THE ORIFICE PLATE DISCHARGE COEFFICIENT EQUATION -THE EQUATION FOR ISO 5167-1

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SUMMARY

This report describes the final work undertaken to achieve the equation which is being balloted in ISO/TC 30/SC 2 for inclusion in ISO 5167-1. It is described as the Agreed Equation since it has the support of the ISO/TC 28 delegation. It includes a description of the work done to check that a change in the expansibility equation would not have a significant effect on discharge coefficient equations fitted to the database.

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NOTATION

A	Function of orifice Reynolds number (see equation (3))
С	Orifice discharge coefficient
C _c	Orifice discharge coefficient using corner tappings
C _s	Dependence of C_c on Reynolds number
C_{∞}	C_c for infinite Reynolds number for $D \ge 71.12 \text{ mm} (2.8 \text{ inch})$
C_{Σ}	$C_{\infty} + C_s + \Delta C_D$
ΔC_D	Small pipe diameter term
$\Delta C_{\rm down}$	Downstream tapping term
ΔC_{up}	Upstream tapping term
D	Pipe diameter
ď	Orifice diameter
L_1	Quotient of the distance of the upstream tapping from the upstream face of the plate and the pipe diameter
<i>L</i> ₂ '	Quotient of the distance of the downstream tapping from the downstream face of the plate and the pipe diameter
<i>M</i> ₂ '	Quotient of the distance of the downstream tapping from the downstream face of the plate and the dam height (as in equation (3))
Re _D	Pipe Reynolds number
S	Standard deviation of the data in the database about an equation
β	Diameter ratio
ε _l	Expansibility referred to upstream conditions

1 INTRODUCTION

Although the orifice plate is the recognized flowmeter for the measurement of natural gas and light hydrocarbon liquids, the orifice discharge coefficient equation in use in the international standard ISO 5167-1: 1991⁽¹⁾ is based on data collected more than 50 years ago. Moreover, for many years the United States and Europe have used different equations, a discrepancy with serious consequences for the oil and gas industry since many companies are multinational. Europe uses the Stolz Equation in ISO 5167-1: 1991 which was previously in ISO 5167: 1980. The United States used the Buckingham Equation⁽²⁾ until the Reader-Harris/Gallagher (RG) Equation (see Reference 3 and below) was adopted in 1990.

The Buckingham equation is based on the data collected by Beitler in the early 1930s at the Ohio State University Engineering Experimental Station⁽⁴⁾. Stolz⁽⁵⁾ used 303 points from the Ohio State University data together with a table of flow coefficients from ISO/R 541⁽⁶⁾. The ISO/R 541 table was established by the German VDI and is based on original data of Witte which are no longer available.

To resolve discrepancies between equations data on orifice plate discharge coefficients were collected in Europe and the United States over more than ten years in order to provide a new database from which an improved discharge coefficient equation could be obtained which would receive international acceptance.

In November 1988 a joint meeting of API (American Petroleum Institute) and EEC flow measurement experts in New Orleans accepted an equation derived by NEL⁽⁷⁾. At that time the database contained 11 346 points, collected in pipes whose diameters ranged from 50 to 250 mm (2 to 10 inch); 600 mm (24 inch) data were being collected but had not yet been included in the database. 600 mm data have since been collected in gas and in water and extend the database both in pipe diameter and in Reynolds number.

The data which were least well fitted by the equation presented at New Orleans were the 50 mm data, and following the meeting the American standard API 2530 was revised to include the Reader-Harris/Gallagher (RG) Equation based on the NEL equation accepted at New Orleans with an additional term proposed by Gallagher for pipes whose diameter lies below 71.12 mm (2.8 inch). Since there was no physical explanation for the additional term for small pipe diameter, additional data were collected in 50 mm pipe in water and oil and included in the database. Measurements by NEL of the edge radius of the plates used in European tests showed that orifices whose diameter is less than 50 mm tend to have edge radii outside those permitted by ISO 5167-1. An equation was therefore derived which included an additional term for small orifice diameter rather than one for small pipe diameter, and it was put forward in a report to EC BCR numbered PR14⁽⁸⁾. It is also described in papers at the North Sea Flow Measurement Workshop in 1992⁽⁹⁾ and in Flow Measurement and Instrumentation⁽¹⁰⁾.

However, neither this equation nor the attempt at compromise put forward at a meeting of ISO/TC 30 in Paris in 1993 were acceptable to the ISO/TC 28 delegation. It was considered by the ISO/TC 28 delegation that the PR14 Equation gave an insufficiently good fit to the data collected in 75 mm (3-inch) pipes, and their need was for an equation which was of the same form as the RG Equation in API MPMS 14.3: $1990^{(3)}$ for $Re_D \ge 4000$; only the

constants and exponents might be changed to give the best fit to the final database. Moreover, measurements by SwRI of the orifice edge radius for the orifice plates used in 50 mm pipe were smaller than those made by NEL. Since one of the principal objectives of the last fourteen years of work was to obtain a common equation for use worldwide, an equation of the form of the RG Equation has been derived and is presented here. It is being ballotted in ISO/TC 30/SC 2 for inclusion in ISO 5167-1. It is described here as the Agreed Equation since it has the support of the ISO/TC 28 Delegation. Given the definition that s is the standard deviation of the data in the database about an equation, the value of s for the Agreed Equation is very similar to the value of s for the PR14 Equation.

2 THE DATABASE

In addition to the database used for deriving the PR14 orifice plate discharge coefficient equation in 1992 an additional 146 points have been added: these are from SwRI, Texas⁽¹¹⁾; their inclusion makes essentially no difference to the final fitted equation.

3 THE AGREED EQUATION

As stated in the Introduction the Agreed Equation had to be of the same form as that of the RG Equation for $Re_D \ge 4000$ with only the constants and exponents changed.

3.1 The Tapping Terms

The form of the upstream and downstream tapping terms, ΔC_{up} and ΔC_{down} , in the RG equation (and also in the NEL equation for New Orleans described in Reference 7) is as follows:

$$\Delta C_{up} = (c_1 + c_2 e^{-f_1 L_1} - (c_1 + c_2) e^{-f_2 L_1})(1 - c_3 A) \frac{\beta^4}{1 - \beta^4}$$
(1)

and

$$\Delta C_{\text{down}} = c_4 (M_2 - c_5 M_2^{f_3}) (1 - c_6 A) \beta^{f_4}$$
⁽²⁾

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where

$$A = \left(\frac{19000\beta}{Re_{D}}\right)^{0.8} \text{ and } M_{2} = \frac{2L_{2}}{1-\beta}.$$
 (3)

For high Reynolds numbers the tapping terms are identical in form to those obtained in deriving the PR14 Equation based on the enlarged database. Therefore, the coefficients c_1 , c_2 , c_4 , and c_5 and the exponents f_i (*i*=1,4), in the tapping terms for high Reynolds number are taken to be the same as those in the PR14 Equation⁽⁸⁻¹⁰⁾, except that it was found that the overall fit to the database was improved by making $c_2 = 0.08$ instead of 0.09. (The upstream tapping term for high Reynolds number is plotted in Figure 1 on the same basis as in References 8, 9 and 10.) Moreover, when the tapping terms for lower Reynolds numbers for the PR14 Equation were derived it was found that the dependence of the sum of the tapping

terms on Re_D for $Re_D \ge 4000$ could be expressed by making ΔC_{up} alone a function of Re_D . When determining the values of c_3 and c_6 to give the best fit of the form of the complete Agreed Equation to the database it was found that to permit a non-zero value of c_6 gives a negligible reduction in the standard deviation of the data about the equation. With $c_6 = 0$ the best-fit value of c_3 was 0.11. So that a good fit for the complete database (including data for $Re_D < 4000$) should still be obtained it is necessary to include an additional term in ΔC_{down} for $Re_D \le 3700$ identical to that in the PR14 Equation. Therefore, the final tapping terms are given by

$$\Delta C_{up} = (0.043 + 0.080e^{-10L_1} - 0.123e^{-7L_1})(1 - 0.11A)\frac{\beta^4}{1 - \beta^4}$$
(4)

and

$$\Delta C_{\text{down}} = -0.031 (M_2' - 0.8 M_2^{1.1}) \{1 + 8 \max(\log_{10}(3700 / Re_D), 0.0)\} \beta^{1.3}$$
(5)

3.2 The Small Pipe Diameter Term

Instead of a small orifice diameter term the RG Equation uses a small pipe diameter term, ΔC_D , of the following form:

$$\Delta C_{D} = h_{1}(h_{2} - \beta) \max(h_{3} - D/25.4, 0.0). \quad (D : mm)$$
(6)

The form of this term has no known physical basis (although the requirement for the term may be due to the edge radius of the orifice plates used in the 50 mm pipes), but the term gives a good fit to the database: C was larger in 50 mm pipes than in larger pipes even with corner and D and D/2 tappings. Since there are essentially only discrete values of D in the database h_3 cannot be determined: following the RG Equation the value of h_3 was taken to be 2.8 inch (71.12 mm), 0.1 inch (2.54 mm) smaller than the internal diameter for 3-inch schedule 80 pipe. The quality of fit to the complete database improves as h_2 reduces to 0.75, the smallest value which ensures that this term does not become negative over the permissible range of use. If $(h_2 - \beta)$ were replaced by max $(h_2 - \beta, 0)$ then the best fit is obtained with h_2 equal to 0.7, but the improvement in fit is very small and the equation significantly different from the RG Equation and also more complicated. With $h_2 = 0.75 h_1$ was determined by fitting the complete database and is equal to 0.011. Therefore, the small pipe diameter term is given by

$$\Delta C_{D} = 0.011(0.75 - \beta) \max(2.8 - D/25.4, 0.0). \quad (D : mm)$$
(7)

3.3 The C_ and Slope Terms

The C_{-} and slope terms are of exactly the same form in the RG and in the PR14 Equations and so in the Agreed Equation are of the following form:

$$C_{\infty} + C_{s} = a_{1} + a_{2}\beta^{m_{1}} + a_{3}\beta^{m_{2}} + b_{1}(10^{6}\beta / Re_{D})^{n_{1}} + (b_{2} + b_{3}A)\beta^{\ell} \max\{(10^{6} / Re_{D})^{n_{2}}, g_{1} - g_{2}(Re_{D} / 10^{6})\}$$
(8)

The exponents used for the PR14 Equation were used for the final equation with the exception that m_1 was taken to be 2 since this value is used in the RG Equation and gives a better fit to the complete database. With m_1 , m_2 , l, n_1 and n_2 given by 2, 8, 3.5, 0.7 and 0.3, respectively, the tapping terms given in equations (4) and (5) and the small pipe diameter term given in equation (7) the optimum values of the constants in equation (8) were determined and the following equation obtained:

$$C_{\infty} + C_{s} = 0.5961 + 0.0261\beta^{2} - 0.216\beta^{8} + 0.000521(10^{6}\beta / Re_{D})^{0.7}$$

$$+ (0.0188 + 0.0063A)\beta^{3.5} \max\{(10^{6} / Re_{D})^{0.3}, 22.7 - 4700(Re_{D} / 10^{6})\}$$
(9)

3.4 The Complete Equation

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Therefore, the complete orifice plate discharge coefficient equation is as follows:

$$C = 0.5961 + 0.0261\beta^{2} - 0.216\beta^{8} + 0.000521(10^{6}\beta / Re_{D})^{0.7} + (0.0188 + 0.0063A)\beta^{3.5} \max\{(10^{6} / Re_{D})^{0.3}, 22.7 - 4700(Re_{D} / 10^{6})\} + (0.043 + 0.080e^{-10L_{1}} - 0.123e^{-7L_{1}})(1 - 0.11A)\frac{\beta^{4}}{1 - \beta^{4}}$$
(10)
$$-0.031(M_{2}' - 0.8M_{2}'^{1.1})\{1 + 8\max(\log_{10}(3700 / Re_{D}), 0.0)\}\beta^{1.3} + 0.011(0.75 - \beta)\max(2.8 - D / 25.4, 0.0). \qquad (D : mm)$$

For $Re_D \ge 4000$ this equation can be written as follows:

For $D \ge 71.12 \text{ mm} (2.8 \text{ inch})$

$$C = 0.5961 + 0.0261\beta^{2} - 0.216\beta^{8} + 0.000521(10^{6}\beta / Re_{D})^{0.7} + (0.0188 + 0.0063A)\beta^{3.5}(10^{6} / Re_{D})^{0.3} + (0.043 + 0.080e^{-10L_{1}} - 0.123e^{-7L_{1}})(1 - 0.11A)\frac{\beta^{4}}{1 - \beta^{4}}$$
(11a)
$$-0.031(M_{2} - 0.8M_{2}^{(1.1)})\beta^{1.3}.$$

Where D < 71.12 mm (2.8 inch) the following term should be added to equation (11a):

$$+0.011(0.75 - \beta)\left(2.8 - \frac{D}{25.4}\right).$$
 (D : mm) (11b)

Equation (11), comprising equation (11a) with the additional term (11b), is the Agreed Equation.

The notation of ISO 5167-1 has been used with the following additions:

$$A = \left(\frac{19000\beta}{Re_D}\right)^{0.8}$$
 and $M_2' = \frac{2L_2'}{1-\beta}$.

4 QUALITY OF FIT

The quality of the fit of equation (10) to the database is very good: the overall standard deviation of the data for $Re_D \ge 4000$ about the equation is 0.259 per cent; the mean deviations of the data about the equation as a function of β , *D*, Re_D and pair of tappings used and of pairs of these independent variables are both small and well-balanced.

The quality of fit is quantified in Tables 1 to 8. Table 1 gives a description of the meaning of the different lines in Tables 2 to 8. These tables give the deviations of the data in the database about the equation as a function of β , *D*, Re_D and pair of tappings used and certain combinations of these. The range of values of β corresponding to each nominal value of β is given in Table 2. The tappings described as Corner (GU) are tappings in the corners which were designed by Gasunie and are simpler to make than those in ISO 5167-1. They are described in Reference 12. The database used is the complete EEC/API database as described except that data with $Re_D < 4000$ were excluded in Tables 5 to 8.

5 COMPARISON BETWEEN EQUATIONS ON THE BASIS OF DEVIATIONS

A direct comparison between equation (11) and the RG and PR14 Equations for $Re_D \ge 4000$ is given here. To do this the data in Table 5 (and similar tables of deviations on the basis of D and β for the other equations) were analysed: the number of boxes (ranges of D and β) over which an equation gave a mean deviation greater than 0.1 per cent was counted and is given in Table 9; the number of boxes for which the mean deviation was greater than 0.2 per cent was also counted and is given in Table 9. A similar count was undertaken for Tables 6 - 8 and the results are also given in Table 9. These figures provide a measure of possible bias in an equation. The standard deviation of the data about each equation is also given as a measure of the quality of fit. The quality of fit for the Agreed Equation is similar to that of the PR14 Equation. They are both better than the RG Equation.

Since the Stolz Equation in ISO 5167-1: 1991 is applicable over a more limited range of values of Re_D and β than the three equations previously considered, the standard deviation and the number of boxes with mean deviations greater than 0.1 or 0.2 per cent are given in Table 10 for all four equations over the range of applicability of the Stolz ISO 5167-1: 1991 Equation. The need for an improved equation even over the limited range of Re_D and β is obvious.

6 THE EFFECT OF THE EXPANSIBILITY EQUATION

Since doubt has been expressed regarding the accuracy of the expansibility equation used for orifice plates in ISO 5167-1¹ (see Kinghorn⁽¹³⁾ and Seidl⁽¹⁴⁾) it has been suggested that the new discharge coefficient equation given in equation (10) and others based on the same database may have been significantly affected by errors in the discharge coefficient data

caused by errors in the expansibility, ε_1 , since the value of ε_1 given in Section 8.3.2.2 of ISO 5167-1: 1991 was used in the computation of discharge coefficient.

In order to test this theory, for each point of the database the value of discharge coefficient which would have been obtained if an alternative equation for ε_1 had been used was calculated and the equation refitted. If the value of discharge coefficient given in the database is termed C_I , based on the expansibility given by the equation in Section 8.3.2.2 of ISO 5167-1: 1991, $\varepsilon_{1,I}$, then C_N , the value of discharge coefficient based on an alternative value of expansibility, $\varepsilon_{1,N}$, is given by

$$C_N \varepsilon_{I,N} = C_I \varepsilon_{I,I}, \qquad (12)$$

where

and

$$\varepsilon_{1,I} = 1 - (0.41 + 0.35\beta^4) \frac{\Delta p}{\kappa p_1}.$$
 (13)

Where the value of $\varepsilon_{1,I}$ is given in the database it is possible to calculate κ using the values of β , Δp and p_1 and then to calculate $\varepsilon_{1,N}$. Where $\varepsilon_{1,I}$ is not given in the database it is necessary, in the first instance, to estimate what value of κ might have been used on the basis of other data; if it were shown to be the case that the discharge coefficient equation fitted to C_N differed significantly from that fitted to C_I it would be necessary to obtain better values for κ .

The only sets of gas data for which $\varepsilon_{1,I}$ was not provided in the database were those from SwRI and Ruhrgas. For SwRI the downstream expansion factor, Y_2 , (see Reference 3) was provided but not $\varepsilon_{1,I}$. So for SwRI and Ruhrgas values for κ of 1.41 and 1.32, respectively, were used: 1.41 is appropriate for nitrogen; 1.32 is a typical value for natural gas.

Three alternative equations for $\varepsilon_{1,N}$ were used: they were as follows:

$$\varepsilon_{1,N,1} = 1 - (0.35 + 0.38\beta^4) \frac{\Delta p}{\kappa p_1},$$
 (14)

$$\varepsilon_{1,N,2} = 1 - (0.352 + 0.433\beta^4) \frac{\Delta p}{\kappa p_1},$$
(15)

$$\varepsilon_{1,N,3} = 1 - (0.357 + 0.557\beta^4) \frac{\Delta p}{\kappa p_1}.$$
 (16)

 $\varepsilon_{1,N,1}$ and $\varepsilon_{1,N,2}$ were taken from equations (9) (rounded as in the conclusions of the paper) and (10) of Kinghorn⁽¹³⁾ and $\varepsilon_{1,N,3}$ was taken from equation (8) (the recommended equation) of Seidl⁽¹⁴⁾.

8

Calculating $C_{N,i}$ on the basis of $\varepsilon_{1,N,i}$ for i=1,3 and using the tapping terms given in equations (4) and (5), the sum of the C_{∞} , C_s and ΔC_D terms, C_{Σ} , was refitted as follows:

$$C_{\Sigma} = C_{\infty} + C_s + \Delta C_D = a_1 + a_2 \beta^2 + a_3 \beta^8 + b_1 (10^6 \beta / Re_D)^{0.7} + (b_2 + b_3 A) \beta^{3.5} \max\{(10^6 / Re_D)^{0.3}, 22.7 - 4700(Re_D / 10^6)\}$$
(17)
+ h(0.75 - \beta) \max(2.8 - D / 25.4, 0.0). (D:mm)

In each case the standard deviation of the data in the database about the equation, s, the number of points which are shifted by more than 0.2 per cent, N_s , and the largest magnitude of shift, S_M , were calculated. The results were as follows:

$$C_{\Sigma,N,1} = 0.59590 + 0.02638\beta^{2} - 0.21794\beta^{8} + 0.0005288(10^{6}\beta / Re_{D})^{0.7} + (0.01904 + 0.005864A)\beta^{3.5} \max\{(10^{6} / Re_{D})^{0.3}, 22.7 - 4700(Re_{D} / 10^{6})\} + 0.01135(0.75 - \beta)\max(2.8 - D / 25.4, 0.0). \quad (D:mm)$$
(18)

 $s_{N,1} = 0.0016775;$ $N_{s,1} = 191;$ $S_{M,3} = 0.98$ per cent.

$$C_{\Sigma,N,2} = 0.59591 + 0.02645\beta^{2} - 0.21778\beta^{8} + 0.0005286(10^{6}\beta / Re_{D})^{0.7} + (0.01895 + 0.005894A)\beta^{35} \max\{(10^{6} / Re_{D})^{0.3}, 22.7 - 4700(Re_{D} / 10^{6})\} + 0.01133(0.75 - \beta)\max(2.8 - D / 25.4, 0.0). \quad (D:mm)$$
(19)

 $s_{N,2} = 0.0016768;$ $N_{s,2} = 177;$ $S_{M,2} = 0.85$ per cent.

$$C_{\Sigma,N,3} = 0.59592 + 0.02662\beta^{2} - 0.21740\beta^{8} + 0.0005281(10^{6}\beta / Re_{D})^{0.7} + (0.01876 + 0.005965A)\beta^{3.5} \max\{(10^{6} / Re_{D})^{0.3}, 22.7 - 4700(Re_{D} / 10^{6})\} + 0.01129(0.75 - \beta)\max(2.8 - D / 25.4, 0.0). \quad (D:mm)$$
(20)

 $s_{N,3} = 0.0016784;$ $N_{s,3} = 139;$ $S_{M,3} = 0.76$ per cent.

Since small differences between equations were being investigated the constants for C_{Σ} with the same number of decimal places as for $C_{\Sigma,N,i}$ are also required where $\varepsilon_{1,I}$ was used:

$$C_{\Sigma,I} = 0.59615 + 0.02609\beta^{2} - 0.21675\beta^{8} + 0.0005216(10^{6}\beta / Re_{D})^{0.7} + (0.01874 + 0.006071A)\beta^{3.5} \max\{(10^{6} / Re_{D})^{0.3}, 22.7 - 4700(Re_{D} / 10^{6})\} + 0.01101(0.75 - \beta)\max(2.8 - D / 25.4, 0.0). \quad (D:mm)$$
(21)

 $s_I = 0.0016747.$

The constants in equations (7) and (9) have been rounded and then rebalanced to ensure that there is no mean deviation between equation and database.

It can be seen that the differences in s and thus in overall quality of fit are very small but that $\varepsilon_{1,l}$ gives the best result. Moreover the coefficients in equations (18) - (21) are very similar. The largest value of S_M for equations (18) - (20) occurs for equation (18); however, even in this case the largest magnitude of difference between the equation and equation (21) is 0.04 per cent for any values of β , D and Re_D except at the very lowest end of the Reynolds number range (below 4000). Therefore the choice of the expansibility equation has very little effect on the discharge coefficient equation and there is no problem in putting equation (11) in ISO 5167-1. However, the choice of expansibility equation has a significant effect both on some individual data points in the database and when it is used in the field, and it is important that the best equation is obtained.

CONCLUSIONS

The derivation of the Agreed discharge coefficient equation which is being ballotted in ISO/TC 30/SC 2 for inclusion in ISO 5167-1 has been described; it has been shown that possible changes to the expansibility equation would have only a small effect on the discharge coefficient equation. Deviations of the data in the database from the Agreed equation have been tabulated and a comparison made with deviations from the PR14, RG and Stolz ISO 5167-1: 1991 equations.

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1 Upstream tapping term as a function of L_1 .

GENERAL INFORMATION ABOUT THE ANALYSIS OF DEVIATIONS IN TABLES 2 TO 8

For each cell, line 1 - Mean per cent error

line 2 - Per cent standard deviation

line 4 - Number of observations

line 5 - Per cent standard deviation about equation.

For the ith point in a cell Per cent error, $P_i = \frac{(C_{im} - C_{ie})}{C_{im}} \times 100$,

where C_{im} is the measured discharge coefficient of the ith point, and

 C_{ie} is the corresponding discharge coefficient from the equation.

Mean per cent error,
$$m = \frac{\sum_{i=1}^{N} P_i}{N}$$
,

where N is the number of points in the cell.

Per cent standard deviation =
$$\sqrt{\frac{\sum_{i=1}^{N} (P_i - m)^2}{N - 1}}$$

Per cent standard deviation about equation = $\sqrt{\frac{\sum_{i=1}^{N} P_i^2}{N}}$.

Statistics for the entire population appear in the bottom right hand cell.

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RESIDUALS FROM EQUATION (10) AS A FUNCTION OF β and D

D(mm)	50	75	100	150	250	600	Summary
							by
β							β
	0.000	0.000	0.000	0.157	-0.004	0.000	0.078
0.100	0.000	0.000	0.000	0.238	0.269	0.000	0.265
(0.0991 to	-	-	-	-	-	-	-
0.1028)	0	0	0	81	79	0	160
	0.000	0.000	0.000	0.284	0.268	0.000	0.276
	0.012	-0.047	0.079	0.088	-0.170	0.028	-0.019
0.200	0.467	0.124	0.228	0.107	0.187	0.239	0.300
(0.1982 to	-	-	-	-	-	-	-
0.2418)	507	57	652	111	714	394	2435
	0.467	0.131	0.241	0.138	0.253	0.240	0.300
	0.073	-0.003	0.088	0.138	-0.106	0.037	0.031
0.375	0.296	0.097	0.255	0.261	0.159	0.113	0.225
(0.3620 to	-	-	-	-	-	-	-
0.3748)	444	106	469	133	439	591	2182
	0.304	0.097	0.269	0.295	0.191	0.119	0.227
	-0.030	0.138	0.135	0.098	0.033	-0.063	0.016
0.500	0.296	0.054	0.190	0.103	0.164	0.118	0.205
(0.4825 to	-	-	-	-	-	-	•
0.5003)	398	69	300	109	392	526	1794
	0.297	0.148	0.233	0.142	0.168	0.134	0.205
	-0.109	0.095	0.028	0.009	0.074	-0.090	0.009
0.570	0.393	0.076	0.233	0.143	0.260	0.117	0.255
(0.5427 to	-	-	-	-	-	-	-
0.5770)	348	72	1008	136	1123	567	3254
	0.408	0.121	0.235	0.143	0.270	0.148	0.255
1	-0.088	0.101	-0.018	-0.097	0.050	-0.136	-0.038
0.660	0.305	0.100	0.245	0.204	0.197	0.143	0.233
(0.6481 to	-	-	-	•	-	-	-
0.6646)	498	64	642	92	823	643	2762
	0.318	0.142	0.246	0.225	0.204	0.197	0.230
	-0.051	0.092	0.120	0.107	-0.024	-0.251	-0.004
0.750	0.342	0.106	0.322	0.333	0.321	0.338	0.340
(0.7239 to	•		-	-	-	-	2025
0.7509)	866		1024	130	14/8	020	0 240
	0.345	0.140	0.344	0.349	0.322	0.421	0.340
	-0.032	0.062	0.067	0.073	-0.013	-0.073	0.002
Summary	0.359	0.113	0.264	0.229	0.202	0.199	0.274
by	-	-	-	700	5049	3057	16522
D	3061	469	4095	192	0 248	0212	0.274
1	0.361	0.129	0.272	0.240	0.202	0.212	0.274

RESIDUALS FROM EQUATION (10) AS A FUNCTION OF D AND PAIR OF TAPPINGS

Tappings	Corner	Flange	D&D/2	Corner	Summary
	(ISO)			(GU)	by
D (mm)					D
	0.008	-0.037	-0.063	0.000	-0.032
	0.411	0.314	0.393	0.000	0.359
50	-	-	-	-	-
1	728	1605	728	0	3061
	0.411	0.316	0.398	0.000	0.361
	0.000	0.062	0.000	0.000	0.062
	0.000	0.113	0.000	0.000	0.113
75	-	-	-	-	-
	0	469	0	0	469
	0.000	0.129	0.000	0.000	0.129
	0.040	0.064	0.104	0.000	0.067
	0.224	0.257	0.313	0.000	0.264
100	-	-	-	-	-
	1084	2078	933	0	4095
ъ <u>ц</u>	0.228	0.265	0.330	0.000	0.272
	0.000	0.073	0.000	0.000	0.073
	0.000	0.229	0.000	0.000	0.229
150	-	-	-	-	-
	0	792	0	0	792
	0.000	0.240	0.000	0.000	0.240
	0.026	-0.068	-0.009	0.044	-0.013
	0.249	0.212	0.280	0.320	0.262
250	-	-	-	-	-
	1155	1841	11 67	885	5048
	0.250	0.223	0.280	0.322	0.262
· ··-	-0.156	0.003	-0.066	-0.097	-0.073
	0.199	0.160	0.200	0.209	0.199
600	-	-	-	-	-
	828	876	1130	223	3057
	0.253	0.160	0.211	0.230	0.212
	-0.013	0.005	-0.009	0.016	-0.002
Summary	0.283	0.248	0.301	0.306	0.274
by	-	-	-	-	-
Tappings	3795	7661	3958	1108	16522
	0.283	0.249	0.301	0.306	0.274

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RESIDUALS FROM EQUATION (10) AS A FUNCTION OF β and Re_D

Ren	10	4000	104	105	10°	107	Summary
	to	to	to	to	to	to	by
β	4000	10 ⁴	10 ⁵	10 ⁶	10 ⁷	10 ⁸	β
	0.095	0.108	0.037	0.000	0.000	0.000	0.078
	0.189	0.282	0.305	0.000	0.000	0.000	0.265
0.100	-	-	-	-	-	-	-
	52	49	59	0	0	0	160
	0.211	0.299	0.305	0.000	0.000	0.000	0.276
	-0.027	0.047	-0.050	-0.051	0.102	0.000	-0.019
	0.556	0.354	0.249	0.240	0.170	0.000	0.300
0.200	-	-	-	-	-	-	-
	237	238	1190	454	316	0	2435
	0.556	0.357	0.254	0.245	0.198	0.000	0.300
	0.376	0.125	0.008	-0.041	0.049	0.082	0.031
	0.509	0.322	0.175	0.157	0.084	0.083	0.225
0.375	-	-	-	-	-	-	-
	125	133	748	711	325	140	2182
	0.631	0.344	0.175	0.162	0.097	0.116	0.227
	-0.057	-0.093	0.034	0.071	-0.090	-0.057	0.016
	0.760	0.281	0.195	0.163	0.134	0.085	0.205
0.500	-	-	-	-	-	-	-
	33	83	436	788	205	249	1794
	0.750	0.294	0.198	0.177	0.162	0.102	0.205
	-0.546	-0.334	-0.040	0.002	0.083	0.028	0.009
	0.968	0.459	0.241	0.195	0.273	0.224	0.255
0.570	-	-	-	-	-	-	-
	18	59	502	1430	/82	463	3254
	1.087	0.564	0.244	0.195	0.285	0.226	0.255
	-0.087	-0.325	-0.110	0.012	0.025	-0.100	-0.038
	0.116	0.522	0.307	0.203	0.193	0.177	0.233
0.660	-	-	-	-	-	-	-
	5	35	466	0.204	4/5	000	0.736
	0.135	0.609	0.326	0.204	0.194	0.203	0.230
	0.000	0.242	-0.073	0.038	0.029	-0.055	-0.004
0.750	0.000	0.514	0.404	0.303	0.315	0.333	0.340
0.750	-		-	1704	1062	176	3035
	0,000	/8	015	0.305	0.316	0.350	0.340
	0.000	0.303	0.410	0.303	0.024	-0.041	-0.002
C	0.0/1	0.019	-0.038	0.013	0.024	0.041	0.274
Summary	0.389	0.411	0.275	0.230	0.255	0.237	
by Ba	- 470	675	4016	6208	3165	1988	16522
Re _D	0.503	0/5	0.276	0.231	0.257	0.242	0.274
	0.555	0.711	0.210				<u></u>

RESIDUALS FROM EQUATION (10) AS A FUNCTION OF β and D ($Re_D \ge 4000$)

D (mm)	50	75	100	150	250	600	Summary
							by
β							β
	0.000	0.000	0.000	0.267	-0.004	0.000	0.069
0.100	0.000	0.000	0.000	0.277	0.269	0.000	0.296
(0.0991 to	-	-	-	-	-	-	-
0.1028)	0	0	0	29	79	0	108
	0.000	0.000	0.000	0.381	0.268	0.000	0.302
	0.052	-0.047	0.079	0.095	-0.170	0.028	-0.018
0.200	0.341	0.124	0.232	0.079	0.187	0.239	0.258
(0.1982 to	-	-	-	-	-	-	-
0.2418)	324	57	626	83	714	394	2198
	0.345	0.131	0.244	0.123	0.253	0.240	0.258
	0.022	-0.003	0.061	0.081	-0.106	0.037	0.010
0.375	0.190	0.097	0.200	0.175	0.159	0.113	0.174
(0.3620 to	-	-	-	-	-	-	-
0.3748)	344	106	455	122	439	591	2057
	0.191	0.097	0.209	0.192	0.191	0.119	0.174
	-0.028	0.138	0.135	0.098	0.033	-0.063	0.017
0.500	0.211	0.054	0.190	0.103	0.164	0.118	0.179
(0.4825 to	-	-	-	-	-	-	-
0.5003)	365	69	300	109	392	526	1761
	0.213	0.148	0.233	0.142	0.168	0.134	0.180
	-0.086	0.095	0.028	0.009	0.074	-0.090	0.012
0.570	0.322	0.076	0.233	0.143	0.260	0.117	0.242
(0.5427 to	-	-	-	-	-	-	-
0.5770)	330	72	1008	136	1123	567	3236
	0.333	0.121	0.235	0.143	0.270	0.148	0.243
	-0.088	0.101	-0.018	-0.097	0.050	-0.136	-0.038
0.660	0.307	0.100	0.245	0.204	0.197	0.143	0.233
(0.6481 to	-	-	-	-	-	-	-
0.6646)	493	64	642	92	823	643	2757
	0.319	0.142	0.246	0.225	0.204	0.197	0.236
	-0.051	0.092	0.120	0.107	-0.024	-0.251	-0.004
0.750	0.342	0.106	0.322	0.333	0.321	0.338	0.340
(0.7239 to	-	-	-	-	-	-	-
0.7509)	866	101	1024	130	1478	336	3935
	0.345	0.140	0.344	0.349	0.322	0.421	0.340
	-0.037	0.062	0.064	0.061	-0.013	-0.073	-0.004
Summary	0.305	0.113	0.259	0.217	0.262	0.199	0.259
by	-	-	-	-	-	-	-
D	2722	469	4055	701	5048	3057	16052
ļ	0.308	0.129	0.267	0.225	0.262	0.212	0.259

RESIDUALS FROM EQUATION (10) AS A FUNCTION OF β AND Re_{D} ($Re_{D} \ge 4000$)

Ren	10	4000	104	103	10°	107	Summary
D	to	to	to	to	to	to	by
β	4000	10 ⁴	10 ⁵	10 ⁶	10 ⁷	108	β
	0.000	0.108	0.037	0.000	0.000	0.000	0.069
	0.000	0.282	0.305	0.000	0.000	0.000	0.296
0.100	-	-	-	-	-	-	-
	0	49	59	0	0	0	108
	0.000	0.299	0.305	0.000	0.000	0.000	0.302
	0.000	0.047	-0.050	-0.051	0.102	0.000	-0.018
	0.000	0.354	0.249	0.240	0.170	0.000	0.258
0.200	-	-	-	-	-	-	-
	0	238	11 90	454	316	0	2198
	0.000	0.357	0.254	0.245	0.198	0.000	0.258
	0.000	0.125	0.008	-0.041	0.049	0.082	0.010
	0.000	0.322	0.175	0.157	0.084	0.083	0.174
0.375	-	1	-	-	-	-	-
	0	133	748	711	325	140	2057
	0.000	0.344	0.175	0.162	0.097	0.116	0.174
	0.000	-0.093	0.034	0.071	-0.090	-0.057	0.017
	0.000	0.281	0.195	0.163	0.134	0.085	0.179
0.500	-	-	-	-	-	-	-
	0	83	436	788	205	249	1761
	0.000	0.294	0.198	0.177	0.162	0.102	0.180
	0.000	-0.334	-0.040	0.002	0.083	0.028	0.012
	0.000	0.459	0.241	0.195	0.273	0.224	0.242
0.570	-	-	-	-	-	-	-
	0	59	502	1430	782	463	3236
	0.000	0.564	0.244	0.195	0.285	0.226	0.243
	0.000	-0.325	-0.110	0.012	0.025	-0.100	-0.038
	0.000	0.522	0.307	0.203	0.193	0.177	0.233
0.660	-	-	-	-	-	-	-
	0	35	466	1121	475	660	2/5/
	0.000	0.609	0.326	0.204	0.194	0.203	0.236
	0.000	0.242	-0.073	0.038	-0.029	-0.053	-0.004
	0.000	0.514	0.404	0.303	0.315	0.355	0.340
0.750	-	-	-	-	-	476	2025
	0	78	615	1/04	1062	4/0	0240
	0.000	0.565	0.410	0.305	0.310	0.339	0.340
	0.000	0.019	-0.038	0.013	0.024	-0.041	-0.004
Summary	0.000	0.411	0.273	0.230	0.255	0.239	0.239
by	-	-	-	(200	-	1000	16052
Re _D		6/5	4016	0208	3103	1700	0.250
	0.000	0.411	0.276	0.231	0.257	0.242	0.239

DEVIATIONS FROM EQUATION (10) AS A FUNCTION OF D AND Re_D ($Re_D \ge 4000$)

Rep	10	4000	104	103	106	10'	Summary
Ľ	to	to	to	to	to	to	by
<i>D</i> (mm)	4000	10 ⁴	10 ⁵	10 ⁶	10 ⁷	10 ⁸	D
	0.000	-0.031	-0.082	0.095	0.000	0.000	-0.037
	0.000	0.467	0.278	0.178	0.000	0.000	0.305
50	-	-	-	-	-	-	-
	0	403	1749	570	0	0	2722
	0.000	0.467	0.289	0.202	0.000	0.000	0.308
	0.000	-0.047	0.046	0.086	0.000	0.000	0.062
	0.000	0.137	0.119	0.097	0.000	0.000	0.113
75	-	-	-	-	-	-	-
	0	22	209	238	0	0	469
	0.000	0.141	0.127	0.129	0.000	0.000	0.129
	0.000	0.149	0.041	0.057	0.114	0.000	0.064
	0.000	0.252	0.271	0.259	0.228	0.000	0.259
100	-	-	-	-	-	-	-
	0	134	1111	2276	534	0	4055
	0.000	0.292	0.274	0.265	0.255	0.000	0.267
	0.000	0.225	0.149	-0.031	-0.119	0.000	0.061
	0.000	0.226	0.244	0.125	0.095	0.000	0.217
150	-	-	-	-	-	-	-
	0	68	275	328	30	0.	701
	0.000	0.317	0.286	0.129	0.151	0.000	0.225
	0.000	-0.175	-0.153	-0.032	0.011	0.194	-0.013
	0.000	0.360	0.212	0.222	0.296	0.231	0.262
250	-	-	-	-	-	-	-
	0	48	646	2348	1490	516	5048
	0.000	0.397	0.261	0.225	0.296	0.301	0.262
	0.000	0.000	-0.323	-0.078	0.002	-0.123	-0.073
	0.000	0.000	0.336	0.194	0.196	0.179	0.199
600	-	-	•	-	-	-	-
	0	0	26	448		1472	3057
	0.000	0.000	0.461	0.209	0.196	0.218	0.212
	0.000	0.019	-0.038	0.013	0.024	-0.041	-0.004
Summary	0.000	0.411	0.273	0.230	0.255	0.239	0.259
by	-	-	-	-	-	-	-
Re _D	0	675	4016	6208	3165	1988	16052
	0.000	0.411	0.276	0.231	0.257	0.242	0.259

DEVIATIONS FROM EQUATION (10) AS A FUNCTION OF β AND PAIR OF TAPPINGS ($Re_D \ge 4000$)

Tappings	Corner	Flange	D&D/2	Corner	Summary
	(ISO)	U		(GU)	by
β	, í				β
	0.000	0.069	0.000	0.000	0.069
	0.000	0.296	0.000	0.000	0.296
0.100	-	_	-	-	-
	o i	108	0	0	108
	0.000	0.302	0.000	0.000	0.302
	0.018	-0.034	-0.002	-0.098	-0.018
	0.274	0.233	0.272	0.259	0.258
0.200	-	-	-	-	-
	537	925	582	154	2198
	0.275	0.235	0.272	0.276	0.258
	-0.006	0.026	0.006	-0.072	0.010
	0.175	0.178	0.155	0.170	0.174
0.375	-	-	-	-	-
	382	1101	466	108	2057
	0.175	0.180	0.155	0.184	0.174
	0.012	0.020	0.029	-0.037	0.017
	0.242	0.154	0.160	0.178	0.179
0.500	-	-	-	-	-
	369	884	403	105	1761
	0.241	0.155	0.163	0.181	0.180
	-0.002	-0.035	0.084	0.080	0.012
	0.231	0.197	0.274	0.314	0.242
0.570	-	-	-	-	-
	794	1366	845	231	3236
	0.231	0.200	0.286	0.323	0.243
	-0.068	-0.045	0.006	-0.040	-0.038
	0.231	0.215	0.256	0.244	-0.233
0.660	-	-	-	-	-
	671	1200	690	196	2757
	0.241	0.220	0.256	0.246	0.236
	-0.026	0.060	-0.147	0.106	-0.004
	0.324	0.290	0.381	0.381	0.340
0.750	-	-	-	-	-
	963	1765	893	314	3935
	0.325	0.296	0.408	0.395	0.340
	-0.017	0.004	-0.011	0.016	-0.004
Summary	0.262	0.229	0.291	0.306	0.259
by	•	-	-	-	-
Tappings	3716	7349	3879	1108	16052
	0.263	0.229	0.291	0.306	0.259

	AGREED EQUATION (11)		PR14 EQUATION		RG EQUATION	
	N	N_2	N ₁	N		$\overline{N_2}$
βvD	10	2	14	2	18	6
$\beta v Re_D$	8	3	6	5	14	6
$D v Re_D$	10	2	7	2	12	2
β v Tappings	2	0 -	2	0	6	1
TOTAL	30	7	29	9	50	15
s (per cent)	0.2	59	0.3	254	0.2	292

ANALYSIS OF DEVIATIONS FOR THE DATABASE ($Re_D \ge 4000$)

TABLE 10

ANALYSIS OF DEVIATIONS FOR THE DATABASE OVER THE RANGE OF THE STOLZ ISO 5167-1:1991 EQUATION ($Re_D \ge 4000$)

	AGR	EED	PR14 EQ	UATION	R	RG		STOLZ	
	EQUAT	ION (11)			EQUATION		ISO 516	7-1:1991	
	Ĩ							TION	
	N_1	N_2	N ₁	N ₂	N_1	N_2	N_1	N_2	
βvD	8	1	15	2	17	6	26	16	
$\beta v Re_D$	4	0	3	1	10	4	16	12	
$D \vee Re_D$	7	2	10	3	10	3	16	10	
β v Tappings	2	0	2	0	5	0	13	7	
TOTAL	21	3	30	6	42	13	71	45	
s (per cent)	0.2	245	0.2	247	0.277		0.3	390	

DEFINITIONS FOR TABLES 9 AND 10:

 N_1 is the number of boxes with the mean deviation greater than 0.1 per cent.

 N_2 is the number of boxes with the mean deviation greater than 0.2 per cent.

s is the standard deviation of the data in the database about the equation.

