## UNIT 4

## Exploring Thousandths

LESSON

## Quick Review

- Numbers with tenths, hundredths, and thousandths can be written as decimals.

$$
\frac{3}{10} \quad 0.3
$$

three tenths
$1 \frac{7}{100}$
1.07
one and seven hundredths
$\frac{213}{1000} \quad 0.213$ two hundred thirteen thousandths

- You can use a place-value chart to show decimals.

| Tens | Ones | Tenths | Hundredths | Thousandths |
| :---: | :---: | :---: | :---: | :---: |
|  | 4 | 6 | 2 | 3 |

- You can write decimals in expanded form.
$4.623=4$ ones +6 tenths +2 hundredths +3 thousandths
$=4+0.6+0.02+0.003$


## Try These

1. Write each number as a decimal.
a) $\frac{7}{100}$ $\qquad$ b) $2 \frac{14}{1000}$
2.014
c) $32 \frac{19}{100}$
32.19
d) $5 \frac{6}{1000}$ $\qquad$ e) $216 \frac{374}{1000}$
216.374
f) $\frac{108}{1000}$ $\qquad$
2. Write each decimal in expanded form.
a) 0.405 $\qquad$ $0.4+0.005$
b) 84.007 $\qquad$
3. Write each number in words.
a) 0.234 two hundred thirty-four thousandths
b) 17.637 seventeen and six hundred thirty-seven thousandths

## Practice

1. Record each number in the place-value chart.
a) 76 thousandths
b) 316 and 536 thousandths
c) 185 thousandths
d) 93 and 3 thousandths

|  | Hundreds | Tens | Ones | © | Tenths | Hundredths |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| a) |  |  | 0 | Thousandths |  |  |
| b) | 3 | 1 | 6 | 0 | 7 | 6 |
| c) |  |  | 0 | 5 | 3 | 6 |
| d) |  | 9 | 3 | 1 | 8 | 5 |

2. Write each number as a fraction or a mixed number.
a) $3.047 \quad 3 \frac{47}{1000}$
b) $62.354 \quad 62 \frac{354}{1000}$
c) $0.739 \quad \frac{739}{1000}$
d) 0.001 $\qquad$ e) 2.72 $\qquad$
f) 1.506 $\qquad$
3. Write each number in question 2 in expanded form.
a) $3+0.04+0.007$
b) $60+2+0.3+0.05+0.004$
c) $0.7+0.03+0.009$
d) 0.001
e) $\underline{2+0.7+0.02}$
f) $1+0.5+0.006$
4. Write each number as a decimal.
a) $2 \frac{9}{1000} \quad 2.009$
b) $17 \frac{6}{100}$
17.06
c) $\frac{85}{1000}$ $\qquad$
d) $5 \frac{25}{1000} \quad 5.025$
e) $\frac{367}{1000}$ $\qquad$ f) $\frac{8}{1000}$ $\qquad$

## Stretch Your Thinking

Use the digits $0,2,3$, and 6 .
Make a number that is greater than 1 but less than 4.
Find as many numbers as you can.
$2.036,2.063,2.306,2.360,2.603,2.630$,
$3.026,3.062,3.206,3.260,3.602,3.620$

## UNH 4

## Comparing and Ordering Decimals

LESSON

## Quick Review



The table shows the masses of Henry's 3 kittens.

Here are 2 ways to order the pets from least to greatest mass.

| Kitten | Mass (kg) |
| :--- | :---: |
| Foofoo | 0.395 |
| Quigley | 0.364 |
| Oscar | 0.391 |

- Use a place-value chart.

| Ones | Tenths | Hundredths | Thousandths |
| :---: | :---: | :---: | :---: |
| 0 | 3 | 9 | 5 |
| 0 | 3 | 6 | 4 |
| 0 | 3 | 9 | 1 |

All 3 numbers have 0 ones and 3 tenths.
0.364 has the least hundredths, so it is the least number.
0.395 has the greatest number of thousandths, so it is the greatest.

The pets in order from least to greatest mass are: Quigley, Oscar, Foofoo. - Use a number line.


Reading numbers from left to right gives the masses from least to greatest.

## Try These

1. Use $>,<$, or $=$ to make each statement true.
a) 0.457 $\qquad$ 0.406
b) 17.63 $\qquad$ 17.630
c) 5.976 $\qquad$ $<$ 6.0
2. Order the numbers from greatest to least.
a) $0.36,0.371,0.329$
$0.371,0.36,0.329$
b) $2.76,5.3,2.485$
$5.3,2.76,2.485$

## Rounding Decimals

## LESSON

## Quick Review

You can use a number line to round decimals.

- Round 2.356 to the nearest whole number.

2.356 is loetween 2 and 3 , but closer to 2 .

So, 2.356 rounded to the nearest whole number is 2 .

- Round 2.356 to the nearest tenth.

2.356 is between 2.3 and 2.4, but closer to 2.4.

So, 2.356 rounded to the nearest tenth is 2.4 .

- Round 2.356 to the nearest hundredth.

2.356 is between 2.35 and 2.36 , but closer to 2.36 .

So, 2.356 rounded to the nearest hundredth is 2.36 .

## Try These

1. Round to the nearest whole number.
a) 3.06 $\qquad$ b) 7.7 $\qquad$ C) 14.135 $\qquad$ d) 0.973 $\qquad$
2. Round to the nearest tenth.
a) 2.25 $\qquad$ b) 5.862
5.9
c) 3.789 3.8
d) 1.173 1.2
3. Round to the nearest hundredth.
a) 0.738
0.74
b) 4.159
4.16
c) 2.235
2.24
d) 9.141 $\qquad$

## UNIT 4

## 5

## Estimating Sums and Differences

LESSON

## Quick Review

Here are 3 ways to estimate $4.548+2.417$.

- Round each decimal to the nearest whole number:
$5+2=7$
R Round only 1 decimal to the nearest whole number:

$$
5+2.417=7.417
$$

R Round each decimal to the nearest tenth or hundredth:
$4.5+2.4=6.9$
$4.55+2.42=6.97$
Here are 2 ways to estimate $4.538-2.417$.

- Round the second decimal to the nearest whole number:
$4.538-2=2.538$
- Round both decimals to the nearest tenth or hundredth:
$4.5-2.4=2.1$
$4.54-2.42=2.12$


## Try These

1. Estimate each sum. Sample Answers
a) $2.54+7.16$
$\qquad$
b) $4.197+3.864$
8
c) $0.765+1.295$
$\qquad$
d) $5.765+3.189$
$\qquad$
e) $0.473+1.697$
f). $2.008+3.801$
$\qquad$
$\qquad$
2. Estimate each difference. Sample Answers
a) $7.546-3.518$
$\qquad$
b) $2.476-1.555$
$\qquad$
c) $7.9-3.267$
$\qquad$
d) $3.204-0.938$
$\qquad$
e) $1.497-0.126$
$\qquad$
f) $12.094-8.259$
$\qquad$

## UNIT 4

 DecimalsLESSON

## Quilk Review

- You can use place value to add 5.763 and 3.949.

Step 1: Estimate.
Step 2: Add as you would with whole numbers.

Round 3.949 to 4 .
Add: $5.763+4=9.763$
5.763
$\begin{array}{r}+3.949 \\ \hline 9.712\end{array}$
9.712 is close to the estimate, so the answer is reasonable.

- You can use place value to subtract 3.949 from 5.763.

Step 1: Estimate.
Step 2: Subtract as you would with whole numbers.

417513
5.768

Subtract $5.763-4=1.763$
$\frac{-3.949}{1.814}$
1.814 is close to the estimate, so the answer is reasonable.

## Try These

1. Add.
a) $\begin{array}{r}4.521 \\ +\quad 3.097 \\ \hline 7.618\end{array}$
b) 2.168
c) 7.169
d) 6.704
$\begin{array}{r}2.168 \\ +0.948 \\ \hline 3.116\end{array}$
$\begin{array}{r}\text { + } 8.473 \\ \hline 15.642\end{array}$
$\begin{array}{r}0.491 \\ \hline 7.195\end{array}$
2. Subtract.
a) $\begin{array}{r}9.732 \\ -\quad 0.489 \\ \hline 9.243\end{array}$
b) $\begin{array}{r}6.371 \\ -\quad 1.098 \\ \hline 5.273\end{array}$
c) $\begin{array}{r}4.152 \\ -4.097 \\ \hline 0.055\end{array}$
d) $\begin{array}{r}3.652 \\ -\quad 1.984 \\ \hline 1.668\end{array}$

## Practice

1. Add. Use subtraction to check each answer.

a) | 4.157 | 10.503 |
| ---: | ---: |
| +6.346 | -6.346 |
| 10.503 | 4.157 |

b) $\begin{array}{r}27.309 \\ +\quad 41.476 \\ \hline 41.167 \\ \hline 4.14 .167 \\ \hline 27.309\end{array}$
c) 3.187
7.866
$+6.346-6.346$
$\begin{array}{r}+4.679 \\ \hline 7.866\end{array} \frac{-4.679}{3.187}$
d) $\begin{array}{r}5.138 \\ +12.349 \\ \hline \mathbf{1 7 . 4 8 7}\end{array} \begin{array}{r}17.487 \\ \hline\end{array}$
f) $36.234 \quad 51.109$

$$
\begin{aligned}
& \text { e) } \begin{array}{r}
0.573 \\
+4.497 \\
\hline 5.070
\end{array} \begin{array}{r}
5.070 \\
\hline
\end{array} \\
& \begin{array}{r}
+12.349 \\
\hline 17.487 \\
-12.349 \\
5.138
\end{array} \\
& \begin{array}{r}
4.497 \\
\hline 5.070
\end{array} \\
& +14.875-14.875
\end{aligned}
$$

2. Subtract. Use addition to check each answer.
a) $\begin{array}{r}7.243 \\ -2.807 \\ \hline 4.436 \\ \hline \mathbf{2 . 8 0 7} \\ \hline 7.243\end{array}$
b) 4.583
2.245
c) 13.040
5.178
$\frac{-2.338}{2.245}+2.338$

$$
\frac{-7.862}{5.178}+\frac{+7.862}{13.040}
$$

$$
\text { d) } \begin{array}{rr}
11.431 & 2.668 \\
-8.763 \\
\hline 2.668 & +8.763 \\
\hline 11.431
\end{array}
$$

e)
$4.010 \quad 1.148$
f) 73.832
22.067
$\frac{-2.862}{1.148}+\frac{2.862}{4.010}$
$\frac{-51.765}{22.067} \frac{+51.765}{73.832}$
3. The difference in the masses of 2 objects is 0.479 kg . Sample Answers
a) What might the mass of each object be? $\qquad$ 2.567 kg and 2.088 kg
b) What might the objects be? $\qquad$ Two beef roasts
4. Salvatore ran 2.457 km on Saturday and 3.169 km on Sunday.
a) How far did Salvatore run in all? $\qquad$ 5.626 km
b) How much further did he run on Sunday than on Saturday?
$\qquad$ 0.712 km

## Stretch Your Thinking

Use each of the digits 1 to 8 once to make this subtraction true.

Sample Answer


## UNH 4

## Multiplying Decimals by 10, 100, 1000, 10000

LESSON

## Quick Review

Use mental math to multiply a decimal by $10,100,1000$, and 10000 .

- When you multiply a decimal by 10 , the digits shift 1 place to the left.
You show this by moving the decimal point 1 place to the right.
- When you multiply a decimal by 100, the digits shift 2 places to the left. You show this by moving the decimal point 2 places to the right.
- When you multiply a decimal by 1000, the digits shift 3 places to the left. You show this by moving the decimal point 3 places to the right.
- When you multiply a decimal by 10000 , the digits shift 4 places to the left.
- You show this by moving the decimal point 4 places to the right.
$2.45 \times 10=24.5$
$0.432 \times 10=4.32$
$6.8 \times 10=68$
$1.367 \times 100=136.7$
$5.3 \times 100=530$
$0.25 \times 100=25$
$5.846 \times 1000=5846$
$3.21 \times 1000=3210$
$0.004 \times 1000=4$
$0.245 \times 10000=2450$
$1.26 \times 10000=12600$
$0.8 \times 10000=8000$


## Try These

Use mental math to find each product.
1.
a) $6.5 \times 10=\underline{65}$
b) $7.34 \times 10=73.4$
c) $0.461 \times 10=4.61$
$6.5 \times 100=\underline{650}$
$7.34 \times 100=734$
$0.461 \times 100=46.1$
$6.5 \times 1000=\underline{6500}$
$7.34 \times 1000=\underline{7340}$
$0.461 \times 1000=461$
$6.5 \times 10000=\underline{65000} 7.34 \times 10000=\underline{73} 4000.461 \times 10000=\underline{4610}$
2. a) $1.9 \times 10=$ $\qquad$ b) $6.73 \times 100=\underline{673}$
c) $9.365 \times 10000=93650$
d) $2.6 \times 100=\underline{260}$
e) $7.2 \times 1000=\underline{7200}$
f) $0.486 \times 1000=\underline{486}$
g) $2.63 \times 10=\underline{26.3}$
h) $1.123 \times 100=\underline{112.3}$
i) $0.586 \times 10000=\underline{5860}$

## UNIT 4

## 8

## Dividing Decimals by 10, 100, 1000, 10000

LESSON

## Quick Review

Use mental math to divide a decimal by $10,100,1000$, and 10000 .

- When you divide a decimal by 10, $\quad 3.62 \div 10=0.362$
the digits shift 1 place to the right. $\quad 8.7 \div 10=0.87$
You show this by moving the decimal
$6.8 \div 10=0.68$ point 1 place to the left.
- When you divide a decimal by 100, $\quad 1.63 \div 100=0.0163$
the digits shift 2 places to the right. $\quad 5.6 \div 100=0.056$ You show this by moving the decimal point 2 places to the left.
- When you divide a decimal by 1000,
$3 \div 100=0.03$
the digits shift 3 places to the right.
You show this by moving the decimal point 3 places to the left.
- When you divide a decimal by 10000 ,
$7.5 \div 10000=0.00075$
the digits shift 4 places to the right.
$1.4 \div 10000=0.00014$
You show this by moving the decimal
$6 \div 10000=0.0006$ point 4 places to the left.
$4.415 \div 1000=0.00415$
$7.2 \div 1000=0.0072$
$1 \div 1000=0.001$


## Try These

Use mental math to find each quotient.
1.
a) $8.2 \div 10=$ $\qquad$ b) $5 \div 10=0.5$ $8.2 \div 100=0.082$ $5 \div 100=\quad 0.05$
$8.2 \div 1000=$ $\qquad$

$$
5 \div 1000=0.005
$$

$8.2 \div 10000=0.00082$
$5 \div 10000=$ $\qquad$
2.
a) $3.4 \div 10=0.34$
b) $1.63 \div 100=\underline{0.0163}$
c) $1.12 \div 1000=\underline{0.00112}$
d) $0.5 \div 100=\underline{0.005}$
e) $8 \div 10000=\underline{0.0008}$
f) $7 \div 10000=\underline{0.0007}$
g) $5.17 \div 10=\underline{0.517}$
h) $9.6 \div 1000=\underline{0.0096}$
i) $6.382 \div 10=\underline{0.6382}$

## UNIT 4

## 10 <br> LESSON

 Multiplying Decimals by a Whole Number
## Quick Review

You can use what you know about multiplying whole numbers to multiply a decimal by a whole number.
Multiply: $2.936 \times 4$
$>$ First estimate.
Round 2.936 to 3.
$3 \times 4=12$
So $2.936 \times 4$ is about 12 .
> Record the numbers without the 2936
decimal point. $\quad \times 4$

Multiply as you would with
24
whole numbers. 120
> Use the estimate to place the 3600
decimal point in the product.
11.744 is close to 12 , so
$\longrightarrow \xrightarrow{8000}$
$2.936 \times 4$ is 11.744 .

## Try These

Multiply.
1.
$\begin{array}{r}5.18 \\ \times \quad 5 \\ \hline 25.9\end{array}$
b) 1.734
c) 0.143
d) 9.431
$\begin{array}{r}\times \quad 8 \\ \hline 13.872\end{array}$
$\begin{array}{r}\times \quad 4 \\ \hline 0.572\end{array}$
$\frac{\times 2}{18.862}$

## Practice

1. Use paper and pencil to find each product.

Record the products on the lines.
Then use the letters next to the products to solve this riddle.
Why did the jellybean
go to school?
$0.396 \times 5=1.98$
(S)
$1.842 \times 2=3.684(X)$
$1.637 \times 3=4.911(A)$
$1.004 \times 7=7.028$
$0.176 \times 4=\underline{0.704}$
$8.145 \times 6=48.87$
$2.534 \times 2=5.068$
$0.941 \times 9=8.469$
$1.935 \times 4=7.74(\mathrm{M})$
$2.123 \times 4=8.492$
$0.132 \times 2=0.264$
(E)
$4.113 \times 2=8.226$
$3.005 \times 3=9.015$
$1.254 \times 3=3.762$
$0.524 \times 6=3.144(H)$
$0.148 \times 5=0.74$


## Stretch Your Thinking

What whole number would you multiply 6.374 by to get the product 25.496 ? $\qquad$

## Dividing Decimals by a Whole Number

## Quick Review

Here is one way to divide a decimal by a whole number.
Divide: $7.938 \div 2$

- Record the numbers without the decimal point. Divide as you would with whole numbers.
- Estimate to place the decimal point. 7.938 rounds to 8.

$$
8 \div 2 \text { is } 4
$$

The answer must be a little less than 4 .
So, $7.938 \div 2=3.969$

- Check by multiplying:
$3.969 \times 2=7.938$
So, the answer is correct.


## Try These

1. Divide.
a) $3.896 \div 4$
b) $5.138 \div 2$
c) $3.045 \div 5$
d) $0.948 \div 2$
$4 \mid 3^{3} 8^{2} 9^{1} 6$
0.974
$2 \frac{5^{1} 113^{18}}{2.569}$
$5 \lcm{3^{3} 0445}$
0.609
209148
0.474
e) $0.924 \div 3$
fi) $7.896 \div 4$
g) $1.268 \div 2$
h) $3.762 \div 6$
$31092^{2} 4$
0.308
$\frac{4 \frac{7^{3} 8^{2} 9^{1} 6}{1.974}}{1.2}$
211268
0.634
$6 \lcm{3^{3} 7^{1} 6^{4} 2}$
0.627

## Practice

1. Divide.
a) $\frac{55.335}{1.067}$
b) $\frac{46.148}{1.537}$
c) $\frac{70.315}{0.045}$
d) $2 \stackrel{4.738}{2.369}$
e) 30.363
0.121
f) $8 \lcm{81.144} 00.143$
g) $\frac{67.542}{1.257}$
h) $\frac{8177.072}{2.134}$
2. Multiply to check each answer in question 1.
a) 1.067

| $\times \quad 5$ |
| :--- |
| 5.335 |

b) 1.537

| $\times \quad 4$ |
| :--- |
| 6.148 |

c) 0.045
$\begin{array}{r}\times \quad 7 \\ \hline 0.315\end{array}$
d) 2.369

| $\times \quad 2$ |
| :--- |
| 4.738 |

e) 0.121
$\begin{array}{r}\times \quad 3 \\ \hline 0.363\end{array}$
f) 0.143
$\begin{array}{r}0.8 \\ \hline 1.144\end{array}$
g) 1.257
$\begin{array}{r}\times \quad 6 \\ \hline 7.542\end{array}$
h) 2.134
$\begin{array}{r}\times \quad 8 \\ \hline 17.072\end{array}$
3. Renee paid $\$ 12.96$ for 6 bags of chips.

- How much did each bag cost? \$2.16

4. Asmaa paid $\$ 9.96$ for 3 pairs of socks.

Jagdeep paid $\$ 14.75$ for 5 pairs of socks.
Which person got the better deal? Explain.
$\$ 9.96 \div 3=\$ 3.32 \quad \$ 14.75 \div 5=\$ 2.95$
Jagdeep got the better deal because he paid less per pair.

## Stretch Your Thinking

What whole number would you divide 2.049 by to get the quotient 0.683 ? $\qquad$

## UNIT

## Dividing Decimals

## Quick Review

- Divide: $9.784 \div 5$

Estimate first: Round 9.784 to 10 .
$10 \div 5=2$
So, $9.784 \div 5$ is a little less than 2 . Divide: $5 \longdiv { 9 . 4 7 2 8 3 4 4 0 }$ 1.9568

Sometimes you need to write zeros in the dividend so you can continue to divide until the remainder is 0 .

Round the quotient to the nearest thousandth: $9.784 \div 5$ is about 1.957 .

- Divide: $25 \div 3$

Estimate first: Round 25 to 24.
$24 \div 3=8$
So, $25 \div 3$ is a little more than 8 .
Divide:
$3 \underline{25.0^{1} 0^{1010}}$
8.3333


Sometimes you never get a remainder of zero.


This is called a repeating decimal.

Round the quotient to the nearest tenth: $25 \div 3$ is about 8.3.

## Try These

1. Divide until the remainder is zero.
a) $\frac{46.374}{1.5935}$
b) $\frac{249.67}{24.835}$
c) 500.473
d) $\begin{array}{r}2 \lcm{29.77} \\ 14.885\end{array}$
e) $5 \lcm{0.573}$
f) $\frac{80.124}{0.0155}$

## Practice

1. Divide until the remainder is zero.
a) $\frac{64.275}{0.7125}$
b) $\frac{845}{5.625}$
c) $\frac{5234}{46.8}$
d) 2000007
e) 20.5
fi) $\frac{427}{6.75}$
2. Use a calculator to divide. Round each quotient to the nearest hundredth.
a) $4 \div 11$
b) $5 \div 8$
c) $30 \div 11$
d) $6 \div 7$
0.36
0.63
2.73
0.86
3. Four students buy a box of popsicles for $\$ 4.29$ and a bag of pretzels for $\$ 3.97$. How much should each person contribute to the total cost?
$\$ 4.29+\$ 3.97=\$ 8.26 \quad \$ 8.26 \div 4=\$ 2.065$
Each person should contribute $\$ 2.07$. There will be $2 ¢ l$ left over.
4. Nataliya jogged 1.367 km in 6 min .

About how far did she jog each minute?
Give your answer in as many different units as you can.
She jogged about 0.228 km each minute.
$0.228 \mathrm{~km}, 228 \mathrm{~m}, 2280 \mathrm{dm}, 22800 \mathrm{~cm}, 228000 \mathrm{~mm}$
5. Twelve friends shared 8 small pizzas equally.

How many pizzas did each person get?
$8 \div 12=0.666 \quad$ Each person gets about 0.67 pizza.

## Stretch Your Thinking

Sample Answers

1. a) Write a story problem you can solve by dividing 11 by 7.

Seven friends decide to share the cost of an \$11 cake equally.
How much will each friend have to pay?
b) Solve your problem.
$\$ 11 \div 7=\$ 1.571$
Each friend will have to pay $\$ 1.58$. There will be 6 c left over.

