.27 cm thick walls. The pipe is surrounded by soil. [Adapted from (Co82b).]

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