

RGI / Effective Charges in Practise



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Workshop on 1. Principles Non-Perturbative QCD
of Hadron Jets
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Outline

1 Introductory Comments

- Papers
- Mass Effects & Corrections

2 $\mathcal{O}(\alpha_s^2)$ Results from Shape Distributions

- Effect of Changing the Renormalisation Scale

3 $\mathcal{O}(\alpha_s^2)$ Results from Mean Values

- Naive Power Correction
- RGI
- RGI vs. Power Terms
- Measuring the β -Function

4 Summary

Talk is mainly based on:

DELPHI Collab., Consistent measurements of α_s from precise oriented event shape distributions ..., (Eur. Phys. J. C14, 557)

- Standard event shapes (depending on **polar** angle)

DELPHI Collab., A study of the energy evolution of event shape distributions and their means ..., (Eur. Phys. J. C29, 285)

- **Data**
 - radiative DELPHI Z events at $E_{CM} = 45, 66$ and 76 GeV
 - DELPHI data from LEP1 and LEP2 ($E_{CM} = 89$ to 202 GeV)
 - low energy data from various experiments
- **Observables**
 - usual event shape means: $T, C, Major, B_T, B_W, (EEC, JCEF)$
 - $M_{h/s}^2/E_{vis}^2$ in alternative definitions "**E/p-scheme**"!

Mass Effects for Event Shapes / Means

Hadron masses influence shape observables.

Two types of observables:

- e.g. **Thrust** : mass-dependence via E -conservation .
- e.g. **Jet Masses**: direct mass-dependence;
avoid by choosing:

(p -scheme)

$$(\vec{p}, E) \longrightarrow (\vec{p}, |\vec{p}|)$$

(E -scheme)

$$(\vec{p}, E) \longrightarrow (\hat{p}E, E)$$

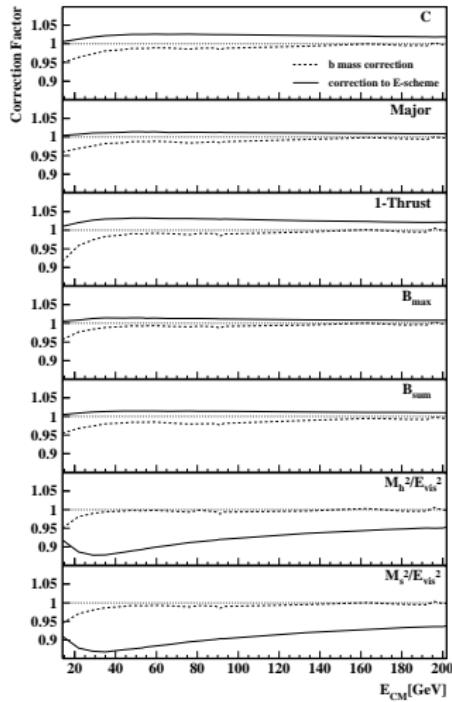
Furthermore:

- Transverse momentum from **B-decays** .

Estimate effects using Monte Carlo models;

b-correction: calculate $b+udsc/udsc$;

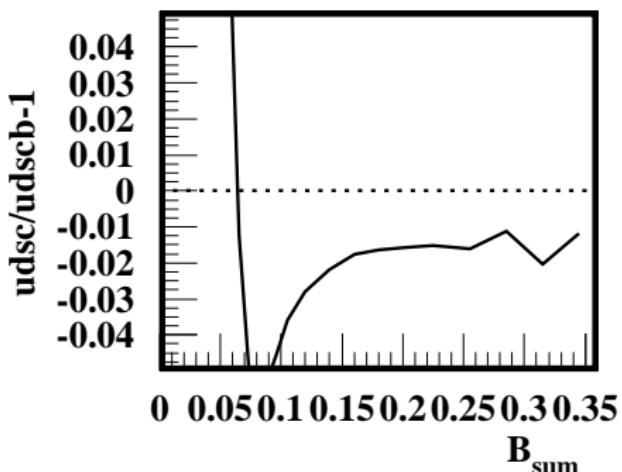
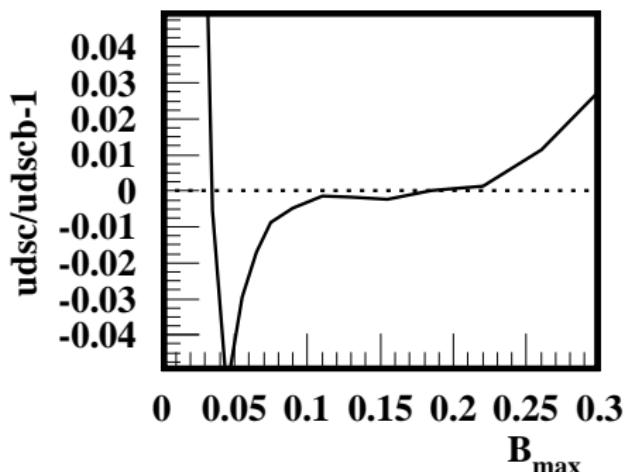
Mass Effects for Event Shape Means



full line
 correction to E-scheme
 dashed line
 B-correction

⇒ For Jet-masses
 change to E-scheme

Mass Effects for Event Shapes



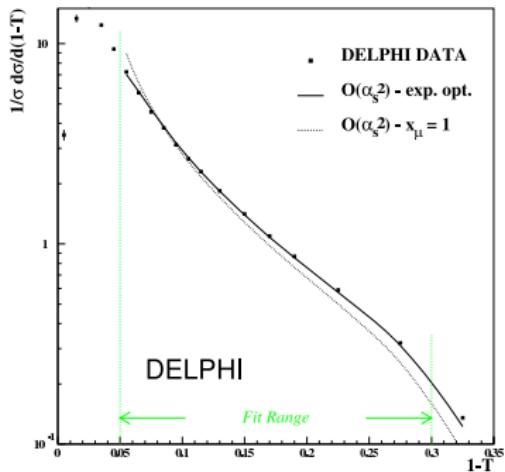
Correction slightly changes slope of distributions!

Description of Event Shape Spectra

$\mathcal{O}(\alpha_s^2)$ -prediction for events shape distributions

$$\frac{1}{\sigma_{tot}} \frac{d\sigma}{df} = A_f \cdot \bar{\alpha}_s(\mu) + (A_f \cdot (\beta_0 \log x_\mu - 2) + B_f) \bar{\alpha}_s(\mu)^2$$

- Change of $x_\mu = \mu/E_{CM}$
“turns” the prediction
- $\mathcal{O}(\alpha_s^2)$ prediction for $x_\mu = 1$
in general inconsistent with data
 - α_s results depend on fit range
 - Good χ^2 only if x_μ is optimised !
- Bad features are partly inherited to the matched predictions.

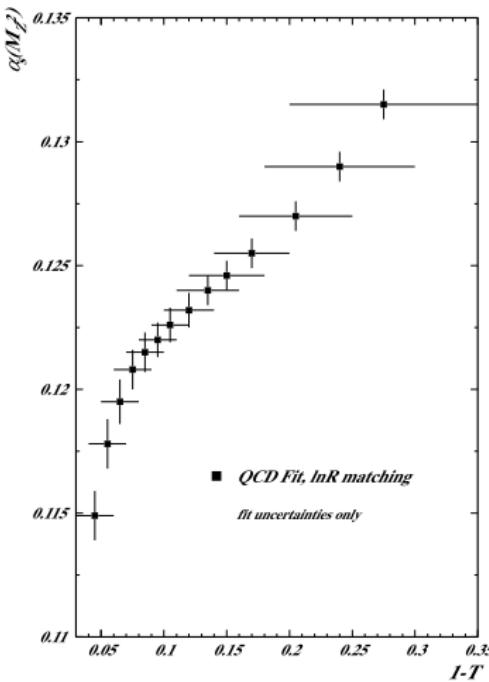
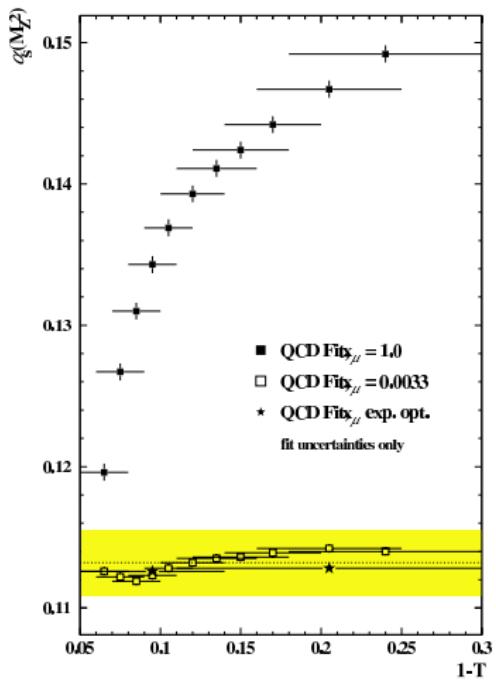


$\alpha_s = \alpha_s(T) -$ the Worst Case

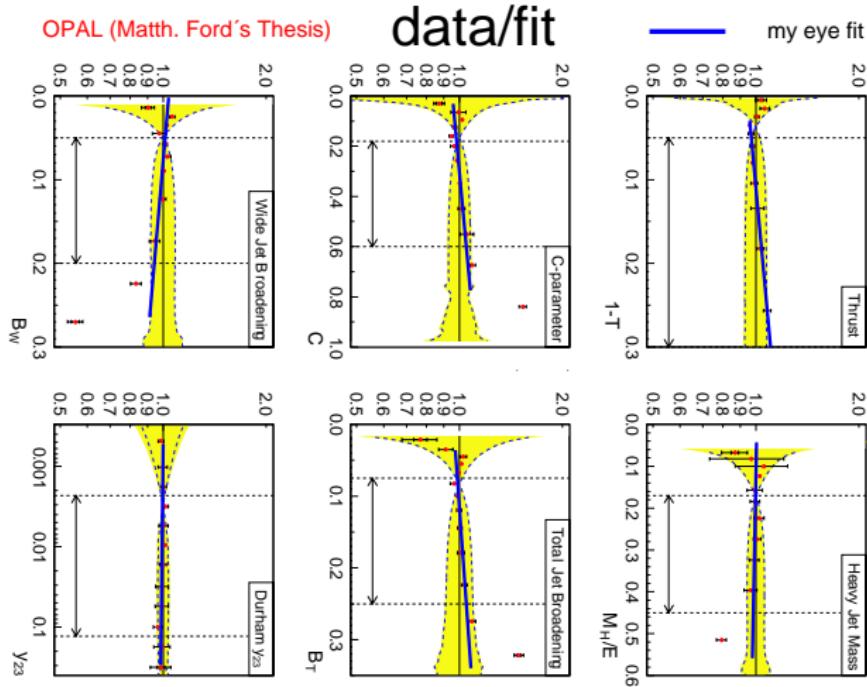
$\mathcal{O}(\alpha_s^2)$

from Siggi Hahns thesis

Matched



Compare T, B_T, C, M_H, y, B_W



note:
 B/A ratios

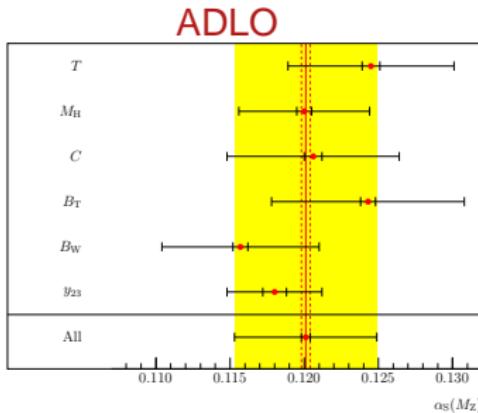
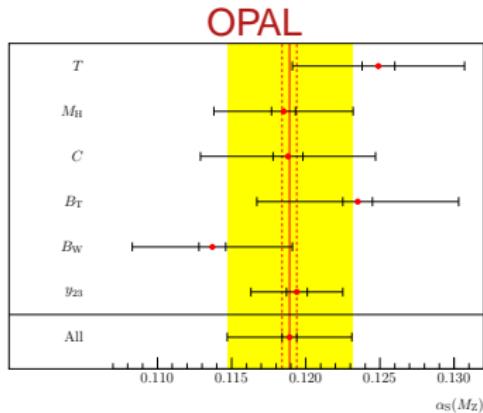
$T, B_T, C \gtrsim 15$
 M_H, y small(er)
 B_W negative

non-optimal scales \Rightarrow

biases of α_s

α_s Results - In R Matched Theory

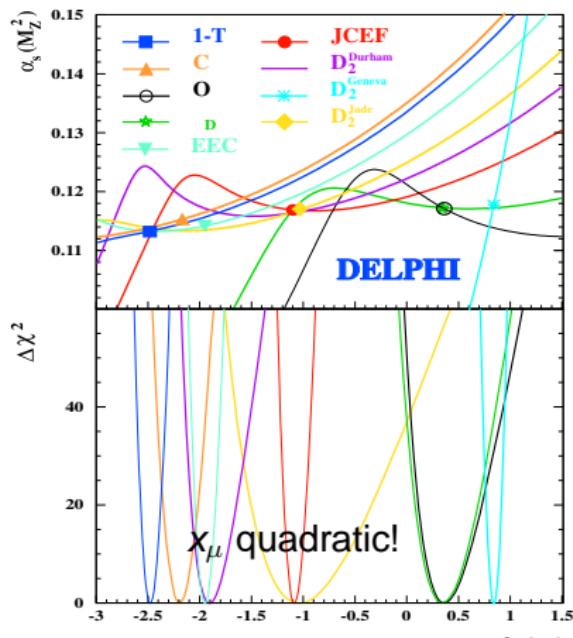
(from M.Fords thesis & LEPQCDWg info)



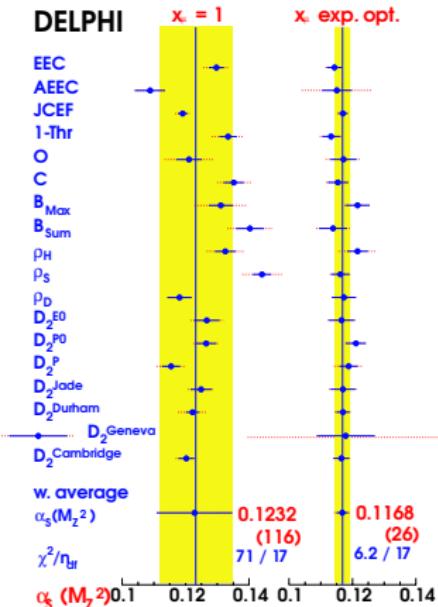
Observe the expected pattern:

$T, B_T, (C?)$ high ; M_H, y central ; B_W small

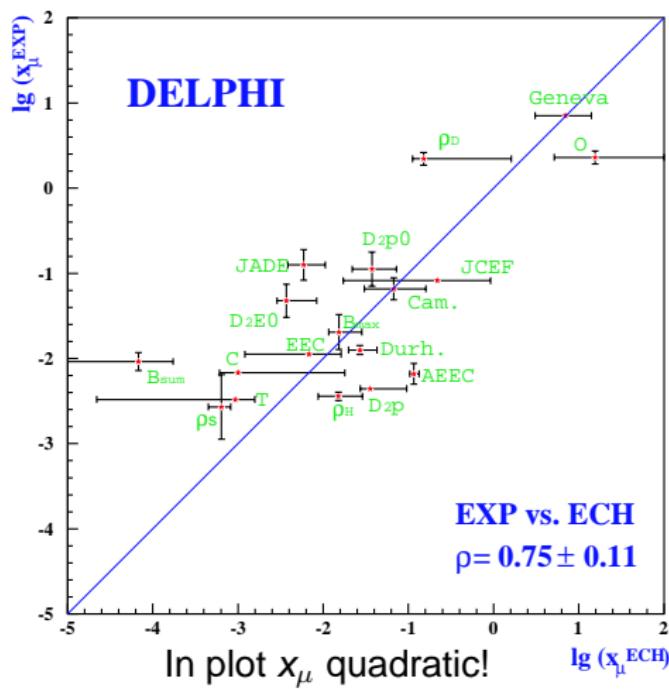
$\mathcal{O}(\alpha_s^2)$ & Experimental Optimisation



Experimental optimisation strongly improves consistency!



Experimental vs. ECH Scales



Experimental scales correlate $\rho = 0.75$ with ECH or PMS scales

Errors:

ECH: scale variation in fit range
 EXP: fit error

Influence of mass effects not considered !

$$10^\sigma(P(\lg(x_\mu^{\text{ECH}} / x_\mu^{\text{EXP}}))) \sim 2.5$$

We “understand” the large range of opt. scales in \overline{MS} !

Naive Power Corrections

Assess power terms of means using:

$$\langle f \rangle = \langle f \rangle_{\mathcal{O}(\alpha_s^2)} + \langle f \rangle_{pow}$$

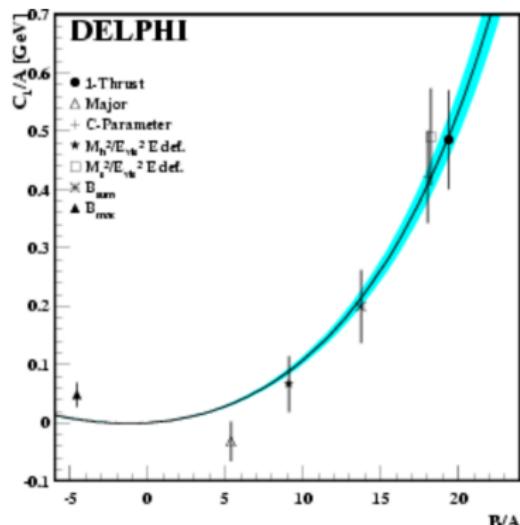
$$\langle f_{pow} \rangle = C_1 / E_{CM}$$

Find expected strongly differing power terms.

Surprising:

“Non-perturbative” p.t.’s correlate with perturbative ratio $B/A \implies$.

Power terms predominantly account for higher order pert. effects?



Renormalisation Group Invariant (RGI) P.T.

Demand observable $R = \langle f \rangle / A$ to fulfil RGE:

$$Q \frac{dR}{dQ} = -bR^2(1 + \rho_1 R + \rho_2 R^2 + \dots) = b\rho(R) .$$

b, ρ_i are scheme invariant . \Rightarrow

vanishes in second order

$$b \ln \frac{Q}{\Lambda_R} = \frac{1}{R} - \rho_1 \ln \left(1 + \frac{1}{\rho_1 R} \right) + \overbrace{\int_0^R dx \left(\frac{1}{\rho(x)} + \frac{1}{x^2(1 + \rho_1 x)} \right)}$$

Simple RGI applies to observables depending on a single E scale.

Numerically RGI=ECH.

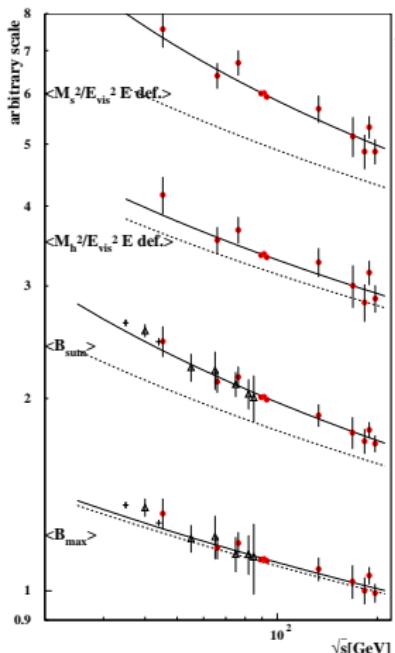
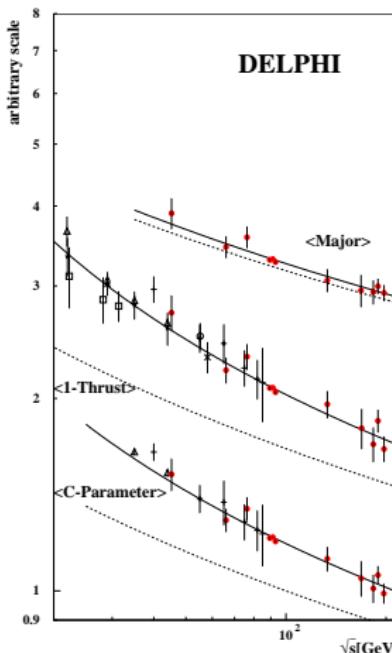
Exact conversion to \overline{MS} .

$$\frac{\Lambda_R}{\Lambda_{\overline{MS}}} = e^{B/2Ab} \left(\frac{2c_1}{b} \right)^{-c_1/b}$$

Include power terms by:

$$\rho(x) \rightarrow \rho(x) - \frac{K_0}{b} x^{-c_1/b} e^{-1/bx}$$

RGI – Description of Shape Observable Means



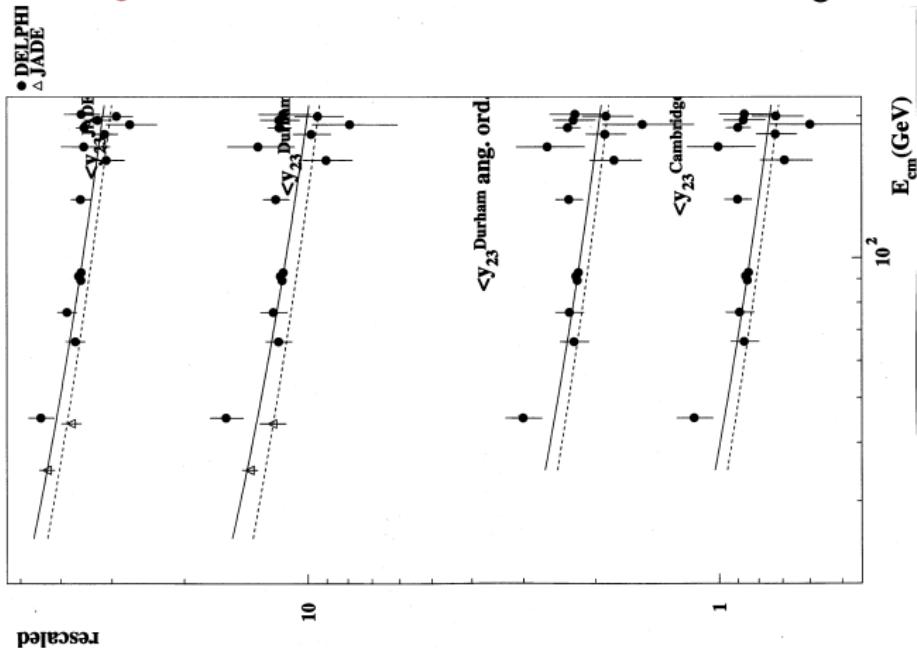
full line
 RGI

dashed
 MS

same Λ

RGI – for $\langle y \rangle$

α_s comes out somewhat lower ! \Rightarrow String effect?



RGI & Means Need no Significant Power Terms

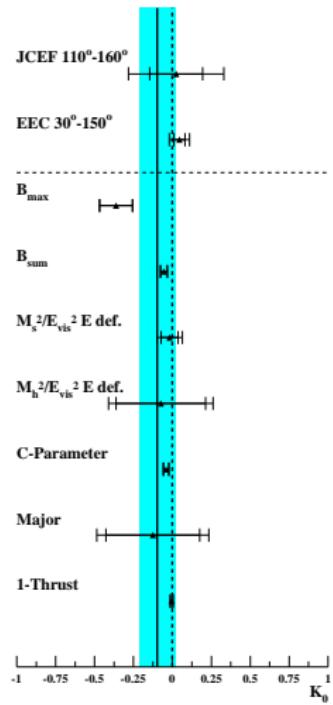
Fitting RGI **with** power-terms to many observable means yields:

K_0 compatible with 0 \Leftrightarrow No P.C.!

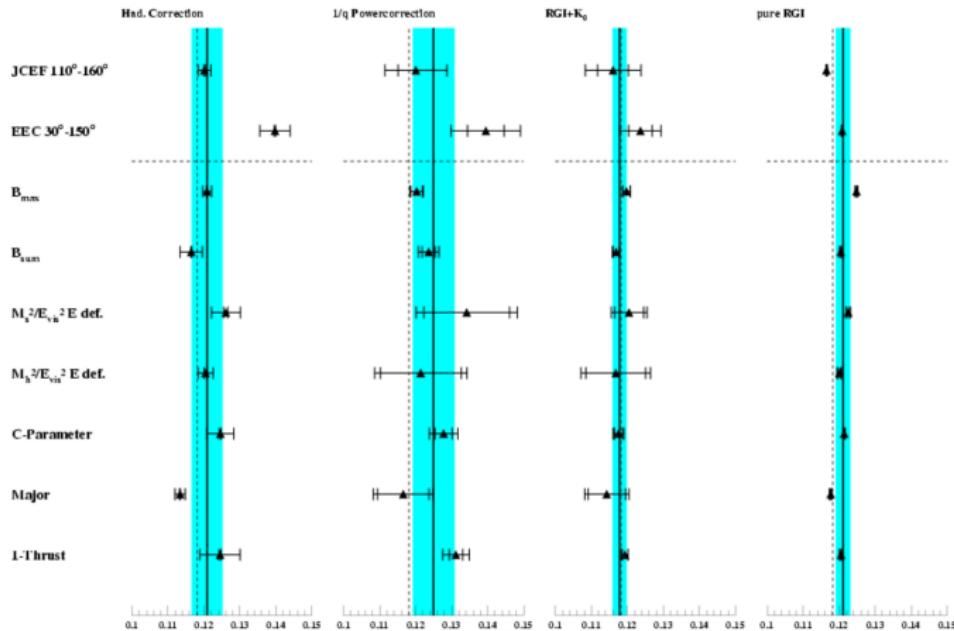
Virtue of both:
 RGI and inclusiveness of mean values.

Presence of genuine power terms for means unclear !

Possible contribution:
 $\mathcal{O}(\sim 2\%)$ (rel.) at the Z.



Cmp. α_s from Means Obtained with Various Methods



RGI yields smallest scatter;

$$\langle \alpha_s(M_Z) \rangle = 0.121 \pm 0.002$$

“Predict” Power Terms using RGI

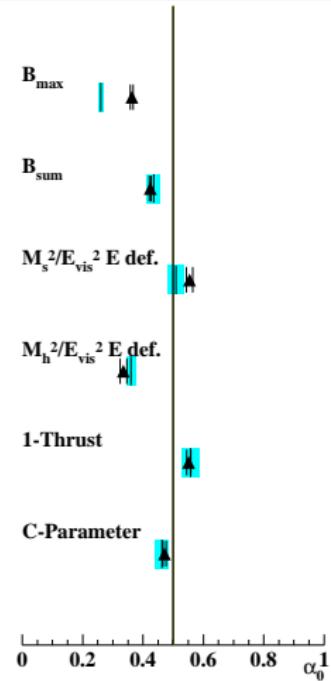
Set RGI and Power Model predictions equal:

$$\langle R \rangle_{RGI} \cdot A = \langle f \rangle_{pert} + \langle f \rangle_{pow}$$

Solve for α_0 .

“Predicted” α_0 follows trend of the data.

Agrees better than any presumed universal value ~ 0.5 .



Measurement of the β -Function

RGI bases on the RGE ,
 β -function can be measured without prior α_s determination!

$$\frac{\partial R^{-1}}{\partial \ln Q^2} = \beta_R = \frac{\beta_0}{4\pi} \left(1 + \frac{\beta_1}{2\pi\beta_0} R + \rho_2 R^2 + \dots \right)$$

⇒ measure $\beta_R \approx \beta$ directly from a mean event shape.
 Measurement is valid even “outside” QCD.

Got consistent results from several observables,
 now use $\langle 1 - T \rangle$ (most data).

Measurement of the β -Function

Using DELPHI and **low energy** data:

$$\frac{\partial R^{-1}}{\partial \ln Q} = 1.38 \pm 0.05$$

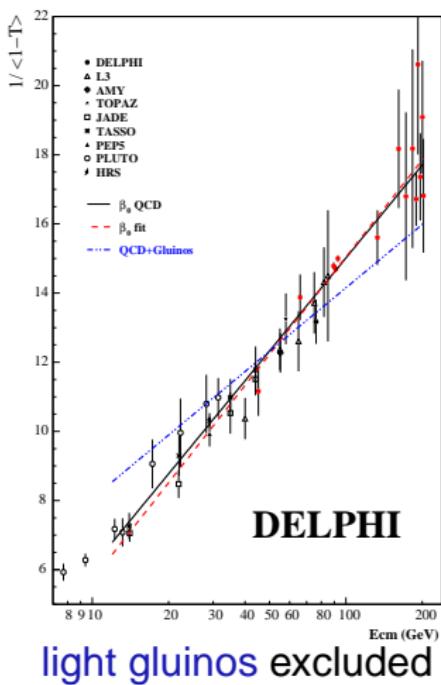
Uncertainty due to power terms **small!**

$$\beta_0 = 7.86 \pm 0.32 \quad n_f = 4.75 \pm 0.44$$

Compare “cross checks” via α_s :

LEP evt. shapes & world data R_τ, F_2, \dots

$$\beta_0 = 7.67 \pm 1.63 \quad \beta_0 = 7.76 \pm 0.44$$



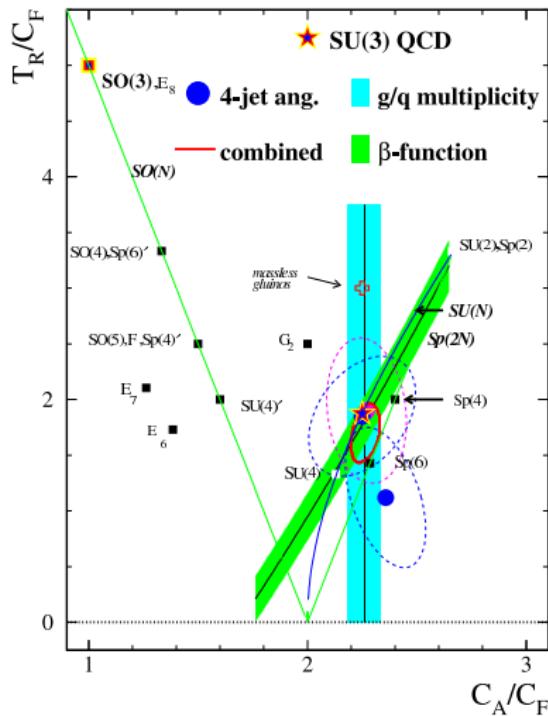
Summary

- $\mathcal{O}(\alpha_s^2)$ predictions with PMS/ECH scales
better describe event shape distributions than \overline{MS} !
 χ^2/n_{df} of α_s average from 18 observabes:

$$\overline{MS} : \frac{71}{17} \quad \text{ECH} : \frac{19}{17} \quad \text{exp. opt.} : \frac{6.2}{17}$$

- Inadequate \overline{MS} scales **bias matched results** !
- RGI can describe E dependence of means **without** power terms.
 \Rightarrow Leads to a direct measurement of the β -function ...

Summary



RGI measurement of the
 β -function
 nicely confirms
 the QCD gauge group!