WALT: multiply and divide fractions

WILF

 Use knowledge of times tables
Multiply the numerators together then multiply the denominators together
Keep, change, flip for division

Can you name the parts of a fraction?





What sort of fractions / numbers are these: proper fraction 8 mixed number $2\frac{3}{8}$ improper fraction⁹

Multiplying Fractions

$\frac{2}{3} \times \frac{3}{4} = \frac{2 \times 3}{3 \times 4} = \frac{6}{12} = \frac{1}{2}$

Multiply the numerators.
Multiply the denominators.
Cancel down.

 $\frac{2}{5} \times \frac{3}{4} = \frac{6}{20} = \frac{3}{10}$

 $\frac{1}{4} \times \frac{1}{2} = \frac{1}{8}$

 $\frac{3}{4} \times \frac{4}{5} = \frac{12}{20} = \frac{3}{5}$

 $\frac{4}{7} \times \frac{2}{5} = \frac{8}{35}$

 $\frac{1}{6} \times \frac{2}{5} = \frac{2}{30} = \frac{1}{15}$

 $\frac{5}{12} \times \frac{2}{5} = \frac{10}{60} = \frac{1}{6}$

 $\frac{5}{9} \times \frac{2}{3} = \frac{10}{27}$

 $\frac{3}{8} \times \frac{4}{9} = \frac{12}{72} = \frac{1}{6}$

Multiplying mixed numbers.

$2\frac{2}{5} \times \frac{1}{2} = \frac{12}{5} \times \frac{1}{2} = \frac{12}{10} = \frac{6}{5} = 1\frac{1}{5}$

- 1. Change the mixed number to an improper fraction.
- 2. Multiply as before.
- 3. Cancel down and change to mixed number if necessary.

 $\mathbf{1}\frac{1}{4} \times \frac{2}{7} = \frac{5}{4} \times \frac{2}{7} = \frac{10}{28} = \frac{5}{14}$

 $2\frac{1}{3} \times \frac{1}{2} = \frac{7}{3} \times \frac{1}{2} = \frac{7}{6} = 1\frac{1}{6}$

 $\frac{3}{4} \times 1\frac{4}{5} = \frac{3}{4} \times \frac{9}{5} = \frac{27}{20} = 1\frac{7}{20}$

 $\mathbf{1}\frac{4}{7} \times \mathbf{1}\frac{2}{5} = \frac{11}{7} \times \frac{7}{5} = \frac{77}{35} = \frac{11}{5} = \mathbf{2}\frac{1}{5}$

Multiplying fractions and whole numbers

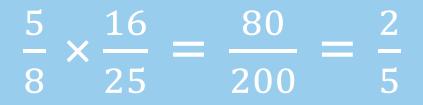
$12 \times \frac{5}{6} = \frac{12}{1} \times \frac{5}{6} = \frac{60}{6} = 10$

- 1. Whole numbers have a denominator of 1.
- 2. Multiply numerators and denominators.
- 3. Cancel down and change to a mixed number if necessary.

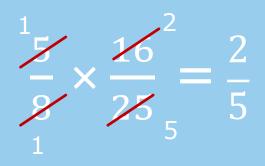
 $\frac{3}{4} \times 6 = \frac{3}{4} \times \frac{6}{1} = \frac{18}{4} = 4\frac{1}{2}$ $\frac{7}{8} \times 12 = \frac{7}{8} \times \frac{12}{1} = \frac{84}{8} = 10\frac{1}{2}$ $5 \times \frac{3}{10} = \frac{5}{1} \times \frac{3}{10} = \frac{15}{10} = 1\frac{1}{2}$ $\frac{5}{7} \times 4 = \frac{5}{7} \times \frac{4}{1} = \frac{20}{7} = 2\frac{6}{7}$ $7 \times \frac{2}{5} = \frac{7}{1} \times \frac{2}{5} = \frac{14}{5} = 2\frac{4}{5}$

Cancelling down.

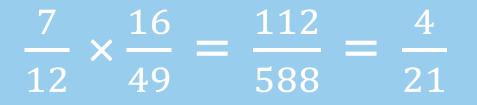
It is often easier to cancel down before you multiply. When you are multiplying fractions, any numerator can be cancelled against any denominator. After multiplication



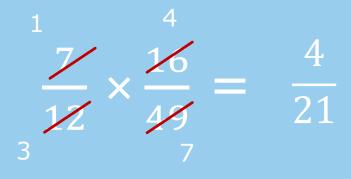
Before multiplication



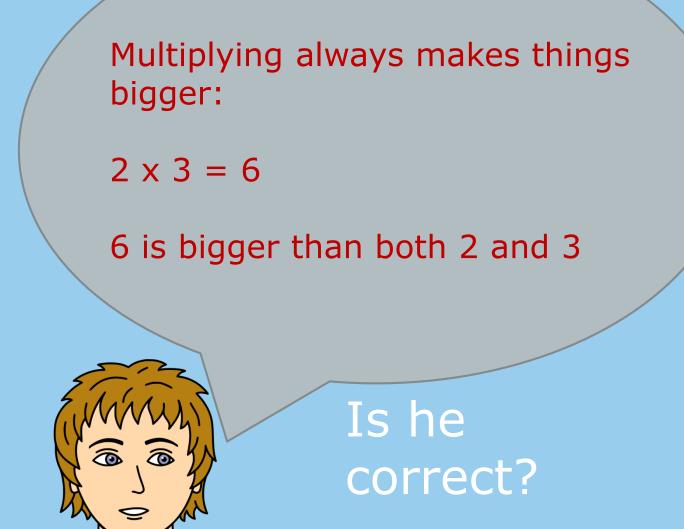
Cancelling after multiplication



Cancelling before multiplication



Which is easier?



If you multiply a number by 1, it does not increase or decrease.

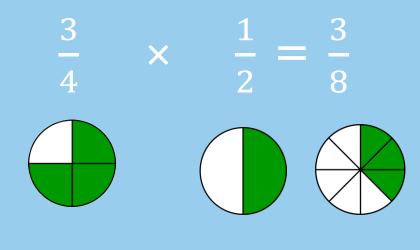
 $3 \times 1 = 3$

If you multiply a number by 0, you get 0 $3 \times 0 = 0$

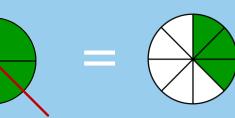
If you multiply a number larger than 1 by a proper fraction, the product is less than the original number.

 $4 \times \frac{1}{2} = 2$ (2 < 4)

If you multiply two proper fractions together, the product is less than either of them:



 $\frac{1}{2}$ of $\frac{3}{4} = \frac{3}{8}$



of means ×

 $\frac{3}{4} \text{ of } \frac{1}{2} = \frac{3}{8}$

Dividing Fractions

$\frac{3}{4} \div \frac{1}{3} = \frac{3}{4} \div \frac{3}{3} = \frac{9}{4} = 2\frac{1}{4}$

- 1. Turn the dividing fraction upside down and change ÷ to ×.
- 2. Multiply numerators and denominators.
- 3. If necessary cancel down and change to a mixed number.

 $\frac{2}{5} \div \frac{1}{4} = \frac{2}{5} \div \frac{4}{4} = \frac{8}{5} = 1\frac{3}{5}$ $\frac{2}{5} = \frac{3}{7} \div \frac{3}{2} = \frac{15}{14} = 1\frac{1}{14}$ 3 7 $\frac{\$}{\$} = \frac{24}{4} = 6$ $\frac{3}{4} \div \frac{1}{8} = \frac{3}{4} \div$ $\frac{1}{3} = \frac{5}{6} \div \frac{3}{3} = \frac{15}{6} = 2\frac{1}{2}$ 5 6 $\frac{4}{9} \div \frac{1}{2} = \frac{4}{9} \div \frac{2}{2} =$ 8 ______ 9

Dividing mixed numbers.

$2\frac{2}{5} \div \frac{1}{2} = \frac{12}{5} \div \frac{1}{2} = \frac{12}{5} \times \frac{2}{1} = \frac{24}{5} = 4\frac{4}{5}$

- 1. Change the mixed number to an improper fraction.
- 2. Divide as before.
- 3. Cancel down and change to a mixed number if necessary.

 $\mathbf{1}_{\frac{5}{5}}^{\frac{4}{5}} \div \frac{1}{\frac{3}{5}} = \frac{9}{5} \div \frac{1}{\frac{3}{5}} = \frac{9}{5} \times \frac{3}{\frac{1}{5}} = \frac{27}{5} = 5\frac{2}{5}$ $2\frac{1}{3} \div \frac{7}{9} = \frac{7}{3} \div \frac{7}{9} = \frac{7}{3} \times \frac{9}{7} = \frac{63}{21} = 3$ $3\frac{1}{2} \div \frac{3}{8} = \frac{7}{2} \div \frac{3}{8} = \frac{7}{2} \times \frac{8}{3} = \frac{56}{6} = 9\frac{1}{3}$ $3\frac{2}{3} \div 1\frac{1}{6} = \frac{11}{3} \div \frac{7}{6} = \frac{11}{3} \times \frac{6}{7} = \frac{66}{21} = 3\frac{1}{7}$

 $\frac{9}{10} \div \mathbf{1}\frac{1}{5} = \frac{9}{10} \div \frac{6}{5} = \frac{9}{10} \times \frac{5}{6} = \frac{45}{60} = \frac{3}{4}$

Dividing fractions and whole numbers

$8 \div \frac{3}{5} = \frac{8}{1} \div \frac{5}{3} = \frac{40}{3} = 13\frac{1}{3}$

1. Whole numbers have a denominator of 1.

2. Turn dividing fraction upside down and multiply numerators and denominators.

3. Cancel down and change to a mixed number if necessary.

$$6 \div \frac{2}{3} = \frac{6}{1} \div \frac{2}{3} = \frac{6}{1} \times \frac{3}{2} = \frac{18}{2} = 9$$

$$4 \div \frac{2}{5} = \frac{4}{1} \div \frac{2}{5} = \frac{4}{1} \times \frac{5}{2} = \frac{20}{2} = 10$$

$$7 \div \frac{5}{6} = \frac{7}{1} \div \frac{5}{6} = \frac{7}{1} \times \frac{6}{5} = \frac{42}{5} = 8\frac{2}{5}$$

$$5 \div \frac{6}{7} = \frac{5}{1} \div \frac{6}{7} = \frac{5}{1} \times \frac{7}{6} = \frac{35}{6} = 5\frac{5}{6}$$

$$8 \div \frac{7}{9} = \frac{8}{1} \div \frac{7}{9} = \frac{8}{1} \times \frac{9}{7} = \frac{72}{7} = 10\frac{2}{7}$$

$$\frac{3}{4} \div 6 = \frac{3}{4} \div \frac{6}{1} = \frac{3}{4} \times \frac{1}{6} = \frac{3}{24} = \frac{1}{8}$$

Division always makes things smaller. If I divide up a rich, tasty chocolate cake, I always get a smaller piece than the whole cake.

 $12 \div 4=3$

3 is less than 12

Is she correct?

If you divide a number by 1, it does not increase or decrease.

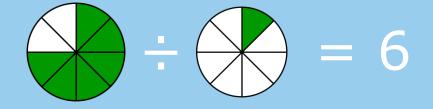
 $3 \div 1 = 3$

If you divide 1, or a number larger than 1, by a proper fraction, the answer is greater than the original number.

 $4 \div \frac{1}{2} = 8 \ (8 > 4)$

If you divide a larger fraction by a smaller one, the answer will be more than 1.

 $\frac{3}{4} \div \frac{1}{8} = 6$



How many $\frac{1}{8}$ are there in $\frac{3}{4}$? 6

1) $\frac{1}{3} \times \frac{1}{3} =$ $\frac{1}{2} \div \frac{1}{4} =$ 6) 2) $\frac{1}{5} \times \frac{1}{5} =$ 7) $\frac{1}{5} \div \frac{3}{10} =$ $\begin{array}{c} \frac{1}{6} \times \frac{1}{6} = \\ \end{array}$ $\begin{array}{c} 4) \quad \frac{2}{7} \times \frac{4}{5} = \end{array}$ $\frac{1}{6} \div \frac{1}{12} =$ 8) 9) $\frac{7}{2} \div \frac{5}{4} =$ 5) $\frac{1}{2} \times \frac{2}{5} =$ 10) $\frac{9}{7} \div \frac{1}{14} =$

6) 1) $\frac{7}{9} \times \frac{4}{5} =$ $\frac{7}{9} \div \frac{4}{7} =$ 2) $\frac{6}{7} \times \frac{11}{12} =$ 7) $\frac{6}{7} \div \frac{11}{12} =$ $\frac{10}{11} \times \frac{12}{15} =$ 8) $\frac{14}{15} \div \frac{8}{9} =$ 3) 9) $\frac{16}{17} \div \frac{21}{23} =$ 4) $2\frac{1}{3} \times \frac{1}{2} =$ 10) $4\frac{1}{3} \div \frac{1}{2} =$ $4\frac{1}{5} \times \frac{1}{4} =$ 5)