

# CCM6+7+ 2016-17

## Unit 10 Angle Relationships

Name \_\_\_\_\_

Teacher \_\_\_\_\_

Projected Test Date \_\_\_\_\_

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## Unit 10 CCM6+7+ Angles and Triangles Vocabulary

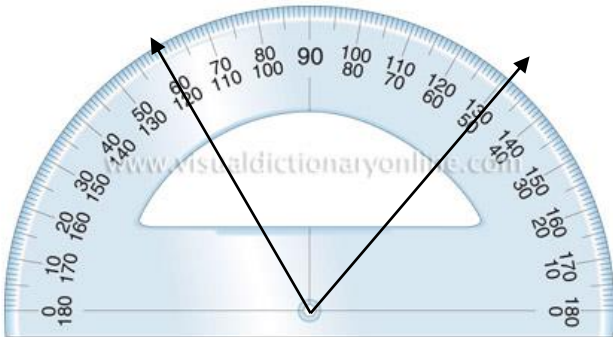
<b>Term</b>	<b>Quick Description</b>	<b>Visual</b>
Angle		
Ray		
Vertex		
Protractor		
Acute angle		
Obtuse angle		
Right angle		
Straight angle		
Reflex angle		
Complementary angles		
Supplementary angles		
Adjacent angles		
Vertical angles		
Interior		
Exterior		
Alternate interior angles		
Alternate exterior angles		
Transversal		
Corresponding angles		

Congruent		
Acute triangle		
Right triangle		
Obtuse triangle		
Scalene triangle		
Isosceles triangle		
Equilateral triangle		
Triangle Sum Theorem		
Sides of a triangle rule		
Exterior Angle Theorem		

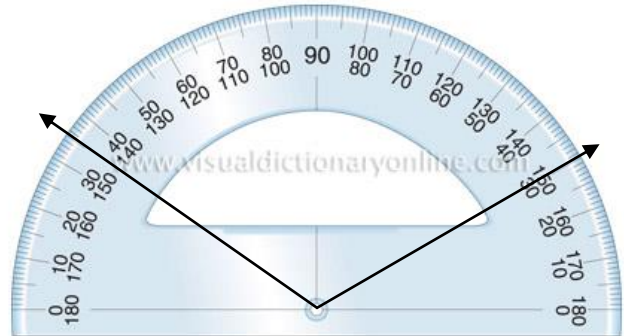
## Measuring Angles

Write the measure of each given angle below.

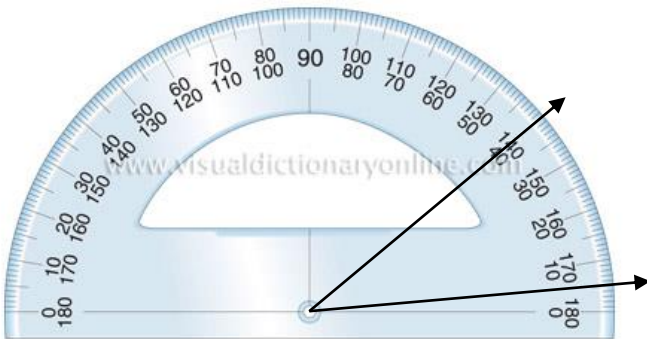
1. Measure = \_\_\_\_\_



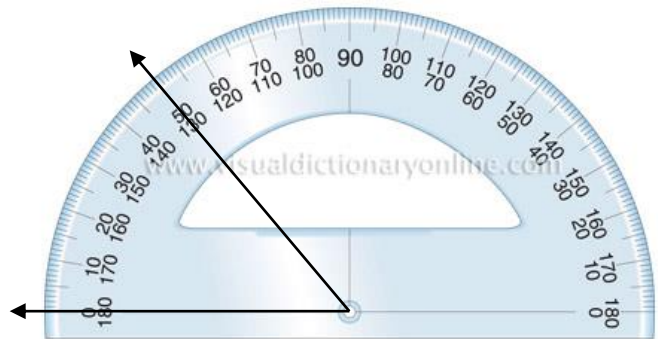
2. Measure = \_\_\_\_\_



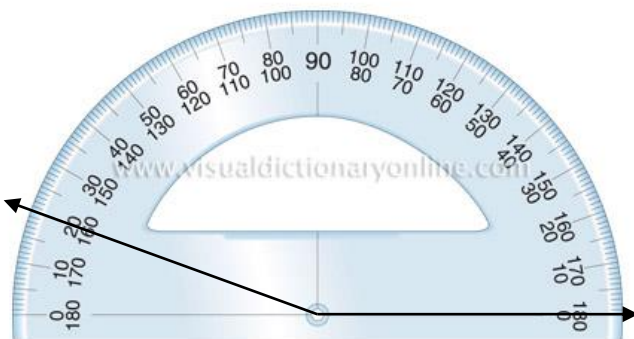
3. Measure = \_\_\_\_\_



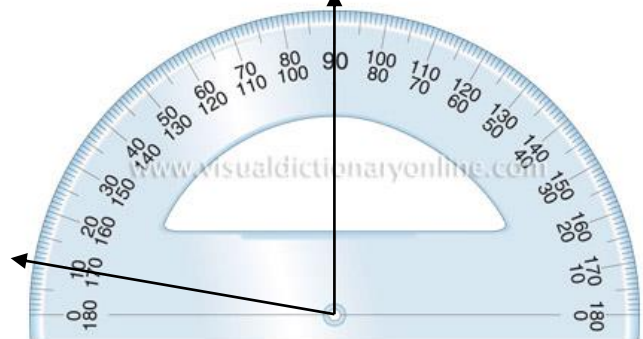
4. Measure = \_\_\_\_\_



5. Measure = \_\_\_\_\_



6. Measure = \_\_\_\_\_



On a separate page, using a protractor, draw the following angles and label them with the given letter as the vertex.

A)  $125^\circ$

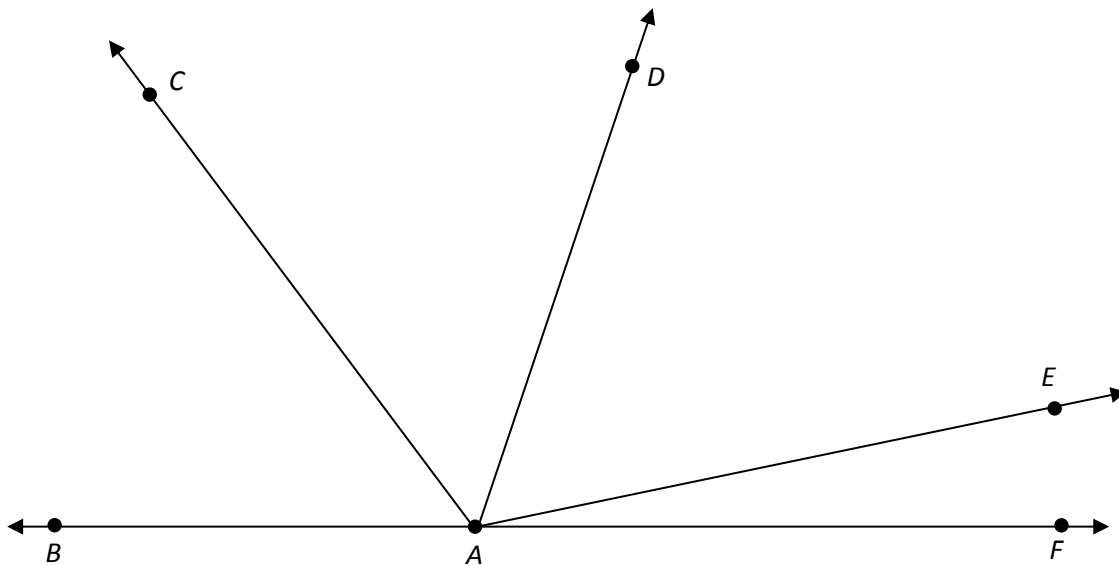
B)  $30^\circ$

C)  $165^\circ$

D) a right angle

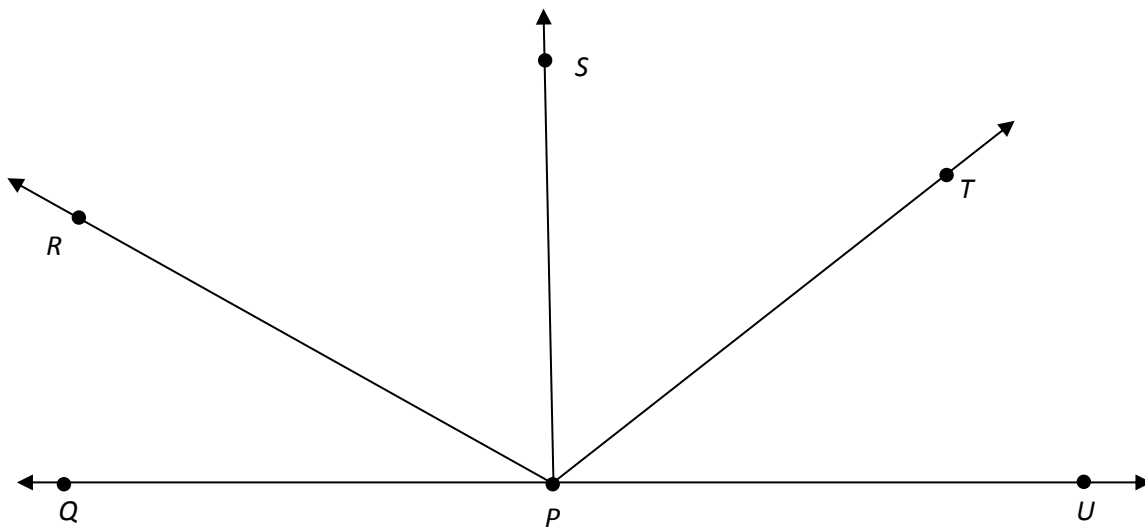
Drawing the angles from the bottom of page 6:

Find the measure of each angle in degrees.



$$m\angle CAB = \underline{\hspace{2cm}} \quad m\angle DAB = \underline{\hspace{2cm}} \quad m\angle EAB = \underline{\hspace{2cm}}$$

$$m\angle CAF = \underline{\hspace{2cm}} \quad m\angle DAF = \underline{\hspace{2cm}} \quad m\angle EAF = \underline{\hspace{2cm}}$$



$$m\angle RPQ = \underline{\hspace{2cm}} \quad m\angle SPQ = \underline{\hspace{2cm}} \quad m\angle TPQ = \underline{\hspace{2cm}}$$

<b>PRACTICE MEASURING ANGLES</b>
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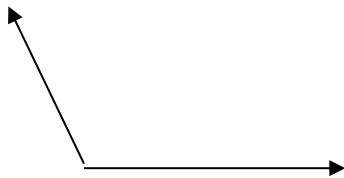
**Part 1:**

Fill the blank with the appropriate vocabulary word.

1. A(n) \_\_\_\_\_ angle is an angle that measures less than  $90^\circ$ .
2. A(n) \_\_\_\_\_ angle is an angle that measures more than  $90^\circ$ .
3. A(n) \_\_\_\_\_ angle is an angle that measures exactly  $90^\circ$ .

**Part 2:**

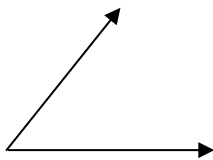
For each angle, first write an estimate measurement, then the actual measurement, and last identify the type of angle.



Estimated Measure: \_\_\_\_\_

Actual Measure: \_\_\_\_\_

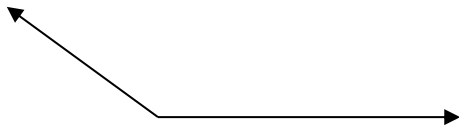
Type of Angle: \_\_\_\_\_



Estimated Measure: \_\_\_\_\_

Actual Measure: \_\_\_\_\_

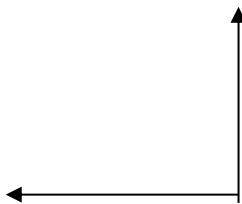
Type of Angle: \_\_\_\_\_



Estimated Measure: \_\_\_\_\_

Actual Measure: \_\_\_\_\_

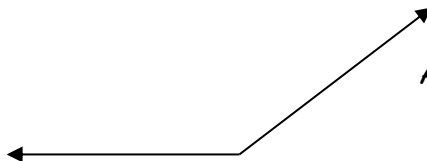
Type of Angle: \_\_\_\_\_



Estimated Measure: \_\_\_\_\_

Actual Measure: \_\_\_\_\_

Type of Angle: \_\_\_\_\_



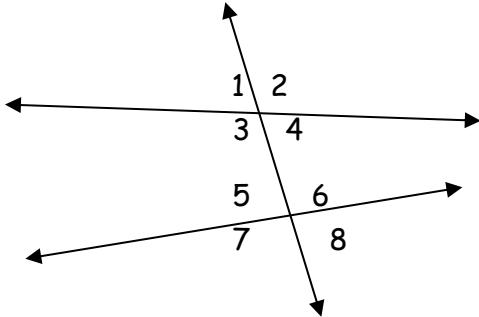
Estimated Measure: \_\_\_\_\_

Actual Measure: \_\_\_\_\_

**Part 3:**

Using the figure below, name the set(s) of angles that are obtuse and the set(s) of angles that are acute.

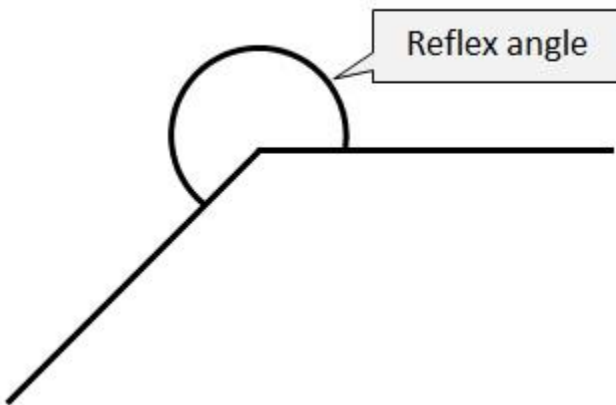
6.



OBTUSE ANGLES:  
\_\_\_\_\_

ACUTE ANGLES:  
\_\_\_\_\_

## Straight angle



A reflex angle is greater than  $180^\circ$ .



## ANGLE RELATIONSHIPS

Complementary Angles: \_\_\_\_\_

\_\_\_\_\_

Supplementary Angles: \_\_\_\_\_

\_\_\_\_\_

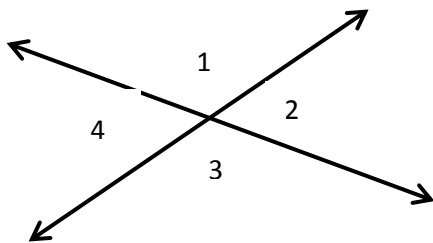
Vertical Angles: \_\_\_\_\_

\_\_\_\_\_

Adjacent Angles: \_\_\_\_\_

\_\_\_\_\_

Find the missing angles in the following examples. Make sure you tell the reason that you know each measure.



$m \angle 1 = 120^\circ$  because given

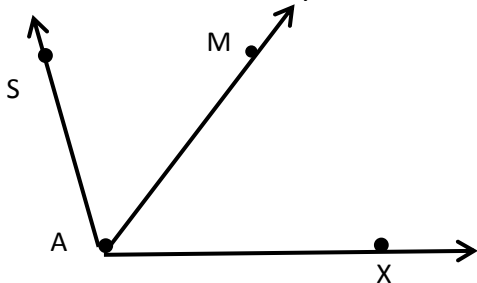
$m \angle 2 =$  \_\_\_\_\_ because \_\_\_\_\_

$m \angle 3 =$  \_\_\_\_\_ because \_\_\_\_\_

$m \angle 4 =$  \_\_\_\_\_ because \_\_\_\_\_

Is there more than one way to solve this? \_\_\_\_\_ Explain: \_\_\_\_\_

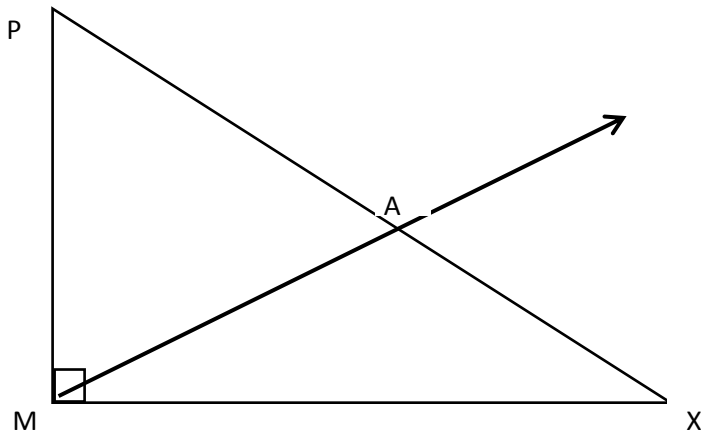
Use what you know to find the angle measures on the following problem.



$m \angle SAX$  is  $118^\circ$  and the  $m \angle MAX$  is  $65^\circ$

Find the measure of  $\angle SAM$

Find the missing measures of all angles below and label them on the drawing.

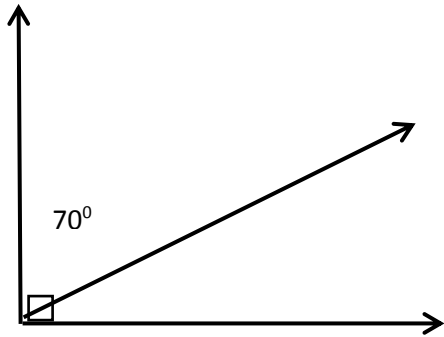


$m \angle PMA = 65^\circ$  and  $m \angle PAM = 60^\circ$

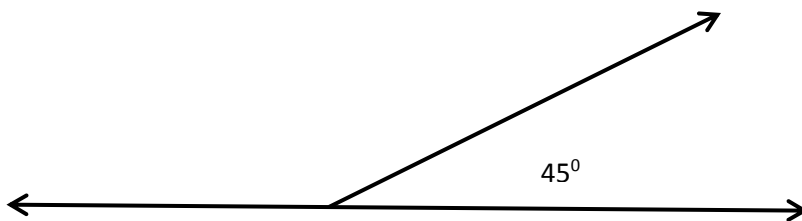
$m \angle AMX = \underline{\hspace{2cm}}$

$m \angle MAX = \underline{\hspace{2cm}}$

Find the missing measure below.

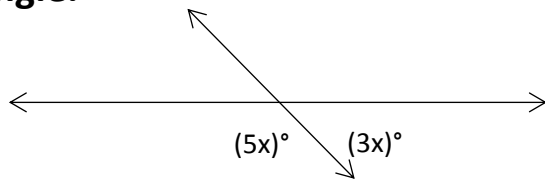


Find the missing measure below.



**Challenge.** Find the value of  $x$  in the diagram. Then find the measure of each angle.

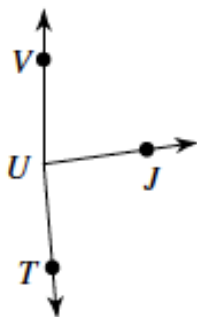
1.



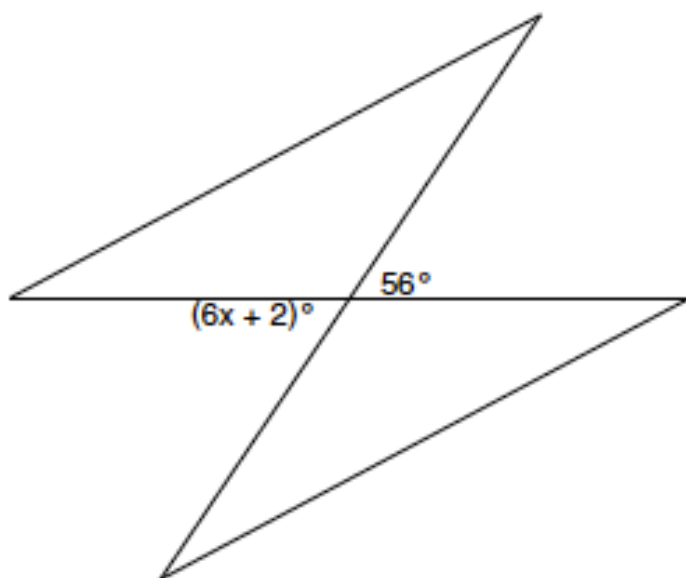
2.  $m\angle VUT = 175^\circ$

$m\angle VUJ = 17x - 3,$

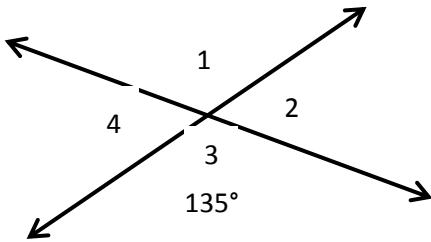
$m\angle JUT = 17x + 8.$  Find  $x$  then find the measure of each angle.



3.



Find the missing angles in the following. Make sure you tell the reason that you know each measure.



$m \angle 1 = 135^\circ$  because given

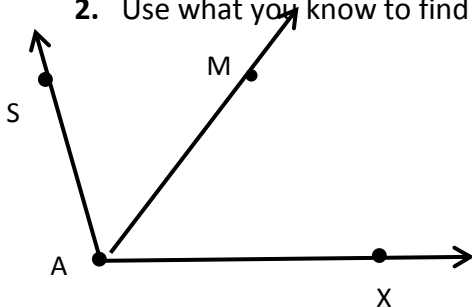
$m \angle 2 =$  \_\_\_\_\_ because \_\_\_\_\_

$m \angle 3 =$  \_\_\_\_\_ because \_\_\_\_\_

$m \angle 4 =$  \_\_\_\_\_ because \_\_\_\_\_

Is there more than one way to solve this? \_\_\_\_\_ Explain: \_\_\_\_\_

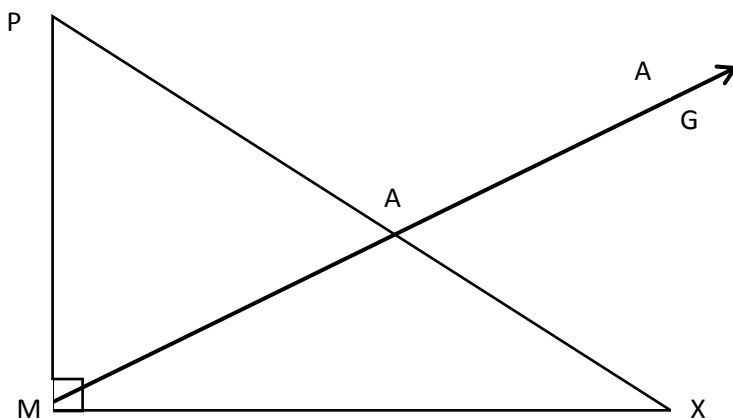
2. Use what you know to find the angle measures on the following problem.



$m \angle SAX$  is  $100^\circ$  and the  $m \angle MAX$  is  $70^\circ$

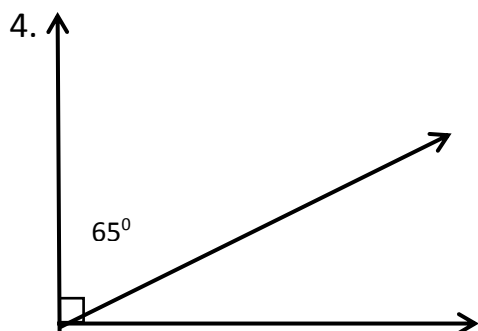
Find the measure of  $\angle SAM$

3. Find the missing measures of all angles below and label them on the drawing.



$m \angle AMX = 30^\circ$  and  $m \angle PAG = 100^\circ$

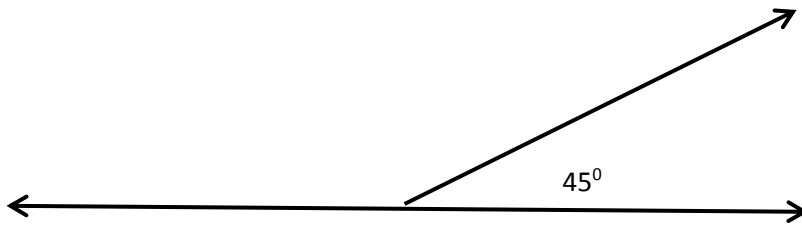
Find the missing measures below.



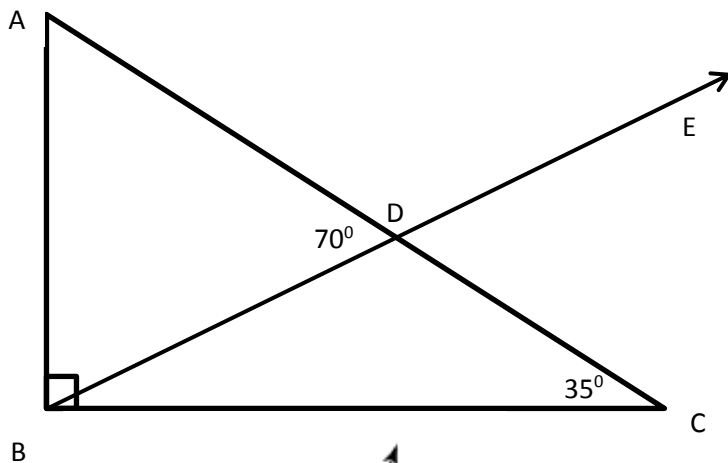
5.

Find the missing measure below.

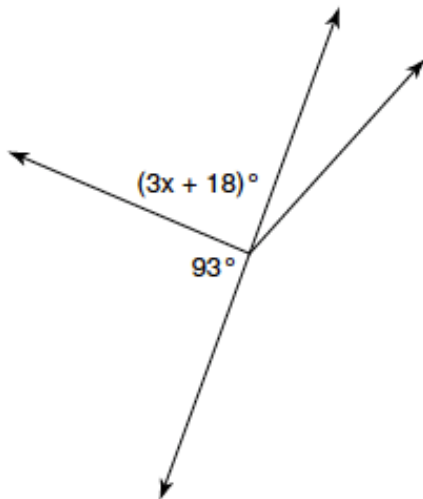
6.



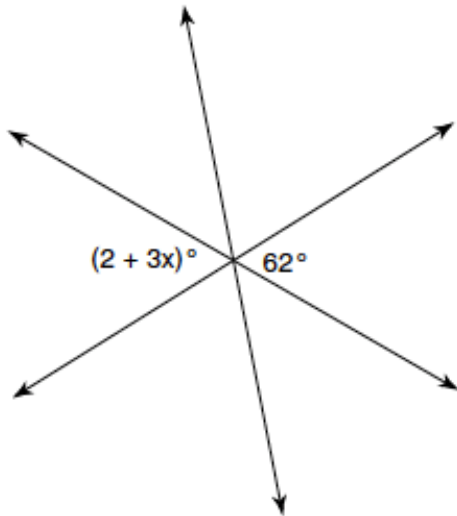
7.



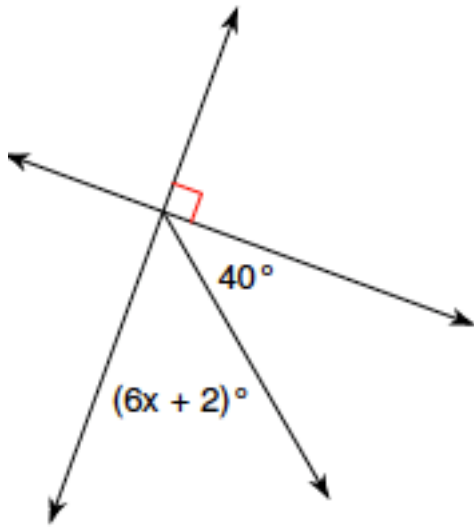
8.



9.



10.



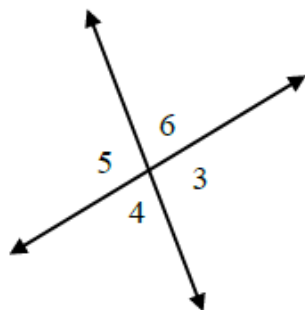
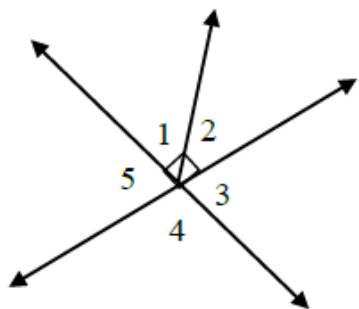
**Vocabulary Review: Write in words and draw a diagram to define each of the following words.**

1. Complementary Angles

2. Supplementary Angles

3. Adjacent Angles

4. Vertical Angles

**Use the figure to the right to answer the following questions.**6. If  $m\angle 5 = 95^\circ$ . Then  $m\angle 6 =$  \_\_\_\_\_.7. If  $m\angle 3 = 115^\circ$  then  $m\angle 6 =$  \_\_\_\_\_.9. If  $m\angle 6 = 2x$  and  $m\angle 4 = 78$ , then  $x =$  \_\_\_\_\_.10.  $m\angle 5 = 4x + 12$  and  $m\angle 4 = x + 8$ , then  $x =$  \_\_\_\_\_. What is the measure of Angle 5? \_\_\_\_\_ What is the measure of angle 4? \_\_\_\_\_**Use the figure below to answer the following questions yes or no?**9. Are  $\angle 1$  and  $\angle 2$  complementary angles? \_\_\_\_\_10. Are  $\angle 2$  and  $\angle 3$  adjacent angles? \_\_\_\_\_11. Are  $\angle 2$  and  $\angle 4$  vertical angles? \_\_\_\_\_12. Are  $\angle 5$  and  $\angle 3$  vertical angles? \_\_\_\_\_13. Are  $\angle 3$  and  $\angle 4$  supplementary angles? \_\_\_\_\_**For each given angle find its complement and supplement. If none exists, write "none".**15.  $m\angle A = 54^\circ$  comp: \_\_\_\_\_ supp: \_\_\_\_\_16.  $m\angle A = 95^\circ$  comp: \_\_\_\_\_ supp: \_\_\_\_\_17.  $m\angle A = 90^\circ$  comp: \_\_\_\_\_ supp: \_\_\_\_\_18.  $m\angle A = 112^\circ$  comp: \_\_\_\_\_ supp: \_\_\_\_\_

**For questions 19 – 24 set up and label a diagram, solve for the variable, and then find the angles given.**

19.  $\angle 1$  and  $\angle 2$  are supplementary angles. If  $m\angle 1 = 3x + 12$  and  $m\angle 2 = 7x - 32$ , find  $x$ ,  $m\angle 1$  and  $m\angle 2$ .

Equation used to solve: \_\_\_\_\_

$x =$  \_\_\_\_\_

$m\angle 1$  \_\_\_\_\_

$m\angle 2$  \_\_\_\_\_

20.  $\angle 1$  and  $\angle 2$  are complementary. If  $m\angle 1 = 6x + 2$  and  $m\angle 2 = 4x + 8$ , find  $x$ ,  $m\angle 1$  and  $m\angle 2$ .

Equation used to solve: \_\_\_\_\_

$x =$  \_\_\_\_\_

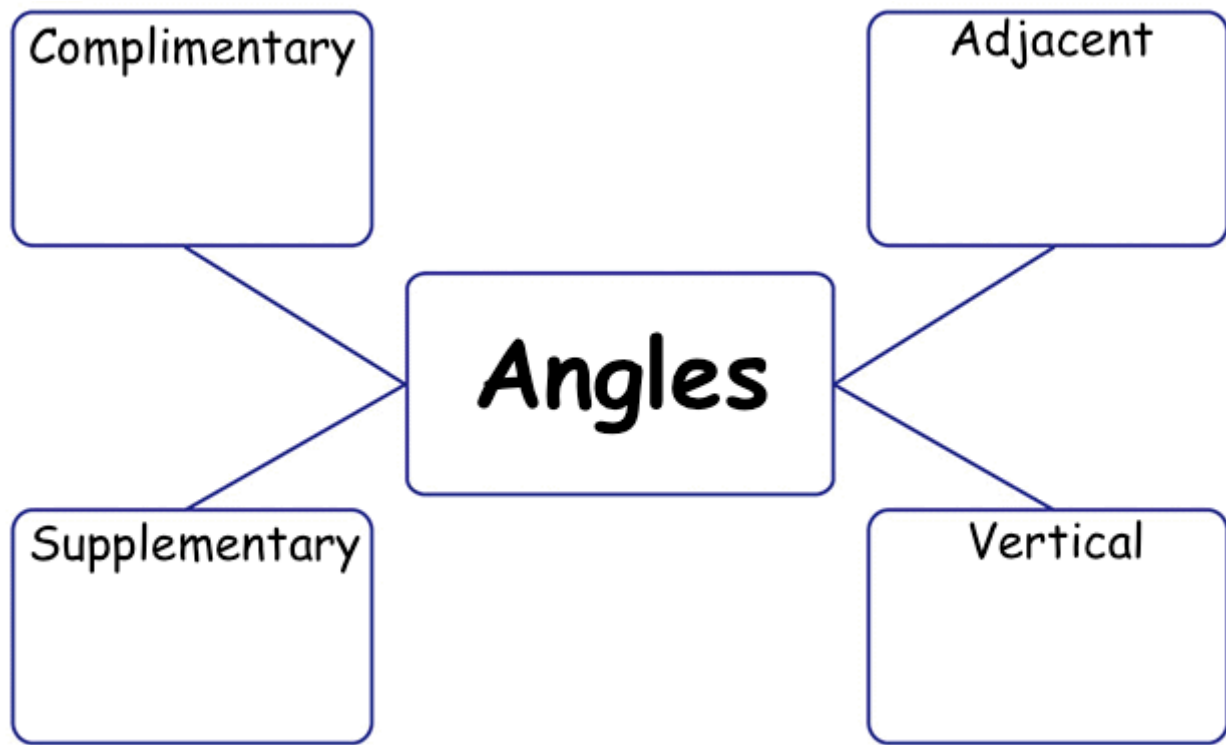
$m\angle 1$  \_\_\_\_\_

$m\angle 2$  \_\_\_\_\_



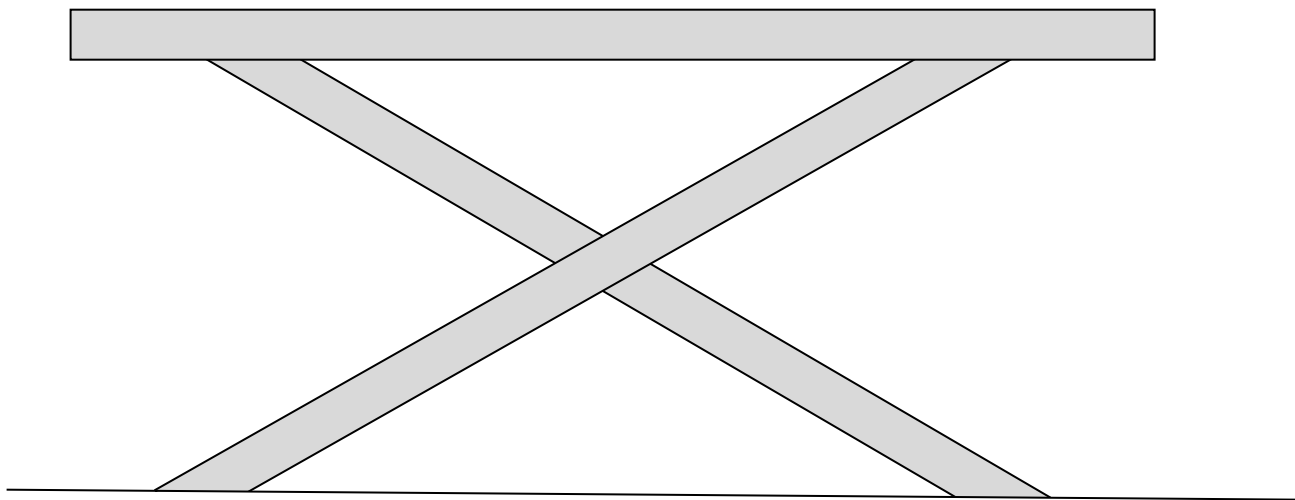
**Concept Map: Angles**

Name: \_\_\_\_\_



## Building A Bench

You are building a bench to add to the flower garden at the local library. The seat of the bench will be parallel to the ground. The legs that you are creating will be two boards crossed to make an x shape under the seat of the bench. The angle at the top part of the x will need to be  $150^\circ$  to safely support the bench seat and make it the right height. Draw a sketch below of the bench and then fill in all of the angle measures for the 12 angles that are formed by the crossed boards that are supporting the bench seat. Include the angles created by the ground and the bottom of the supports.



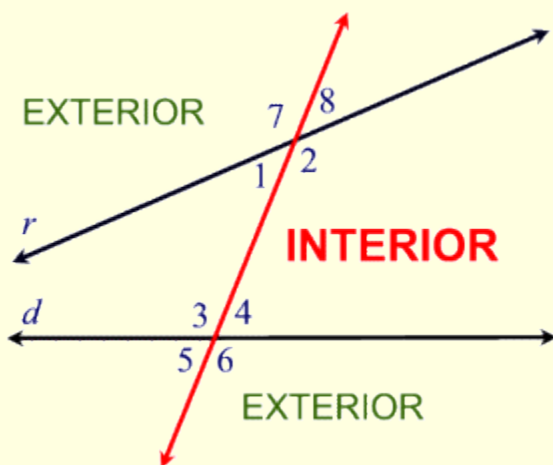
## Angles Created from Parallel Lines cut by a Transversal Line

A **transversal** is a line that intersects two or more lines (in the same plane). When lines intersect, angles are formed in several locations. Certain angles are given "names" that describe "where" the angles are located in relation to the lines. These names describe angles whether the lines involved are parallel or not parallel.

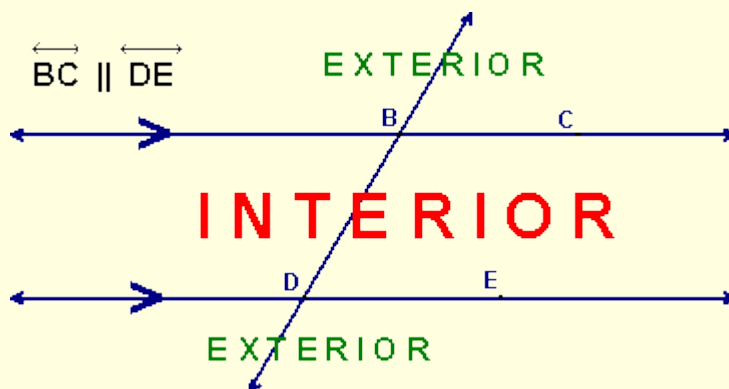
Remember that:

- the word **INTERIOR** means **BETWEEN** the lines.
- the word **EXTERIOR** means **OUTSIDE** the lines.
- the word **ALTERNATE** means "**alternating sides**" of the transversal.

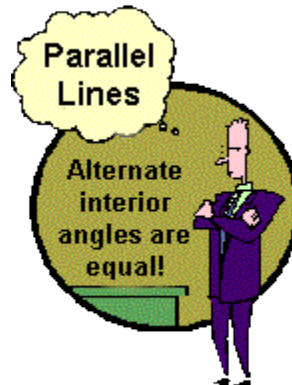
When the lines are NOT parallel ...



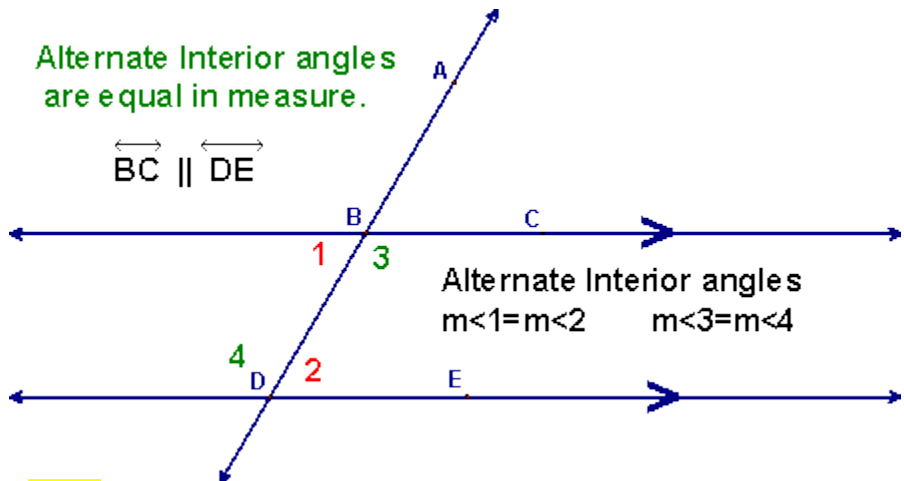
When the lines are parallel...



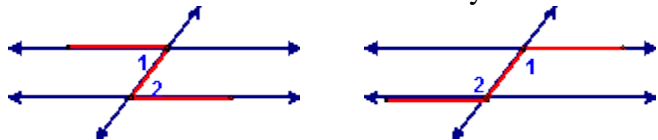
**When the lines are parallel:**  
**Alternate Interior Angles**  
**(measures are equal)**  
 The name clearly describes "where" these angles are located.



Look carefully at the diagram below:



**Hint:** If you draw a Z on the diagram, the alternate interior angles are found in the corners of the Z. The Z may also be a backward Z.

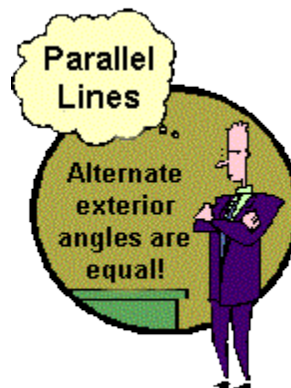


**Theorem:** If two parallel lines are cut by a transversal, the alternate interior angles are congruent.

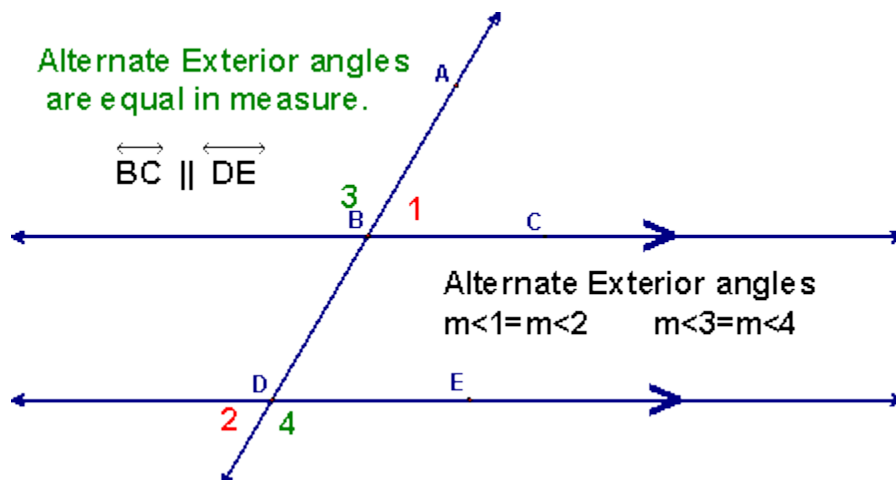
**Theorem:** If two lines are cut by a transversal and the alternate interior angles are congruent, the lines are parallel.

When the lines are parallel:  
**Alternate Exterior Angles**  
 (measures are equal)

The name clearly describes "where" these angles are located.



Look carefully at the diagram below:



**Theorem:** If two parallel lines are cut by a transversal, the alternate exterior angles are congruent.

**Theorem:** If two lines are cut by a transversal and the alternate exterior angles are congruent, the lines are parallel.

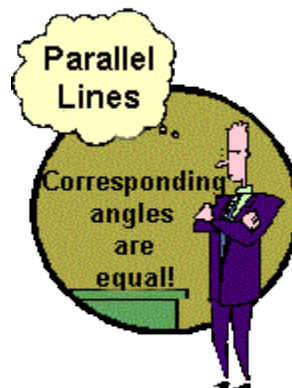
When the lines are parallel:

## Corresponding Angles

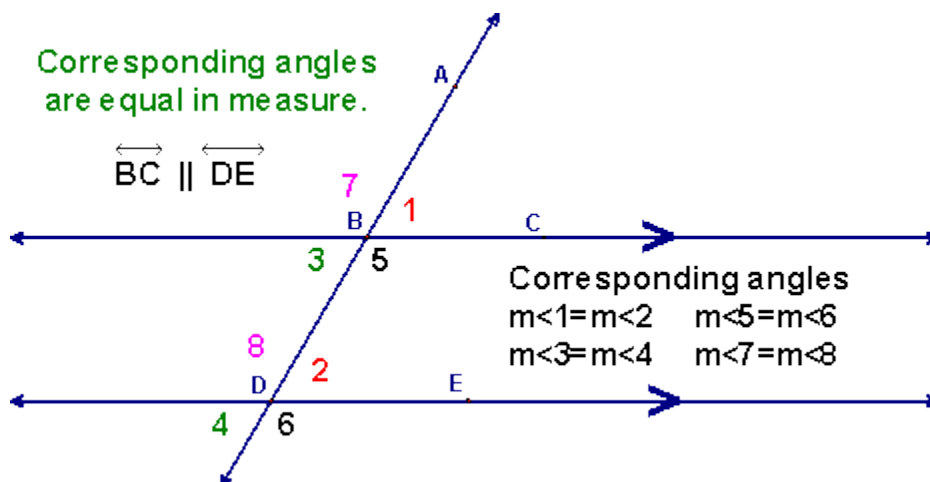
**(measures are equal)**

Unfortunately, the name of these angles does not clearly indicate "where" they are located. They are located:

- on the SAME SIDE of the transversal
  - one INTERIOR and one EXTERIOR
  - and they are NOT adjacent (*they don't touch*).
- (They lie on the same side of the transversal, in corresponding positions.)

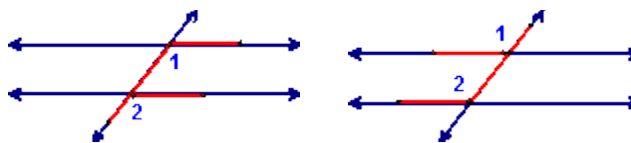


Corresponding angles are equal in measure.



**Hint:** If you took a picture of one corresponding angle and slid the angle up (or down) the same side of the transversal, you would arrive at the other corresponding angle.

**Also:** If you draw an F on the diagram, the corresponding angles can be found in the "corners" of the F. The F may be backward and/or upside-down.



**DRAW CIRCLES to find CORRESPONDING ANGLES!**

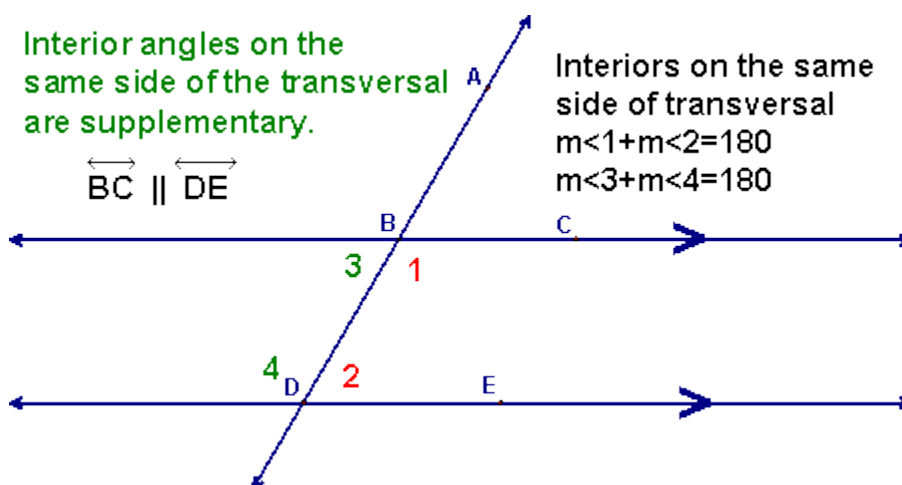
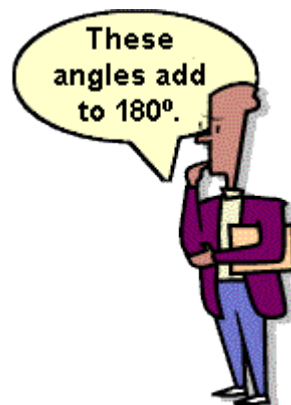
**Theorem:** If two parallel lines are cut by a transversal, the corresponding angles are congruent.

**Theorem:** If two lines are cut by a transversal and the corresponding angles are congruent, the lines are parallel.

When the lines are parallel:  
**Interior Angles on the Same Side of the Transversal**

➔ **(measures are supplementary)**

Their "name" is simply a description of where the angles are located.



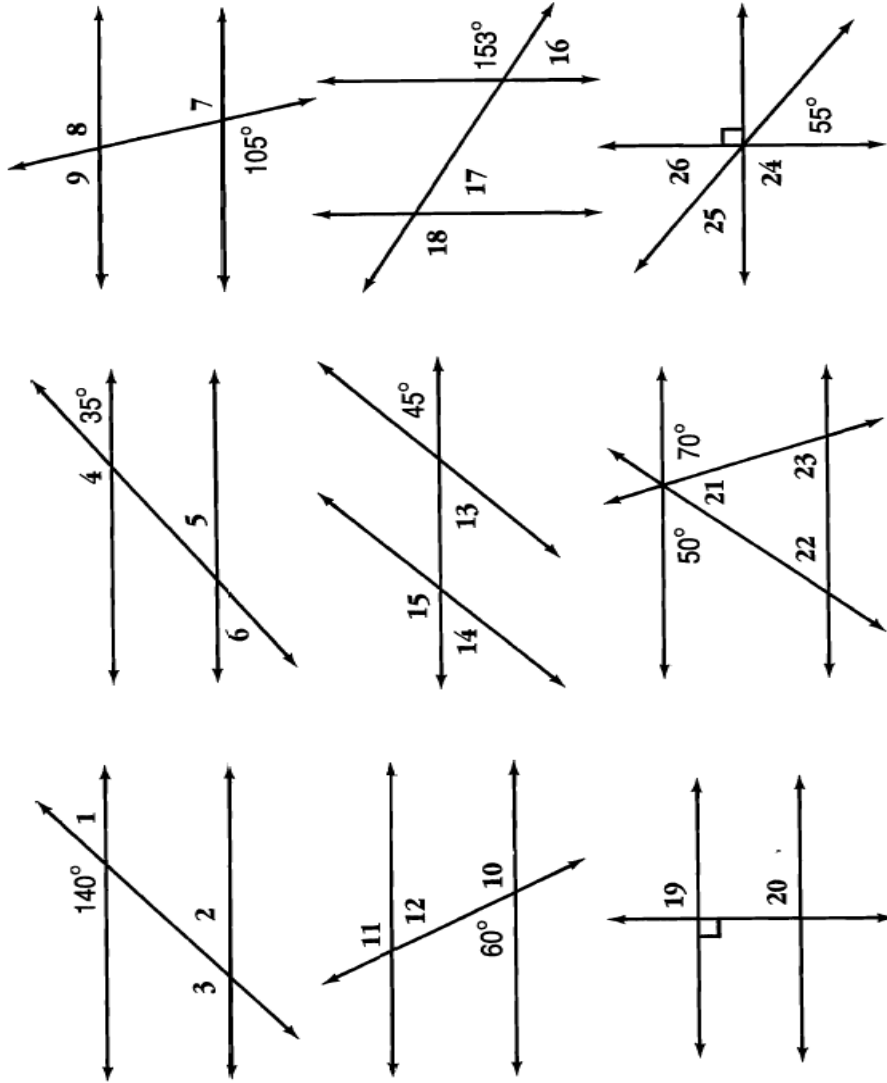
**Theorem:** If two parallel lines are cut by a transversal, the interior angles on the same side of the transversal are supplementary.

**Theorem:** If two lines are cut by a transversal and the interior angles on the same side of the transversal are supplementary, the lines are parallel.

# Why Couldn't the Two Elephants Go Swimming Together?

Give the measure of each numbered angle. Find your answer in the Code Key and notice the letter next to it. Write this letter in the box containing the number of the angle. (Assume that lines in each figure that do not intersect are parallel.)

CODE KEY	
27°	A
35°	O
40°	R
45°	Y
50°	I
55°	P
60°	T
70°	U
75°	F
90°	N
105°	H
120°	E
135°	K
140°	L
145°	S
153°	D



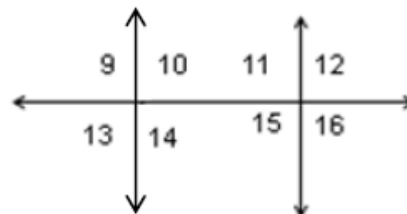
12	7	10	14	8	16	18	6	20	3	13	25	19	11	26	17	22	1	5	9	21	2	23	24	15	4
----	---	----	----	---	----	----	---	----	---	----	----	----	----	----	----	----	---	---	---	----	---	----	----	----	---



Use the figure at the right to answer problems 1- 8.

Classify each pair of angles as one of the following:

- (a) alternate interior angles      (b) corresponding angles  
 (c) alternate exterior angles      (d) vertical angles  
 (e) supplementary angles      (f) none



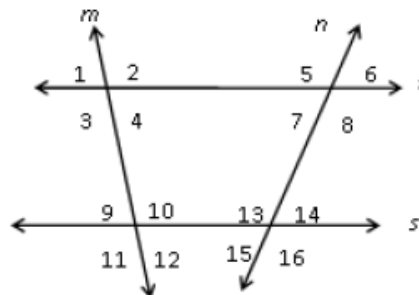
1. \_\_\_\_  $\angle 9$  &  $\angle 16$       5. \_\_\_\_  $\angle 9$  &  $\angle 11$   
 2. \_\_\_\_  $\angle 15$  &  $\angle 11$       6. \_\_\_\_  $\angle 9$  &  $\angle 15$   
 3. \_\_\_\_  $\angle 10$  &  $\angle 15$       7. \_\_\_\_  $\angle 13$  &  $\angle 14$   
 4. \_\_\_\_  $\angle 12$  &  $\angle 15$       8. \_\_\_\_  $\angle 14$  &  $\angle 11$

9.  $m\angle 2 = 97^\circ$        $m\angle 6 = 83^\circ$

$m\angle 3 =$  \_\_\_\_       $m\angle 5 =$  \_\_\_\_

$m\angle 10 =$  \_\_\_\_       $m\angle 7 =$  \_\_\_\_

$m\angle 9 =$  \_\_\_\_       $m\angle 16 =$  \_\_\_\_

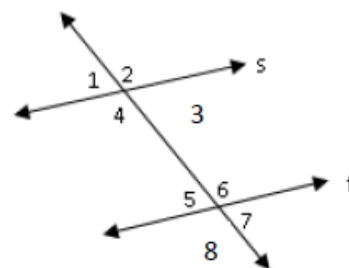


Find the value of x given that s // t

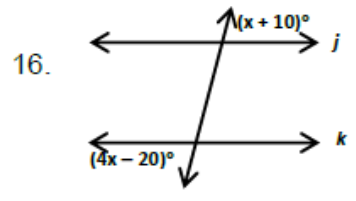
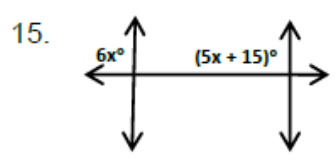
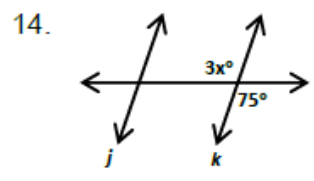
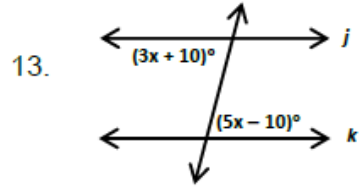
10.  $m\angle 4 = 77^\circ$ ,  $m\angle 8 = 4x + 57$

11.  $m\angle 3 = 5x + 13$ ,  $m\angle 5 = 53^\circ$

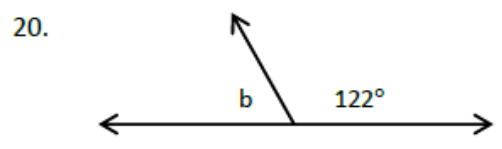
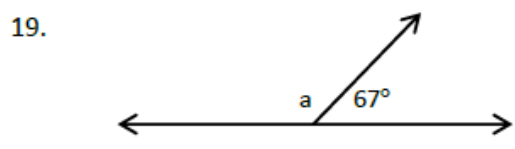
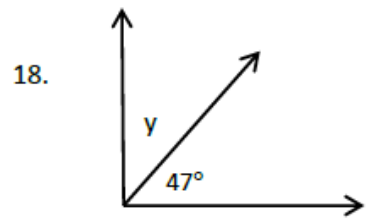
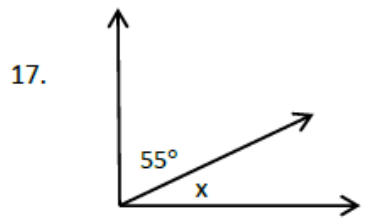
12.  $m\angle 1 = 6x - 5$ ,  $m\angle 7 = 115^\circ$



Find the value of  $x$  that makes  $j \parallel k$ .

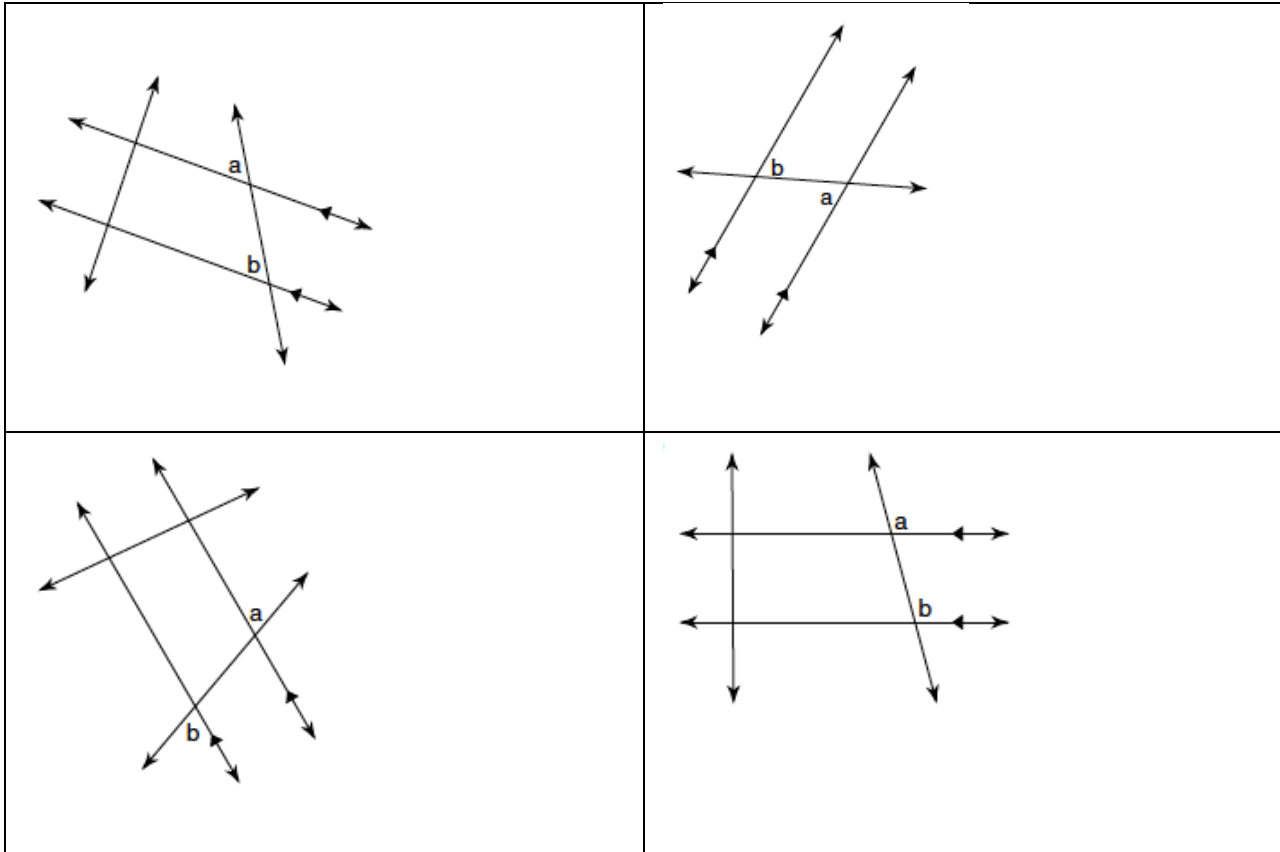


Determine the missing angles.

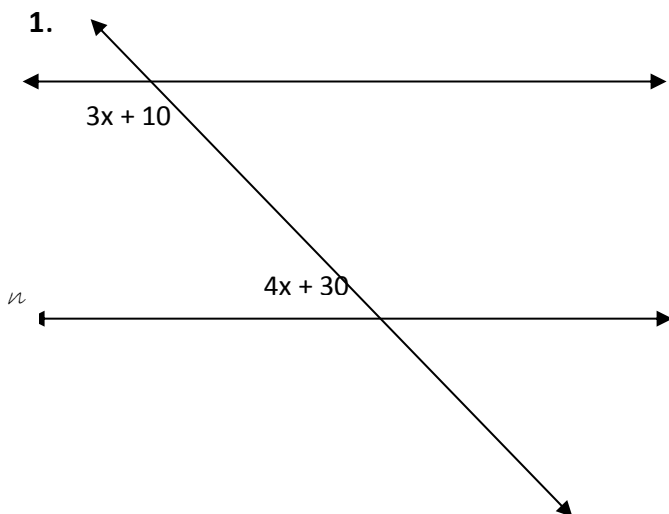


# Parallel Lines

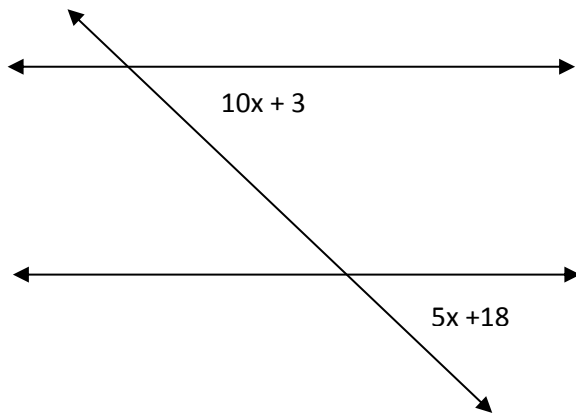
Name the relationship as alternate interior, corresponding, or alternate exterior.



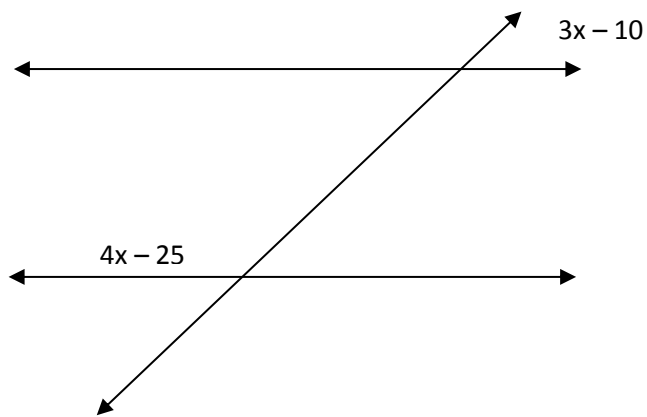
Find the missing measures on all the angles below.



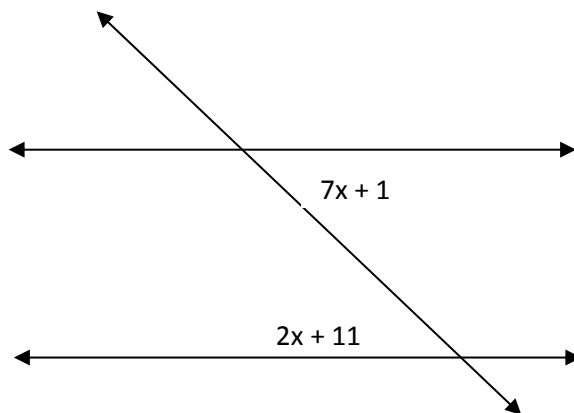
2.



3.



4.



Kuta Software - Infinite Geometry

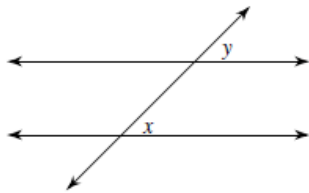
Name \_\_\_\_\_

Parallel Lines and Transversals

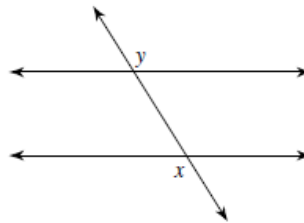
Date \_\_\_\_\_ Period \_\_\_\_

Identify each pair of angles as corresponding, alternate interior, alternate exterior, or consecutive interior.

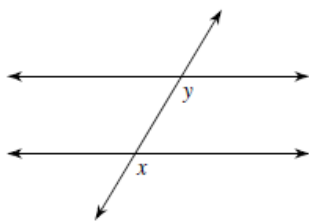
1)



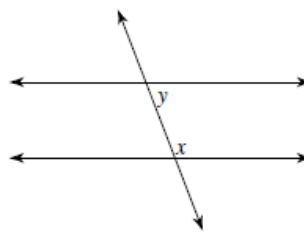
2)



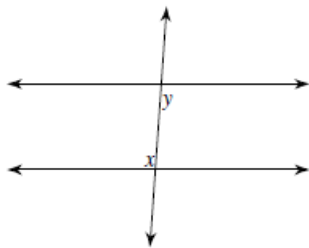
3)



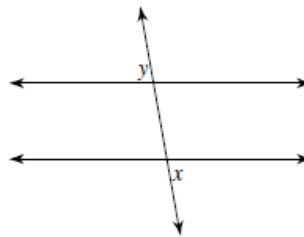
4)



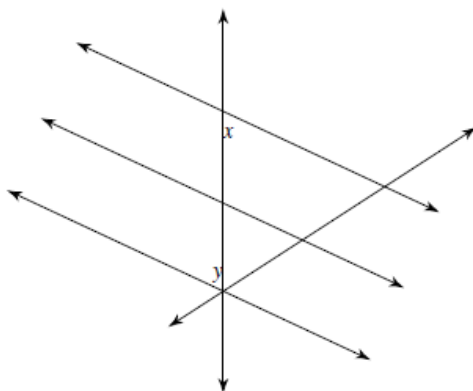
5)



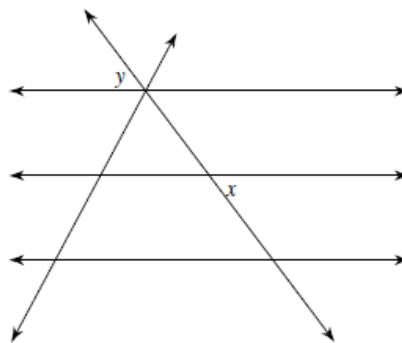
6)



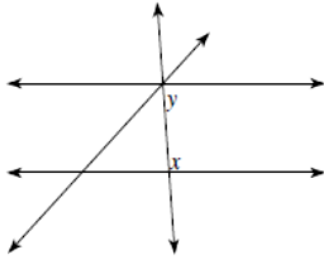
7)



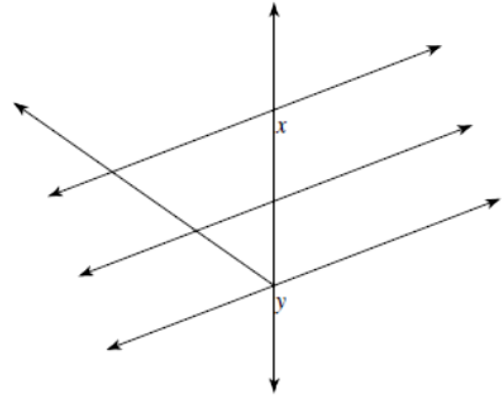
8)



9)

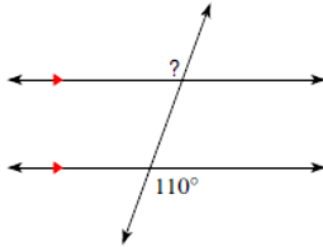


10)

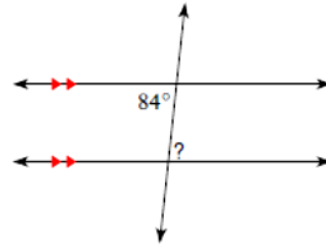


Find the measure of each angle indicated.

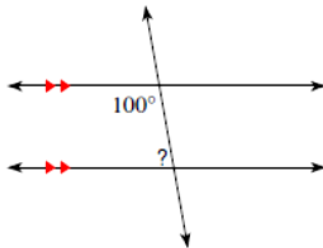
11)



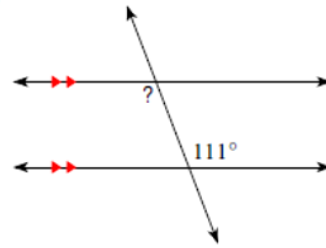
12)



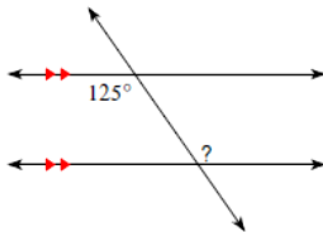
13)



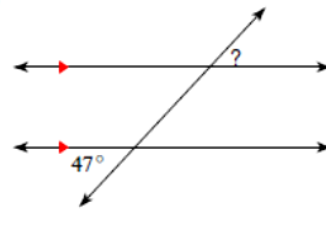
14)



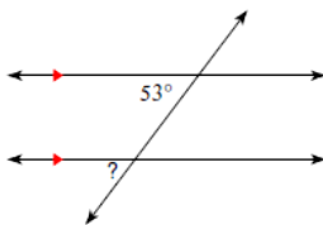
15)



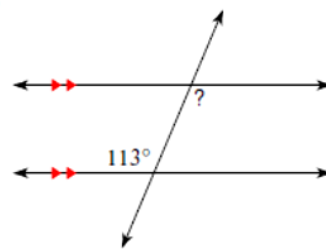
16)



17)

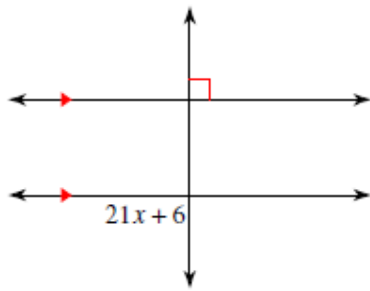


18)

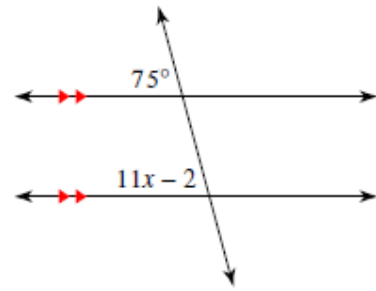


Solve for  $x$ .

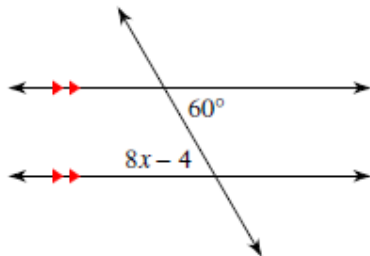
19)



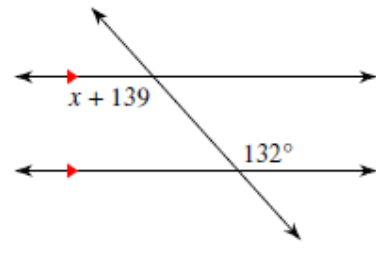
20)



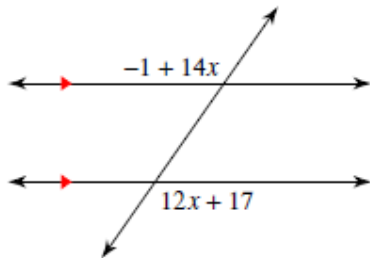
21)



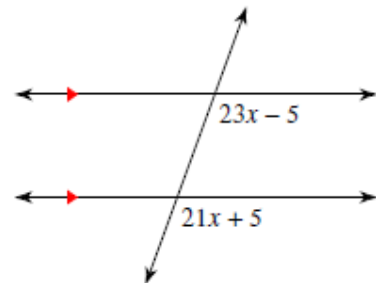
22)



23)

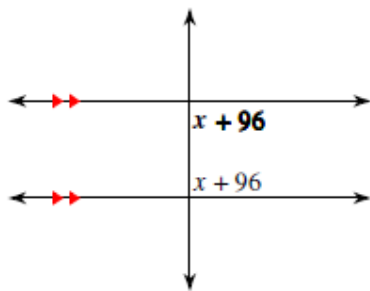


24)

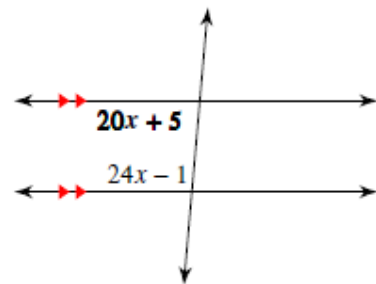


Find the measure of the angle indicated in bold.

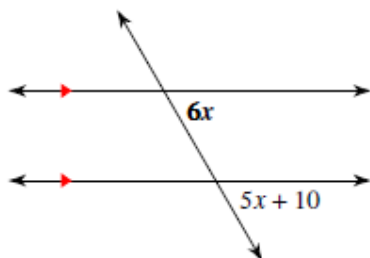
25)



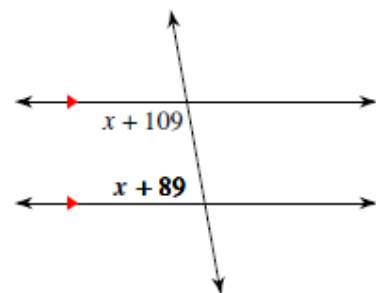
26)



27)



28)



## **Classifying Triangles by Sides:**

Name each type and draw a picture of each.

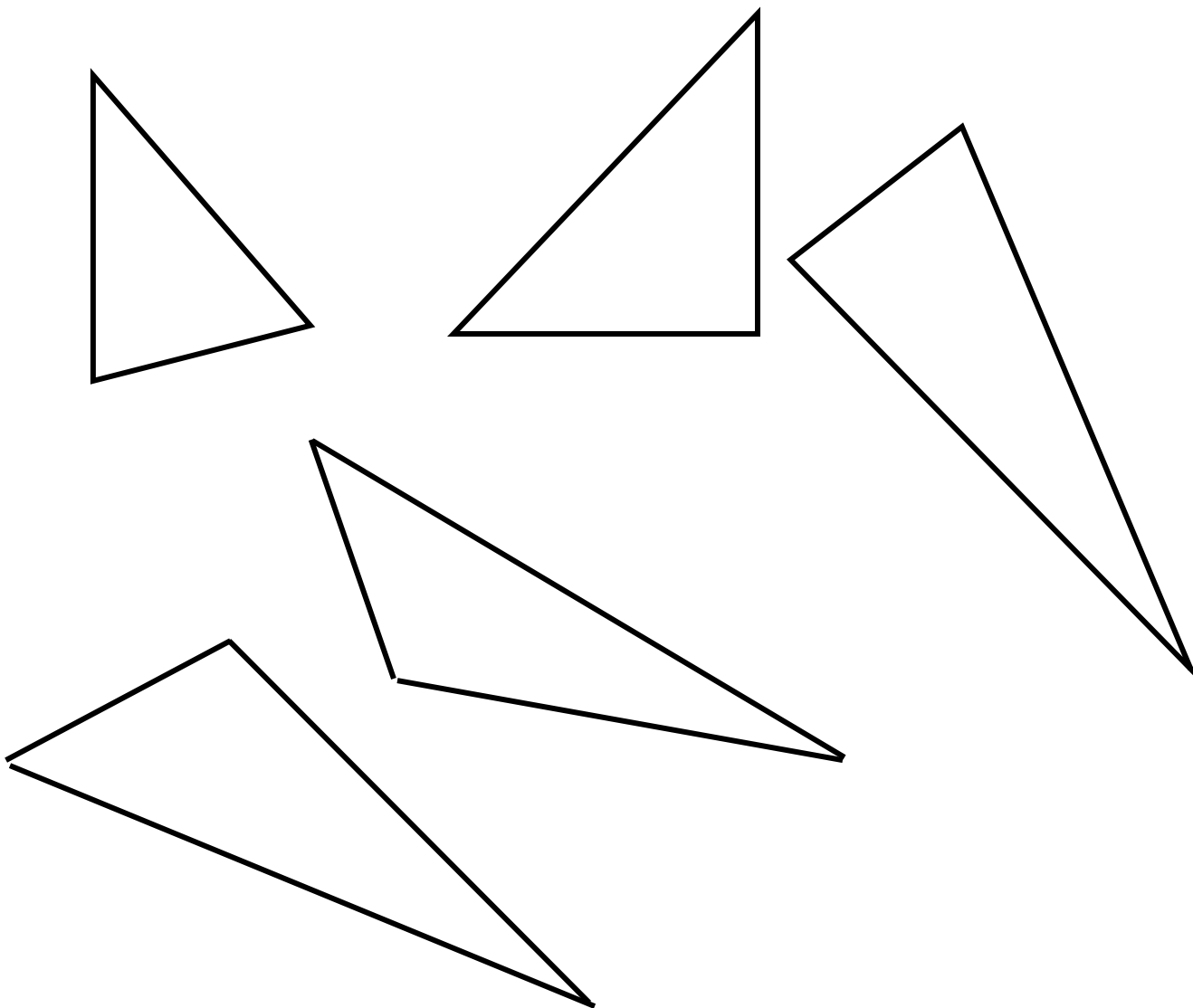
## **Classifying Triangles by Angles:**

Name each type and draw a picture of each.



Using a ruler, measure each side of each triangle (in cm to nearest tenth).

What do you notice about the relationship between the two shorter sides and the longest side?



Can you draw a triangle with sides of 2, 3, and 7? EXPLAIN:

Can you draw a triangle with sides of 5, 5, and 12? EXPLAIN:

Can you draw a triangle with sides of 5, 3, and 7? EXPLAIN:

After your investigation, complete the following statement:

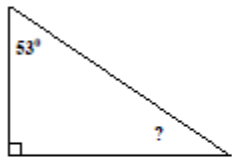
**In any triangle, the sum of the two \_\_\_\_\_ sides will be \_\_\_\_\_  
than the length of the longest side.**

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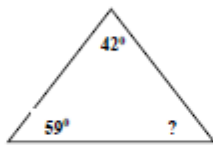
Fill in the missing information for each triangle named.

TRIANGLE	Length of Side 1	Length of Side 2	Length of Side 3	Sum of all Sides	Name of Triangle by Sides
Triangle MAD	12 mm		12 mm	42 mm	
Triangle ZEN		15 mm			Equilateral $\Delta$
Triangle POD	5 mm	9 mm		28 mm	
Triangle CAT				60 mm	Equilateral $\Delta$
Triangle CRY		8 mm	13 mm	29 mm	Isosceles $\Delta$

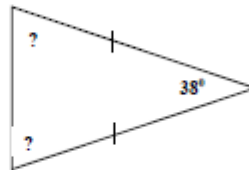
Identify the missing measurement for each triangle below and then classify the triangle by its angles. DO NOT USE A PROTRACTOR. (Triangles shown are not to scale.)



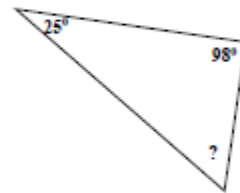
Missing Measure: \_\_\_\_\_  
Name: \_\_\_\_\_



Missing Measure: \_\_\_\_\_  
Name: \_\_\_\_\_



Missing Measure: \_\_\_\_\_  
Name: \_\_\_\_\_

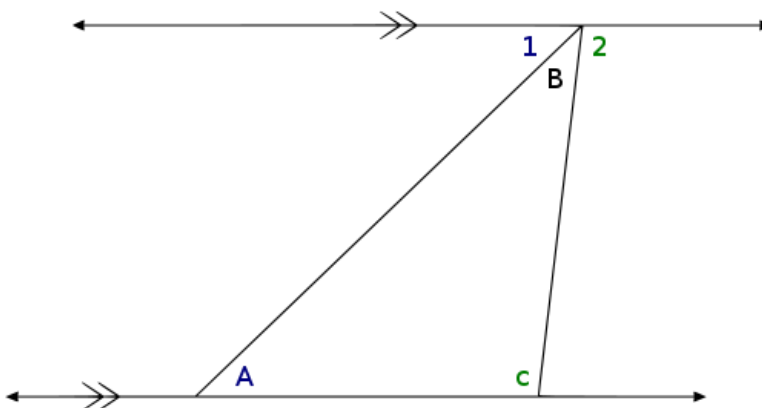


Missing Measure: \_\_\_\_\_  
Name: \_\_\_\_\_

## Making Connections - Parallel Lines and the Triangle Sum Theorem

How can I show that the sum of the interior angles of a triangle is equal to  $180^\circ$  using what I know about the relationships between the angles of parallel lines cut by a transversal?

Use the following figure to answer the questions that follow.



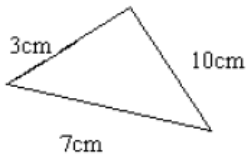
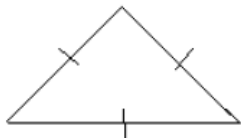
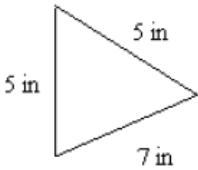
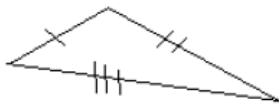
1. Knowing that angle 1, angle B and angle 2 form a straight line, what is their sum?
2. What kind of angles are angle C and angle 2? What is their relationship?
3. What kind of angles are angle A and angle 1? What is their relationship?
4. Based on your answers to questions 1 - 3, how do you know that the sum of the angle A, angle B, and angle C is  $180^\circ$ ?

### TRIANGLE SUM THEOREM:

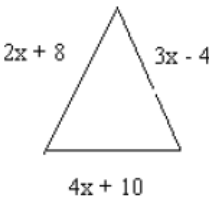
**The sum of all 3 angles of a triangle ALWAYS EQUALS  $180^\circ$ .**

### Triangle Homework

For #1-4, name the triangle

<p>1) _____</p> 	<p>2) _____</p> 
<p>3) _____</p> 	<p>4) _____</p> 

For numbers 5-8, find the missing side length.

<p>5) The perimeter of an equilateral triangle is 45cm. What is the length of each side?</p>	<p>6) If the perimeter of the triangle below is 36in find the value of <math>x</math> and the length of each side.</p> 
<p>7) Two sides of an isosceles triangle are 4 less than twice the value of the third side. If the perimeter of the triangle is 42cm, what is the value of <math>x</math>? What are the lengths of the 3 sides?</p>	<p>8) The perimeter of an equilateral triangle is 108in. Find the length of each side.</p> <p>An isosceles triangle has the same perimeter, what can be the lengths of the sides?</p>

For numbers 9-12, state whether the sides can form a triangle

<p>9) 2cm, 6cm, 4cm</p>	<p>10) 9cm, 11cm, 4cm</p>
<p>11) 15cm, 7cm, 9cm</p>	<p>12) 60cm, 60cm, 20cm</p>

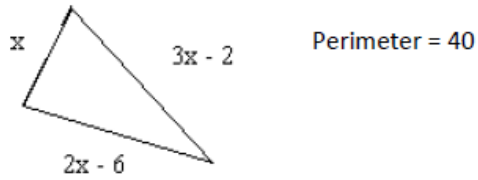
Find the value of  $x$  and the measurement of each side:

1)  $x =$  \_\_\_\_\_

Side 1 = \_\_\_\_\_

Side 2 = \_\_\_\_\_

Side 3 = \_\_\_\_\_

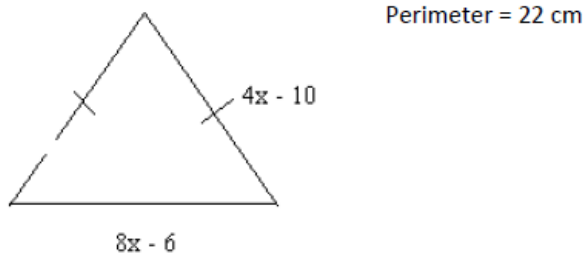


2)  $x =$  \_\_\_\_\_

Side 1 = \_\_\_\_\_

Side 2 = \_\_\_\_\_

Side 3 = \_\_\_\_\_

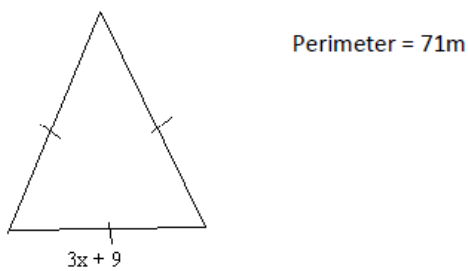


3)  $x =$  \_\_\_\_\_

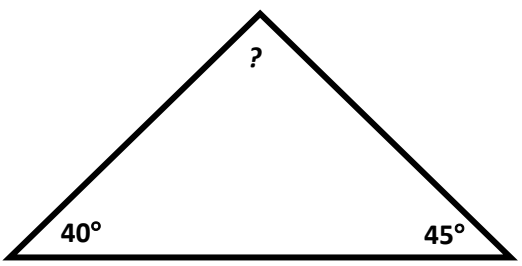
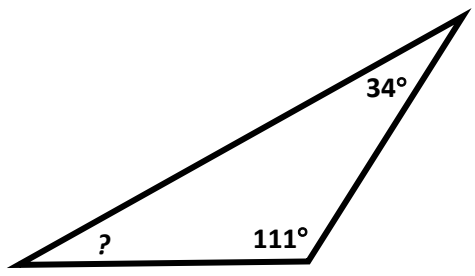
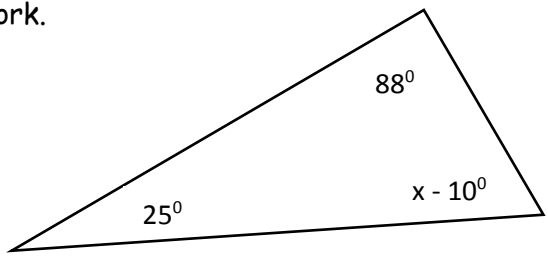
Side 1 = \_\_\_\_\_

Side 2 = \_\_\_\_\_

Side 3 = \_\_\_\_\_



Find each missing angle measure.

<p>1.</p> 	<p>2. In a triangle the measure of two of the angles is <math>35^\circ</math> and <math>65^\circ</math>. Find the measure of the third angle.</p>
<p>3. In triangle <math>DEF</math> the measure of angle <math>D</math> is <math>33^\circ</math> and the measure of angle <math>E</math> is <math>97^\circ</math>. Find the measure of angle <math>F</math>.</p>	<p>4.</p> 
<p>5. Triangle <math>ABC</math> is a right triangle. The measure of angle <math>A</math> is <math>37^\circ</math>. Find the measures of angle <math>B</math> and <math>C</math>.</p>	<p>6. Four isosceles triangles cap the Smith Tower in Seattle. If one of the base angles measures <math>65^\circ</math>, what are the measures of the other two angles?</p>
<p>7. Find the missing angle measure without using a protractor. Triangle is not drawn to scale. Set up an equation and show your work.</p> 	<p>8. Draw a triangle and give it the following measures then list the measure of all three angles. <math>m\angle 1 = 102^\circ</math>, <math>m\angle 2 = x + 2</math>, and <math>m\angle 3 = x + 20</math>.</p> <p><math>m\angle 1 = \underline{\hspace{2cm}}</math></p> <p><math>m\angle 2 = \underline{\hspace{2cm}}</math></p> <p><math>m\angle 3 = \underline{\hspace{2cm}}</math></p>

9. Can you draw a right triangle that is also an isosceles triangle? Explain.

10. Can a triangle have more than one obtuse angle? Explain.

Tell if the following combinations are lengths that could create a triangle.

11. 3, 5, 9

12. 8, 8, 8

13. 7, 8, 2

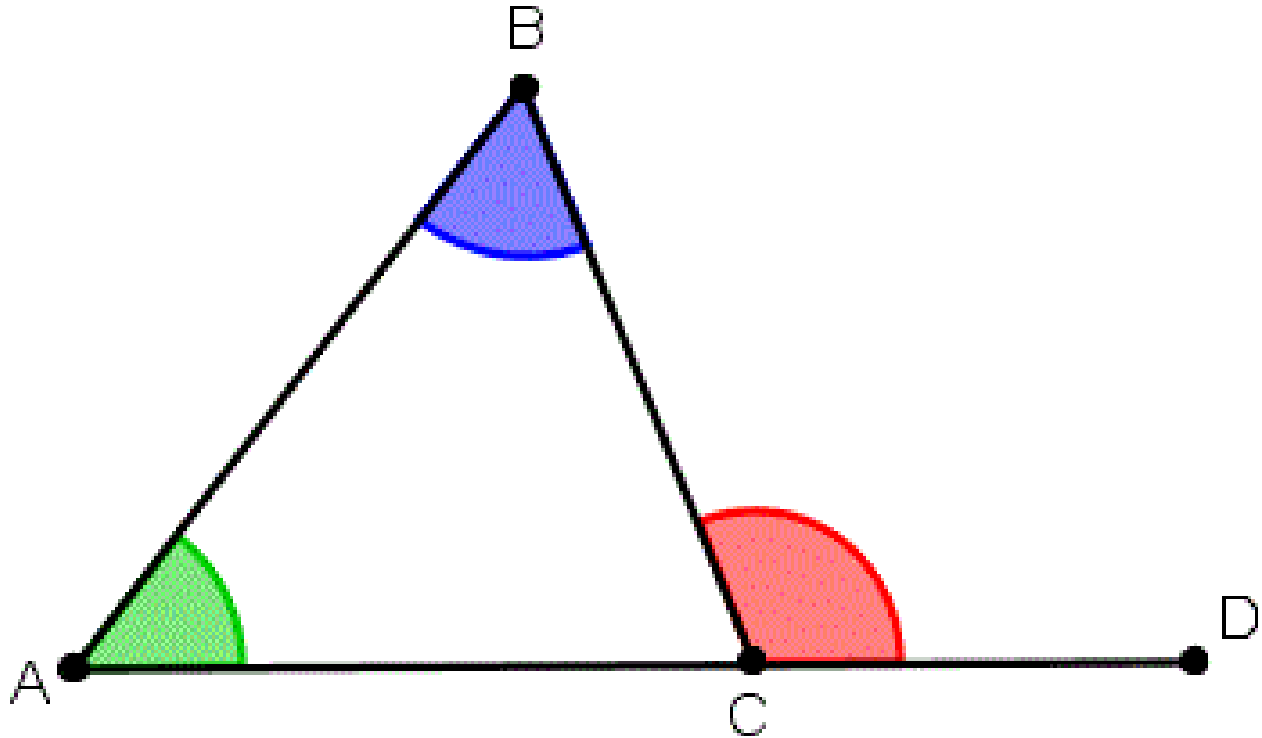
How did you determine the answers to #11-13?

14. In congruent triangles, what is true about corresponding sides?

---

15. In congruent triangles, what is true about corresponding angles?

## Triangles...Exterior Angle Theorem



Using a protractor, measure these angles:

$$\angle BAC = \underline{\hspace{2cm}}^\circ$$

$$\angle ABC = \underline{\hspace{2cm}}^\circ$$

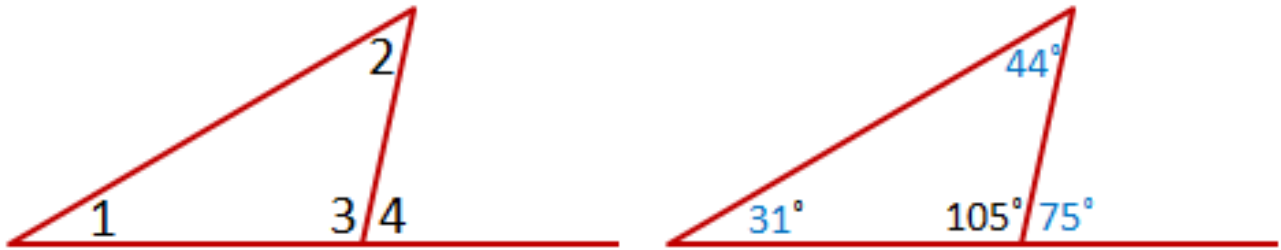
$$\angle ACB = \underline{\hspace{2cm}}^\circ$$

What is the relationship between these angles?

How could you use that relationship to find missing angles?



Which angles are interior and which exterior?



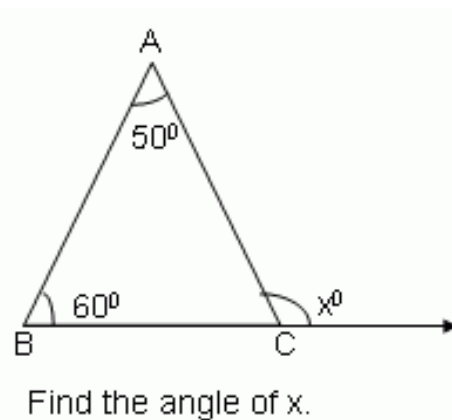
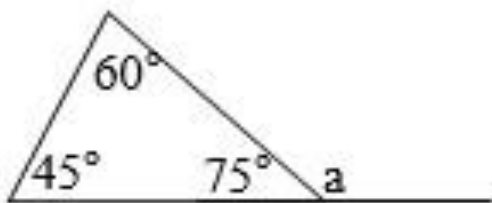
What's the relationship between angles 3 and 4?

What do you know about the sum of angles 1, 2, and 3?

So, what is the relationship between angles 1 and 2 and angle 4?

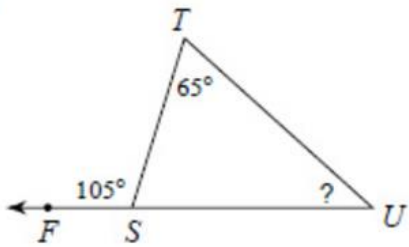
Does this work at the top right with the angle measures given? Why?

Use what you've learned to find the missing angles:

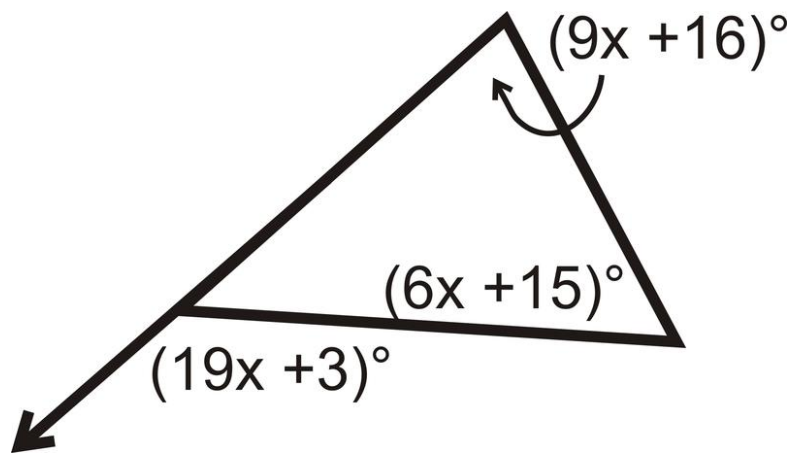
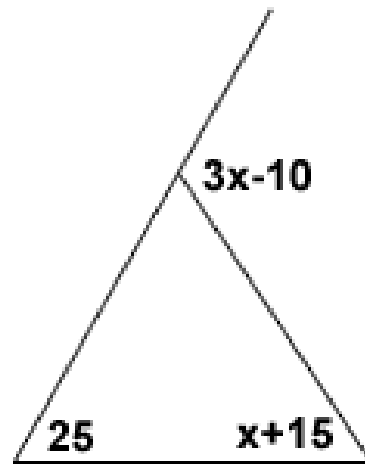
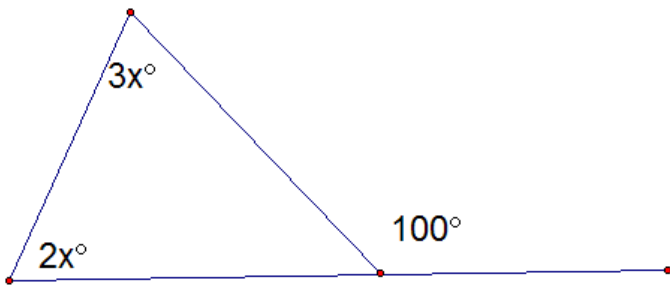
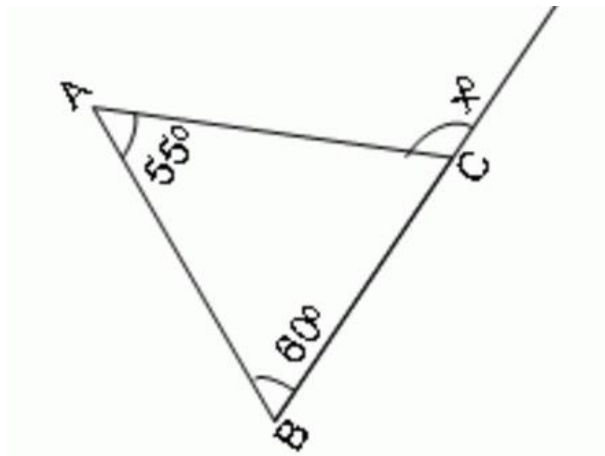


Find all missing angle measures.

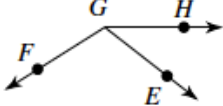
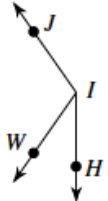
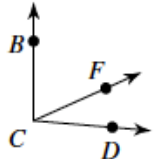
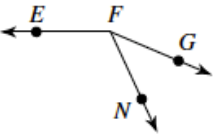
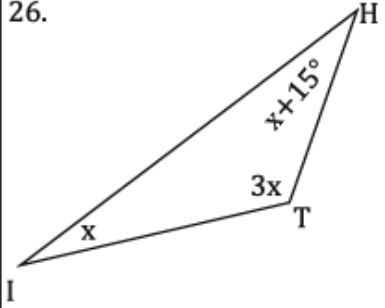
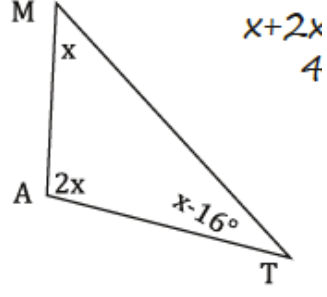
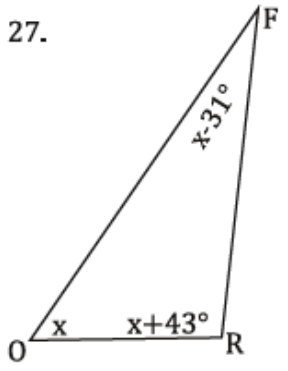
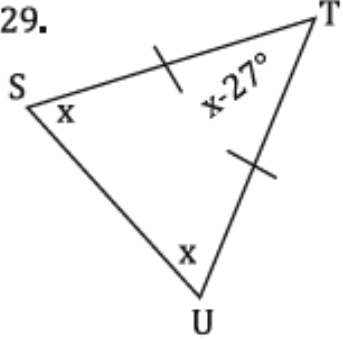
1)



- A)  $35^\circ$
- B)  $75^\circ$
- C)  $40^\circ$
- D)  $36^\circ$

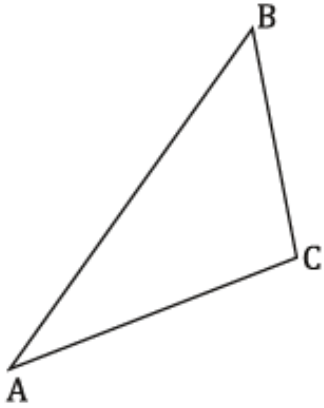


### Find the Missing Angle Practice

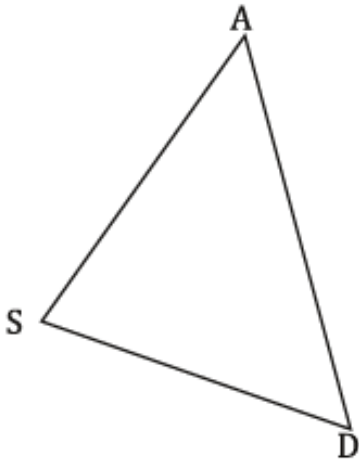
<p><math>m\angle HGF = 16x + 4</math>, <math>m\angle EGF = 110^\circ</math>, and <math>m\angle HGE = 3x + 11</math>. Find <math>x</math>.</p> 	<p>Find <math>m\angle HIW</math> if <math>m\angle WIJ = 10x</math>, <math>m\angle HIJ = 145^\circ</math>, and <math>m\angle HIW = 2x + 13</math>.</p> 
<p><math>m\angle FCD = x + 41</math>, <math>m\angle BCF = x + 78</math>, and <math>m\angle BCD = 95^\circ</math>. Find <math>x</math>.</p> 	<p><math>m\angle GFN = 4x + 10</math>, <math>m\angle NFE = 14x + 3</math>, and <math>m\angle GFE = 157^\circ</math>. Find <math>m\angle NFE</math>.</p> 
<p>26.</p> 	
<p>27.</p> 	<p>29.</p> 

Mark the diagram with the given information. Then, find the measure of the indicated angle.

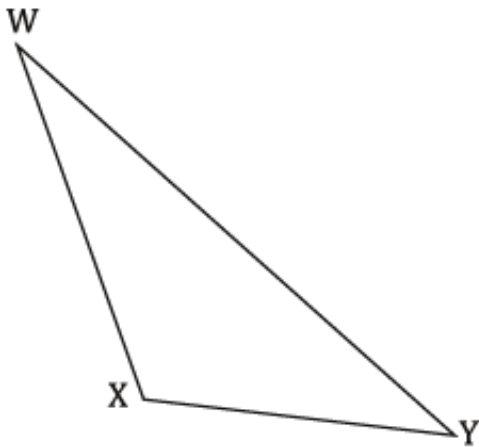
31.  $m\angle A = X$ ,  $m\angle B = 2X$ ,  $m\angle C = 2X + 30^\circ$ . Find  $m\angle B$ .



32.  $m\angle S = 2x$ ,  $m\angle A = X - 23$ ,  $m\angle D = X - 17^\circ$ .  
Find  $m\angle S$ .

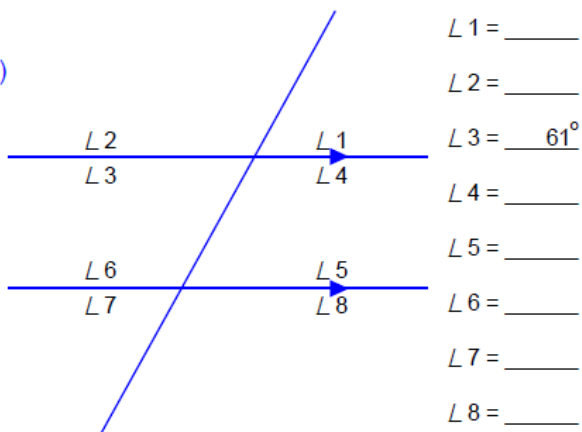


35.  $m\angle W = x - 22^\circ$ ,  $m\angle X = 3x + 19^\circ$ ,  $m\angle Y = x - 17^\circ$ . Find  $m\angle X$ .

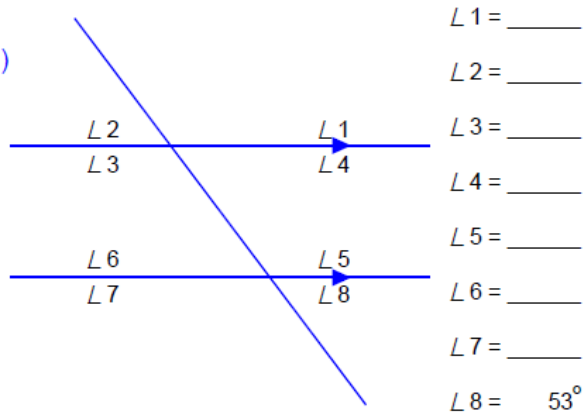


Find all of the missing angles.

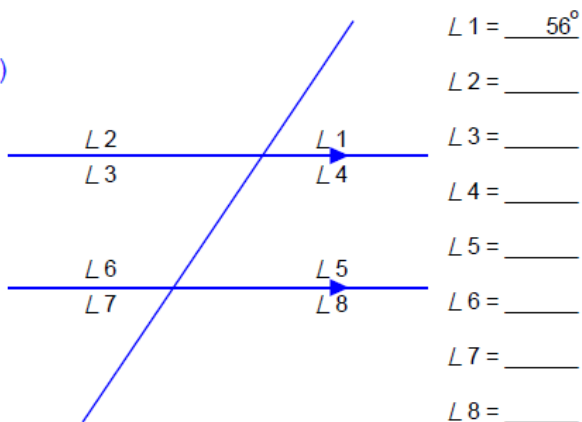
1)



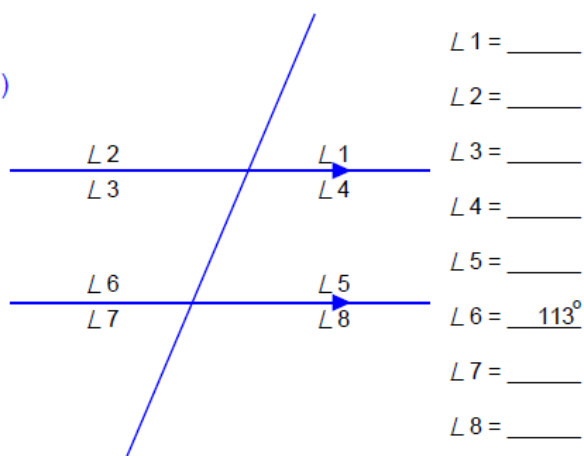
2)



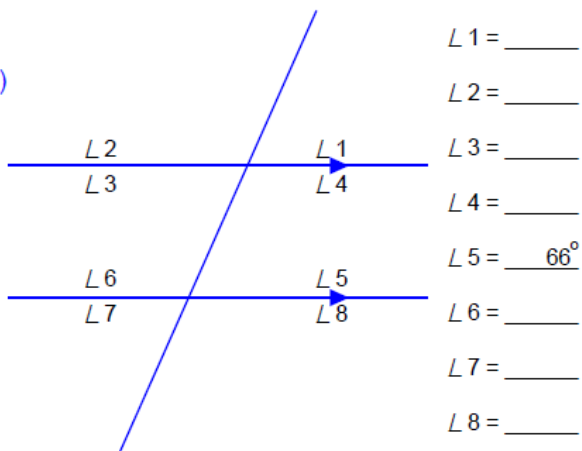
3)



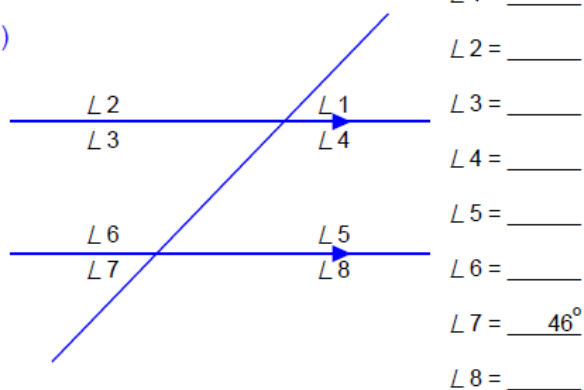
4)



5)



6)



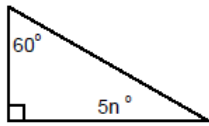
Math-Aids.Com



**Triangle Angle Sum**

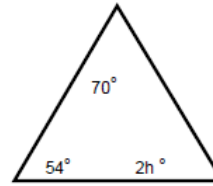
Solve for the given variable.

1)



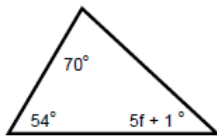
$$n = \underline{\quad}$$

5)



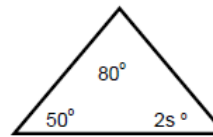
$$h = \underline{\quad}$$

2)



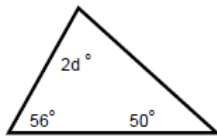
$$f = \underline{\quad}$$

6)



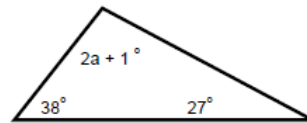
$$s = \underline{\quad}$$

3)



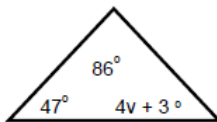
$$d = \underline{\quad}$$

7)



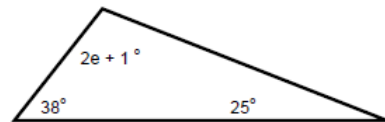
$$a = \underline{\quad}$$

4)



$$v = \underline{\quad}$$

8)



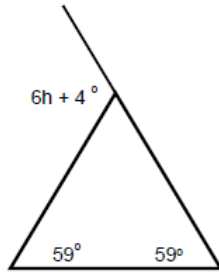
$$e = \underline{\quad}$$



**Exterior Angle Theorem**

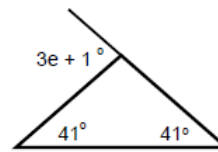
Solve for the given variable.

1)



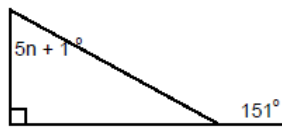
$$h = \underline{\quad}$$

5)



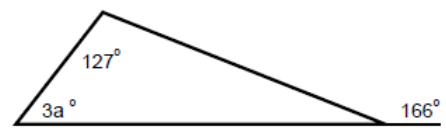
$$e = \underline{\quad}$$

2)



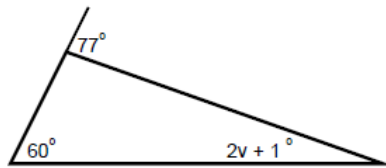
$$n = \underline{\quad}$$

6)



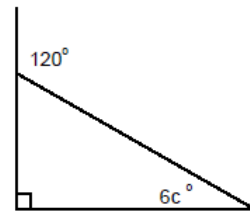
$$a = \underline{\quad}$$

3)



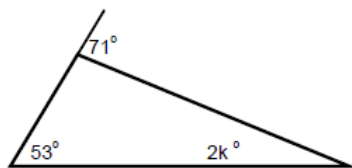
$$v = \underline{\quad}$$

7)



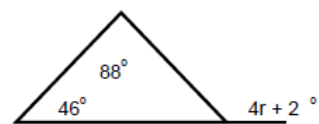
$$c = \underline{\quad}$$

4)



$$k = \underline{\quad}$$

8)



$$r = \underline{\quad}$$




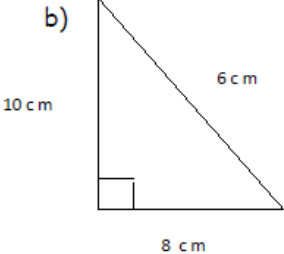
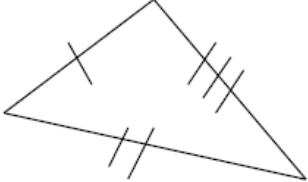
# STUDY GUIDE

## Unit 10 Review for Assessment

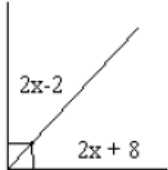
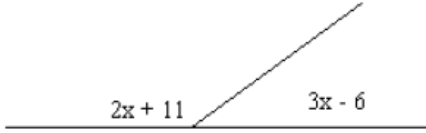
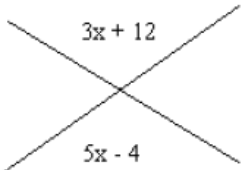
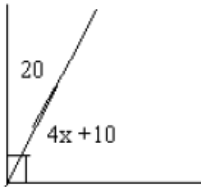
Define the following words:

<ul style="list-style-type: none"> <li>• supplementary angles</li> <li>• complementary angles</li> <li>• vertical angles</li> <li>• adjacent angles</li> <li>• acute triangle</li> <li>• obtuse triangle</li> <li>• right triangle</li> <li>• isosceles triangle</li> <li>• scalene triangle</li> </ul>	<ul style="list-style-type: none"> <li>• equilateral triangle</li> <li>• parallel lines</li> <li>• transversal</li> <li>• congruent angles</li> <li>• corresponding angles</li> <li>• alternate interior angles</li> <li>• alternate exterior angles</li> <li>• triangle sum theorem</li> <li>• exterior angle theorem</li> </ul>
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Name each triangle by its sides and lengths

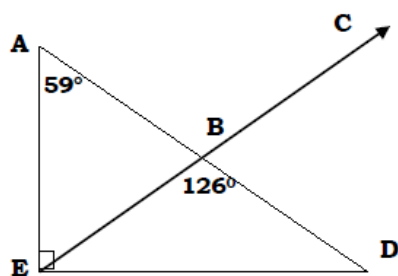
<p>a)</p>  <p>_____</p>	<p>b)</p>  <p>_____</p>	<p>c)</p>  <p>_____</p>
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For # 1-10, find the measure of the missing angle

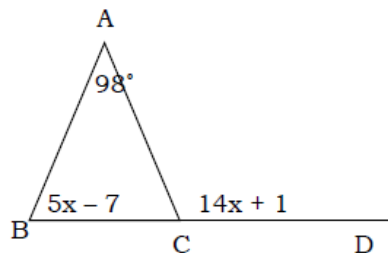
<p>1)</p> 	<p>2)</p> 
<p>3)</p> 	<p>4)</p> 



5) Use the diagram to find the missing angle measures B and D.



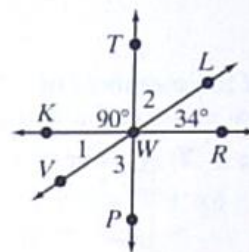
6)



## Practice 9-2 Angle Relationships and Parallel Lines

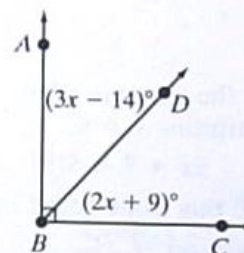
Find the measure of each angle in the figure at the right.

1.  $m\angle 1$
2.  $m\angle 2$
3.  $m\angle 3$
4.  $m\angle VWR$



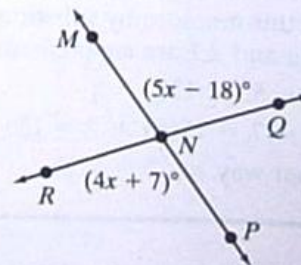
Use the figure at the right for Exercises 5-8.

5. Write an equation. \_\_\_\_\_
6. Find the value of  $x$ . \_\_\_\_\_
7. Find  $m\angle ABD$ . \_\_\_\_\_
8. Find  $m\angle DBC$ . \_\_\_\_\_



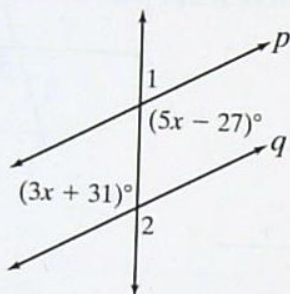
Use the figure at the right for Exercises 9-12.

9. Write an equation. \_\_\_\_\_
10. Find the value of  $x$ . \_\_\_\_\_
11. Find  $m\angle MNQ$ . \_\_\_\_\_
12. Find  $m\angle MNR$ . \_\_\_\_\_



In each figure, find the measures of  $\angle 1$  and  $\angle 2$ .

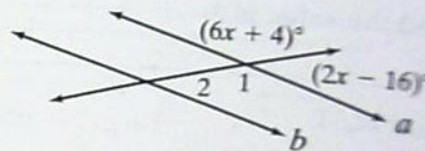
13. Given  $p \parallel q$ .



$m\angle 1 =$

$m\angle 2 =$

14. Given  $a \parallel b$ .



$m\angle 1 =$

$m\angle 2 =$

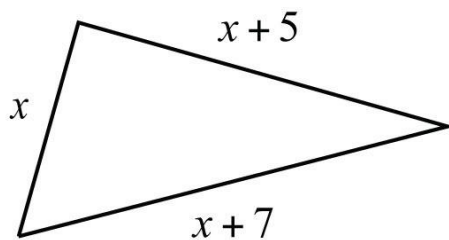
15. Find a pair of complementary angles such that the difference of their measures is  $12^\circ$ .

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Lesson 9-2 Practice

Could you have a triangle with side lengths 7cm, 8cm, and 1cm? Explain your reasoning.

Use the triangle below to find the perimeter (as much as you can).



If the triangle above has a perimeter of 27 units, what is the measure of each side?