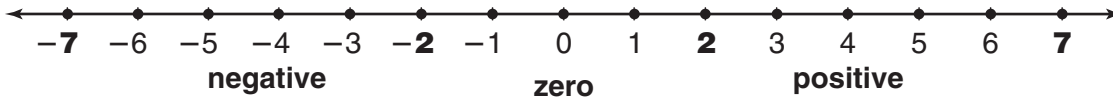


Reteaching 1-1

Comparing and Ordering Integers

The numbers 2 and -2 are opposites. The numbers 7 and -7 are opposites.

Integers are the set of positive whole numbers, their opposites, and zero.



You can use the number line to compare integers.

-2 is less than 0.
 $-2 < 0$

7 is greater than 2.
 $7 > 2$

Numbers to the left are less. -2 is farther left than 0.	Numbers to the right are greater. 7 is farther to the right than 2.
---	--

Compare using $<$, $>$, or $=$.

- | | | |
|----------------------|----------------------|--------------------|
| 1. $4 \square 2$ | 2. $-3 \square -2$ | 3. $3 \square -4$ |
| 4. $-1 \square -2$ | 5. $0 \square 5$ | 6. $0 \square -4$ |
| 7. $-6 \square 4$ | 8. $-8 \square -2$ | 9. $3 \square 0$ |
| 10. $-7 \square -10$ | 11. $-10 \square 10$ | 12. $1 \square -1$ |

Find the opposite of each number.

- | | | |
|-------------|----------------|---------------|
| 13. 8 _____ | 14. -5 _____ | 15. 147 _____ |
|-------------|----------------|---------------|

Find each sum.

- | | | |
|---------------------|----------------------|------------------------|
| 16. $12 + 12$ _____ | 17. $-15 + 15$ _____ | 18. $18 + 18$ _____ |
| 19. $5 + 5$ _____ | 20. $-24 + 24$ _____ | 21. $-225 + 225$ _____ |

Order the numbers from least to greatest.

- | | |
|------------------------------------|------------------------------------|
| 22. $-4, 5, -2, 0, 1$
_____ | 23. $6, -3, -5, 4, -6$
_____ |
| 24. $3, -5, 4, -4, -7, 0$
_____ | 25. $1, 3, -7, -6, 5, -2$
_____ |

Reteaching 1-2

Adding and Subtracting Integers

Use these rules to add and subtract integers.



<ul style="list-style-type: none"> • The sum of two positive integers is positive. Example: $6 + 16 = 22$ • The sum of two negative integers is negative. Example: $-9 + (-3) = -12$ 	<ul style="list-style-type: none"> • First find the absolute values of each number. • Then subtract the lesser absolute value from the greater. • The sum has the sign of the integer with the greater absolute value. Example: $-10 + 9 = -1$
--	--

Subtracting Integers

- To subtract integers, add the opposite.
 - Then following the rules for adding integers.
Example: $6 - (-3) = 6 + 3 = 9$

Find each sum.

- | | | |
|-----------------------|----------------------|----------------------|
| 1. $8 + (-2)$ _____ | 2. $-9 + 4$ _____ | 3. $3 + (-2)$ _____ |
| 4. $-1 + 11$ _____ | 5. $12 + 13$ _____ | 6. $-9 + 5$ _____ |
| 7. $7 + 2$ _____ | 8. $-1 + (-7)$ _____ | 9. $-3 + 0$ _____ |
| 10. $-1 + (-1)$ _____ | 11. $6 + 5$ _____ | 12. $3 - (-2)$ _____ |

Complete.

- | | |
|------------------|--|
| 13. $-3 - 4$ | Change to addition: $-3 + \underline{\hspace{1cm}} = \underline{\hspace{1cm}}$ |
| 14. $5 - 2$ | Change to addition: $5 + \underline{\hspace{1cm}} = \underline{\hspace{1cm}}$ |
| 15. $-6 - (-10)$ | Change to addition: $-6 + \underline{\hspace{1cm}} = \underline{\hspace{1cm}}$ |

Find each difference.

- | | | |
|-----------------------|-----------------------|-----------------------|
| 16. $4 - 5$ _____ | 17. $-5 - 4$ _____ | 18. $-8 - (-7)$ _____ |
| 19. $19 - (-6)$ _____ | 20. $-10 - 12$ _____ | 21. $-12 - 10$ _____ |
| 22. $-4 - (-5)$ _____ | 23. $-2 - (-3)$ _____ | 24. $9 - (-7)$ _____ |
| 25. $0 - 3$ _____ | 26. $6 - 8$ _____ | 27. $0 - (-10)$ _____ |

Reteaching 1-3

Multiplying and Dividing Integers

To multiply integers:

- If the signs are alike, the product is positive.

$$2 \cdot 3 = 6$$

$$-2 \cdot -3 = 6$$

- If the signs are different, the product is negative.

$$2 \cdot -3 = -6$$

$$-2 \cdot 3 = -6$$

To divide integers:

- If the signs are alike, the quotient is positive.

$$6 \div 3 = 2$$

$$-6 \div -3 = 2$$

- If the signs are different, the quotient is negative.

$$6 \div -3 = -2$$

$$-6 \div 3 = -2$$

Study these four examples. Write positive or negative to complete each statement.

$$7 \cdot 3 = 21$$

$$-7 \cdot -3 = 21$$

$$7 \cdot -3 = -21$$

$$-7 \cdot 3 = -21$$

1. When both integers are positive, the product is _____.
2. When one integer is positive and one is negative, the product is _____.
3. When both integers are negative, the product is _____.

$$21 \div 3 = 7$$

$$21 \div -3 = -7$$

$$-21 \div -3 = 7$$

$$-21 \div 3 = -7$$

4. When both integers are positive, the quotient is _____.
5. When both integers are negative, the quotient is _____.
6. When one integer is positive and one is negative, the quotient is _____.

Tell whether each product or quotient will be *positive* or *negative*.

7. $4 \cdot 7$

8. $-4 \cdot 7$

9. $-4 \cdot -7$

10. $4 \cdot -7$

11. $10 \cdot -4$

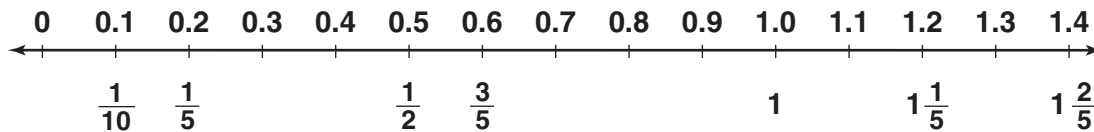
12. $-25 \div 5$

13. $-2 \cdot -2$

14. $100 \div 10$

Reteaching 1-4

Fractions and Decimals



To change a fraction to a decimal, divide the numerator by the denominator.

$\frac{3}{5}$ Think: $3 \div 5$

$$\begin{array}{r} 0.6 \\ 5 \overline{)3.0} \\ \underline{-30} \\ 0 \end{array}$$

$\frac{3}{5} = 0.6$

To change a decimal to a fraction:

- ① Read the decimal to find the denominator. Write the decimal digits over 10, 100, or 1,000.
- ② 0.65 is 65 *hundredths* $\rightarrow \frac{65}{100}$

Use the GCF to write the fraction in simplest form.

The GCF of 65 and 100 is 5.

$$\frac{65}{100} = \frac{65 \div 5}{100 \div 5} = \frac{13}{20}$$

Write each fraction as a decimal.

- | | | |
|--------------------------|--------------------------|---------------------------|
| 1. $\frac{4}{5} =$ _____ | 2. $\frac{3}{4} =$ _____ | 3. $\frac{1}{6} =$ _____ |
| 4. $\frac{1}{4} =$ _____ | 5. $\frac{2}{3} =$ _____ | 6. $\frac{7}{10} =$ _____ |
| 7. $\frac{5}{9} =$ _____ | 8. $\frac{1}{5} =$ _____ | 9. $\frac{3}{8} =$ _____ |

Write each decimal as a mixed number or fraction in simplest form.

- | | | |
|-------------------|------------------|------------------|
| 10. 0.4 = _____ | 11. 0.75 = _____ | 12. 1.5 = _____ |
| 13. 0.35 = _____ | 14. 2.7 = _____ | 15. 1.8 = _____ |
| 16. 0.625 = _____ | 17. 0.78 = _____ | 18. 0.88 = _____ |

Order from least to greatest.

- | | | |
|---|---|--|
| 19. $2.\bar{6}, \frac{13}{6}, 2\frac{5}{6}$ | 20. $2.\overline{02}, 2\frac{1}{200}, 2.0202$ | 21. $\frac{5}{4}, 1\frac{4}{5}, 1.\bar{4}$ |
| _____ | _____ | _____ |

Reteaching 1-5

A **rational number** is a number that can be written as a quotient of two integers, where the divisor is not zero.

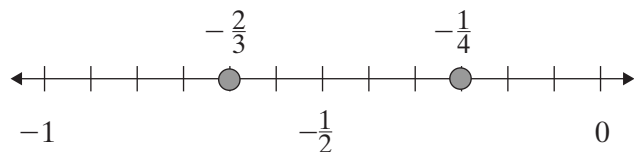
A negative rational number can be written in three different ways.

$$-\frac{2}{3} = -\frac{2}{3} = -\frac{2}{3}$$

Comparing Negative Rational Numbers

Compare $-\frac{2}{3}$ and $-\frac{1}{4}$.

Method 1 Use a number line. Graph both points on a number line and see which is farther to the left.



Since $-\frac{2}{3}$ is farther to the left, $-\frac{2}{3} < -\frac{1}{4}$.

Method 2 Use the lowest common denominator.

$$-\frac{2}{3} = \frac{-2}{3} = \frac{-2 \times 4}{3 \times 4} = \frac{-8}{12} \qquad -\frac{1}{4} = \frac{-1}{4} = \frac{-1 \times 3}{4 \times 3} = \frac{-3}{12}$$

Since $\frac{-8}{12} < \frac{-3}{12}$, then $-\frac{2}{3} < -\frac{1}{4}$.

Compare. Use $<$, $>$, or $=$.

1. $-\frac{4}{9} \square -\frac{2}{3}$

2. $-1 \square -\frac{4}{5}$

3. $-\frac{7}{8} \square -\frac{1}{8}$

4. $-\frac{1}{3} \square -\frac{5}{6}$

5. $-\frac{2}{5} \square -\frac{1}{10}$

6. $-\frac{2}{8} \square -\frac{1}{4}$

Order from least to greatest.

7. $-\frac{1}{3}, 0.3, -0.35, -\frac{3}{10}$

8. $\frac{1}{5}, -0.25, 0.21, \frac{3}{10}$

9. You and your brother invested an equal amount of money in a college savings plan. In the last quarter your investment was worth $1\frac{5}{6}$ of its original value. Your brother's investment was worth 1.85 of its original value. Whose investment is worth more?

Reteaching 1-6 Adding and Subtracting Rational Numbers

Use these rules to add and subtract rational numbers.

Adding and Subtracting Integers

← Same Sign

Different Signs →

- | | |
|---|---|
| <ul style="list-style-type: none"> • The sum of two positive rational numbers is positive.
Example: $15.6 + 4.5 = 20.1$
Example: $\frac{2}{9} + \frac{8}{9} = 1\frac{1}{9}$ • The sum of two negative rational numbers is negative.
Example: $-3.42 + (-5.74) = -9.16$
Example: $-1\frac{3}{4} + (-4\frac{3}{4}) = -6\frac{1}{2}$ | <ul style="list-style-type: none"> • First find the absolute values of each addend. • Then subtract the lesser absolute value from the greater. • The sum has the sign of the addend with the greater absolute value.
Example: $-25.8 + 17.3 = -8.5$
Example: $-2\frac{1}{2} + 1\frac{1}{4} = -1\frac{1}{4}$ |
|---|---|

Subtracting Rational Numbers



- To subtract rational numbers, add the opposite.
- Then following the rules for adding rational numbers.
Example: $-9.25 - (-3.4) = -9.25 + 3.4 = -5.85$
Example: $4 - (-2\frac{3}{10}) = 4 + (2\frac{3}{10}) = 6\frac{3}{10}$

Find each sum.

1. $43.2 + 26.7$

2. $-81.22 + 14.9$

3. $-4.8 + (-53.5)$

4. $2\frac{5}{9} + 3\frac{4}{9}$

5. $-2\frac{3}{5} + 1\frac{1}{5}$

6. $-6\frac{1}{3} + (-7\frac{1}{3})$

Find each difference.

7. $15.64 - 8.5$

8. $-0.392 - 0.26$

9. $-5.4 - (-1.6)$

10. $6 - 5\frac{5}{6}$

11. $-4\frac{3}{4} - 2\frac{1}{4}$

12. $-7\frac{4}{5} - (-3\frac{3}{5})$

Reteaching 1-7

Multiplying Rational Numbers

Remember these rules when multiplying rational numbers.

1. When both factors are positive, the product is positive.

$$\text{Multiply: } \left(2\frac{2}{3}\right)\left(1\frac{5}{8}\right) = \left(\frac{8}{3}\right)\left(\frac{13}{8}\right) = \frac{104}{24} = 4\frac{1}{3}$$

2. When both factors are negative, the product is positive.

$$\text{Multiply: } (-4.35)(-2.44) = 10.614$$

3. When both factors have different signs, the product is negative.

$$\text{Multiply: } -\frac{3}{4} \times \frac{2}{5} = \frac{-3 \times 2}{4 \times 5} = \frac{-6}{20} = -\frac{6}{20} = -\frac{3}{10}$$

Find each product. Write the product in simplest form.

1. 2.8×0.05

2. $\frac{5}{8} \cdot \frac{2}{5}$

3. $1.45 \cdot 0.7$

4. $2\frac{3}{5} \cdot \frac{7}{8}$

5. $(-2.07)(-4.9)$

6. $\frac{5}{12} \cdot \left(-\frac{3}{10}\right)$

7. $9.3(-0.56)$

8. $\frac{1}{2} \times 5\frac{1}{6}$

9. $0.006(3.75)$

10. $-1\frac{2}{3} \times 5$

11. -3.8×912

12. $\left(-2\frac{3}{5}\right)\left(-\frac{1}{4}\right)$

Reteaching 1-8

Dividing Rational Numbers

<p>Divide: $38.25 \div 1.5$.</p> <p>1. Rewrite the problem with a whole number divisor.</p> $1.5 \overline{)38.25}$ <p style="text-align: center;">↓</p> <p>2. Place the decimal point in the quotient.</p> $1.5 \overline{)38.25}$ <p style="text-align: center;">↑ ↑</p> <p style="text-align: center;">Move 1 place each.</p> <p>3. Divide. Then check.</p> $\begin{array}{r} 25.5 \\ 15 \overline{)382.5} \\ \underline{-30} \\ 82 \\ \underline{-75} \\ 75 \\ \underline{-75} \\ 0 \end{array}$ <p style="text-align: center;">$25.5 \times 15 = 382.5 \checkmark$</p> <p style="text-align: center;">Multiply to check.</p>	<p>Divide: $3\frac{3}{4} \div 1\frac{2}{5}$.</p> <p>1. Rewrite mixed numbers as improper fractions as needed.</p> $\frac{15}{4} \div \frac{7}{5}$ <p>2. Multiply by the reciprocal of the divisor.</p> $\frac{15}{4} \cdot \frac{5}{7}$ <p>3. Multiply numerators. Multiply denominators.</p> $\frac{15 \cdot 5}{4 \cdot 7} = \frac{75}{28}$ <p>4. Simplify.</p> $\frac{75}{28} = 2\frac{19}{28}$
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Find each quotient. Simplify your answers.

1. $1\frac{5}{8} \div \frac{5}{8}$

2. $-43.55 \div 6.5$

3. $-\frac{2}{5} \div \frac{4}{25}$

4. $-0.072 \div 0.8$

5. $-12\frac{4}{5} \div (-1\frac{1}{15})$

6. $340.2 \div -4.2$

7. $-15 \div \frac{1}{2}$

8. $12.6 \div 0.21$

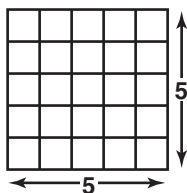
9. $-7\frac{1}{3} \div 2\frac{1}{5}$

10. $-11.1 \div (-37)$

Reteaching 1-9

Irrational Numbers and Square Roots

- The *square* of 5 is 25.
 $5 \cdot 5 = 5^2 = 25$
- The *square root* of 25 is 5
because $5^2 = 25$.



$$\left. \begin{array}{l} 1^2 = 1 \\ 2^2 = 4 \\ 3^2 = 9 \\ 4^2 = 16 \\ 5^2 = 25 \end{array} \right\} \text{perfect squares}$$

$$\sqrt{25} = 5$$

Example: You can use a calculator to find square roots.
Find $\sqrt{36}$ and $\sqrt{21}$ to the nearest tenth.

$$36 \sqrt{\square} = 6 \quad 21 \sqrt{\square} \approx 4.5825757 \approx 4.6$$

You can estimate square roots like $\sqrt{52}$ and $\sqrt{61}$.

Perfect squares	↗	49		$\sqrt{49} = 7$		$\sqrt{49} = 7$
		52	Estimate	$\sqrt{52} \approx 7$	Estimate	$\sqrt{61} \approx 8$
	↘	64		$\sqrt{64} = 8$		$\sqrt{64} = 8$

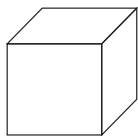
Find each square root. Estimate to the nearest integer if necessary.
Use \approx to show that a value is estimated.

- | | | | |
|------------------------|-------------------------|------------------------|-------------------------|
| 1. $\sqrt{16}$ | 2. $\sqrt{85}$ | 3. $\sqrt{26}$ | 4. $\sqrt{36}$ |
| _____ | _____ | _____ | _____ |
| 5. $\sqrt{98}$ | 6. $\sqrt{40}$ | 7. $\sqrt{100}$ | 8. $\sqrt{18}$ |
| _____ | _____ | _____ | _____ |
| 9. $\sqrt{5}$ | 10. $\sqrt{121}$ | 11. $\sqrt{68}$ | 12. $\sqrt{144}$ |
| _____ | _____ | _____ | _____ |
| 13. $\sqrt{29}$ | 14. $\sqrt{64}$ | 15. $\sqrt{37}$ | 16. $\sqrt{75}$ |
| _____ | _____ | _____ | _____ |

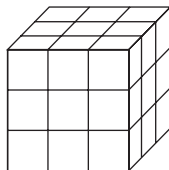
- 17.** If a whole number is not a perfect square, its square root is an *irrational number*.
List the numbers from exercises 1–16 that are irrational.

Reteaching 1-10

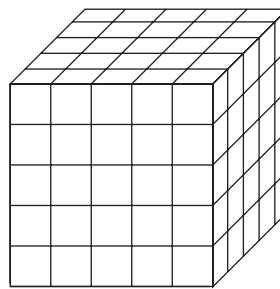
Cube Roots



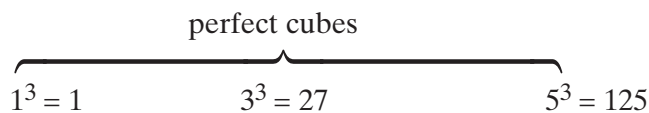
The cube of 1 is 1.
 $1 \times 1 \times 1 = 1^3 = 1$



The cube of 3 is 27.
 $3 \times 3 \times 3 = 3^3 = 27$



The cube of 5 is 125.
 $5 \times 5 \times 5 = 5^3 = 125$



Example: You can solve cube root equations: $x^3 = \frac{27}{216}$

$$\sqrt[3]{x^3} = \sqrt[3]{\frac{27}{216}} \leftarrow \text{Find the cube root of each side.}$$

$$= \frac{\sqrt[3]{27}}{\sqrt[3]{216}} \leftarrow \text{Find the cube root of the numerator and denominator.}$$

$$x = \frac{3}{6} = \frac{1}{2} \leftarrow \text{Simplify.}$$

Find the cube root of each number.

1. 729

2. 125

3. 512

4. -64

5. $\frac{1}{216}$

6. $\frac{125}{1000}$

Solve each equation by finding the value of x .

7. $x^3 = 27$

8. $x^3 = 1,728$

9. $x^3 = \frac{343}{729}$
