#### **Table 16.1** Some Common Acids and Bases and their Household Uses.

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Substance	Use

#### **Acids**

Acetic acid, CH<sub>3</sub>COOH Flavoring, preservative Citric acid, H<sub>3</sub>C<sub>6</sub>H<sub>5</sub>O<sub>7</sub> Flavoring Ascorbic acid, H<sub>2</sub>C<sub>6</sub>H<sub>6</sub>O<sub>6</sub> Aluminum salts, NaAl(SO<sub>4</sub>)<sub>2</sub>·12H<sub>2</sub>O

Vitamin C; nutritional supplement

In baking powder, with sodium hydrogen

carbonate



Sodium hydroxide (lye), NaOH Ammonia, NH<sub>3</sub> Sodium carbonate, Na<sub>2</sub>CO<sub>3</sub> Sodium hydrogen carbonate, NaHCO<sub>3</sub>

Sodium phosphate, Na<sub>3</sub>PO<sub>4</sub>

Oven and drain cleaners

Household cleaner

Water softener, grease remover

Fire extinguisher, rising agent in cake mixes

(baking soda), mild antacid

Cleaner for surfaces before painting or

wallpapering









## 16.1

## **Arrhenius Acid-Base Definition**

This is the earliest acid-base definition, which classifies these substances in terms of their behavior in *water*.

An **acid** is a substance with H in its formula that dissociates to yield  $H_3O^+$ .

A **base** is a substance with OH in its formula that dissociates to yield OH<sup>-</sup>.

When an acid reacts with a base, they undergo neutralization:

$$H^+(aq) + OH^-(aq) \rightarrow H_2O(I)$$





## **Brønsted-Lowry Acid-Base Definition**

An acid is a *proton donor*, any species that donates an *H*<sup>+</sup> *ion*.

An acid must contain H in its formula.

A base is a *proton acceptor*, any species that accepts an *H*<sup>+</sup> *ion*.

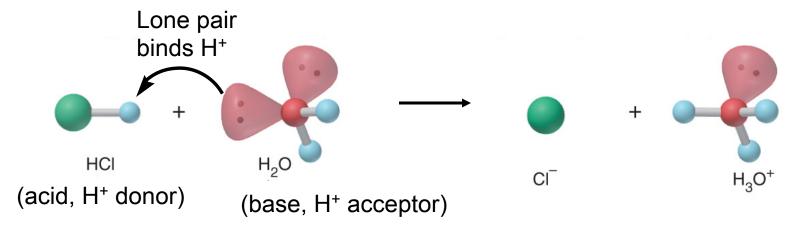
 A base must contain a *lone pair of electrons* to bond to H<sup>+</sup>.

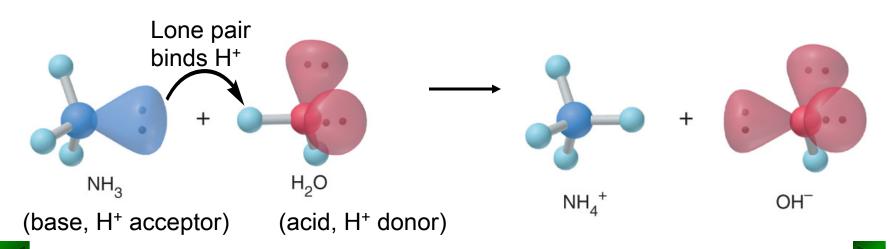
An acid-base reaction is a *proton-transfer process*.





Figure 16.2 Dissolving of an acid or base in water as a Brønsted-Lowry acid-base reaction.





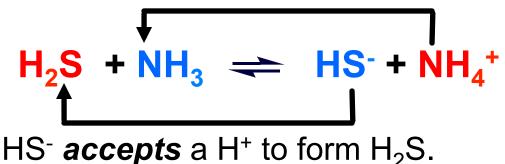
## **Conjugate Acid-Base Pairs**

#### In the **forward** reaction:

H<sub>2</sub>S *donates* a H<sup>+</sup> to form HS<sup>-</sup>.

#### In the **reverse** reaction:

NH<sub>4</sub><sup>+</sup> donates a H<sup>+</sup> to form NH<sub>3</sub>.







## **Conjugate Acid-Base Pairs**

$$H_2S + NH_3 \implies HS^- + NH_4^+$$

H<sub>2</sub>S and HS<sup>-</sup> are a *conjugate acid-base pair*: HS<sup>-</sup> is the *conjugate base* of the acid H<sub>2</sub>S.

NH<sub>3</sub> and NH<sub>4</sub><sup>+</sup> are a conjugate acid-base pair: NH<sub>4</sub><sup>+</sup> is the *conjugate acid* of the base NH<sub>3</sub>.

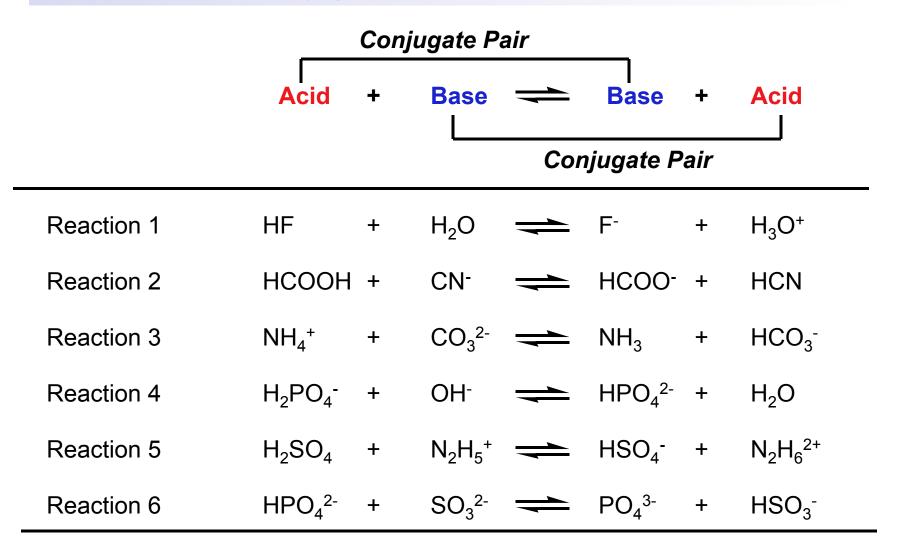
A Brønsted-Lowry acid-base reaction occurs when an acid and a base react to form their *conjugate base* and *conjugate acid*, respectively.

$$acid_1 + base_2 \Rightarrow base_1 + acid_2$$





## Table 16.2 The Conjugate Pairs in some Acid-Base Reactions







#### **Identifying Conjugate Acid-Base Pairs**

**PROBLEM:** The following reactions are important environmental processes. Identify the conjugate acid-base pairs.

(a) 
$$H_2PO_4^{-1}(aq) + CO_3^{2-1}(aq) \implies HPO_4^{2-1}(aq) + HCO_3^{-1}(aq)$$

**(b)** 
$$H_2O(I) + SO_3^{2-}(aq) \implies OH^{-}(aq) + HSO_3^{-}(aq)$$

**PLAN:** To find the conjugate pairs, we find the species that donated an H<sup>+</sup> (acid) and the species that accepted it (base). The acid donates an H<sup>+</sup> to becomes its conjugate base, and the base accepts an H<sup>+</sup> to becomes it conjugate acid.

#### **SOLUTION:**

(a) 
$$H_2PO_4^{-1}(aq) + CO_3^{2-1}(aq) \implies HPO_4^{2-1}(aq) + HCO_3^{-1}(aq)$$
  
 $acid_1$   $base_2$   $base_1$   $acid_2$ 

The conjugate acid-base pairs are H<sub>2</sub>PO<sub>4</sub>-/HPO<sub>4</sub><sup>2-</sup> and CO<sub>3</sub><sup>2-</sup>/HCO<sub>3</sub>-.





(b) 
$$H_2O(I) + SO_3^{2-}(aq) \implies OH^{-}(aq) + HSO_3^{-}(aq)$$
  
 $acid_1 \quad base_2 \quad base_1 \quad acid_2$ 

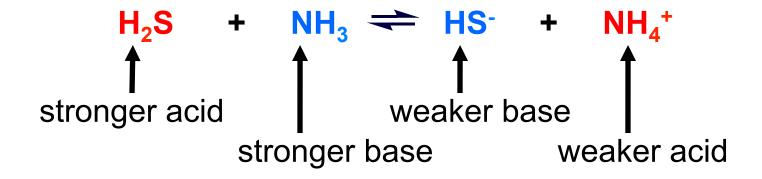
The conjugate acid-base pairs are H<sub>2</sub>O/OH<sup>-</sup> and SO<sub>3</sub><sup>2-</sup>/HSO<sub>3</sub><sup>-</sup>.



## **Net Direction of Reaction**

The *net* direction of an acid-base reaction depends on the *relative* strength of the acids and bases involved.

A reaction will favor the formation of the *weaker* acid and base.

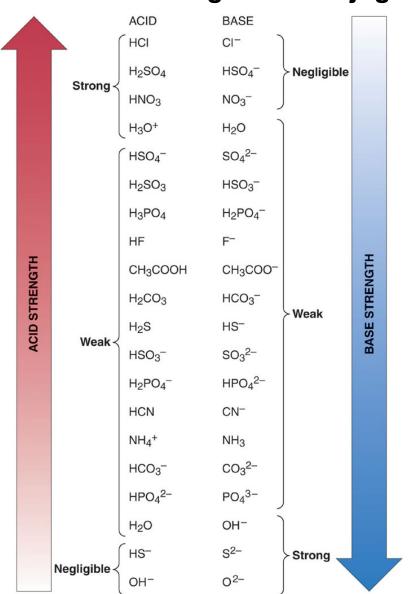


This reaction favors the formation of the *products*.





## Figure 16.3 Strengths of conjugate acid-base pairs.



The stronger the acid is, the weaker its conjugate base. When an acid reacts with a base that is farther down the list, the reaction proceeds to the **right** ( $K_c > 1$ ).

### Predicting the Net Direction of an Acid-Base Reaction

**PROBLEM:** Predict the net direction and whether *K* is greater or less than 1 for each of the following reactions (assume equal initial concentrations of all species):

(a) 
$$H_2PO_4^{-1}(aq) + NH_3(aq) \implies HPO_4^{2-1}(aq) + NH_4^{+1}(aq)$$

**(b)** 
$$H_2O(I) + HS^-(aq) \Rightarrow OH^-(aq) + H_2S(aq)$$

**PLAN:** We identify the conjugate acid-base pairs and consult figure 18.8 to see which acid and base are stronger. The reaction favors the formation of the weaker acid and base.

#### **SOLUTION:**

(a) 
$$H_2PO_4^-(aq) + NH_3(aq) \implies HPO_4^{2-}(aq) + NH_4^+(aq)$$
  
stronger acid stronger base weaker base weaker acid

The net direction for this reaction is to the right, so K > 1.





**(b)**  $H_2O(I) + HS^-(aq) \iff OH^-(aq) + H_2S(aq)$  weaker acid weaker base stronger base stronger acid

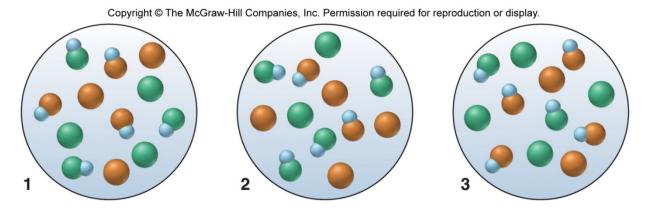
The net direction for this reaction is to the left, so K < 1.





## Using Molecular Scenes to Predict the Net Direction of an Acid-Base Reaction

**PROBLEM:** Given that 0.10 *M* of HX (*blue and green*) has a pH of 2.88, and 0.10 *M* HY (*blue and orange*) has a pH 3.52, which scene best represents the final mixture after equimolar solutions of HX and Y<sup>-</sup> are mixed?

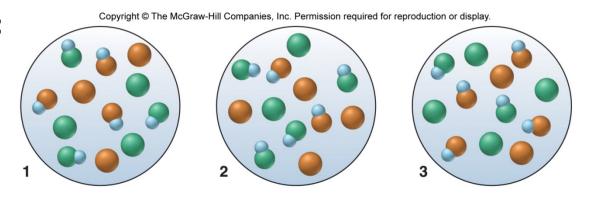


**PLAN:** A stronger acid and base yield a weaker acid and base, so we have to determine the relative acid strengths of HX and HY to choose the correct molecular scene. The concentrations of the acid solutions are equal, so we can recognize the stronger acid by comparing the pH values of the two solutions.





**SOLUTION:** 



The HX solution has a lower pH than the HY solution, so HX is the stronger acid and Y<sup>-</sup> is the stronger base. The reaction of HX and Y<sup>-</sup> has a  $K_c > 1$ , which means the equilibrium mixture will contain more HY than HX.

Scene 1 has equal numbers of HX and HY, which could occur if the acids were of equal strength. Scene 2 shows fewer HY than HX, which would occur if HY were the stronger acid.

Scene 3 is consistent with the relative acid strengths, because it contains more HY than HX.





## **Strong and Weak Acids**

A **strong** acid dissociates **completely** into ions in water:  $HA(g \text{ or } I) + H_2O(I) \rightarrow H_3O^+(aq) + A^-(aq)$ 

A dilute solution of a *strong* acid contains *no HA molecules*.

A weak acid dissociates slightly to form ions in water:

$$HA(aq) + H_2O(I) \rightleftharpoons H_3O^+(aq) + A^-(aq)$$

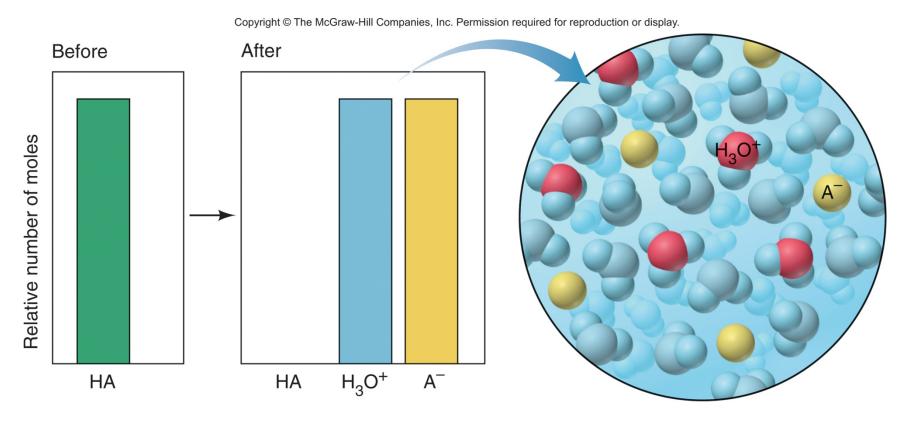
In a dilute solution of a **weak** acid, **most HA molecules are undissociated**.

$$K = \frac{[H_3O^+][A^-]}{[HA][H_2O]}$$
 has a very **small** value.





## Figure 16.4A The extent of dissociation for strong acids.



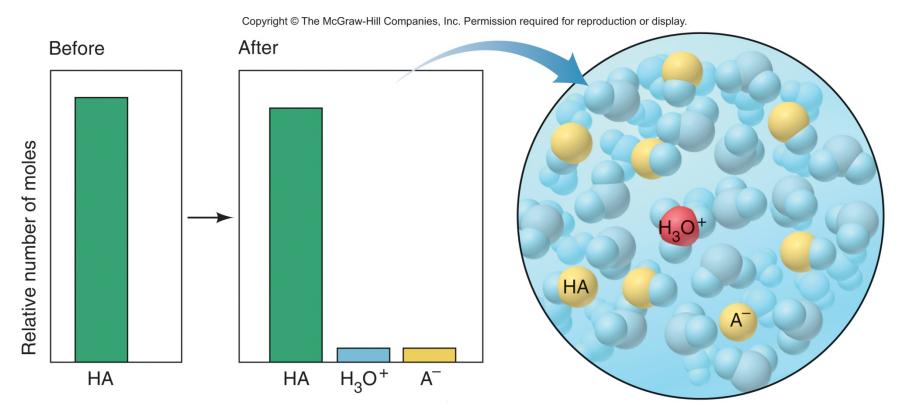
Strong acid:  $HA(g \text{ or } l) + H_2O(l) \rightarrow H_3O^+(aq) + A^-(aq)$ 

There are no HA molecules in solution.





## Figure 16.4B The extent of dissociation for weak acids.



Weak acid:  $HA(aq) + H_2O(I) \implies H_3O^+(aq) + A^-(aq)$ 

Most HA molecules are undissociated.





## The Acid Dissociation Constant, $K_a$

$$HA(aq) + H_2O(I) \Longrightarrow H_3O^+(aq) + A^-(aq)$$

**OR**  $HA(aq) \Rightarrow H^+(aq) + A^-(aq)$ 

$$K_a = \frac{[H^+][A^-]}{[HA]}$$

The value of  $K_a$  is an indication of acid strength.

Stronger acid  $\longrightarrow$  higher  $[H_3O^+] \longrightarrow$  larger  $K_a$ 

Weaker acid  $\longrightarrow$  lower % dissociation of HA  $\longrightarrow$  smaller  $K_a$ 





## Table 16.4 $K_a$ Values for some Monoprotic Acids at 25°C

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Name (Formula)	Lewis Structure*	<b>K</b> <sub>a</sub>	р <i>К</i> <sub>а</sub>	
Chlorous acid (HClO <sub>2</sub> )	H—Ö—Ö⊫Ö	$1.1 \times 10^{-2}$	1.96	
Nitrous acid (HNO <sub>2</sub> )	H—Ö—N=Ö	$7.1 \times 10^{-4}$	3.15	4
Hydrofluoric acid (HF)	н—Ё:	$6.8 \times 10^{-4}$	3.17	
Formic acid (HCOOH)  Acetic acid (CH <sub>3</sub> COOH)	H—C—C—Ö—H H :O: H—C—Ö—H	$1.8 \times 10^{-4}$ $1.8 \times 10^{-5}$		ACID STRENGTH
Propanoic acid (CH <sub>3</sub> CH <sub>2</sub> COOH)	H H :0: H—C—C—C—Ö—H H H	$1.3 \times 10^{-5}$	4.89	ACID
Hypochlorous acid (HClO)	H—Ö—ÜI:	$2.9 \times 10^{-8}$	7.54	
Hydrocyanic acid (HCN)	H—c≡N:	$6.2 \times 10^{-10}$	9.21	

<sup>\*</sup>Red type indicates the ionizable proton; all atoms have zero formal charge.

## Classifying the Relative Strengths of Acids

## Strong acids include

- the hydrohalic acids (HCI, HBr, and HI) and
- oxoacids in which the number of O atoms exceeds the number of ionizable protons by two or more (eg., HNO<sub>3</sub>, H<sub>2</sub>SO<sub>4</sub>, HClO<sub>4</sub>.)

#### Weak acids include

- the hydrohalic acid HF,
- acids in which H is not bonded to O or to a halogen (eg., HCN),
- oxoacids in which the number of O atoms equals or exceeds the number of ionizable protons by one (eg., HClO, HNO<sub>2</sub>), and
- carboxylic acids, which have the general formula RCOOH (eg., CH<sub>3</sub>COOH and C<sub>6</sub>H<sub>5</sub>COOH.)





## Classifying the Relative Strengths of Bases

## Strong bases include

- water-soluble compounds containing O<sup>2-</sup> or OH<sup>-</sup> ions.
- The cations are usually those of the most active metals:
- M<sub>2</sub>O or MOH, where M = Group 1 metal (Li, Na, K, Rb, Cs)
- MO or M(OH)<sub>2</sub> where M = group 2 metal (Ca, Sr, Ba).

#### Weak bases include

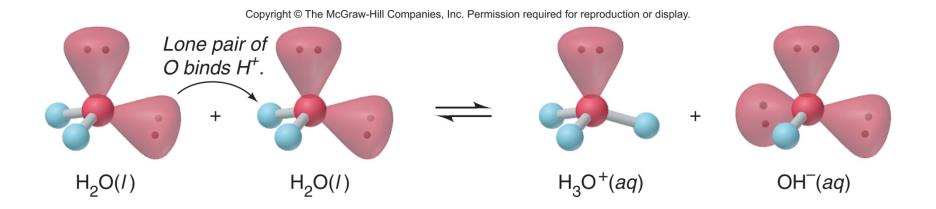
- ammonia  $(NH_3)$ ,
- amines, which have the general formula  $R\ddot{\mathbf{N}}H_2$ ,  $R_2\ddot{\mathbf{N}}H$ , or  $R_3\ddot{\mathbf{N}}$
- The common structural feature is an N atom with a lone electron pair.





## 16.2

## **Autoionization of Water**



Water dissociates very slightly into ions in an equilibrium process known as *autoionization* or *self-ionization*.

$$H_2O(I) \implies H^+(aq) + OH^-(aq)$$





## The Ion-Product Constant for Water $(K_w)$

$$H_2O(I) \Rightarrow H^+(aq) + OH^-(aq)$$

$$K_{\rm w} = [H^+][OH^-] = 1.0 \times 10^{-14} \text{ (at 25°C)}$$

In pure water,  

$$[H^+] = [OH^-] = \boxed{1.0 \times 10^{-14}} = 1.0 \times 10^{-7} \text{ (at } 25^{\circ}\text{C)}$$

Both ions are present in all aqueous systems.





A change in [H<sub>3</sub>O<sup>+</sup>] causes an inverse change in [OH<sup>-</sup>], and vice versa.

```
Higher [H<sup>+</sup>] → lower [OH<sup>-</sup>]
Higher [OH<sup>-</sup>] → lower [H<sup>+</sup>]
```

We can define the terms "acidic" and "basic" in terms of the relative concentrations of H<sub>3</sub>O<sup>+</sup> and OH<sup>-</sup> ions:

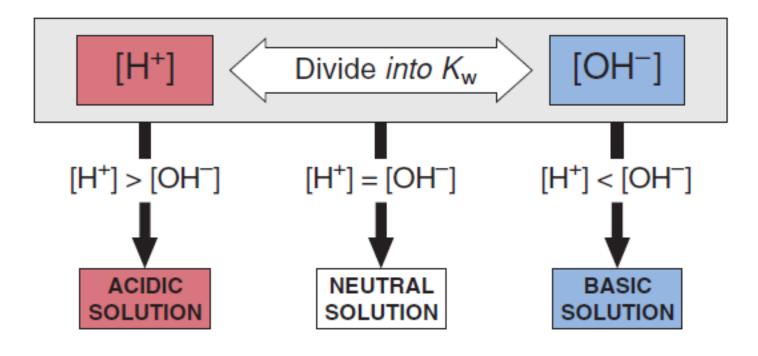
```
In an acidic solution, [H^+] > [OH^-]
In a neutral solution, [H^+] = [OH^-]
In basic solution, [H^+] < [OH^-]
```





# Figure 16.6 The relationship between [H<sub>3</sub>O<sup>+</sup>] and [OH<sup>-</sup>] and the relative acidity of solutions.

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## Calculating [H<sub>3</sub>O<sup>+</sup>] or [OH<sup>-</sup>] in an Aqueous Solution

**PROBLEM:** A research chemist adds a measured amount of HCl gas to pure water at 25°C and obtains a solution with  $[H_3O^+] = 3.0x10^{-4} M$ . Calculate  $[OH^-]$ . Is the solution neutral, acidic, or basic?

**PLAN:** We use the known value of  $K_{\rm w}$  at 25°C (1.0x10<sup>-14</sup>) and the given [H<sup>+</sup>] to solve for [OH<sup>-</sup>]. We can then compare [H<sub>3</sub>O<sup>+</sup>] with [OH<sup>-</sup>] to determine whether the solution is acidic, basic, or neutral.

#### **SOLUTION:**

$$K_{\rm w} = 1.0 \times 10^{-14} = [{\rm H}^{+}] [{\rm OH}^{-}] {\rm so}$$

$$[OH^{-}] = \frac{K_w}{[H^{+}]} = \frac{1.0 \times 10^{-14}}{3.0 \times 10^{-4}} = 3.3 \times 10^{-11} M$$

[H $^+$ ] is > [OH $^-$ ] and the solution is acidic.





## The pH Scale

$$pH = -log[H^+]$$

The pH of a solution indicates its relative acidity:

In an acidic solution,	pH < 7.00
In a neutral solution,	pH = 7.00
In basic solution,	pH > 7.00

The *higher* the pH, the *lower* the [H<sup>+</sup>] and the *less acidic* the solution.





## pH, pOH, and p $K_{\rm w}$

$$K_{\rm w} = [{\rm H}^+][{\rm OH}^-] = 1.0 \times 10^{-14} {\rm at} \ 25^{\circ}{\rm C}$$

$$pH = -log[H^+]$$
  
 $pOH = -log[OH^-]$ 

$$pK_w = pH + pOH = 14.00 at 25°C$$

pH + pOH = p $K_w$  for any aqueous solution at any temperature.

Since  $K_w$  is a constant, the values of pH, pOH, [H<sup>+</sup>], and [OH<sup>-</sup>] are interrelated:

- If [H<sup>+</sup>] increases, [OH<sup>-</sup>] decreases (and vice versa).
- If pH increases, pOH decreases (and vice versa).





Figure 16.8 The relations among [H<sub>3</sub>O<sup>+</sup>], pH, [OH<sup>-</sup>], and pOH.

		[H <sub>3</sub> O <sup>+</sup> ]	pН	[OH <sup>-</sup> ]	рОН
1		1.0 x 10 <sup>-15</sup>	15.00	1.0 x 10 <sup>1</sup>	-1.00
2		1.0 x 10 <sup>-14</sup>	14.00	1.0 x 10 <sup>0</sup>	0.00
BASIC		1.0 x 10 <sup>-13</sup>	13.00	1.0 x 10 <sup>-1</sup>	1.00
iii	BASIC	1.0 x 10 <sup>-12</sup>	12.00	1.0 x 10 <sup>-2</sup>	2.00
MORE		1.0 x 10 <sup>-11</sup>	11.00	1.0 x 10 <sup>-3</sup>	3.00
_		1.0 x 10 <sup>-10</sup>	10.00	1.0 x 10 <sup>-4</sup>	4.00
		1.0 x 10 <sup>-9</sup>	9.00	1.0 x 10 <sup>-5</sup>	5.00
		1.0 x 10 <sup>-8</sup>	8.00	1.0 x 10 <sup>-6</sup>	6.00
	NEUTRAL	1.0 x 10 <sup>-7</sup>	7.00	1.0 x 10 <sup>-7</sup>	7.00
		1.0 x 10 <sup>-6</sup>	6.00	1.0 x 10 <sup>-8</sup>	8.00
		1.0 x 10 <sup>-5</sup>	5.00	1.0 x 10 <sup>-9</sup>	9.00
MORE ACIDIC		1.0 x 10 <sup>-4</sup>	4.00	1.0 x 10 <sup>-10</sup>	10.00
AC	ACIDIC	1.0 x 10 <sup>-3</sup>	3.00	$1.0 \times 10^{-11}$	11.00
끭	ACIDIC	1.0 x 10 <sup>-2</sup>	2.00	$1.0 \times 10^{-12}$	12.00
<u>M</u>		1.0 x 10 <sup>-1</sup>	1.00	$1.0 \times 10^{-13}$	13.00
		1.0 x 10 <sup>0</sup>	0.00	1.0 x 10 <sup>-14</sup>	14.00
4		1.0 x 10 <sup>1</sup>	-1.00	1.0 x 10 <sup>-15</sup>	15.00
		1.0 × 10	1.00	1.0 X 10	10.00



### Calculating [H<sup>+</sup>], pH, [OH<sup>-</sup>], and pOH

**PROBLEM:** In an art restoration project, a conservator prepares copper-plate etching solutions by diluting concentrated HNO<sub>3</sub> to 2.0 mol/L, 0.30 mol/L, and 0.0063 mol/L HNO<sub>3</sub>. Calculate [H<sup>+</sup>], pH, [OH<sup>-</sup>], and pOH of the three solutions at 25°C.

**PLAN:** HNO<sub>3</sub> is a strong acid so it dissociates completely, and [H<sup>+</sup>] =  $[HNO_3]_{init}$ . We use the given concentrations and the value of  $K_w$  at 25°C to find [H<sup>+</sup>] and [OH<sup>-</sup>]. We can then calculate pH and pOH.

#### **SOLUTION:**

Calculating the values for 2.0 mol/L HNO<sub>3</sub>:

[H+] = 2.0 M pH = 
$$-\log[H_3O^+] = -\log(2.0) = -0.30$$
  
[OH-] =  $\frac{K_w}{[H^+]} = \frac{1.0x10^{-14}}{2.0} = 5.0x10^{-15} \text{ mol/L}$   
pOH =  $-\log[OH^-] = -\log(5.0x10^{-15}) = 14.30$ 



Calculating the values for 0.30 mol/L HNO<sub>3</sub>:

[H+] = 0.30 M pH = 
$$-\log[H^+] = -\log(0.30) = 0.52$$
  
[OH-] =  $\frac{K_w}{[H^+]} = \frac{1.0x10^{-14}}{0.30} = 3.3x10^{-14} \text{ mol/L}$   
pOH =  $-\log[OH^-] = -\log(3.3x10^{-14}) = 13.48$ 

Calculating the values for 0.0063 mol/L HNO<sub>3</sub>:

$$[H_3O^+] = 0.0063 \text{ mol/L}$$
 pH =  $-\log[H^+] = -\log(0.30) = 2.20$ 

$$[OH^{-}] = \frac{K_w}{[H^{+}]} = \frac{1.0 \times 10^{-14}}{0.0063} = 1.6 \times 10^{-12} \text{ mol/L}$$

$$pOH = -log[OH^{-}] = -log(1.6x10^{-12}) = 11.80$$





## Figure 16.9 Methods for measuring the pH of an aqueous solution.

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pH paper



pH meter





## **Weak Bases**

A Brønsted-Lowry base is a species that accepts an H<sup>+</sup>. For a weak base that dissolves in water:

$$B(aq) + H_2O(I) \Rightarrow BH^+(aq) + OH^-(aq)$$

The **base-dissociation** or **base-ionization constant** is given by:

$$K_b = \frac{[BH^+][OH^-]}{[B]}$$

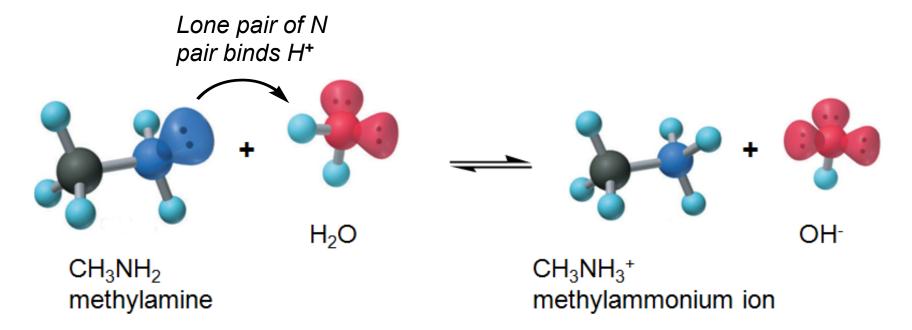
Note that **no base actually dissociates** in solution, but **ions** are produced when the base reacts with H<sub>2</sub>O.





## Figure 16.10 Abstraction of a proton from water by the base methylamine.

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## Table 16.6 K<sub>b</sub> Values for Some Molecular (Amine) Bases at 25°C

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Name (Formula)	Lewis Structure*	$K_{ m b}$	
Diethylamine [(CH <sub>3</sub> CH <sub>2</sub> ) <sub>2</sub> NH]	H—C—C— <u>N</u> —C—C—H 	$8.6 \times 10^{-4}$	
Dimethylamine [(CH <sub>3</sub> ) <sub>2</sub> NH]	H—C— <u>N</u> —C—H 	$5.9 \times 10^{-4}$	
Methylamine (CH <sub>3</sub> NH <sub>2</sub> )	H H—C—N—H 	$4.4 \times 10^{-4}$	BASE STRENGTH
Ammonia (NH <sub>3</sub> )	H— <mark>N</mark> —H     H	$1.76 \times 10^{-5}$	BASE
Pyridine $(C_5H_5N)$	N:	$1.7 \times 10^{-9}$	
Aniline (C <sub>6</sub> H <sub>5</sub> NH <sub>2</sub> )	<u>й</u> —н	$4.0 \times 10^{-10}$	

<sup>\*</sup>Blue type indicates the basic nitrogen and its lone pair.

### **Anions of Weak Acids as Weak Bases**

The anions of weak acids often function as weak bases.

$$A^{-}(aq) + H_{2}O(I) \implies HA(aq) + OH^{-}(aq) \qquad K_{b} = \frac{[HA][OH^{-}]}{[A^{-}]}$$

A solution of HA is *acidic*, while a solution of A<sup>-</sup> is *basic*.

$$HF(aq) + H_2O(I) \Rightarrow H_3O^+(aq) + F^-(aq)$$

HF is a weak acid, so this equilibrium lies to the left. [HF] >> [F-], and  $[H_3O^+]_{from\ HF}$  >>  $[OH^-]_{from\ H_2O}$ ; the solution is therefore *acidic*.





If NaF is dissolved in H<sub>2</sub>O, it dissolves completely, and F-can act as a weak base:

$$F^{-}(aq) + H_2O(I) \Rightarrow HF(aq) + OH^{-}(aq)$$

HF is a weak acid, so this equilibrium also lies to the left.  $[F^-] >> [HF]$ , and  $[OH^-]_{from F^-} >> [H_3O^+]_{from H_2O}$ ; the solution is therefore **basic**.



### $K_a$ and $K_b$ for a Conjugate Acid-Base Pair

$$\frac{HA + H_2O \implies H_3O^+ + A^-}{A^- + H_2O \implies HA + OH^-}$$

$$2H_2O \implies H_3O^+ + OH^-$$

 $K_c$  for the overall equation =  $K_1 \times K_{2}$ , so

$$\frac{[H_{3}O^{+}][A^{-}]}{[HA]} \times \frac{[HA][OH^{-}]}{[A^{-}]} = [H_{3}O^{+}][OH^{-}]$$

$$K_{a} \times K_{b} = K_{w}$$

This relationship is true for any conjugate acid-base pair.





# Solving Problems Involving Weak-Acid/Base Equilibria

### The notation system

- Molar concentrations are indicated by [].
- A bracketed formula with no subscript indicates an equilibrium concentration.

### The assumptions

- [H<sub>3</sub>O<sup>+</sup>] from the autoionization of H<sub>2</sub>O is negligible.
- A weak acid has a small  $K_a$  and its dissociation is negligible. [HA]  $\approx$  [HA]<sub>init</sub>. OR for weak bases, [B]  $\approx$  [B]<sub>init</sub>.





## Finding $K_a$ of a Weak Acid from the Solution pH

**PROBLEM:** A substance called 2-phenylacetic acid ( $C_6H_5CH_2COOH$ , simplified here as HPAc) builds up in the blood of persons with phenylketonuria, an inherited disorder that, if untreated, causes mental retardation and death. A study of the acid shows that the pH of 0.12 mol/L HPAc is 2.62. What is the  $K_a$  of phenylacetic acid?

**PLAN:** We start with the balanced dissociation equation and write the expression for  $K_a$ . We assume that  $[H_3O^+]$  from  $H_2$  is negligible and use the given pH to find  $[H_3O^+]$ , which equals  $[PAc^-]$  and  $[HPAc]_{dissoc}$ . We assume that  $[HPAc] \approx [HPAc]_{init}$  because HPAc is a weak acid.

**SOLUTION:** HPAc(aq) + H<sub>2</sub>O(I)  $\Longrightarrow$  H<sub>3</sub>O<sup>+</sup>(aq) + PAc<sup>-</sup>(aq)

$$K_a = \frac{[H_3O^+][PAc^-]}{[HPAc]}$$





Concentration (mol/L) HPAc(
$$aq$$
) + H<sub>2</sub>O( $I$ )  $\rightleftharpoons$  H<sub>3</sub>O<sup>+</sup>( $aq$ ) + PAc<sup>-</sup>( $aq$ )

Initial 0.12 - 0 -  $x$  -  $x$  +  $x$ 

Equilibrium 0.12 -  $x$  -  $x$ 

 $[H_3O^+] = 10^{-pH} = 2.4 \times 10^{-3} \text{ mol/L}$  which is >>  $10^{-7}$  (the  $[H_3O^+]$  from water)

$$x \approx 2.4 \times 10^{-3} M \approx [H_3 O^+] \approx [PAc^-]$$
 [HPAc] = 0.12 -  $x \approx 0.12$  mol/L

$$[HPAc] = 0.12 - x \approx 0.12 \text{ mol/L}$$

So 
$$K_a = \frac{(2.4 \times 10^{-3}) (2.4 \times 10^{-3})}{0.12}$$
 = 4.8x10<sup>-5</sup>

Checking the assumptions by finding the percent error in concentration:

$$[H_3O^+]_{from H_2O} = \frac{1 \times 10^{-7} \text{ mol/L}}{2.4 \times 10^{-3} \text{ mol/L}} \times 100 = 4 \times 10^{-3} \% (<5\%; \text{ assumption is justified}).$$

$$[HPAc]_{dissoc} = \frac{2.4 \times 10^{-3} \text{ mol/L}}{0.12 \text{ mol/L}} \times 100 = 2.0 \% (<5\%; \text{ assumption is justified}).$$



## Determining Concentration from $K_a$ and Initial [HA]

**PROBLEM:** Propanoic acid (CH<sub>3</sub>CH<sub>2</sub>COOH, which we simplify as EtCOOH) is a carboxylic acid whose salts are used to retard mold growth in foods. What is the [H<sub>3</sub>O<sup>+</sup>] of 0.10 mol/L EtCOOH ( $K_a = 1.3 \times 10^{-5}$ )?

**PLAN:** We write a balanced equation and the expression for  $K_a$ . We know [EtCOOH]<sub>init</sub> but not [EtCOOH] (i.e., the concentration at equilibrium). We define x as [EtCOOH]<sub>dissoc</sub> and set up a reaction table. We assume that, since EtCOOH has a small  $K_a$  value, it dissociates very little and therefore [EtCOOH]  $\approx$  [EtCOOH]<sub>init</sub>.

#### **SOLUTION:**

EtCOOH(
$$aq$$
) + H<sub>2</sub>O (I)  $\longrightarrow$  H<sub>3</sub>O<sup>+</sup>( $aq$ ) + EtCOO<sup>-</sup>( $aq$ )
$$K_a = [H_3O^+][EtCOO^-]$$
[EtCOOH]





Concentration (*M*) EtCOOH(
$$aq$$
) + H<sub>2</sub>O( $l$ )  $\Longrightarrow$  H<sub>3</sub>O<sup>+</sup>( $aq$ ) + EtCOO-
Initial 0.10 - 0
Change  $-x$  -  $+x$  + $x$ 

Equilibrium 0.10 -  $x$  -  $x$ 

Since  $K_a$  is small, we will assume that x << 0.10 and [EtCOOH]  $\approx 0.10$  mol/L.

$$K_{\rm a} = 1.3 \times 10^{-5} = \frac{[{\rm H_3O^+}][{\rm EtCOO^-}]}{[{\rm EtCOOH}]} = \frac{\chi^2}{0.10}$$

$$x = \sqrt[3]{(0.10)(1.3\times10^{-5})} = 1.1\times10^{-3} \text{ mol/L} = [H_3O^+]$$

Check: 
$$[EtCOOH]_{diss} = \frac{1.1x10^{-3} \text{ mol/L}}{0.10 \text{ mol/L}} \times 100 = 1.1\% (< 5\%; assumption is justified.)$$





### Determining pH from $K_h$ and Initial [B]

**PROBLEM:** Dimethylamine,  $(CH_3)_2NH$ , a key intermediate in detergent manufacture, has a  $K_b$  of 5.9x10<sup>-4</sup>. What is the pH of 1.5 mol/L  $(CH_3)_2NH$ ?

**PLAN:** We start with the balanced equation for the reaction of the amine with  $H_2O$ , remembering that it is a weak base. We then write the expression for  $K_b$ , set up a reaction table and solve for  $[OH^-]$ . From  $[OH^-]$  we can calculate  $[H_3O^+]$  and pH. We make similar assumptions to those made for weak acids. Since  $K_b >> K_w$ , the  $[OH^-]$  from  $H_2O$  is neglible. Since  $K_b$  is small, we can assume that the amount of amine reacting is also small, so  $[(CH_3)_2NH] \approx [(CH_3)_2NH]_{init}$ .

**SOLUTION:**  $(CH_3)_2NH(aq) + H_2O(I) \implies (CH_3)_2NH_2^+(aq) + OH^-(aq)$ 

$$K_{b} = \frac{[(CH_{3})_{2}NH_{2}^{+}][OH^{-}]}{[(CH_{3})_{2}NH]}$$





### Concentration(mol/L) (CH<sub>3</sub>)<sub>2</sub>NH(aq) + H<sub>2</sub>O(I) $\rightleftharpoons$ (CH<sub>3</sub>)<sub>2</sub>NH<sub>2</sub>+(aq) + OH-(aq)

Initial	1.50	-	0	0
Change	<b>-</b> x	-	+x	+x
Equilibrium	1.50 - <i>x</i>	-	$\mathcal{X}$	$\mathcal{X}$

Since  $K_b$  is small, x << 1.50 and  $1.50 - x \approx 1.50$ 

$$K_{\rm b} = \frac{[({\rm CH_3})_2 {\rm NH_2}^+][{\rm OH^-}]}{[({\rm CH_3})_2 {\rm NH}]} = 5.9 \times 10^{-4} \approx \frac{x^2}{1.5}$$

$$x = [OH^{-}] = 3.0x10^{-2} mol/L$$

Check assumption:

$$3.0x \underline{10^{-2} \text{ mol/L}}$$
 x 100 = 2.0% (< 5%; assumption is justified). 1.5 mol/L





[H<sup>+</sup>] = 
$$\frac{K_{\text{w}}}{[\text{OH}^{-}]} = \frac{1.0 \times 10^{-14}}{3.0 \times 10^{-2}} = 3.3 \times 10^{-13} \text{ mol/L}$$

$$pH = -log (3.3x10^{-13}) = 12.48$$





### Determining the pH of a Solution of A-

**PROBLEM:** Sodium acetate (CH<sub>3</sub>COONa, or NaOAc for this problem) has applications in photographic development and textile dyeing. What is the pH of 0.25 mol/L NaOAc?  $K_a$  of acetic acid (HAc) is  $1.8 \times 10^{-5}$ .

**PLAN:** Sodium salts are soluble in water and acetate is the anion of HAc so it acts as a weak base. We write the base dissociation equation and the expression for  $K_b$ , and solve for [OH-]. We recall that any soluble ionic salt dissociates completely in solution, so  $[OAc^-]_{init} = 0.25 \text{ mol/L}$ .

**SOLUTION:** OAc<sup>-</sup>(aq) + H<sub>2</sub>O(I) HOAc(aq) + OH<sup>-</sup>(aq)  $K_{b} = \frac{[HAc][OH^{-}]}{[OAc^{-}]}$ 





Concentration (mol/L) OAc-
$$(aq)$$
 + H<sub>2</sub>O( $I$ ) HOAc( $aq$ ) + OH- $(aq)$ 
Initial 0.25 - 0 0

Change - $x$  - + $x$  + $x$ 

Equilibrium 0.25 -  $x$  -  $x$ 

$$K_{\rm b} = \frac{K_{\rm w}}{K_{\rm a}} = \frac{1.0 \times 10^{-14}}{1.8 \times 10^{-5}} = 5.6 \times 10^{-10} \,\text{mol/L}$$

$$K_{\rm b} = 5.6 \times 10^{-10} = \frac{[{\rm HOAc}][{\rm OH}^{-}]}{[{\rm OAc}^{-}]} \approx \frac{x^2}{0.25}$$
 so  $x = [{\rm OH}^{-}] = 1.2 \times 10^{-5} \; {\rm mol/L}$ 

Checking the assumption:

OK!





$$[H_3O^+] = \frac{K_w}{[OH^-]} = \frac{1.0x10^{-14}}{1.2x10^{-5}} = 8.3x10^{-10} \text{ mol/L}$$

$$pH = -log (8.3x10^{-10}) = 9.08$$



### **Polyprotic Acids**

A **polyprotic acid** is an acid with more than one ionizable proton. In solution, each dissociation step has a different value for  $K_a$ :

$$H_3PO_4(aq) + H_2O(I) \implies H_2PO_4^-(aq) + H_3O^+(aq)$$
  $K_{a1} = \frac{[H_3O^+][H_2PO_4^-]}{[H_3PO_4]} = 7.2 \times 10^{-3}$ 

$$H_2PO_4^-(aq) + H_2O(I) \Rightarrow HPO_4^{2-}(aq) + H_3O^+(aq) K_{a2} = \frac{[H_3O^+][HPO_4^{2-}]}{[H_2PO_4^-]} = 6.3x10^{-8}$$

$$HPO_4^{2-}(aq) + H_2O(I) \implies PO_4^{3-}(aq) + H_3O^+(aq)$$
  $K_{a3} = \frac{[H_3O^+][PO_4^{3-}]}{[HPO_4^{2-}]} = 4.2 \times 10^{-13}$ 

$$K_{a1} > K_{a2} > K_{a3}$$

We usually neglect [H<sub>3</sub>O<sup>+</sup>] produced after the first dissociation.





## Table 16.7 Successive $K_a$ values for Some Polyprotic Acids at 25°C

Name (Formula)	Copyright © The McGraw-Hill Compani <b>Lewis Structure*</b>	es, Inc. Permission require $oldsymbol{\mathit{K}_{a1}}$	red for reproduction or dis $ extit{\emph{K}}_{ extbf{a2}}$	play. <b>K</b> a3	
Oxalic acid (H <sub>2</sub> C <sub>2</sub> O <sub>4</sub> )	:0: :0:       H—Ö—C—C—Ö—H	5.6×10 <sup>-2</sup>	$5.4 \times 10^{-5}$		
Sulfurous acid (H <sub>2</sub> SO <sub>3</sub> )	:0:    H—Ö—S—Ö—Н	$1.4 \times 10^{-2}$	$6.5 \times 10^{-8}$		
Phosphoric acid (H <sub>3</sub> PO <sub>4</sub> )	:0: H—Ö—P—Ö—H :O—H	$7.2 \times 10^{-3}$	$6.3 \times 10^{-8}$	$4.2 \times 10^{-13}$	RENGTH
Arsenic acid (H <sub>3</sub> AsO <sub>4</sub> )	:O:    H—Ö—As—Ö—H   :O—H	$6 \times 10^{-3}$	$1.1 \times 10^{-7}$	3×10 <sup>-12</sup>	ACID STRENGTH
Carbonic acid (H <sub>2</sub> CO <sub>3</sub> )	:0:    н—ё—с—ё—н	$4.5 \times 10^{-7}$	4.7×10 <sup>-11</sup>		
Hydrosulfuric acid (H <sub>2</sub> S)	H—Ë—H	$9 \times 10^{-8}$	$1 \times 10^{-17}$		

<sup>\*</sup>Red type indicates the ionizable protons.





## Calculating Equilibrium Concentrations for a Polyprotic Acid

**PROBLEM:** Ascorbic acid ( $H_2C_6H_6O_6$ ;  $H_2$ Asc for this problem), known as vitamin C, is a diprotic acid ( $K_{a1} = 1.0 \times 10^{-5}$  and  $K_{a2} = 5 \times 10^{-12}$ ) found in citrus fruit. Calculate [ $H_2$ Asc], [ $HAsc^-$ ], [ $Asc^2$ -], and the pH of 0.050 *mol/L*  $H_2$ Asc.

**PLAN:** We first write the dissociation equations and the associated  $K_a$  expressions. Since  $K_{a1} >> K_{a2}$ , we can assume that the first dissociation produces almost all the  $H_3O^+$ . Also, since  $K_{a1}$  is small, the amount of  $H_2ASc$  that dissociates can be neglected. We set up a reaction table for the first dissociation, with x equal to  $[H_2Asc]_{dissoc}$ , and solve for  $[H_3O^+]$  and  $[HAsc^-]$ .

#### **SOLUTION:**

$$H_2Asc(aq) + H_2O(I) \Longrightarrow HAsc^-(aq) + H_3O^+(aq)$$
  $K_{a1} = \frac{[HAsc^-][H_3O^+]}{[H_2Asc]} = 1.0x10^{-5}$ 
 $HAsc^-(aq) + H_2O(I) \Longrightarrow Asc^2-(aq) + H_3O^+(aq)$   $K_{a2} = \frac{[Asc^2-][H_3O^+]}{[HAsc^-]} = 5x10^{-12}$ 





Concentration (mol/L)  $H_2Asc(aq) + H_2O(I) \implies HAsc^{-}(aq) + H_3O^{+}(aq)$ 

Initial
 
$$0.050$$
 -
 0
 0

 Change
 -x
 -
 +x
 +x

 Equilibrium
  $0.050 - x$ 
 -
 x
 x

$$K_{a1} = \frac{[HAsc^{-}][H_3O^{+}]}{[H_2Asc]} = 1.0x10^{-5} = \frac{x^2}{0.050 - x} \approx \frac{x^2}{0.050}$$

$$x = [H_3O^+] = [HAsc^-] = [10.050)(1.0x10^{-5})$$
 = 7.1x10<sup>-4</sup> mol/L

$$pH = -log[H_3O^+] = -log(7.1x10^{-4}) = 3.15$$





### Checking assumptions:

1.  $[H_3O^+]_{from \ HAsc^-} << [H_3O^+]_{from \ H_2Asc}$ : For any second dissociation,  $[H_3O^+]_{from \ HAsc^-} \approx ?[HAsc^-](K_{a2}) = ?[7.1x10^{-4})(5x10^{-12}) = 6x10^{-8} \ mol/L$ 

This is even less than  $[H_3O^+]_{from\ H_2O}$ , so the assumption is justifed.

2. 
$$[H_2Asc]_{dissoc} << [H_2Asc]_{init}$$
:

$$\frac{7.1 \times 10^{-4} M}{0.050 M}$$
 x 100 = 1.4% (< 5%; assumption is justified).





### 16.5 Acid Strength of Nonmetal Hydrides

For nonmetal hydrides (E-H), acid strength depends on:

- the electronegativity of the central nonmetal (E), and
- the strength of the E-H bond.

Across a period, acid strength increases.

Electronegativity increases across a period, so the acidity of E-H increases.

Down a group, acid strength increases.

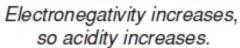
The length of the E-H bond increases down a group and its bond strength therefore decreases.

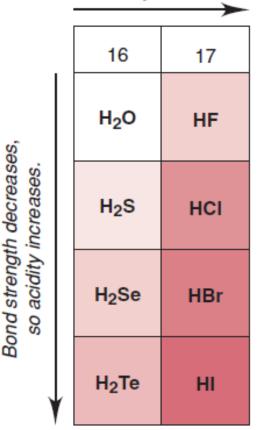




## Figure 16.11 The effect of atomic and molecular properties on nonmetal hydride acidity.

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### **Acid Strength of Oxoacids**

All oxoacids have the acidic H bonded to an *O atom*.

Acid strength of oxoacids depends on:

- the electronegativity of the central nonmetal (E), and
- the number of O atoms around E.

For oxoacids with the **same** number of O atoms, acid strength increases as the electronegativity of E increases.

For oxoacids with *different* numbers of O atoms, acid strength increases with the number of O atoms.





### Figure 16.12 The relative strengths of oxoacids.

Electronegativity increases, so acidity increases.

Number of O atoms increases, so acidity increases.





### **Hydrated Metal Ions**

Some *hydrated* metal ions are able to transfer an H<sup>+</sup> to H<sub>2</sub>O. These metal ions will form *acidic* solutions.

Consider a metal ion in solution,  $M^{n+}$ :

$$M^{n+}(aq) + H_2O(I) \rightarrow M(H_2O)_x^{n+}(aq)$$

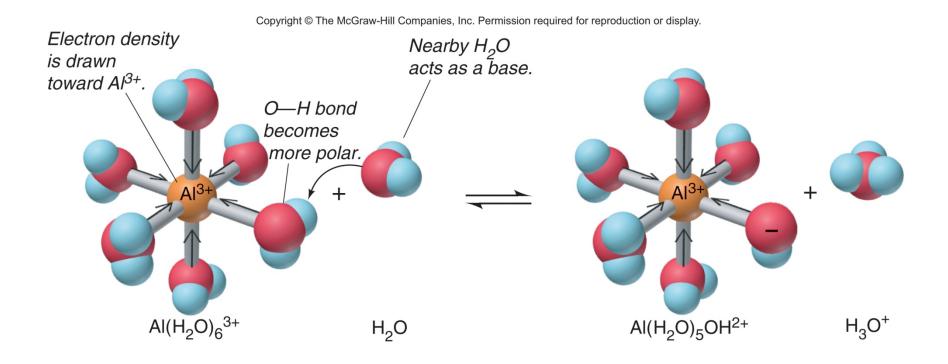
If M<sup>n+</sup> is **small** and **highly charged**, it will withdraw enough e<sup>-</sup> density from the O-H bonds of the bound H<sub>2</sub>O molecules to release H<sup>+</sup>:

$$M(H_2O)_x^{n+}(aq) + H_2O(I) \implies M(H_2O)_{x-1}OH^{(n-1)}_{(aq)} + H_3O^+(aq)$$





### Figure 16.13 The acidic behavior of the hydrated Al<sup>3+</sup> ion.

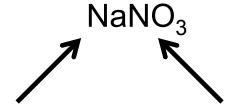






### Salts that Yield Neutral Solutions

A salt that consists of the **anion** of a **strong acid** and the **cation** of a **strong base** yields a **neutral** solution.



Na<sup>+</sup> is the cation of NaOH, a strong base.

NO<sub>3</sub><sup>-</sup> is the anion of HNO<sub>3</sub>, a strong acid.

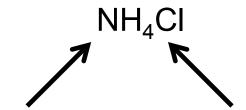
This solution will be neutral, because neither Na<sup>+</sup> nor NO<sub>3</sub><sup>-</sup> will react with H<sub>2</sub>O to any great extent.





### Salts that Yield Acidic Solutions

A salt that consists of the *anion* of a *strong acid* and the *cation* of a *weak base* yields an *acidic* solution.



NH<sub>4</sub> <sup>+</sup> is the cation of Cl<sup>-</sup> is the anion of NH<sub>3</sub>, a weak base.

HCI, a strong acid.

This solution will be *acidic*, because NH<sub>4</sub><sup>+</sup> will react with  $H_2O$  to produce  $H_3O^+$ :

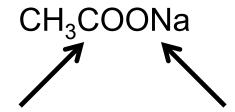
$$NH_4^+(aq) + H_2O(I) \Rightarrow NH_3(aq) + H_3O^+(aq)$$





### Salts that Yield Basic Solutions

A salt that consists of the *anion* of a *weak acid* and the *cation* of a *strong base* yields a *basic* solution.



CH<sub>3</sub>COO<sup>-</sup> is the anion of Na<sup>+</sup> is the cation of CH<sub>3</sub>COOH, a weak acid. NaOH, a strong base.

This solution will be **basic**, because CH<sub>3</sub>COO<sup>-</sup> will react with H<sub>2</sub>O to produce OH<sup>-</sup>:

$$CH_3COO^-(aq) + H_2O(I) \Rightarrow CH_3COOH(aq) + OH^-(aq)$$





## Predicting Relative Acidity of Salt Solutions from Reactions of the lons with Water

- **PROBLEM:** Predict whether aqueous solutions of the following are acidic, basic, or neutral, and write an equation for the reaction of any ion with water:
- (a) Potassium perchlorate, KClO<sub>4</sub> (b) Sodium benzoate, C<sub>6</sub>H<sub>5</sub>COONa
- (c) Chromium(III) nitrate, Cr(NO<sub>3</sub>)<sub>3</sub>
- PLAN: We identify the cation and anion from the formula for each salt. Depending on an ion's ability to react with water, the solution will be neutral (strong-acid anion with strong-base cation), acidic (weak-base cation with strong-acid anion), or basic (weak-acid anion and strong-base cation).

#### **SOLUTION:**

(a)  $K^+$  is the cation of a strong base (KOH) while  $ClO_4^-$  is the anion of a strong acid (HClO<sub>4</sub>). This solution will be neutral.





**(b)** Na<sup>+</sup> is the cation of a strong base (NaOH) while the benzoate anion (C<sub>6</sub>H<sub>5</sub>COO<sup>-</sup>) is the anion of a weak acid (benzoic acid). The benzoate ion will react with H<sub>2</sub>O to produce OH<sup>-</sup> ions:

$$C_6H_5COO^-(aq) + H_2O(I) \rightleftharpoons C_6H_5COOH(aq) + OH^-(aq)$$

This solution will be basic.

(c) NO<sub>3</sub><sup>-</sup> is the anion of a strong acid (HNO<sub>3</sub>) and will not react with H<sub>2</sub>O to any great extent. Cr<sup>3+</sup> is a small metal cation with a fairly high charge density. It will become hydrated and the hydrated ion will react with H<sub>2</sub>O to form H<sub>3</sub>O<sup>+</sup> ions:

$$Cr(H_2O)_6^{3+}(aq) + H_2O(I) \implies Cr(H_2O)_5OH^{2+}(aq) + H_3O^{+}(aq)$$

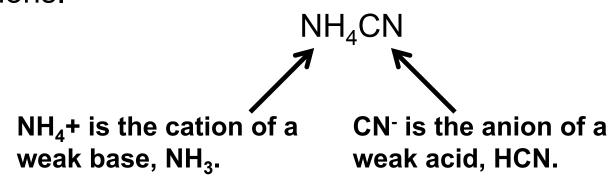
This solution will be acidic.





# Salts of Weak Conjugate Acids and Weak Conjugate Bases

If a salt that consists of the **anion** of a **weak acid** and the **cation** of a **weak base**, the pH of the solution will depend on the relative acid strength or base strength of the ions.



$$NH_4^+(aq) + H_2O(I) \Rightarrow NH_3(aq) + H_3O^+(aq)$$

$$CN^{-}(aq) + H_2O(I) \Rightarrow HCN(aq) + OH^{-}(aq)$$





The reaction that proceeds farther to the right determines the pH of the solution, so we need to compare the  $K_a$  of NH<sub>4</sub><sup>+</sup> with the  $K_b$  of CN<sup>-</sup>.

$$K_{\rm a} \text{ of NH}_4^+ = \frac{K_{\rm w}}{K_{\rm b} \text{ of NH}_3} = \frac{1.0 \times 10^{-14}}{1.76 \times 10^{-5}} = 5.7 \times 10^{-10}$$

$$K_{\rm b}$$
 of CN<sup>-</sup> =  $\frac{K_{\rm w}}{K_{\rm a}}$  of HCN =  $\frac{1.0 \times 10^{-14}}{6.2 \times 10^{-10}}$  = 1.6×10<sup>-5</sup>

Since  $K_b$  of  $CN^- > K_a$  of  $NH_4^+$ ,  $CN^-$  is a stronger base than  $NH_4^+$  is an acid. A solution of  $NH_4CN$  will be basic.





16.7

### The Levelling Effect

All strong acids and bases are equally strong in water.

All strong acids dissociate completely to form H<sub>3</sub>O<sup>+</sup>, while all strong bases dissociate completely to form OH<sup>-</sup>.

In water, the strongest acid possible is  $H_3O^+$  and the strongest base possible is  $OH^-$ .

H<sub>2</sub>O exerts a *leveling effect* on any strong acid or base.





### The Lewis Acid-Base Definition

A **Lewis base** is any species that **donates** an **electron pair** to form a bond.

A *Lewis acid* is any species that *accepts* an *electron pair* to form a bond.



The Lewis definition views an acid-base reaction as the donation and acceptance of an electron pair to form a covalent bond.



