

#### Warm Up

Lesson Presentation

Lesson Quiz

**Holt McDougal Geometry** 

#### **Warm Up** Solve each proportion.

- **1.**  $\frac{6}{11} = \frac{8}{b}$  **2.**  $\frac{5}{z} = \frac{z}{20}$  **3.**  $\frac{3}{10} = \frac{6}{x+12}$   $b = \frac{44}{3} \text{ or } 14\frac{2}{3}$   $z = \pm 10$ **3.**  $\frac{3}{x} = \frac{6}{x+12}$
- 4. If ΔQ̃RS ~ Δ̃XYZ, identify the pairs of congruent angles and write 3 proportions using pairs of corresponding sides.

 $\angle Q \cong \angle X; \ \angle R \cong \angle Y; \ \angle S \cong \angle Z;$ 

 $\frac{QR}{XY} = \frac{RS}{YZ}; \frac{RS}{YZ} = \frac{QS}{XZ}; \frac{QS}{XZ} = \frac{QR}{XY}$ 

## **Objectives**

# Prove certain triangles are similar by using AA, SSS, and SAS.

Use triangle similarity to solve problems.

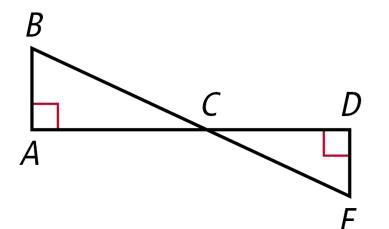
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There are several ways to prove certain triangles are similar. The following postulate, as well as the SSS and SAS Similarity Theorems, will be used in proofs just as SSS, SAS, ASA, HL, and AAS were used to prove triangles congruent.

Postulate 7-3-1 Angle-Angle (AA) Similarity		
POSTULATE	HYPOTHESIS	CONCLUSION
If two angles of one triangle are congruent to two angles of another triangle, then the triangles are similar.	$B = \begin{bmatrix} A \\ C \\ C \\ C \\ F \end{bmatrix}$	∆ <b>AB</b> C ~ ∆ <b>D</b> EF

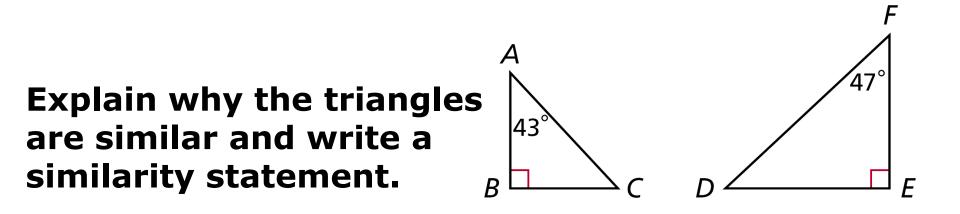
#### **Example 1: Using the AA Similarity Postulate**

#### Explain why the triangles are similar and write a similarity statement.



Since  $AC \parallel DC$ ,  $\angle B \cong \angle E$  by the Alternate Interior Angles Theorem. Also,  $\angle A \cong \angle D$  by the Right Angle Congruence Theorem. Therefore  $\triangle ABC \sim \triangle DEC$  by AA~.

#### **Check It Out! Example 1**



By the Triangle Sum Theorem,  $m \angle C = 47^{\circ}$ , so  $\angle C \cong \angle F$ .  $\angle B \cong \angle E$  by the Right Angle Congruence Theorem. Therefore,  $\triangle ABC \sim \triangle DEF$  by AA ~.

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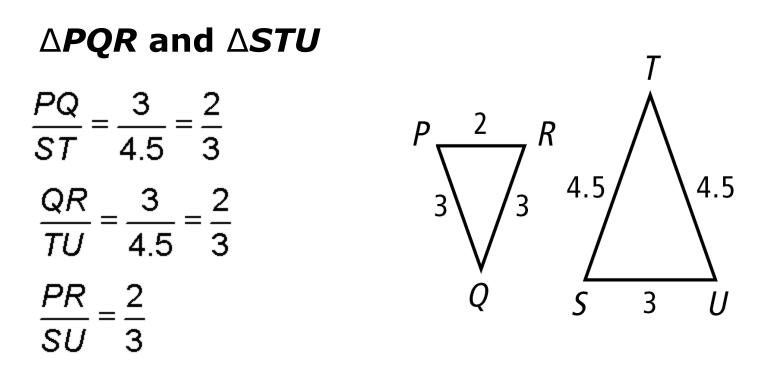
Theorem 7-3-2 Side-Side (SSS) Similarity		
THEOREM	HYPOTHESIS	CONCLUSION
If the three sides of one triangle are proportional to the three corresponding sides of another triangle, then the triangles are similar.	$B \xrightarrow{A} E_{C} \xrightarrow{D} F$	$\triangle ABC \sim \triangle DEF$

Theorem 7-3-3 Side-An	gle-Side (SAS) Similarity	
THEOREM	HYPOTHESIS	CONCLUSION
If two sides of one triangle are proportional to two sides of another triangle and their included angles are congruent, then the triangles are similar.	A $C$ $C$ $C$ $C$ $C$ $C$ $C$ $C$ $C$ $F$ $C$ $C$ $C$ $F$ $C$ $C$ $C$ $F$	△ <b>AB</b> C ~ △ <b>DE</b> F

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#### **Example 2A: Verifying Triangle Similarity**

#### Verify that the triangles are similar.

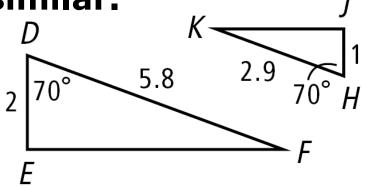


Therefore  $\Delta PQR \sim \Delta STU$  by SSS ~.

#### **Example 2B: Verifying Triangle Similarity**

Verify that the triangles are similar.

△*DEF* and △*HJK* 



 $\angle D \cong \angle H$  by the Definition of Congruent Angles.

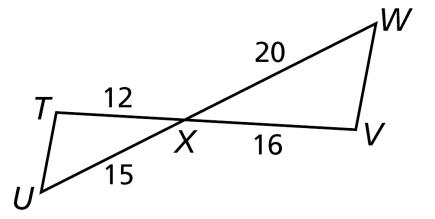
$$\frac{DE}{HJ} = \frac{2}{1} = 2 \qquad \frac{DF}{HK} = \frac{5.8}{2.9} = 2$$

Therefore  $\Delta DEF \sim \Delta HJK$  by SAS ~.

#### **Check It Out! Example 2**

#### Verify that $\triangle TXU \sim \triangle VXW$ .

 $\angle TXU \cong \angle VXW$  by the Vertical Angles Theorem.



$$\frac{TX}{VX} = \frac{12}{16} = \frac{3}{4} \qquad \frac{XU}{XW} = \frac{15}{20} = \frac{3}{4}$$

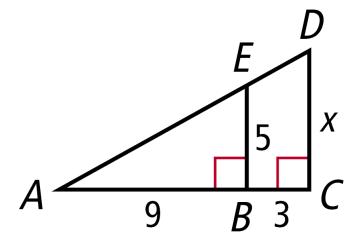
Therefore  $\Delta TXU \sim \Delta VXW$  by SAS ~.

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**Example 3: Finding Lengths in Similar Triangles** 

## Explain why △ABE ~ △ACD, and then find CD.

**Step 1** Prove triangles are similar.



 $\angle A \cong \angle A$  by Reflexive Property of  $\cong$ , and  $\angle B \cong \angle C$  since they are both right angles.

Therefore  $\triangle ABE \sim \triangle ACD$  by AA ~.

#### **Example 3 Continued**

#### Step 2 Find CD.

- $\frac{CD}{BE} = \frac{CA}{BA} = \frac{CB + BA}{BA}$  $\frac{x}{5} = \frac{3+9}{9}$
- x(9) = 5(3 + 9)
  - 9x = 60 $x = \frac{60}{9} = 6\frac{2}{3}$

Corr. sides are proportional. Seg. Add. Postulate.

- Substitute x for CD, 5 for BE, 3 for CB, and 9 for BA.
- Cross Products Prop.

Simplify.

Divide both sides by 9.

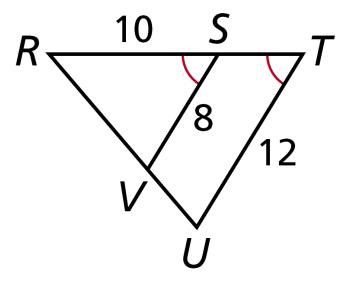
#### **Check It Out! Example 3**

#### Explain why $\triangle RSV \sim \triangle RTU$ and then find *RT*.

Step 1 Prove triangles are similar.

It is given that  $\angle S \cong \angle T$ .  $\angle R \cong \angle R$  by Reflexive Property of  $\cong$ .

Therefore  $\Delta RSV \sim \Delta RTU$  by AA ~.



#### **Check It Out! Example 3 Continued**

#### Step 2 Find *RT*.

- $\frac{RT}{RS} = \frac{TU}{SV}$  Corr. sides are proportional.
- $\frac{RT}{10} = \frac{12}{8}$ Substitute RS for 10, 12 for TU, 8 for SV.
- RT(8) = 10(12) Cross Products Prop.
  - 8RT = 120 Simplify.
    - RT = 15 Divide both sides by 8.

You learned in Chapter 2 that the Reflexive, Symmetric, and Transitive Properties of Equality have corresponding properties of congruence. These properties also hold true for similarity of triangles.

Properties of Similarity
Reflexive Property of Similarity
$\triangle ABC \sim \triangle ABC$ (Reflex. Prop. of ~)
Symmetric Property of Similarity
If $\triangle ABC \sim \triangle DEF$ , then $\triangle DEF \sim \triangle ABC$ . (Sym. Prop. of $\sim$ )
Transitive Property of Similarity
If $\triangle ABC \sim \triangle DEF$ and $\triangle DEF \sim \triangle XYZ$ , then $\triangle ABC \sim \triangle XYZ$ . (Trans. Prop. of ~)