## Trigonometry

## TWELFTH EDITION

# Trigonometry <br> TWELFTH EDITION 

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## ScoutAutomatedPrintCode

This text is dedicated to you-the student. We hope that it helps you achieve your goals. Remember to show up, work hard, and stay positive. Everything else will take care of itself.

The Lial Author Team

## Contents

Preface xiii
Resources for Success xviii

## R Algebra Review 1

R. 1 Basic Concepts from Algebra 2

Sets of Numbers ■ Additive Inverses ■ Absolute Value ■ Inequality and Order on a Number Line
R. 2 Real Number Operations and Properties 12

Operations on Real Numbers ■ Distance between Points on a Number Line ■ Exponents ■ Order of Operations ■ Properties of Real Numbers
R. 3 Exponents, Polynomials, and Factoring 24

Rules for Exponents ■ Zero as an Exponent ■ Polynomials ■ Addition, Subtraction, and Multiplication of Polynomials ■ Factoring Polynomials

## R. 4 Rational Expressions 34

Rational Expressions ■ LowestTerms of a Rational Expression ■ Multiplication and Division ■ Addition and Subtraction ■ Complex Fractions
R. 5 Radical Expressions 44

Square Roots ■ Cube, Fourth, and Higher Roots ■ Product and Quotient Rules for Radicals ■ Operations with Radicals ■ Rationalizing Denominators Simplified Radicals
R. 6 Equations and Inequalities 56

Basic Terminology of Equations ■ Linear Equations ■ Quadratic Equations ■ Inequalities ■ Linear Inequalities and Interval Notation ■ Three-Part Inequalities
R. 7 Rectangular Coordinates and Graphs 67

The Rectangular Coordinate System $\quad$ The Distance Formula $\quad$ The Midpoint Formula ■ Equations in Two Variables ■ Circles

## R. 8 Functions 76

Relations and Functions $■$ Domain and Range $■$ Determining Whether Relations Are Functions ■ Function Notation ■ Increasing, Decreasing, and Constant Functions ■ Continuity
R. 9 Graphing Techniques $\mathbf{8 8}$

Stretching and Shrinking ■ Reflecting ■ Symmetry ■ Even and Odd Functions ■ Translations

```
Test Prep 104 ■ Review Exercises 112 ■ Test 116
```

1 Trigonometric Functions ..... 119
1.1 Angles ..... 120
Basic Terminology ■ Degree Measure ■ Standard Position Coterminal Angles
1.2 Angle Relationships and Similar Triangles ..... 128
Geometric Properties Triangles
Chapter 1 Quiz (Sections 1.1-1.2) ..... 139
1.3 Trigonometric Functions ..... 140
The Pythagorean Theorem and the Distance Formula ■ TrigonometricFunctions ■ Quadrantal Angles
1.4 Using the Definitions of the Trigonometric Functions ..... 148
Reciprocal Identities ■ Signs and Ranges of Function Values ■ PythagoreanIdentities ■ Quotient Identities
Test Prep $\mathbf{1 5 7} ■$ Review Exercises $\quad 160 ■$ Test 163
2 Acute Angles and Right Triangles ..... 165
2.1 Trigonometric Functions of Acute Angles ..... 166
Right-Triangle-Based Definitions of the Trigonometric FunctionsCofunctions ■ How Function Values Change as Angles ChangeTrigonometric Function Values of Special Angles
2.2 Trigonometric Functions of Non-Acute Angles ..... 174
Reference Angles ■ Special Angles as Reference Angles ■ Determination of Angle Measures with Special Reference Angles
2.3 Approximations of Trigonometric Function Values ..... 182
Calculator Approximations of Trigonometric Function Values $\quad$ ■Calculator Approximations of Angle Measures $■$ An Application
Chapter 2 Quiz (Sections 2.1-2.3) ..... 189
2.4 Solutions and Applications of Right Triangles ..... 190
Historical Background $■$ Significant Digits - Solving TrianglesAngles of Elevation or Depression
2.5 Further Applications of Right Triangles ..... 200
Historical Background ■ Bearing ■ Further Applications
Test Prep 209 ■ Review Exercises 211 ■ Test 215

## 3 Radian Measure and the Unit Circle

3.1 Radian Measure 218

Radian Measure ■ Conversions between Degrees and Radians Trigonometric Function Values of Angles in Radians

### 3.2 Applications of Radian Measure 224

Arc Length on a Circle $■$ Area of a Sector of a Circle

### 3.3 The Unit Circle and Circular Functions 235

Circular Functions ■ Values of the Circular Functions ■ Determining a Number with a Given Circular Function Value ■Applications of Circular Functions ■ Function Values as Lengths of Line Segments

Chapter 3 Quiz (Sections 3.1-3.3) 245
3.4 Linear and Angular Speed 246

Linear Speed ■ Angular Speed
Test Prep $\mathbf{2 5 2}$ ■ Review Exercises $\mathbf{2 5 4}$ ■ Test 257

## 4 Graphs of the Circular Functions 259

4.1 Graphs of the Sine and Cosine Functions 260

Periodic Functions $\square$ Graph of the Sine Function $\square$ Graph of the Cosine Function ■ Techniques for Graphing, Amplitude, and Period ■ Connecting Graphs with Equations ■ ATrigonometric Model

4.2 Translations of the Graphs of the Sine and Cosine
Functions
273

Horizontal Translations ■ Vertical Translations ■ Combinations of Translations ■ ATrigonometric Model

Chapter 4 Quiz (Sections 4.1-4.2) 284
4.3 Graphs of the Tangent and Cotangent Functions 284

Graph of the Tangent Function ■ Graph of the Cotangent Function ■ Techniques for Graphing ■ Connecting Graphs with Equations

### 4.4 Graphs of the Secant and Cosecant Functions <br> 293

Graph of the Secant Function ■ Graph of the Cosecant Function ■ Techniquesfor Graphing ■ Connecting Graphs with Equations ■ Addition of OrdinatesSummary Exercises on Graphing Circular Functions 301

### 4.5 Harmonic Motion <br> 301

Simple Harmonic Motion ■ Damped Oscillatory Motion

```
Test Prep 308■ Review Exercises 310 ■ Test 313
```

5 Trigonometric Identities ..... 315
5.1 Fundamental Identities ..... 316
Fundamental Identities ■ Uses of the Fundamental Identities
5.2 Verifying Trigonometric Identities ..... 322
Strategies ■ Verifying Identities by Working with One Side Verifying Identities by Working with Both Sides
5.3 Sum and Difference Identities for Cosine ..... 331
Difference Identity for Cosine ■ Sum Identity for Cosine ■ Cofunction Identities Applications of the Sum and Difference Identities $■$ Verifying an Identity
5.4 Sum and Difference Identities for Sine and Tangent ..... 341
Sum and Difference Identities for Sine $■$ Sum and Difference IdentitiesforTangent $\square$ Applications of the Sum and Difference Identities ■Verifying an Identity
Chapter 5 Quiz (Sections 5.1-5.4) ..... 350
5.5 Double-Angle Identities ..... 350
Double-Angle Identities ■ An Application ■ Product-to-Sum andSum-to-Product Identities
5.6 Half-Angle Identities ..... 358
Half-Angle Identities ■ Applications of the Half-Angle Identities Verifying an Identity
Summary Exercises on Verifying Trigonometric Identities ..... 365
Test Prep $366 ■$ Review Exercises 368 ■ Test 370
6 Inverse Circular Functions and Trigonometric Equations ..... 371
6.1 Inverse Circular Functions ..... 372Inverse Functions ■ Inverse Sine Function ■ Inverse Cosine Function ■ Inverse
Tangent Function ■ Other Inverse Circular Functions ■ Inverse Function Values
6.2 Trigonometric Equations I ..... 388
Linear Methods ■ Zero-Factor Property Method ■ Quadratic Methods Trigonometric Identity Substitutions ■ An Application
6.3 Trigonometric Equations II ..... 395
Equations with Half-Angles ■ Equations with Multiple Angles ■ An Application
Chapter 6 Quiz (Sections 6.1-6.3) 402
6.4 Equations Involving Inverse Trigonometric Functions ..... 402
Solution for $x$ in Terms of $y$ Using Inverse Functions ■ Solution of InverseTrigonometric Equations
Test Prep 409 ■ Review Exercises 411 ■ Test 413
7 Applications of Trigonometry and Vectors ..... 415
7.1 Oblique Triangles and the Law of Sines ..... 416
Congruency and ObliqueTriangles ■ Derivation of the Law of SinesSolutions of SAA and ASA Triangles (Case 1) ■ Area of a Triangle
7.2 The Ambiguous Case of the Law of Sines ..... 426
Description of the Ambiguous Case $■$ Solutions of SSATriangles (Case 2)Analyzing Data for Possible Number of Triangles
7.3 The Law of Cosines ..... 432
Derivation of the Law of Cosines $■$ Solutions of SAS and SSSTriangles (Cases 3 and 4) ■ Heron's Formula for the Area of a Triangle Derivation of Heron's Formula
Chapter 7 Quiz (Sections 7.1-7.3) ..... 445
7.4 Geometrically Defined Vectors and Applications ..... 446
BasicTerminology ■ The Equilibrant ■ Incline ApplicationsNavigation Applications
7.5 Algebraically Defined Vectors and the Dot Product ..... 456
Algebraic Interpretation of Vectors ■ Operations with VectorsThe Dot Product and the Angle between Vectors
Summary Exercises on Applications of Trigonometry and Vectors ..... 465
Test Prep 466 ■ Review Exercises 469 ■ Test ..... 473
8 Complex Numbers, Polar Equations, and Parametric Equations ..... 475
8.1 Complex Numbers ..... 476
Basic Concepts of Complex Numbers ■ Complex Solutions of Quadratic Equations (Part 1) ■ Operations on Complex Numbers ■ Complex Solutions of Quadratic Equations (Part 2) ■ Powers of $i$
8.2 Trigonometric (Polar) Form of Complex Numbers ..... 486
The Complex Plane and Vector Representation ■ Trigonometric (Polar) FormConverting between Rectangular and Trigonometric (Polar) FormsAn Application of Complex Numbers to Fractals
8.3 The Product and Quotient Theorems ..... 492
Products of Complex Numbers in Trigonometric Form ■ Quotients of ComplexNumbers in Trigonometric Form
8.4 De Moivre's Theorem; Powers and Roots of Complex Numbers ..... 498
Powers of Complex Numbers (De Moivre'sTheorem) ■ Roots of ComplexNumbers
Chapter 8 Quiz (Sections 8.1-8.4) ..... 505
8.5 Polar Equations and Graphs ..... 505
Polar Coordinate System ■ Graphs of Polar Equations $■$ Conversion fromPolar to Rectangular Equations ■ Classification of Polar Equations
8.6 Parametric Equations, Graphs, and Applications ..... 518
Basic Concepts ■ Parametric Graphs andTheir Rectangular Equivalents The Cycloid ■ Applications of Parametric Equations
Test Prep $\mathbf{5 2 6}$ ■ Review Exercises $\mathbf{5 2 9}$ ■ Test ..... 532
Answers to Selected Exercises ..... A-1Photo Credits C-1
Index ..... I-1

## WELCOME TO THE 12TH EDITION

In the twelfth edition of Trigonometry, we continue our ongoing commitment to providing the best possible text to help instructors teach and students succeed. In this edition, we have remained true to the pedagogical style of the past while staying focused on the needs of today's students. Support for all classroom types (traditional, corequisite, flipped, hybrid, and online) may be found in this classic text and its supplements backed by the power of Pearson's MyLab Math.

In this edition, we have drawn on the extensive teaching experience of the Lial team, with special consideration given to reviewer suggestions. General updates include enhanced readability as we continually strive to make math understandable for students, updates to our extensive list of applications and real-world mathematics problems, use of color in displays and side comments, and coordination of exercises and their related examples.

The authors understand that teaching and learning mathematics today can be a challenging task. Some students are prepared for the challenge, while other students require more review and supplemental material. This text is written so that trigonometry students with varying abilities and backgrounds will all have an opportunity for a successful learning experience.

The Lial team believes this to be our best edition of Trigonometry yet, and we sincerely hope that you enjoy using it as much as we have enjoyed writing it. Additional texts in this series are as follows.

College Algebra, Thirteenth Edition
College Algebra and Trigonometry, Seventh Edition
Precalculus, Seventh Edition

## HIGHLIGHTS OF NEW CONTENT

- New Chapter R provides a thorough review of the basic algebraic concepts that trigonometry students need in order to succeed. Topics include real number operations and properties, rules for exponents, operations on polynomials and factoring, rational and radical expressions, solving equations and inequalities, circles, functions, domain, range, and graphing techniques.

Instructors may choose to cover review topics from Chapter $\mathbf{R}$ at the beginning of their course or to insert these topics as-needed in a just-in-time fashion. Either way, students who are under-prepared for the demands of trigonometry, as well as those who need a quick review, will benefit from the material contained here. It is our hope that this chapter, which also includes a comprehensive end-of-chapter Test Prep, would serve as a valuable resource throughout all course types for students and instructors alike.

- The exercise sets were a key focus of this revision, and Chapters 3 and 4 are among the chapters that have benefitted. Specifically, Section 3.2 Applications of Radian Measure has additional exercises devoted to finding arc length and area of a sector. Section 3.4 Linear and Angular Speed now contains new applications of linear and angular speed. Chapter 4 includes updated real data applications and additional Connecting Graphs with Equations exercises, as well as new applications of harmonic motion.
- Proofs of identities in Chapter 5 now feature a drop-down style for increased clarity and student understanding. Based on reviewer requests, Section 6.4 Equations Involving Inverse Trigonometric Functions includes new exercises in which solutions of inverse trigonometric equations are found.
- In response to reviewer suggestions, Section 7.5 Algebraically Defined Vectors and the Dot Product has new exercises on finding the angle between two vectors, determining magnitude and direction angle for a vector, and identifying orthogonal vectors. Additionally, Chapter 8 contains new exercises requiring students to graph polar and parametric equations and give parametric representations of plane curves.


## FEATURES OF THIS TEXT

## SUPPORT FOR LEARNING CONCEPTS

We provide a variety of features to support students' learning of the essential topics of trigonometry. Explanations that are written in understandable terms, figures and graphs that illustrate examples and concepts, graphing technology that supports and enhances algebraic manipulations, and real-life applications that enrich the topics with meaning all provide opportunities for students to deepen their understanding of mathematics. These features help students make mathematical connections and expand their own knowledge base.

- Examples Numbered examples that illustrate the techniques for working exercises are found in every section. We use traditional explanations, side comments, and pointers to describe the steps taken-and to warn students about common pitfalls. Some examples provide additional graphing calculator solutions, although these can be omitted if desired.
- Now Try Exercises Following each numbered example, the student is directed to try a corresponding odd-numbered exercise (or exercises). This feature allows for quick feedback to determine whether the student understands the principles illustrated in the example.
- Real-Life Applications We have included hundreds of real-life applications, many with data updated from the previous edition. They come from fields such as sports, biology, astronomy, geology, music, and environmental studies.
- Function Boxes Special function boxes offer a comprehensive, visual introduction to each type of trigonometric function and also serve as an excellent resource for reference and review. Each function box includes a table of values, traditional and calculator-generated graphs, the domain, the range, and other special information about the function. These boxes are assignable in MyLab Math.
- Figures and Photos Today's students are more visually oriented than ever before, and we have updated the figures and photos in this edition to promote visual appeal. Guided Visualizations with accompanying exercises and explorations are available and assignable in MyLab Math.
- Cautions and Notes Text that is marked CAUTION warns students of common errors, and NOTE comments point out explanations that should receive particular attention.
- Looking Ahead to Calculus These margin notes offer glimpses of how the topics currently being studied are used in calculus.
- Use of Graphing Technology We have integrated the use of graphing calculators where appropriate, although this technology is completely optional and can be omitted without loss of continuity. We continue to stress that graphing calculators support understanding but that students must first master the underlying mathematical concepts. Exercises that require the use of a graphing calculator are marked with the icon $\quad$.


## SUPPORT FOR PRACTICING CONCEPTS

This text offers a wide variety of exercises to help students master trigonometry. The extensive exercise sets provide ample opportunity for practice and increase in difficulty so that students at every level of understanding are challenged. The variety of exercise types promotes mastery of the concepts and reduces the need for rote memorization.

■ Concept Preview Each exercise set begins with a group of CONCEPT PREVIEW exercises designed to promote understanding of vocabulary and basic concepts in each section. These exercises are assignable in MyLab Math and provide support especially for hybrid, online, and flipped courses.

- Exercise Sets In addition to traditional drill exercises, this text includes writing exercises, optional graphing calculator exercises and multiplechoice, matching, true/false, and completion exercises. Those marked Concept Check focus on conceptual thinking. Connecting Graphs with Equations exercises challenge students to write equations that correspond to given graphs. Video solutions for select problems are available in MyLab Math.
- Relating Concepts Exercises Appearing at the end of selected exercise sets, these groups of exercises are designed so that students who work them in numerical order will follow a line of reasoning that leads to an understanding of how various topics and concepts are related. All answers to these exercises appear in the student answer section, and these exercises are assignable in MyLab Math.


## SUPPORT FOR REVIEW AND TEST PREP

Ample opportunities for review are found both within the chapters and at the ends of chapters. Quizzes interspersed within chapters provide a quick assessment of students' understanding of the material presented up to that point in the chapter. Chapter Test Preps provide comprehensive study aids to help students prepare for tests.

- Quizzes Students can periodically check their progress with in-chapter quizzes that appear in all chapters, beginning with Chapter 1. All answers, with corresponding section references, appear in the student answer section. These quizzes are assignable in MyLab Math.

■ Summary Exercises These sets of in-chapter exercises give students the all-important opportunity to work mixed review exercises, requiring them to synthesize concepts and select appropriate solution methods.

- End-of-Chapter Test Prep Following the final numbered section in each chapter, the Test Prep provides a list of Key Terms, a list of New Symbols (if applicable), and a two-column Quick Review that includes a section-bysection summary of concepts and examples. This feature concludes with a comprehensive set of Review Exercises and a Chapter Test. The Test Prep, Review Exercises, and Chapter Test are assignable in MyLab Math.


## Get the most out of MyLab Math

## Pearson

 MyLabMyLab Math for Trigonometry 12e<br>(access code required)

MyLab Math is tightly integrated with author style, offering a range of author-created resources, to give students a consistent experience.

## Preparedness

Preparedness is one of the biggest challenges in many math courses. Pearson offers a variety of content and course options to support students with just-in-time remediation and key-concept review as needed.

## Integrated Review in MyLab Math

Integrated Review can be used in corequisite courses or simply to help students who enter a course without a full understanding of prerequisite skills and concepts. Premade, editable Integrated Review assignments are available to assign in the Assignment Manager. Integrated Review landing pages (shown below) are visible by default at the start of most chapters, providing objective-level review.

- Students begin each chapter by completing a Skills Check to pinpoint which topics, if any, they need to review.
- Personalized review homework provides extra support for students who need it on just the topics they didn't master in the preceding Skills Check.

- Additional review materials, including worksheets and videos, are available.
pearson.com/mylab/math


## Get the most out of MyLab Math

P Pearson MyLab

## Updated! Videos

Updated videos cover all topics in the text to support students outside of the classroom. Quick Review videos cover key definitions and procedures. Example Solution videos offer a detailed solution process for every example in the textbook.



## Updated! MyNotes and MyClassroomExamples

MyNotes give students a note-taking structure to use while they read the text or watch the MyLab Math videos. MyClassroomExamples offer structure for notes taken during lecture and are for use with the ClassroomExamples found in the Annotated Instructor Edition.

Both sets of notes are available in MyLab Math and can be customized by the instructor.

## New! Enhanced Sample Assignments

Author Callie Daniels makes course set-up easier by giving instructors a starting point for each section. Following Callie's best practices in the classroom, Enhanced Sample Assignments maximize students' performance.

- Section Prep Assignments include Example Videos with assessment questions. This assignment pairs with MyNotes. Students actively participate while taking notes from the Example Video and then work the related exercises.
- Section Homework includes author-selected problems and increases in difficulty.
- Cumulative Review Homework Assignments draw from section homework questions covered to that point in the course-helping students prepare for a final exam.
pearson.com/mylab/math


## Resources for Success

## Pearson

MyLab

## Instructor Resources

Online resources can be downloaded at pearson.com/mylab/math or from www.pearson.com.

## Annotated Instructor's Edition

ISBN: 0135926033 / 9780135926031
Answers are included on the same page beside the text exercises where possible for quick reference. Helpful Teaching Tips and Classroom Examples are also provided.

## Online Instructor's Solution Manual

By Beverly Fusfield
Provides complete solutions to all text exercises

## Online Instructor's Testing Manual

Includes diagnostic pretests, grouped by section, with answers provided

## Testgen ${ }^{\circledR}$

TestGen (www.pearsoned.com/testgen) enables instructors to build, edit, print, and administer tests using a computerized bank of questions developed to cover all the objectives of the text.

## PowerPoint ${ }^{\circledR}$ Lecture Slides and Classroom Example PowerPoints

- The PowerPoint Lecture Slides feature presentations written and designed specifically for this text, including figures and examples from the text.
- Classroom Example PowerPoints include fully worked-out solutions to all Classroom Examples.


## Learning Catalytics ${ }^{T M}$

With MyLab Math, instructors and students have access to Learning Catalytics, which instructors can use to generate class discussion, guide lectures, and actively engage students. Prebuilt Learning Catalytics questions have been created specifically for this text. Simply search the tag "LialCollegeAlgebra" within the Learning Catalytics Question Library.

## Student Resources

## Additional resources enhance student

 success.
## Student's Solution Manual

## By Beverly Fusfield

Provides detailed solutions to all odd-numbered text exercises

## Video Lectures

- Quick Reviews cover key definitions and procedures from each section.
- Example Solutions walk students through the detailed solution process for every example in the textbook.


## MyNotes with Integrated Review Worksheets

MyNotes offer structure for students as they watch videos or read the text. These are available as a printed supplement and in MyLab Math.

- Includes textbook examples along with ample space for students to write solutions and notes
- Includes key concepts along with prompts for students to read, write, and reflect on what they have just learned
- Customizable-instructors can add their own examples or remove examples that are not covered in their course.

Integrated Review Worksheets prepare students for the Trigonometry material.

- Includes key terms, guided examples with ample space for students to work, and references to extra help in MyLab Math


## MyClassroomExamples

- Available in MyLab Math and offer structure for classroom lecture
- Includes Classroom Examples along with ample space for students to write solutions and notes
- Includes key concepts along with fill-in-the-blank opportunities to keep students engaged
- Customizable-instructors can add their own examples or remove Classroom Examples that are not covered in their course.


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As an author team, we are committed to providing the best possible trigonometry course to help instructors teach and students succeed. As we continue to work toward this goal, we welcome any comments or suggestions you might send, via e-mail, to math@ pearson.com.

Margaret L. Lial<br>John Hornsby<br>David I. Schneider<br>Callie J. Daniels

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