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## Stem Sentences. Spine 3: Fractions

Part-whole relationship
Unit fractions
Non Unit Fractions
Making a whole
Counting in fractional steps
Improper fractions and mixed numbers
Equivalent Fractions
Simplifying Fractions
Comparing Fractions
Adding and subtracting fractions
Multiplying whole numbers and fractions
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Linking fractions, decimals and percentages

Year 3: 3.1
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|  | Part-Whole relationships |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { PD } \\ & \text { Link } \end{aligned}$ | Example of stem sentence | Type of stem sentence | Examples from the NCETM PD Materials |  |  |
| $\begin{gathered} \text { Year 3: } \\ 3.1 \\ 1: 1 \\ 1: 4 \end{gathered}$ | If $\qquad$ is the whole then $\qquad$ is part of the whole. | Structure | If Europe is the whole, then the United Kingdon is part of the whole. |  |  |
| $\begin{aligned} & \hline \text { Year 3: } \\ & 3.1 \\ & 1: 5 \end{aligned}$ | A part is always smaller than the whole. | Generalisation |  |  |  |
| $\begin{aligned} & \text { Year 3: } \\ & 3.1 \\ & 1: 7 \end{aligned}$ | If $\qquad$ is the whole then $\qquad$ is not part of the whole. | Structure | If my face is the whole then my foot is not part of the whole. |  |  |
| $\begin{aligned} & \text { Year 3: } \\ & 3.1 \\ & 2: 2 \\ & \hline \end{aligned}$ | The whole has been divided into $\qquad$ equal / unequal parts. | Structure / <br> language |  |  |  |
| $\begin{aligned} & \text { Year 3: } \\ & 3.1 \\ & 2: 3 \end{aligned}$ | The whole has been divided into $\qquad$ equal parts. | Structure | The whole has been divided into 4 equal parts. |  |  |

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| $\begin{array}{\|l} \hline \text { Year 3: } \\ 3.1 \\ 2: 6 \end{array}$ | The parts are equal, I know this because the number of $\qquad$ in each part is the same. | Structure |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \hline \text { Year 3: } \\ & 3.1 \\ & 2: 6 \end{aligned}$ | The parts are unequal, I know this because the number of $\qquad$ in each part is not the same. | Structure / language |  |  |
| $\begin{aligned} & \text { Year 3: } \\ & 3.1 \\ & 2: 7 \end{aligned}$ | Equal-sized parts do not have to look the same. | Generalisation |  |  |
| $\begin{aligned} & \hline \text { Year 3: } \\ & 3.1 \\ & 3: 2 \end{aligned}$ | Different parts of the samesized whole can be directly compared based on their size. | Generalisation | $000 \cdot 0 \cdot 0$ <br> $00000 \cdot 0$ <br> In the first set of counters, the yel smaller part of the whole then in | w counters make up a e second set. |
| $\begin{aligned} & \hline \text { Year 3: } \\ & 3.1 \\ & 3: 4 \end{aligned}$ | As the while increases in size and the size of the selected part remains the same, each part becomes smaller in relation to the whole. | Generalisation |  |  |
|  | Unit Fractions |  |  |  |
| $\begin{aligned} & \hline \text { Year } 3 \\ & 3: 2 \\ & 2: 1 \end{aligned}$ | A unit fraction is any fraction where the numerator is one. | Generalisation | Numerator (1 for a unit fraction) <br> $1 \leftarrow$ One of the parts of the whole <br> $\mathbf{2} \leftarrow$ Denominator <br> The number of equal parts in the whole |  |
| $\begin{aligned} & \text { Year 3: } \\ & 3.2 \\ & 2: 1 \end{aligned}$ | The whole has been divided into $\qquad$ equal parts $\qquad$ of the parts has been shaded. | Structure / language | The whole has been divided into the parts has been shaded. | hree equal parts. One pf |
| $\begin{aligned} & \hline \text { Year 3: } \\ & 3.2 \\ & 2: 2 \end{aligned}$ |  | Language / structure | Say | Write |
|  |  |  | 'The whole has been divided...' | The division bar:- |
|  |  |  | '...into 3 equal parts.' | The denominator: 3 |
|  |  |  | 'One of the parts has been shaded.' | The numerator: 1 |

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| Year 3: <br> 3.2 <br> 2:2 | The denominator is $\qquad$ because the whole is divided into $\qquad$ equal parts. <br> The numerator is one because one part is shaded. | Structure | The denominaor is 4 because the whole is divided into 4 equal parts. <br> The numerator is 1 because one part is shaded. |
| :---: | :---: | :---: | :---: |
| $\begin{aligned} & \hline \text { Year 3: } \\ & 3.2 \\ & 3: 1 \end{aligned}$ | The whole has been divided into $\qquad$ equal parts. <br> Each part is one $\qquad$ of the whole. $\qquad$ of the whole ribbon has been cut off. | Structure |  |
| $\begin{aligned} & \hline \text { Year 3: } \\ & 3.2 \\ & 3: 2 \end{aligned}$ | The whole has been divided into $\qquad$ equal parts. One of these parts is highlighted. This part is one $\qquad$ of the whole line. | Structure | The whole has been divided into 5 equal parts. One of these parts is highlighted. This part is one fifth of the whole line. |
| $\begin{aligned} & \text { Year 3: } \\ & 3.2 \\ & 3: 6 \end{aligned}$ | The whole has been divided into $\qquad$ equal parts. One of these parts in one $\qquad$ of the whole. | Structure | Dividing 12 counters into equal groups: |
| $\begin{aligned} & \text { Year 3: } \\ & 3.2 \\ & 5: 1 \end{aligned}$ | When the whole is the same, the greater the number of equal parts, the smaller each equal part is. <br> When the whole is the same, the smaller the number of equal parts, the bigger each equal part is. | Generalisation |  |
| Year 3: <br> 3.2 <br> 5:1 | When comparing unit fractions, the greater the denominator, the smaller the fraction. | Generalisation | Ordering the fractions: |

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| Year 3: <br> 3.2 <br> 5:4 | When we compare fractions, the whole has to be the same. | Generalisation | Emma looks at these two diagrams. Shesays that they prove that $\frac{1}{4}>\frac{1}{2}$. Do you agree or disagree?' <br> - 'Disagree: to compare fractions, the wholes must the same' |
| :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { Year 3: } \\ & 3.2 \\ & 6: 4 \end{aligned}$ | If one $\qquad$ is a part, then the whole is $\qquad$ times as much. Take $\qquad$ parts and put them together to make a whole. | Structure | First: If one half is a part, then the whole istwo times as much. Take two parts and put them together to make one whole.' <br> Second: If one-third is a part, then the whole is three times as much. Take three parts and put them together to make one whole.' |
|  | Non- Unit Fractions |  |  |
| $\begin{aligned} & \hline \text { Year 3: } \\ & 3.3 \\ & 1: 4 \end{aligned}$ | I have $\qquad$ one tenths. I have $\qquad$ tenths. | Structure / language | $\frac{1}{10}$ $\frac{1}{10}$ $\frac{1}{10}$ $\frac{1}{10}$ $\frac{1}{10}$ $\frac{1}{10}$ $\frac{1}{10}$ $\frac{1}{10}$ $\frac{1}{10}$ $\frac{1}{10}$ <br> $\frac{1}{10}$         $\frac{1}{10}$$\frac{1}{10}$ <br> - 'I have three one-tenths. I have three-tenths.' |
| $\begin{aligned} & \text { Year 3: } \\ & 3.3 \\ & 1.6 \end{aligned}$ | There are $\qquad$ equal parts in the whole. There are $\qquad$ parts shaded. $\qquad$ is shaded. | Structure / language | 'There are five equal parts in the whole.' <br> - There are fourparts shaded.' <br> - Four-fifths is shaded.' |
| $\begin{aligned} & \hline \text { Year 3: } \\ & 3.3 \\ & 2: 1 \end{aligned}$ | The whole has been divided into $\qquad$ equal parts. $\qquad$ of the parts are shaded. That is $\qquad$ of the whole. | Structure / language | - 'The whole has been divided into six equal parts.' <br> - 'Five of theparts areshaded.' <br> - 'That is five-sixths of the whole.' |
| $\begin{aligned} & \text { Year 3: } \\ & 3.3 \\ & 2: 5 \end{aligned}$ | The whole has been divided into $\qquad$ equal parts. $\qquad$ of the parts have been shaded; that is $\qquad$ of the whole. | Structure / language |  <br> The whole has been divided into 7 equal parts. 5 of the parts have been shaded; that is $5 / 7$ of the whole. |

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Counting in fractional steps

| $\begin{aligned} & \hline \text { Year 4: } \\ & 3.5 \\ & 2: 3 \end{aligned}$ | The line is divided into $\qquad$ equal parts. This allows us to count in $\qquad$ . | Structure |  |
| :---: | :---: | :---: | :---: |
| $\begin{aligned} & \hline \text { Year 4: } \\ & 3.5 \\ & 2: 4 \end{aligned}$ | The interval is divided into $\qquad$ equal parts. This allows us to count in $\qquad$ - | Structure | 'Each interval on the line is divided intofour equal parts. This allows us to count inquarters' |

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| $\begin{aligned} & \hline \text { Year 5: } \\ & 3.7 \\ & 3: 8 \end{aligned}$ | is not in its simplest form because $\qquad$ is a common factor of $\qquad$ and $\qquad$ <br> is in its simplest form because one is the only common factor of $\qquad$ and _. $\qquad$ | Language / structure. | 'Sort the following numbers according to whether they are expressed in their simplest form or not.' $\begin{array}{lllllllllll} \frac{3}{15} & \frac{2}{5} & \frac{4}{20} & & \frac{25}{36} & & \frac{1}{6} & & \frac{7}{21} & \frac{18}{30} & \frac{9}{17} \\ & & \frac{5}{15} & & \frac{11}{20} & & \frac{23}{30} & & & \end{array}$ <br> 4/20 is not in its simplest form because four is a common factor of 4 and 20 $23 / 50$ is in its simplest form because one is the only common factor of 23 and 30 . |
| :---: | :---: | :---: | :---: |
|  | Comparing Fractions |  |  |
| $\begin{aligned} & \text { Year 3: } \\ & 3.3 \\ & 7: 2 \end{aligned}$ | is $\qquad$ lot of 1 ' $\square$ $\square$ is $\qquad$ lots of $\square$ $\stackrel{1}{\square}$ $\square$ <br> 'I know that $\qquad$ is less than ...' $\qquad$ | Language / structure | $\frac{1}{4}<\frac{3}{4}$ <br> $1 / 4$ is 1 lots of $1 / 4$ <br> $3 / 4$ is 3 lots fo $1 / 4$ <br> I know that 1 is less than 3 so $1 / 4$ is less than $3 / 4$. |
| $\begin{aligned} & \hline \text { Year 3: } \\ & 3.3 \\ & 7: 5 \\ & 3.5 \\ & 3: 3 \end{aligned}$ | When we compare fractions with the same denominator, the greater the numerator, the greater the fraction. | Generalisation | $\frac{3}{8}<\frac{5}{8}$ <br> $\begin{array}{cc}\frac{18}{24} & \frac{23}{24} \\ \downarrow & \downarrow \\ \text { 18 lots of } \frac{1}{24} & 23 \text { lots of } \frac{1}{24}\end{array}$ $\frac{18}{24}<\frac{23}{24}$ |
| $\begin{aligned} & \hline \text { Year 3: } \\ & 3.3 \\ & 8: 1 \\ & 8: 4 \end{aligned}$ | When comparing unit fractions, the greater the denominator the smaller the fraction. | Generalisation |  |
| $\begin{aligned} & \hline \text { Year 3: } \\ & 3.3 \\ & 8: 12 \end{aligned}$ | When we compare fractions with the same numerator, the greater the denominator, the smaller the fraction. | Generalisation |  |
| $\begin{aligned} & \hline \text { Year 5: } \\ & 3.8 \\ & 5: 1 \end{aligned}$ | To compare fractions with different numerators and denominator convert to common denominators. | Generalisation | $\begin{array}{ccc} \frac{1}{3} & \text { ( }) & \frac{3}{4} \\ \downarrow & & \downarrow \\ \frac{4}{12} & \text { ( } & \frac{9}{12} \end{array}$ |

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|  | Adding and subtracting Fractions |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { Year 3: } \\ & 3.3 \\ & 5: 2 \end{aligned}$ | $\square$ <br> is $\qquad$ lot of $\square$ 1 | Language / structure | $\frac{1}{5}$ $\frac{1}{5}$ $\frac{1}{5}$ $\frac{1}{5}$$\begin{aligned} & \frac{1}{5}+\frac{1}{5}+\frac{1}{5}=\frac{3}{5} \\ & \frac{3}{5}=\frac{1}{5}+\frac{1}{5}+\frac{1}{5} \end{aligned}$ <br> $3 / 5$ is 3 lots of $1 / 5$. | $\frac{1}{5}$ |
| $\begin{aligned} & \text { Year 3: } \\ & 3.4 \\ & 1: 7 \end{aligned}$ | $\qquad$ tenths and $\qquad$ more tenths make $\qquad$ tenths. | Structure | 6 tenths and 2 more tenths make 8 |  |
| $\begin{array}{\|l} \text { Year 3: } \\ 3.4 \\ 1: 9 \end{array}$ |  | Structure | , $\frac{6}{10}$ is six lots of $\frac{1}{10}$.' <br> , $\frac{2}{10}$ is two lots of $\frac{1}{10}$. <br> 'I know that $6+2=8$.' <br> '...so, I know that $\frac{6}{10}+\frac{2}{10}=\frac{8}{10}$. |  |
| $\begin{array}{\|l} \hline \text { Year 3: } \\ 3.4 \\ 1: 12 \end{array}$ | When adding fractions with the same denominators, just add the numerators. | Generalisation |  |  |
| $\begin{aligned} & \text { Year 3: } \\ & 3.4 \\ & 2: 3 \end{aligned}$ | $\qquad$ /10 is $\qquad$ lots of $1 / 10$ $\qquad$ /10 is $\qquad$ lots of $1 / 10$ <br> I know that $\qquad$ $=$ $\qquad$ So I know that $\qquad$ /10 $\qquad$ $=\ldots / 10$ | Structure | Method 3-verbal reasoning: <br> - $\frac{8}{10}$ is eightlots of $\frac{1}{10}$. <br> - ' $\frac{2}{10}$ is two lots of $\frac{1}{10}$.' <br> - I know that $8-2=6$.' <br> '...so, Iknow that $\frac{8}{10}-\frac{2}{10}=\frac{6}{10}$.' |  |
| $\begin{aligned} & \hline \text { Year 3: } \\ & 3.4 \\ & 2: 5 \end{aligned}$ | When subtracting fractions with the same denominators, just subtract the numerators. | Generalisation | $\begin{aligned} & \frac{8}{9}-\frac{3}{9}=\frac{5}{9} \\ & \frac{8}{10}-\frac{2}{10}=\frac{6}{10} \end{aligned}$ |  |
| $\begin{aligned} & \text { Year 4: } \\ & 3.4 \\ & 4: 3 \end{aligned}$ | To subtract from one whole, first convert the whole to a fraction where the denominator and numerator are the same. | Generalisation | 'A watermelon is cut into 8 equal pieces.' <br> ' $\frac{6}{8}$ of the watermelon is eaten' <br> What fraction of the watermelon is left?' | $\begin{aligned} & -\frac{6}{8}=\frac{2}{8} \\ & -\frac{6}{8}=\frac{2}{8} \end{aligned}$ |

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| $\begin{array}{\|l} \hline \text { Year 4: } \\ 3.5 \\ 4: 2 \end{array}$ | The parts are $\qquad$ and $\qquad$ The total or whole is . $\qquad$ | Language / structure. | 'The parts are $\frac{2}{5}$ and $1 \frac{1}{5}$. The total, or whole, is $1 \frac{3}{5}$.' |
| :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { Year 5: } \\ & 3.8 \\ & 1: 6 \end{aligned}$ | Related fractions have denominators where one denominator is a multiple of the other. | Generalisation | $\frac{1}{3} \text { and } \frac{1}{9}$ <br> We can change $\frac{1}{3}$ to $\frac{3}{9}$.' |
| $\begin{aligned} & \text { Year 5: } \\ & 3.8 \\ & 1: 8 \end{aligned}$ | and $\square$ are realted fractions because the denominator $\qquad$ is a multiple of the other denominator $\qquad$ | Structure / language | $\frac{1}{16}$ and $\frac{1}{4}$ are related fractions because the denominator, "16", is a multiple of the other denominator, "4"." |
| Year 5: <br> 3.8 | Fractions must have the same denominator before they can be added or subtracted. | Generalisation |  |
| Year 5: $3.8$ | When fractions have the same denominator, we call this a common denominator. | Generalisation |  |
| Year 5: $3.8$ | To add or subtract fractions with different denominators, first convert to fractions with a common denominator. | Generalisation | $\begin{aligned} \frac{2 x}{36}+\frac{1}{6} & =\frac{2}{6}+\frac{1}{6} \\ & =\frac{2+1}{6}=\frac{3^{1}}{52}=\frac{1}{2} \end{aligned}$ <br> To solve $1 / 3+1 / 6$, convert $1 / 3$ to $2 / 6$ by scaling 1 and 3 up by two then add $2 / 6$ and $1 / 6$ together. |
| Year 5: $3.8$ | To find a common denominator, identify the lowest common multiple of the denominators then create an equivalent fraction. | Generalisation | Multiples of 3: 3, 6, 9, 12, 15 <br> Multiples of 5: $5,10,15$ <br> The lowest common multiple of 3 and 5 is 15 . |
| Year 5: $3.8$ | We can find a common denominator for two nonrelated fractions by multiplying their denominators. | Generalisation | If you multiply the two denominators 3 and 5 you will get the common denominator product of 15 . |

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| Year 6: <br> 3.10 <br> $6: 2$ | To find 10\% of a number, <br> divide it by ten. | Generalisation | 'Rishi has completed $10 \%$ of the same bike ride. How far <br> hashe cycled?' |
| :--- | :--- | :--- | :--- |
|  |  |  |  |

