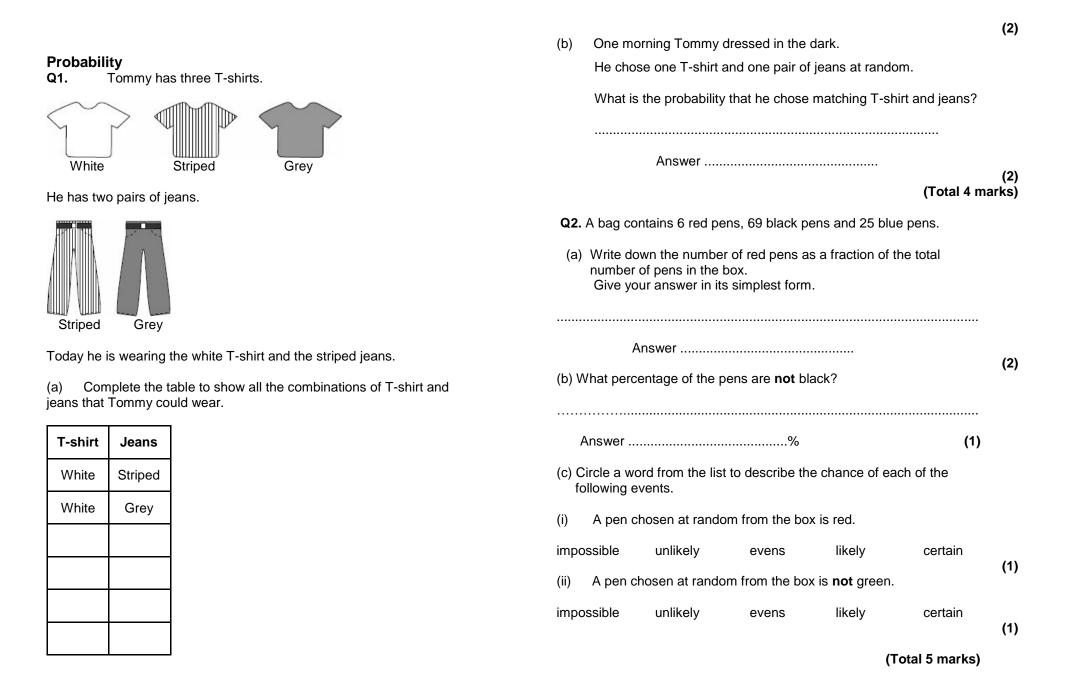


St Paul's Catholic School Mathematics GCSE Revision MAY HALF TERM

PACK 4 – STATISTICS AND PROBABILITY TOPICS TO GRADE 4/5

Name: _____

Maths Teacher:_____



Q3. Ronan is designing a game.

He has two sets of discs laid face down on a table.

The first set of five discs are labelled 1, 3, 5, 7, 9.

The second set of four discs are labelled 2, 4, 6, 8.

Players turn over one disc, at random, from each set and add the numbers together.

(a) Complete the table to show **all** the possible totals.

	1	3	5	7	9
2	3	5	7		
4	5				
6					
8					

(b) What is the probability of getting a total less than six?

Answer

(1)

(2)

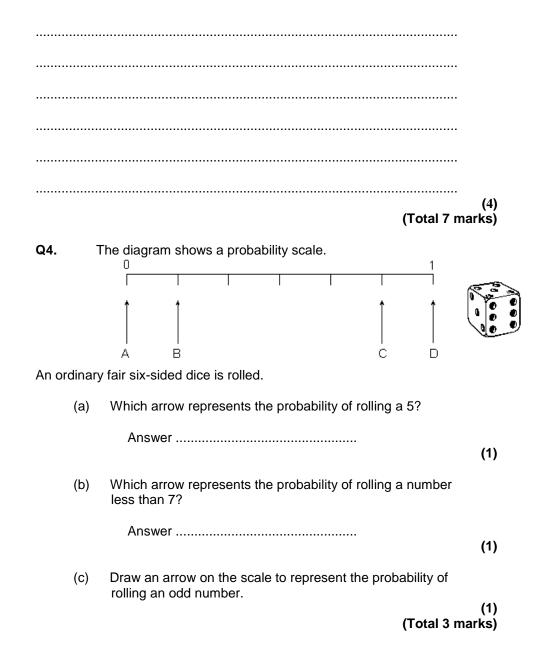
(c) Ronan uses the game to raise money for charity.

Each player pays 20 p to play the game.

If a player gets a total of exactly 13 they win a bar of chocolate.

It costs Ronan 50 p for each bar of chocolate.

If 100 people play the game, show that Ronan should expect to raise \pounds 12.50 for charity.



5	7 5 6 4 9 8 10 5						Sarah is pla She spins	the coin	and then	throws the	e dice.		
(a)	Work out the me	dian.				show	coin shows n on the dic umber show	e. If the	coin show				
	/er					(a)	Complete	e the tabl	e to show	/ all possib	le scores		(2)
7 (110)					(2)					D	ice		
(b)	One of the numb	ers is chosen at random.					ſ	1	2	3	4	5	6
(i)	What is the prob	ability that the number is	5?			Coin	Heads				5		
							Tails	-1					
	Answe	r			(1)	(b)	Work out t	he proba	bility that	Sarah's s	core is		
(ii)	Put these events	in order of likelihood sta	rting with	the least likely.		(i)	negative	ne proba	bility that	Odiali 5 3			
	А	The number is 5.				(1)	-	ver					
	В	The number is even.											(1)
	С	The number is greater	r than 8.			(ii)	more than	3.					
							A	nswer					(2)
													(2)

(1)

+ Fill in the missing number in the table. (a) Work out the probability that the total is 6. (i) (b) Answer (ii) Work out the probability that the numbers on the dice are the same.

Q7. Two fair dice are thrown and their scores added together.

The table shows some of the possible totals.

- Answer
- Work out the probability that the total is a square number. (iii)
 - Answer
- (2) (Total 5 marks)

(1)

(1)

(1)

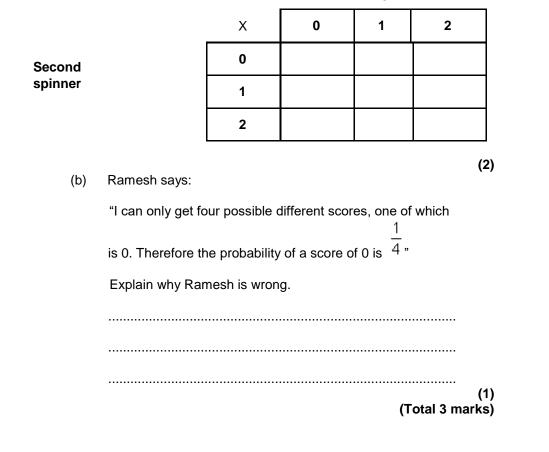
Q8. Ramesh uses two identical, fair 3-sided spinners in a game.



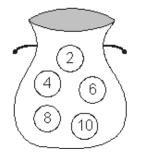
He spins both spinners. His score is the two numbers multiplied together.

Show his possible scores in the table. (a)

First spinner



Q9. A bag contains five discs as shown.



One disc is taken from the bag at random. It is then replaced. Another disc is then taken from the bag at random. The numbers on the two discs are added to make a score.

Complete the table of scores. (a)

+	2	4	6	8	10
2	4	6	8		
4	6	8			
6	8				
8					18
10				18	20

.....

.....

What is the probability that the score is 16? (b)

(1)

(2)

(c) Which is greater: the probability that the score is a square number or the probability that the score is a cube number? You must explain your answer. (Total 5 marks)

Collecting Data and Questionnaires

Q10. Jane conducts a survey of the favourite colours of the students in her class. She records the results.

Male	Red	Female	Yellow
Male	Yellow	Female	Red
Male	Red	Female	Green
Female	Green	Female	Green
Female	Red	Male	Red
Male	Green	Male	Yellow
Male	Green		

Record the results in a two-way table.

(Total 3 marks)

(2)

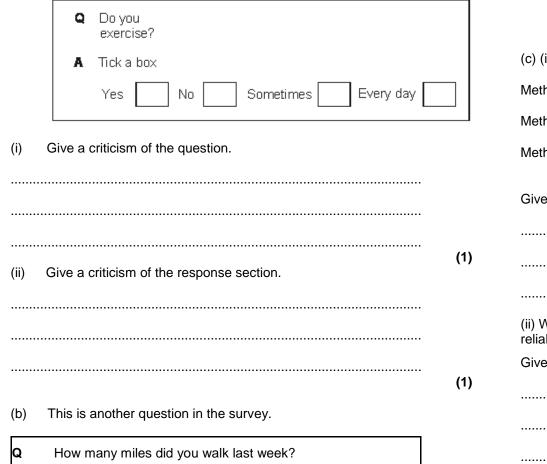
Answer

Q11. A doctor wants to encourage her patients to take more exercise.

The doctor has approximately 500 patients.

She decides to do a survey about what exercise her patients take.

(a) This is a question in the survey.



Give a suitable response section for this question.

(c) (i) The doctor decides to use one of three methods to do the survey.									
	Method 1 Give the survey to the first 50 patients seen in a week								
	Method 2	2 Choose 50 patients at random							
	Method 3	Choose 26 patients, picking one whose surname begins with each letter of the alphabet							
	Give a reason why method 3 is not suitable.								
(ii) Which of the other two methods for doing the survey will give the most reliable results?									
	Give a reaso	on for your choice.							
			(1)						
		<u> </u>							

Scatter Graphs

Q12. Clive works for the local council.

One of his jobs is to check that taxi companies charge reasonable fares.

Each week he checks 10 taxi journeys with local companies.

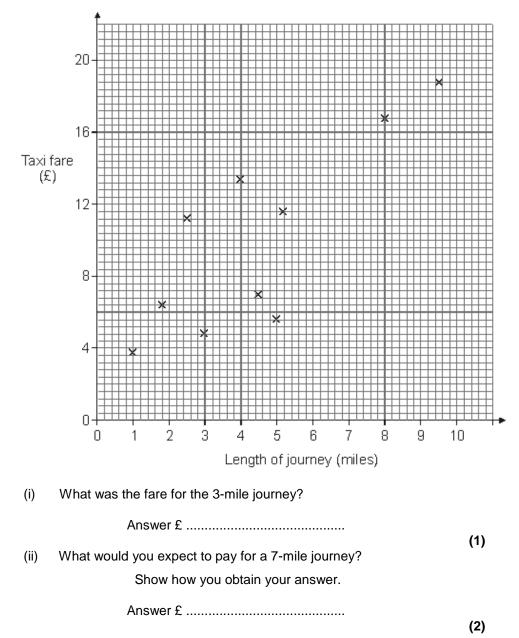
(a) Design a suitable observation sheet for Clive to use to record the fare and distance of each journey.

(b) Clive expects strong positive correlation between the length of the journey and the fare charged.

Explain why he might expect this.

.....

(c) The scatter diagram shows the results for a week in January 2009.

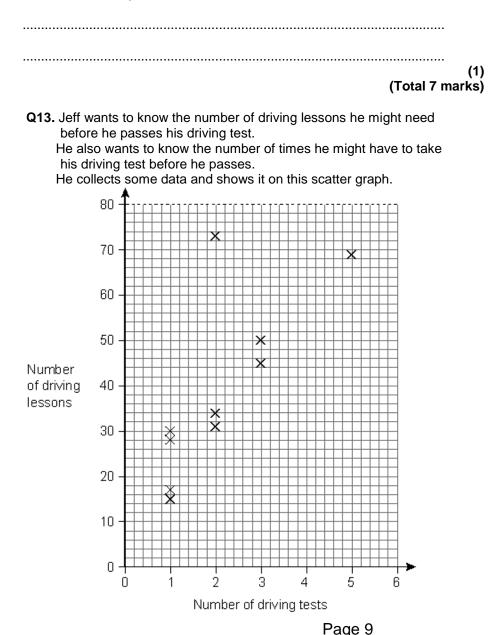


(2)

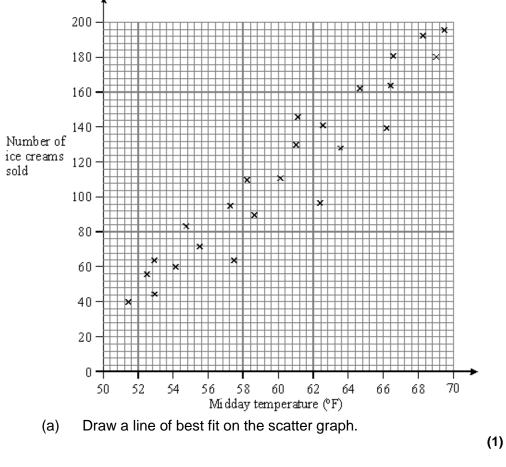
(1)

(d) Does the data support Clive's view about the expected correlation between the length of journey and the fare?

Give a reason for your answer.



(a) Jeff ignores one of the points on the scatter graph. Circle this point and give a reason why it should be ignored. Reason (2) Draw a line of best fit on the scatter graph. (b) (1) Jeff has already failed his driving test three times after a total of (c) 40 driving lessons. Estimate how many more driving lessons Jeff needs if he (i) is to pass his driving test on the fourth attempt. Answer (2) Give a reason why this estimate might be unreliable. (ii) (1) (Total 6 marks)



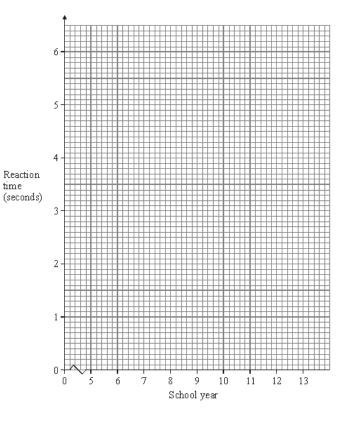
Q14. The scatter graph shows the number of ice creams sold plotted against the midday temperature.

(b) Describe the relationship between the number of ice creams sold and the midday temperature.

 Q15. The table shows the school year and the reaction time of eight people who took part in the same test.

School year	5	7	8	9	10	11	12	13
Reaction time (seconds)	6	5	4.8	4.5	4	4.2	3.5	3

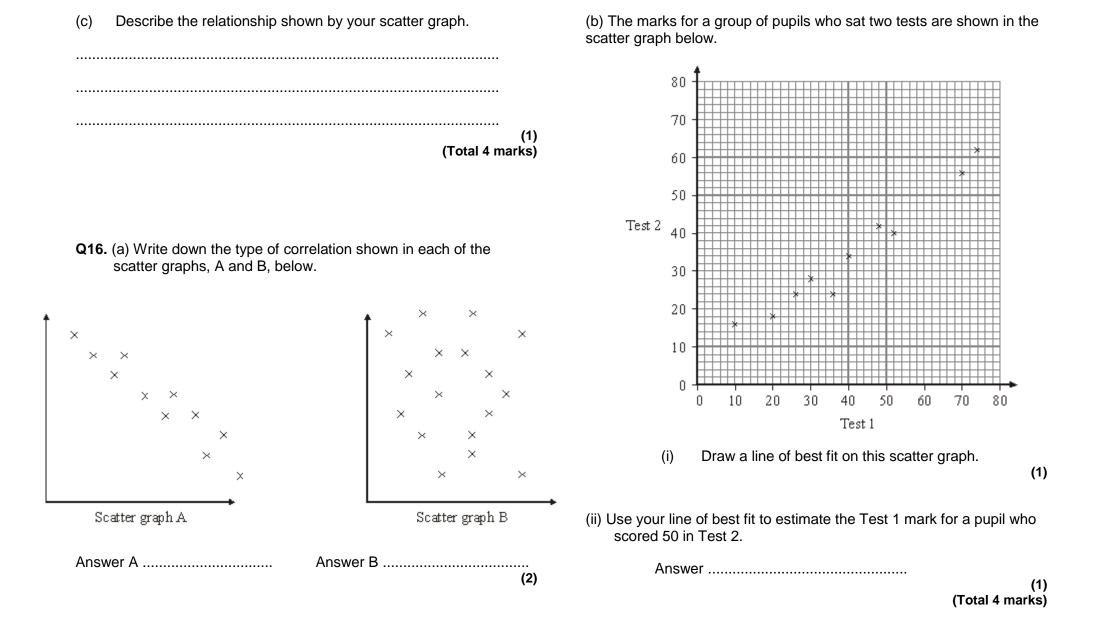
(a) Draw a scatter graph of these data.



(b) Draw a line of best fit on your scatter graph.

(1)

(2)



Averages

Q17. A girls' basketball team plays six matches. The scores are

28 30 25 35 39

(a) What is the median score?

Answer

.....

.....

.....

26

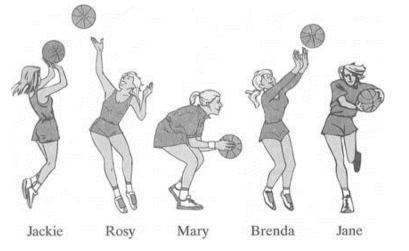
(b) What is the mean score?

Answer

(3)

(2)

(c) These are the members of the team.



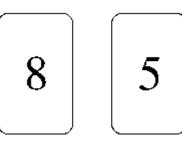
One girl is to be chosen at random to be captain.

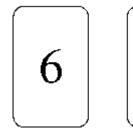
What is the probability that her name begins with J?

Answer

(2) (Total 7 marks)

Q18. Here are four cards.

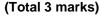




5

James says that the mean of the numbers on the cards is higher than the mode.

Show that James is correct.



(a)	• • • •		ne rang									
	Aı											(1)
(b)	(i)	Write	e down	the m	ode of	f these	e scor	es.				
	A	nswer.						. poin	ts			(1)
(ii)	In the	e next i	match t	the Tiq	gers s	core 2	25 poii	nts.				
Wha	t effec	t does	this ha	ve on	the m	ode?						
Tick	the co	rrect b	ox.									
Dec	rease		No cha	inge		Incre	ease					
										(Tota	al 3 ma	(1) arks)
pers	on hac	before	pass dr e passi ven me	ng the	ir driv	ring te		e num	ber of	lessons	that e	ach
	10	17	15	5	10	12	8	3	19			
(a)	Worl	k out th	ne rang	e of th	iese n	umbe	rs.					

Q19. The number of points scored by the Tigers in the last 10 rugby

(b) Calculate the mean of these numbers.

(3)

(c) The number of driving lessons taken by a sample of women is summarised in the table.

		Women
Range	Э	14
Mear	1	9

Write down **two** comparisons between the number of driving lessons taken by the men and the women.

Comparison 1

 Q21. A company puts this advert in the local paper.

AQA Motor Company

Mechanic needed

Average wage over £400 per week

The following people work for the company.

Job	Wage per week (£)
Apprentice	200
Cleaner	200
Foreman	350
Manager	800
Mechanic	250
Parts Manager	520
Sales Manager	620

(a) What is the mode of these wages?

Answer £

What is the median wage? (b) Answer £ (2) Calculate the mean wage. (C) Answer £ (3) (d) Explain why the advert is misleading. (1) (Total 7 marks)

(1)

Q22.	Jim re ten d		how r	nany te	ext mes	sages	he rec	eives e	each da	ay for		Q23. Jody has a set of five single-digit number cards.	
	3 (a)	0 Worl	1 k out t	4 ne mec	1 lian.	4	6	1	20	0		$\begin{bmatrix} 2 \\ 3 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \end{bmatrix} \begin{bmatrix} 4 \\ 1 \end{bmatrix}$	
												(a) She says the median is greater than the mode. Show that Jody is correct.	
											(2)		(2)
(b)	Work	c out th	ne mea	an.								(b) Here is another set of five cards.	
												Jody is asked to write numbers on the remaining two cards so that the median is the same as the mode.	
		A	nswer								(2)	She says, "If I write down two fives or two sixes or one of each, I cannot fail."	
(c)		h of th plain y			ages b	etter re	preser	nts the	data?			Show that Jody is correct.	
										Total 5 m	(1) arks)		
													(3)

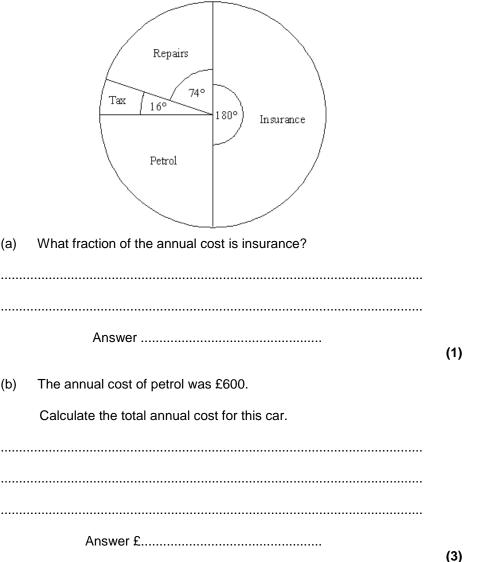
Q24. Every hour a bank records the number of customers waiting to be served.

The results for one Monday are shown.

Time 10 am 1 am 12 pm 1 pm 2 pm | 3 pm | 4 pm Number of customers waiting 7 5 9 15 24 6 4 Repairs At which one of these times were most customers waiting? (a) Tax 16° Answer (1) Petrol Calculate the mean number of customers waiting at these (b) times. (a) Answer (3) (c) On Friday of the same week the mean number of customers waiting at these times was 20. (b) On which day should the bank employ more staff? Explain your answer. (2) (Total 6 marks)

Pie Charts

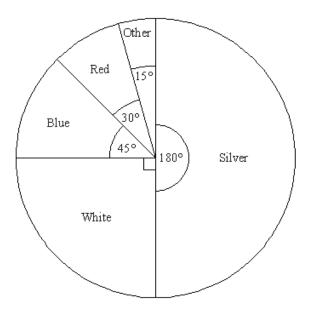
Q25. A young driver has a small car. The pie chart shows the annual costs for the car.



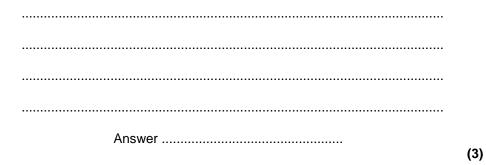
(Total 4 marks)

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Q26. (a) 120 men were asked what colour car they own. The pie chart shows the results.



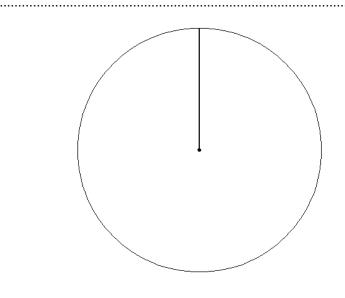
Work out the number of men who own a blue car.



(b) 120 women were also asked what colour car they own. The results are shown in the table.

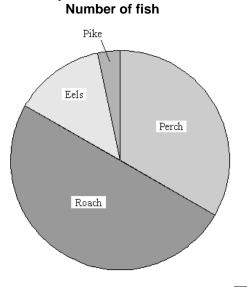
Colour	Number of women
White	42
Blue	35
Silver	25
Red	10
Other	8

Draw and label a pie chart to show this information.



⁽⁴⁾ (Total 7 marks)

Q27. The pie chart shows the number of each type of fish that Frank caught in one day.



- (a) Tick **one** box for each statement below.
- (i) Half the fish caught were roach
- (ii) There were more eels caught than pike.

(iii) The pike weighed more than all of the roach.

(b) Frank caught 30 fish altogether.One-third of the fish caught were perch.How many eels and pike were caught altogether?

Answer

True False Cannot say

(3)

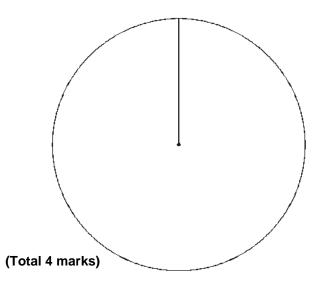
(Total 6 marks)

Q28. The number of complaints made about different parts of the Health Service last year is shown in the table.

Туре	Number of complaints
Hospitals	400
Doctors	200
Dentists	80
Other	120

Draw and label a pie chart to represent these data.

.....



Q29. The table shows the races that 60 primary school pupils entered on their Sports Day. They each entered one race.

Race entered	Number of pupils
Egg and spoon	18
3-legged	20
Sack	12
Obstacle	10

(a) Draw and label a pie chart to represent the information in the table.

.....

.....

.....

(b) Work	out the	e percen	tage of	pupils w	/ho entei	ed the e	egg and	spoon	race.	
		Answ	/er				%			(2)	
(c)	The p	oupils in	the obs	stacle ra	ce took	these tir	nes in s	econds.			
23	36	18	29	44	39	36	54	43	41		
Draw	an or	dered st	tem and	l leaf dia	igram to	show th	is inforn	nation.			
		Key:	I	2 3	s repre	esents 2	3 secon	ds			
	J							(Tot	tal 9 m	(3) arks)	

(4)

Stem & Leaf Diagrams

Q30. A rounders coach records the number of rounders the players in her squad scored in a season.All the players scored at least once.She shows the data in a stem and leaf diagram.

Key 2 7 represents 27 rounders scored								
0	1	1	2	7				
1	2	5	5					
2	3	7						
3	6							
4	0							
5	0	9						
(b) Her				ara thara in tha aguad?	(
(b) Hov	w man	у ріа 	yers	are there in the squad?				
		Ansv	/er		(*			
(c) Wh	at is th	ne me	edian	number of rounders scored?				
		Ansv	ver		('			

(d) Calculate the mean number of rounders scored.



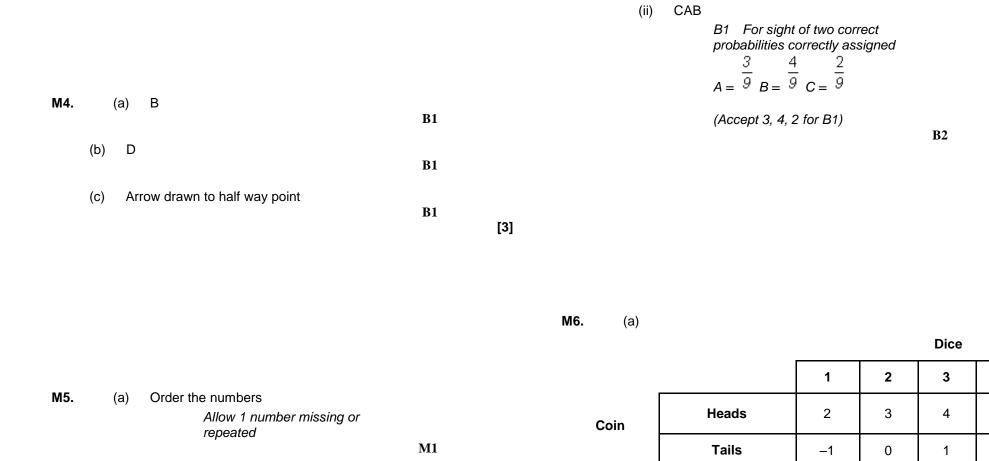
Q31. The stem and leaf diagram shows the ages, in years, of 15 members of a badminton club.

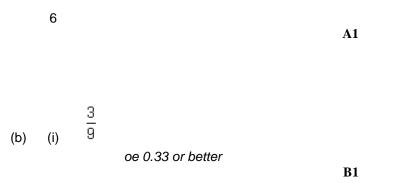
	2 3 4 5 6		Key	1	•			f 27 years
	2	7	8					
	3	0	2	4	8			
	4	1	2	3	3	4	б	
	5	3	б					
	6	2						
1)	(a) Wh	at is the	median a	age of the	e membe	ers?		
1)						ers? yea	rs	
1) 1)		Answer .					rs	

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М1. (b)			B2 B1 B1	[4]	МЗ.	(a) (3), (5), (5), 7, 9, 11 7, 9, 11, 13 9, 11, 13, 1 <u>3</u> <u>20</u>	, 13 , 15	B2
м2 <u>6</u> 100	2. (a) Ē	6 3+69+25				(b)	20	Oe	B1
100	<u>3</u> 50		M1			(c)	P(13) = ³ /20	implies 15 winners in 100 plays	B1
	50		A1					costs) £7.50	B1
(b)) 31							00 × 20 (= £20)	B1
			B1				(Profit) £20	– £7.50 (= £12.50) Award partial marks for stages	B1
(c)	(i) Unlike	ely	B1					shown	
	(ii) Certa	in	B1	[5]					

[7]





(i) $\frac{1}{12}$ ft from a completed table or correct ft may be cancelled eg $(\frac{\delta}{12}) =$

(b)

[5]

4

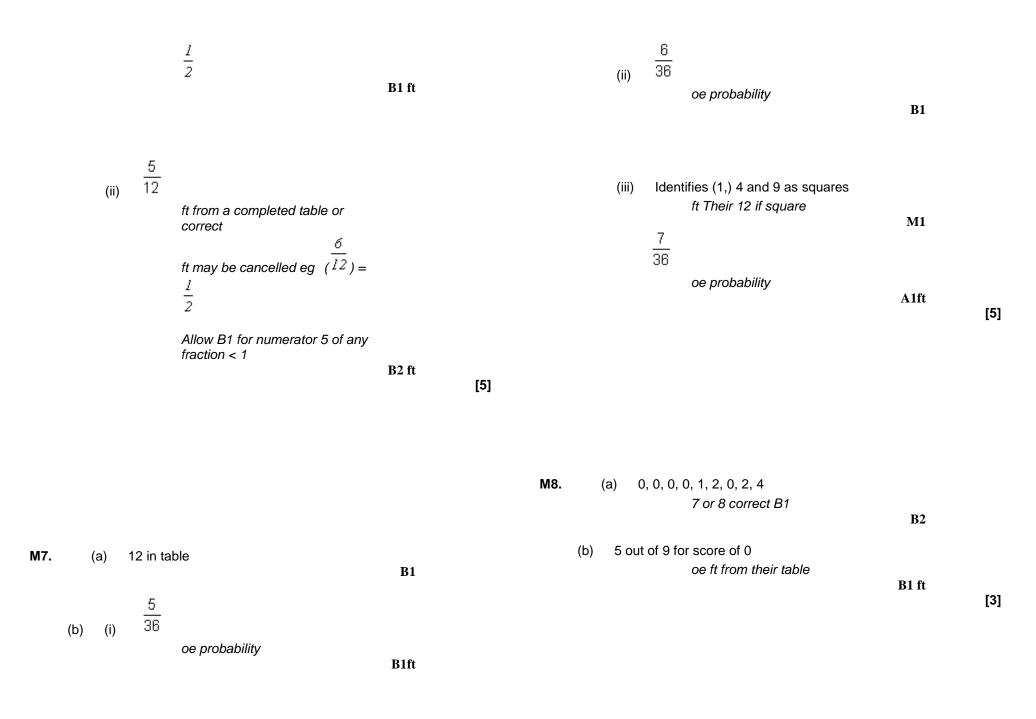
5

2

5

6

3



are cube numbers and chooses square

oe eg, convincingly lists appropriate outcomes or annotates table

B1 Part of the B2 explanation

but one missing

or incorrect value or values correct but does not choose B0 There are 2 square numbers but only 1 cube number

B2ft

[5]

M9. (a) All entries are correct

						0//////////////////////////////////////
+	2	4	6	8	10	correct but does not ch
2	4	6	8	10	12	B0 There are 2 numbers but on
4	6	8	10	12	14	1 cube nun
6	8	10	12	14	16	
8	10	12	14	16	18	
10	12	14	16	18	20	
r				•	4	

B1

M10. R Υ G Their 3 Μ 2 2 3 25 (b) F 3 2 1 B1 Denominator of 25, fraction of Table 3×2 or 2×3 value less than 1 If gender ignored and total 3 number of students used M0 SC1 35 **M1** B2ft Fully correct Accept tally marks;

(c) There are 4 outcomes that are square numbers but only 3 that

Accept tally marks; 4 or 5 correct entries A1; SC2 for

M F					
R Y G R Y G					
3 2 2 2 1 3			(h)	Dependence existing that accurry values from 0 to at lo	oot F
or			(b)	Response section that covers values from 0 to at le with no missing	asi o
M F				values and no overlapping values	B1
R 3 R 2					
Y 2 Y 1			(c)	(i) Too small a sample or other sensible reason	
G 2 G 3 Or				eg, may not have anyone whose surname begins with X or Z	
C/ R Y G					B1
M 3 2 2				(ii) Method 2, all patients have equal chance	B1
R Y G					
F 2 1 3					
4 or 5 correct entries SC1					
	A2	[3]			
		M12.		(a) Sheet with 10 rows or columns and a section t	for
				distance and fare	
				Deduct a mark if not complete	B2
M11. (a) (i) Too vague			(b)	Longer taxi rides always cost more and cost per mi should be about same	ile
Oe				oe	B1
	B1			-	
(ii) Not enough choices or choices overlap					
Oe	B1		(c)	(i) £4.60 - £5.00	

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[5]

			B1				B1
	(ii) Line c	of best fit			(c)	(i)	Their reading from their line of best fit at $x = 4$
		Fares about double distance	M1				ft A line of best fit with a positive gradient (intended straight) M1
	14	ft their line of best fit	A1				Their reading – 40 evaluated correctly A1 ft
(d)	Yes, positive	e correlation Accept: No, correlation is weak positive	B1	[7]		(ii)	Quite a small sample or mention of any other variable which may confound eg, depends on age / instructor / examiner etc Jeff better than ave / worse than ave Allow incorrect or irrelevant statements as long as they are not contradictory
М13.	(a) Circles	s (2, 73) Any clear indication	B1				B1
	This is an o	utlier / extreme value Does not follow pattern oe eg, far more lessons than expected	B1 dep		M14.	(a)	Line crossing between 20 and 40 and within 1 cm of (70,200) <i>Must be ruled, at least 10 cm long</i> B1
(b)	Line of best	fit Must pass between (1, 15) and (1, 25) and (5, 65) and (5, 80)			(b)	As o	one goes up so does the other Positive correlation oe Or hotter it gets the more ice

[6]

	creams sold oe	D 1					B1
		B1	[2]	(b)	(i)	Suitable line	
M15.	(a) All 8 points plotted correctly $\frac{1}{2}$					From x = 20 to x = 70 (20, 10 – 24) to (70, 50 – 64) inclusive	B1
	± ² square Only 6 or 7 points correct Ignore extra points B1				(ii)	About "60" ft line if correct $\pm \frac{1}{2}$ square	
		B2				56 - 66 inclusive if no line	B1 ft
(b)	Suitable straight line of best fit drawn Must reach $x = 5$ and $x = 11$ and pass between (5, 5.5 to 6.5) and (11, 3.5 to 4.2)			M17.	(a)	Arranging in order 25, 26, 28, 30, 35, 39	M1
	Dotted line OK	B1			29		A1
(c)	The older the person the quicker they can do Accept negative correlation	the test		(b)	Att	empt to add all 6 (= 183)	M1
		B1	[4]		Th	eir 183 ÷ 6 If no total shown brackets must be round their added numbers	
M16.	(a) A Negative					<i>ie (</i> 28+ +26) ÷ 6 I	DM1
		B1			30	.5	A1
	B Zero						
	Accept: None or No						

[4]

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(ii) No change **B1** $\frac{2}{5}$ (C) oe; numerator, B1; denominator, B1 (fraction \leq 1) **B2** [7] M20. (a) 11 **B1** Adding at least 6 values (b) M18. Mode = 5**B1** Total of 72-110 \rightarrow M1 **M1** 24 5 "total" ÷ 7 M1 **M1** = 13 Mean = 6 A1 oe valid explanation eg, mean > 5 because all the numbers are ≥ 5 A1 Comparison of spread [3] (c) Strict ft eg Women have a bigger range Men's range is 11 and women's range is 14 B1 ft M19. (a) 60 **B1** Comparison of mean Strict ft (i) 16 (b) eg Men have a bigger mean **B1** Men's mean is 13 and

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[3]

			women's mean is 9							B1
			or men have more lessons							
			(on average)							
				B1 ft						
					[6]					
M21.	corre	ect answer th								
		ept £4.20p an Ilise £4.2 and	d 420p with the £ sign crosse I £420p	d out;		M22.	(a)	001	1 1 3 4 4 6 20 At least first 6 or last 6 in correct	
	(a)	£200							order	M1
	(u)	~200	Allow names, Apprentice and/o	or						M1
			Cleaner				2			
				B1						A1
	(b)	Put data in o	order	741		(F)	Σ.	x÷10		
				M1		(b)				
		£350							Allow 38 $\leq \sum x \leq 42$ if no	
			Foreman						addition seen	
				A1						M1
							4			
							•			A1
	(\mathbf{a})	200 + 200 +	250 .			(c)	Moo	dian - or	mits rogue value	
	(c)	200 + 200 +				(0)	INICC		This togue value	
			Attempt to add the 7 numbers; total underneath column OK						or	
				M1			Mea	an - use	es all values	
		Their 2940	. 7				Wiet			B1
			. /	M1 dep						
				_						
		£420								
				A1						
	(d)	Average is f mechanic	or the whole company not just for	or the						
			Mechanic only gets £250 oe he gets £150 less (than average)	9						

[7]

[5]

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M23. Median = 2 M24. (a) 1 pm (a) **B1** oe eg, 13:00 **B1** Mode = 1**B1** Attempts to sum the values (b) Sight of 70 5,5 gives 5, 5, 5, 5, 6 (b) **M1** Median = mode = 5Attempts to divide Their sum by 7 6,6 gives 5, 5, 6, 6, 6 M1dep Median = mode = 610 5,6 gives 5, 5, 5, 6, 6 A1 Median = mode = 5E2 For 2 correct medians and modes and reordering shown or for all 3 correct medians Friday, because there are more people waiting on a Friday (C) and modes oe B1 Friday, reason attempted but reordering not shown strict follow through from E1 For 1 correct median and their (b) mode B2ft and reordering shown or for 2 correct medians and Alt modes but reordering not shown Cannot tell, one set of data for each day is not enough **E3** oe B1 Cannot tell, reason [5] attempted

B2ft

[6]

$$M25. (a) = \frac{1}{2}$$

$$M25. (b) = \frac{1}{2}$$

$$M25. (c) = \frac{1}{2}$$

$$M26. (c) = \frac{45}{360} \text{ or } 360 + 45(=8)$$

$$160^{\circ} = 60 \text{ men}$$

$$M26. (c) = \frac{45}{360} \text{ or } 380 + 45(=8)$$

$$160^{\circ} = 60 \text{ men}$$

$$M1 = \frac{1}{4}$$

$$M27. (c) = (10) \text{ True}$$

$$M27. (c) = (10) \text{ True}$$

$$M1 = \frac{45}{360} \times 120$$

$$M1 = \frac{1}{120} \text{ men}$$

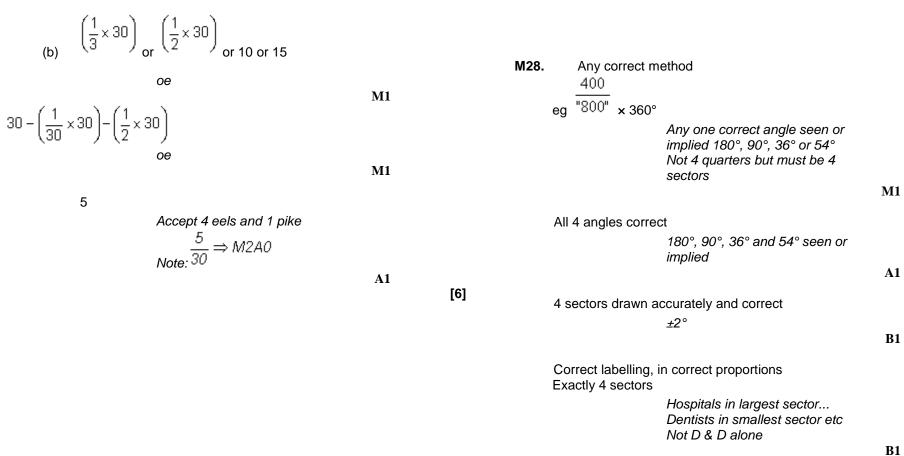
$$M27. (c) = (10) \text{ True}$$

$$M27. (c) = (10) \text$$

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[7]

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[4]

M29. (a) Fully correct pie chart, correctly labelled wit angles correct (108°, 120°, 72° and 60°) (sectors ± 2°)	h all sector	9) (6,6,9) (I,3,4) (4) B1 for 3 or 4 rows correct B1 not ordered				
B3 4 correct sectors drawn with no/wrong labels or 2 correct sectors drawn and			<i>(</i>)		B2	[9]
4 labels in correct order of size	M	30.	(a) 58		B1	
B2 2 correct sectors drawn; with no/wrong labels or 1 correct sector drawn and		(b)	13		B1	
4 labels in correct order of size or		(c)	15		B1	
4 correct angles calculated B1 1 correct sector drawn; no/						
wrong labels or		(d)	$\sum x$ at least 6	6 values 11 + 42 + 50 + 36 + 40 + 109		
1 correct angle calculated or 4 sectors labelled in correct				11 + 42 + 50 + 50 + 40 + 109	M1	
order of size	B4		their 288 ÷ t	heir 13	M1 dep	
(b) 18 ÷ 60 × 100			22.(2)	22.1; 22.15() or 22 with		
oe eg ³ / ₁₀ ×100 or ¹⁰⁸ / ₃₆₀ × 100	M1			working	A1	[6]
30		131.	(a) 42		D 1	[0]
		(b)	35		B1	
(c) Stem (1, 2, 3, 4, 5)		. ,			B1	[2]
(0) (0) $(1, 2, 0, 7, 0)$	B1					