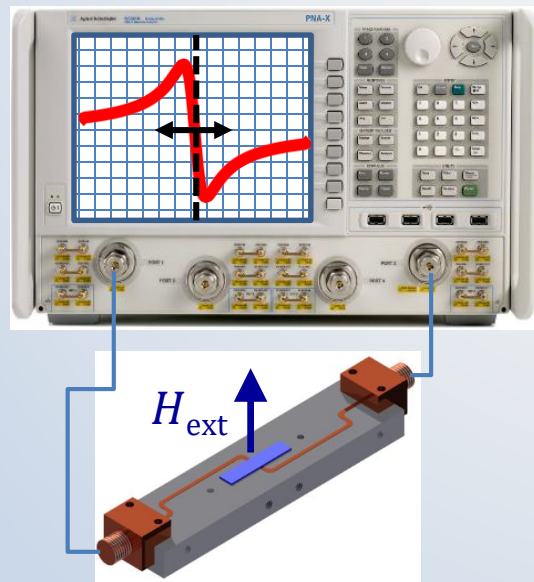


Broadband Ferromagnetic Resonance Spectroscopy: The “Swiss Army Knife” for Understanding Spin–Orbit Phenomena

Justin M. Shaw

National Institute of Standards and Technology, Boulder, CO 80305, USA



UPCOMING CONFERENCES



JAN 14, 2019 - JAN 18, 2019

MMM-INTERMAG JOINT CONFERENCE - WASHINGT...

JUN 24, 2019 - JUN 27, 2019

MAGNETIC FRONTIERS 2019

JUL 28, 2019 - AUG 1, 2019

MAGNONICS 2019

AUG 25, 2019 - AUG 29, 2019

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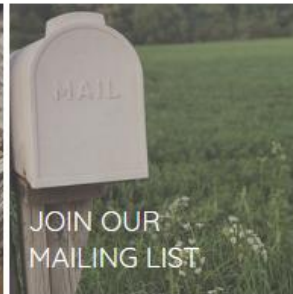
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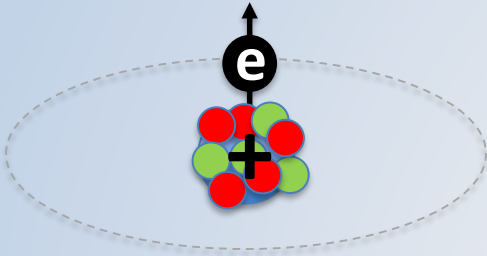
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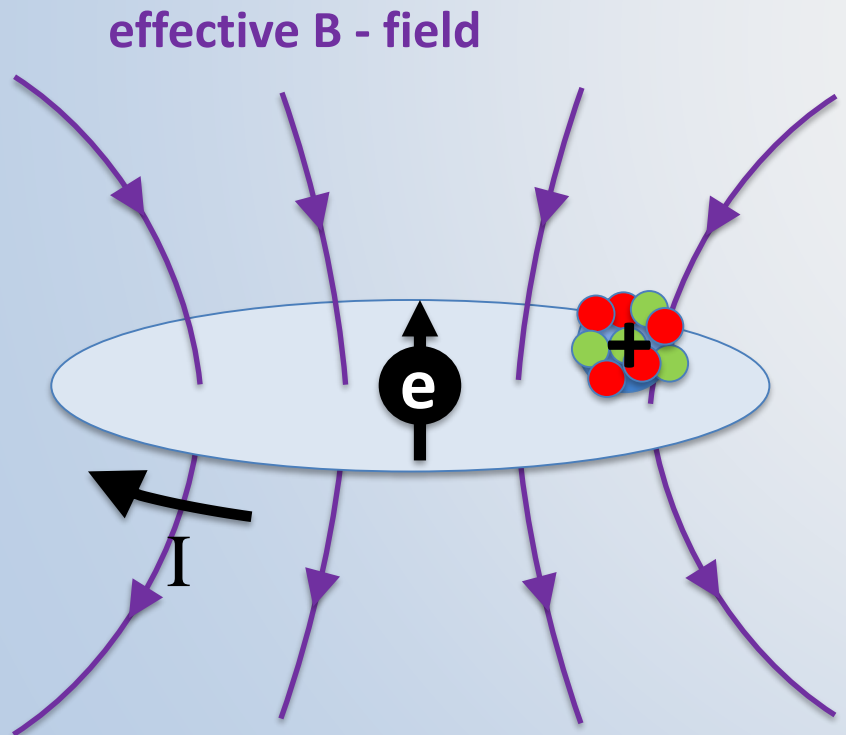
www.magnetism.org

- Spin-Orbit Interaction
- Ferromagnetic Resonance Spectroscopy
- Anisotropy and Orbital Moments
- Damping and Spin-Pumping
- Spin-Orbit Torques

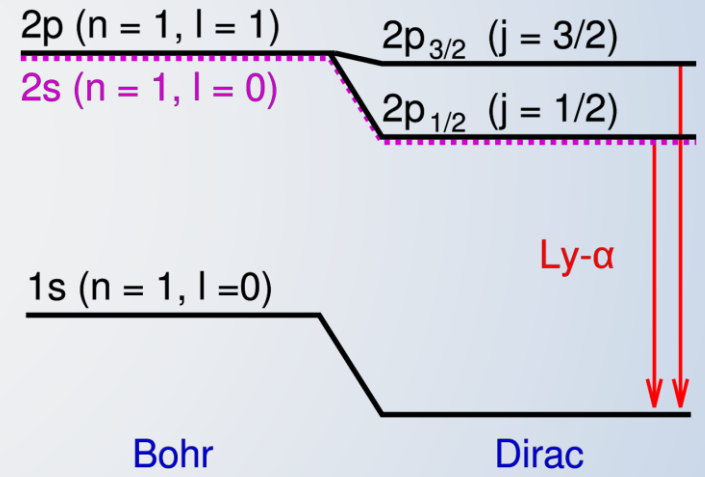
“Classical” electron spin orbiting nucleus



From the rest frame of the electron spin



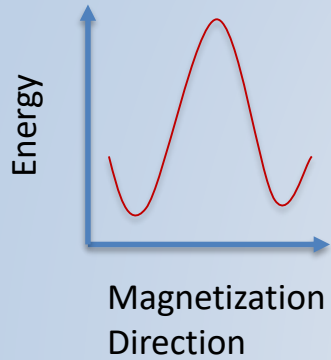
- In reality, Spin-Orbit is a relativistic effect
- This effective **B** field leads to a splitting of energy levels → **Fine Structure**



wikipedia

- In solids the spin-orbit interaction is included as an addition to the Hamiltonian

$$H_{SO} = \xi_{SO} \vec{L} \cdot \vec{S}$$

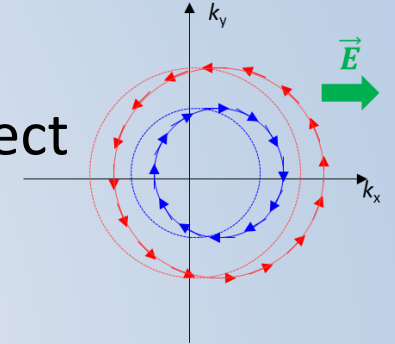


Anomalous Hall Effect

Topological Surface States

Magnetic Anisotropy

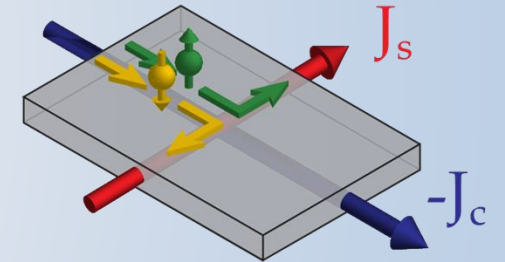
Rashba-Edelstein effect



Orbital Moments in Solids

Spin-Orbit Coupling

Spin Hall Effect



charge current spin current

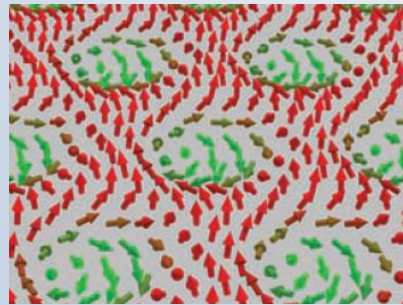
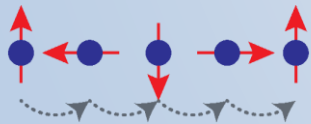
M Weiler

Dzyaloshinskii-Moriya Interaction (DMI)

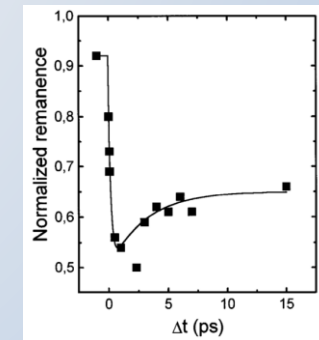
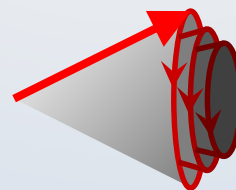
$$H_{SO} = \xi_{SO} \vec{L} \cdot \vec{S}$$

Spin-lattice Coupling

Damping

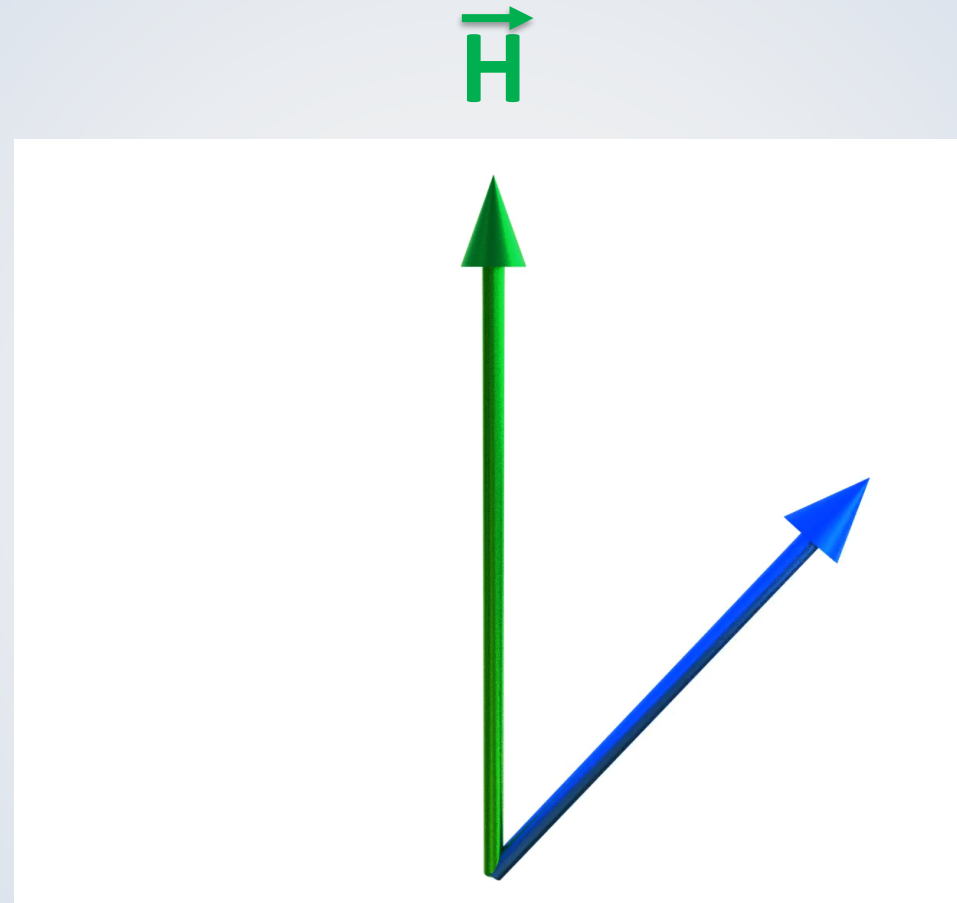


Science, 323, 915 (2009)



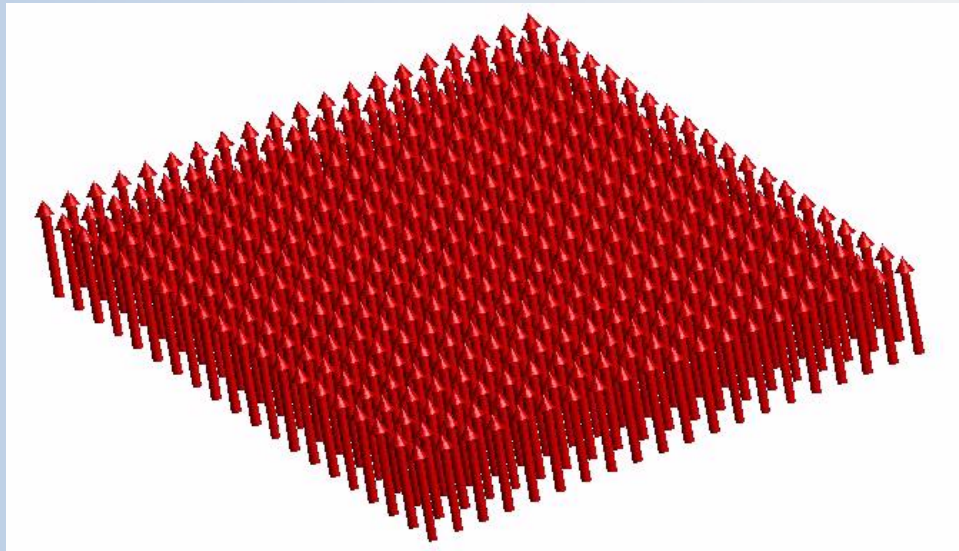
Beaurepaire PRL 76 (1996)

- Spin-Orbit Interaction
- Ferromagnetic Resonance Spectroscopy
- Anisotropy and Orbital Moments
- Damping and Spin-Pumping
- Spin-Orbit Torques



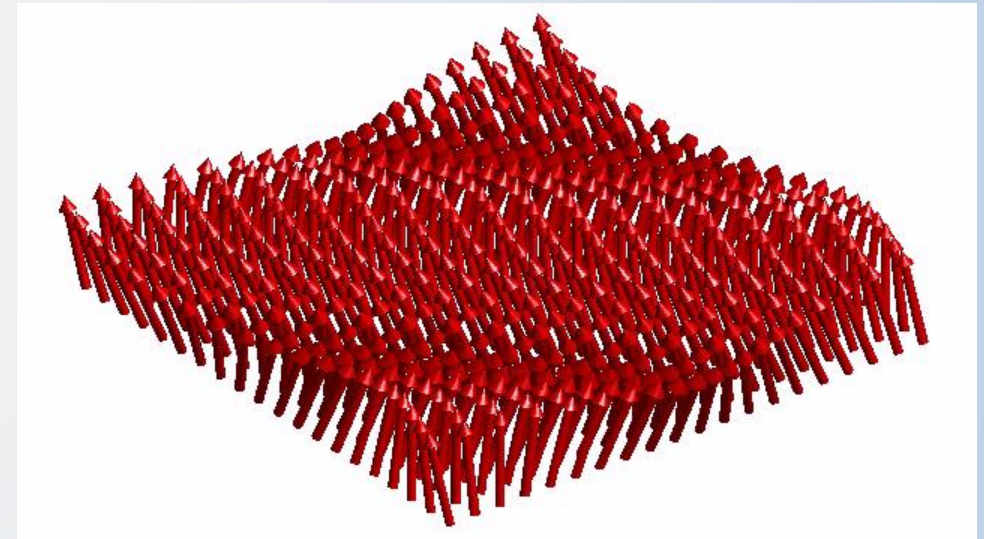
Ferromagnetic Resonance (FMR) Mode

All spin precess in phase



Other Spinwave (Magnon) Modes

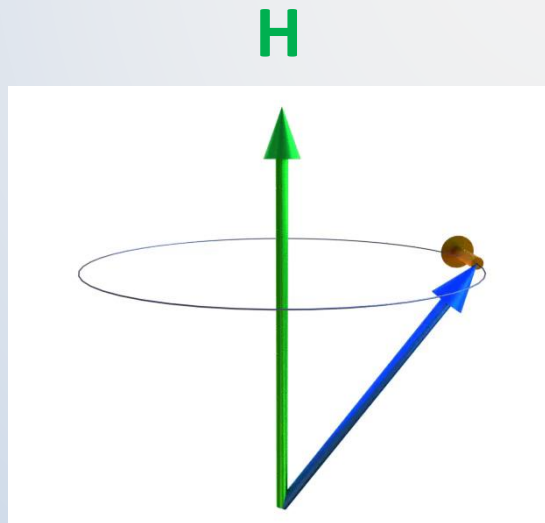
Non-zero phase relationship



Landau-Lifshitz equation

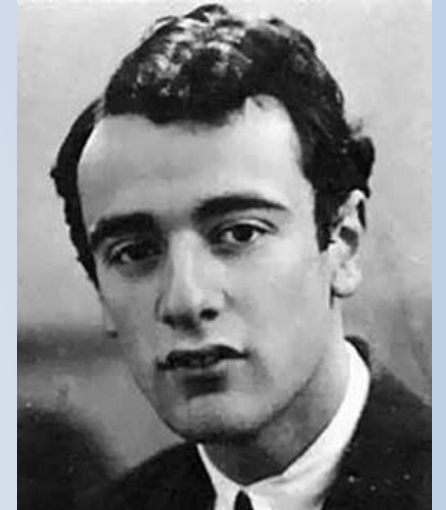
$$\frac{d\vec{M}}{dt} = -|\gamma|\mu_0(\vec{M} \times \vec{H})$$


 Larmor Term

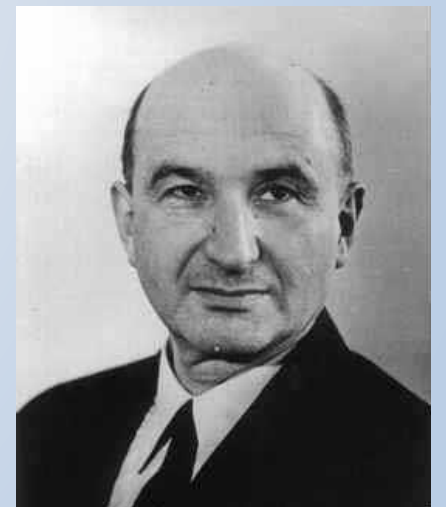


animations courtesy of Helmut Schultheiss

Lev Landau



Evgeny Lifshitz

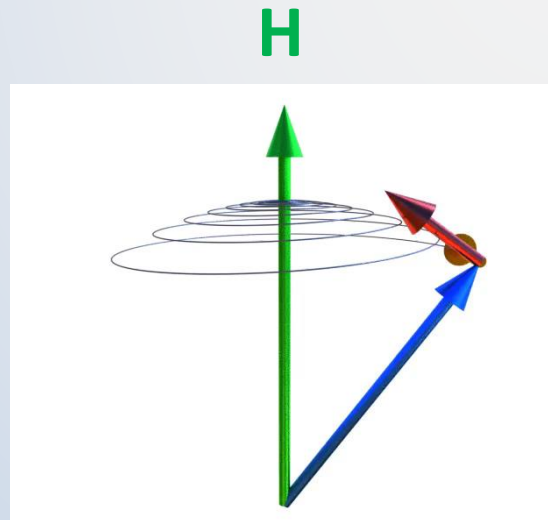


Landau-Lifshitz equation

$$\frac{d\vec{M}}{dt} = \underbrace{-|\gamma|\mu_0(\vec{M} \times \vec{H})}_{\text{Larmor Term}} - \underbrace{\frac{\alpha|\gamma|\mu_0}{M_s} [\vec{M} \times (\vec{M} \times \vec{H})]}_{\text{Damping Term}}$$

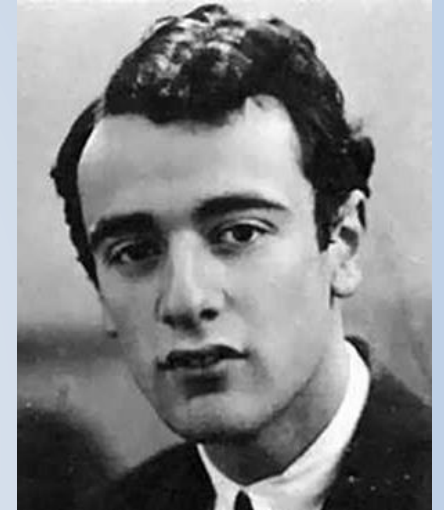
Larmor Term

Damping Term

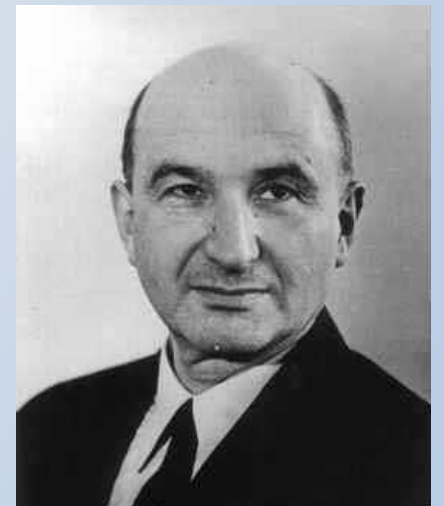


animations courtesy of Helmut Schultheiss

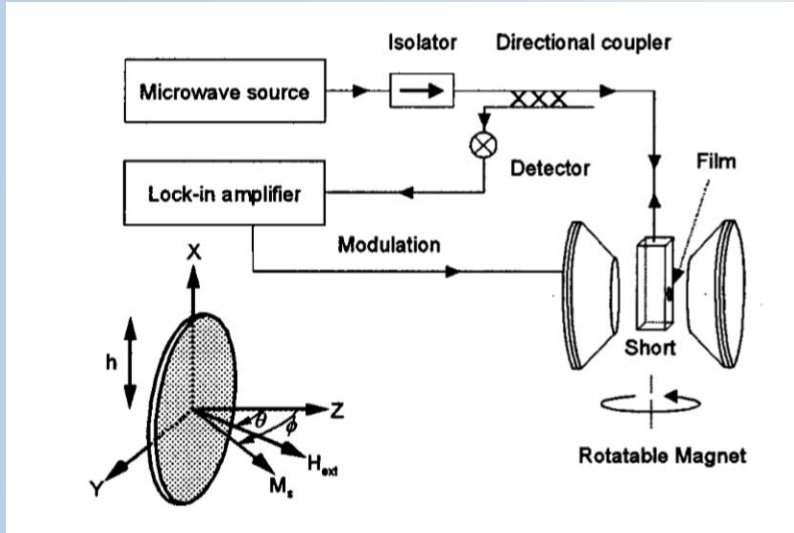
Lev Landau



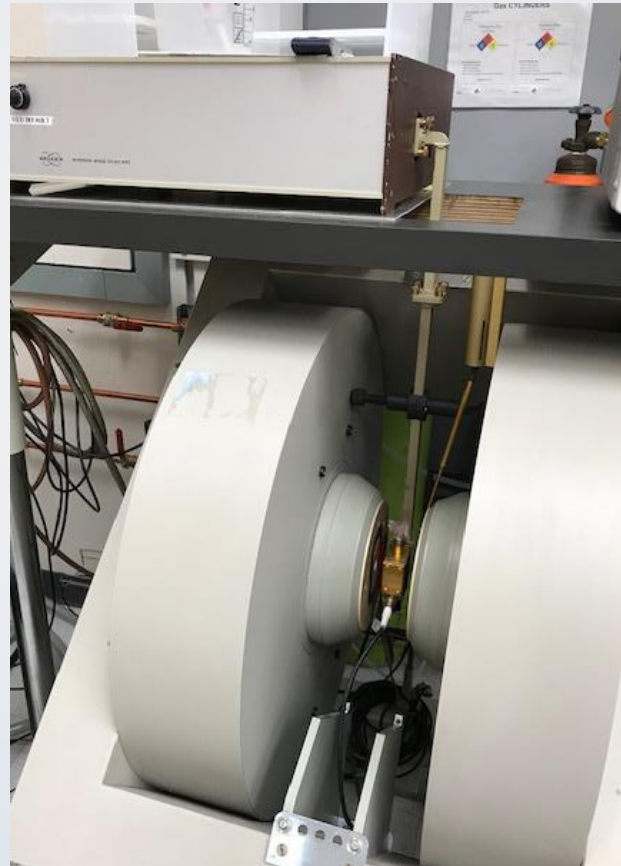
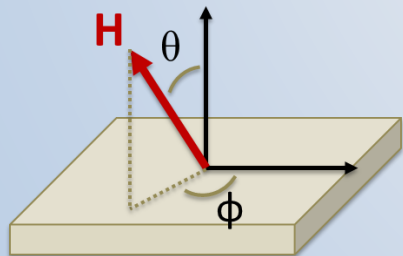
Evgeny Lifshitz



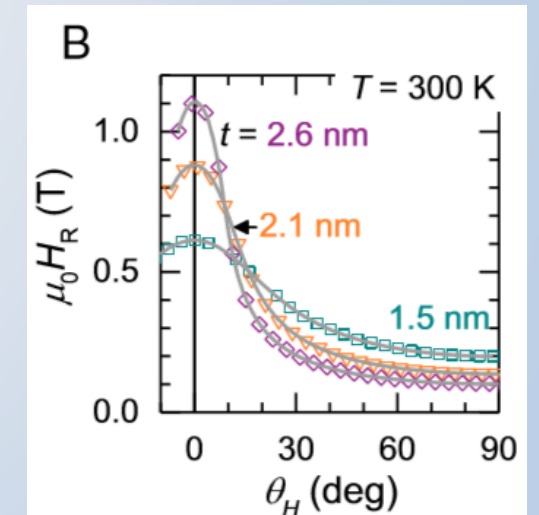
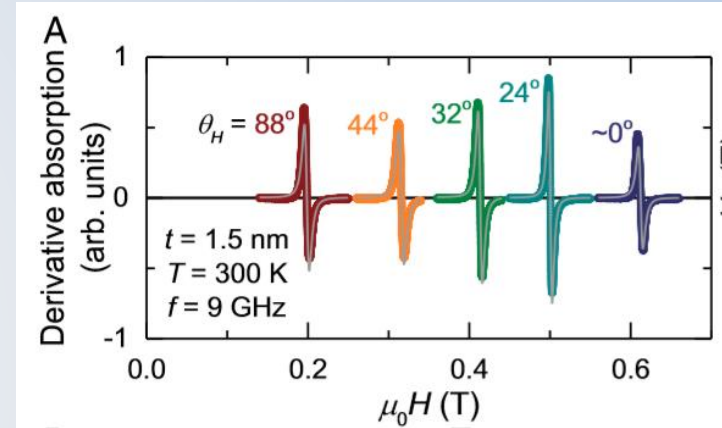
Cavity Based → single frequency!



Srivastava, JAP 85 7841 (1999)



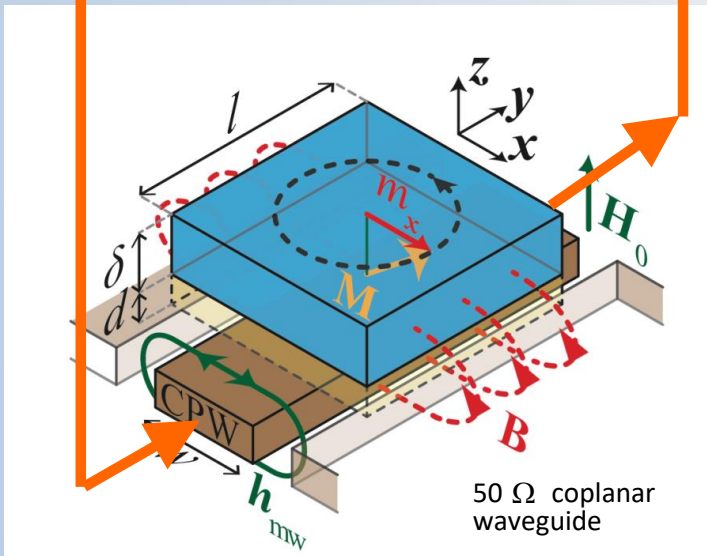
Constant Frequency, vary angle



Vector-network-analyzer



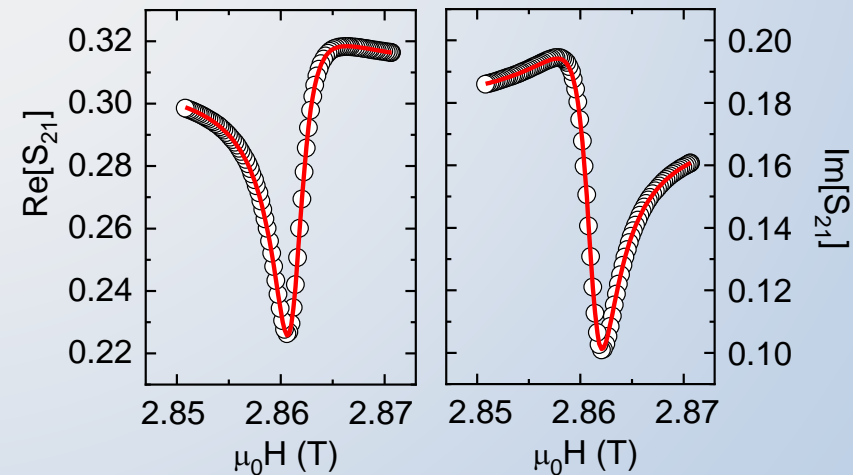
Port 1 Port 2



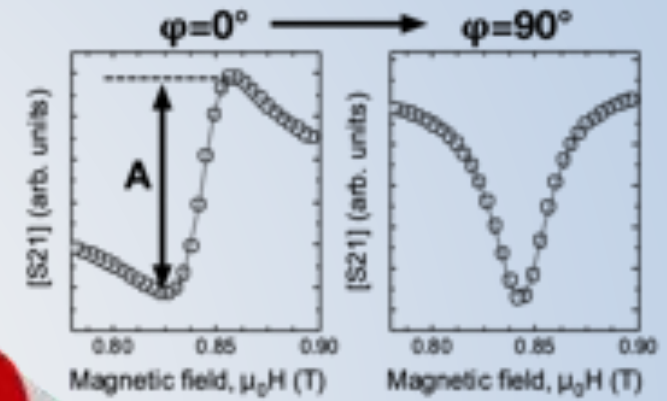
$$\chi(H, f) = \frac{M_{eff}(H - M_{eff})}{(H - M_{eff})^2 - H_{eff}^2 - i\Delta H(H - M_{eff})}$$

M_{eff} : Effective magnetization = $M_s - H_k$
 H_k : perpendicular anisotropy field
 M_s : Saturation magnetization
 ΔH : Linewidth

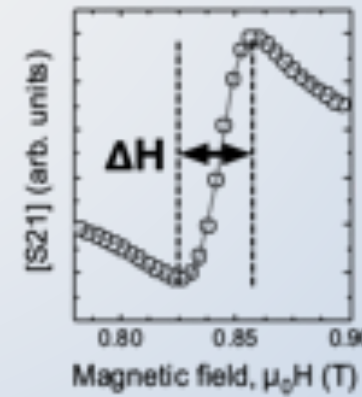
$$S_{21} = \underbrace{A}_{\text{Amplitude}} e^{i\phi}_{\text{Phase}} \underbrace{\chi(H, f)}_{\text{Resonance Field, Linewidth}} + \text{background}$$



- Spin Orbit Torques

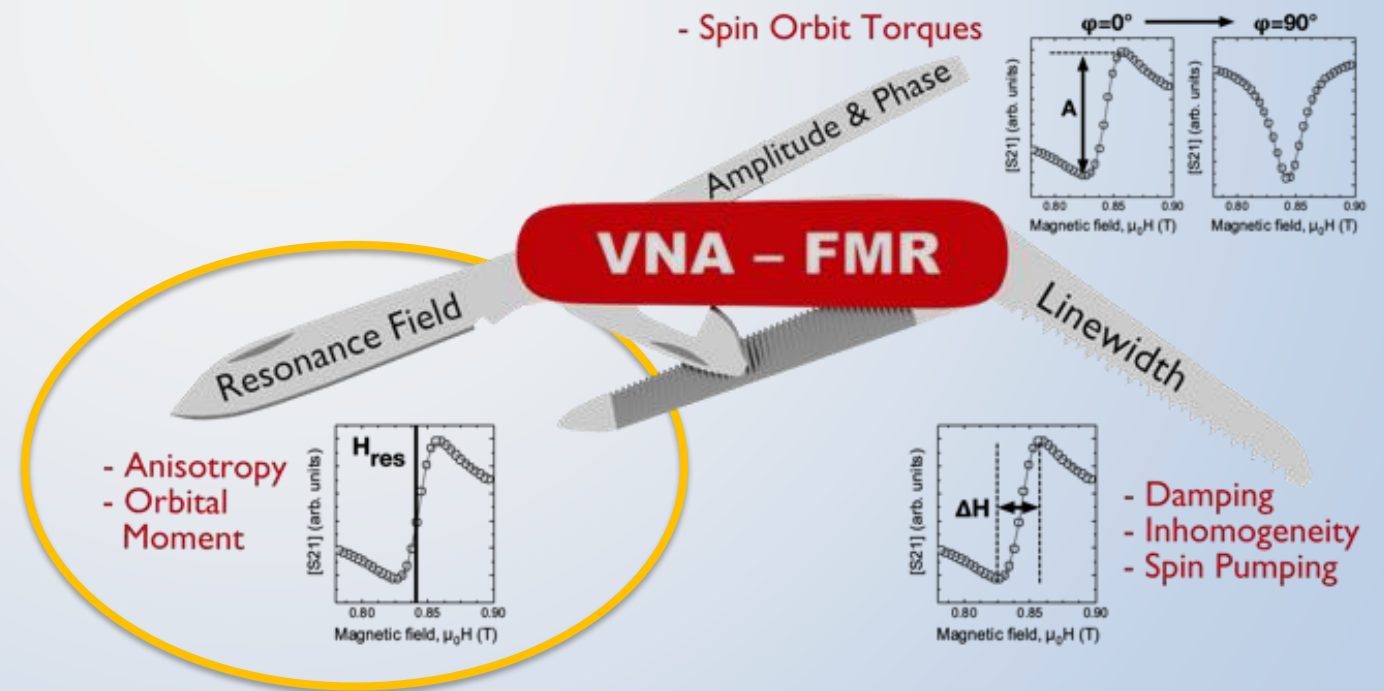


- Anisotropy
- Orbital Moment



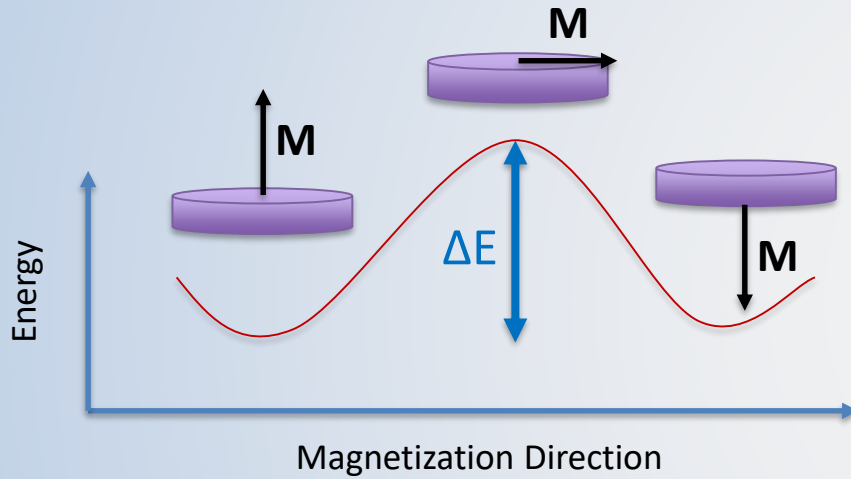
- Damping
- Inhomogeneity
- Spin Pumping

- Spin-Orbit Interaction
- Ferromagnetic Resonance Spectroscopy
- Anisotropy and Orbital Moments
- Damping and Spin-Pumping
- Spin-Orbit Torques



Magnetic Anisotropy gives a preferred orientation to the spontaneous magnetization

Why important?



Can originate from:

- Magnetocrystalline
- Interfaces
- Strain (Magnetostriction)
- Shape (Magnetostatic energy)



Seagate



Duke U



Simple model of Anisotropy Energy

$$\Delta E = A \frac{\xi_{SO}}{4\mu_B} (\mu_L^\perp - \mu_L^\parallel)$$

ΔE magnetic anisotropy energy

ξ_{SO} spin-orbit coupling constant

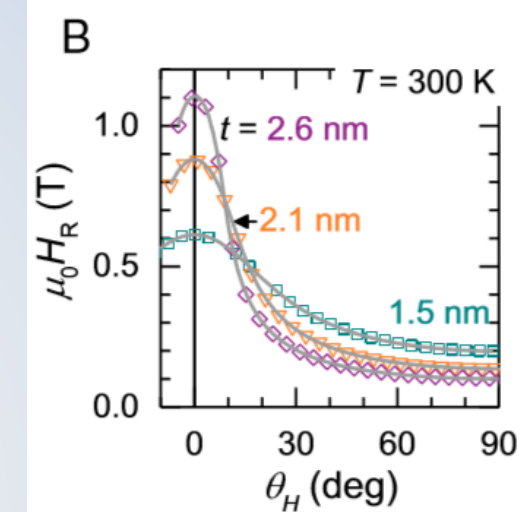
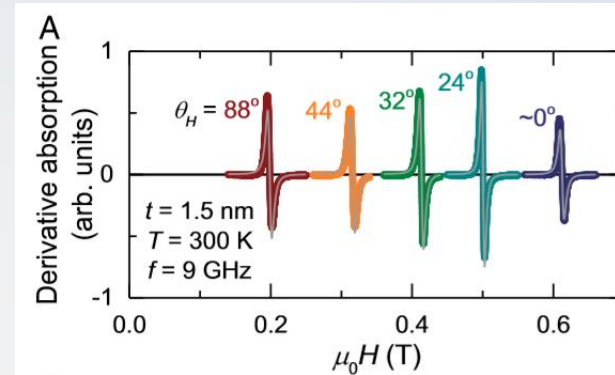
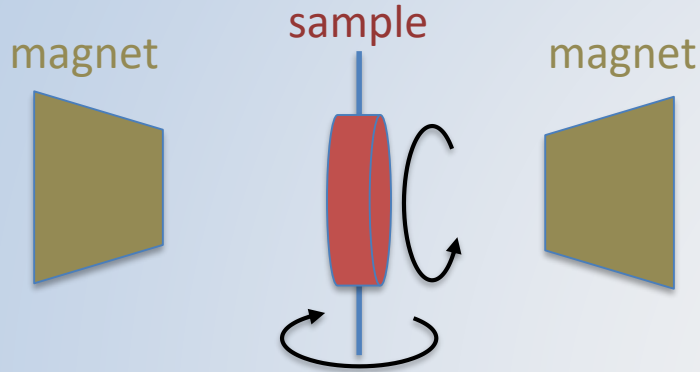
A prefactor (< 0.2) - function of electronic structure

μ_L orbital moment

P. Bruno, PRB 39, 865 (1989)



- Angular Dependence of Resonance Field (H_{res})



A. Okada, PNAS, 114, 3815 (2017)

- Frequency (f) Dependence of Resonance Field (H_{res})

Kittel Equation:

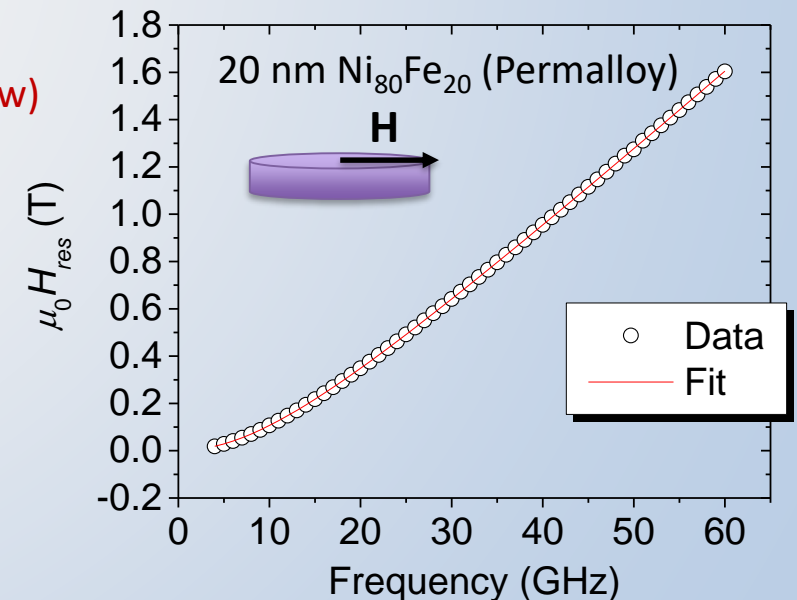
Can include anisotropy terms of any symmetry (see Farle, RPP (1998) for review)

$$f(H_{res}) = \frac{g \parallel \mu_0 \mu_B}{2\pi \hbar} \sqrt{(H_{res} + H_K)(H_{res} + M_{eff} + H_K)}$$

In-plane anisotropy field

Perpendicular anisotropy field

Effective Magnetization: $M_{eff} = M_s - H_K^\perp$



g -factor relates the spin (μ_S) and orbital (μ_L) moments:

$$g = 2 + \frac{2\mu_L}{\mu_S}$$

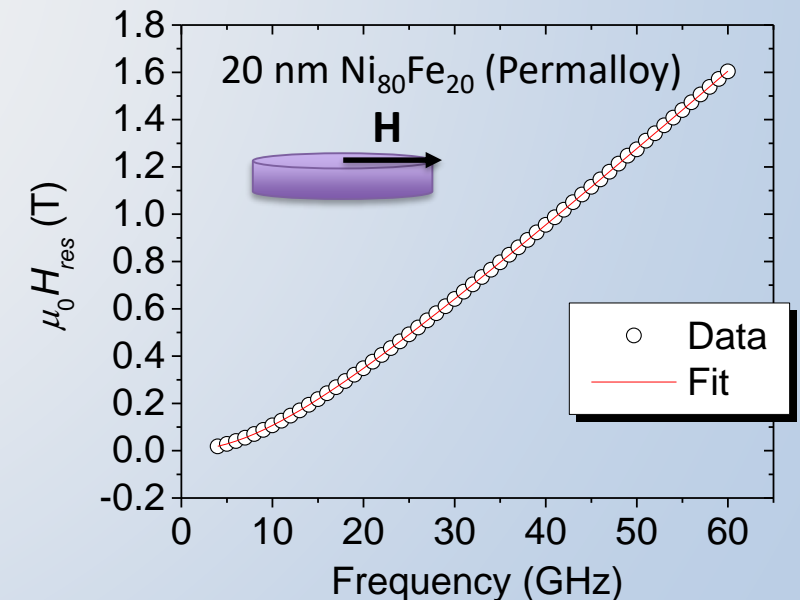
Since $\mu_S \gg \mu_L$, g is typically slightly larger than 2 in ferromagnets

- Frequency (f) Dependence of Resonance Field (H_{res})

Spectroscopic g -factor

$$f(H_{res}) = \frac{g^{\parallel} \mu_0 \mu_B}{2\pi\hbar} \sqrt{(H_{res} + H_K)(H_{res} + M_{eff} + H_K)}$$

Effective Magnetization: $M_{eff} = M_s - H_K^{\perp}$



g -factor relates the spin (μ_S) and orbital (μ_L) moments:

$$g = 2 + \frac{2\mu_L}{\mu_S}$$

Since $\mu_S \gg \mu_L$, g is typically slightly larger than 2 in ferromagnets

PROBLEM: A small error in g leads to large error in μ_L

Consider $g = 2.05 \pm 0.02$ (1% error)
 → 40% error in μ_L

PROBLEM: Reported values of g -factors can vary considerably

Permalloy Thickness	g -factor	Method	Frequency range	Reference
5–50 nm (extrapolated to bulk value)	2.109 ± 0.003	VNA-FMR with asymptotic analysis	4–60 GHz	This work
50 nm	2.20 ± 0.12	Einstein-de-Haas	—	[27]
50 nm	2.0–2.1	PIMM	0–2 GHz	[28]
50 nm	2.1	PIMM	0–3 GHz	[29]
10 nm	2.05	PIMM	0–3 GHz	[29]
bulk	2.12 ± 0.02	FMR	19.5 & 26 GHz	[30]
bulk	2.12	Einstein-de-Haas	—	[31]
4–50 nm	2.08 ± 0.01	FMR	not reported	[32]
bulk	2.08 ± 0.03	FMR	10 GHz	[9]
bulk	2.12 ± 0.03	FMR	24 GHz	[9]

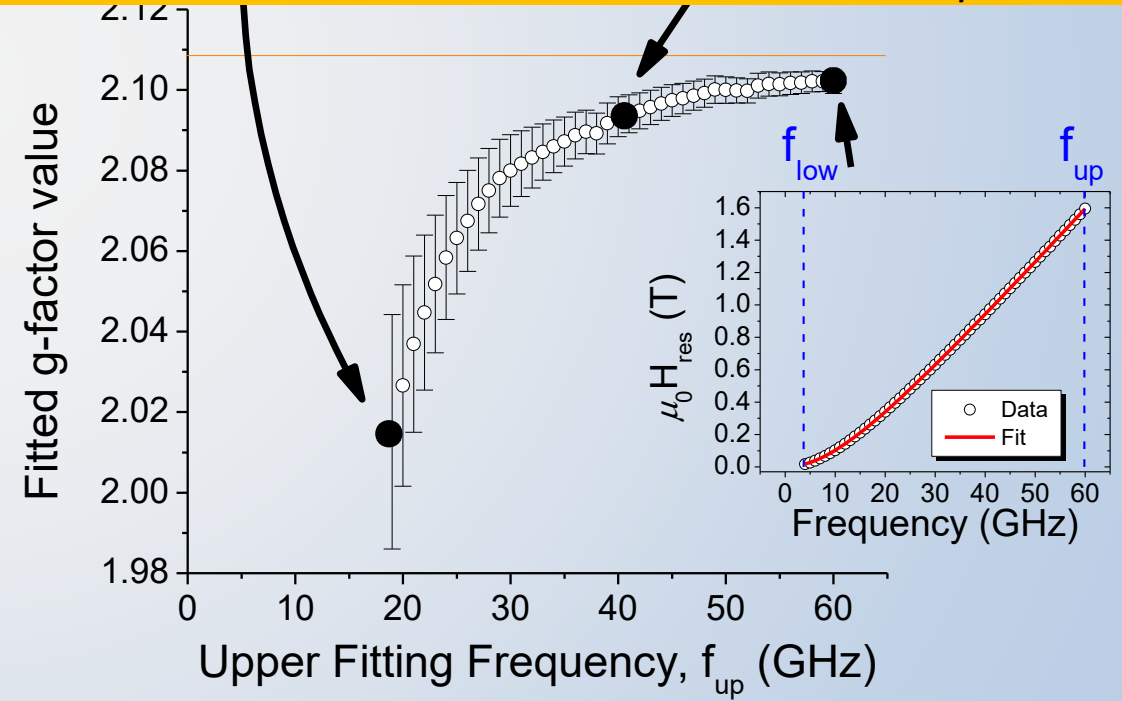
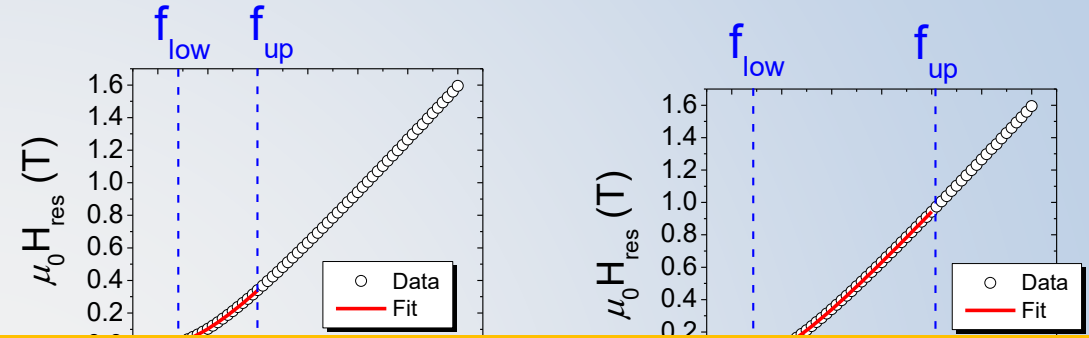
$$f(H_{res}) = \frac{g \mu_0 \mu_B}{2\pi \hbar} \sqrt{H_{res}(H_{res} + M_{eff})}$$

$$M_{eff} = M_s - \frac{2K}{\mu_0 M_s}$$

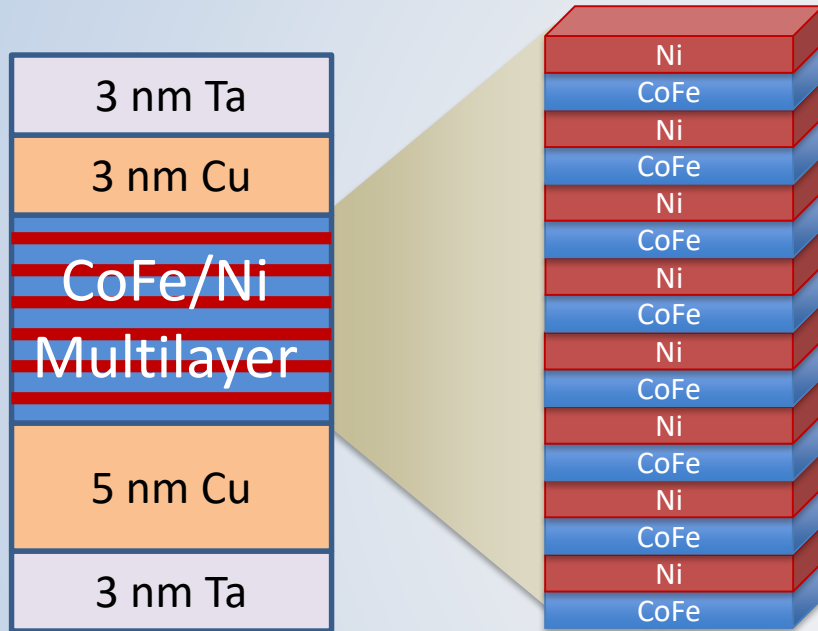
g_{fit} asymptotically approaches a value as $f_{up} \rightarrow \infty$

We make the assumption that the y-intercept (limit of $f_{up} \rightarrow \infty$) is the intrinsic value of g and M_{eff} .

Can achieve a precision better than 0.2 % in permalloy

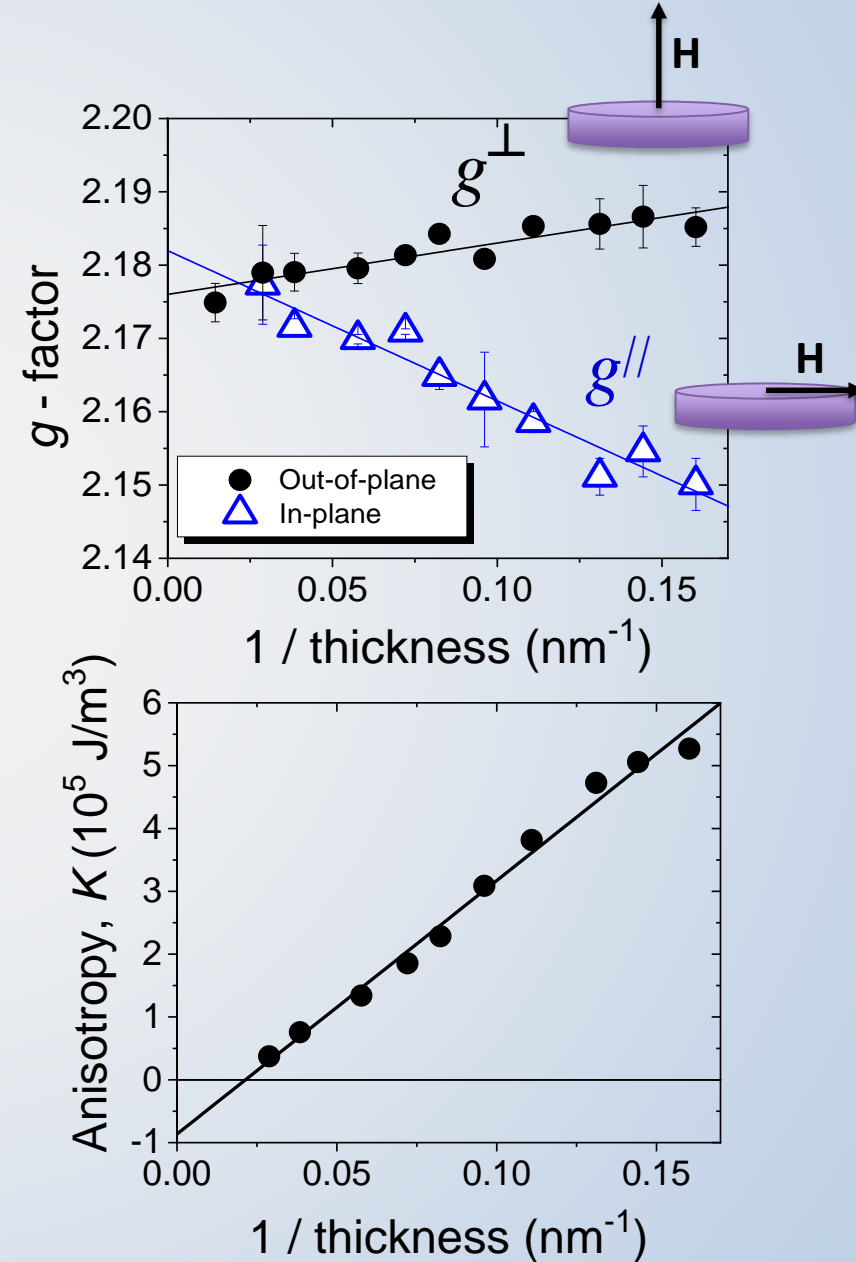


- Field misalignment
- Higher order anisotropy terms
- Rotatable (history dependent) anisotropy
- Pinning of local spins
 - Defects
 - Interfaces
- Excessive fitting parameters
- Any missing or field dependent term in Kittel eqn.



- Anisotropy is tuned by varying the thickness.

J.M. Shaw, *et al.*, Phys. Rev. B, 87, 054416 (2013)



A test of Bruno's theory:

$$K = - \left(A \frac{\xi_{SO} N}{4V} \right) \frac{(\mu_L^\perp - \mu_L^\parallel)}{\mu_B}$$

P. Bruno, PRB 39, 865 (1989)

- K anisotropy energy density
- ξ spin-orbit coupling constant
- A prefactor due to electronic structure
- N number atoms per unit cell
- V volume of unit cell

Fit to the data:

$$A = 0.097 \pm 0.007$$

Compare to previous reports:

$A = 0.2$ at RT, Au/Co/Au

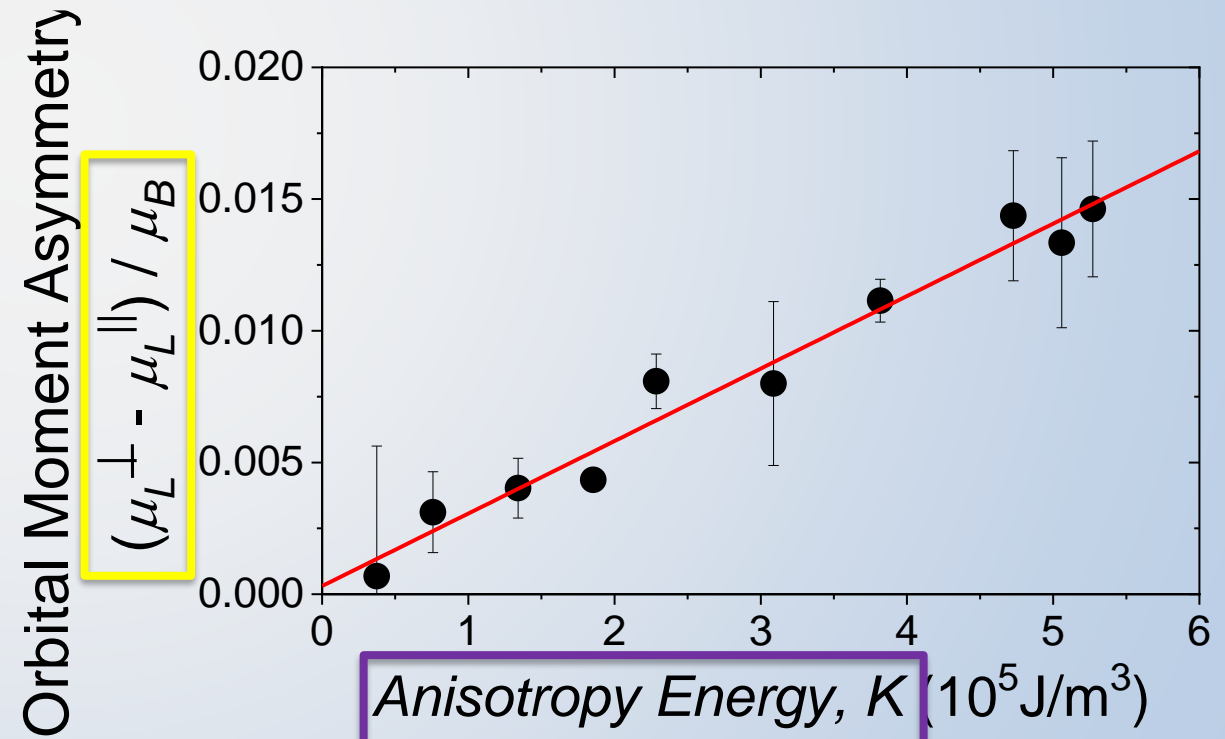
D. Weller, et al. PRL 75, 3752 (1995)

$A = 0.1$ at near 0 K, Ni/Pt MLs

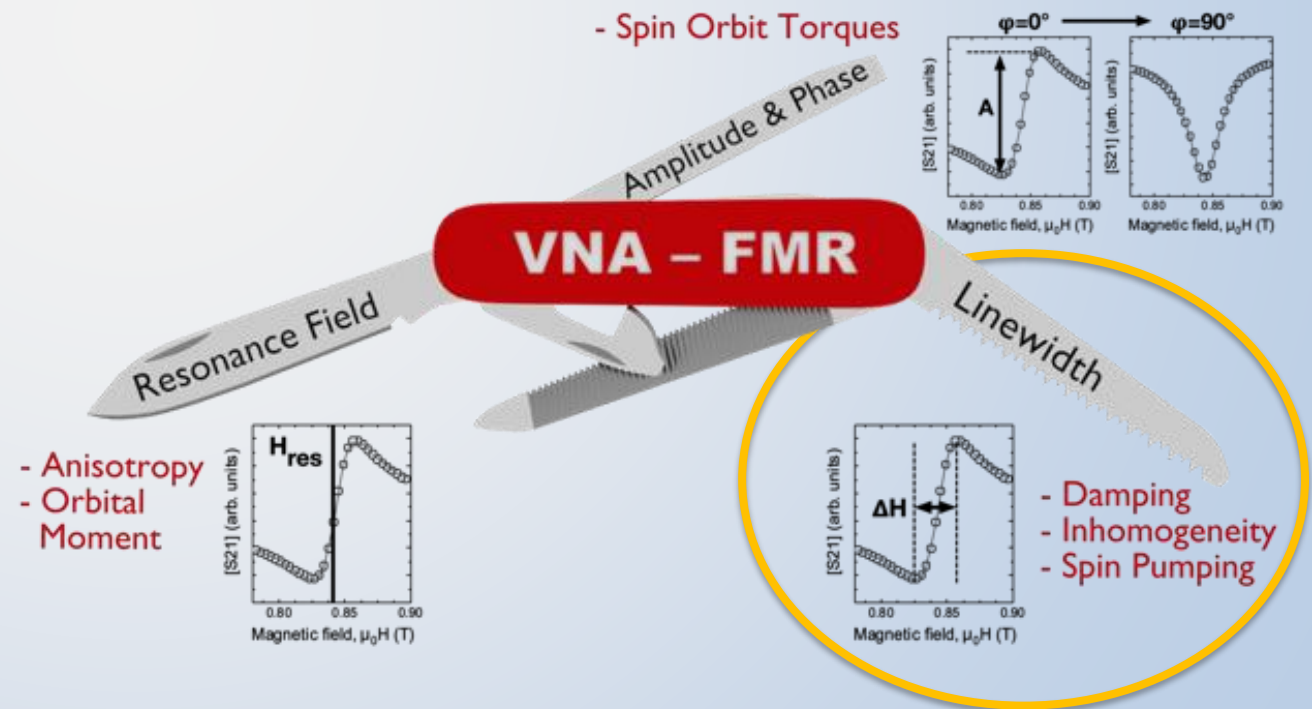
F. Wilhelm, et al. PRL 75, 3752 (1995)

$A = 0.05$ at near 0 K, Fe/V MLs

A. Anisimov, et al. PRL 82, 2390 (1999)

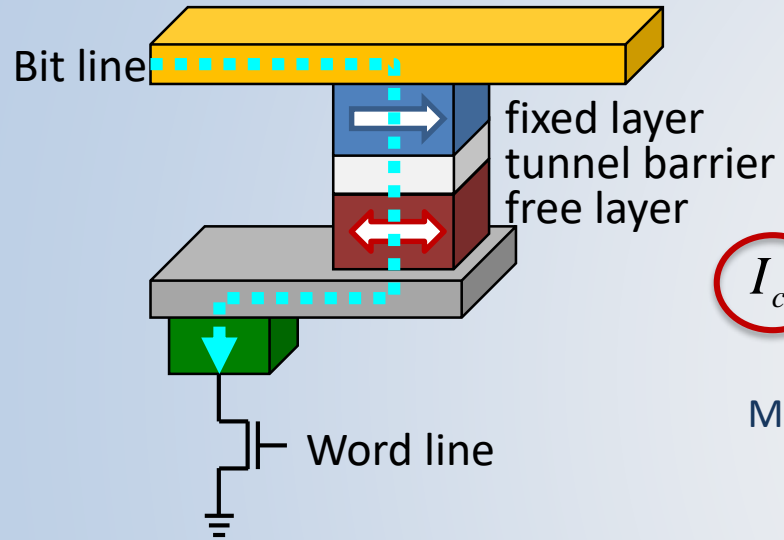


- Spin-Orbit Interaction
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Data Storage & Magnetic Memory (STT-RAM)

2-terminal Spin-Transfer Torque (STT)

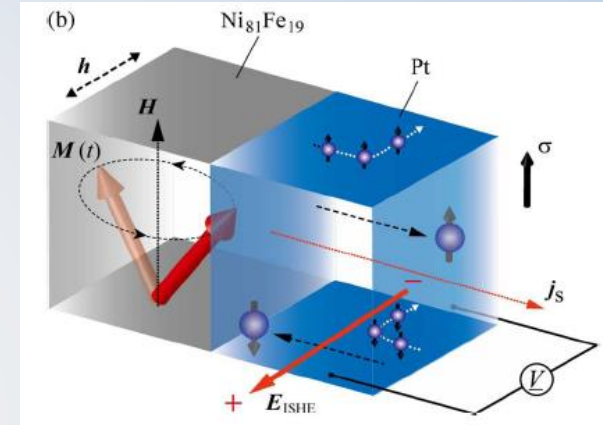


Critical current needed to switch an MRAM cell

$$I_{c0} = \left(\frac{2e}{\hbar} \right) \alpha M_s V g(\theta) p H_{eff}$$

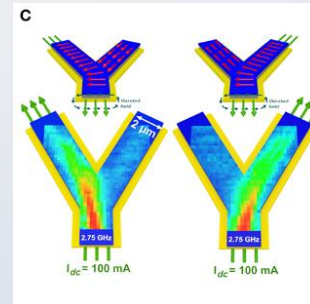
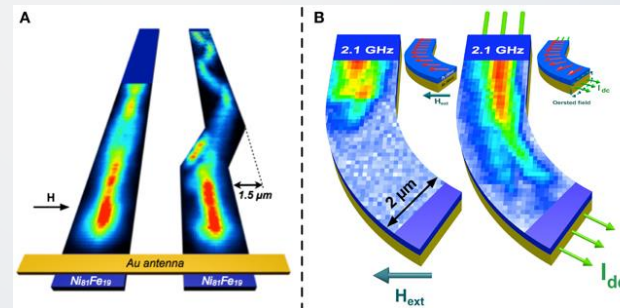
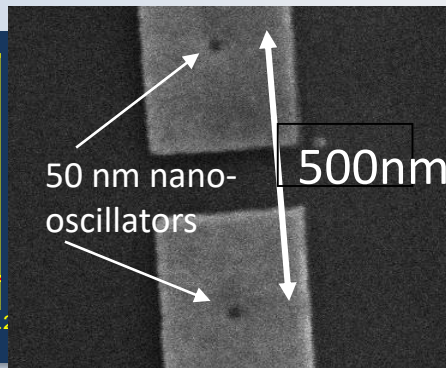
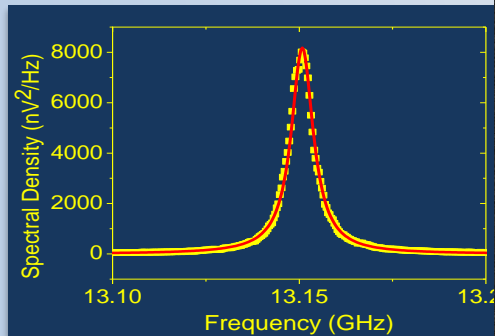
Mangin APL (2009)

Spin current source



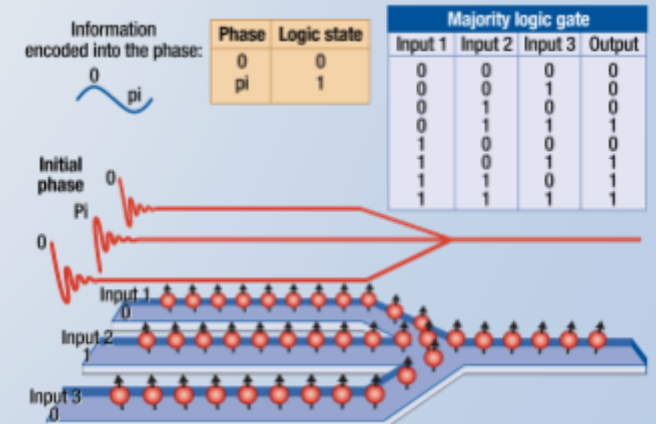
Nakayama, IEEE Trans Mag. (2010)

Spin-torque nano-oscillators



H.Schultheiss, HZDR

Magnonics and Spin Logic



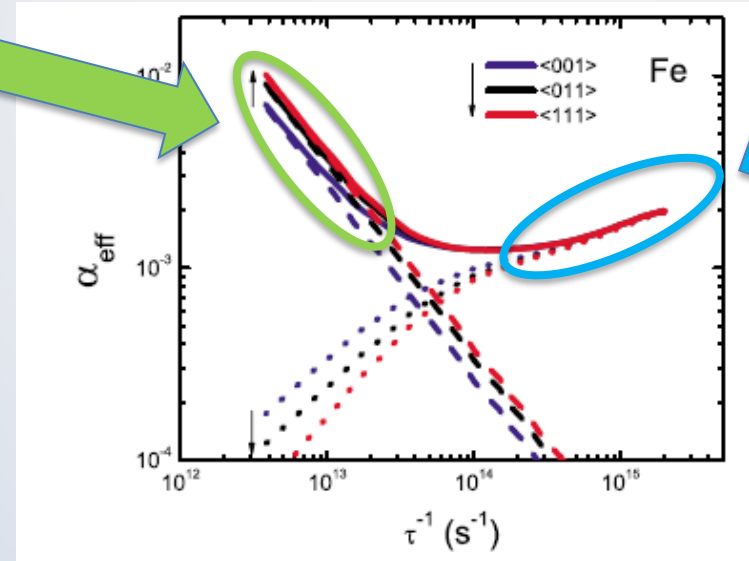
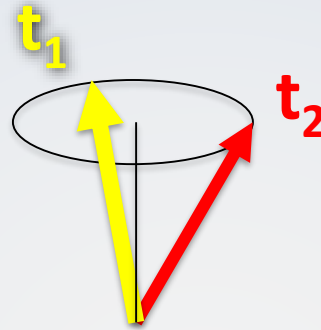
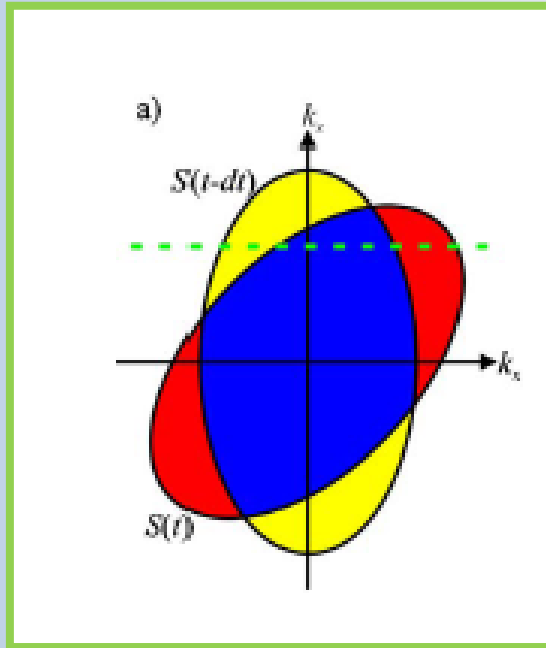
K.Wang UCLA26

$$\frac{d\vec{M}}{dt} = -|\gamma|\mu_0(\vec{M} \times \vec{H}) - \frac{\alpha}{M_s} |\gamma|\mu_0 [\vec{M} \times (\vec{M} \times \vec{H})]$$

- Breathing Fermi surface model:
 Kamberský, V. *Czechoslovak Journal of Physics B* **34**, 1111–1124 (1984)
 Kamberský, V. *Czechoslovak Journal of Physics B* **26**, 1366–1383 (1976)
 Kambersky, V. & Patton, C. E. *Phys. Rev. B* **11**, 2668–2672 (1975)
- Generalized torque correlation model:
 Gilmore, K., Idzerda, Y. U. & Stiles, M. D. *Phys. Rev. Lett.* **99**, 027204 (2007)
 Thonig, D. & Henk, J. *New J. Phys.* **16**, 013032 (2014)
- Scattering theory:
 Brataas, A., Tserkovnyak, Y. & Bauer, G. E. W. *Phys. Rev. Lett.* **101**, 037207 (2008)
 Liu, Y., Starikov, A. A., Yuan, Z. & Kelly, P. J. *Phys. Rev. B* **84**, 014412 (2011)
- Numerical realization of torque correlation via linear response:
 Mankovsky, S., Ködderitzsch, D., Woltersdorf, G. & Ebert, H. *Phys. Rev. B* **87**, 014430 (2013)
- First principles calculations:
 M. C. Hickey & J. S. Moodera, *Phys. Rev. Lett.* **102**, 137601 (2009)
 Ritwik Mondal,* Marco Berritta, and Peter M. Oppeneer, *Phys. Rev. B* **94**, 144419 (2016)

Intraband

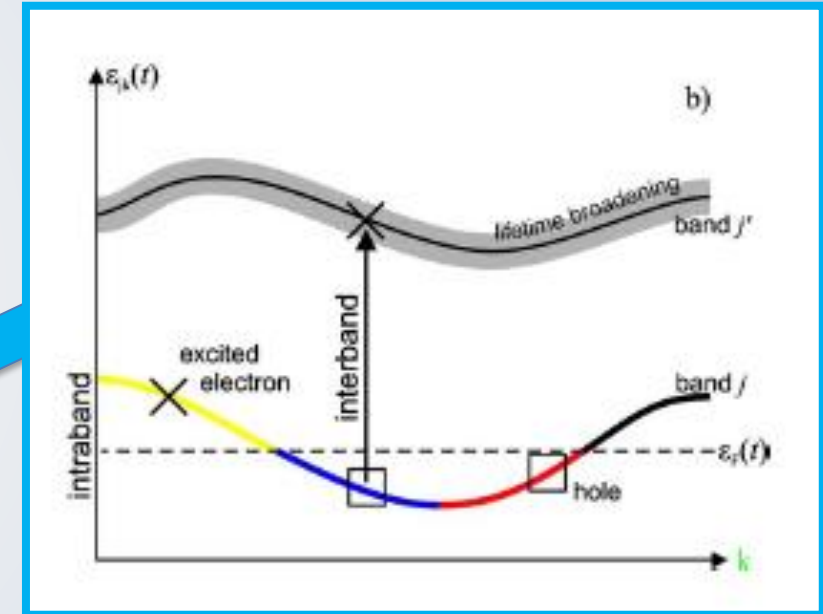
“Breathing Fermi Surface”
“Conductivity-like damping”



Inverse scattering time ($1/\tau$)
Temperature →
Defect density →

Interband

“Bubbling Fermi Surface”
“Resistivity-like damping”



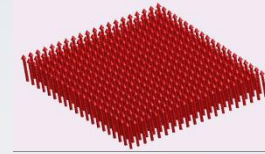
Kamberský's Torque Correlation model:

Sum over all electronic states, bands

$$\alpha \propto \left\langle \sum_{m,n} |\Gamma_{mk,nk}^-|^2 W_{mk,nk} \right\rangle_k$$

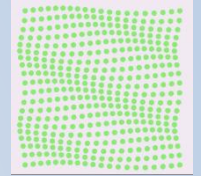
Torque between spin and orbital moments $\propto \xi_{SO}$

uniform mode



spin-orbit damping

dissipation in lattice



Courtesy of Claudia Mewes

spectral overlap

function of Bloch state lifetime

Critical Parameters affecting intrinsic damping:

$N(E_F)$: Density of states at the Fermi energy, E_F

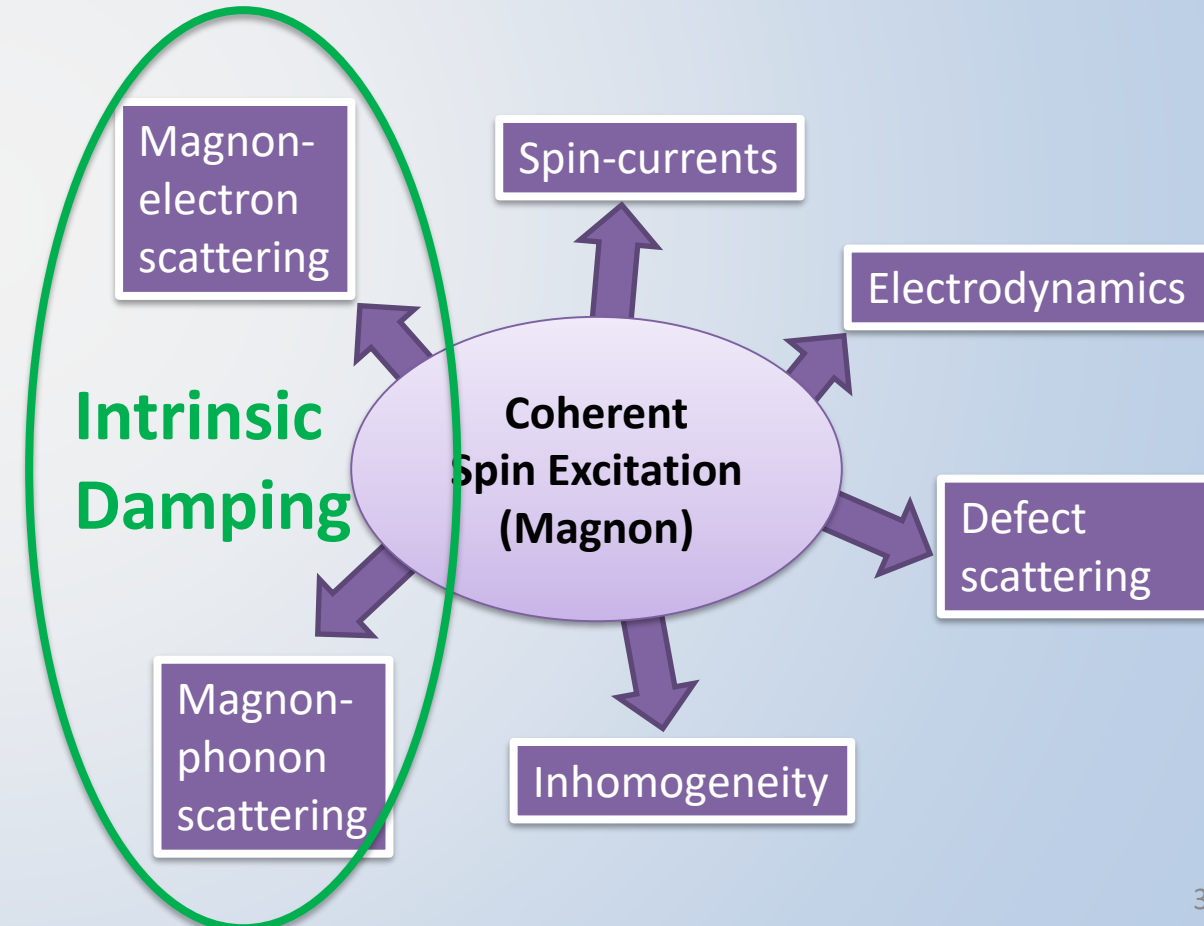
ξ_{SO} : Spin-Orbit Interaction

τ : Spin scattering times

$$\frac{d\vec{M}}{dt} = -|\gamma|\mu_0(\vec{M} \times \vec{H}) - \frac{\alpha}{M_s} |\gamma|\mu_0 [\vec{M} \times (\vec{M} \times \vec{H})]$$

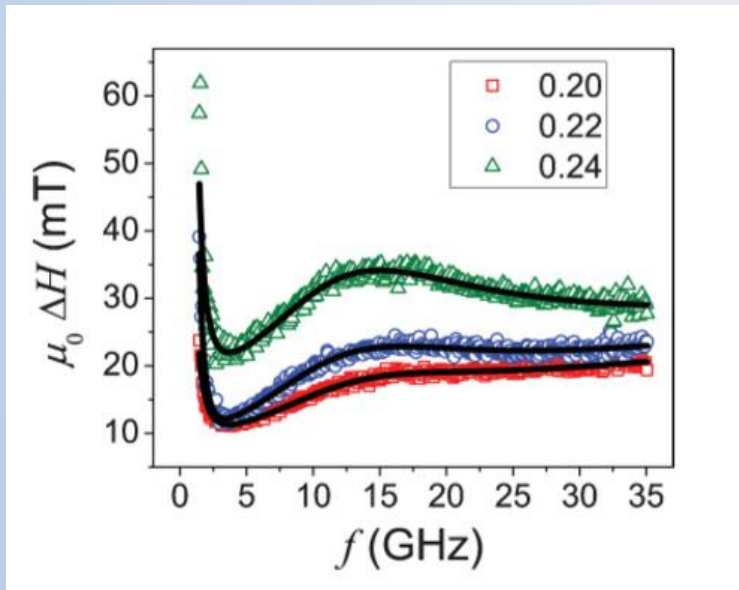
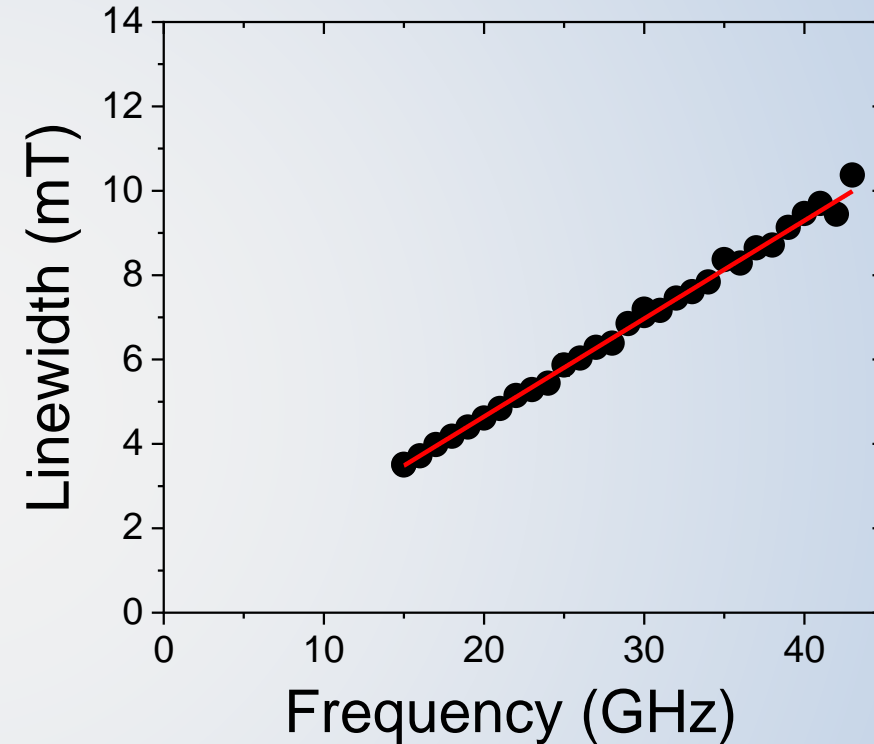
- Originally just a phenomenological parameter
- Theory has worked to calculate damping parameter α from first principles

In reality, α includes **many** intrinsic and extrinsic sources and is not necessarily a constant



LL equation predicts linewidth is proportional to frequency

$$\Delta H = \frac{2h\alpha}{g\mu_0\mu_B} f$$



However, that is not always observed

- Inhomogeneous Broadening
- Low-field losses
- 2-magnon scattering
- Spin-pumping
- Radiative Damping
- k^2 Damping
- Other Contributions
 - Eddy Currents
 - Slow relaxer
 - Motional Narrowing
 - Chiral Damping
- Intrinsic Damping

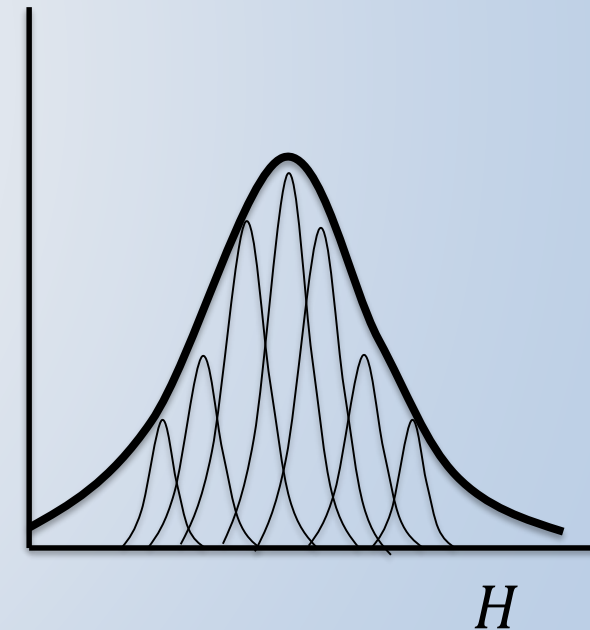
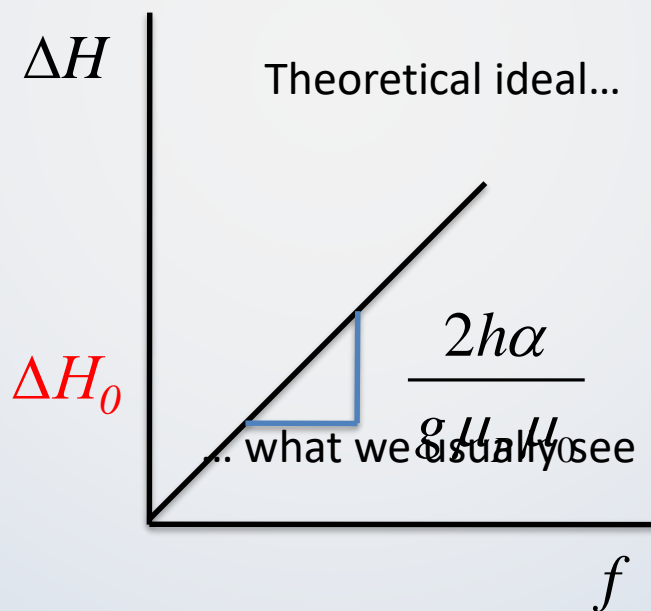
- **Many** relaxation mechanisms and contributions to linewidth exist
- Careful separation and quantification of all mechanisms is needed to compare with theory

Point of emphasis:
Broadband measurements are critical.

- Inhomogeneous Broadening
 - Low-field losses
 - 2-magnon scattering
 - Spin-pumping
 - Radiative Damping
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$$\Delta H = \frac{2h\alpha}{g\mu_0\mu_B} f + \Delta H_0$$

Inhomogeneous Linewidth

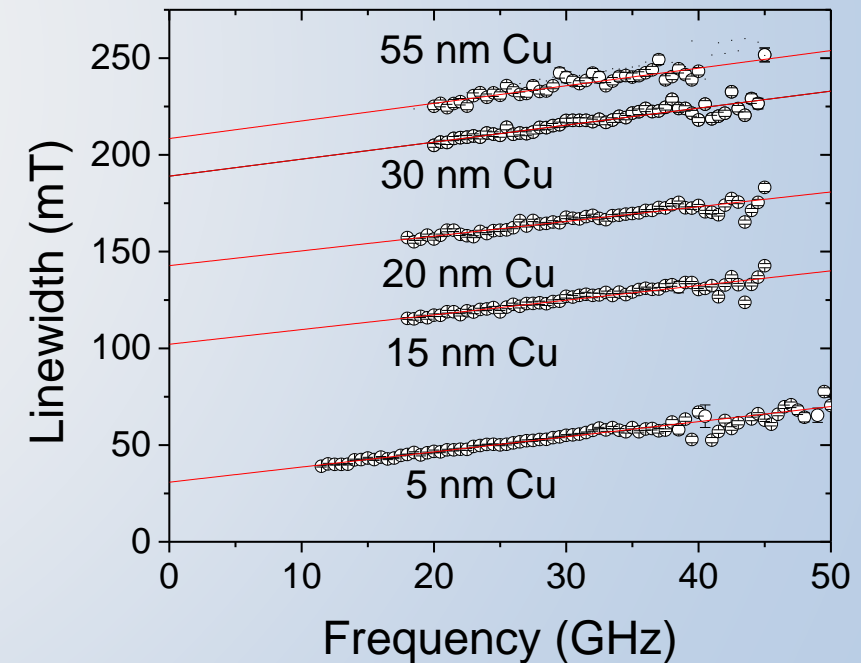
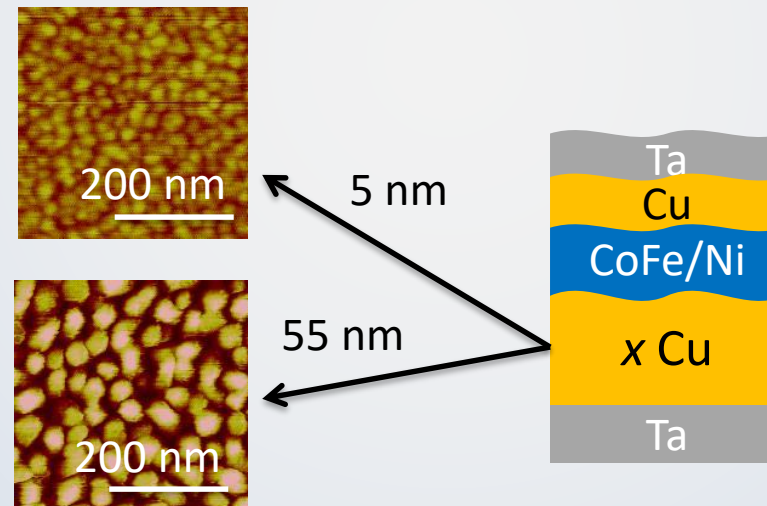


Heinrich, JAP, 57, 3690 (1985)
 Farle, Rep. Prog. Phys. 61, 755 (1998)
 McMichael, PRL 90, 227601 (2003)

- Inhomogeneous Broadening
 - Low-field losses
 - 2-magnon scattering
 - Spin-pumping
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$$\Delta H = \frac{2h\alpha}{g\mu_0\mu_B} f + \Delta H_0$$

Inhomogeneous Linewidth



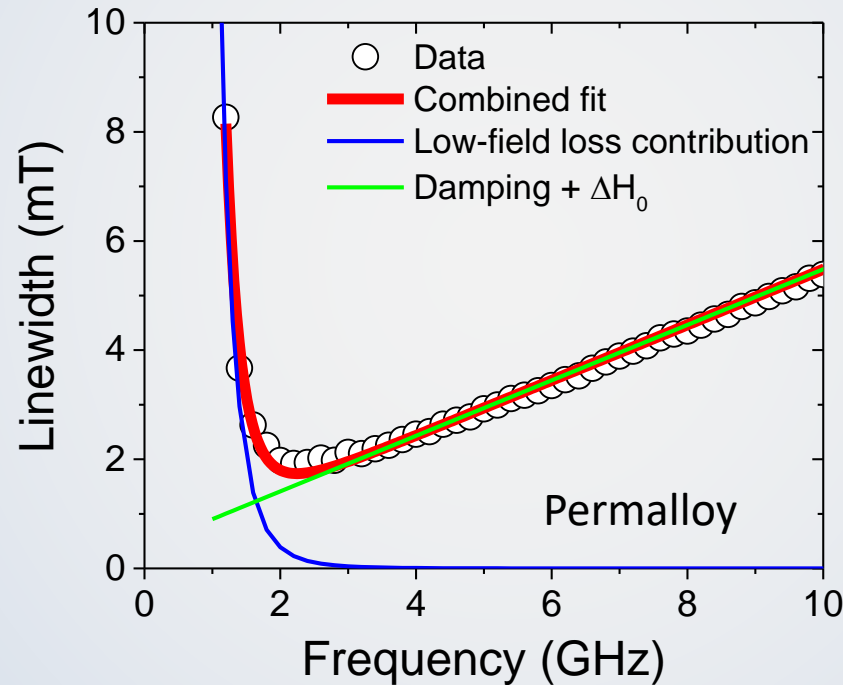
Heinrich, JAP, 57, 3690 (1985)
 Farle, Rep. Prog. Phys. 61, 755 (1998)
 McMichael, PRL 90, 227601 (2003)

- Inhomogeneous Broadening
- Low-field losses
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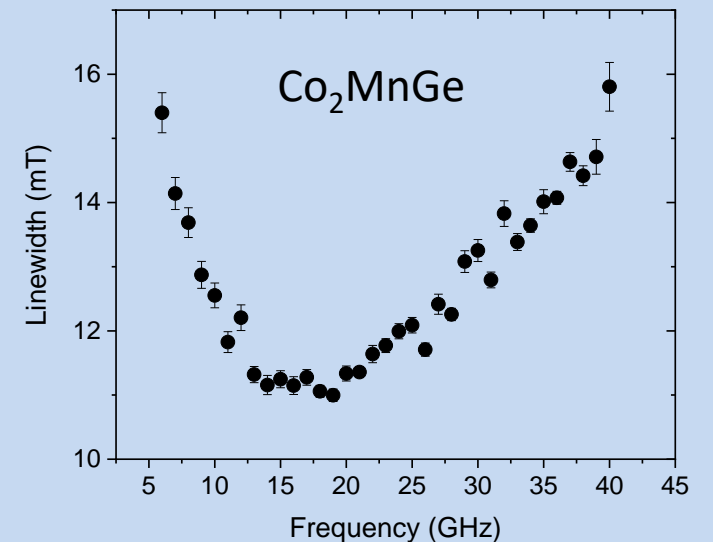
- At low fields (frequency), sample may not be saturated.
 - ➔ Linewidth Broadening

$$\Delta H_{low-field} = \frac{\beta}{f^n}$$

- Described by a power law fit

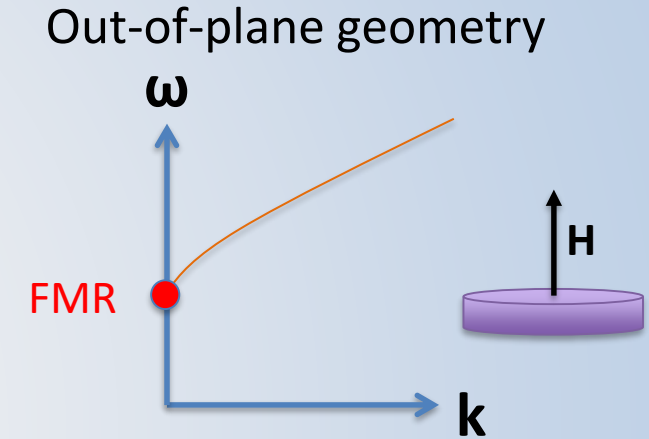
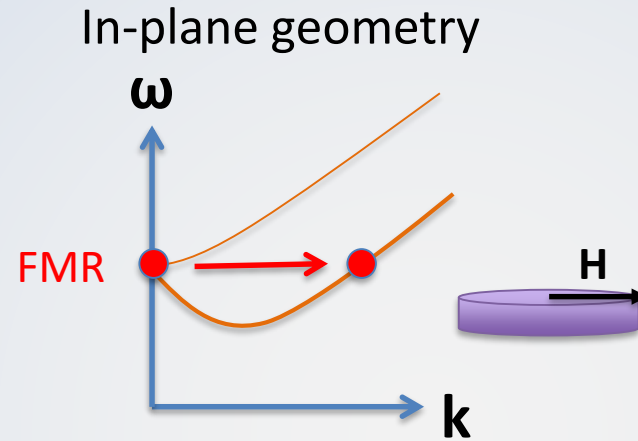


- Effect can extend to higher frequencies for some materials

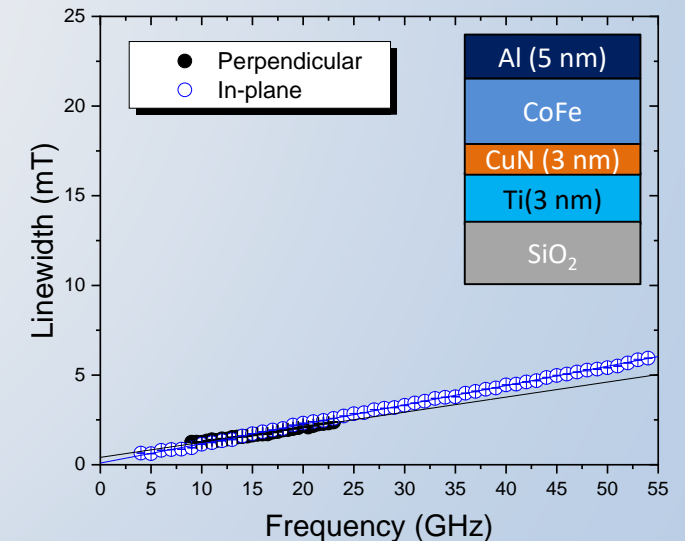
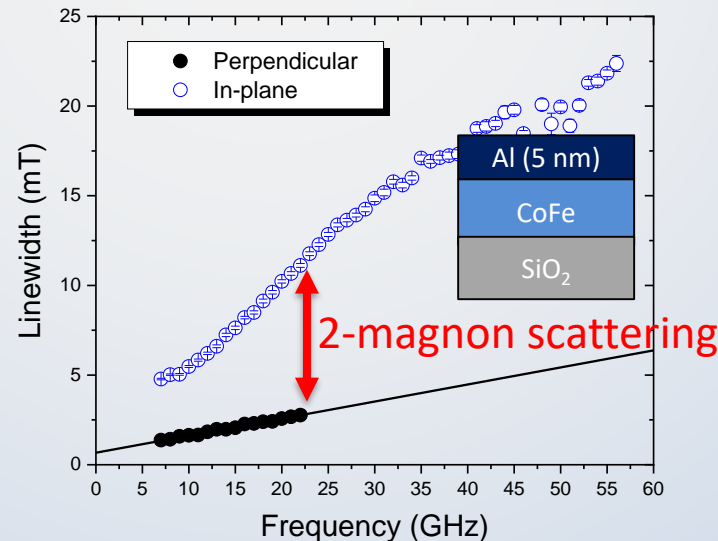


- Inhomogeneous Broadening
- Low-field losses
- 2-magnon scattering**
- Spin-pumping
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- Mediated by Defect Scattering



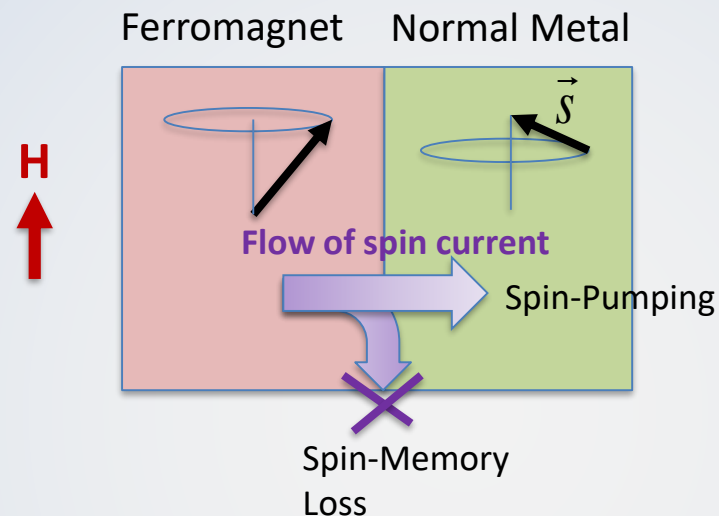
- Can reduce/eliminate with out-of-plane geometry



Sparks, Phys Rev. 122, 791 (1961)
 Hurben, JAP 83, 4344 (1989)
 McMichael, JAP 91, 8647 (2002)
 Lindner, PRB 68, 060102 (2003)
 Barsukov, PRB 84, 140410 (2011)

- Inhomogeneous Broadening
- Low-field losses
- 2-magnon scattering
- Spin-pumping**
- Radiative Damping
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Loss of angular momentum at or across an interface



Can be phenomenologically treated as an interfacial damping term

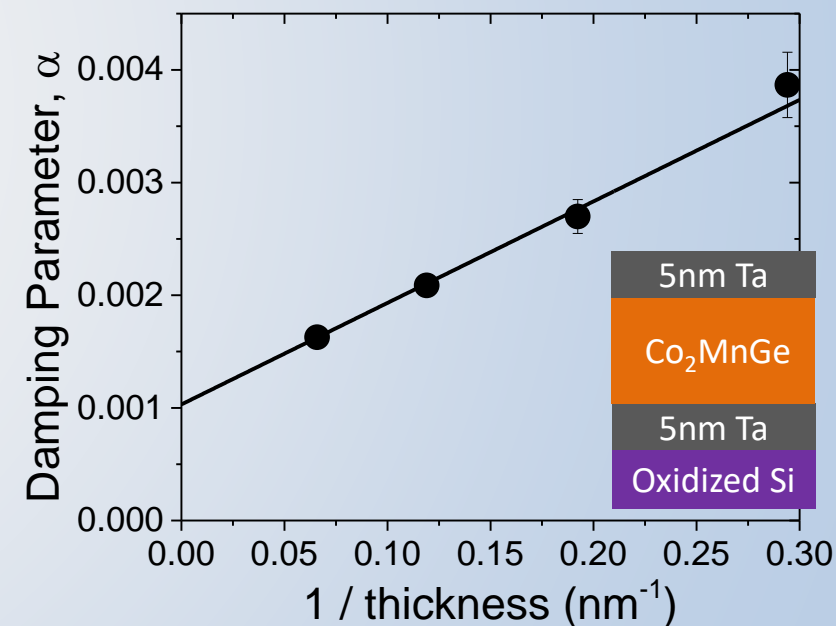
$$\alpha(t) = \alpha_{int} + g\mu_B \frac{g_{eff}^{\uparrow\downarrow}}{4\pi M_s} \frac{1}{t}$$

t = thickness

g = g-factor

$g^{\uparrow\downarrow}$ = effective real part spin-mixing conductance

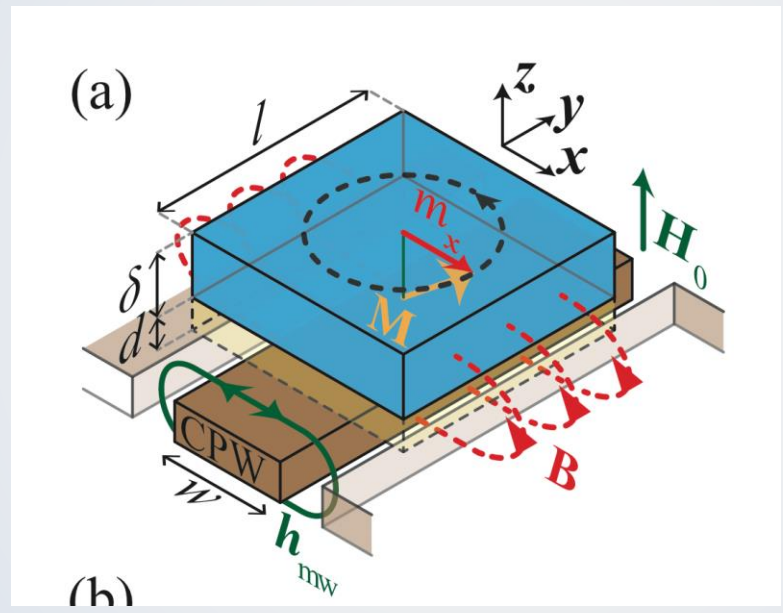
y-intercept is the damping without spin-pumping contribution



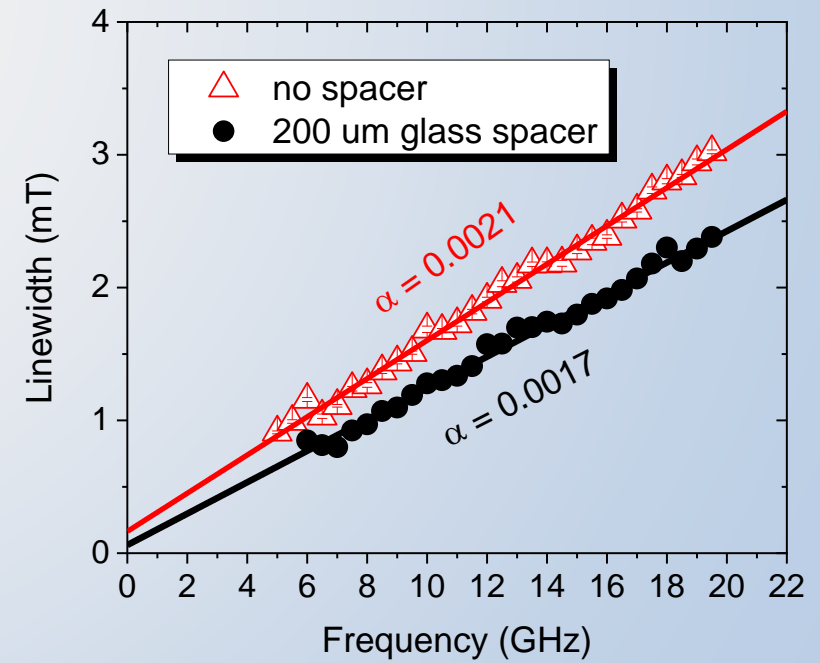
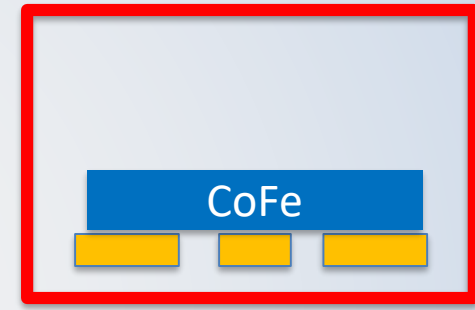
- Inhomogeneous Broadening
- Low-field losses
- 2-magnon scattering
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Damping contribution due to inductive coupling of the sample to the waveguide

30 nm $\text{Co}_{25}\text{Fe}_{75}$ Sample



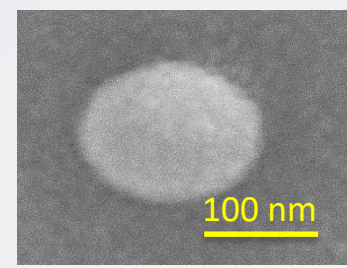
δ = thickness
 Z_0 = waveguide impedance



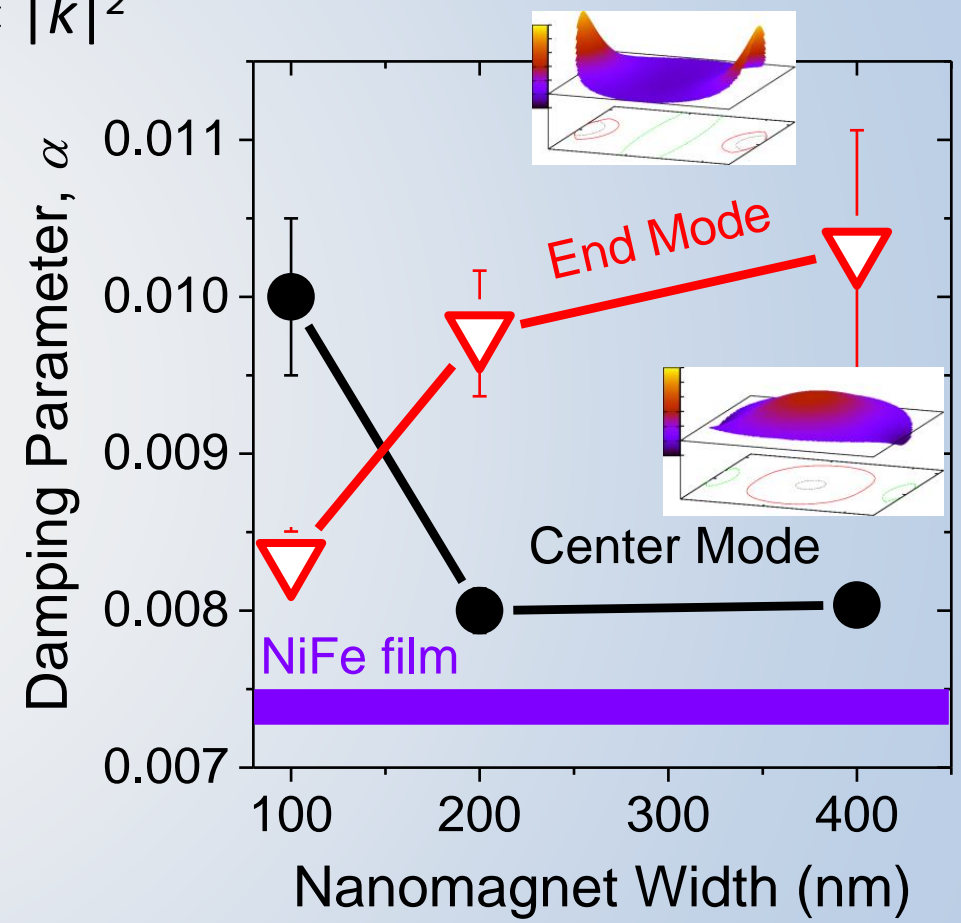
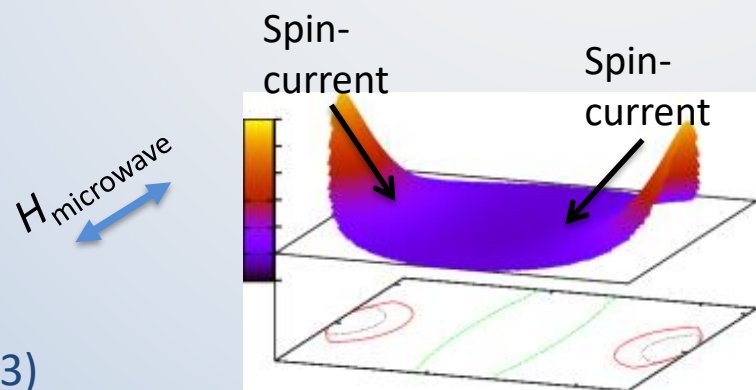
- Inhomogeneous Broadening
- Low-field losses
- 2-magnon scattering
- Spin-pumping
- Radiative Damping
- k^2 Damping
- Other Contributions
 - Eddy Currents
 - Slow relaxer
 - Motional Narrowing
 - Chiral Damping
- Intrinsic Damping

Theory predicts a wavevector (k) dependence of damping $\propto |k|^2$

Y. Tserkovnyak Phys. Rev. B 79, 094415 (2009)
 S. Zhang Phys. Rev. Lett., 102, 086601 (2009)

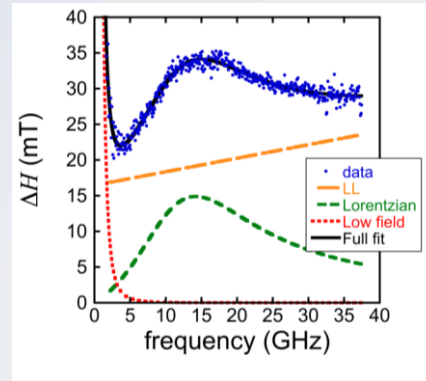


→ Generation of intralayer spin currents



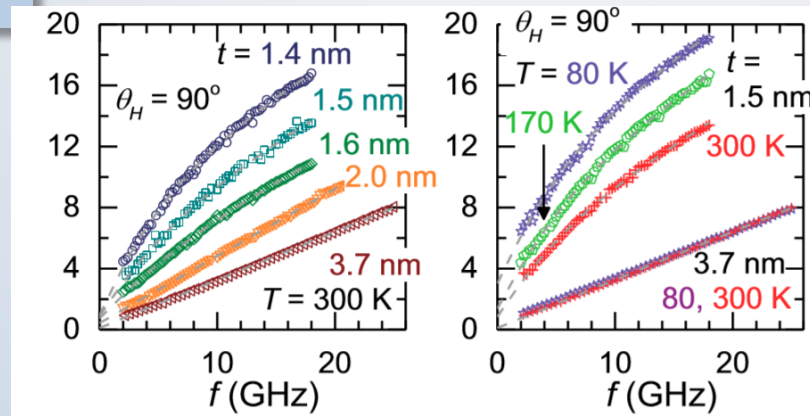
- Inhomogeneous Broadening
- Low-field losses
- 2-magnon scattering
- Spin-pumping
- Radiative Damping
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- Other Contributions
 - Eddy Currents
 - Slow relaxer
 - Motional Narrowing
 - Chiral Damping
- Intrinsic Damping

Slow Relaxer (Resonant Damping)



Van Vleck, PRL 11, 65 (1963).
 Woltersdorf, PRL 102, 257602 (2009)
 Nembach, PRB, 84, 054424 (2011)

Motional Narrowing



A. Okada, PNAS, 114, 3815 (2017)

Eddy Currents

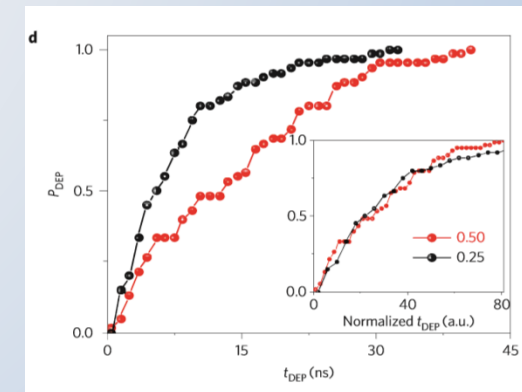
$$\alpha^{\text{eddy}} = \frac{C \gamma \mu_0^2 M_s \delta^2}{8 \rho}$$

δ = thickness
 ρ = resistivity
 C = correction factor

Generally not significant for metallic thin films < 20 nm

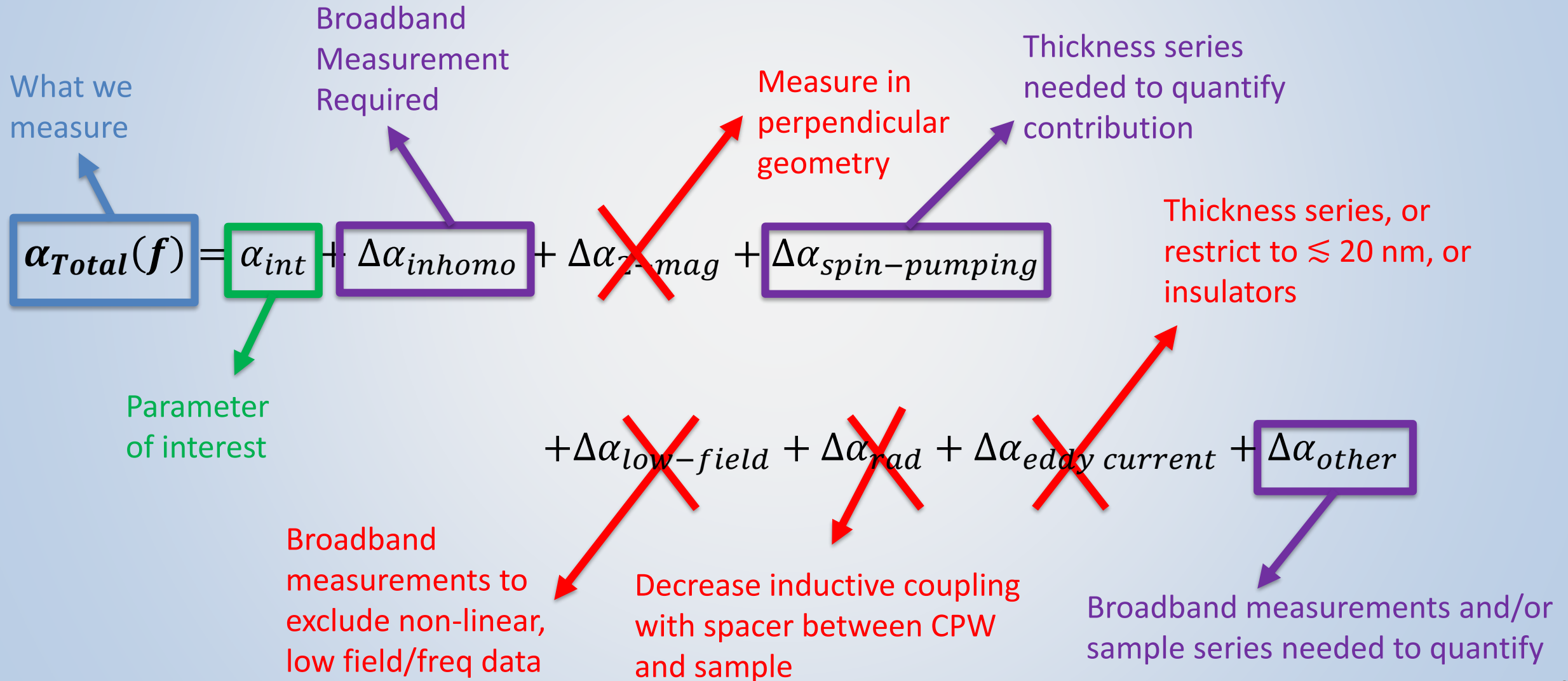
J. M. Lock, British JAP 17, 1645 (1966)
 C. Scheck, APL 88, 252510 (2006)

Chiral Damping

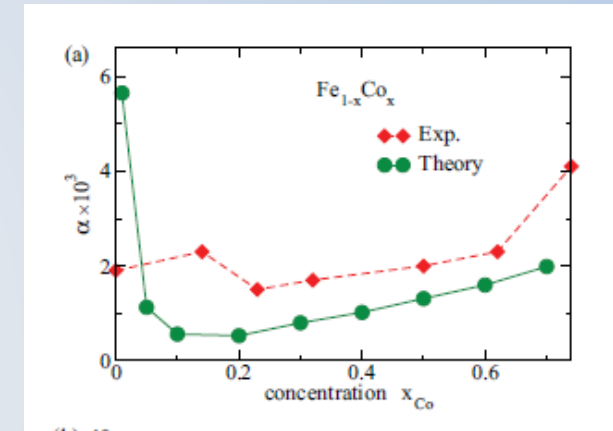
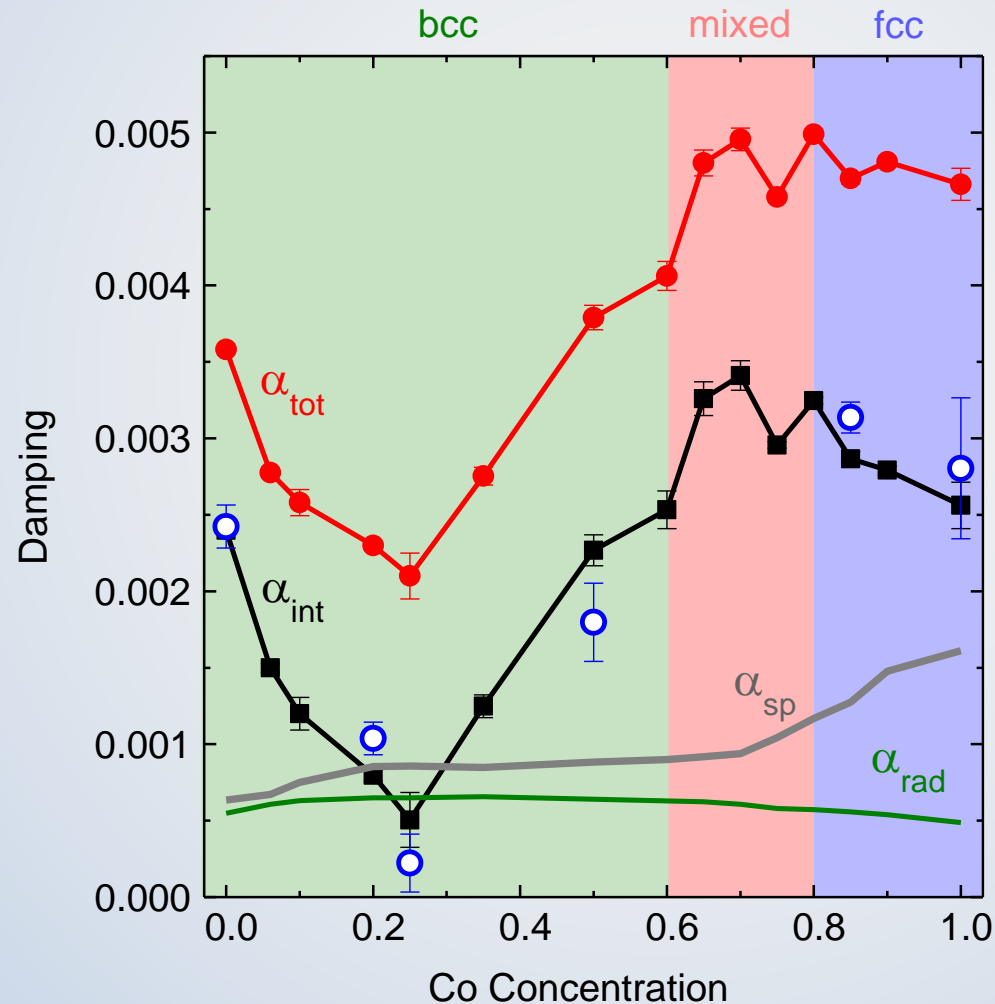


E. Jue, Nature Materials 15, 272 (2015)

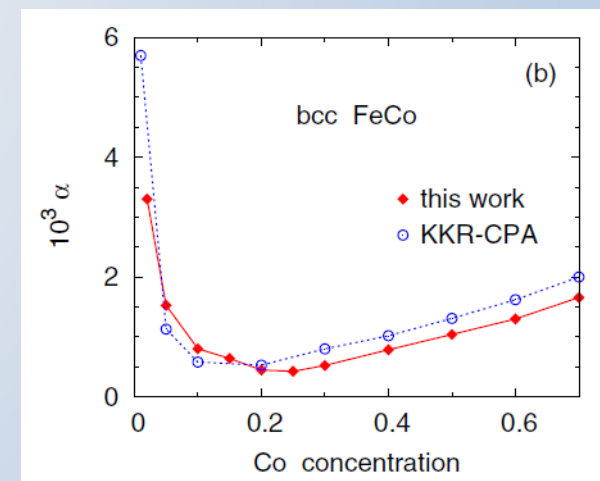
- To compare with theory, we must account for or eliminate additional damping terms.



Prediction of ultra-low damping ($\alpha \approx 0.0005$) in CoFe

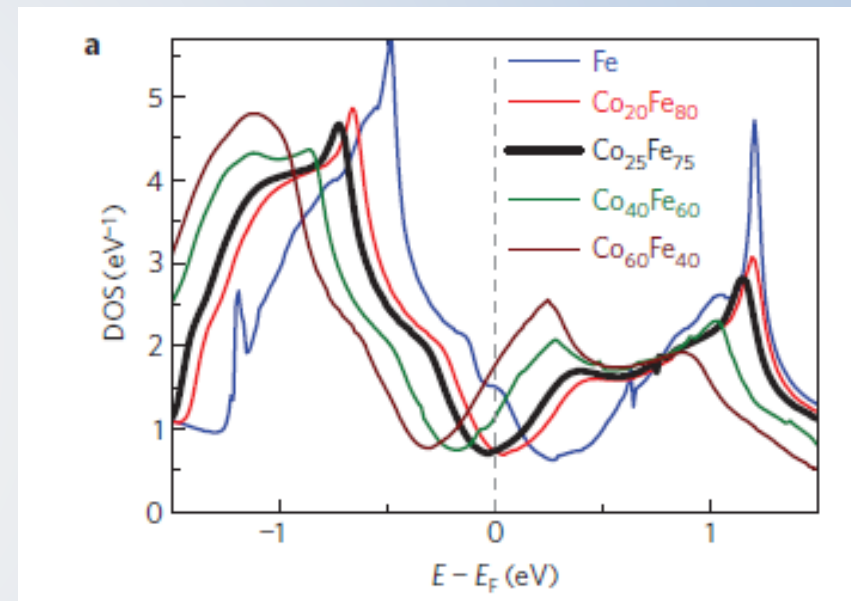
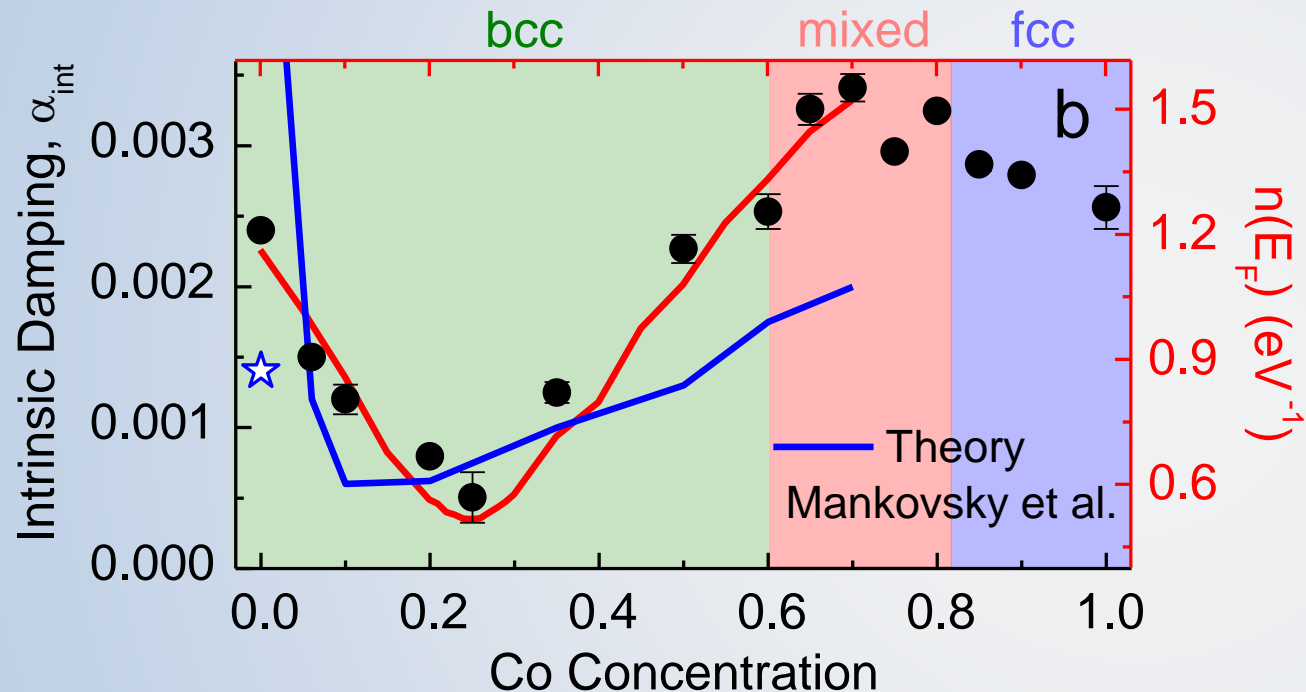


Mankovsky, PRB **87**, 014430 (2013)



Turek, PRB **92**, 214407 (2015) 43

Damping is strongly controlled by the DOS at E_F



Schoen, Nature Physics 12, 839 (2016)

ARTICLE

DOI: 10.1038/s41467-017-00332-x

OPEN

Metallic ferromagnetic films with magnetic damping under 1.4×10^{-3}

Aidan J. Lee¹, Jack T. Brangham¹, Yang Cheng¹, Shane P. White¹, William T. Ruane¹, Bryan D. Esser², David W. McComb², P. Chris Hammel¹ & Fengyuan Yang¹

APPLIED PHYSICS LETTERS 111, 132406 (2017)

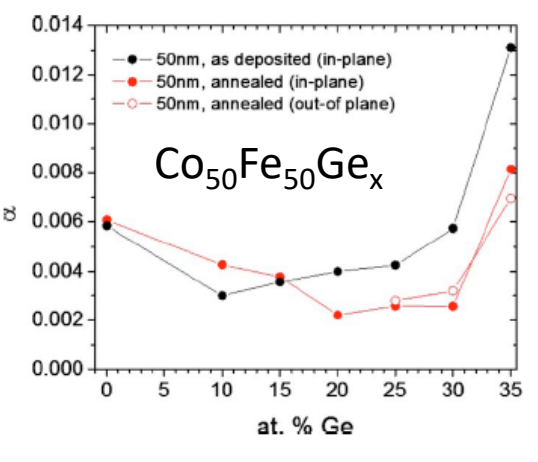
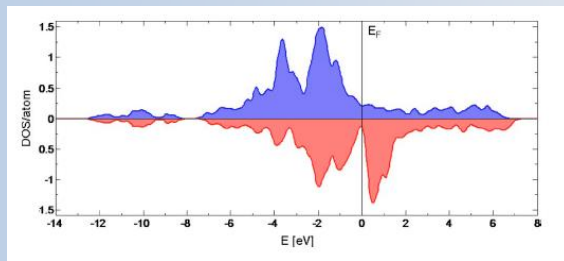


Magnetic damping in poly-crystalline $\text{Co}_{25}\text{Fe}_{75}$: Ferromagnetic resonance vs. spin wave propagation experiments

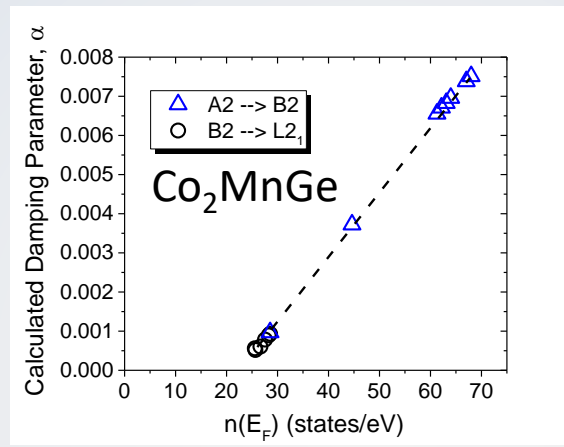
H. S. Körner, M. A. W. Schoen, T. Mayer, M. M. Decker, J. Stigloher, T. Weindler, T. N. G. Meier, M. Kronseder, and C. H. Back¹
 Institute of Experimental and Applied Physics, University of Regensburg, D-93040 Regensburg, Germany

(Received 4 July 2017; accepted 2 September 2017; published online 27 September 2017)

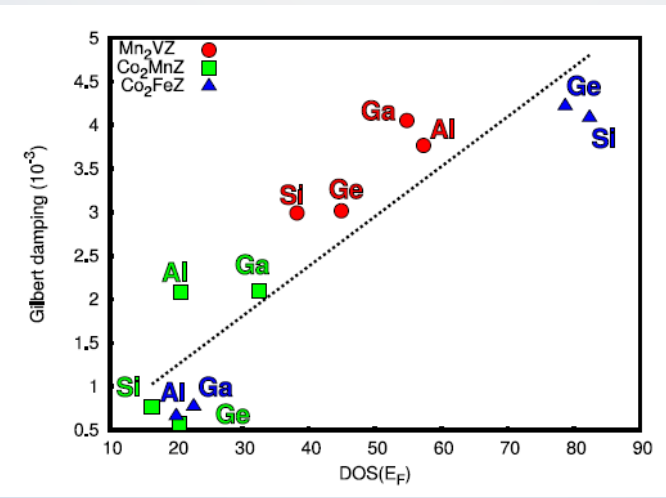
Alloying in Ge in $\text{Co}_{50}\text{Fe}_{50}$ enhances the “pseudo-gap” a moves it to the Fermi level



H.Lee, APL 95, 082502 (2009)



J.Shaw, PRB, 97, 094420 (2018)



J.Chico, PRB, 93, 214439 (2016)

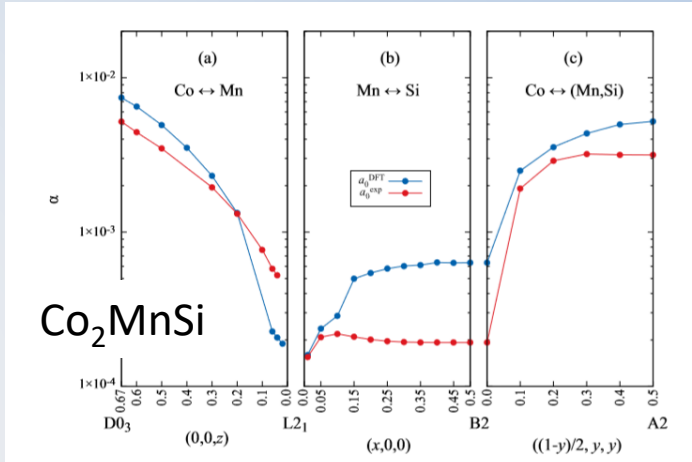
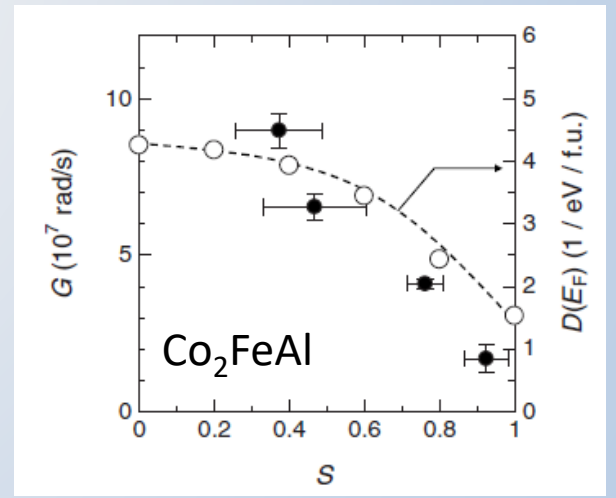


FIG. 7. Gilbert damping parameter α as a function of the disorder rates (x,y,z) and calculated with the two values of the lattice parameter.

Pradines, PRB, 95, 094425 (2017)

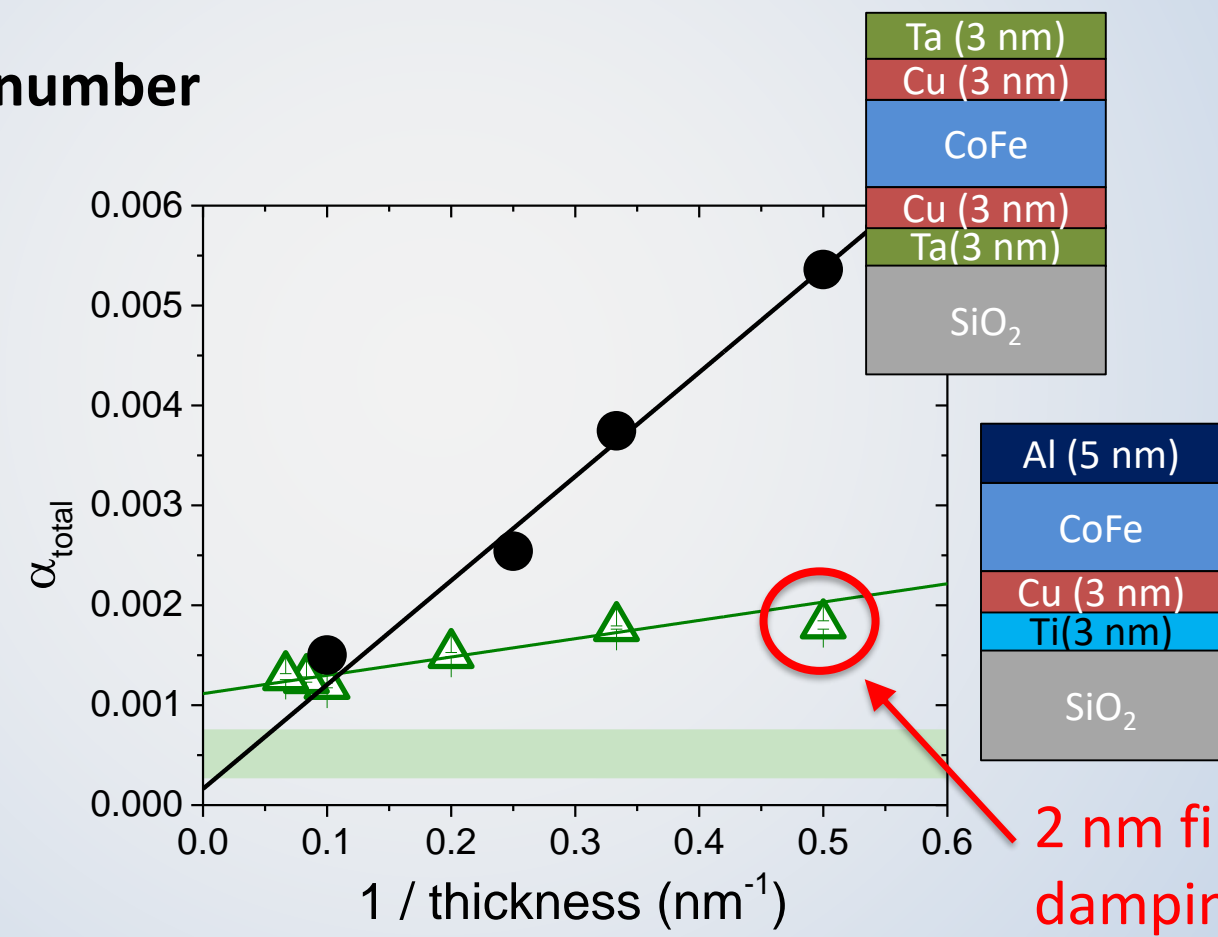


Mizukami, JAP, 105, 07D306 (2009)

How do we reduce spin pumping?

Replace Ta with low atomic number elements or insulators

11, 054036 (2019)



2 nm film with a **total** damping of 0.0018 !!!

Consider Relationship between Perpendicular Anisotropy (PMA) and Damping

APPLIED PHYSICS LETTERS 98, 082501 (2011)

Tunable magnonic frequency and damping in [Co/Pd]₃ multilayers with variable Co layer thickness

S. Pal,¹ B. Rana,¹ O. Hellwig,² T. Thomson,² and A. Barman^{1,a)}

¹Department of Material Sciences, S. N. Bose National Centre for Basic Sciences, Block JD, Sector III, Salt Lake, Kolkata 700 098, India

²San Jose Research Center, Hitachi Global Storage Technologies, 3403 Yerba Buena Rd., San Jose, California 95135, USA

Applied Physics Express 4 (2011) 013005
DOI: 10.1143/APEX.4.013005

Gilbert Damping in Ni/Co Multilayer Films Exhibiting Large Perpendicular Anisotropy

Shigemi Mizukami^{*}, Xianmin Zhang, Takahide Kubota, Hiroshi Naganuma¹, Mikihiro Oogane¹, Yasuo Ando¹, and Terunobu Miyazaki

WPI Advanced Institute for Materials Research, Tohoku University, Sendai 980-8577, Japan
¹Department of Applied Physics, Graduate School of Engineering, Tohoku University, Sendai 980-8579, Japan
Received November 17, 2010; accepted December 14, 2010; published online January 7, 2011

3036 IEEE TRANSACTIONS ON MAGNETICS, VOL. 47, NO. 10, OCTOBER 2011

Time-Resolved Magnetization Dynamics and Damping Constant of Sputtered Co/Ni Multilayers

T. Kato¹, Y. Matsumoto¹, S. Okamoto², N. Kikuchi², O. Kitakami², N. Nishizawa³, S. Tsunashima⁴, and S. Iwata¹

¹Department of Quantum Engineering, Nagoya University, Nagoya 464-8603, Japan
²Institute of Multidisciplinary Research for Advanced Materials, Tohoku University, Sendai 980-8577, Japan
³Department of Electrical Engineering and Computer Science, Nagoya University, Nagoya 464-8603, Japan
⁴Department of Research, Nagoya Industrial Science Research Institute, Nagoya 464-0819, Japan

APPLIED PHYSICS LETTERS 102, 102401 (2013)

Observation of the intrinsic Gilbert damping constant in Co/Ni multilayers independent of the stack number with perpendicular anisotropy

Hyon-Seok Song,¹ Kyeong-Dong Lee,¹ Jeong-Woo Sohn,^{1,2} See-Hun Yang,³ Stuart S. P. Parkin,³ Chun-Yeol You,⁴ and Sung-Chul Shin^{1,2,a)}

¹Department of Physics and Center for Nanospinics of Spintronic Materials, Korea Advanced Institute of Science and Technology, Daejeon 305-701, South Korea
²Department of Emerging Materials Science, DGIST, Daegu 711-873, South Korea
³IBM Research Division, Almaden Research Center, San Jose, California 95120, USA
⁴Department of Physics, Inha University, Incheon 402-751, South Korea
(Received 26 September 2012; accepted 26 February 2013; published online 11 March 2013)

APPLIED PHYSICS LETTERS 103, 022406 (2013)

Relationship between Gilbert damping and magneto-crystalline anisotropy in a Ti-buffered Co/Ni multilayer system

Hyon-Seok Song,^{1,2} Kyeong-Dong Lee,^{1,3} Jeong-Woo Sohn,^{1,2} See-Hun Yang,⁴ Stuart S. P. Parkin,⁴ Chun-Yeol You,⁵ and Sung-Chul Shin^{1,2,a)}

¹Department of Physics and Center for Nanospinics of Spintronic Materials, Korea Advanced Institute of Science and Technology, Daejeon 305-701, South Korea
²Department of Emerging Materials Science, DGIST, Daegu 711-873, South Korea
³Department of Materials Science and Engineering, KAIST, Daejeon, 305-701, South Korea
⁴IBM Research Division, Almaden Research Center, San Jose, California 95120, USA
⁵Department of Physics, Inha University, Incheon 402-751, South Korea
(Received 19 March 2013; accepted 21 June 2013; published online 9 July 2013)

“...a linear relation between the perpendicular magnetic anisotropy and α is established”

“No correlation of g with the increase in α ... is enhanced locally at the interface between the multilayer and buffer (capping) layer... may be attributed to the spin-pumping effect”

“The estimated α was found to be independent both on total thickness and anisotropy field of the multilayer...”

...the intrinsic Gilbert damping constant was found to be independent of the perpendicular magnetic anisotropy...”

“We find that the magneto-crystalline anisotropy and the Gilbert damping constant show a linear relationship.”

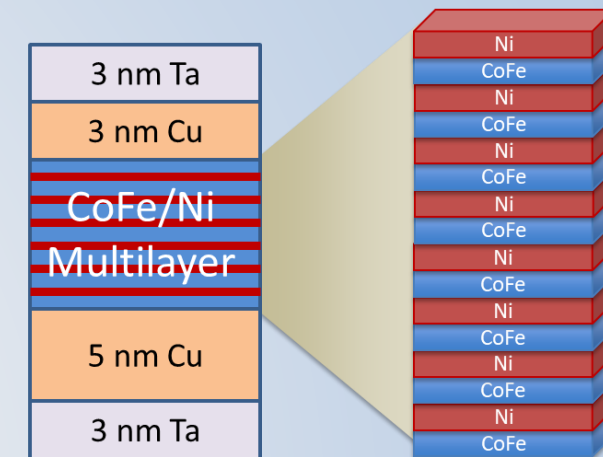
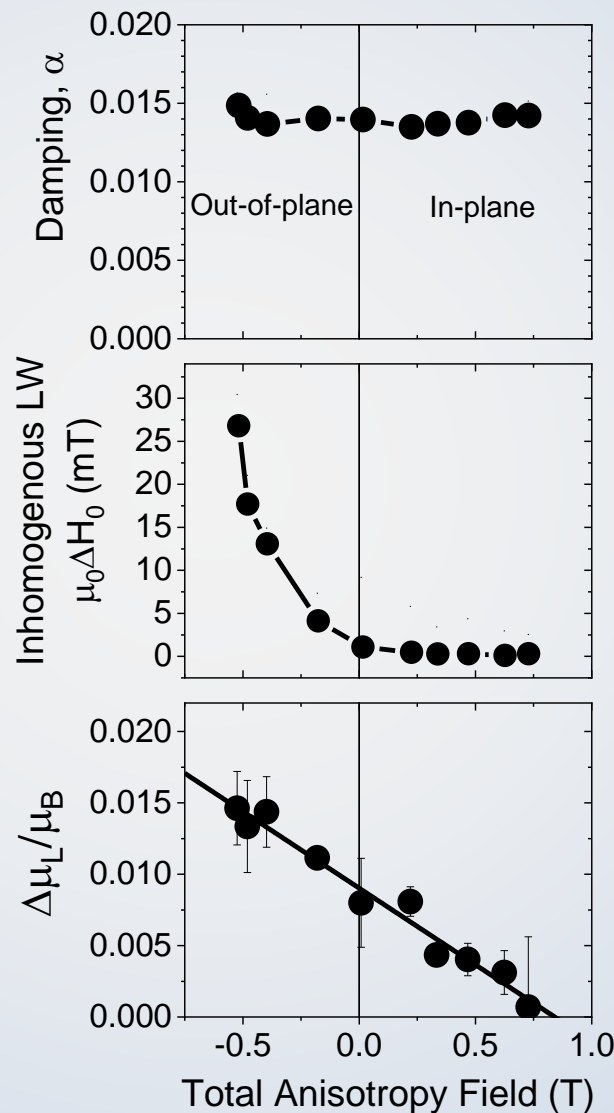
- No relationship between anisotropy and PMA

→ spin-orbit parameter does not vary

- Anisotropy results from orbital moment asymmetry NOT increased spin-orbit

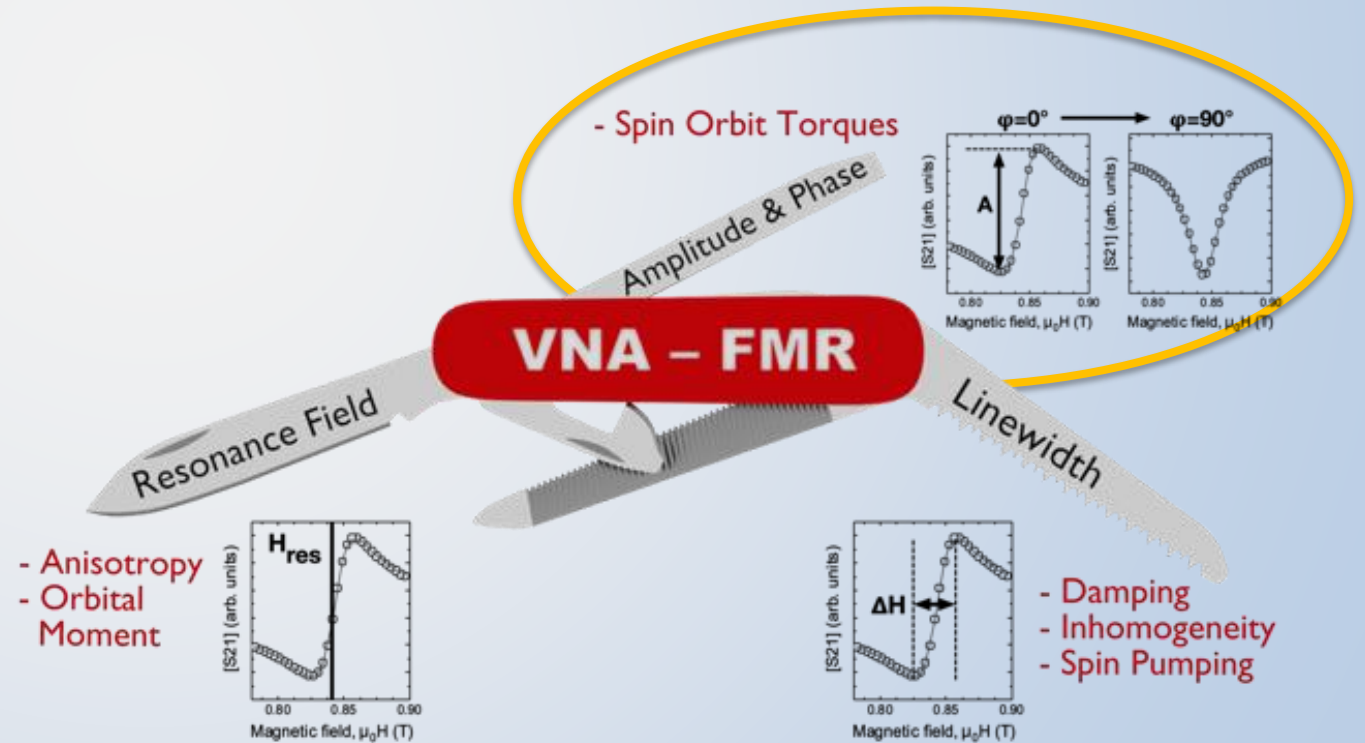
→ Independent of damping.

$$K = - \left(A \frac{\xi_{SO} N}{4V} \right) \frac{\Delta\mu_L}{\mu_B}$$



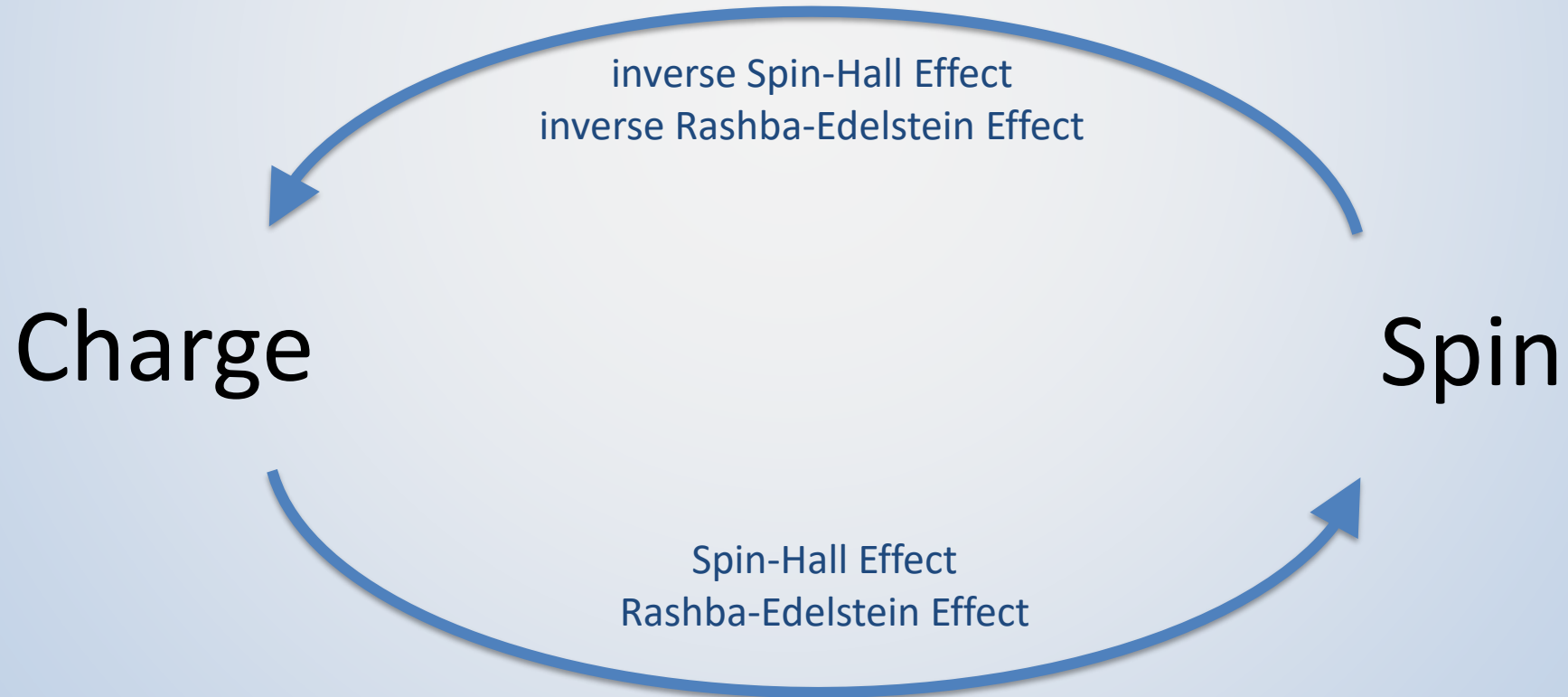
Co₉₀Fe₁₀/Ni Multilayers
Anisotropy is tuned by varying the total thickness.

- Spin-Orbit Interaction
- Ferromagnetic Resonance Spectroscopy
- Anisotropy and Orbital Moments
- Damping and Spin-Pumping
- Spin-Orbit Torques

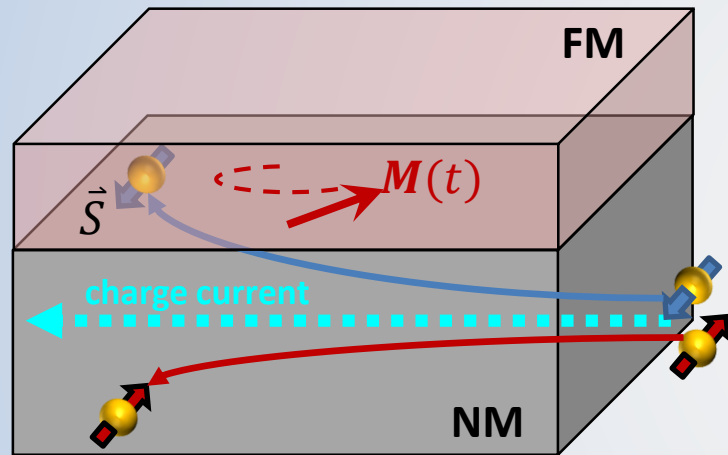


Spin-Orbit Torques → transfer of angular momentum from lattice to carriers to magnetization

- Consider Ferromagnet (FM)/Heavy Metal interface
- Heavy metals have large spin-orbit coupling
- A charge current through the heavy metal can generate a transverse pure spin current

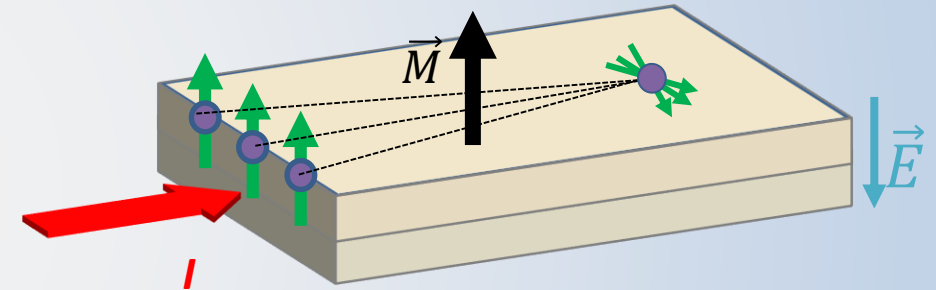


Spin-Hall Effect
“Damping-like Torque”



$$SOT \propto \vec{M} \times (\vec{M} \times \vec{S})$$

Rashba-Edelstein Effect (interfacial)
“Field Like Torque”

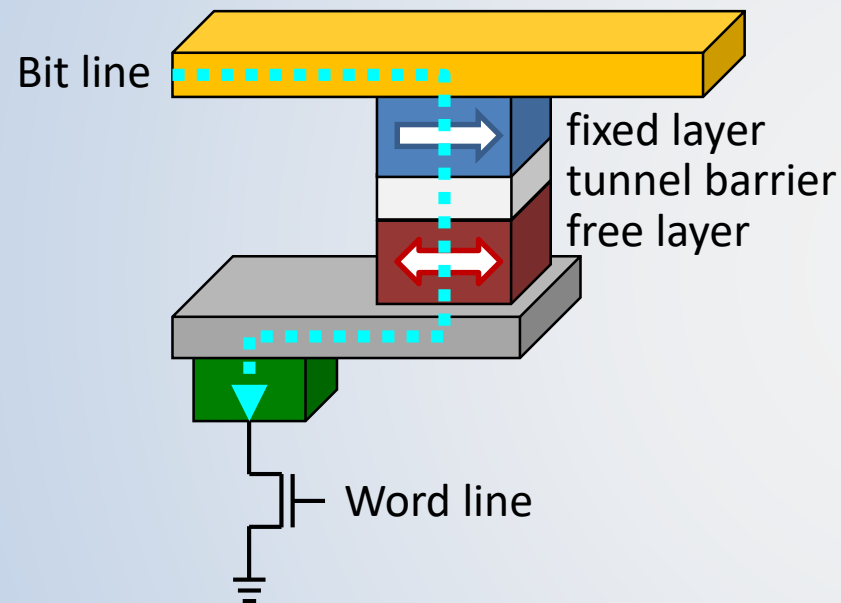


$$SOT \propto \vec{M} \times \vec{S}$$

In reality, neither SHE or REE are purely “damping-like” or “field-like,” but can be mixed.

Efficient switching of magnetic memory

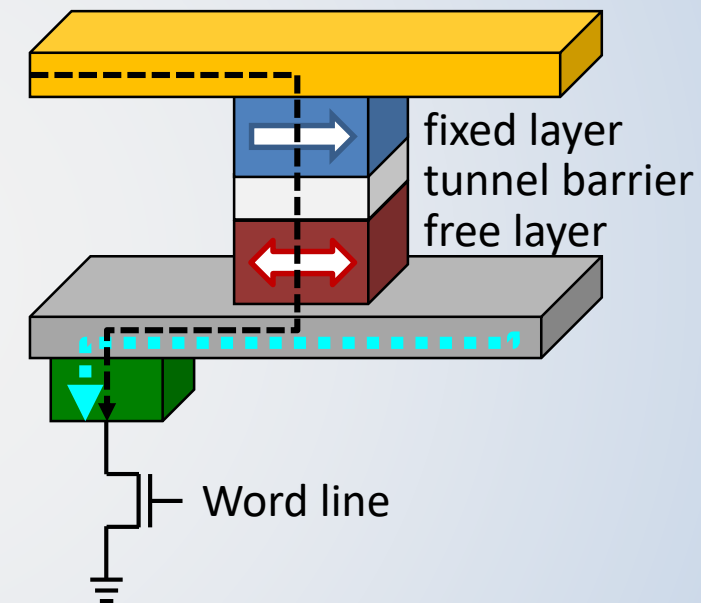
2-terminal Spin-Transfer Torque (STT)



Shared read/write path:

- ✘ Large current density for write operations can damage tunnel barrier
- ✘ Read operations have finite probability of flipping the bit

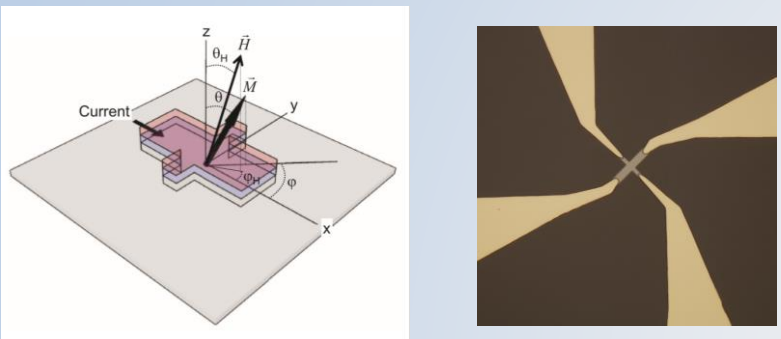
3-terminal Spin-Orbit Torque (SOT)



Separate read and write paths

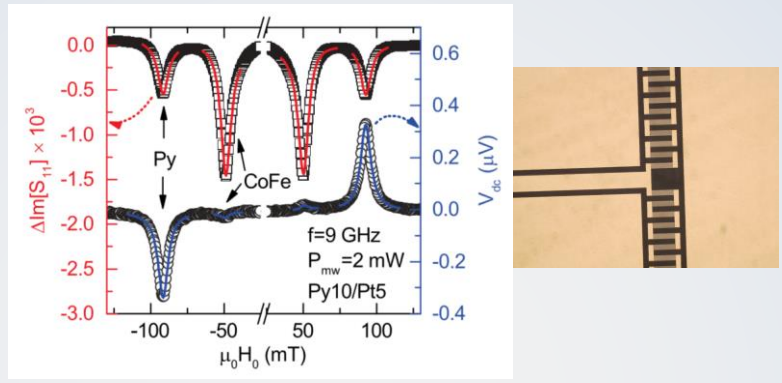
- ✓ Can apply large current density through write line without damaging MTJ

Harmonic Method with Hall Cross

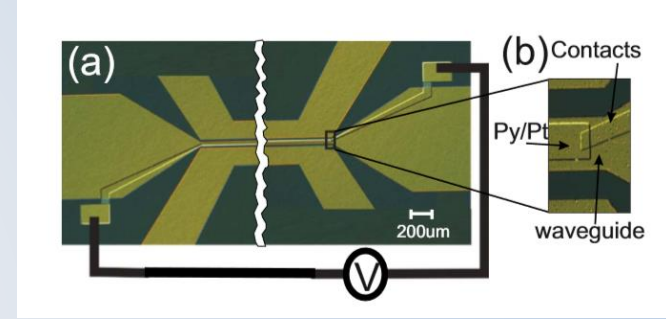


Hayashi et al. PRB 89, 144425 (2014)

Inverse SHE DC devices

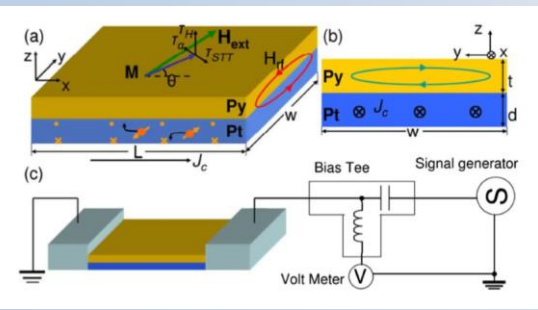


Weiler, IEEE Magn. Lett. 5, 3700104 (2014)

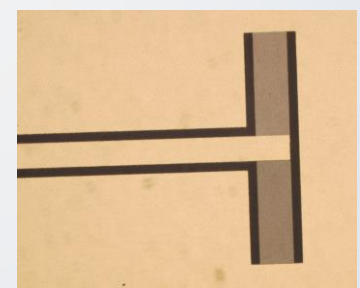
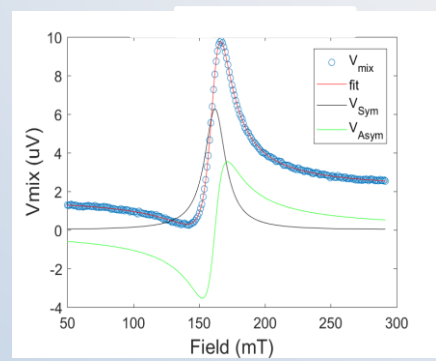
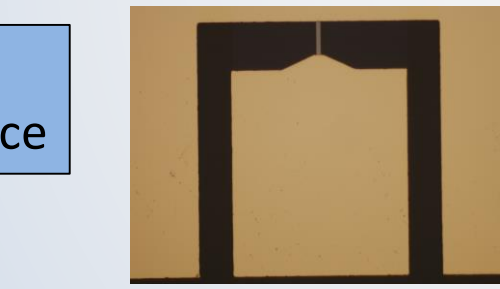


Mosendz et al., PRB, 82, 214403 (2010)

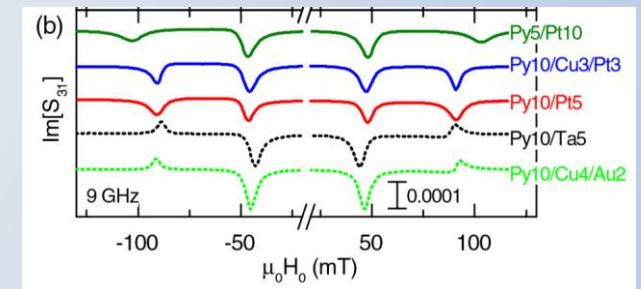
Spin-Torque Ferromagnetic Resonance



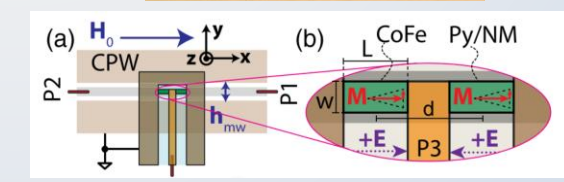
Liu et al., PRL, 106 (2011)



Inverse SHE AC devices



M. Weiler, PRL 113, 157204 (2014)



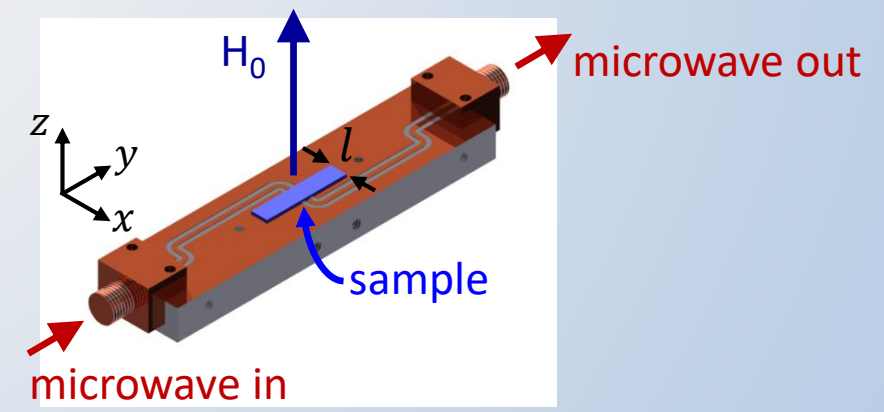
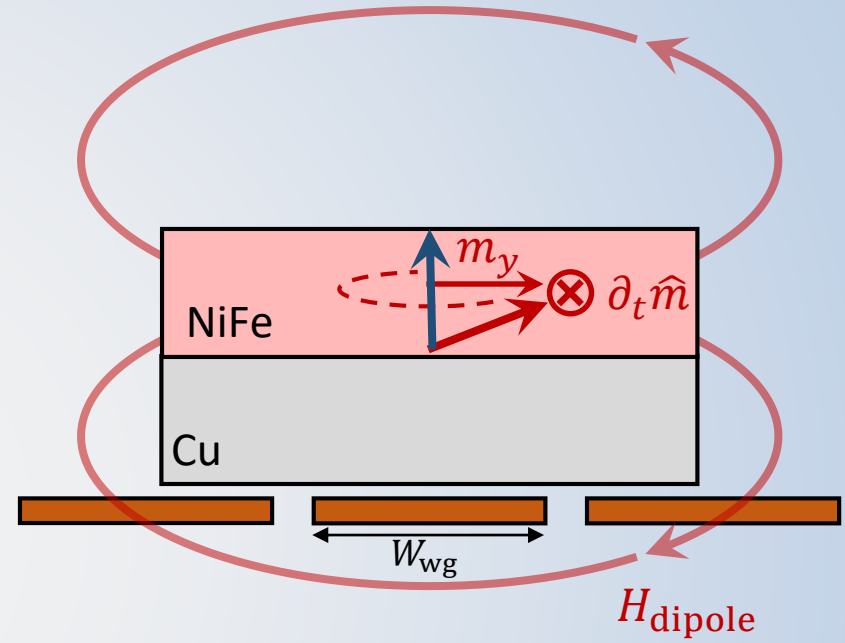
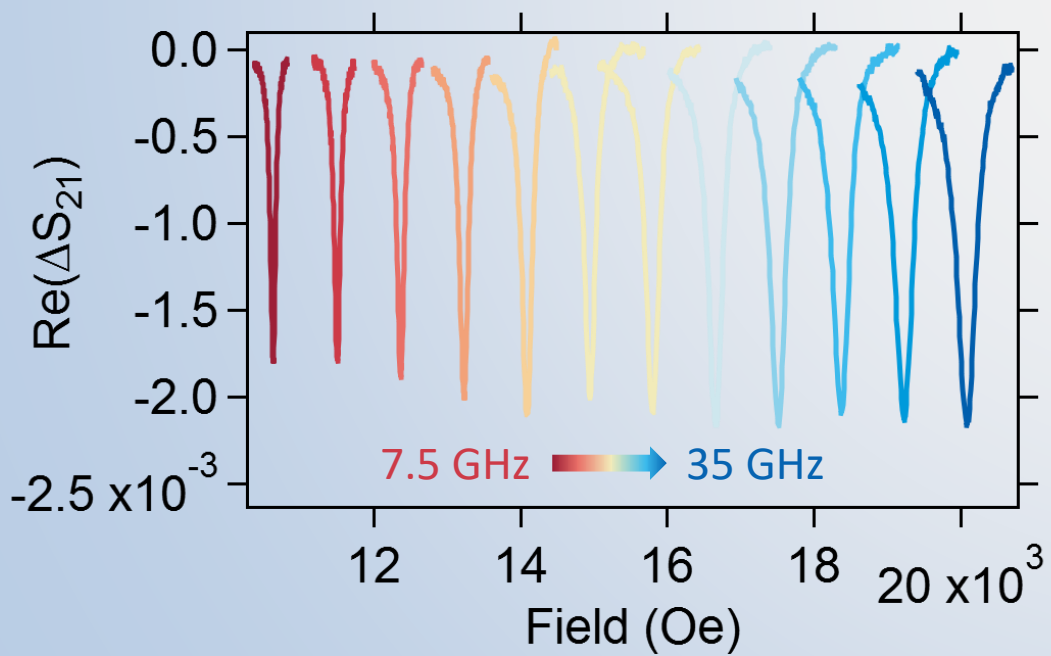
...and now VNA-FMR...at the film level

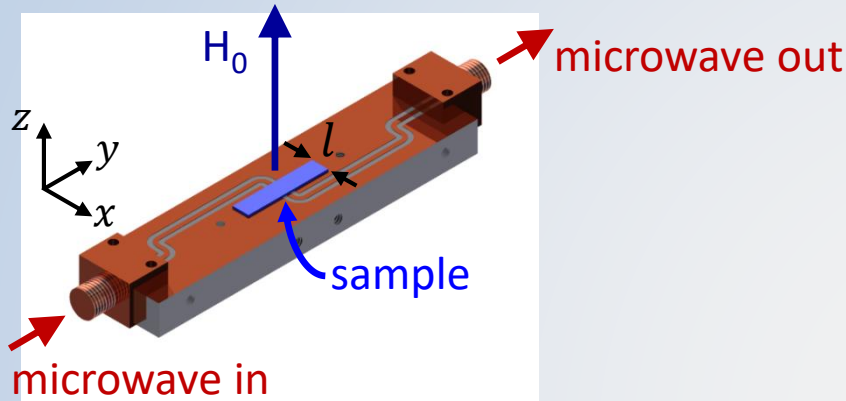
Measured signal

$$\Delta S_{21} \approx -\frac{i\omega}{Z_0} (L_{NiFe} + L_{Cu}) \quad \text{with } L_{Cu} \text{ crossed out and } \sim 0$$

$$L_{FM} = \frac{\mu_0 l d_{FM}}{4W_{wg}} \chi_{yy}$$

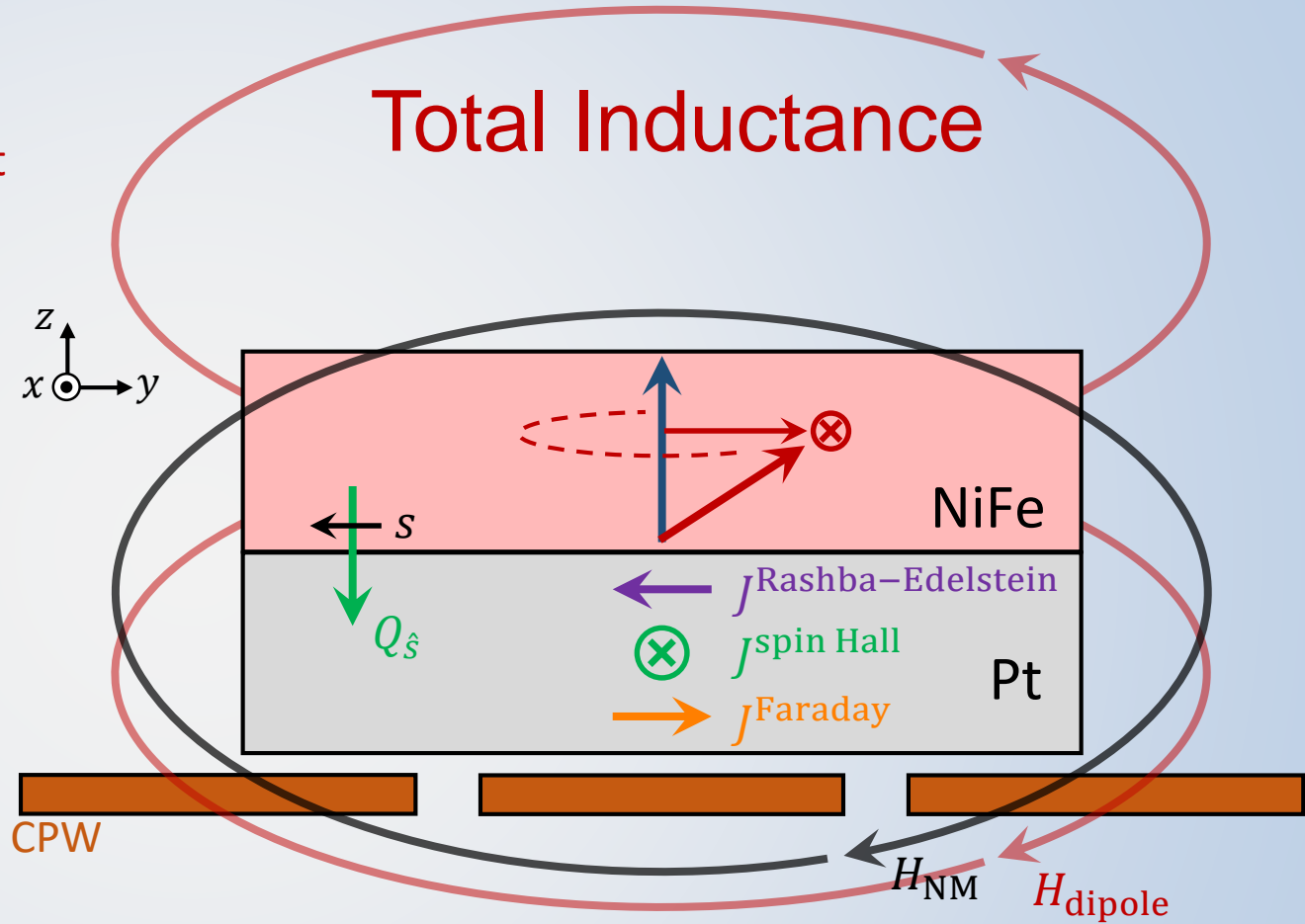
~ Constant signal as a function of frequency





The inductance (L) of the sample arises from anything that produces a flux around the CPW

$$L = \frac{\Phi}{I_{\text{CPW}}} = L_{\text{NiFe}} + L_{\text{Pt}}(\omega)$$



- | | | |
|--|---|-------------------------|
| 1. Dipolar inductive coupling, \sim frequency-independent | } | L_{NiFe} |
| 2. Second-order inductive coupling $\sim i\omega$ (Faraday-induced currents in the NM) | | |
| 3. Damping-like $\sim \omega$ (e.g. spin Hall effect) | } | $L_{\text{Pt}}(\omega)$ |
| 4. Field-like $\sim i\omega$ (e.g. Rashba-Edelstein effect) | | |

Frequency Dependent

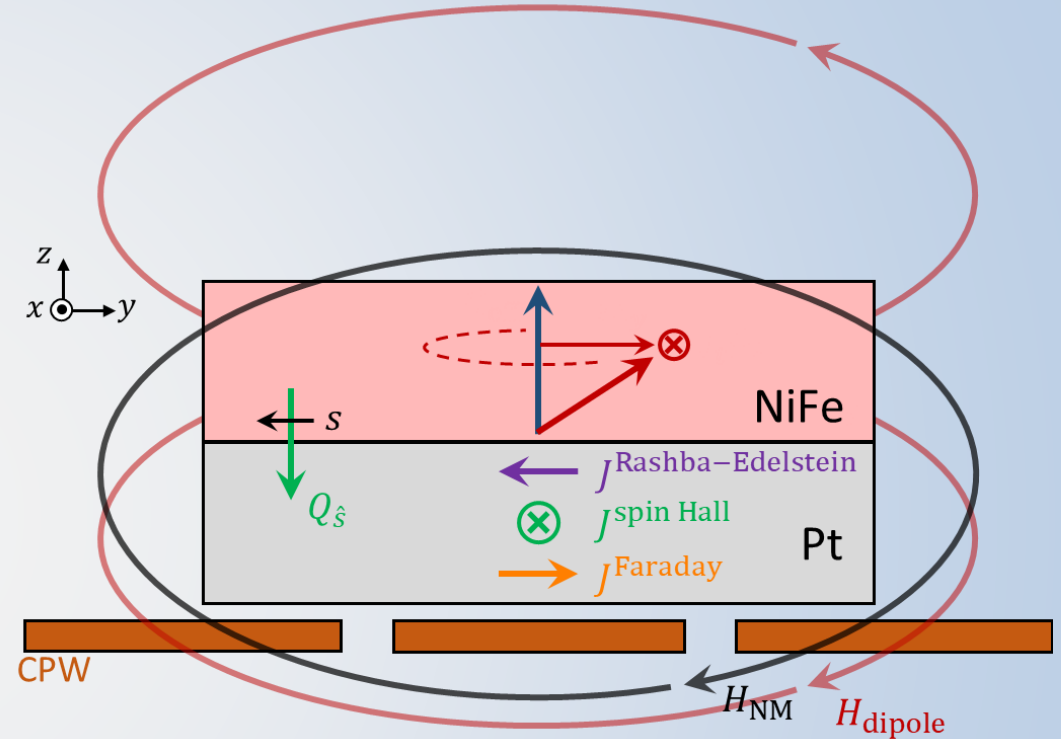
$$\Delta S_{21} \approx -\frac{i\omega}{Z_0} (L_{NiFe} + L_{Pt}(\omega))$$

Field-like terms

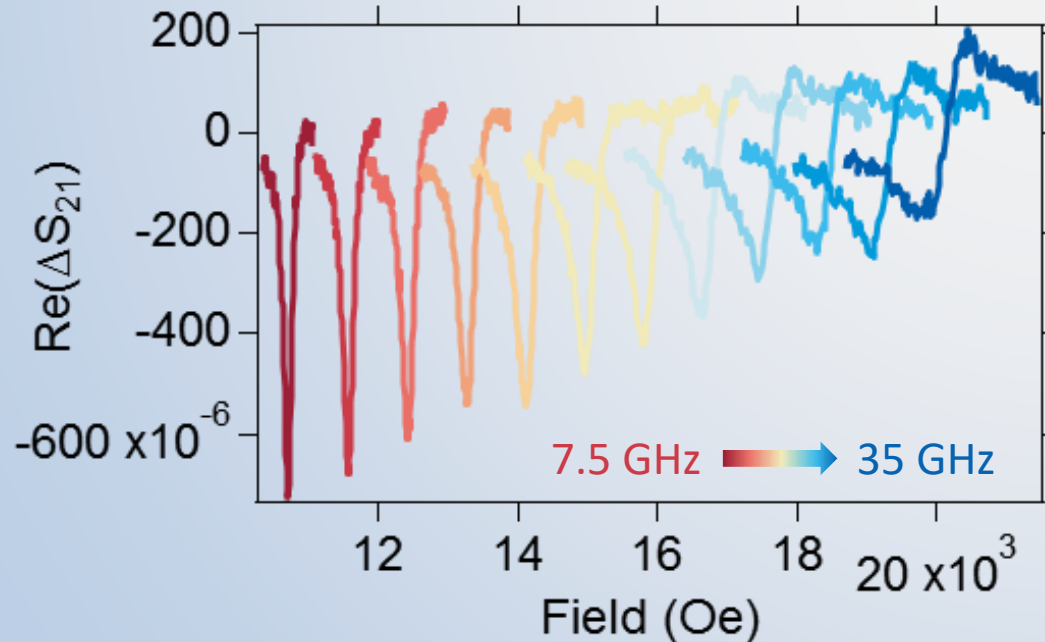
$$\text{Re}(L) \propto \mu_0 l d_{FM} + L_{12} \frac{\hbar\omega}{e} (\sigma_{fl}^{SOT} - \sigma_{fl}^F)$$

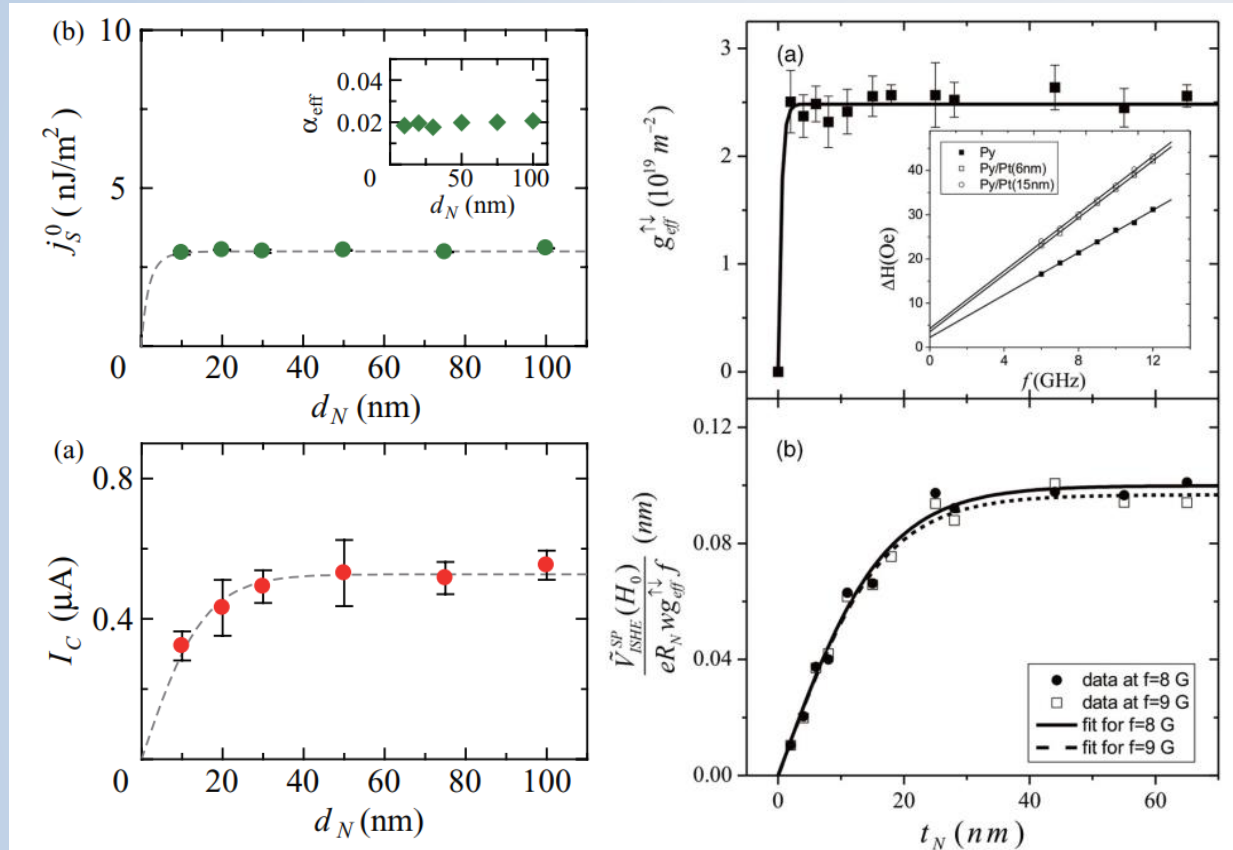
Damping-like terms

$$\text{Im}(L) \propto -L_{12} \frac{\hbar\omega}{e} \sigma_{dl}^{SOT}$$



Change in both Amplitude and Phase





Nakayama,
PRB **85**, 144408 (2012)

Feng,
PRB **85**, 214423 (2012)

← From damping measurements

← From spin Hall measurements

If the pumped spin current is generating the charge current via the SHE, *how can this be?*

PROBLEM: Inconsistency in Spin diffusion length in Pt

Spin-pumping \rightarrow < 2 nm

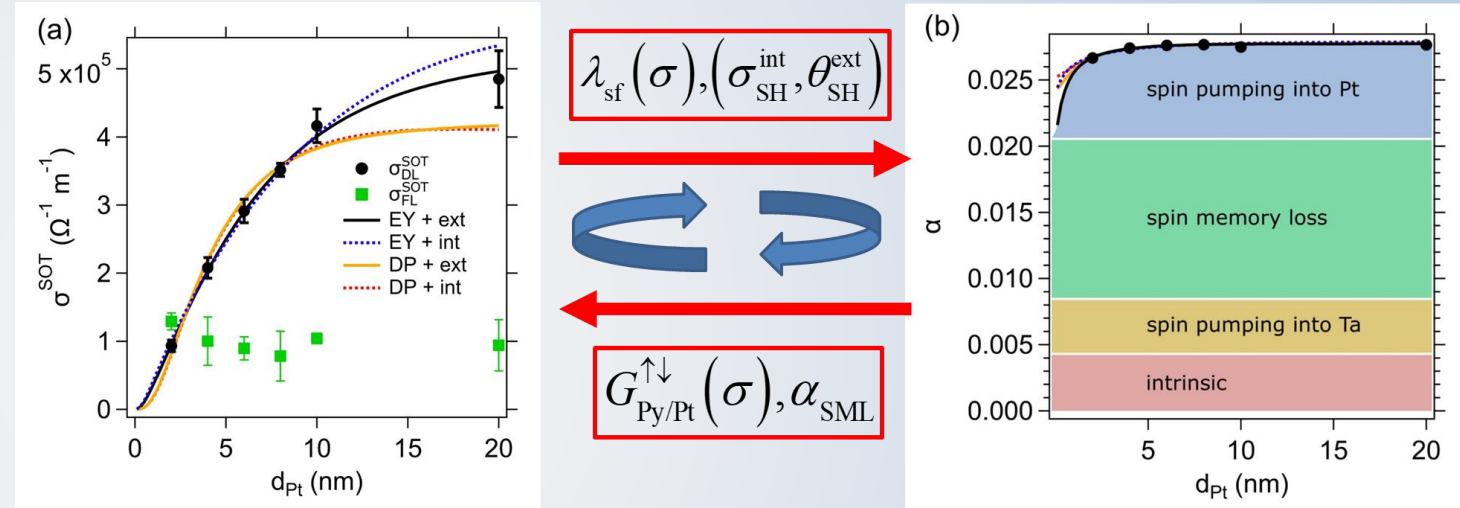
iSHE measurements \rightarrow 4-8 nm

Nakayama, PRB **85**, 144408 (2012)

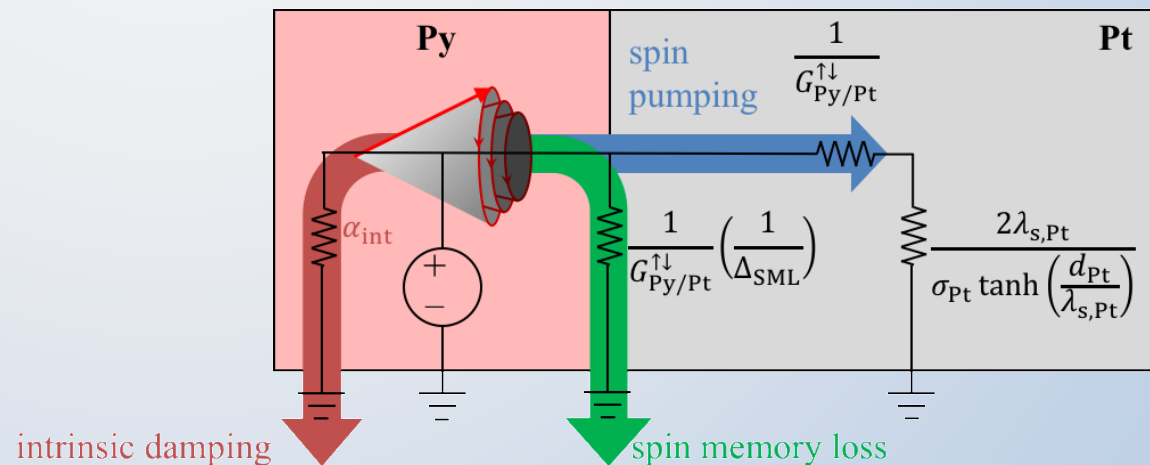
Feng, PRB **85**, 214423 (2012)



VNA-FMR \rightarrow self-consistent, simultaneous measurement of spin-pumping and iSHE



Berger, et al. PRB **97** 094407 (2018)



- No rectification artifacts
 - No need for sample patterning
 - Phase sensitive separation of damping-like and field-like contributions
 - Simultaneous extraction of spin pumping contribution to damping
 - Identical method for both perpendicular and in-plane anisotropy FM materials

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Tom Silva
Martin Schoen (U.Manitoba)
Mathias Weiler (WMI, Munich)
Eric Edwards (IBM)
Carl Boone
Mike Schneider
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Yaroslav Kvashnin
Olof "Charlie" Karis



T.U. Munich

Christian Back



Eindhoven University

Juriaan Lucassen
Bert Koopmans



- Spin-orbit (SO) coupling generates a wealth of phenomena in magnetic systems
- Recent advances in VNA-FMR techniques enables access to measure many of these SO phenomena.
- Improved precision of VNA-FMR measurements advanced our understanding of many phenomena:
 - Precise measurement of orbital moment to compare with theory
 - Determination of intrinsic damping and quantification of other sources
 - Better understanding of factors that control damping
 - Quantification of SOT without device fabrication
 - Self-consistent separation of spin-pumping and spin-memory losses

