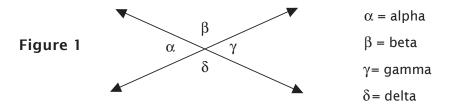
LESSON 6

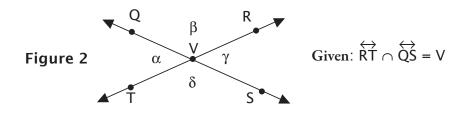
Supplementary and Complementary Angles

Greek Letters

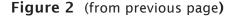


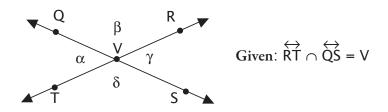
Adjacent Angles - Angles that share a common side and have the same origin are called *adjacent angles*. They are side by side. In figure 1, α is adjacent to both β and δ . It is not adjacent to γ . In figure 1, there are four pairs of adjacent angles: α and β , β and γ , γ and δ , δ and α .

In figure 2, we added points so we can name the rays that form the angles. The common side shared by adjacent angles α and β is \overrightarrow{VQ} .



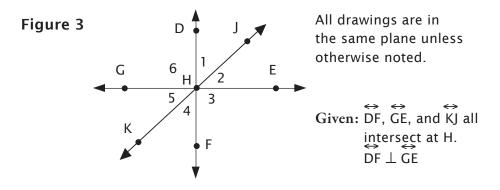
Vertical Angles - Notice that $\angle \gamma$ is opposite $\angle \alpha$. Angles that share a common origin and are opposite each other are called vertical angles. They have the same measure and are congruent. $\angle \beta$ and $\angle \delta$ are also vertical angles.





If $m \angle \beta$ is 115°, then $m \angle \delta$ is also 115°. If this is true, then do we have enough information to find $m \angle \alpha$? We know from the information given in figure 2 that \overleftrightarrow{RT} and \overleftrightarrow{QS} are lines. Therefore, $\angle RVT$ is a straight angle and has a measure of 180°. If $\angle RVQ (\angle \beta)$ is 115°, then $\angle QVT (\angle \alpha)$ must be 180° - 115°, or 65°. Since $\angle RVS (\angle \gamma)$ is a vertical angle to $\angle QVT$, then it is also 65°.

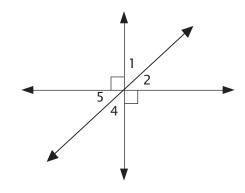
Supplementary Angles - Two angles such as $\angle \alpha$ and $\angle \beta$ in figure 2, whose measures add up to 180°, or that make a straight angle (straight line), are said to be supplementary. In figure 2, the angles were adjacent to each other, but they don't have to be adjacent to be classified as supplementary angles.



Complementary Angles - We can observe many relationships in figure 3. $\angle 1$ is adjacent to both $\angle 6$ and $\angle 2$. Angle 3 and $\angle 6$ are vertical angles, as are $\angle 1$ and $\angle 4$. Angle 6 and $\angle 3$ are also right angles since $\overrightarrow{DF} \perp \overrightarrow{GE}$. The new concept here is the relationship between $\angle DHE$ and $\angle GHF$. Both of these are right angles because the lines are perpendicular; therefore their measures are each 90°. Then $m\angle 1 + m\angle 2 = 90^\circ$, and $m\angle 4 + m\angle 5 = 90^\circ$. Two angles whose measures add up to 90° are called complementary angles. Notice that from what we know about vertical angles, $\angle 1$ and $\angle 5$ are also complementary. Let's use some real measures to verify our conclusions.

GEOMETRY

Figure 4 (a simplified figure 3)



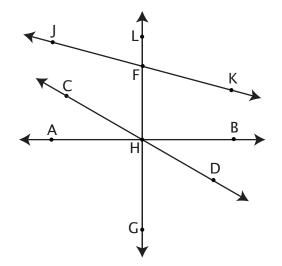
In figure 4, let's assume that $m \angle 1 = 47^\circ$. Then $m \angle 2$ must be 43° , since $m \angle 1$ and $m \angle 2$ add up to 90°. If $m \angle 1 = 47^\circ$, then $m \angle 4$ must also be 47° , since $\angle 1$ and $\angle 4$ are vertical angles. Also, $m \angle 5$ must be 43° . So $\angle 1$ and $\angle 5$ are complementary, as are $\angle 2$ and $\angle 4$. Remember that supplementary and complementary angles do not have to be adjacent to qualify.

It helps me to not get supplementary and complementary angles mixed up if I think of the s in straight and the s in supplementary. The c in complementary may be like the c in corner.

LESSON PRACTICE

Use the drawing to fill in the blanks.

- 1. $\angle AHC$ is adjacent to $\angle _$ and $\angle _$.
- 2. \angle BHD is adjacent to \angle and \angle .
- 3. \angle FHB and \angle ______ are vertical angles.
- 4. \angle FHC and \angle _____ are vertical angles.
- 5. \angle LFJ and \angle _____ are supplementary angles.
- ∠FHC and ∠_____ are complementary angles.
- 7. \angle JFH and \angle _____ are supplementary angles.
- 8. \angle BHD and \angle _____ are complementary angles.



Given: \overrightarrow{AB} , \overrightarrow{CD} , \overrightarrow{LG} , and \overrightarrow{JK} are straight lines. m \angle FHB = 90°.

The drawing is a sketch and not necessarily to scale. Don't make any assumptions about the lines and angles other than what is actually given.

9. If $m \angle CHA = 40^\circ$, then $m \angle BHD =$ _____.

LESSON PRACTICE 6A

Use the drawing from the previous page to fill in the blanks.

10. If $m \angle JFL = 65^\circ$, then $m \angle KFH =$ _____.

11. If $m \angle FHB = 90^\circ$, then $m \angle FHA =$ _____.

12. If $m \angle CHA = 40^\circ$, then $m \angle FHC =$ _____.

13. If $m \angle LFJ = 65^\circ$, then $m \angle LFK =$ _____.

14. If $m \angle FHB = 90^\circ$, then $m \angle AHG =$ _____.

Use the letters to match each term to the best answer.

15. β ____ a. share a common ray

16. adjacent angles ____ b. alpha

17. supplementary angles _____ c. always have the same measure

18. α ____ d. add up to 90°

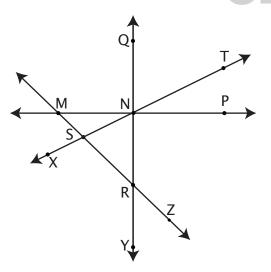
19. complementary angles _____e. add up to 180°

20. vertical angles ____ f. beta

LESSON PRACTICE

Use the drawing to fill in the blanks.

- 1. \angle MNS is adjacent to \angle ______. and \angle ______.
- 2. \angle QNT is adjacent to \angle _____and \angle _____.
- ∠SRN and ∠_____ are vertical angles.
- ∠MNS and ∠_____ are vertical angles.
- 5. \angle QNP and \angle _____ are supplementary angles.
- 6. \angle QNT and \angle _____ are complementary angles.
- 7. \angle NRZ and \angle _____ are supplementary angles.
- 8. \angle MNS and \angle _____ are complementary angles.



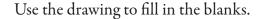
Given: All lines that appear to be straight lines are straight lines. $m \angle QNP = 90^{\circ}$.

The drawing is a sketch and not necessarily to scale. Do not make any assumptions about the lines and angles other than what is actually given. Use the drawing from the previous page to fill in the blanks.

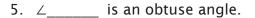
9. If $m \angle MNS = 35^\circ$, then $m \angle SNR =$ 10. If $m \angle MNS = 35^\circ$, then $m \angle TNP =$ _____. 11. If $m \angle QNP = 90^\circ$, then $m \angle PNR =$. 12. If $m \angle MSN = 95^\circ$, then $m \angle NSR =$ _____. 13. If $m \angle SRN = 40^\circ$, then $m \angle YRZ =$. 14. If $m \angle XNY = 55^\circ$, then $m \angle QNT =$. Fill in the blanks with the correct terms. 15. The name of the Greek letter α is _____. 16. Two angles whose measures add up to 90° are called . 17. Two angles whose measures add up to 180° are called ______. 18. The name of the Greek letter γ is 19. Intersecting lines form two pairs of ______ angles. 20. The name of the Greek letter δ is _____.

SYSTEMATIC REVIEW

60



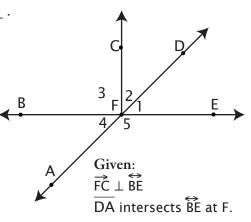
- 1. $\angle 1$ is adjacent to $\angle _$ and $\angle _$.
- 2. $\angle 1$ and \angle are vertical angles.
- 3. $\angle AFE$ and $\angle _$ are vertical angles.
- 4. \angle is a straight angle.



6. $\angle 2$ and \angle are complementary angles.

7. If $m \angle 2 = 50^{\circ}$, then $m \angle 1 =$ _____. Why?

- 8. If $m \angle 2 = 50^{\circ}$, then $m \angle 4 =$ ____. Why?
- 9. $\angle 5$ and \angle are supplementary angles.
- 10. If $m \angle 4 = 40^{\circ}$, then $m \angle 5 =$ _____. Why?
- 11. Name two acute angles.
- 12. Name two right angles.



From now on, we will assume lines that look straight to be straight lines. Do not make any assumptions about the size of the angles.

SYSTEMATIC REVIEW 6C

Follow the directions.

13. Draw a line segment 1½ inches long. Then draw its perpendicular bisector using compass and straightedge.

14. Draw a 52° angle and bisect it.

Fill in the blanks with the correct terms.

- 15. Two lines forming a right angle are said to be ______ to each other.
- 16. A right angle has a measure of _____°.
- 17. A straight angle has a measure of _____º.
- 18. The measures of two complementary angles add up to_____°.
- 19. The measures of two supplementary angles add up to _____º.
- 20. The intersection of two sets with no elements in common is the ______ set.

SYSTEMATIC REVIEW

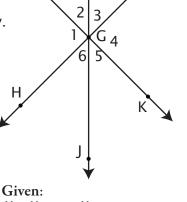
Use the drawing to tell if each statement is true or false.

- 1. $\angle 2$ and $\angle 5$ are vertical angles.
- 2. If $\overrightarrow{FH} \perp \overrightarrow{DK}$, then $\angle 2$ and $\angle 3$ are supplementary.
- 3. $\angle 3$ and $\angle 4$ are adjacent angles.
- 4. \angle FGK is known to be a right angle.
- 5. \vec{GJ} is the common side for $\angle JGK$ and $\angle KGF$.
- 6. $\angle 2$, $\angle 3$, and $\angle 5$ appear to be acute.

Use the drawing to fill in the blanks.

- 7. If $m \angle 3 = 39^{\circ}$, then $m \angle 6 =$ ____. Why?
- 8. If $\overrightarrow{FH} \perp \overrightarrow{DK}$ and $m \angle 3 = 39^\circ$, then $m \angle 2 =$ ____. Why?
- 9. If $\overrightarrow{FH} \perp \overrightarrow{DK}$, then m $\angle 1$ and m $\angle 4$ are each _____. Why?
- 10. If $m \ge 1$ is 90°, then it is a(n) _____ angle.
- 11. If the measures of $\angle 4$ and $\angle 1$ add up to 180°, they are called ______ angles.

12. $m \perp 1 + m \perp 2 + m \perp 3 + m \perp 4 + m \perp 5 + m \perp 6 = _______{\circ}$.



F

D

 $\vec{DK}, \vec{EJ}, and \vec{FH}$ intersect at G.

Lines that look straight are straight. Do not make any other assumptions.

SYSTEMATIC REVIEW 6D

Use the letters to match each description to the correct term.

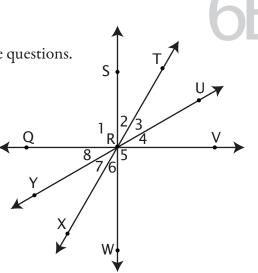
13.	Greek letter beta	a.	α
14.	less than 90°	b.	complementary
15.	measures add up to 90°	C.	δ
16.	Greek letter alpha	d.	obtuse
17.	Greek letter gamma	e.	acute
18.	between 90° and 180°	f.	β
19.	measures add up to 180°	g.	γ

20. Greek letter delta ______ h. supplementary

SYSTEMATIC REVIEW

Use the drawing to fill in the blanks or answer the questions.

- 1. Name a line containing \vec{RV} .
- 2. Name a line segment contained in RT.
- If all eight angles were congruent, rather than as given, what would the measure of each be?
- 4. Since $m \angle 1$ is 90°, what is $m \angle 2 + m \angle 3 + m \angle 4$?
- 5. $\angle 4 + \angle 5$ is a(n) _____ angle.
- 6. Are $\angle 1$ and $\angle 5$ supplementary?
- 7. Are $\angle 1$ and $\angle 5$ complementary?
- 8. Are $\angle 1$ and $\angle 5$ vertical angles?
- 9. If $\angle 2 \cong \angle 3 \cong \angle 4$, then $m \angle 8 = ______{\circ}$.
- 10. ∠6 ≅ ∠ ____.
- 11. $\angle 2$ and $\angle 3$ are ______ angles (size).
- 12. If $m \angle 2 = 25^{\circ}$, and $m \angle 4 = 35^{\circ}$, then $m \angle 3 =$ _____.
- 13. If $m \angle 2 = 25^\circ$, and $m \angle 4 = 35^\circ$, then $m \angle YRX =$ _____.
- 14. Which ray is the common side for \angle SRQ and \angle QRX?



Given: $\overrightarrow{SW} \perp \overrightarrow{QV}$ All four straight lines intersect at R.

Remember the drawing is a sketch.

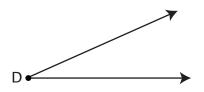
Use the measurements given in the questions, even if the drawing appears to be different.

SYSTEMATIC REVIEW 6E

15. Draw the perpendicular bisector of the given line segment.

A•-----• B

16. Draw a ray that bisects the given angle.



€ Sharpen your algebra skills!

Be very careful when squaring negative numbers.

EXAMPLE 1 $(-5)^2 = (-5)(-5) = +25$

EXAMPLE 2 $-(8)^2 = -(8)(8) = -64$

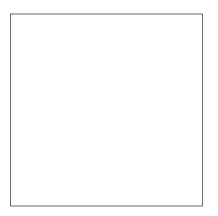
EXAMPLE 3 $-6^2 = -(6)(6) = -36$

- 17. $(-7)^2 =$ 18. $-(15)^2 =$
- 19. $-12^2 = 20. -(9)^2 =$

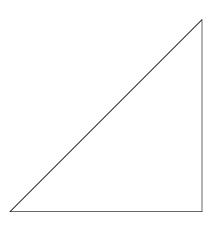


Here are some more figures you may use to practice your bisection skills.

1. Draw the perpendicular bisectors of each line inside the square.



- 2. Using dotted lines or a different colored pencil, bisect each angle in the original square.
- 3. Draw the perpendicular bisectors of each side of the triangle. You have marked off two line segments on each side of the triangle. Now construct a perpendicular bisector for each of those line segments. What kinds of shapes do you see inside the large triangle?



4. If you wish, draw other shapes and construct bisectors as you did above. Try parallelograms, trapezoids, octagons, and other kinds of triangles for interesting results.

Read and follow the directions.

5. Lindsay's base pay is X dollars an hour. For every hour of overtime she works, she gets her base pay plus .5X. Last week she worked six hours of overtime. Let P be her total overtime pay for the week, and write an equation to find P.

6. Lindsay's base pay is \$8 an hour. Use the equation you wrote in #9 to find her total overtime pay for the week.

Circle your answer.

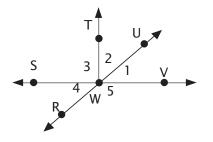
- 1. Two angles whose measures add up to 180° are called:
 - A. straight
 - B. complementary
 - C. acute
 - D. obtuse
 - E. supplementary
- 2. Vertical angles are:
 - A. supplementary
 - B. complementary
 - C. congruent
 - D. adjacent
 - E. obtuse

3. $m \angle XYZ = 35^{\circ}$. What is the measure of its complement?

- A. 145°
- B. 55°
- C. 35°
- D. 65°
- E. 125°
- 4. $m \angle GEF = 40^{\circ}$. What is the measure of its supplement?
 - A. 60°
 - B. 50°
 - C. 140°
 - D. 320°
 - E. 40°

- 5. Angle A is 20° and angle B is 70°. What is their relationship?
 - A. supplementary
 - B. vertical
 - C. reflexive
 - D. coplanar
 - E. complementary

Use this diagram for #6-10.



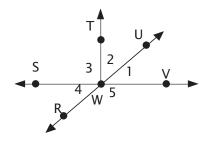
Given: $\overrightarrow{WT} \perp \overrightarrow{SV}$; $\overrightarrow{RU} \cap \overrightarrow{SV}$ at W.

6. $\angle 1$ is adjacent to:

- A. ∠1
- B. $\angle 2$ and $\angle 5$
- C. ∠3
- D. ∠4
- E. ∠2
- 7. The sum of $m \angle 1$ and $m \angle 2$ is:
 - A. 90°
 - B. 180°
 - C. 45°
 - D. 360°
 - E. can't tell from information given

TEST 6

Use this diagram for #6-10.



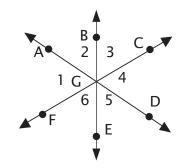
Given: $\overrightarrow{WT} \perp \overrightarrow{SV}$; $\overrightarrow{RU} \cap \overrightarrow{SV}$ at W.

- 8. The measure of $\angle UWV$ is:
 - A. 45°
 - B. 30°
 - C. 90°
 - D. 35°
 - E. can't tell from information given
- 9. $\angle 4$ and what other angle are vertical angles?
 - A. ∠3
 - B. ∠4
 - C. ∠2
 - D. ∠1
 - E. ∠TWV

10. \angle SWT + \angle TWU + \angle UWV =

- A. 180°
- B. 360°
- C. 90°
- D. 100°
- E. can't tell from information given

Use this diagram for #11–15.

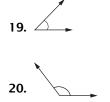


Given: \overrightarrow{FC} , \overrightarrow{AD} , \overrightarrow{BE} intersect at G.

- A. if the quantity in column I is greater.
- B. if the quantity in column II is greater.
- C. if the two quantities are equal.
- D. if the relationship cannot be determined from the information given.

Write the correct letter in the blank.

11.	l m∠2	II m∠5	
12.	m∠4 + m∠5	136°	
13.	180°	$m \angle 2 + m \angle 3$	
14.	m∠2	m∠3	
15.	185°	sum of the measures of 2 right angles	



Systematic Review 5E

- 1. f
- **2.** e
- **3.** b
- **4.** c
- **5.** g
- **6.** a
- **7.** d
- 8. false: Use a compass and a straightedge
- 9. true
- 10. false: The two parts are congruent.
- false: The line will be perpendicular only if it forms a 90° angle.
- 12. true
- 13. Use a ruler to check.
- 14. Use a ruler to check. The segment on each side of the bisector should measure $\frac{7}{8}$ in.
- 15. Use a protractor to check.
- Use a protractor to check.
 ∠XYG and ∠ZYG
 should each measure 10°.

17.
$$24Q + 18Y = 30$$

 $6(4Q + 3Y) = 6(5)$
 $4Q + 3Y = 5$

18.
$$-14Q - 21D = -42$$

 $-7(2Q + 3D) = -7(6)$
 $2Q + 3D = 6$

19.
$$16X - 8 = 56$$
$$8(2X - 1) = 8(7)$$
$$2X - 1 = 7$$
$$2X = 7 + 1$$
$$2X = 8$$
$$X = \frac{8}{2} = 4$$

20.
$$22X + 33 = 44$$
$$11(2X + 3) = 11(4)$$
$$2X + 3 = 4$$
$$2X = 4 - 3$$
$$2X = 1$$
$$X = \frac{1}{2}$$

Lesson Practice 6A

- 1. ∠AHG, ∠CHF
- **2.** ∠FHB, ∠GHD
- **3.** ∠AH**G**
- **4.** ∠GHD
- **5.** \angle LFK or \angle JFH
- **6.** ∠CHA
- **7.** \angle HFK or \angle JFL
- **8.** ∠DH**G**
- 9. 40°: vertical angles
- 10. 65°: vertical angles
- 11. 90°: supplementary angles
- 12. 50°: complementary angles
- 13. 115°: supplementary angles
- 14. 90°: vertical angles
- 15. f
- 16. a
- 1**7.** e
- 18. b
- 1**9.** d
- **20.** c

Lesson Practice 6B

- 1. \angle MNQ, \angle SNR
- 2. ∠MNQ, ∠TNP
- **3.** ∠YR**Z**
- **4.** ∠TNP
- **5.** \angle QNM or \angle PNR

- **6.** ∠TNP
- **7.** \angle YRZ or \angle SRN
- **8.** ∠SNR
- **9.** 55°: complementary angles
- 10. 35°: vertical angles
- 11. 90°: supplementary angles
- 12. 85°: supplementary angles
- 13. 40°: vertical angles
- 14. 55°: vertical angles
- 15. alpha
- 16. complementary
- 17. supplementary
- 18. gamma
- 19. vertical
- 20. delta

Systematic Review 6C

- 1. 2; 5: If the student referred to these angles using their three-letter names, that would be correct as well.
- 2. 4
- 3. BFD
- 4. BFE or AFD
- 5. BFD or AFC or AFE
- **6.** 1
- 7. 40°; complementary angles
- 8. 40°; If $m \angle 2 = 50^\circ$, then $m \angle 1 = 40^\circ$, since $\angle 1$ and $\angle 2$ are complementary. If $m \angle 1 = 40^\circ$, then $m \angle 4 = 40^\circ$, since $\angle 1$ and $\angle 4$ are vertical angles.
- **9.** 1 or 4
- 10. 140°; supplementary angles
- 11. any two of angles 1, 2, and 4
- **12.** ∠3; ∠CFE
- 13. Use a ruler to check. The segments on each side of the bisector should measure $\frac{3}{4}$ in.

- Use a protractor to check. The angles on each side of the bisector should measure 26°.
- 15. perpendicular
- **16.** 90°
- **17.** 180°
- **18.** 90°
- **19.** 180°
- 20. empty or null

Systematic Review 6D

- 1. true
- 2. false: They are complementary.
- 3. true
- 4. false: Perpendicular angles were not in the list of given information.
- 5. false: ray GK is the common side.
- 6. true
- 7. 39°: vertical angles
- 8. 51°: complementary angles
- **9.** 90°: perpendicular lines form 90° angles
- 10. right
- 11. supplementary
- **12.** 360°
- **13.** f
- 14. e
- **15.** b
- 1**6.** a
- 17. g
- 1**8.** d
- 1**9.** h
- **20.** c

Systematic Review 6E

- 1. lines QR, RV, and QV
- **2.** $\overline{\text{RT}}$, $\overline{\text{XR}}$, $\overline{\text{XT}}$
- **3.** $360^{\circ} \div 8 = 45^{\circ}$