

## Welcome to Chem 253

<http://www.cchem.berkeley.edu/pdygrp/chem253.html>

## Chemistry 253 A & B Materials & Solid State Chemistry

**Lecture: Tu. Thurs. 12:30-2:00 pm @ 425 Latimer**

**Instructor:**

**Professor Peidong Yang, B68 Hild.,  
Office Hours: Friday 10:00-12:00pm or by appointment  
[p\\_yang@berkeley.edu](mailto:p_yang@berkeley.edu)**

**TA:**

Michael Moore  
[michael.moore@berkeley.edu](mailto:michael.moore@berkeley.edu)

Chong Liu  
[chongliu@berkeley.edu](mailto:chongliu@berkeley.edu)

**Grading:**

**Problem sets (2)**                      **40%**

**Final**                                      **60%**

**Description:**

Structure and structure determination of crystalline solids;  
Solid State Synthesis  
Solid State Characterization  
Electronic band structure;  
Chemical bonding in solids;  
Structure-property relationships.

**Main Reference Books**

West: Basic solid state chemistry (Wiley, 1999).

West: Solid State Chemistry and its Applications (Wiley, 1988)

Gersten and Smith: The Physics and Chemistry of Materials (Wiley,  
2001)

Hoffmann: Solids and Surfaces (VCH, 1988)

Burdett: Chemical Bonding in Solids (Oxford 1995)

Kittel: Introduction to solid State Physics (Wiley, 1996)

Ashcroft and Mermin: Solid State Physics (Saunders College, latest  
edition)

Cheetham and Day: Solid State Chemistry: Techniques (Oxford, 1987)

Cheetham and Day: Solid State Chemistry: Compounds (Oxford, 1992)

Cox: The Electronic Structure and Chemistry of Solids (Oxford, 1987)

Wells: Structural Inorganic Chemistry (Clarendon Press, 1984)

Wold and Dwight: Solid State Chemistry (Chapman Hall, 1993)

## Materials Chemistry I

- |      |                                     |               |
|------|-------------------------------------|---------------|
| 1).  | No Lecture                          |               |
| 2).  | Bravais Lattice, Reciprocal Lattice | Ashcroft: 4-7 |
| 3).  | XRD, Structural Factor              | Ashcroft: 4-7 |
| 4).  | Diffraction                         | West: 5       |
| 5).  | Descriptive crystal chemistry       | West: 7,8     |
| 6).  | Descriptive crystal chemistry       |               |
| 7).  | Crystal Chemistry, Phase diagrams   | West: 11, 12  |
| 8).  | Phase Diagram                       | Callister 9   |
| 9).  | Phase Diagram                       |               |
| 10). | Final                               |               |

## Materials Chemistry II

- |      |  |  |
|------|--|--|
| 11). | Free Electron Model  | Ashcroft/Mermin: 1-3, 8-10,<br>Kittel: 6-9 |
| 12). | Nearly free electron model, Fermi surface,<br>Effective Mass, Exciton. |  |
| 13). | Fermi's Golden Rule, Optical Transition                                |  |
| 14). | Quantum well/wire/dot  | Gersten, 7,11                              |
| 15). | Tight Binding Model<br>MO Theory                                       | Hoffmann, Burdett 1-3                      |
| 16). | Tight Binding Model  |  |
| 17). | Tight Binding Model  |  |
| 18). | Final  |  |

## Solid State and Materials Chemistry

**Synthesis, structure,  
properties, applications of solid materials**

*Inorganic, organic, biological*

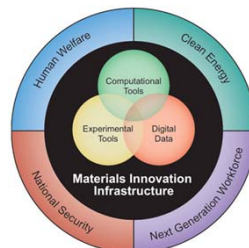
## Materials by Design

**Theoretician: predict structure/composition with  
particular properties**

**Chemist/Physicist: Make/measure/characterize**

**Materials Genome Initiative**

<http://www.whitehouse.gov/mgi>



## Characterization Techniques:

**Organic/Organometallic:** NMR, IR, crystallography

**Solid state:** X-ray powder diffraction,  
Electron microscopy  
Physical property characterization

## Superconductivity

1908, Kammerlingh-Onnes experiments on liquid He ( a few ml)

Hg resistance: 0.08 ohm @ 5K to 0.000003 ohm @ 4.2 K

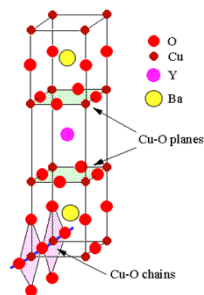
1986, J. G. Bednorz, K. H. Muller (IBM)

La-Ba-Cu-O

Oxide:  $T_c = 35$  K

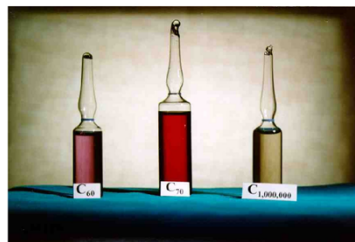
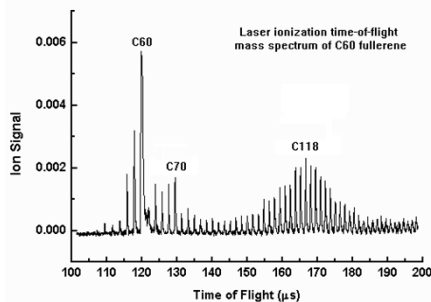
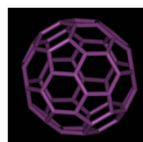
1997 Nobel prize in Physics

*French Group (B. Raveau)*



## Bucky Ball; fullerene 1996 Nobel prize in chemistry

*J.R. Heath, S.C. O'Brien, H.W. Kroto,  
R.F. Curl, R.E. Smalley,  
Nature 318, 162, (1985)*



*Models*, edited by H. H. Douglas (Plenum, New York and London, 1976), and by C. M. Varma and H. C. Dymns, *ibid.*  
\*We have chosen 0.5 eV somewhat arbitrarily to do-

fine fit. It is the energy near the  $F_{2g}$  scattering within which leads to over 90% of most of the anomalies.  
\*\*W. Kohn, *Phys. Rev. Lett.* **2**, 393 (1959); A. W. Overhauser, *Phys. Rev. Lett.* **2**, 415 (1959).

### Electrical Conductivity in Doped Polyacetylene

C. K. Chiang, C. R. Fincher, Jr., V. W. Park, and A. J. Heeger  
*Department of Physics and Laboratory for Research on the Structure of Matter, University of Pennsylvania, Philadelphia, Pennsylvania 19104*  
and  
H. Shirakawa,<sup>1,2</sup> E. J. Louis, S. C. Gau, and Alan G. MacDiarmid  
*Department of Chemistry and Laboratory for Research on the Structure of Matter, University of Pennsylvania, Philadelphia, Pennsylvania 19104*  
(Received 22 June 1977)

Doped polyacetylene forms a new class of conducting polymers in which the electrical conductivity can be systematically and continuously varied over a range of eleven orders of magnitude. Transport studies and far-infrared transmission measurements imply a metal-to-insulator transition at dopant concentrations near 5%.

We find that films of the semiconducting polymer, polyacetylene, show a dramatic increase in electrical conductivity when doped with controlled amounts of the halogens chlorine, bromine, or iodine, and with arsenic pentafluoride (AsF<sub>5</sub>). The concentration dependence in combination with far-infrared transmission data suggests the occurrence of a metal-insulator transition as a function of dopant concentration.

Polyacetylene is one of the simplest linear conjugated polymers with a single-chain structure as shown in Fig. 1. Each carbon is  $\sigma$  bonded to one hydrogen and two neighboring carbon atoms consistent with  $sp^2$  hybridization. The  $\pi$  electrons are therefore available to delocalize into a band. In the idealized situation of a uniform chain, the resulting conduction band would give rise to metallic behavior. However, such a system is unstable with respect to bond alternation, which causes the formation of an energy gap in the electronic spectrum. Studies of  $\pi-\pi^*$  transitions in short-chain polyenes show that the frequencies do not fall as  $n^{-2}$  as expected for a free-electron picture, but appear to saturate at  $\Delta E_{\pi-\pi^*} \approx 2.4$  eV.<sup>1</sup> Bond alternation is present in the polymer and would be expected to lead to semiconducting behavior. However, Ovchinnikov<sup>2</sup> has stimulated the bond-alternation energy gap to be too small and attributed the observed value to Coulomb correlation effects, i.e., a Hubbard gap. In a series of studies Shirakawa and co-workers<sup>3-5</sup> succeeded in synthesizing high-quality

polycrystalline films of (CH)<sub>x</sub>, and developed techniques for controlling the *cis/trans* content.<sup>6,7</sup> These materials are semiconductors<sup>8</sup>; the *trans* isomer is the thermodynamically stable form at room temperature.

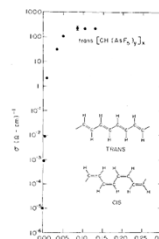


FIG. 1. Electrical conductivity of *trans*-(CH)<sub>x</sub> as a function of (AsF<sub>5</sub>) dopant concentration. The *trans* and *cis* polymer structures are shown in the inset.

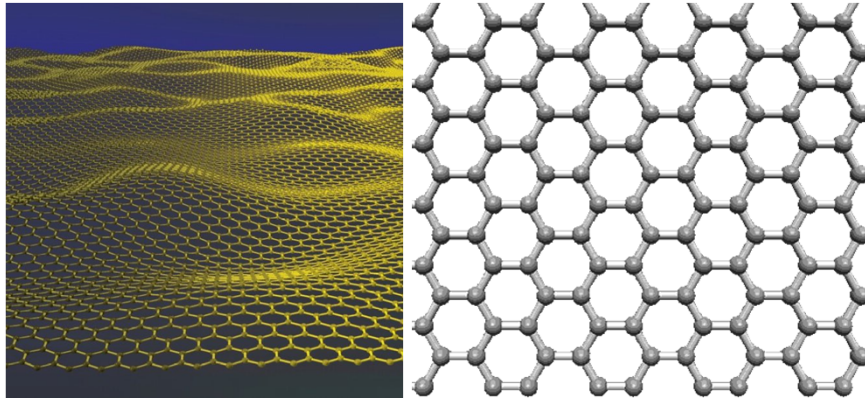
## Conducting Polymer

[2000 Alan Heeger,](#)  
[Alan G. MacDiarmid,](#)  
[Hideki Shirakawa](#)

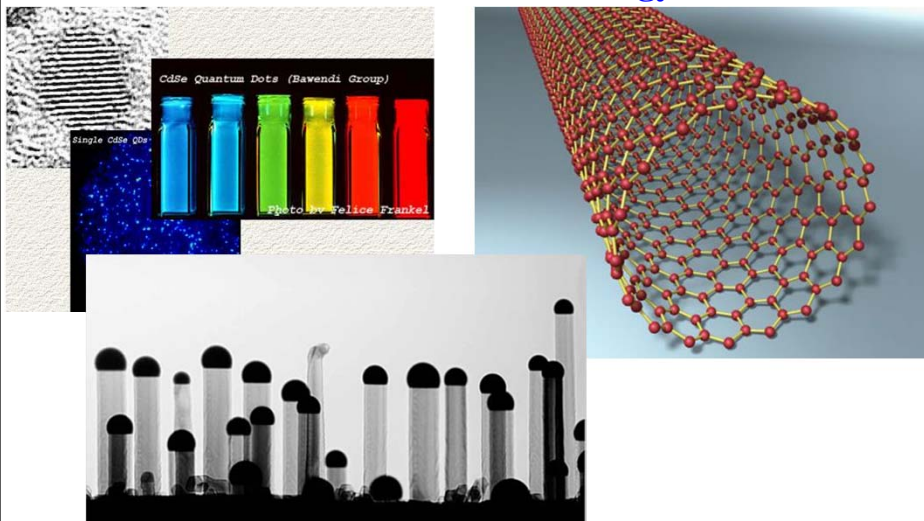
Nobel Prize in Chemistry

# Graphene

The Nobel Prize in Physics 2010  
Andre Geim, Konstantin Novoselov



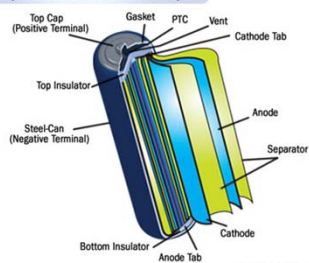
**Materials Chemistry is the foundation for the  
field of  
Nanoscience and technology.**



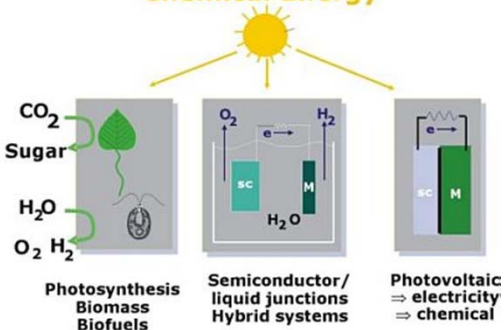
## Energy Research



Cylindrical lithium-ion battery

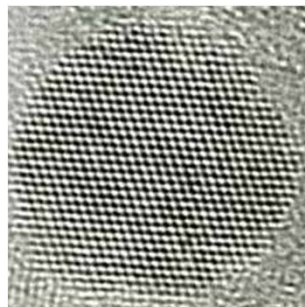
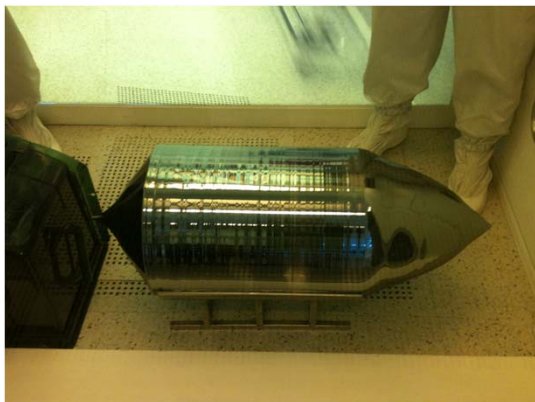


### Solar to Electrical and Chemical Energy



## Crystal Structure

*Reading: Ashcroft 4-7*





## Crystal Structure

Reading: Ashcroft 4-7

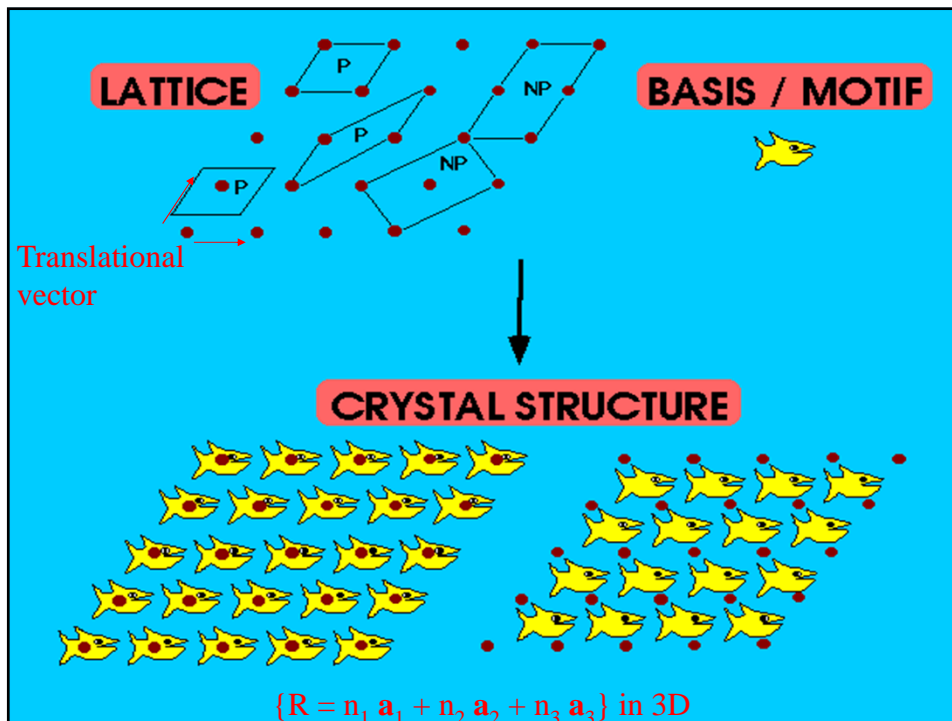
**Ideal Crystal:** Contain periodical array of atoms/ions  
Represented by a simple lattice of points  
A group of atoms attached to each lattice points

*Basis*

**LATTICE** = An infinite array of points in space, in which each point has identical surroundings to all others.

**CRYSTAL STRUCTURE** = The periodic arrangement of atoms in the crystal.

It can be described by associating with each lattice point a group of atoms called the **MOTIF (BASIS)**



**LATTICE**      **BASIS / MOTIF**

**CRYSTAL STRUCTURE**

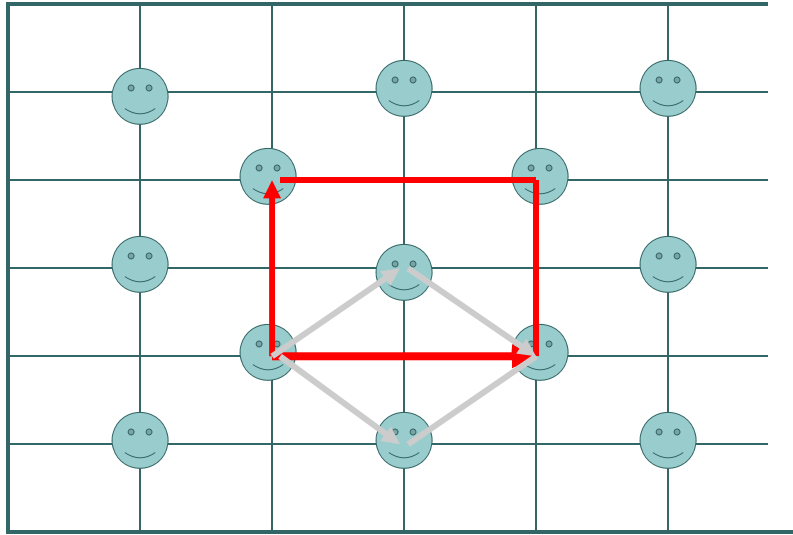
**UNIT CELL** = *The smallest component of the crystal, which when stacked together with pure translational repetition reproduces the whole crystal*

**Primitive Cell:** *simplest cell, contain one lattice point*  
*Not necessary have the crystal symmetry*

Chem 253, UC, Berkeley ● ● ●

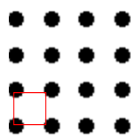
White and black birds  
by the artist, M. C. Escher

## Unit Cells?



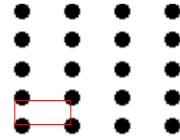
**Conventional cell** vs. Primitive Cell  
*Reflecting the symmetry*  
*Different Basis*

**Bravais Lattice:** an infinite array of discrete points with an arrangement and orientation that appears exactly the same from whichever of the points the array is viewed.



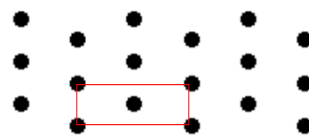
Square

**P**



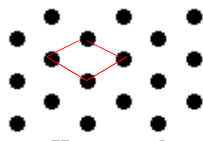
Rectangular

**P**

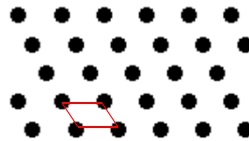


Centered Rectangular

**NP**



Hexagonal

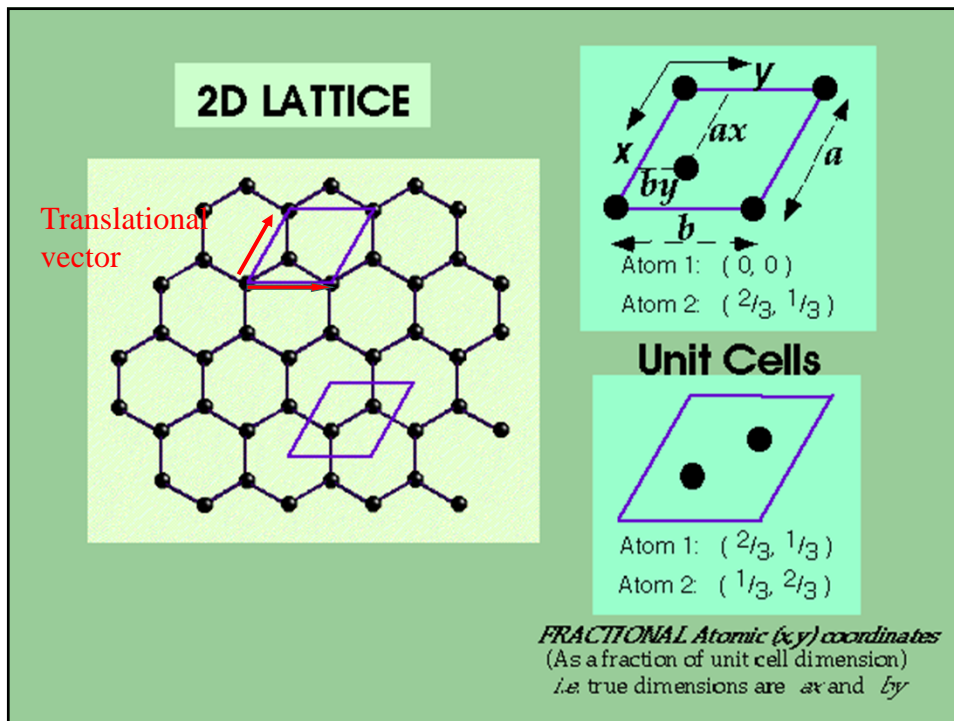


Oblique

## 5 Bravais Lattice in 2D

|                      |            |                  |
|----------------------|------------|------------------|
| Square               | $a=b$      | $\gamma = 90$    |
| Rectangular          | $a \neq b$ | $\gamma = 90$    |
| Centered Rectangular | $a \neq b$ | $\gamma = 90$    |
| Hexagonal            | $a=b$      | $\gamma = 120$   |
| Oblique              | $a \neq b$ | $\gamma \neq 90$ |

## 5 Bravais Lattice in 2D



## 3D: 14 Bravais Lattice, 7 Crystal System

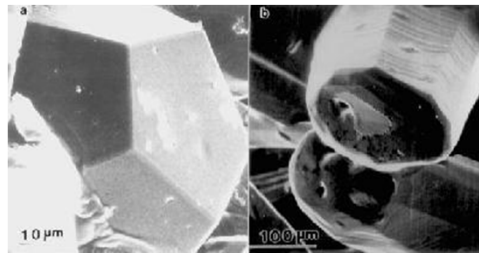
| Name         | Number of Bravais lattices | Conditions  |
|--------------|----------------------------|---|
| Triclinic    | 1 (P)                      | $a_1 \neq a_2 \neq a_3$<br>$\alpha \neq \beta \neq \gamma$                  |
| Monoclinic   | 2 (P, C)                   | $a_1 \neq a_2 \neq a_3$<br>$\alpha = \beta = 90^\circ \neq \gamma$          |
| Orthorhombic | 4 (P, F, I, A)             | $a_1 \neq a_2 \neq a_3$<br>$\alpha = \beta = \gamma = 90^\circ$             |
| Tetragonal   | 2 (P, I)                   | $a_1 = a_2 \neq a_3$<br>$\alpha = \beta = \gamma = 90^\circ$                |
| Cubic        | 3 (P, F, I)                | $a_1 = a_2 = a_3$<br>$\alpha = \beta = \gamma = 90^\circ$                   |
| Trigonal     | 1 (P)                      | $a_1 = a_2 = a_3$<br>$\alpha = \beta = \gamma < 120^\circ \neq 90^\circ$    |
| Hexagonal    | 1 (P)                      | $a_1 = a_2 \neq a_3$<br>$\alpha = \beta = 90^\circ$<br>$\gamma = 120^\circ$ |

Allowed rotation axis:

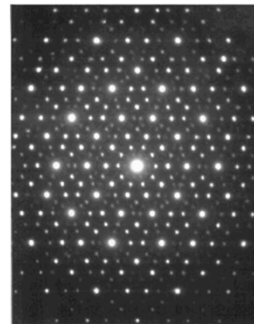
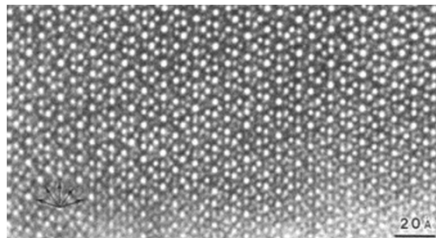
1, 2, 3, 4, 6

NOT 5, > 6

Quasicrystal: *AlFeCu*

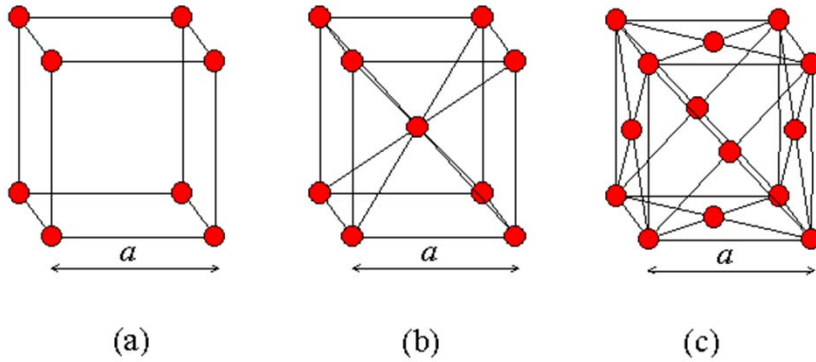


Shechtman, D., Blech, I., Gratias, D. & Cahn, J. W.  
*Phys. Rev. Lett.* **53**, 1951-1953 (1984).

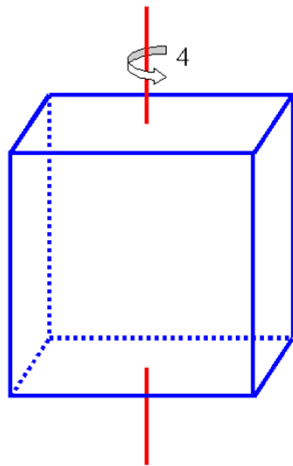


The Nobel Prize in Chemistry 2011  
Dan Shechtman

**Cubic: four 3-fold + three 4-fold**

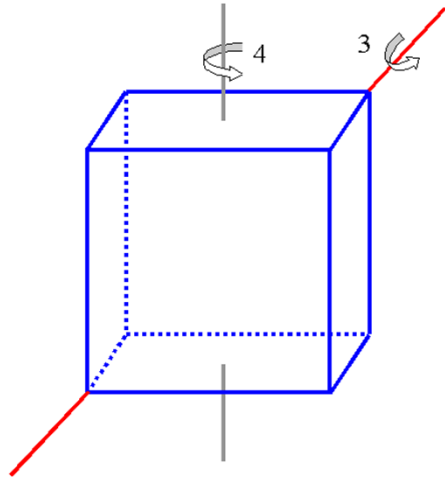


### Unit cell symmetries - cubic



- **4 fold rotation axes**  
(passing through pairs of opposite face centers, parallel to cell axes)
- TOTAL = 3**

## Unit cell symmetries - cubic



- 4 fold rotation axes  
TOTAL = 3
- **3-fold rotation axes**  
(passing through cube  
body diagonals)  
TOTAL = 4

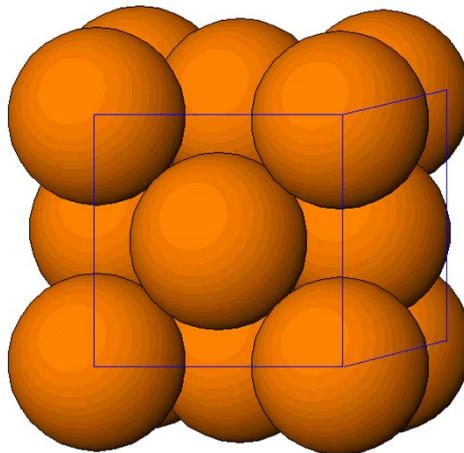
## FCC Lattice

Copper metal is  
**face-centered  
cubic**

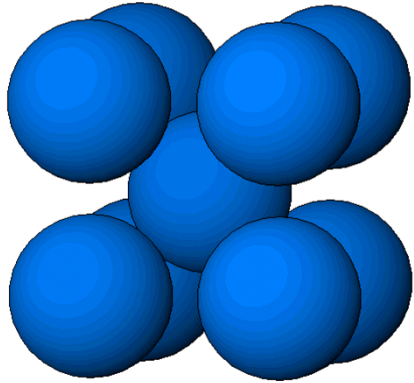
Identical atoms at  
corners and at face  
centers

**Lattice type F**

also Ag, Au, Al, Ni...



## BCC Lattice



$\alpha$ -Iron is **body-centered cubic**

Identical atoms at corners and body center (nothing at face centers)

**Lattice type I**

Also Nb, Ta, Ba, Mo...

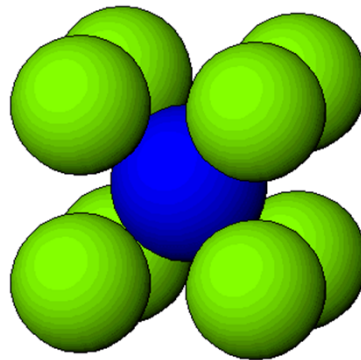
## Simple Cubic Lattice

Caesium Chloride (CsCl) is **primitive cubic**

Different atoms at corners and body center. **NOT** body centered, therefore.

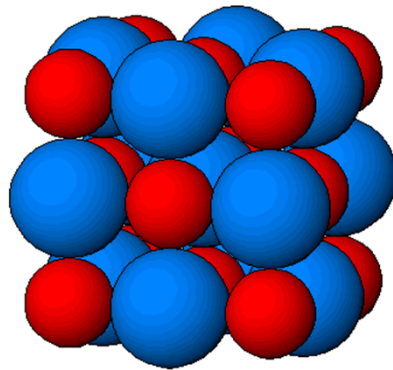
**Lattice type P**

Also CuZn, CsBr, LiAg





# FCC Lattices



Sodium Chloride (NaCl) -  
Na is much smaller than  
Cs

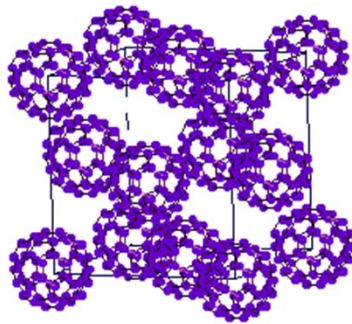
Face Centered Cubic

Rocksalt structure

**Lattice type F**

Also NaF, KBr, MgO....

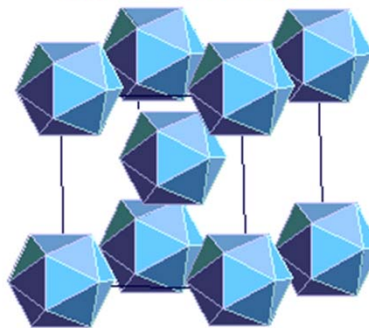
## BUCKMINSTERFULLERENE



**FCC**

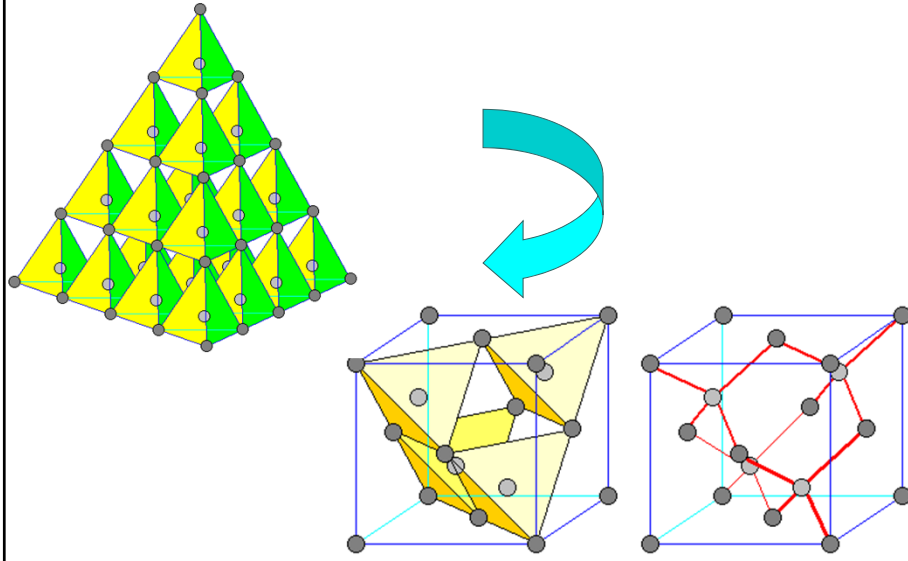
*Nature* 353, 147 - 149 (12 Sep 1991)

## FOOT & MOUTH VIRUS

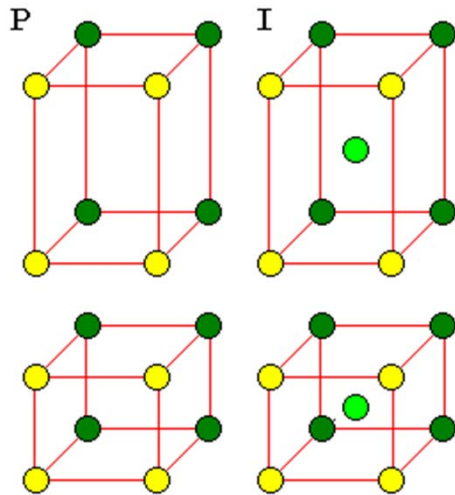


**BCC**

### Diamond Structure: two sets of FCC Lattices



### Tetragonal: P, I

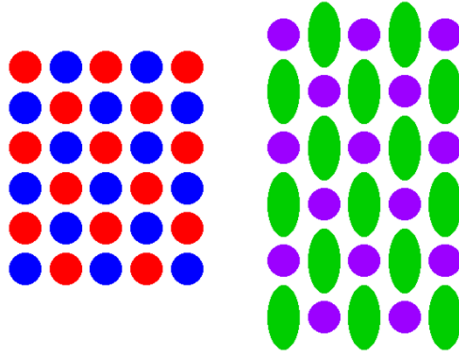
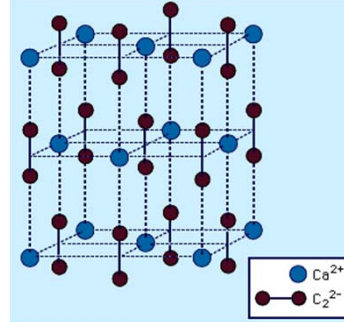


One 4-fold axes

Why not F tetragonal?

## Example

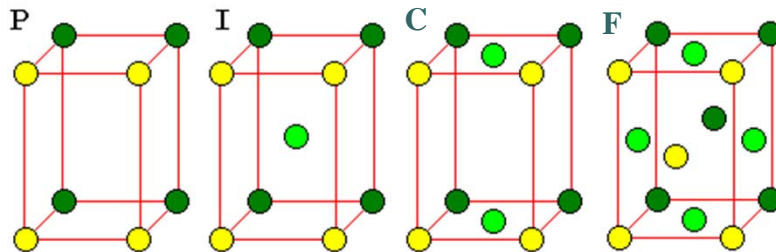
$\text{CaC}_2$  - has a rocksalt-like structure  
but with non-spherical carbides



Carbide ions are  
aligned parallel to **c**

$\therefore c > a, b \rightarrow$   
tetragonal symmetry

## Orthorhombic: P, I, F, C



## Another type of centering

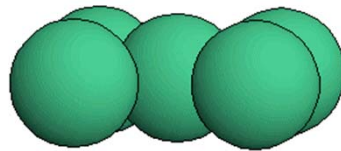
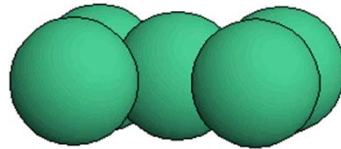
Side centered unit cell

Notation:

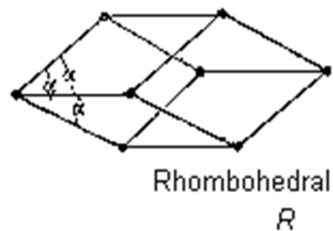
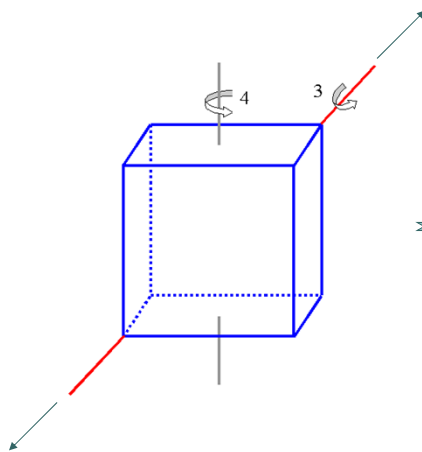
**A**-centered if atom in bc plane

**B**-centered if atom in ac plane

**C**-centered if atom in ab plane

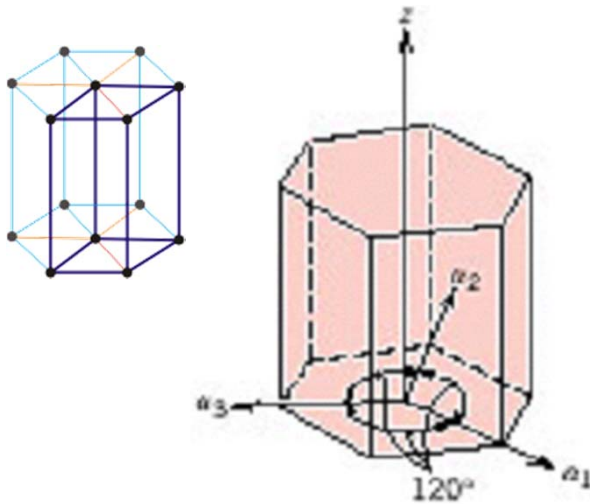


## Trigonal: P : 3-fold rotation



Rhombohedral  
R

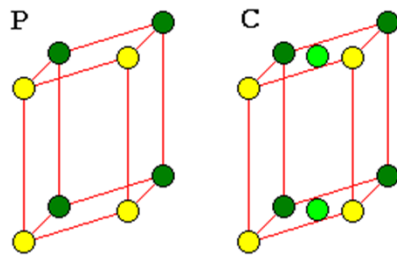
$$a_1 = a_2 = a_3$$
$$\alpha = \beta = \gamma < 120^\circ \neq 90^\circ$$



## Hexagonal

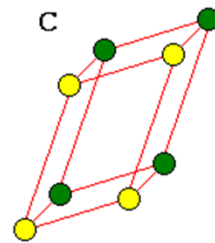
$$\begin{aligned} a_1 &= a_2 \neq a_3 \\ \alpha &= \beta = 90^\circ \\ \gamma &= 120^\circ \end{aligned}$$

## Monoclinic

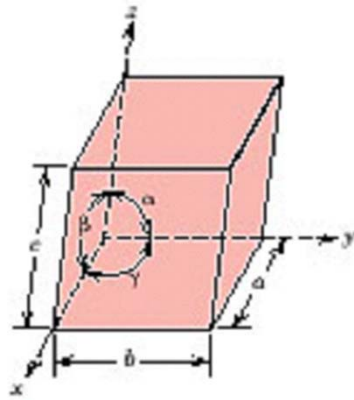


$$\begin{aligned} a_1 &\neq a_2 \neq a_3 \\ \alpha &= \beta = 90^\circ \neq \gamma \end{aligned}$$

## Triclinic



$$\begin{aligned} a_1 &\neq a_2 \neq a_3 \\ \alpha &\neq \beta \neq \gamma \end{aligned}$$

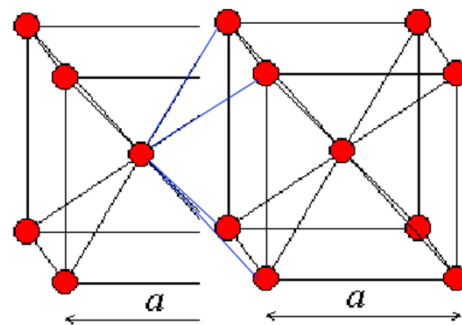


Lattice parameters:  
 $a, b, c; \alpha, \beta, \gamma$

## 7 Crystal Systems

Table 3.2 Lattice Parameter Relationships and Figures Showing Unit Cell Geometries for the Seven Crystal Systems

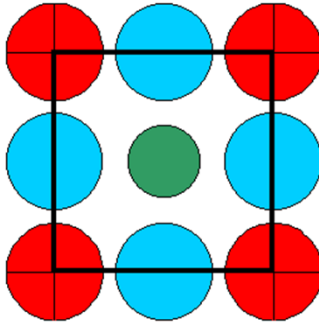
| Crystal System | Axial Relationships | Interaxial Angles                               | Unit Cell Geometry |
|----------------|---------------------|---|--------------------|
| Cubic          | $a = b = c$         | $\alpha = \beta = \gamma = 90^\circ$            |                    |
| Hexagonal      | $a = b \neq c$      | $\alpha = \beta = 90^\circ, \gamma = 120^\circ$ |                    |
| Tetragonal     | $a = b \neq c$      | $\alpha = \beta = \gamma = 90^\circ$            |                    |
| Rhombohedral   | $a = b = c$         | $\alpha = \beta = \gamma \neq 90^\circ$         |                    |
| Orthorhombic   | $a \neq b \neq c$   | $\alpha = \beta = \gamma = 90^\circ$            |                    |
| Monoclinic     | $a \neq b \neq c$   | $\alpha = \gamma = 90^\circ \neq \beta$         |                    |
| Triclinic      | $a \neq b \neq c$   | $\alpha \neq \beta \neq \gamma \neq 90^\circ$   |                    |



The choice of unit cell: reflect the crystal symmetry

## Unit cell contents

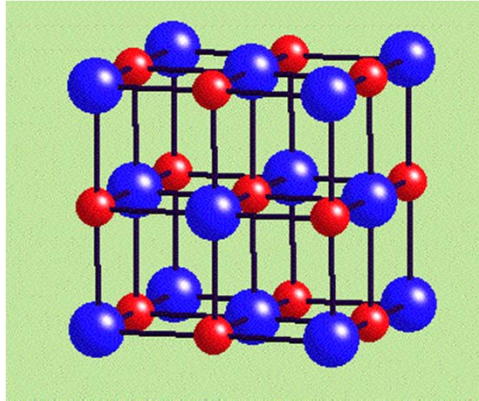
Counting the number of atoms within the unit cell



Many atoms are shared between unit cells

| Atoms       | Shared Between: | Each atom counts: |
|-------------|-----------------|-------------------|
| corner      | 8 cells         | 1/8               |
| face center | 2 cells         | 1/2               |
| body center | 1 cell          | 1                 |
| edge center | 4 cells         | 1/4               |

| lattice type | cell contents               |
|--------------|-----------------------------|
| P            | 1 [=8 x 1/8]                |
| I            | 2 [= (8 x 1/8) + (1 x 1)]   |
| F            | 4 [= (8 x 1/8) + (6 x 1/2)] |
| C            | 2 [= (8 x 1/8) + (2 x 1/2)] |



e.g. NaCl

Na at corners:  $(8 \times 1/8) = 1$

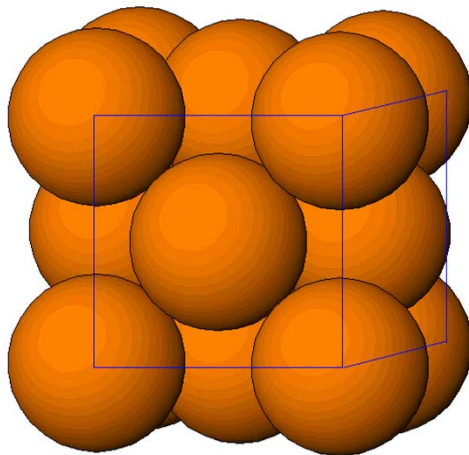
Na at face centres  $(6 \times 1/2) = 3$

Cl at edge centres  $(12 \times 1/4) = 3$

Cl at body centre = 1

Unit cell contents are  $4(\text{Na}^+\text{Cl}^-)$

## Fractional Coordinates



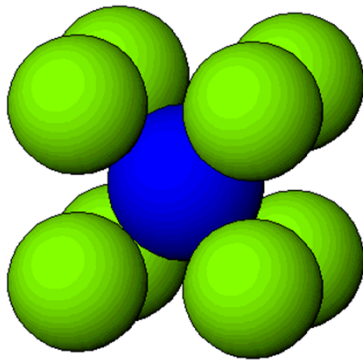
$(0,0,0)$

$(0, 1/2, 1/2)$

$(1/2, 1/2, 0)$

$(1/2, 0, 1/2)$





Cs (0,0,0)  
Cl (1/2, 1/2, 1/2)

## Density Calculation

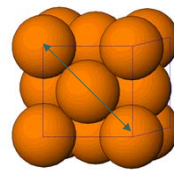
$$\rho = \frac{nA}{V_C N_A}$$

$n$ : number of atoms/unit cell

$A$ : atomic mass

$V_C$ : volume of the unit cell

$N_A$ : Avogadro's number  
( $6.023 \times 10^{23}$  atoms/mole)



Calculate the density of copper.

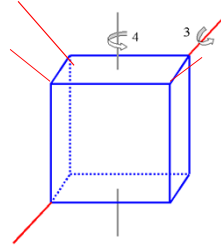
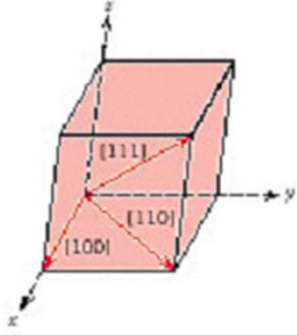
$R_{Cu} = 0.128 \text{ nm}$ , Crystal structure: FCC,  $A_{Cu} = 63.5 \text{ g/mole}$

$n = 4 \text{ atoms/cell}$ ,  $V_C = a^3 = (2R\sqrt{2})^3 = 16\sqrt{2}R^3$

$$\rho = \frac{(4)(63.5)}{[16\sqrt{2}(1.28 \times 10^8)^3 \times 6.023 \times 10^{23}]} = 8.89 \text{ g/cm}^3$$

*8.94 g/cm<sup>3</sup> in the literature*

## Crystallographic Directions And Planes



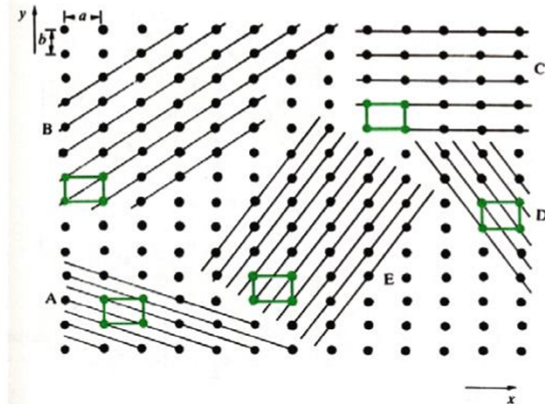
### Lattice Directions

*Individual directions:  $[uvw]$*

*Symmetry-related directions:  $\langle uvw \rangle$*

## Lattice planes

- ◆ It is possible to describe certain directions and planes with respect to the crystal lattice using a set of three integers referred to as Miller Indices



## Crystallographic Directions And Planes

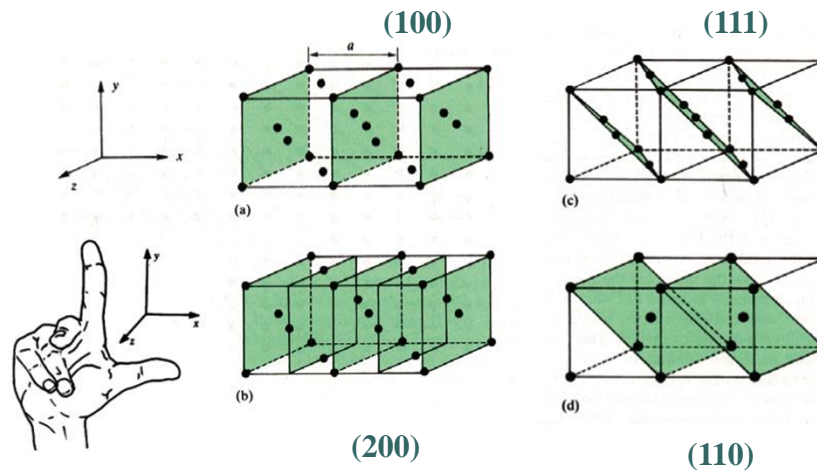
### Miller Indices:

1. Find the intercepts on the axes in terms of the lattice constant  $a, b, c$
2. Take the reciprocals of these numbers, reduce to the three integers having the same ratio

**(hkl)**

**Set of symmetry-related planes: {hkl}**

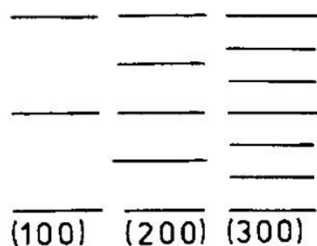
## Examples of Miller indices



# Families of planes

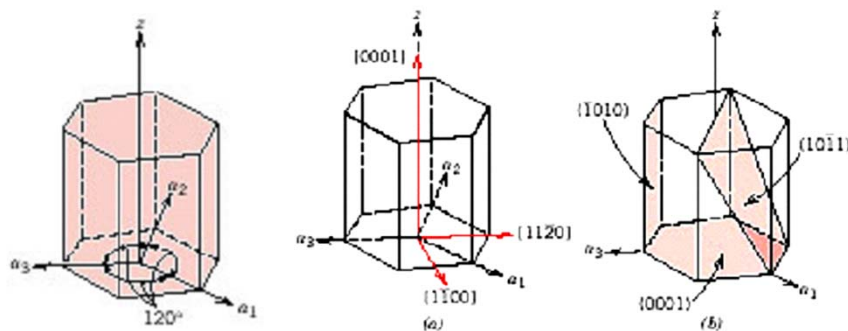
- ◆ Miller indices describe the orientation and spacing of a family of planes
  - The spacing between adjacent planes in a family is referred to as a “d-spacing”

Three different families of planes  
 d-spacing between (300) planes is one third of the (100) spacing



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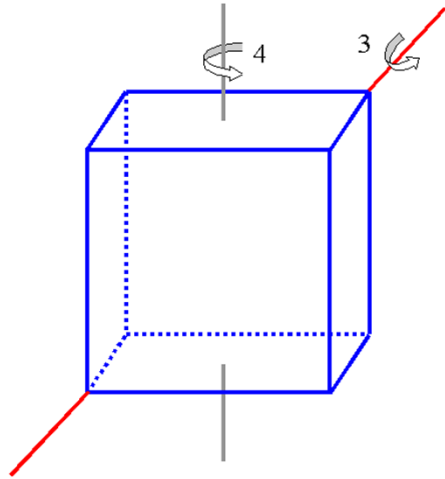
## Crystallographic Directions And Planes



*Miller-Bravais indices*

$[uvtw], (hkil)$

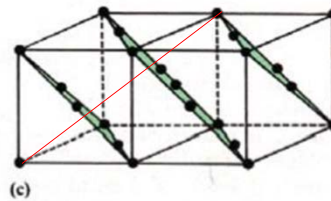
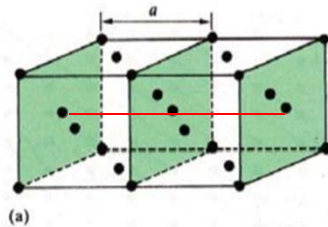
$t = -(u+v)$      $i = -(h+k)$



In cubic system,  
[hkl] direction  
perpendicular to (hkl) plane

## Lattice spacing

$$\frac{1}{d_{hkl}^2} = \frac{h^2 + k^2 + l^2}{a^2} \quad \text{For cubic system}$$



## d-spacing formulae

---

- For a unit cell with orthogonal axes
  - $(1 / d_{hkl}^2) = (h^2/a^2) + (k^2/b^2) + (l^2/c^2)$
- Hexagonal unit cells
  - $(1 / d_{hkl}^2) = (4/3)([h^2 + k^2 + hk] / a^2) + (l^2/c^2)$

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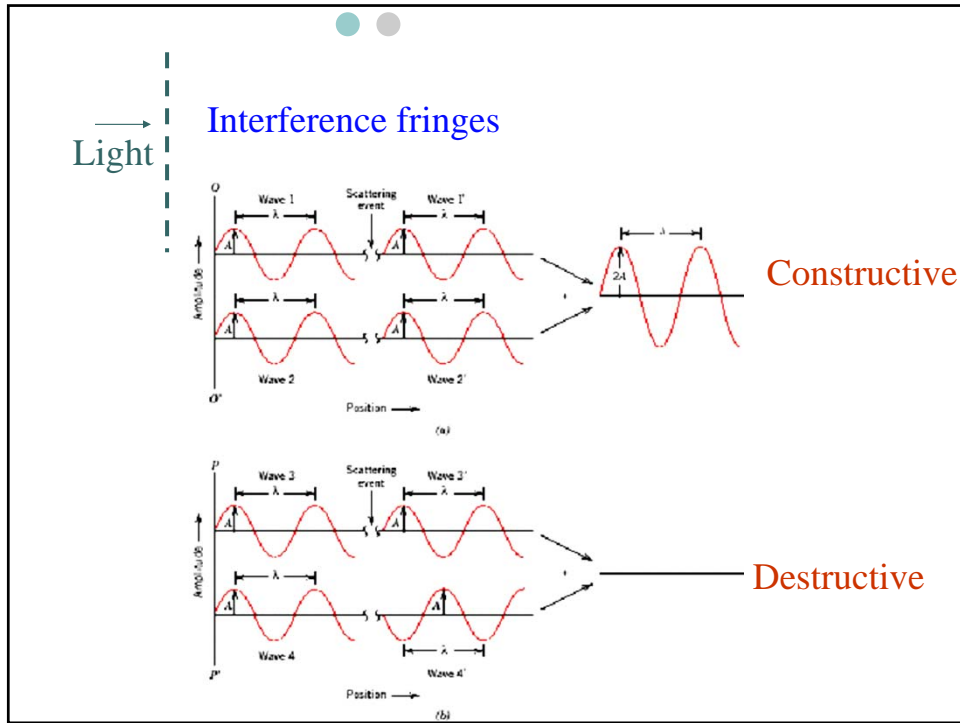
### **Crystal Structure Analysis**

**X-ray diffraction**

**Electron Diffraction**

**Neutron Diffraction**

**Essence of diffraction: Bragg Diffraction**



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## Bragg's Law

$$\begin{aligned}
 n\lambda &= \overline{SQ} + \overline{QT} \\
 &= d_{hkl} \sin \theta + d_{hkl} \sin \theta \\
 &= 2d_{hkl} \sin \theta
 \end{aligned}$$

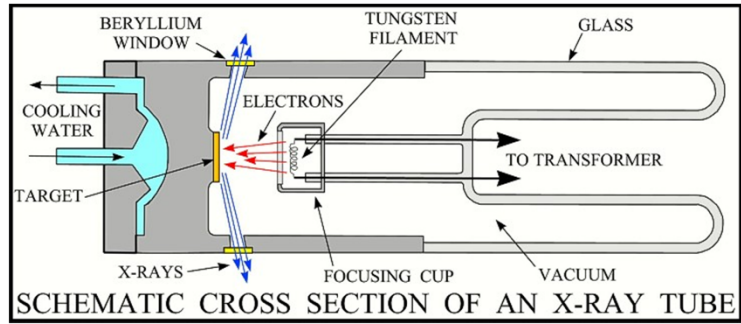
For cubic system:

$$d_{hkl} = \frac{a}{\sqrt{h^2 + k^2 + l^2}}$$

*But not all planes have the diffraction !!!*

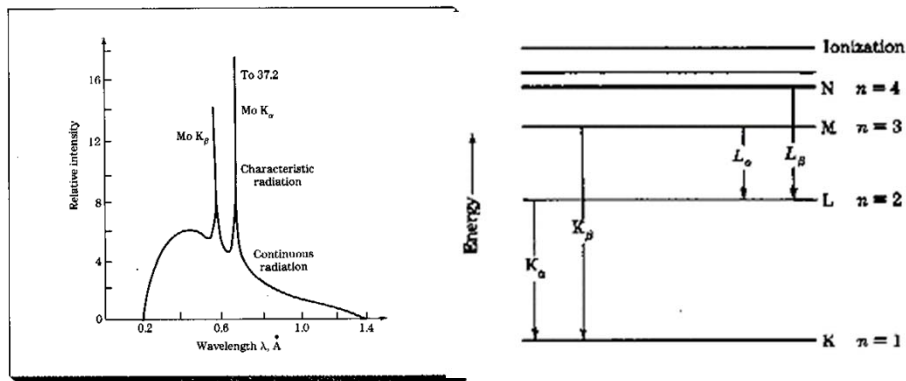
# X-Ray Diffraction

$$E = h\nu = hc / \lambda$$



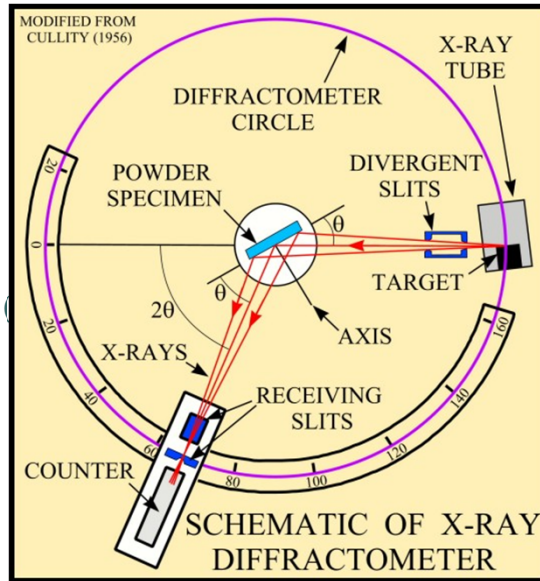
Mo: 35KeV ~ 0.1-1.4Å<sup>o</sup>  
Cu K 1.54 Å

# X-Ray Diffraction

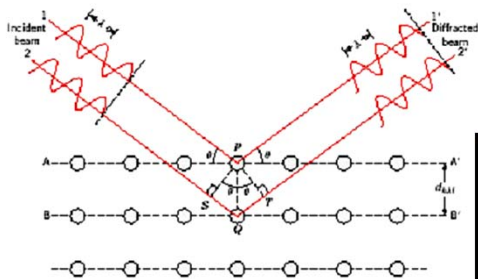




### Powder diffraction



### Powder diffraction



**BRAGG LAW**

$$2d(\sin\theta) = \lambda_0$$

where:  
 d = lattice interplanar spacing of the crystal  
 θ = x-ray incidence angle (Bragg angle)  
 λ = wavelength of the characteristic x-rays

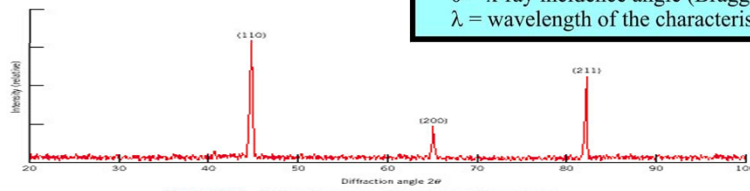
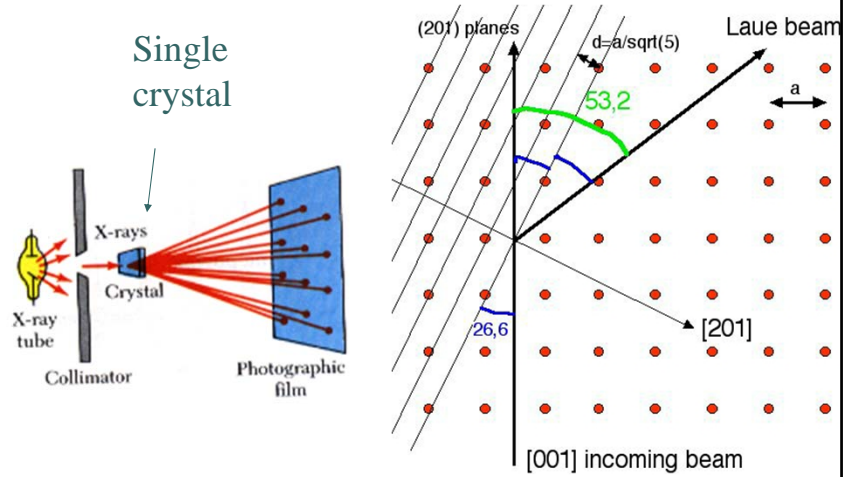
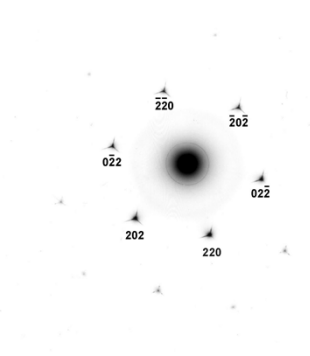
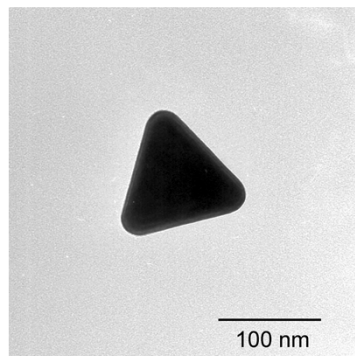


FIGURE 3.20 Diffraction pattern for polycrystalline α-iron.

## Laue Diffraction



## Electron Diffraction

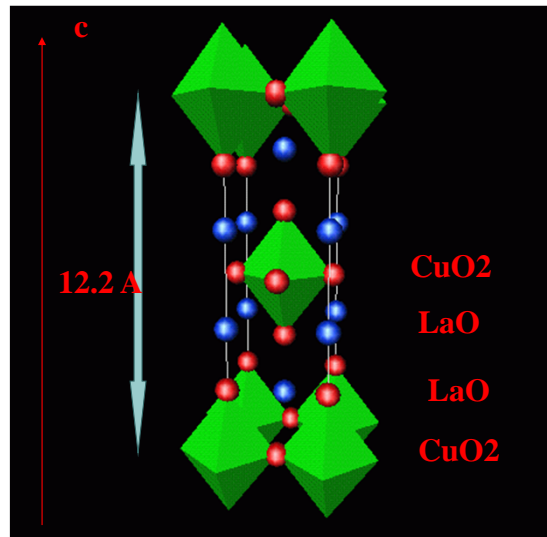
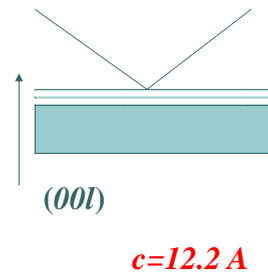


**Layered Cuprates**  
*Thin film, growth oriented  
 along c axis*

**Example:  $\text{La}_2\text{CuO}_2$**

$$2d \sin \theta = n\lambda$$

| 2*theta | d    | (hkl) |
|---------|------|-------|
| 7.2     | 12.1 | (001) |
| 14.4    | 6.1  | (002) |
| 22      | 4.0  | (003) |



Example:  $\text{Ca}_{0.5}\text{Sr}_{0.5}\text{CuO}_2$

Layered Cuprates  
Thin film, growth oriented  
along c axis

$$2d \sin \theta = n\lambda$$

| 2*theta | d    | (hkl) |
|---------|------|-------|
| 12.7    | 6.96 | (001) |
| 26      | 3.42 | (002) |
| 42.2    | 2.15 | (003) |

