

# ROOT: Functions & Fitting

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## Review of previous Exercise\*:

\* Good to practice some  
exercises side by side in  
order to understand

## Exercise:

1)

- Create a gaussian function using **TF1** class of Root, set its parameters(500.,65.,5.), plot it and finally save the plot.

Hint: Gaussian function:

```
TF1 f1("gauss", "[0] / sqrt(2.0 * TMath::Pi()) / [2] * exp(-(x-[1])*(x-[1])/2./[2]/[2])", 0, 100)
```

- Create a gaussian distributed random numbers using the Random number generator class **TRandom3** and using the provided basic Random distribution "Gaus(mean=65,sigma=5)". Create a 1-dimensional histogram **TH1D** and fill in with the generated random numbers. Finally book a canvas **TCanvas** and plot the distribution and save it
- Fit the histogram from (2) with function (1)

```
void fit_bgsig()
{
gRandom=new TRandom3();

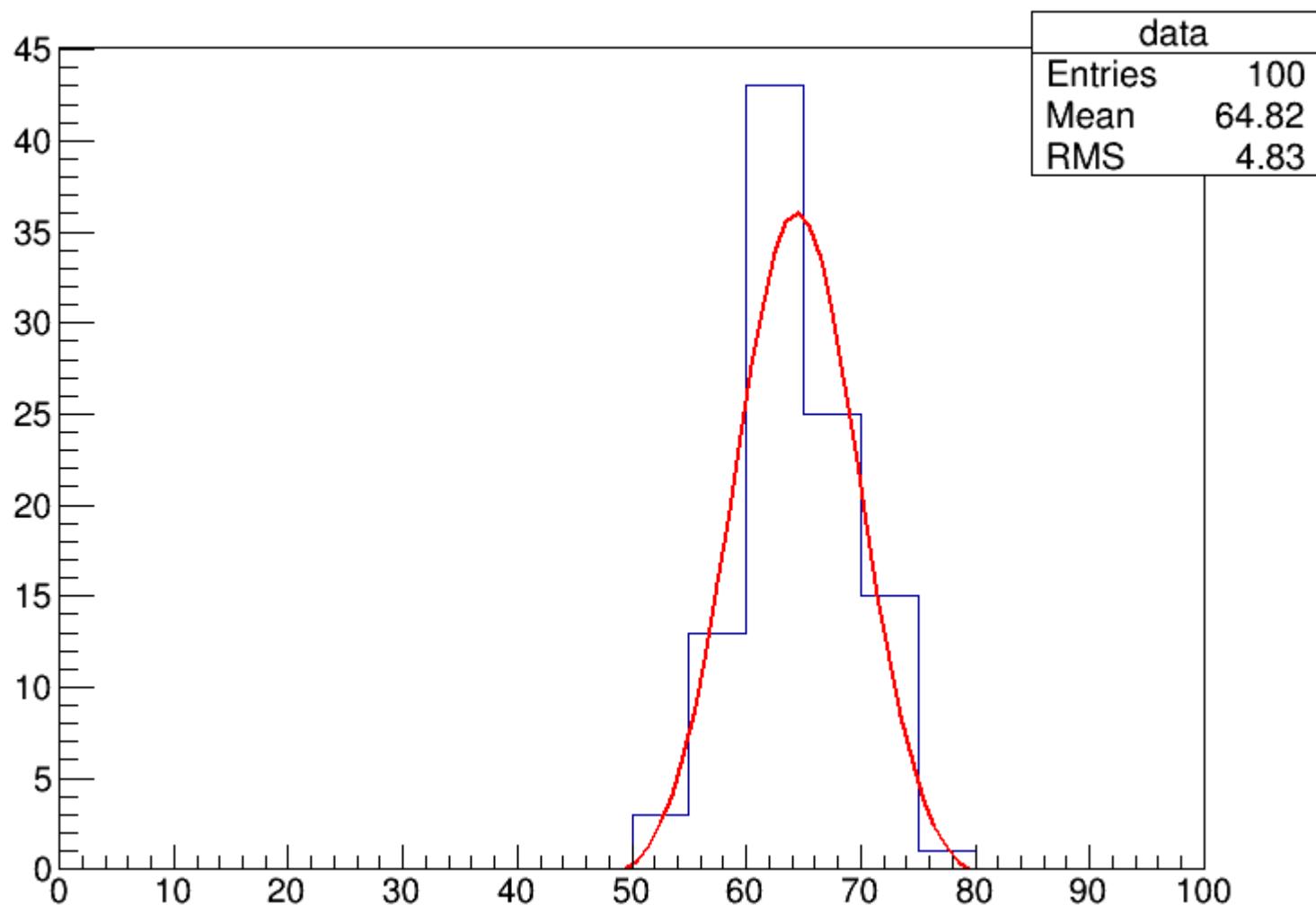
//Define a histogram
TH1D *hist= new TH1D("data","",20,0.0,100.0);

//Fill histogram with Random Number using random distribution "Gaus"
for(int i=0;i<100;i++)
hist->Fill(gRandom->Gaus(65.0,5.0));

//Define Gaussian function with Mean=65.& RMS=5.(Same as histogram)
TF1 *f1=new TF1("myfunc","[0]/sqrt(2.0*TMath::Pi())/[2]*exp(-(x-[1])*(x-[1])/2./[2]/[2])+[3]",0,100);

f1->SetParNames("Constant","Mean","Sigma","Flat");
f1->SetParameters(500.,hist->GetMean(),hist->GetRMS(),2.);

TCanvas *c1=new TCanvas("c1","fit sig+bg", 5,5,800,600);
TFile f("fitting.root","RECREATE");
hist->Fit("myfunc");
hist->Draw();
hist->Write();
f.Close();
hist->SaveAs("fit_ngsig.eps");
}
```



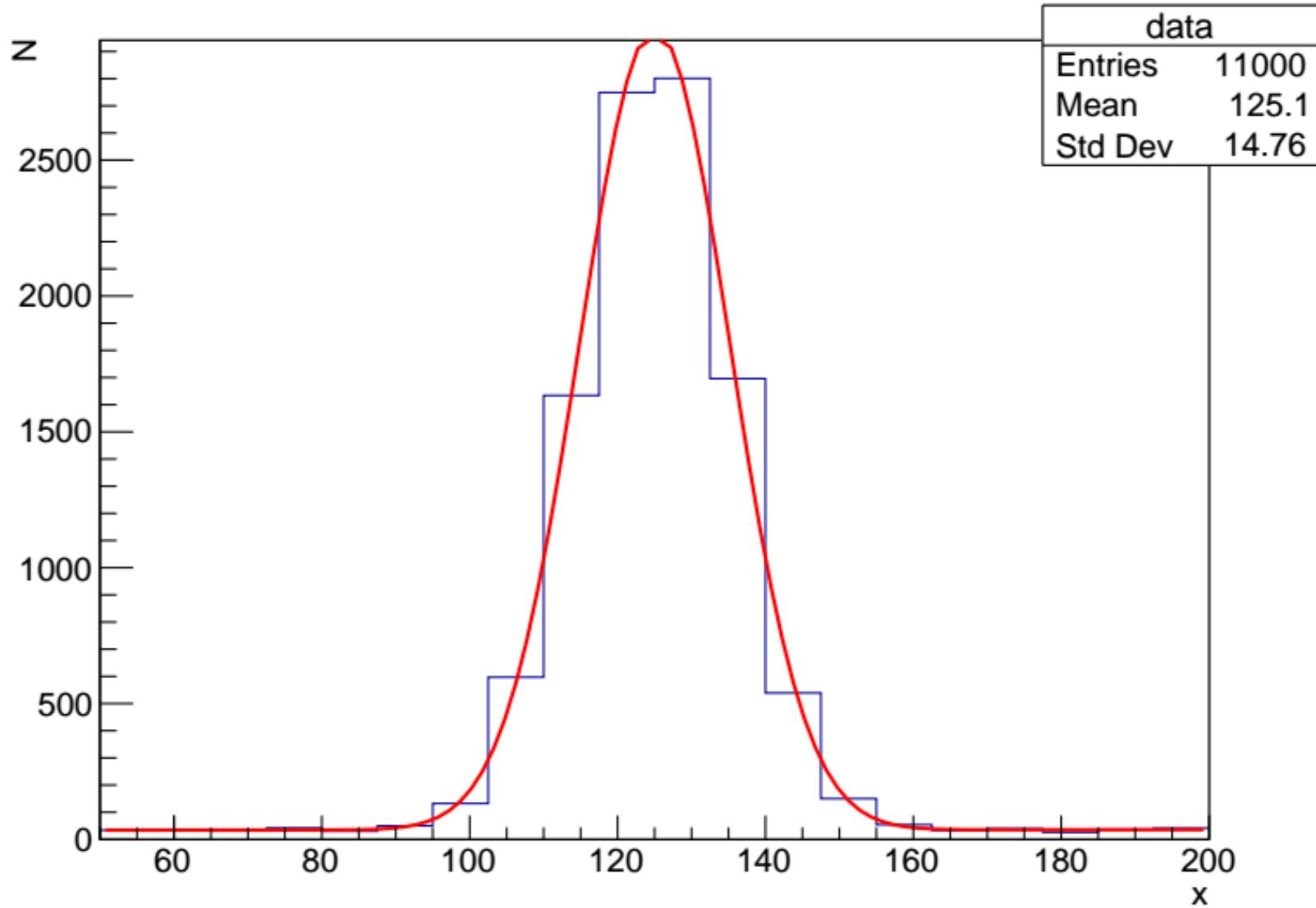
2) Write a root macro that creates randomly generated data as a signal peak (gaussian) with mean= 125.0 & sigma=10.0. Perform fit with a gaussian function and inspect the parameters .

- Add background as uniform
- Fit using function gaus+pol2
- Write down the good parameters.

```

[root [0] gRandom=new TRandom3()
(class TRandom *) 0x7fda455c0600
[root [1] TH1D * hist = new TH1D("data",";x;N",20,50,200)
(class TH1D *) 0x7fda458b9010
[root [2] for (int i = 0; i < 1000; ++i)hist->Fill(200.0 * gRandom->Uniform())
[root [3] for (int i = 0; i < 10000; ++i)hist->Fill(gRandom->Gaus(125,10))
root [4] TF1 *f2 = new TF1("myfunc","[0] / sqrt(2.0 * TMath::Pi()) / [2] * exp(-(x-[1])*(x-[1])/2./[2]/[2]) + [3] + [4] * x * x", 0, 200)
(class TF1 *) 0x7fda43533a40
[root [5] f2->SetParNames("Constant","Mean","Sigma","Flat","pol2")
[root [6] f2->SetParameters(11000,hist->GetMean(),hist->GetRMS(),20,0.0005)
[root [7] f2->SetParLimits(0,9000,13000)
[root [8] f2->SetParLimits(1,100,150)
[root [9] f2->SetParLimits(2,20,60)
[root [10] f2->SetParLimits(3,0,50)
[root [11] f2->SetParLimits(4,0,1)
[root [12] f2->SetLineWidth(2)
[root [13] f2->SetLineColor(2)
[root [14] TCanvas * c1 = new TCanvas("c1", "fit",5,5,800,600)
(class TCanvas *) 0x7fda4354cd30
[root [15] hist->Fit("myfunc")
Info in ROOT::Math::ParameterSettings::: lower/upper bounds outside current parameter value. The value will be set to (low+up)/2
FCN=7476.63 FROM MIGRAD    STATUS=CONVERGED    228 CALLS    229 TOTAL
                           EDM=3.69806e-09    STRATEGY= 1    ERROR MATRIX ACCURATE
EXT PARAMETER                      STEP          FIRST
NO.   NAME        VALUE       ERROR      SIZE      DERIVATIVE
 1  Constant    1.30000e+04  7.55087e+00  3.67019e-03** at limit **
 2  Mean        1.25314e+02  4.13529e-01  6.98473e-04  1.13793e-03
 3  Sigma        2.00000e+01  8.43365e-03  1.22623e-03** at limit **
 4  Flat        3.42013e+01  1.69370e+00  3.07688e-03  1.60653e-04
 5  pol2        1.32894e-13  8.59659e-05  7.82025e-04** at limit **
(TFitResultPtr) @0x7fda45c353c0

```



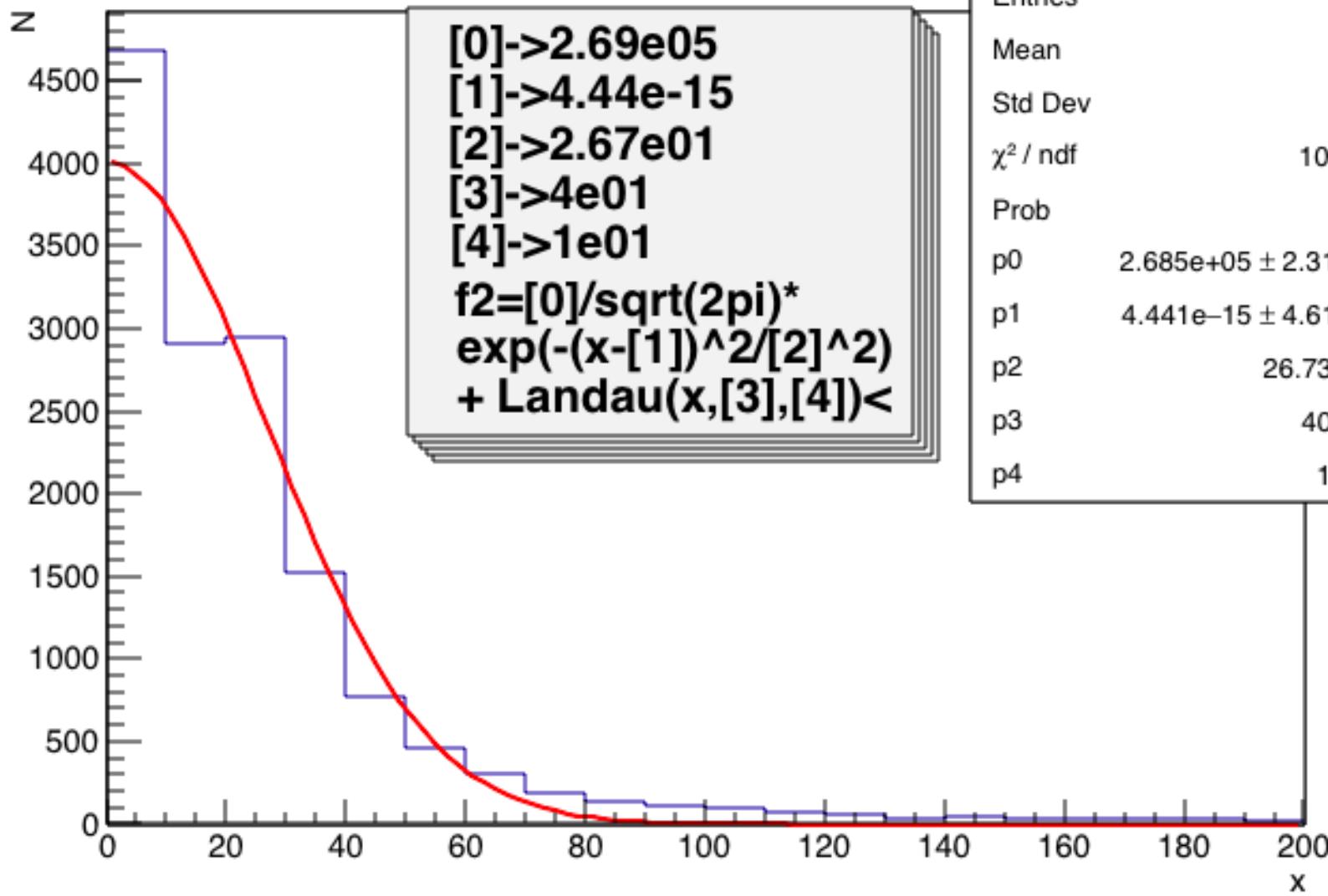
# Full Exercise upto now

- Fill a histogram randomly ( $n \approx 10,000$ ) with a Landau distribution with a most probable value at 20 and a “width” of 5 (use the ROOT website to find out about the Landau function)
- Fill the same histogram randomly ( $n \approx 5,000$ ) with a Gaussian distribution centered at 5 with a “width” of 3
- Write a compiled script with a fit function that describes the total histogram nicely (it might be a good idea to fit both peaks individually first and use the fit parameters for a combined fit)
- Add titles to x- and y-axis
- Include a legend of the histogram with number of entries, mean, and RMS values
- Add text to the canvas with the fitted function parameters
- Draw everything on a square-size canvas (histogram in blue, fit in red)
- Save as png, eps, and root file

```

[root [0] gRandom=new TRandom3()
(class TRandom *) 0x7fc96a526800
[root [1] TH1D * hist = new TH1D("data",";x;N",20,0,200)
(class TH1D *) 0x7fc96b97d510
[root [2] for (int i = 0; i < 10000; ++i)hist->Fill(gRandom->Landau(20,5))
[root [3] hist->Draw()
Info in <TCanvas::MakeDefCanvas>: created default TCanvas with name c1
[root [4] for (int i = 0; i < 5000; ++i)hist->Fill(gRandom->Gaus(5,3))
[root [5] hist->Draw()
root [6] TF1 *f2 = new TF1("myfunc","[0] / sqrt(2.0 * TMath::Pi()) / [2] * exp(-(x-[1])*(x-[1])/2./[2]/[2]) + TMath::Landau(x,[3],[4])", 0, 200)
(class TF1 *) 0x7fc96969bed0
[root [7] f2->SetParameters(70000,hist->GetMean(),hist->GetRMS(),20,5)
[root [8] f2->SetParLimits(0,60000,80000)
[root [9] f2->SetParLimits(1,10,100)
[root [10] f2->SetParLimits(1,0,10)
[root [11] f2->SetParLimits(2,0,40)
[root [12] f2->SetParLimits(3,0,40)
[root [13] f2->SetParLimits(4,0,10)
[root [14] hist->Fit("myfunc")
Info in ROOT::Math::ParameterSettings>: lower/upper bounds outside current parameter value. The value will be set to (low+up)/2
FON=5446.85 FROM MIGRAD      STATUS=CONVERGED      237 CALLS      238 TOTAL
                           EDM=6.0734e-08   STRATEGY= 1    ERROR MATRIX ACCURATE
EXT PARAMETER                      STEP                      FIRST
NO.   NAME        VALUE       ERROR          SIZE      DERIVATIVE
 1 p0           8.00000e+04   1.43744e+01   1.93264e-03*** at limit ***
 2 p1           1.00000e+01   4.96284e-03   1.60588e-03*** at limit ***
 3 p2           1.32694e+01   2.91448e-01   5.57703e-04   6.07687e-03
 4 p3           4.00000e+01   3.81453e+01   9.09214e-02*** at limit ***
 5 p4           1.00000e+01   7.81224e+00   6.11331e-02*** at limit ***
(TFitResultPtr) @0x7fc96bc5fc20

```



# **Simple Straight Line fitting**

# Straight line fit: $y=mx + c$

```
#include <iostream>
#include "TH1D.h"
#include <TMath.h>
#include <TROOT.h>
#include "TF1.h"
using namespace std;

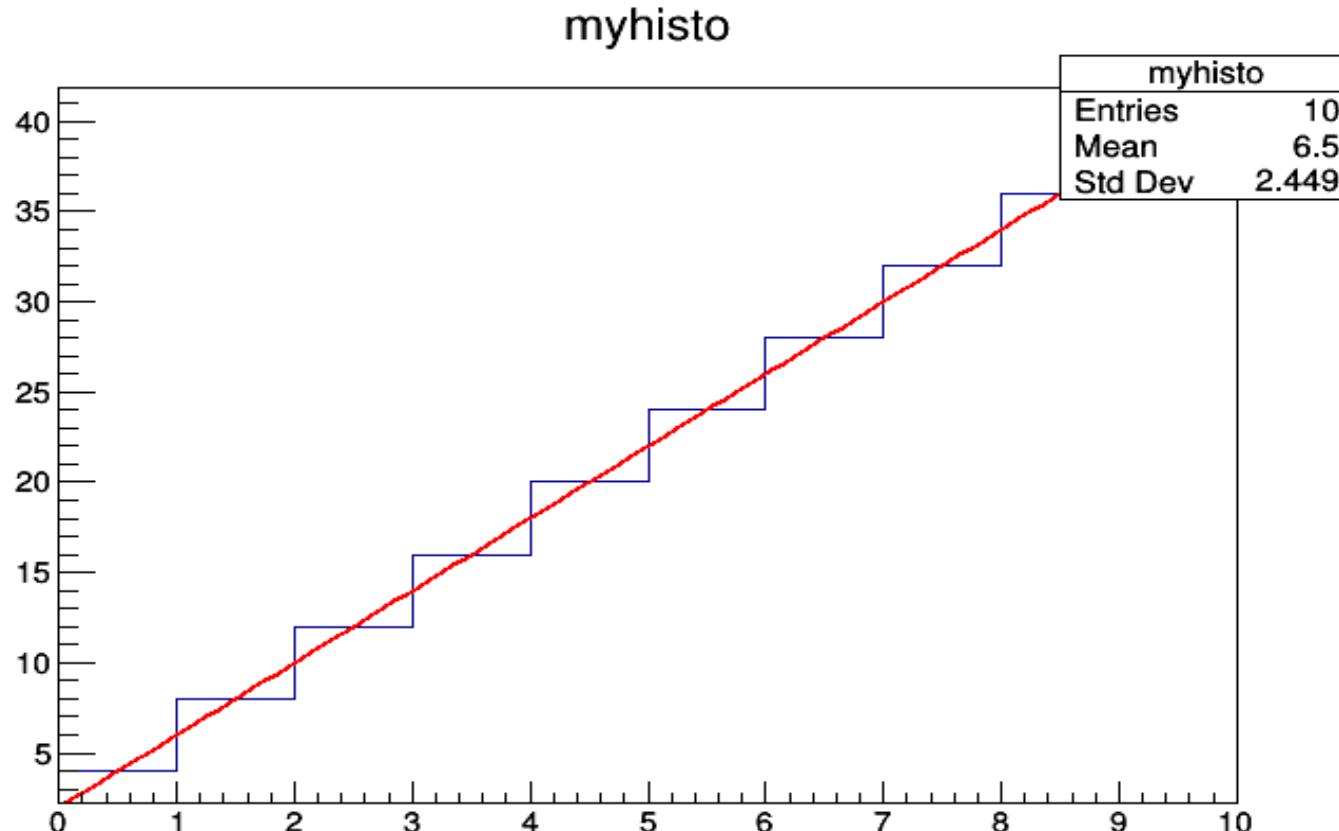
//Declare a user defined function for fitting
Double_t fitf(Double_t *x, Double_t *par)
{
    Double_t value=par[0]+(par[1]*x[0]); //Here par[0]=constant/intercept & par[1] is Gradient
    return value;
}

int run(){
    //Create a histogram to be fitted
    TH1D* myhisto=new TH1D("myhisto","myhisto",10,0,10);
    //Fill the histogram
    for (int i=1; i<=10; i++){
        myhisto->SetBinContent(i,i*4); //Randomly
    }
}
```

## Contd:

```
//Create a TF1 object with the function defined above..  
//The last three parameters specify the range and number of parameters of the function.  
TF1 *func=new TF1("fit", fitf,0,10,2);  
  
//Set the initial paramters of the function  
func->SetParameters(0.04,0.1);  
  
//Give the parameters meaningful name  
func->SetParNames("intercept","gradient");  
  
//Call TH1::Fit with the name of TF1 Object  
myhisto->Fit("fit");  
  
//Access the Fit results directly  
cout<<"The y-intercept is: "<<func->GetParameter(0)<<endl;  
cout<<"The gradient(constant) is: "<<func->GetParameter(1)<<endl;  
cout<<"Fitting completed...."<<endl;  
  
return 0; }
```

```
harinder@harinder-Latitude-E6430:~/root_examples$ root -l run.C
root [0]
Processing run.C...
Info in <TCanvas::MakeDefCanvas>: created default TCanvas with name c1
FCN=1.43736e-23 FROM MIGRAD      STATUS=CONVERGED      30 CALLS      31 TOTAL
                           EDM=2.87472e-23    STRATEGY= 1    ERROR MATRIX ACCURATE
EXT PARAMETER                      STEP          FIRST
NO.   NAME        VALUE       ERROR        SIZE      DERIVATIVE
  1  intercept     2.00000e+00  1.73039e+00  5.70614e-04  1.95947e-12
  2  gradient      4.00000e+00  4.37916e-01  1.44407e-04 -1.07963e-11
The y-intercept is: 2
The gradient(constant) is: 4
Fitting completed....
(int) 0
```



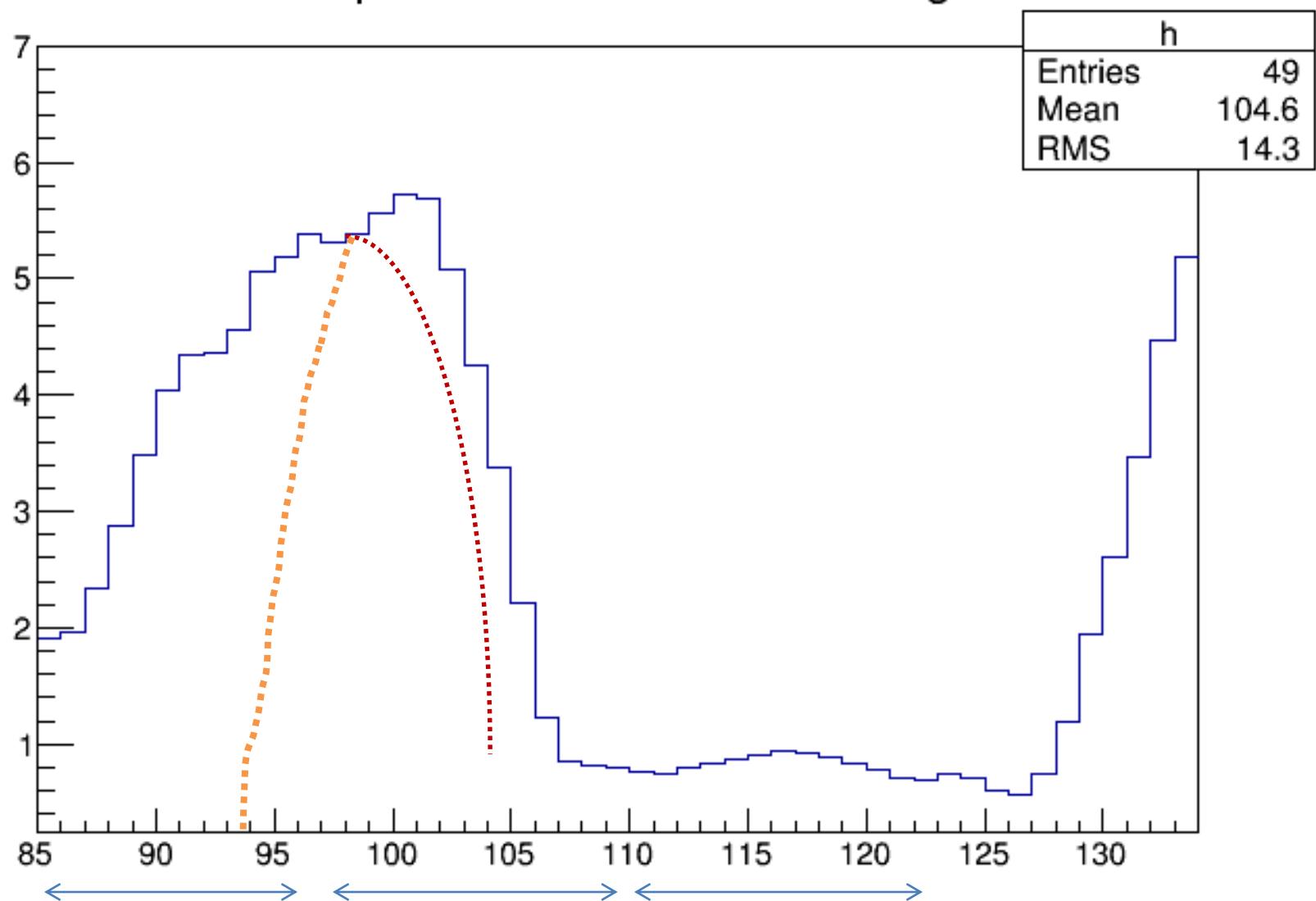
# Complex fitting

# Multi Peak Histogram Fitting

```
#include "TH1.h"
#include "TF1.h"
void multifit() {
    const Int_t np = 49;
    Float_t x[np] = {1.913521, 1.953769, 2.347435, 2.883654, 3.493567,
                     4.047560, 4.337210, 4.364347, 4.563004, 5.054247,
                     5.194183, 5.380521, 5.303213, 5.384578, 5.563983,
                     5.728500, 5.685752, 5.080029, 4.251809, 3.372246,
                     2.207432, 1.227541, 0.8597788, 0.8220503, 0.8046592,
                     0.7684097, 0.7469761, 0.8019787, 0.8362375, 0.8744895,
                     0.9143721, 0.9462768, 0.9285364, 0.8954604, 0.8410891,
                     0.7853871, 0.7100883, 0.6938808, 0.7363682, 0.7032954,
                     0.6029015, 0.5600163, 0.7477068, 1.188785, 1.938228,
                     2.602717, 3.472962, 4.465014, 5.177035};

    TH1F *h = new TH1F("h", "Example of several fits in subranges", np, 85, 134);
    h->SetMaximum(7);
    for (int i=0;i<np;i++) {
        h->SetBinContent(i+1,x[i]);
    }
    h->Draw();
```

## Example of several fits in subranges



# Fitting

 (Fitting multiple functions to different ranges of a 1-D histogram)

```
Double_t par[9];
```

//3 gaussians are fitted in sub-ranges of this histogram

```
TF1 *g1 = new TF1("g1","gaus",85,95);//sub-Range
```

```
TF1 *g2 = new TF1("g2","gaus",98,108);
```

```
TF1 *g3 = new TF1("g3","gaus",110,121);
```

//A new function (a sum of 3 gaussians) is fitted on another subrange

```
TF1 *total = new TF1("total","gaus(0)+gaus(3)+gaus(6)",85,125);
```

```
total->SetLineColor(2);
```

```
h->Fit(g1,"R"); //Fit according to sub-Range only
```

```
h->Fit(g2,"R+");
```

```
h->Fit(g3,"R+");
```

//Note that when fitting simple functions, such as gaussians, the initial values of parameters are automatically computed by ROOT.

// In the more complicated case of the sum of 3 gaussians, the initial values of parameters must be given. In this particular case, the initial values are taken from the result of the individual fits

```
g1->GetParameters(&par[0]);
```

<https://root.cern.ch/doc/master/classTF1.html>

```
g2->GetParameters(&par[3]);
```

```
g3->GetParameters(&par[6]);
```

```
total->SetParameters(par);
```

```
h->Fit(total,"R+"); }
```

```

root [1] .x multifit.C
Warning in <TROOT::Append>: Replacing existing TH1: h (Potential memory leak).
Info in <TCanvas::MakeDefCanvas>: created default TCanvas with name c1
FCN=0.0848003 FROM MIGRAD STATUS=CONVERGED 105 CALLS 106 TOTAL
EDM=1.77382e-007 STRATEGY= 1 ERROR MATRIX ACCURATE

EXT PARAMETER STEP FIRST
NO. NAME VALUE ERROR SIZE DERIVATIVE
1 Constant 4.96664e+000 2.83221e+000 4.26889e-004 1.67619e-004
2 Mean 9.54663e+001 1.23905e+001 7.53972e-004 -2.63161e-004
3 Sigma 6.82779e+000 7.49131e+000 5.87496e-005 3.68521e-003
FCN=0.0771026 FROM MIGRAD STATUS=CONVERGED 72 CALLS 73 TOTAL
EDM=2.00364e-007 STRATEGY= 1 ERROR MATRIX ACCURATE

EXT PARAMETER STEP FIRST
NO. NAME VALUE ERROR SIZE DERIVATIVE
1 Constant 5.96312e+000 1.14355e+000 4.82019e-004 1.52951e-004
2 Mean 1.00467e+002 1.53372e+000 3.74926e-004 6.69980e-004
3 Sigma 3.54806e+000 1.16899e+000 3.22077e-005 3.86167e-003
FCN=0.0087702 FROM MIGRAD STATUS=CONVERGED 93 CALLS 94 TOTAL
EDM=5.57239e-007 STRATEGY= 1 ERROR MATRIX ACCURATE

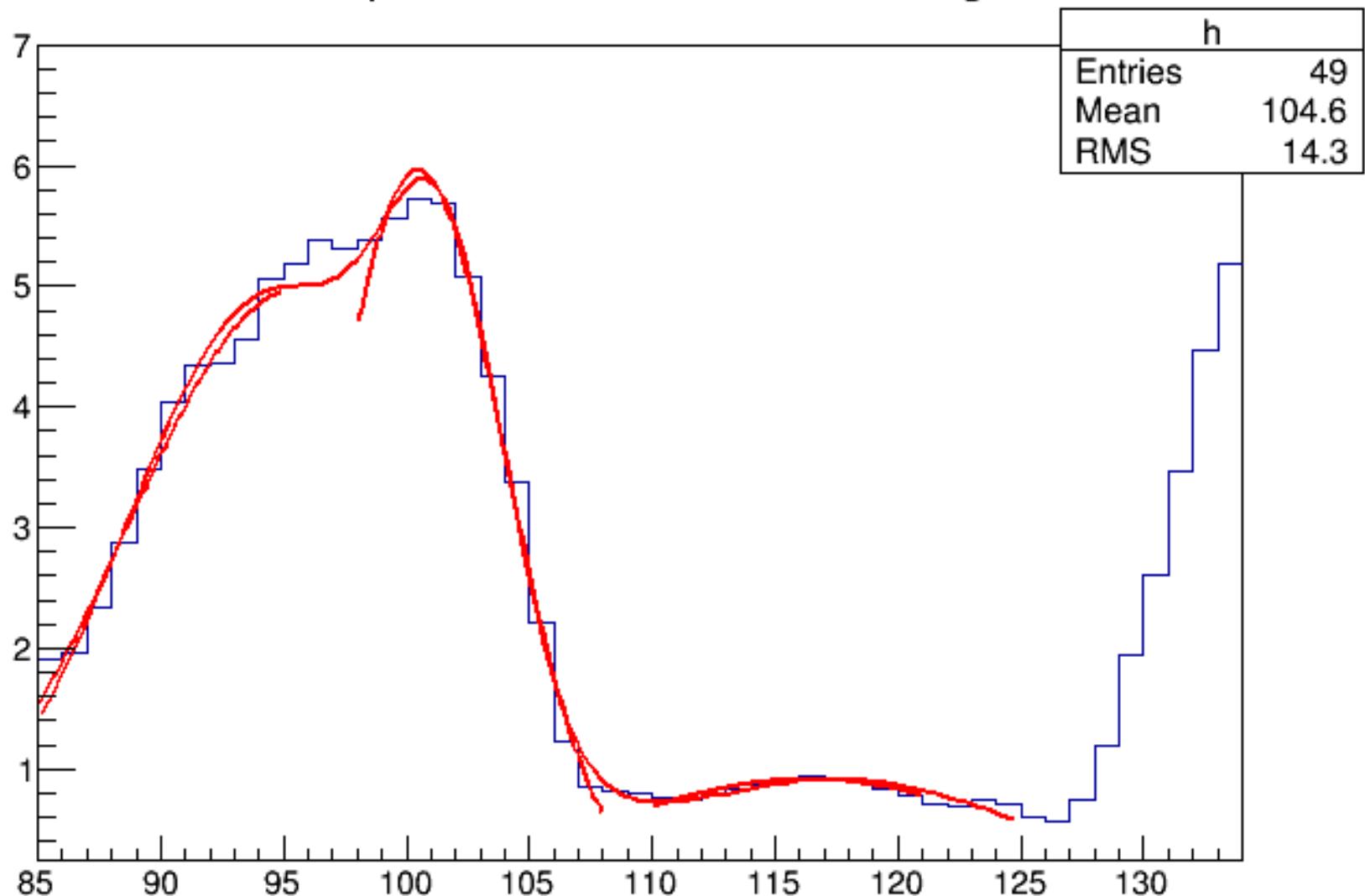
EXT PARAMETER STEP FIRST
NO. NAME VALUE ERROR SIZE DERIVATIVE
1 Constant 9.12665e-001 4.37176e-001 1.46528e-004 2.91010e-004
2 Mean 1.16309e+002 8.37408e+000 3.57386e-003 -3.17966e-005
3 Sigma 8.38413e+000 1.84577e+001 4.99414e-004 -4.98793e-004
FCN=0.312817 FROM MIGRAD STATUS=CONVERGED 515 CALLS 516 TOTAL
EDM=1.73245e-007 STRATEGY= 1 ERROR MATRIX ACCURATE

EXT PARAMETER STEP FIRST
NO. NAME VALUE ERROR SIZE DERIVATIVE
1 p0 4.91145e+000 1.41387e+000 3.61239e-004 -3.22790e-004
2 p1 9.44525e+001 3.71612e+000 5.60861e-004 -6.78941e-005
3 p2 5.94796e+000 2.41732e+000 4.25396e-004 2.68176e-005
4 p3 3.22134e+000 3.11650e+000 5.86729e-004 -1.82620e-004
5 p4 1.01663e+002 1.67863e+000 5.56527e-004 3.95769e-004
6 p5 2.48454e+000 1.91461e+000 3.85832e-004 7.23818e-005
7 p6 9.11463e-001 3.68235e-001 1.45489e-004 5.77239e-004
8 p7 1.17582e+002 5.06329e+000 2.01798e-003 -8.25382e-005
9 p8 7.58627e+000 8.76000e+000 2.12468e-003 2.02614e-005

```

```
root [2]
```

## Example of several fits in subranges



# Exercise

- ❖ First create an histogram with a double gaussian peaks and then we fit it.
- ❖ Create an histogram with 100 bins between 0 and 10.
- ❖ Fill with 5000 Gaussian number with mean 3 and width 1.5.
- ❖ Fill with 5000 Gaussian number with a mean of 8 and width of 1.
- ❖ Create a function composed of the sum of two Gaussian and fit to the histogram.
- ❖ Do the fit works ? What do you need to do to make the fit working ?

## Hint

Before fitting you need to set sensible parameter values. You can do this by fitting first a single Gaussian in the range [0,5] and then a second Gaussian in the range [5,10]. If you don't set good initial parameter values, (for example if you set the amplitude of the Gaussians to 1, the means of the Gaussians to 5 and widths to 1), the fit will probably not converge.

# BACKUP

# Functions

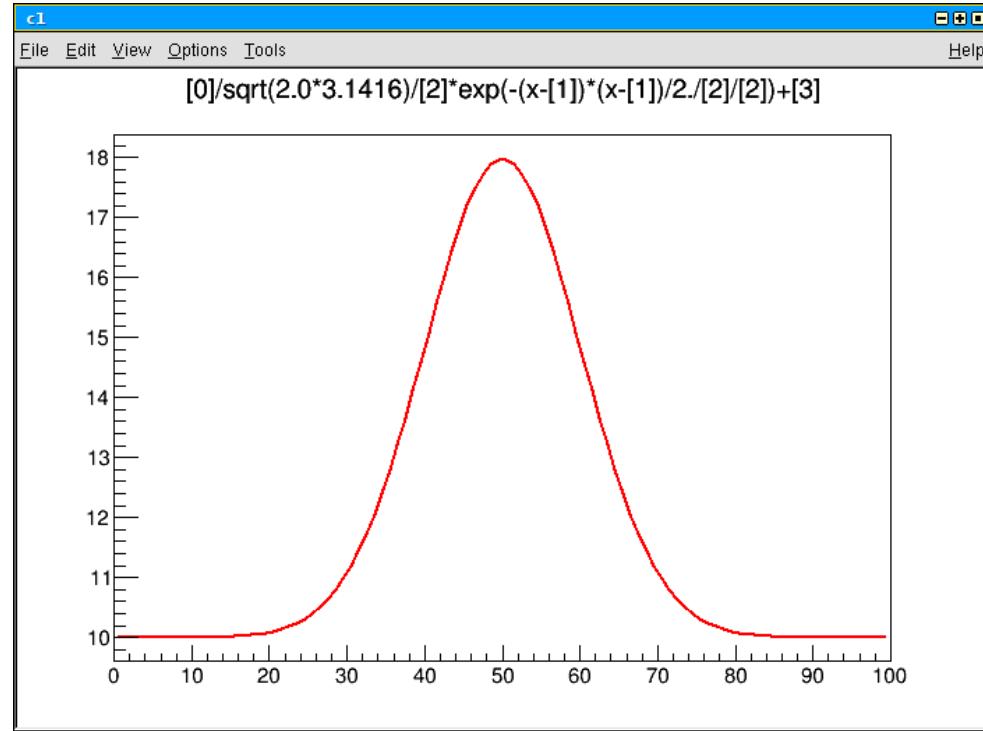
# TF1 with parameters

A function can have **parameters** (e.g. floating parameters for fits...)

{

```
TF1 * f1 = new TF1("f1",
                    "[0] / sqrt(2.0 * 3.1416) / [2] * exp(-(x-[1])*(x-[1])/2./[2]/[2]) + [3]",
                    0., 100.);
f1->SetParameter(0, 200.0);
f1->SetParameter(1, 50.0);
f1->SetParameter(2, 10);
f1->SetParameter(3, 10);
f1->Draw();

} --- . .
root [6] f1->GetParameter(0)
(const Double_t)2.0000000000000000e+02
root [7] f1->GetParameter(1)
(const Double_t)5.0000000000000000e+01
root [8] f1->GetParameter(2)
(const Double_t)1.0000000000000000e+01
root [9] f1->GetParameter(3)
(const Double_t)1.0000000000000000e+01
```

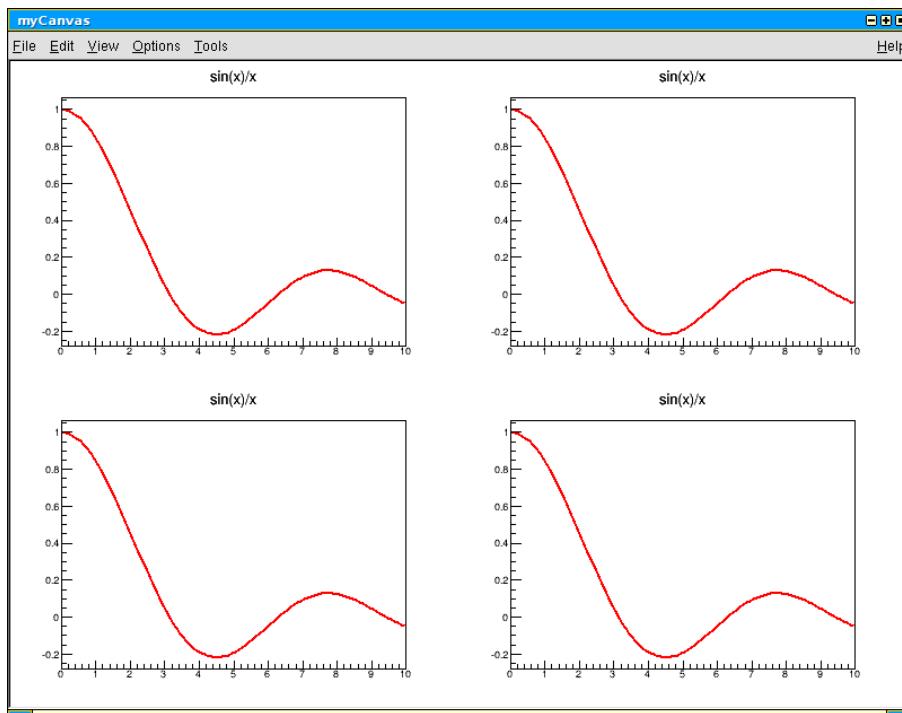


# Let's draw a TF1 on a TCanvas

Like most objects in ROOT, functions can be drawn on a canvas

a TCanvas is an object too...

```
root [3] TF1 of("myFunction","sin(x)/x",0,10)
root [4] of.Draw()
Info in <TCanvas::MakeDefCanvas>: created default TCanvas
with name _c1
```



```
root [10] TCanvas c("myCanvas", "myCanvas"
, 800, 600)
```

...it can be divided in TPads

```
root [1] c.Divide(2,2)
root [3] c.cd(2)
(class TVirtualPad*) 0x242a890
root [4] of.Draw()
root [5] c.cd(1)
(class TVirtualPad*) 0x242a510
root [6] of.Draw()
root [7] c.cd(3)
(class TVirtualPad*) 0x242ac30
root [8] of.Draw()
root [9] c.cd(4)
(class TVirtualPad*) 0x242afb0
root [10] of.Draw()
```

...and saved as an image

```
root [6] c.SaveAs("myFunction.png")
Info in <TCanvas::Print>: png file myFunction.png has
been created
```

# Functions and Histograms

## ➤ Define a function:

```
TF1 *myfunc=new TF1("myfunc","gaus",0,3);  
Myfunc->SetParameters(10., 1.5, 0.5);  
Myfunc->Draw();
```

## ➤ Generate histograms from functions:

```
(Myfunc->GetHistogram())->Draw();
```

## ➤ Generate histograms with random numbers from a function:

```
TH1F *hgaus=new TH1F("hgaus","histo from gaus", 50,  
0,3);  
hgaus->FillRandom("myfunc",10000);  
hgaus->Draw();
```

## ➤ Write histogram to a rootfile:

```
TFile *myfile= new Tfile("hgaus.root","RECREATE");  
hgaus->Write();  
myfile->Close();
```

# Fitting Histograms

Let us try to fit the histogram created by the previous step:

Interactively:

- Open rootfile containing histogram:  
`root -l hgaus.root`
- Draw histogram  
`hgaus->Draw()`
- Right click on the histogram and select “Fit Panel”
- Check to ensure:
- “gaus” is selected in the Function->Predefined pop-menu
- “Chi-square” is selected in the Fit Settings->Method menu
- Click on “Fit” at the bottom

[Display fit parameters: Select Options->FitParameters]

# A couple of words about Fitting

## Fitting in a nut-shell:

A mathematical procedure to find parameter values of a TFn function,  $f$ , describing *the best* your histogram or graph ( $x, y$ ). The most commonly used criteria for an optimum fit is to *minimize* the  $\chi^2$ -function:

$$\chi^2 = \sum \left( \frac{y_i - f(x_i)}{\sigma_i} \right)^2$$

Thumb rule for *Goodness of Fit*:  $\chi^2/\text{NDF} \sim 1$

...but there is *much much more* to fitting and statistical data analysis, which fills a course by itself...

## Fitting contd:

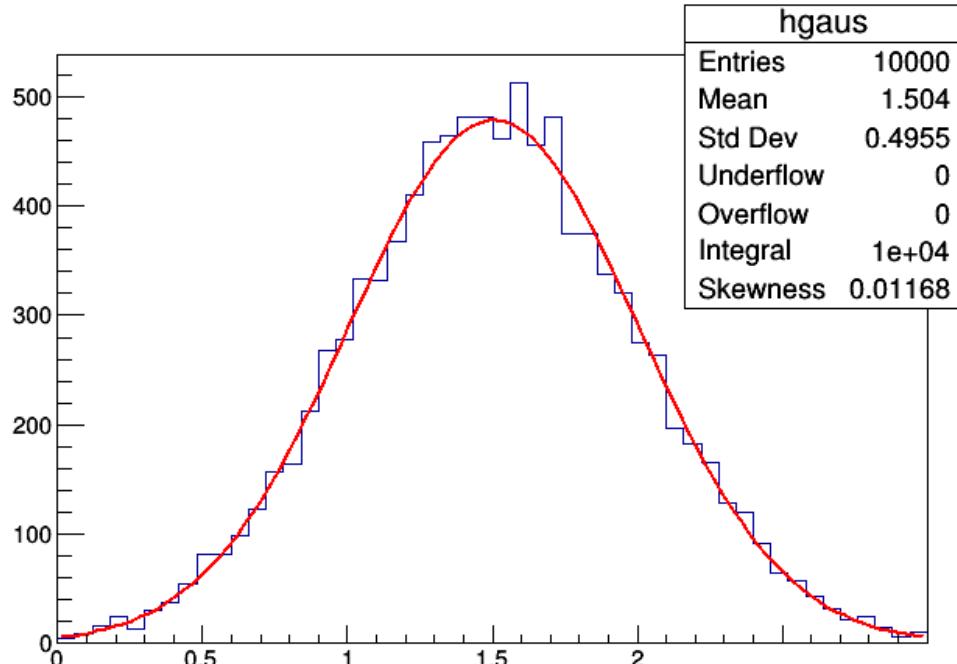
Using user defined functions:

- Create a file called user\_func.C with the following contents:

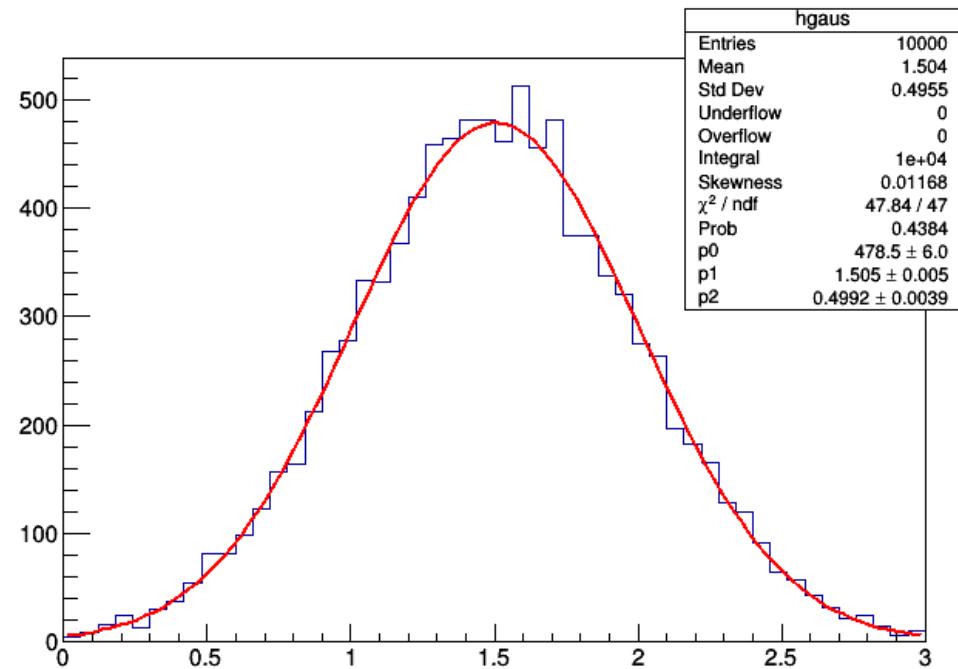
```
harinder@harinder-Latitude-E6430: ~/ROOT
double user_func(double *x, double *par){
    double arg=0;
    if(par[2])arg=(x[0]-par[1])/par[2];
    return par[0]*TMath::Exp(-0.5*arg*arg);
}
```

```
harinder@harinder-Latitude-E6430:~/ROOT$ ls
gaus.root  histo.C  user_func.C
harinder@harinder-Latitude-E6430:~/ROOT$ root -l gaus.root
root [0]
Attaching file gaus.root as _file0...
(class TFile *) 0x9136958
root [1] .L user_func.C
root [2] TF1 *f1=new TF1("f1", user_func, 0, 3, 3); ←
root [3] hgaus->Draw()
Info in <TCanvas::MakeDefCanvas>: created default TCanvas with name c1
root [4] f1->SetParameters(10, hgaus->GetMean(), hgaus->GetRMS());
root [5] hgaus->Fit("f1");
FCN=28.5714 FROM MIGRAD   STATUS=CONVERGED   172 CALLS   173 TOTAL
                           EDM=4.37095e-11   STRATEGY= 1   ERROR MATRIX ACCURATE
EXT PARAMETER            STEP          FIRST
NO. NAME      VALUE       ERROR        SIZE      DERIVATIVE
 1 p0          7.97277e+02  9.78840e+00  2.11998e-02 -5.33649e-07
 2 p1          1.50390e+00  5.00504e-03  1.32879e-05 -1.59987e-03
 3 p2          4.99048e-01  3.55395e-03  7.69647e-06 -1.76223e-04
root [6]
```

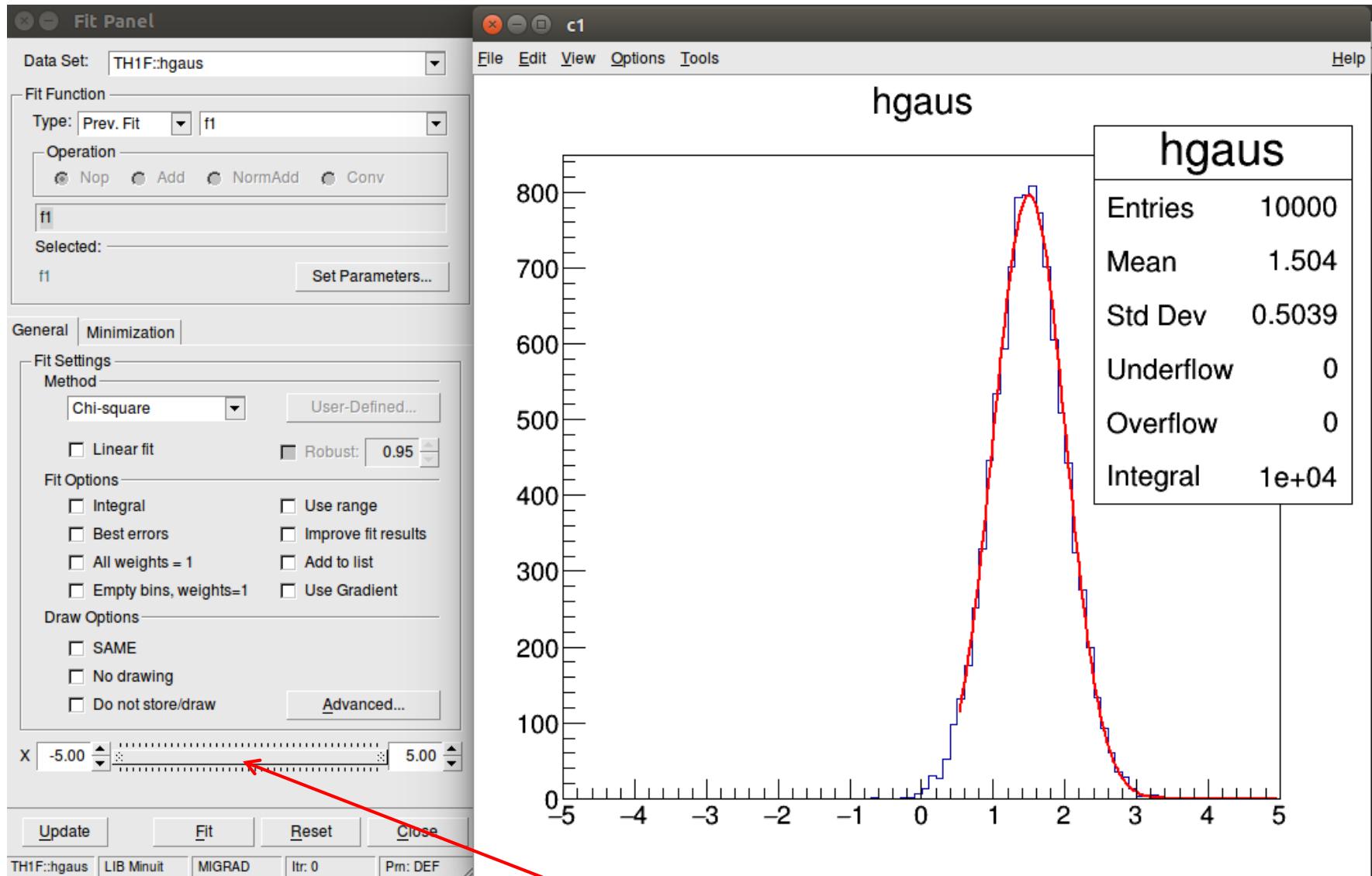
Last 3 parameters specify  
the number of parameters  
for the function



gStyle->SetOptStat(1111111)  
Also can try :  
gStyle->SetOptFit(1111)



# Fitting contd:



Move the slider to change fit Range

```
void fit_bgsig()
{
    // style setting
    gROOT->SetStyle("Plain");
    gStyle->SetOptFit(111111);
    gStyle->SetFrameBorderMode(0);
    gStyle->SetFillColor(0);
    gStyle->SetCanvasColor(0);
    gStyle->SetFrameFillColor(0);
    gStyle->SetCanvasBorderMode(0);

    // create a random number generator
    gRandom = new TRandom3();

    // create a histogram
    TH1D * hist = new TH1D("data", ";x;N", 20, 0.0, 100.0);

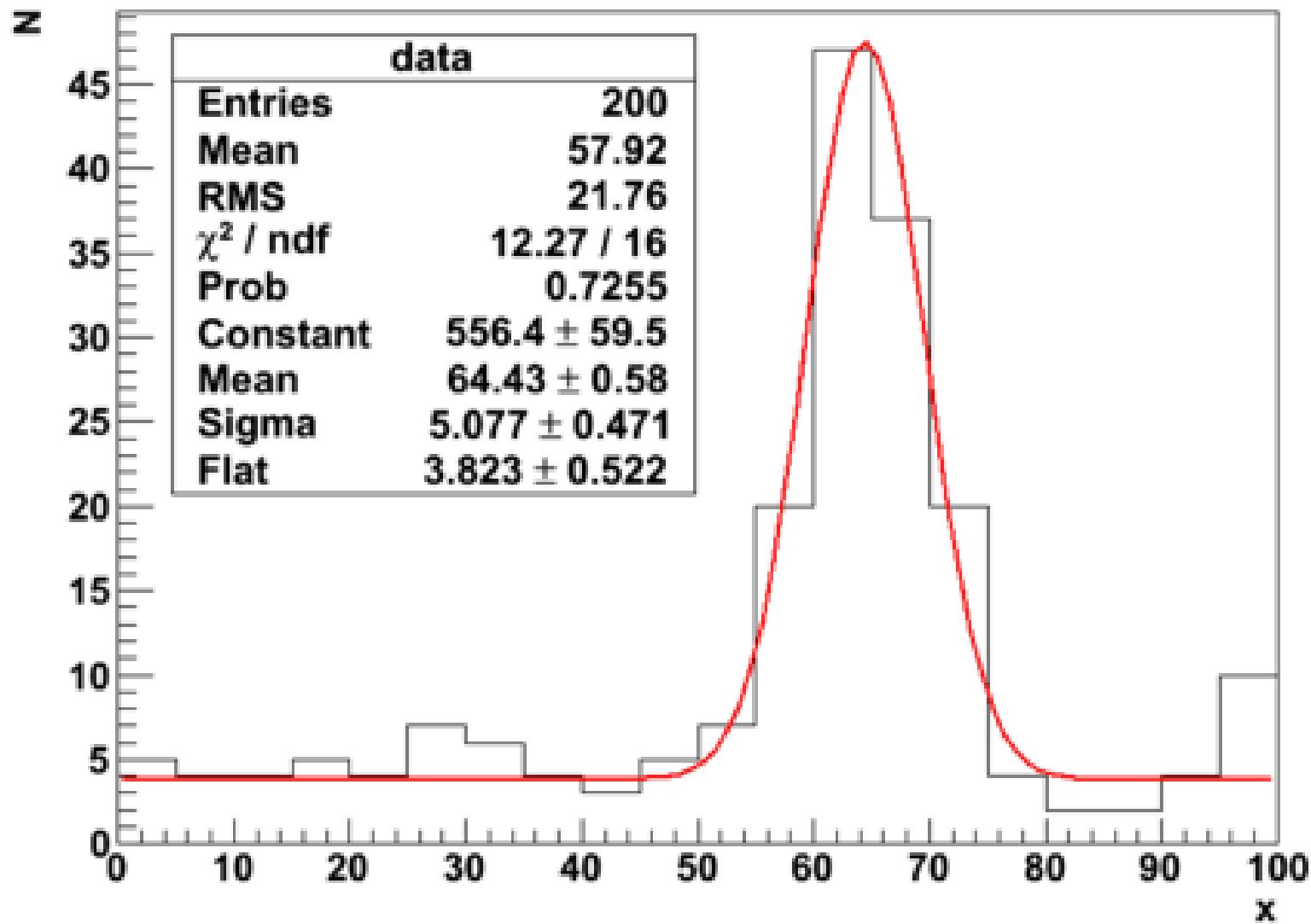
    // fill in signal
    for (int i = 0; i < 100; ++i)
        hist->Fill(gRandom->Gaus(65.0, 5.0));
    // fill background
    for (int i = 0; i < 100; ++i)
        hist->Fill(100.0 * gRandom->Uniform());

    // define a fit function = gauss + pol0
    TF1 * f1 = new TF1("myfunc", "[0] / sqrt(2.0 * TMath::Pi()) / [2] * exp(-(x-[1])*(x-[1])/2./[2]/[2]) + [3]", 0, 100);

    //set parameter start values (mandatory).
    f1->SetParNames("Constant","Mean","Sigma","Flat");
    f1->SetParameters(700.,hist->GetMean(),hist->GetRMS(),2.);
    f1->SetParLimits(0, 100.0, 700.0);
    f1->SetParLimits(1, 50.0, 90.0);
    f1->SetParLimits(2, 0.1, 10.0);
    f1->SetParLimits(3, 0.0, 10.0);
    f1->SetLineWidth(2);
    f1->SetLineColor(2);

    // create a canvas to draw the histogram
    TCanvas * c1= new TCanvas("c1", "fit sig+bg",5,5,800,600);
    // perform fit
    hist->Fit("myfunc");
    hist->Draw();
    hist->SaveAs("fit_bgsig.eps");
}
```

Mean=65, sigma=5.



# Generating with standard PDF's

- Provided methods of TRandomN objects:
  - `Exp(tau)`
  - `Integer(imax)`
  - `Gaus(mean, sigma)`
  - `Rndm()`
  - `RndmArray(n, x)`
  - `Uniform(x)`
  - `Uniform(x1, x2)`
  - `Landau(mpv, sigma)`
  - `Poisson(mean)`
  - `Binomial(ntot, prob)`

<https://root.cern.ch/doc/master/classTRandom.html>