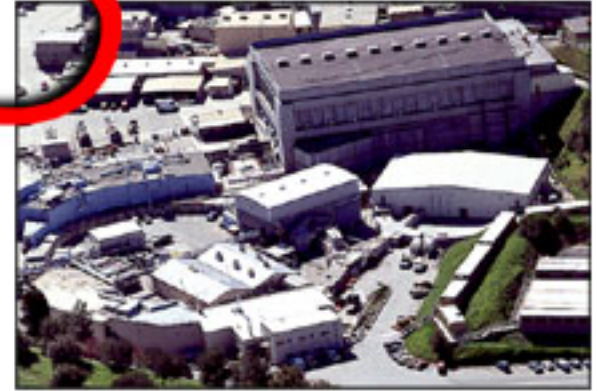


STANFORD SYNCHROTRON RADIATION LABORATORY



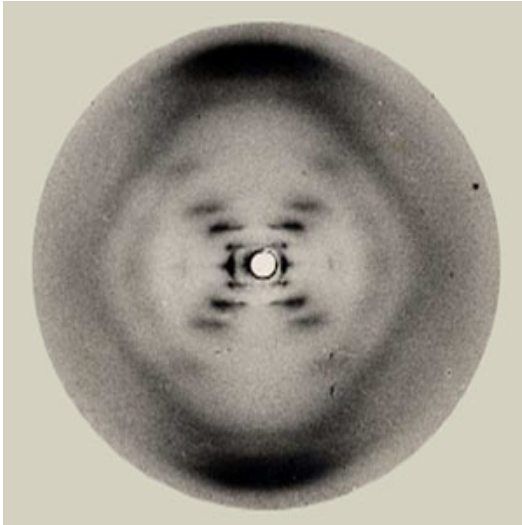
*Everything You Ever Wanted to Know About  
SAXS But Were Afraid to Ask*

**John A Pople**

*Stanford Synchrotron Radiation Laboratory,  
Stanford Linear Accelerator Center, Stanford CA 94309*

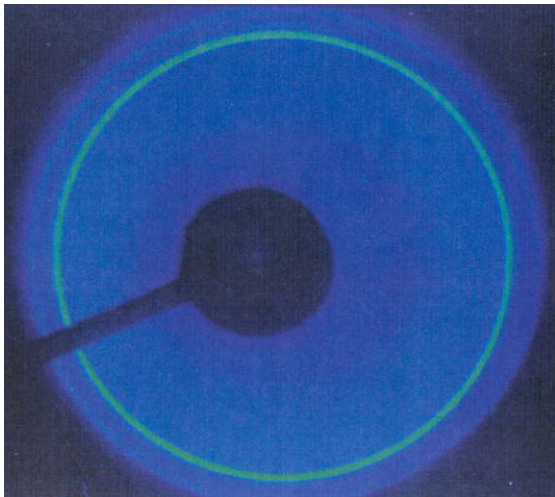
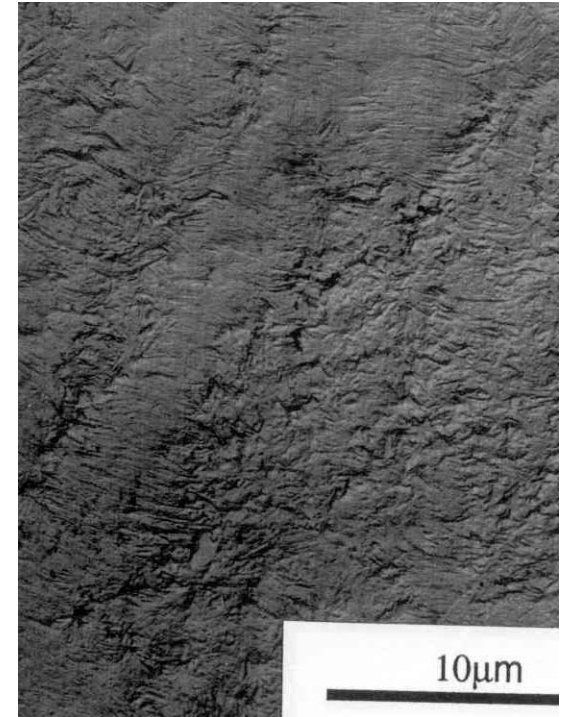
When should I use the  
Scattering Technique?

## Ideal Studies for Scattering

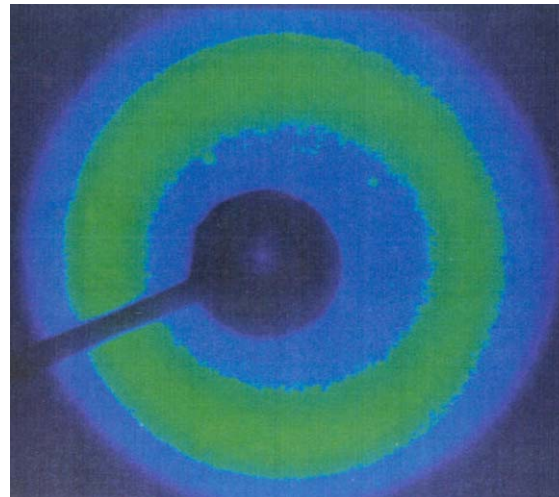


### Scattering good for:

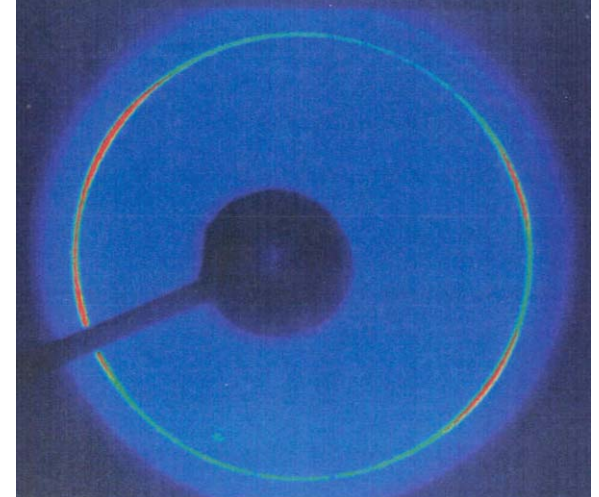
- Global parameters, distributions; 1<sup>st</sup> order
- Different sample states
- In-situ transitional studies
- Non destructive sample preparation



Solid

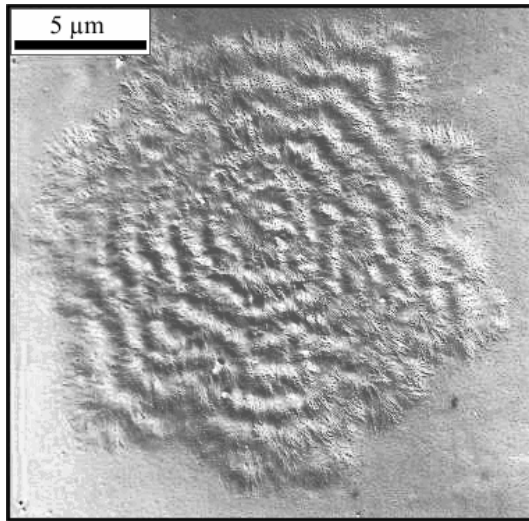


Melted & Sheared



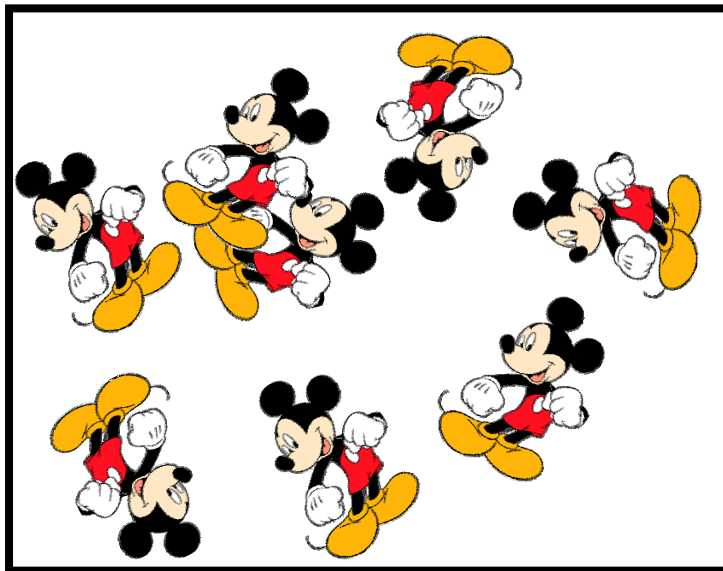
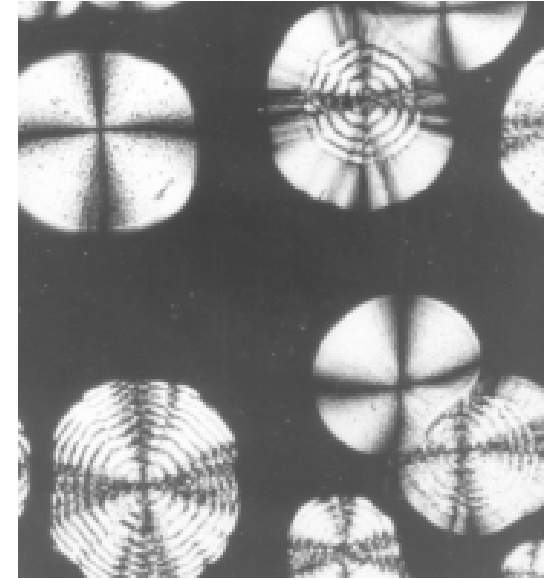
Recrystallized

# *Ideal Studies for Microscopy*



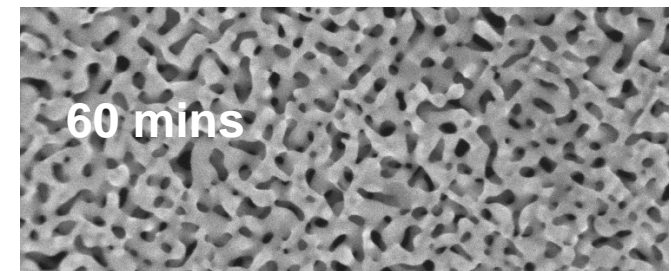
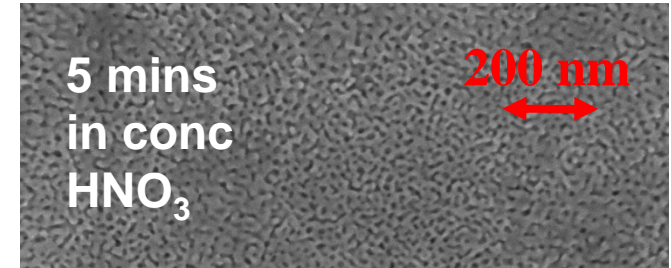
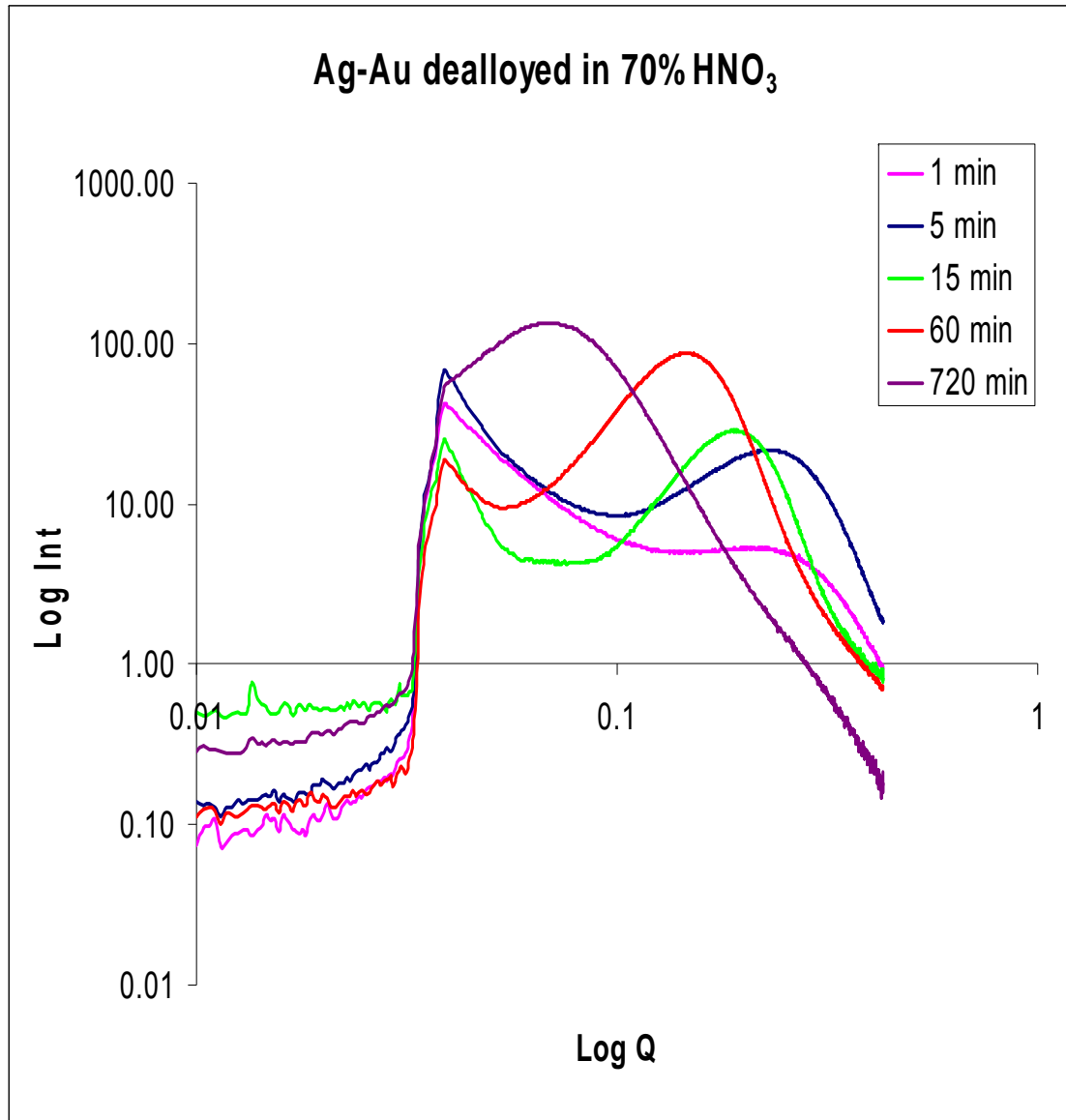
## *Microscopy good for:*

- Local detail
- Surface detail
- Faithfully represents local complexities



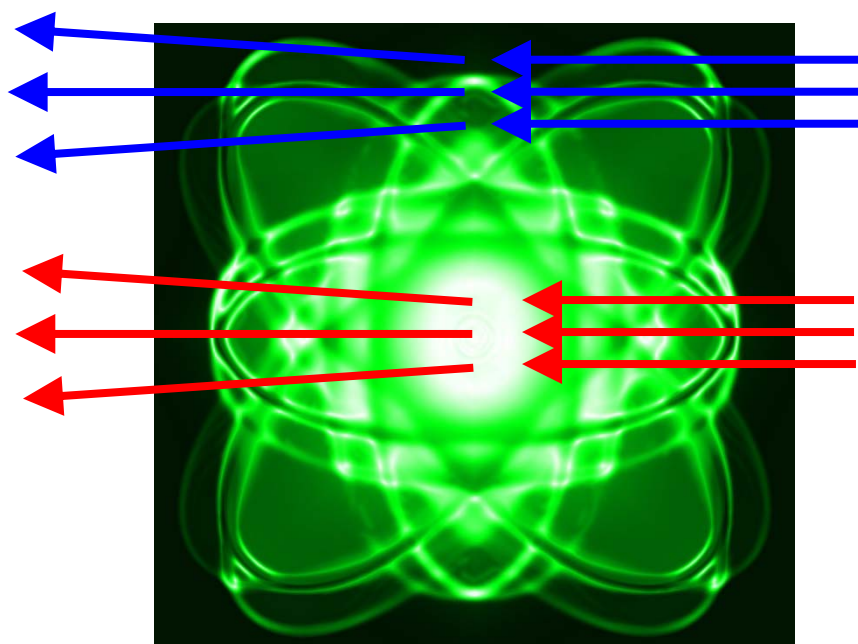
E.g. if objective is to monitor the degree to which Mickey's nose(s) and ears hold to a circular micromorphology... use microscopy not scattering

# Complementary Scattering and Microscopy



Forming a bi-continuous porous network with ligament width on the nanoscale by removing the less noble element from a binary alloy, in this case Ag-Au

## Scattering: Neutrons or Photons?



X-rays

Sensitive to electron density contrast

Neutrons

Sensitive to nuclear scattering length contrast

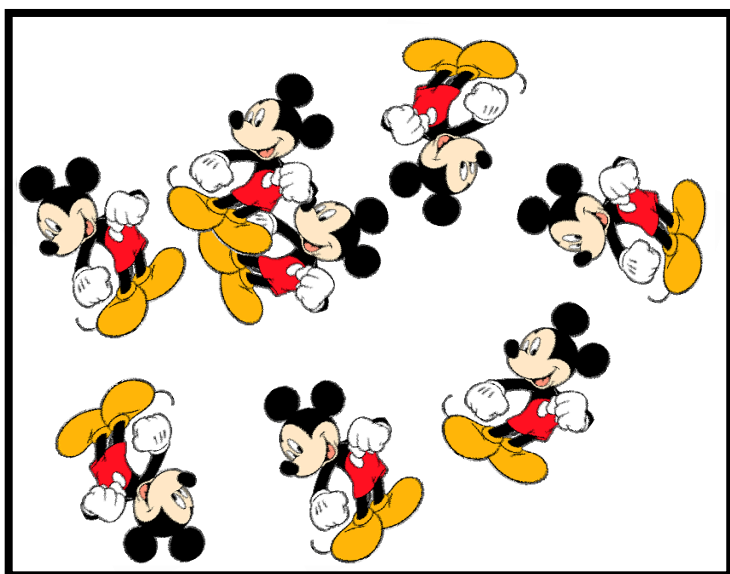
Neutron scattering: Deuteration allows species selection

Advantages of X-ray scattering:

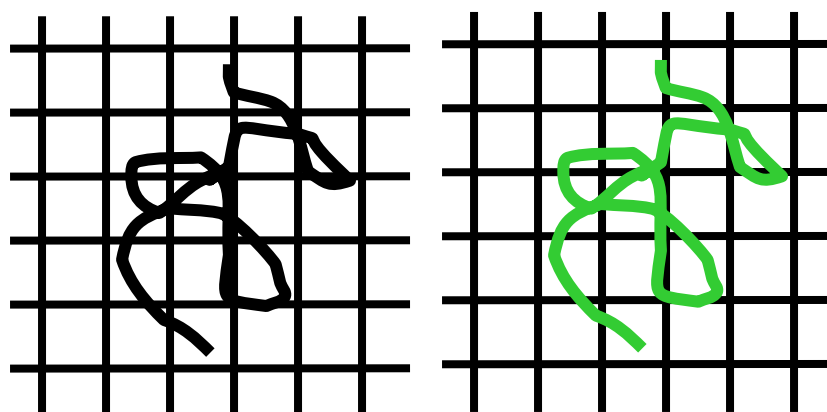
- Relatively small sample quantities required
- Relatively fast data acquisition times - allows time resolved effects to be characterized

# Scattering: Neutrons or Photons?

Neutrons: Deuteration allows species selection

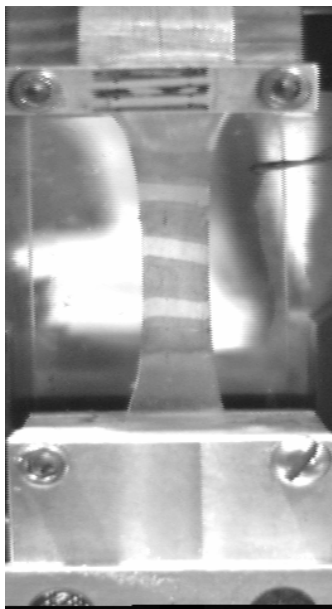
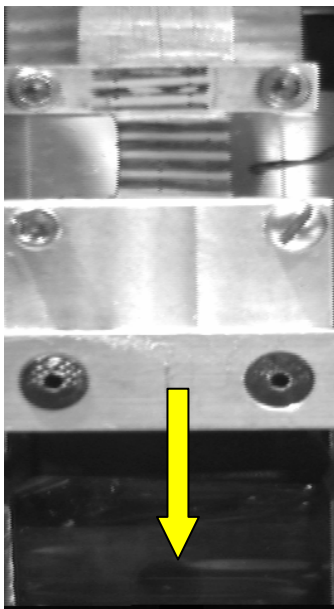


This essentially permits a dramatic alteration to the 'visibility' of the tagged elements in terms of their contribution to the reciprocal space scattering pattern

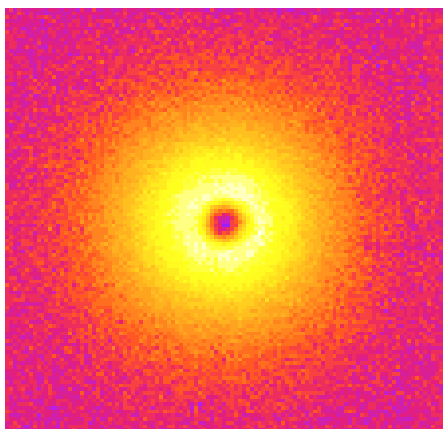


Atom	Scattering length ( $\times 10^{12}$ cm <sup>2</sup> )	Incoherent scattering ( $\times 10^{24}$ cm <sup>2</sup> )
■ <sup>1</sup> H	-0.374	80
■ <sup>2</sup> D	0.667	2

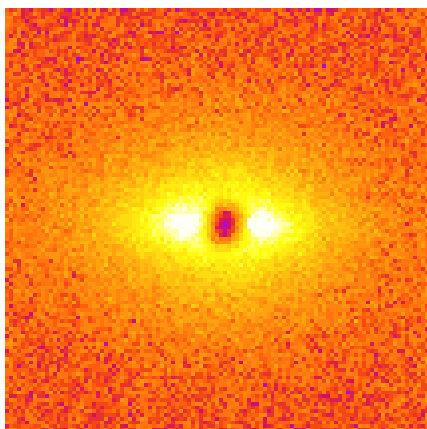
## Scattering: Neutrons or Photons?



Photos of deformation



$\lambda = 0\%$



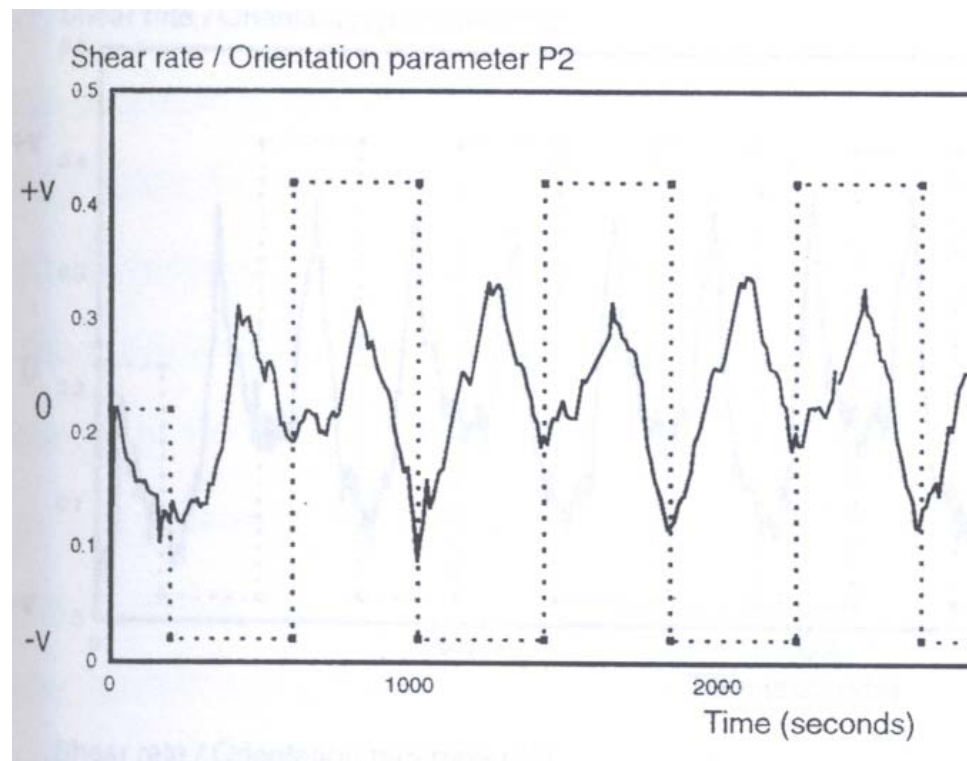
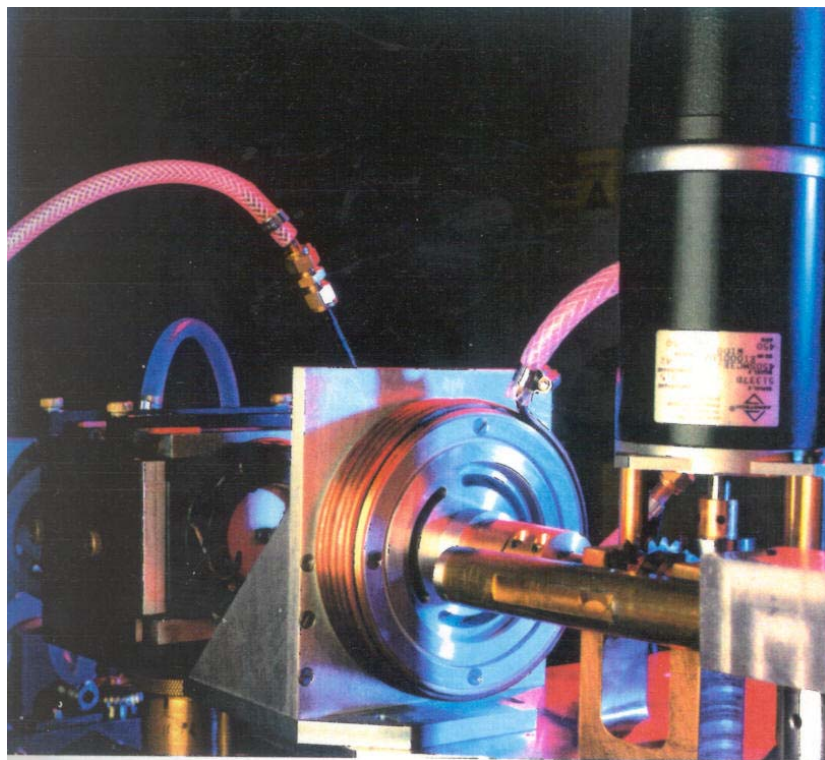
$\lambda = 300\%$

SANS patterns



## Scattering: Neutrons or Photons?

X-rays:           Order of magnitude better spatial resolution  
Fast data acquisition times for time resolved data



Oscillatory Shearing of lyotropic HPC – a liquid crystal polymer

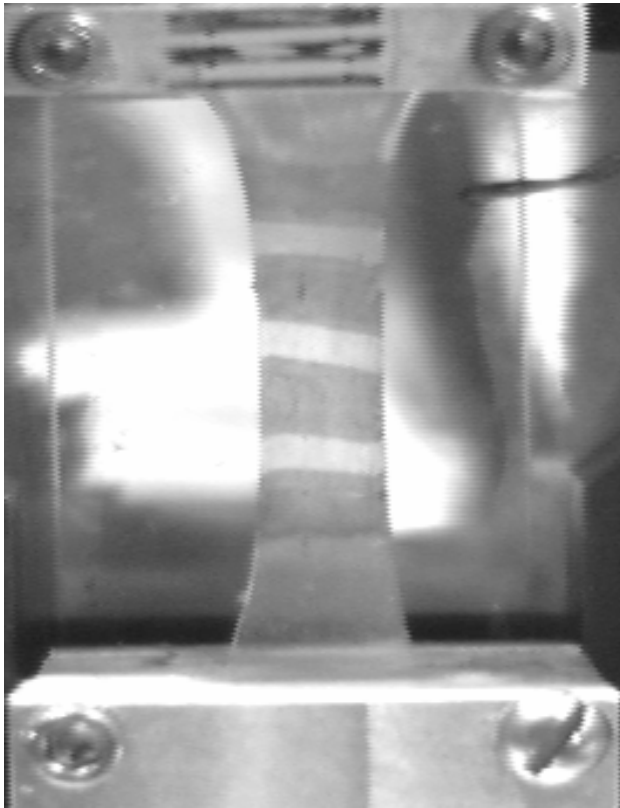
# *X-ray Scattering: Transmission or Reflection?*

Need to be conscious of:

Constituent elements, i.e. absorption cutoffs

Multiple scattering

Area of interest: surface effect or bulk effect



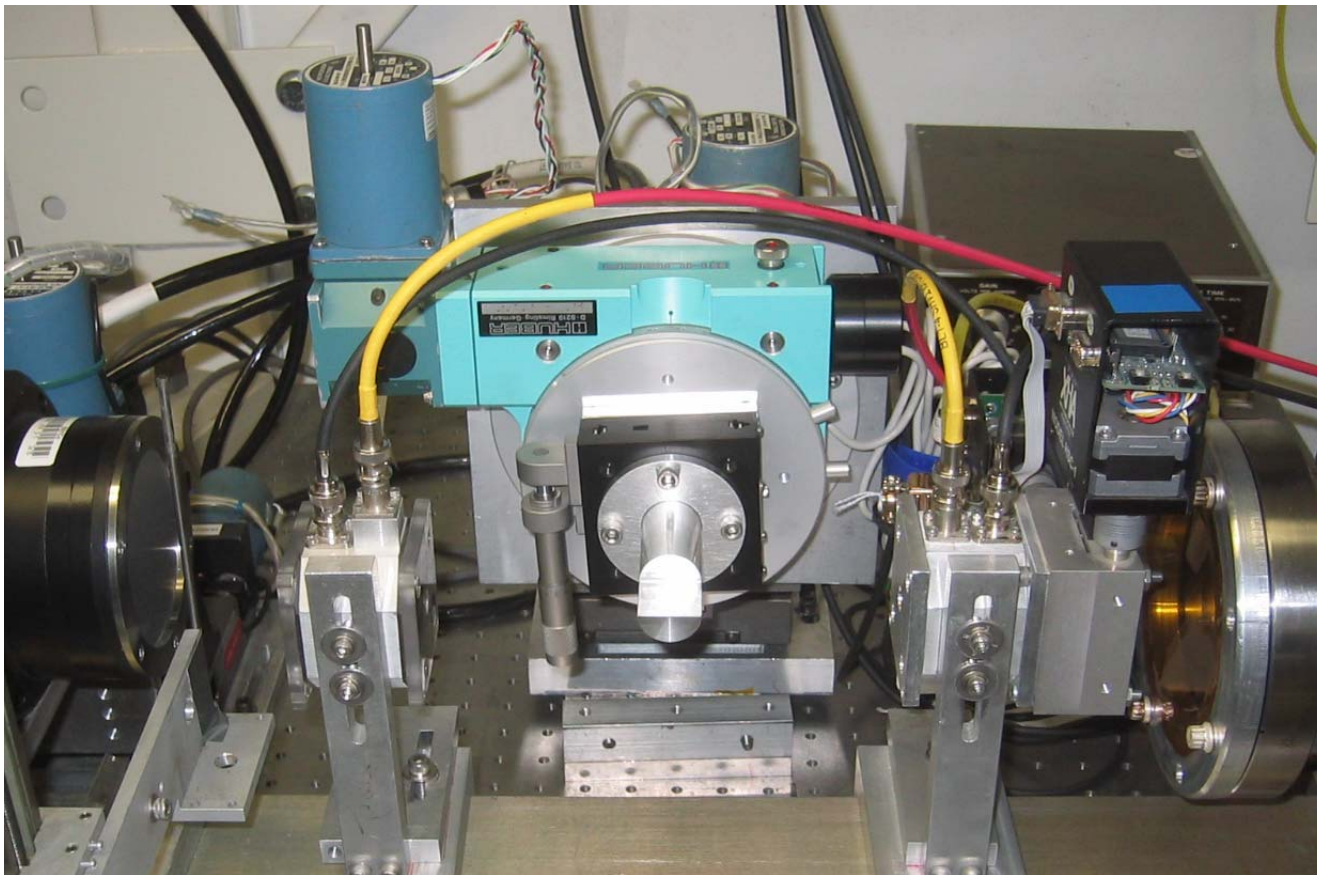
Transmission geometry appropriate for:

- Extracting bulk parameters, especially in deformation
- Weakly scattering samples: can vary path length

## *X-ray Scattering: Transmission or Reflection?*

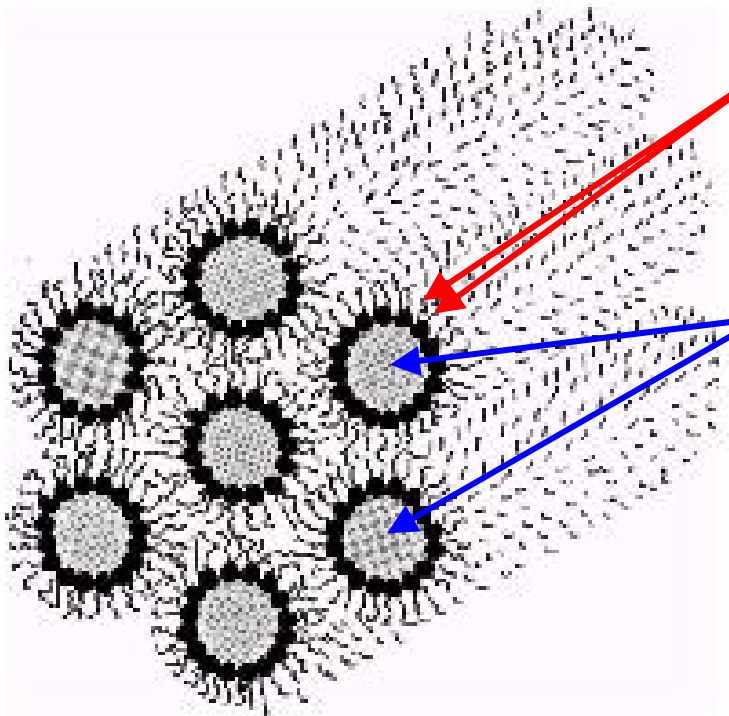
Reflection geometry appropriate for:

- Films on a substrate (whether opaque or not)
- Probing surface interactions



# X-ray Scattering: SAXS or WAXS?

No fundamental difference in physics: a consequence of chemistry



WAXS patterns contain data concerning correlations on an intra-molecular, inter-atomic level (0.1-1 nm)

SAXS patterns contain data concerning correlations on an inter-molecular level: necessarily samples where there is macromolecular or aggregate order (1-100 nm)

As synthesis design/control improves, SAXS becomes more relevant than ever before

# X-ray Scattering: SAXS or WAXS?

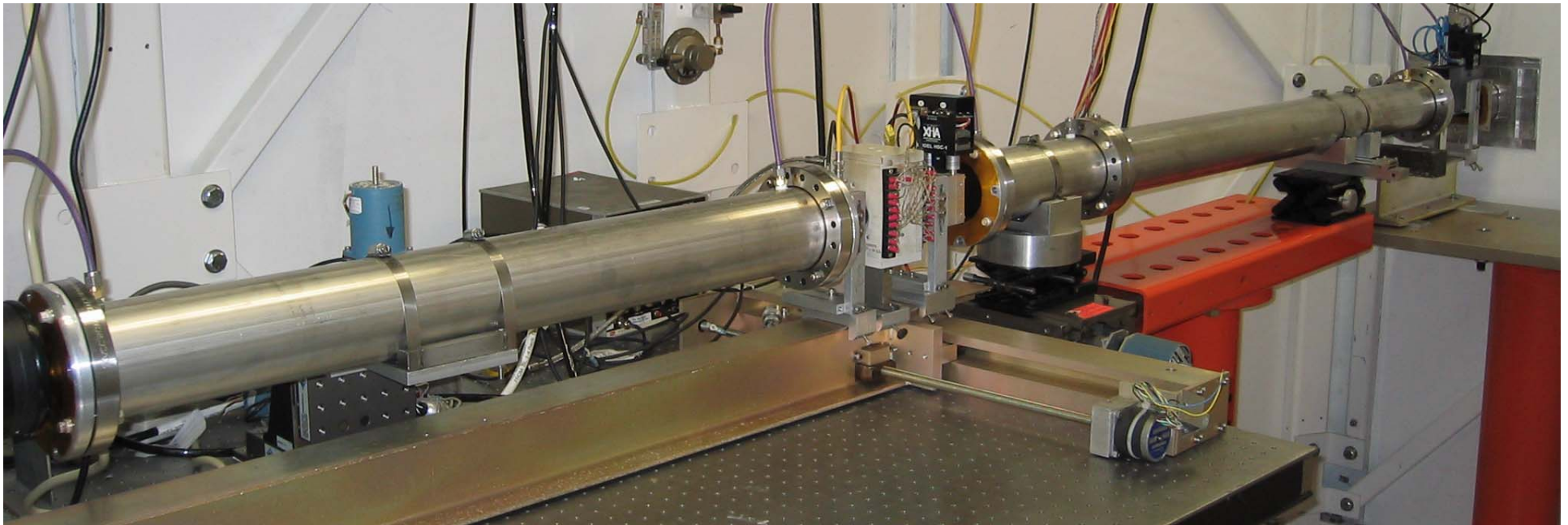
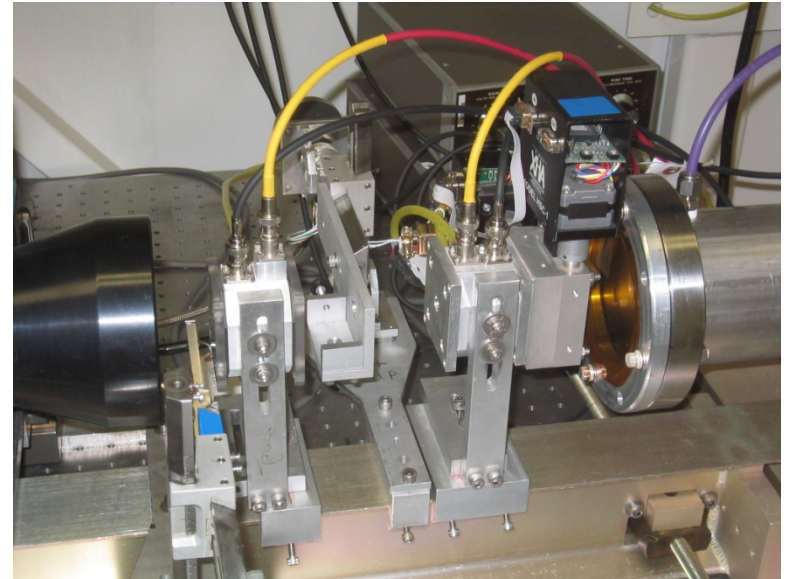
Experimental consequences

WAXS: Detector close to sample, consider:

- Distortion of reciprocal space mapping
- Thermal effects when heating sample
- No ion chamber for absorption

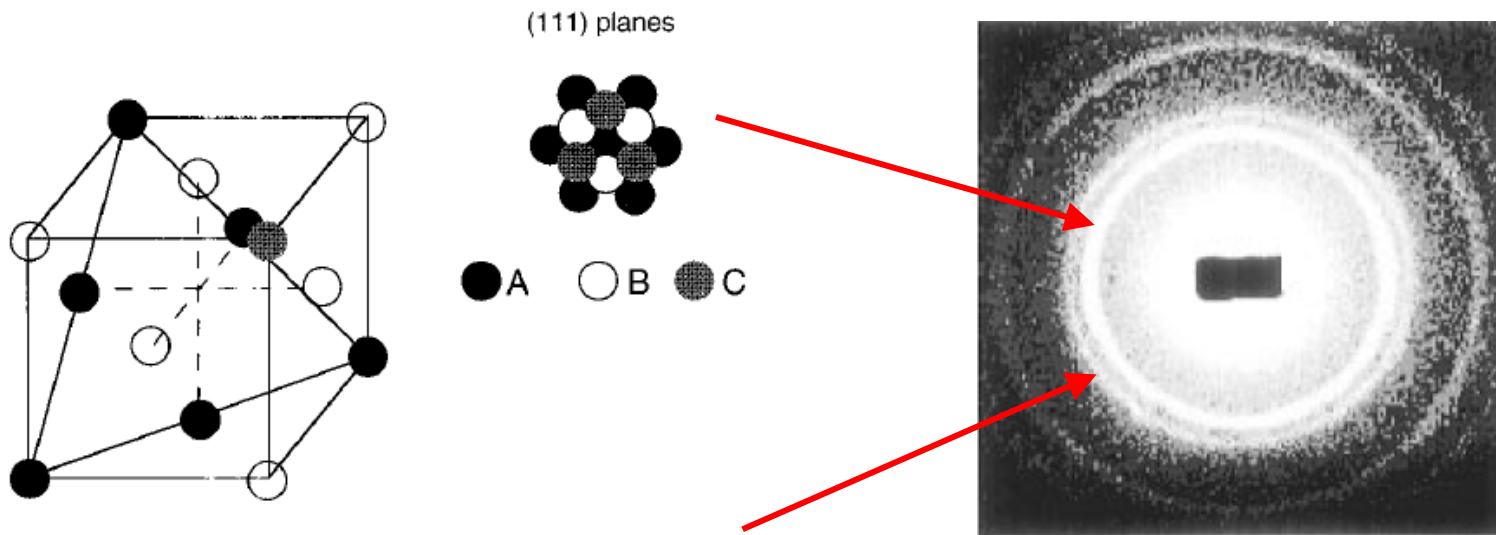
SAXS: Detector far from sample, consider:

- Absorption from intermediate space
- Interception of appropriate  $q$  range



What can I Learn from a  
SAXS Pattern?

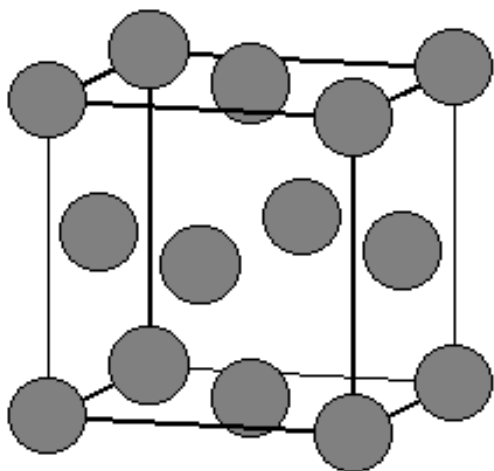
# Recognizing Reciprocal Space Patterns: Indexing



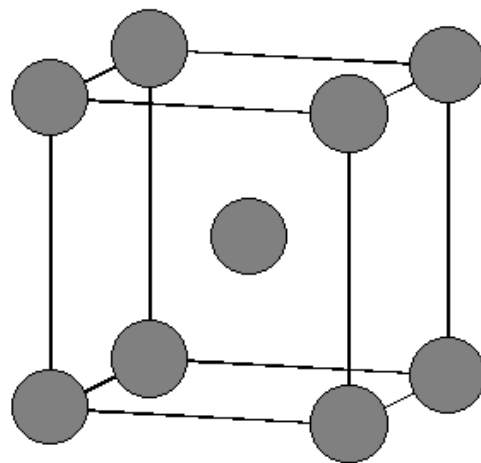
Face centered cubic pattern from diblock copolymer gel

# Recognizing Reciprocal Space Patterns: Indexing

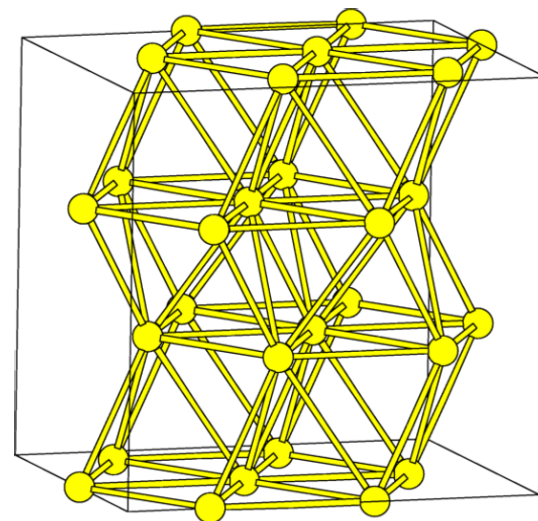
Real space packing



Face centered cubic



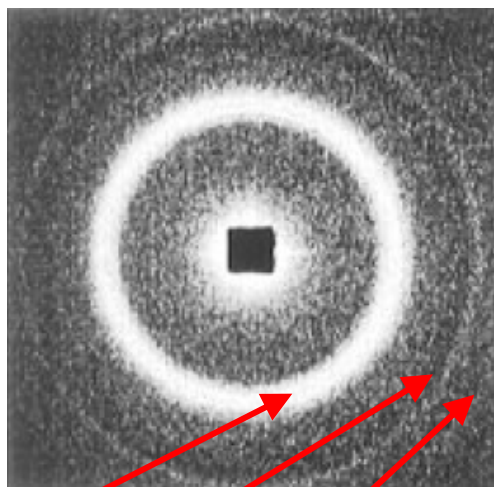
Body centered cubic



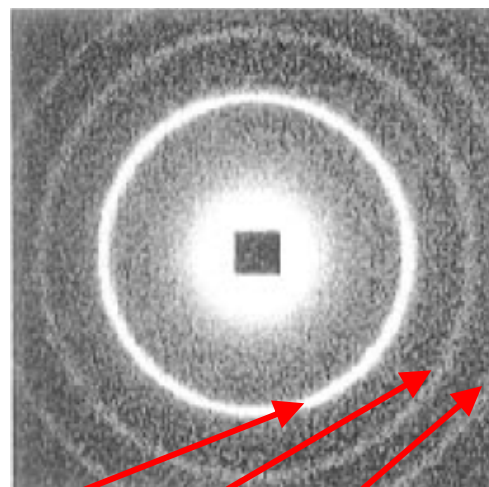
Hexagonal

Reciprocal space image

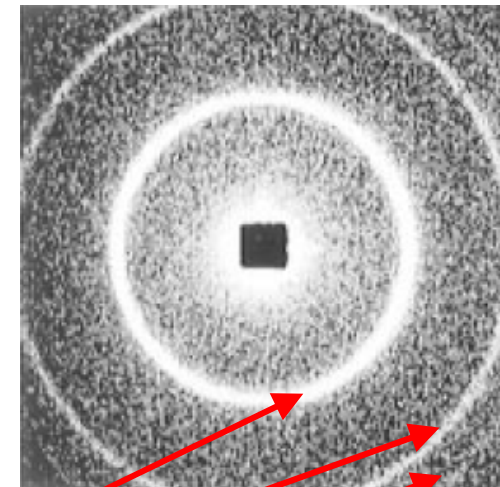
(unoriented domains)



Normalized peak positions  $\equiv 1; =\sqrt{4/3}; =\sqrt{8/3}$



$\equiv 1; =\sqrt{2}; =\sqrt{3}$



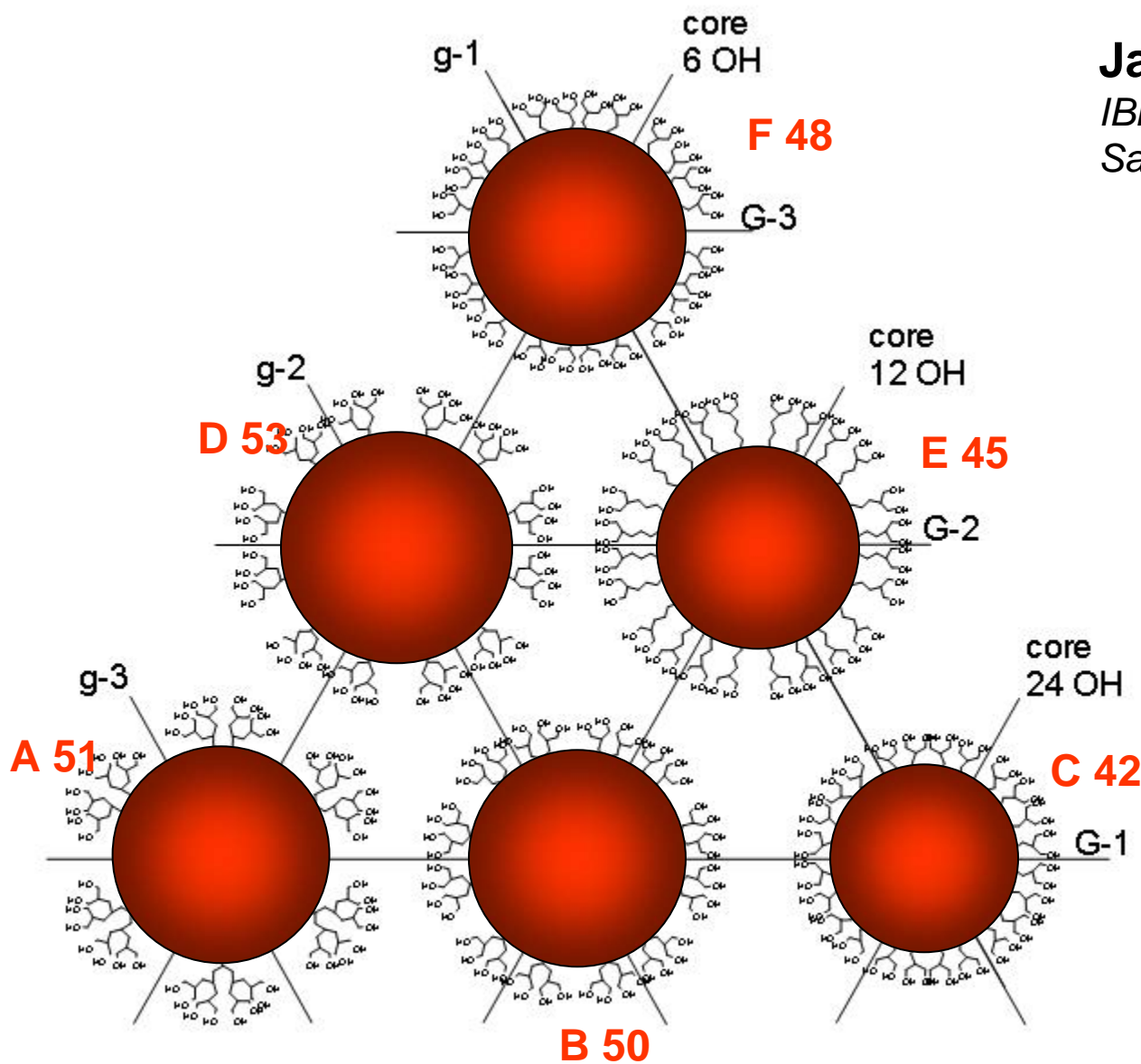
$\equiv 1; =\sqrt{3}; =\sqrt{4}$



# Recognizing Reciprocal Space Patterns: $R_g$

**James L Hedrick**

*IBM Almaden, 650 Harry Road,  
San Jose, CA 95120*

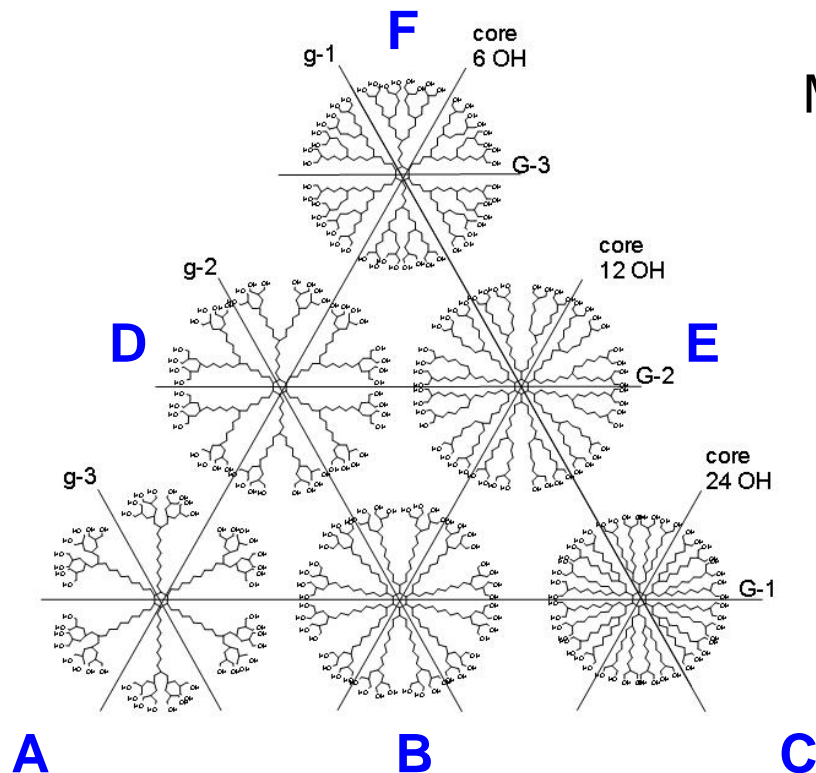


Dendrimers designed as poragens for nanoporous media: interest in monodispersity and density distribution per poragen

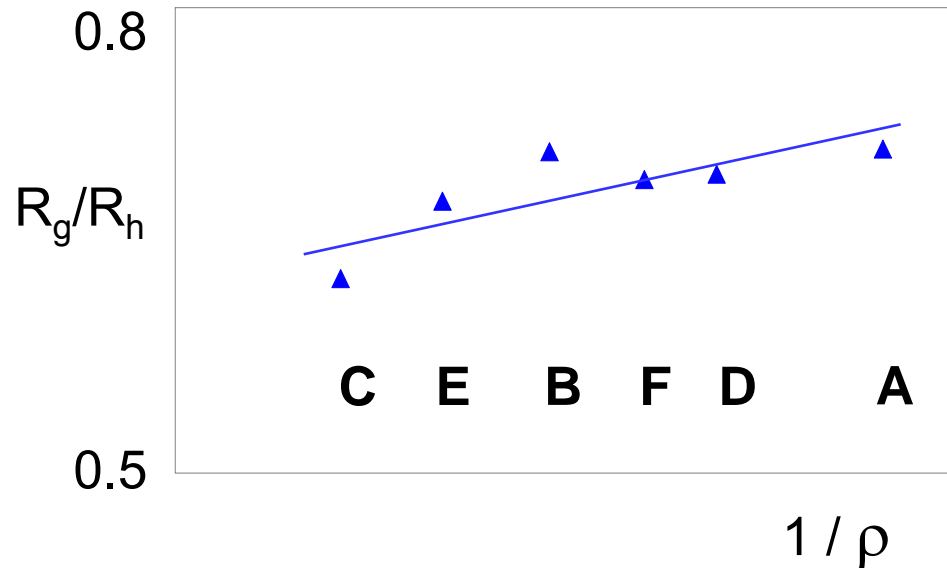
$$R_g^2 \propto \ln I(q) / q^2$$

# Modeling Radial Density of Isomer Architectures

Relate the internal density (and thus functionality as nano-electronic application) of dendrimer isomer to the design architecture, modelling as a star with  $f$  arms. Can predict size and density of sphere from architectural model.

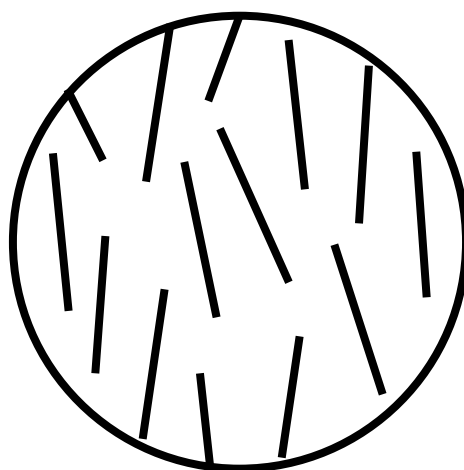
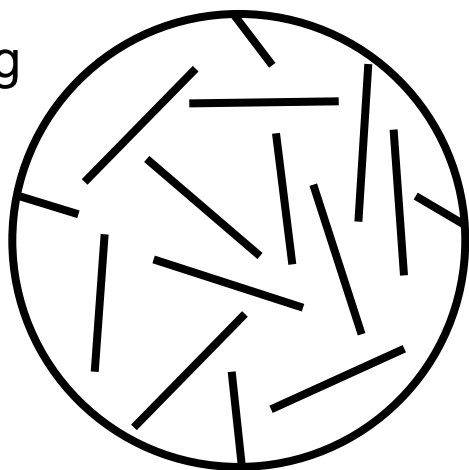


$$\text{Model: } \rho(r) = \int f^{(3v-1)/2v} r^{(1-3v)/v} dr$$



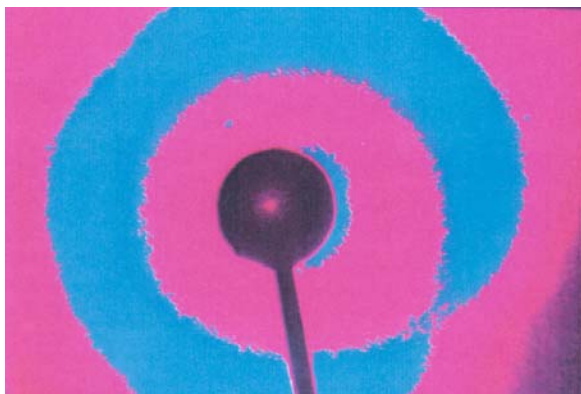
# Recognizing Reciprocal Space Patterns: Preferential Orientation

Real  
space  
packing



Reciprocal  
space  
image

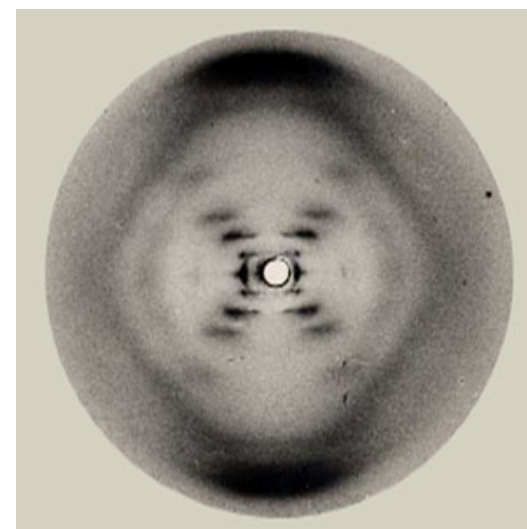
Randomly  
aligned rods



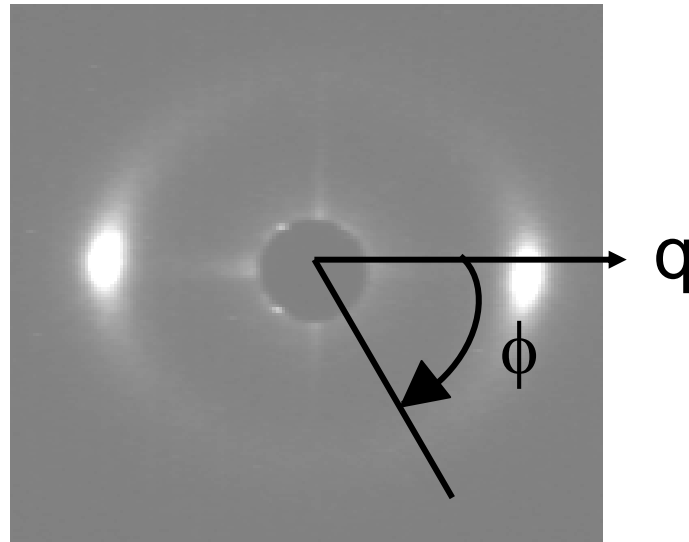
Preferentially  
aligned rods



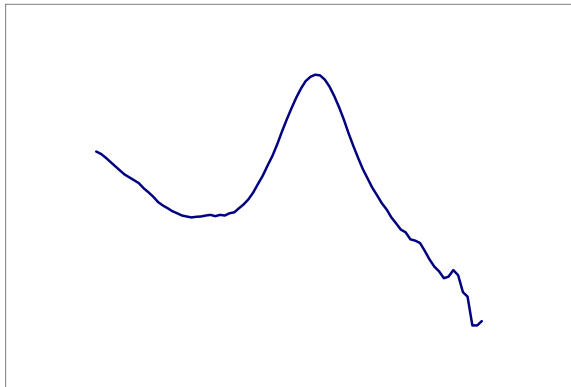
Hydrated DNA



# *Extracting Physical Parameters from X-ray data*

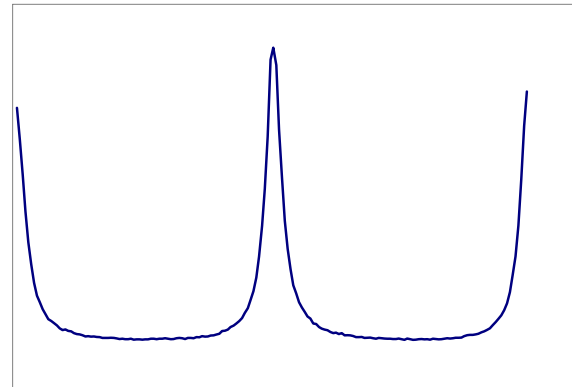


$I(q)$



$q$

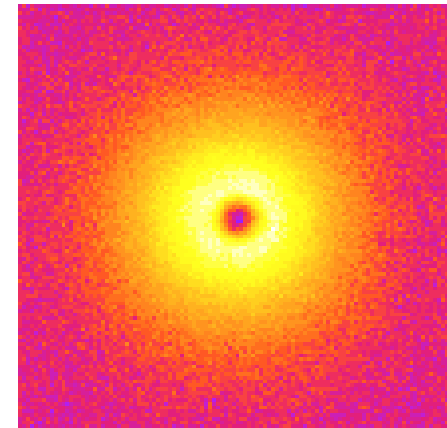
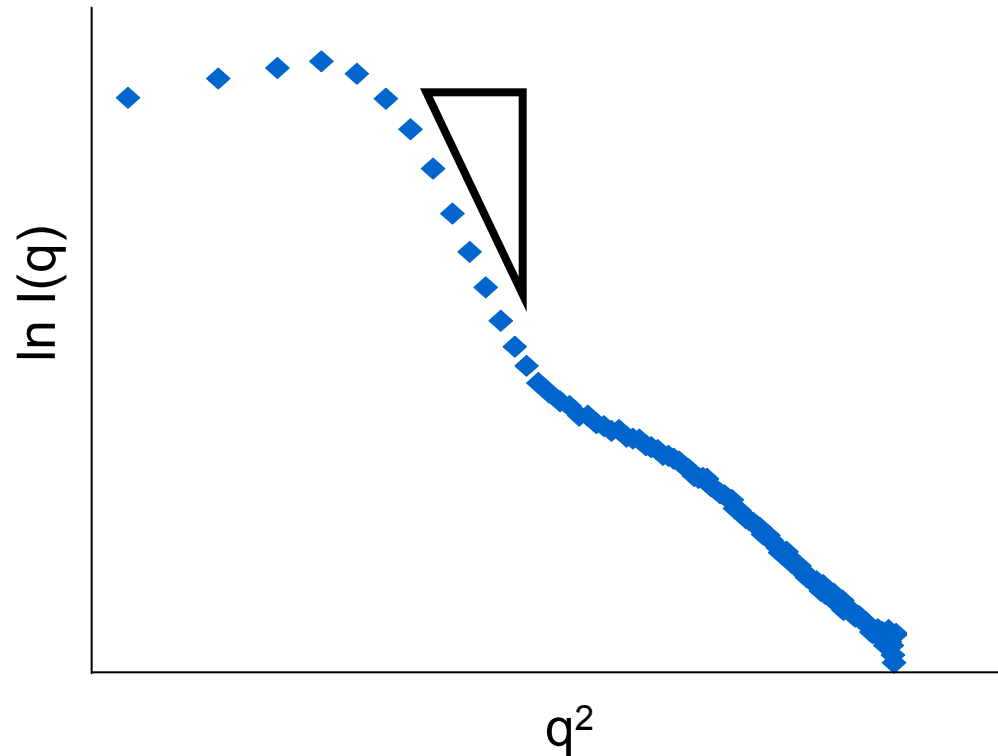
$I(\phi)$



$\phi$

# Extracting Physical Parameters from X-ray data

Molecular size: Radius of gyration ( $R_g$ )



$$I(q) = I(0) \exp [-q^2 R_g^2 / 3]$$

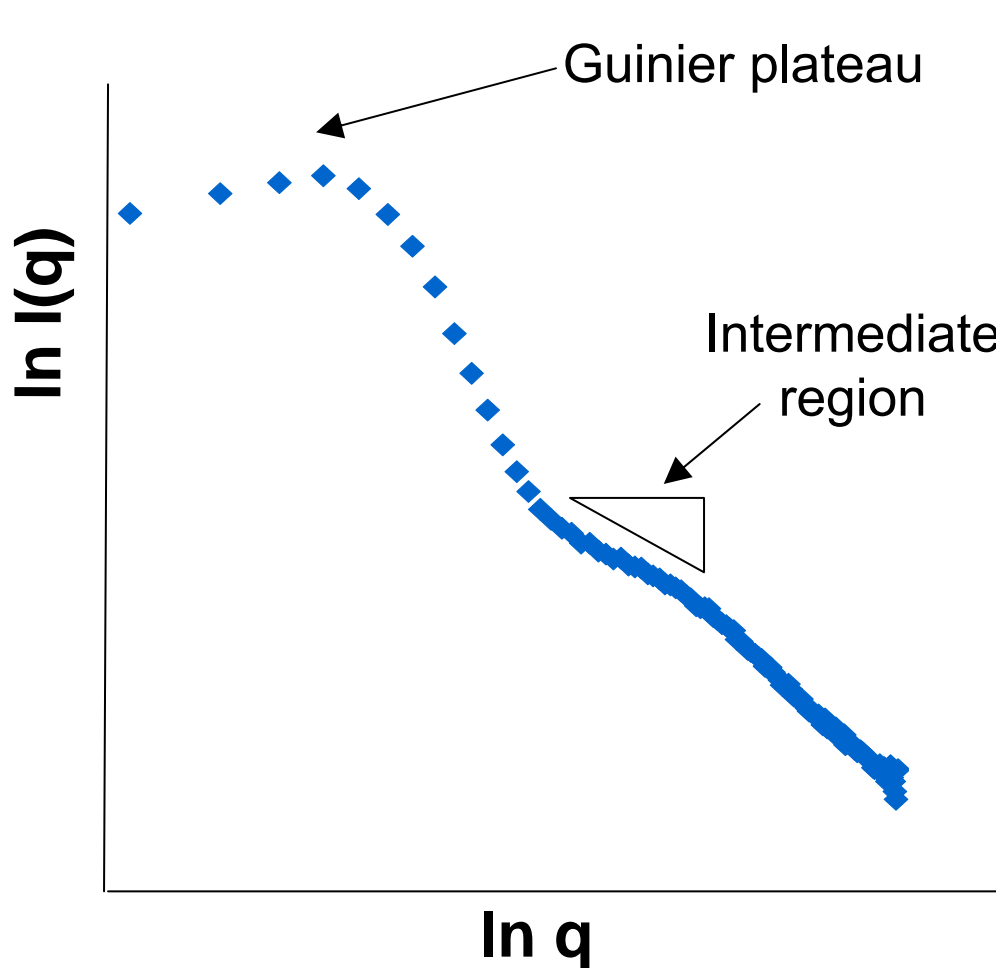
$$R_g^2 \propto \ln I(q) / q^2$$

Guinier region:  $q < 1 / R_g$

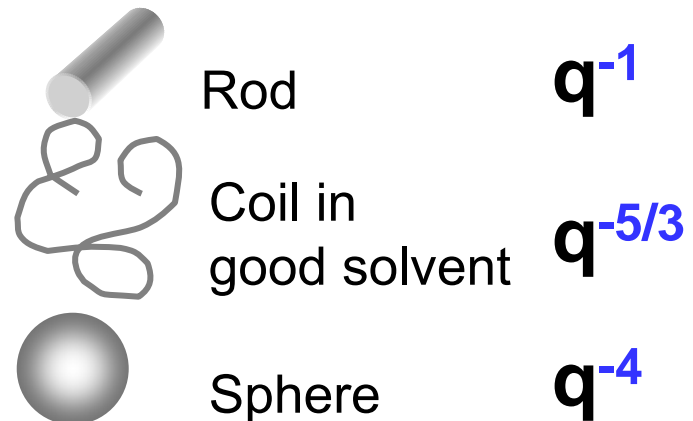
**Guinier plot**

# Extracting Physical Parameters from X-ray data

## Molecular conformation: Scaling exponent



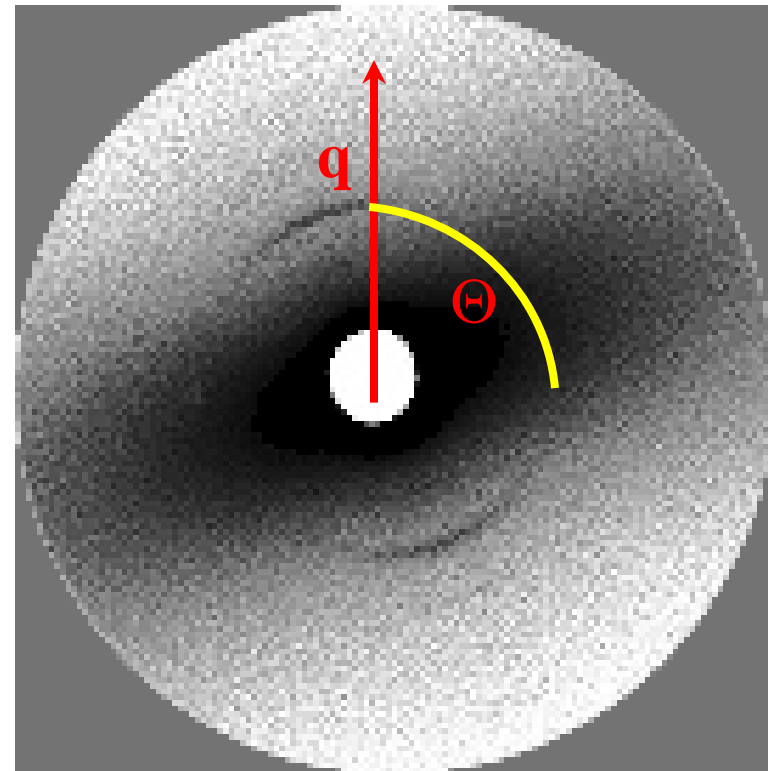
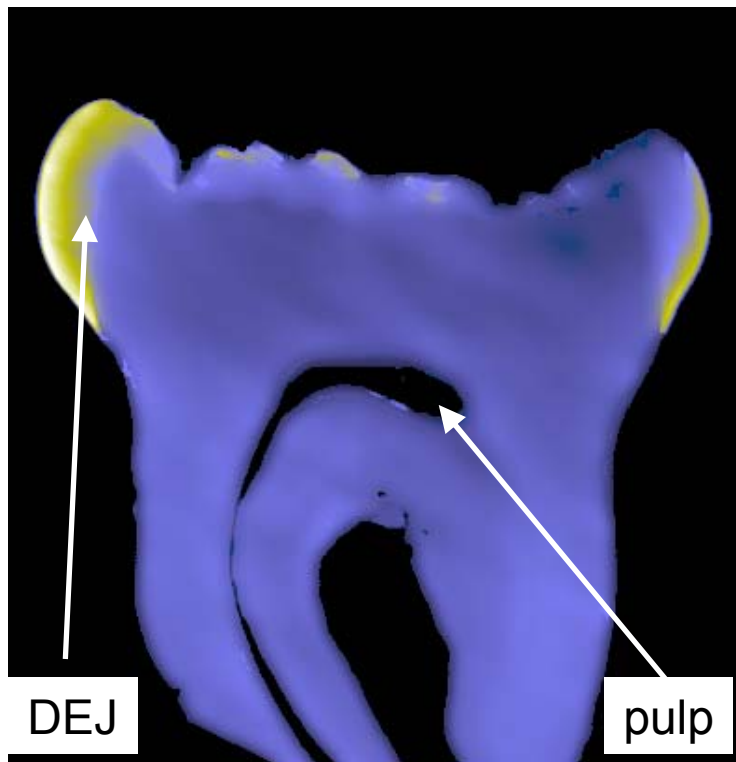
Gradient of profile in intermediate region implies fractal dimension of scattering unit



# Molecular Conformation in Dentin

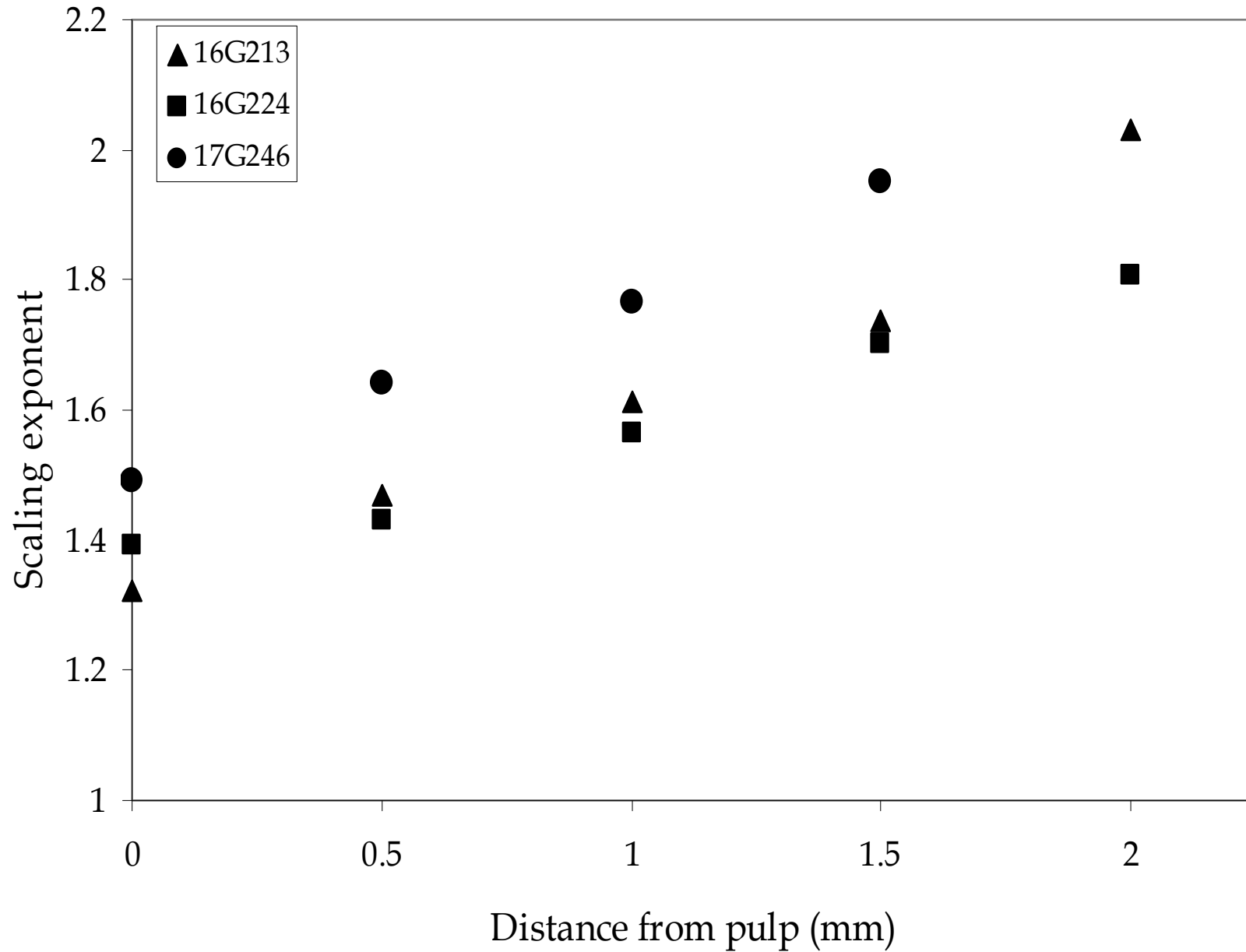
**John H Kinney**

*Department of Preventive and Restorative Dental Sciences,  
University of California, San Francisco, CA 94143*



SAXS pattern

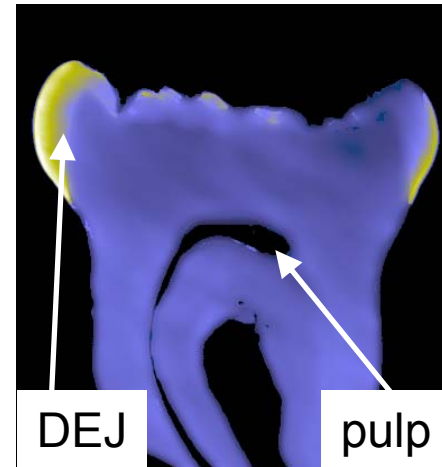
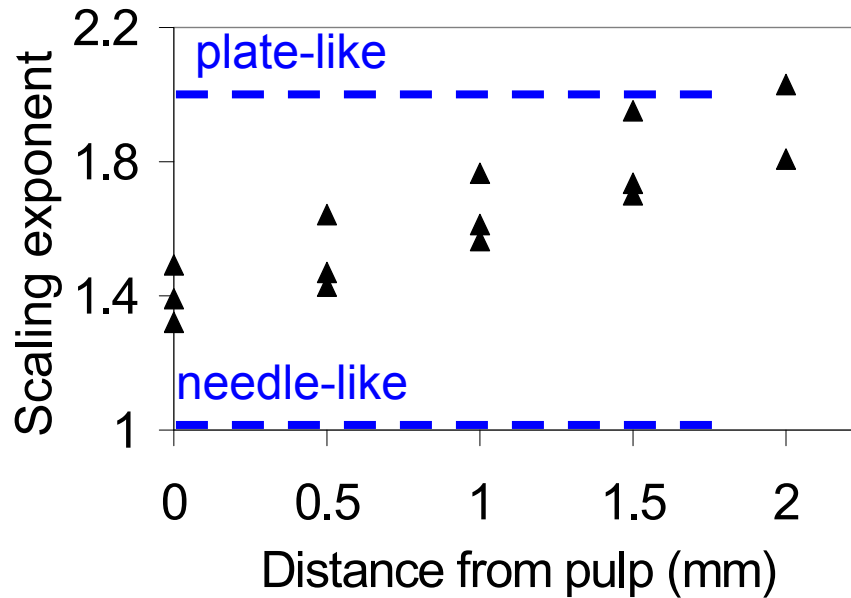
# *Molecular Conformation in Dentin*



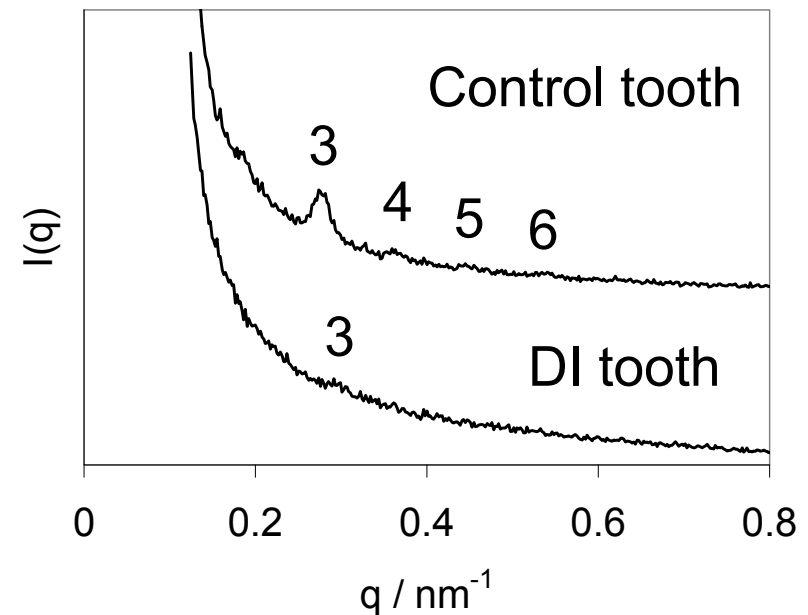


# Molecular Conformation in Dentin

Shape change of mineral crystallites from needle-like to plate-like from pulp to dentin-enamel junction (DEJ).



Dentinogenesis imperfecta (DI) teeth shown to exhibit impaired development of intrafibrillar mineral: characteristic scattering peaks are absent from the diseased tooth.

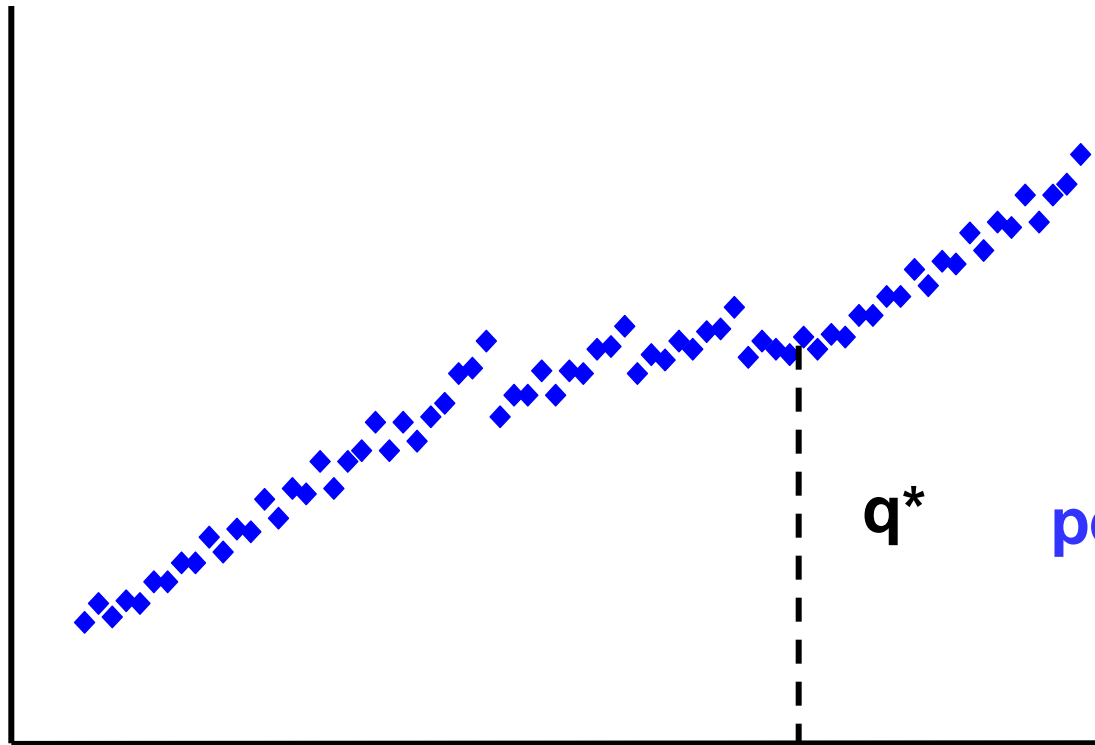


# Extracting Physical Parameters from X-ray data

Molecular conformation: Persistence length of coiled chain

$I(q) q^2$

Kratky plot



$q^*$

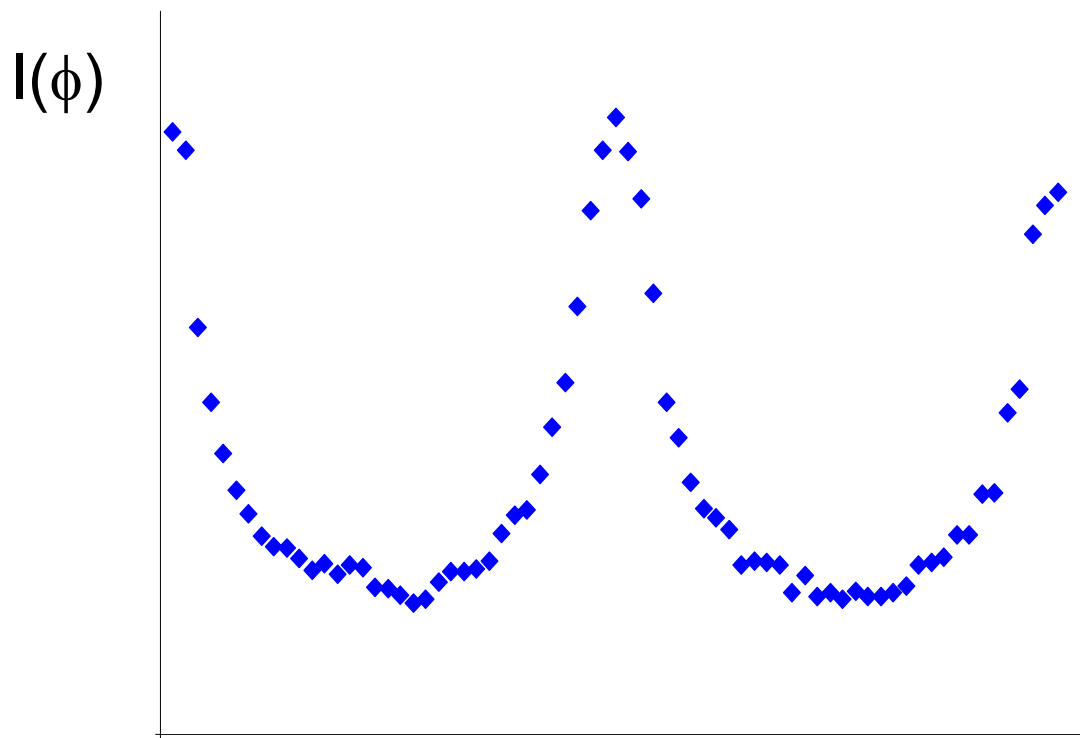
persistence length  
 $= 6 / (\pi q^*)$

$q$

# Extracting Physical Parameters from X-ray data

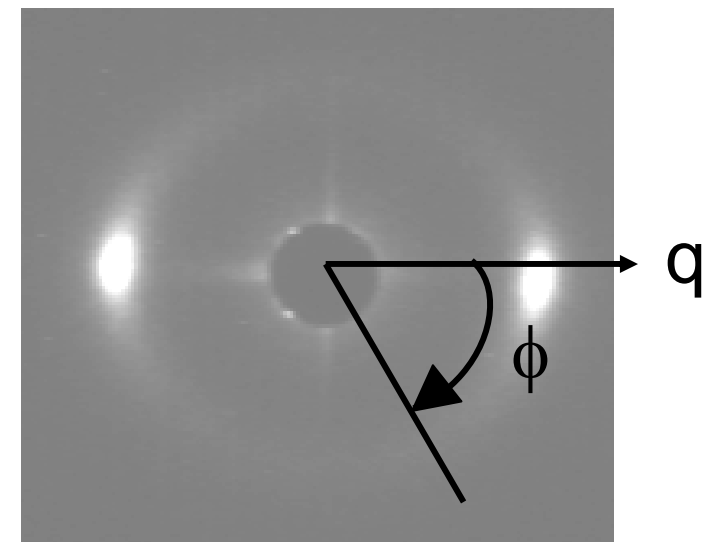
Molecular orientation: Orientation parameter  $P_2$

$$\langle P_{2n}(\cos \phi) \rangle = \frac{\int I(s, \phi) P_{2n}(\cos \phi) \sin \phi \, d\phi}{\int I(s, \phi) \sin \phi \, d\phi}$$



**Azimuthal profile**  $\phi$

Normalized:  
 $-0.5 < P_2 < 1$



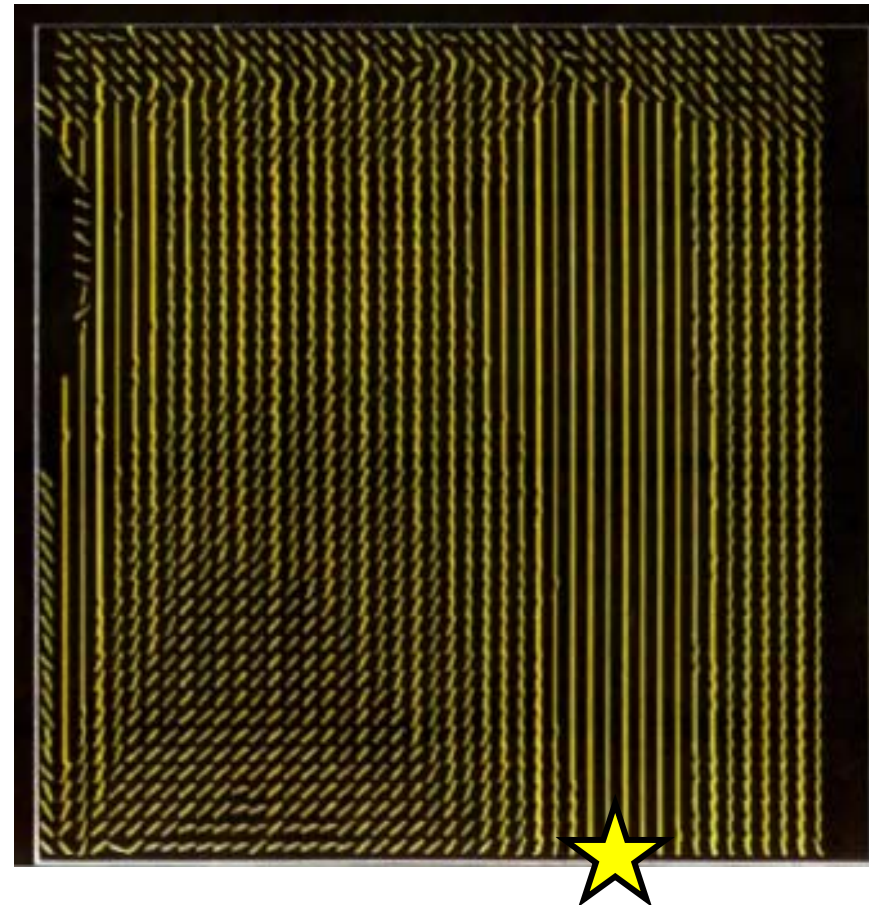
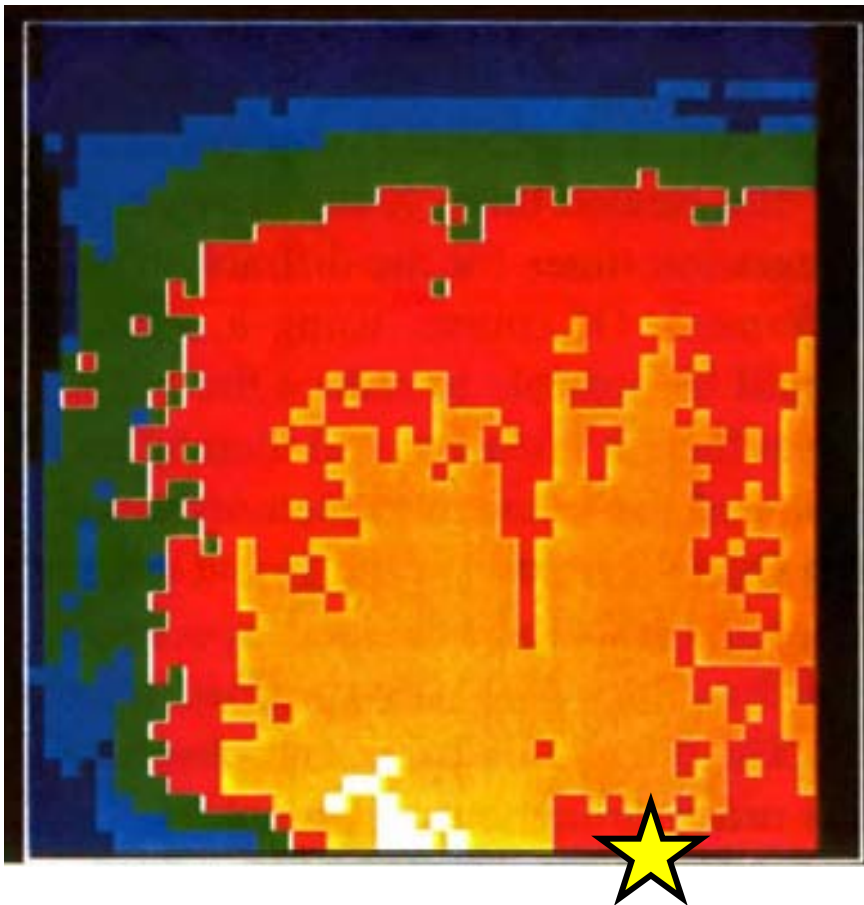
# Molecular Orientation in Injection Moldings

Measuring the degree and inclination of preferential molecular orientation in a piece of injection molded plastic (e.g. hip replacement joints). ~ 1500 WAXS patterns

★ Marks the injection point

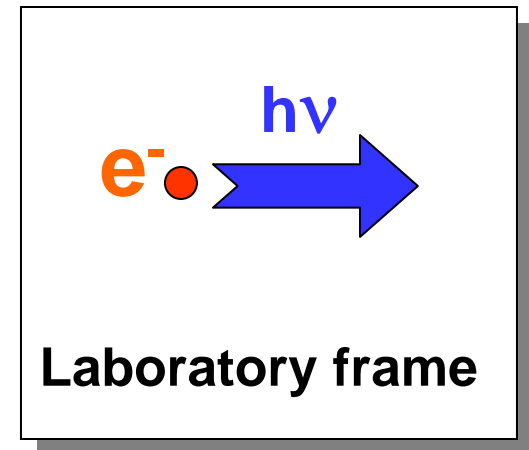
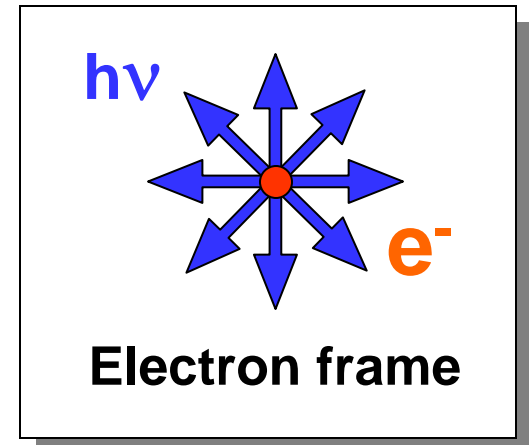
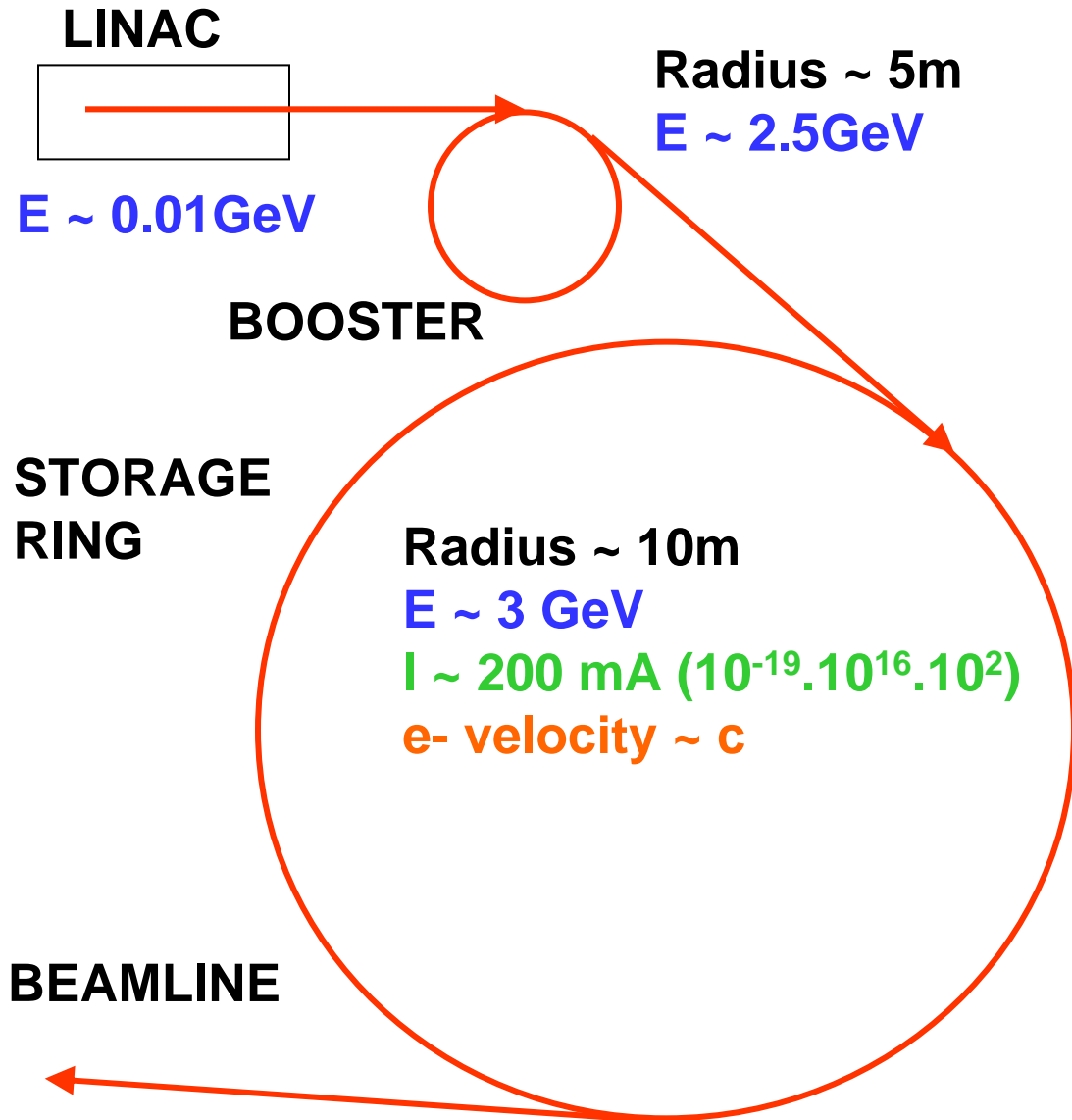
Orientation parameters:  $0 < P_2 < 0.3$

Axis of orientation

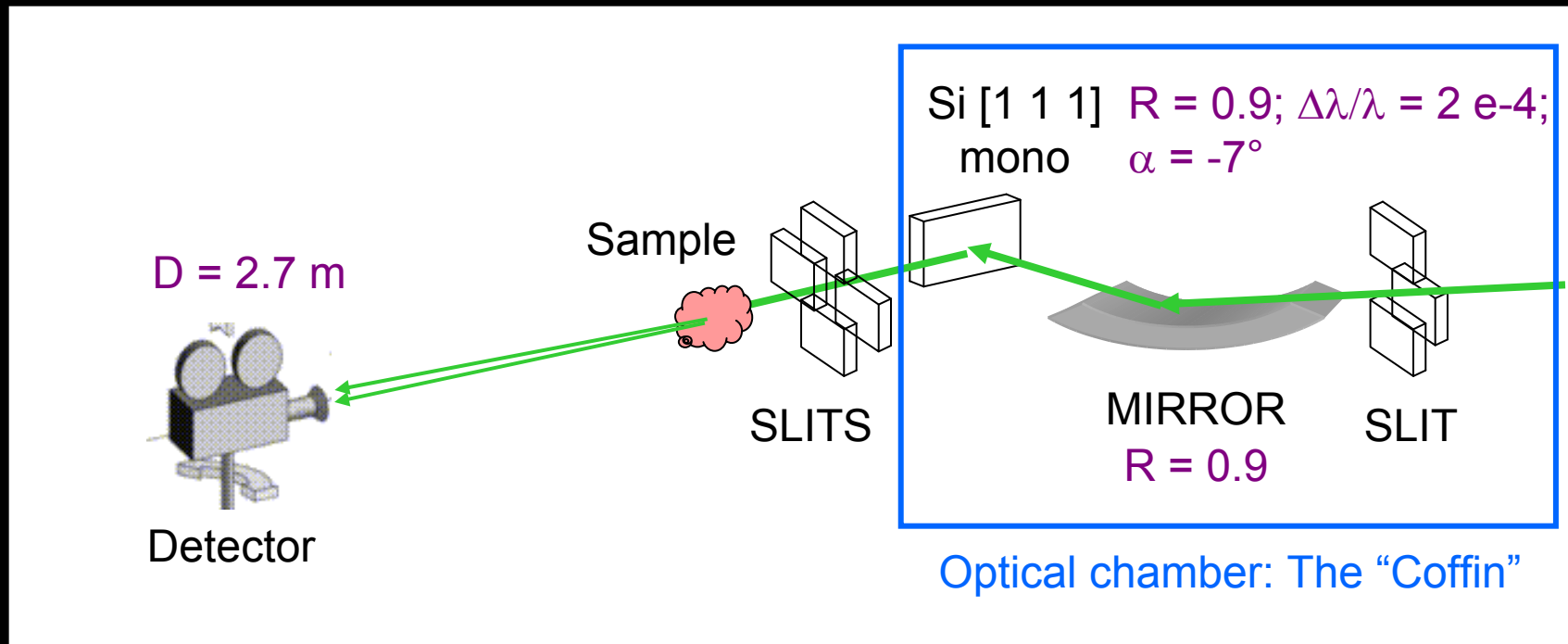


What can the SAXS beamline  
at SSRL do?

# GENERIC SYNCHROTRON LAYOUT



# Beamline 1-4: Materials Science Scattering



Unfocused  $\phi \sim 4 \text{e}11 \text{ h}\nu \text{ s}^{-1} \text{ mA}^{-1}$

Source size:  $8\,000 \mu\text{m}^2$

Min  $q \sim 0.015 \text{ nm}^{-1}$

Max  $d \sim 400 \text{ nm}$

Bent mirror, V focus  
Bent, offcut Xtl mono,  
H focus

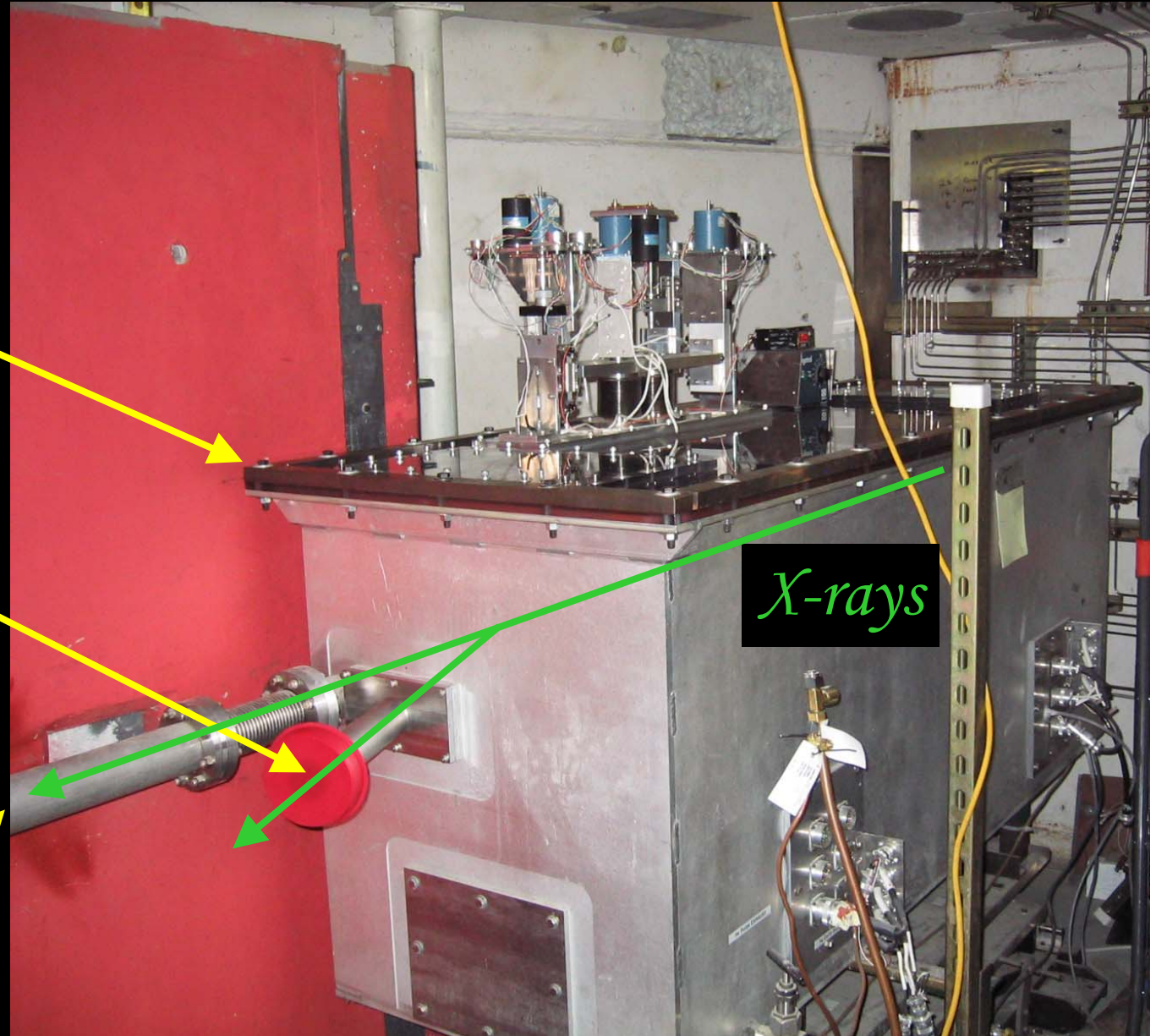
SPEAR3 bend magnet  
 $I = 500 \text{ mA}$ ,  $E = 8333 \text{ eV}$   
 $\sigma(x), \sigma(y) 160 \times 50 \mu\text{m}$

# *Beamline 1-4 upstream optics: The 'Coffin'*

*Helium filled  
drift tank:  
The 'Coffin'*

*Beamline 1-4  
(early design)*

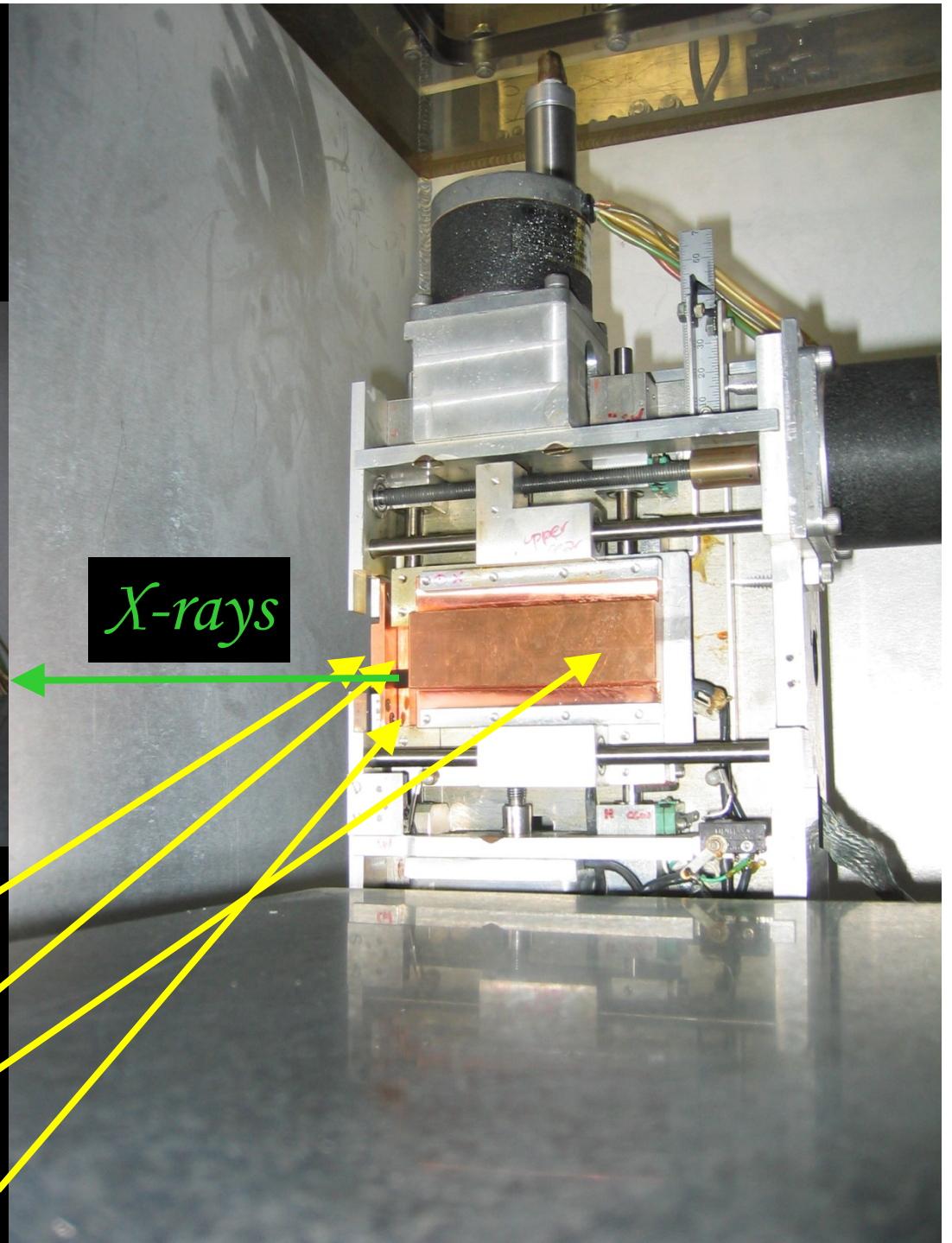
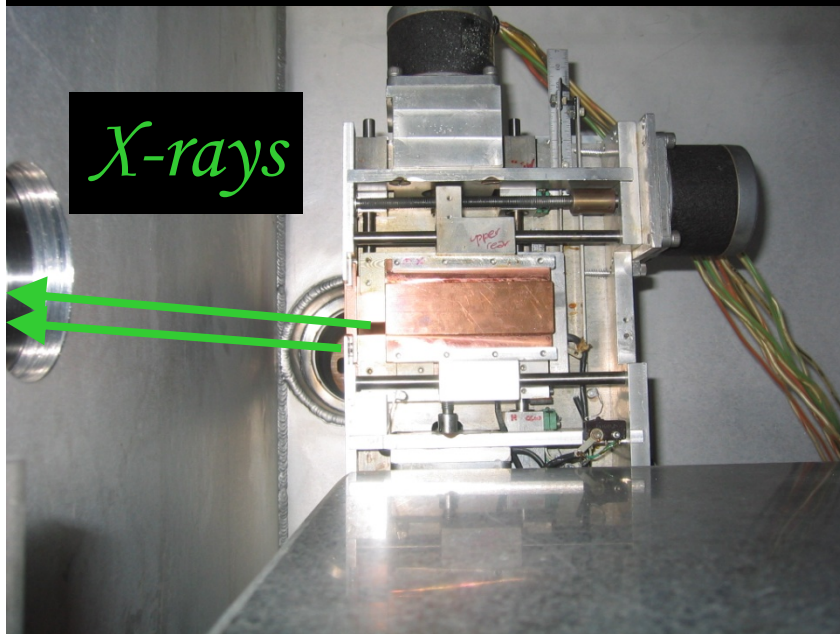
*Beamline 1-5*



*X-rays*



*Inside the 'Coffin':  
Three jaw slit*



*X-rays*

*X-rays*

*Cu side shielding*

*Cu Upper slit*

*Cu Side slit*

*Cu Lower slit*

# *Inside the 'Coffin': Cu cooled Bent Mirror M0*

*Finger comb pressing  
contact onto M0*

*Copper contact bar*

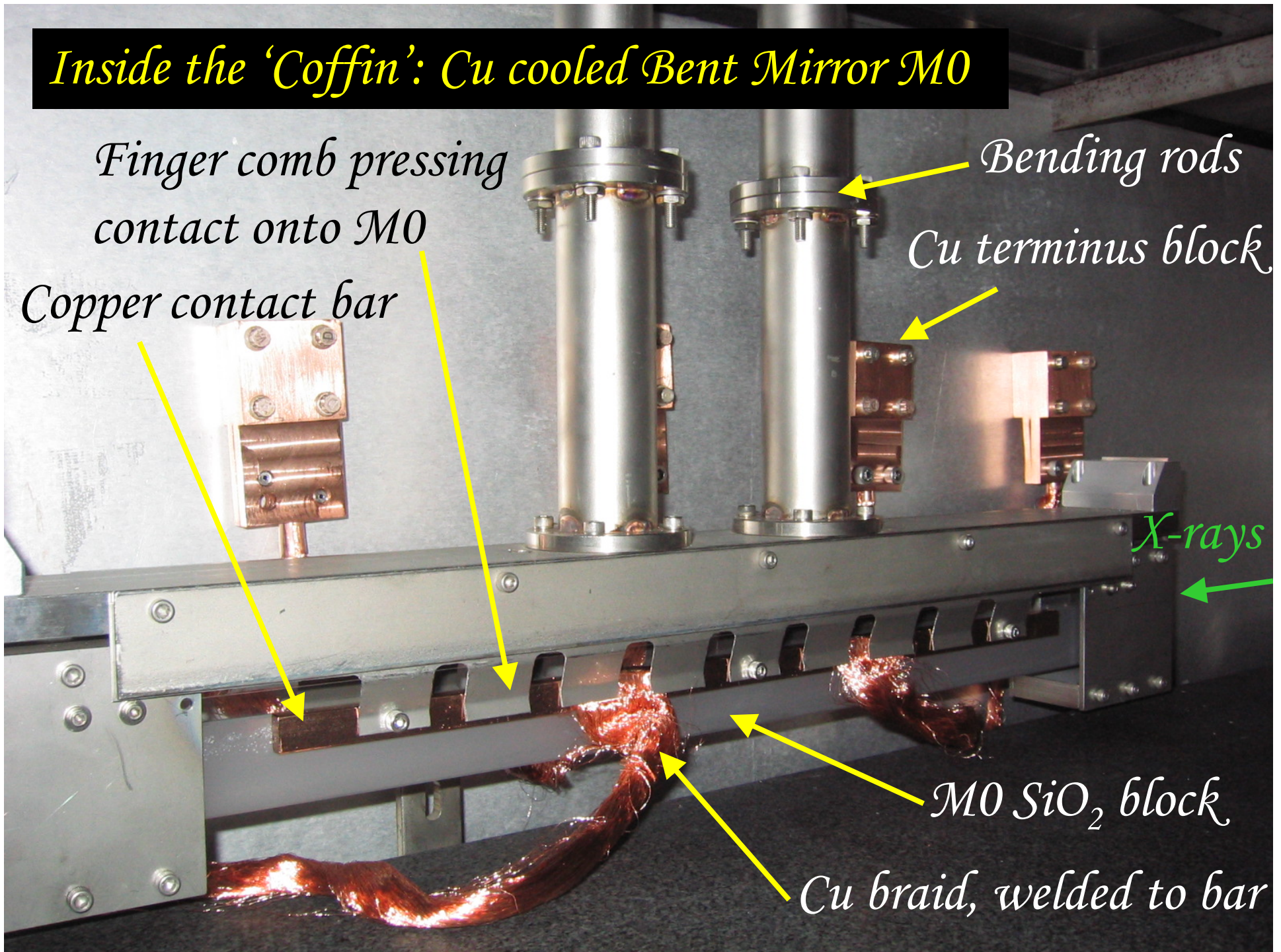
*Bending rods*

*Cu terminus block*

*X-rays*

*M0 SiO<sub>2</sub> block*

*Cu braid, welded to bar*



*MO cooling  
Cu terminus*

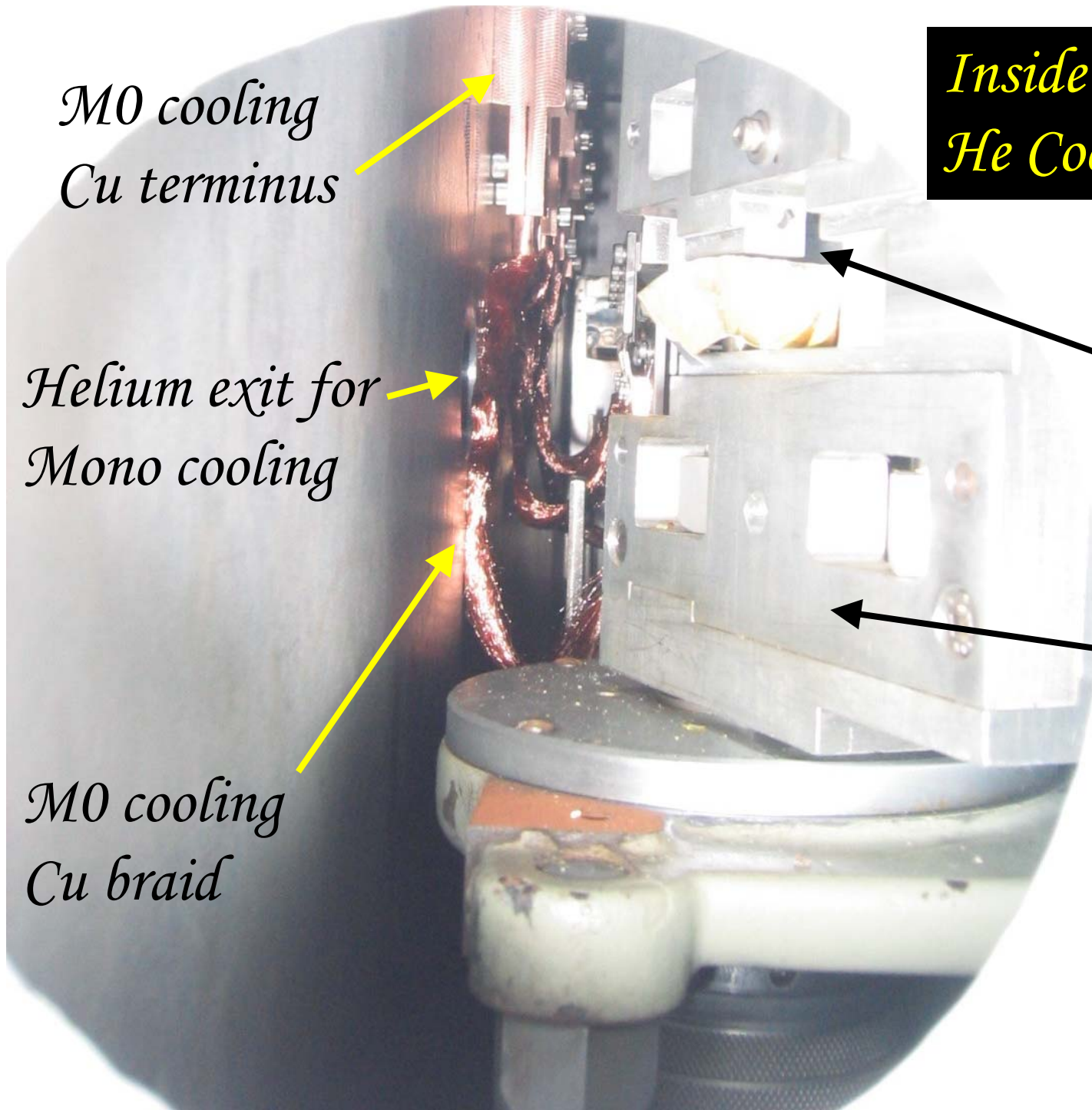
*Helium exit for  
Mono cooling*

*MO cooling  
Cu braid*

*Inside the 'Coffin':  
He Cooled Si Mono*

*Si [111]  
crystal*

*1-4 mono  
assembly*

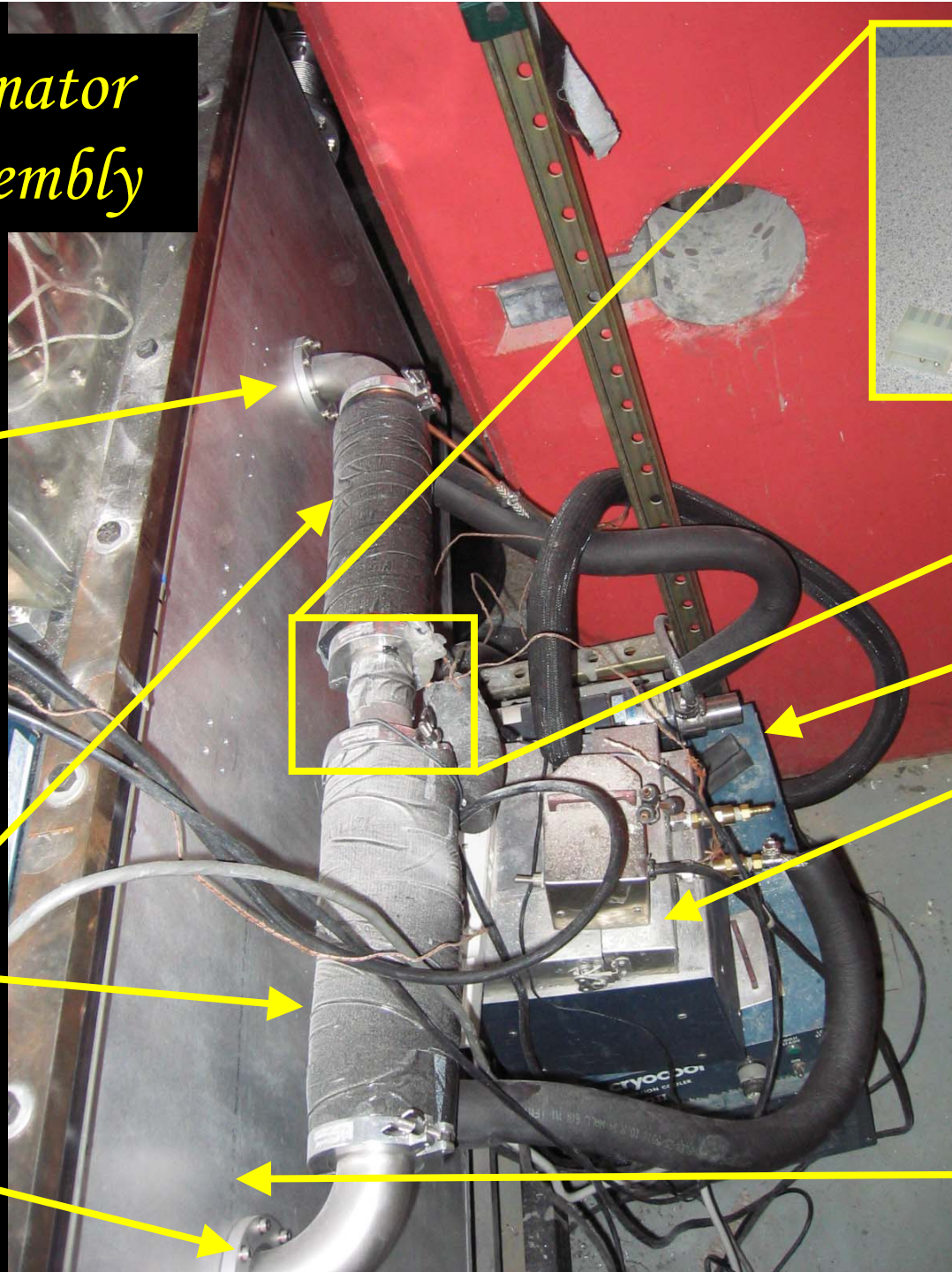


*Monochromator  
cooling assembly*

*He Outlet  
onto mono*

*Cu coils  
around  
He drift  
tubes*

*Intake*

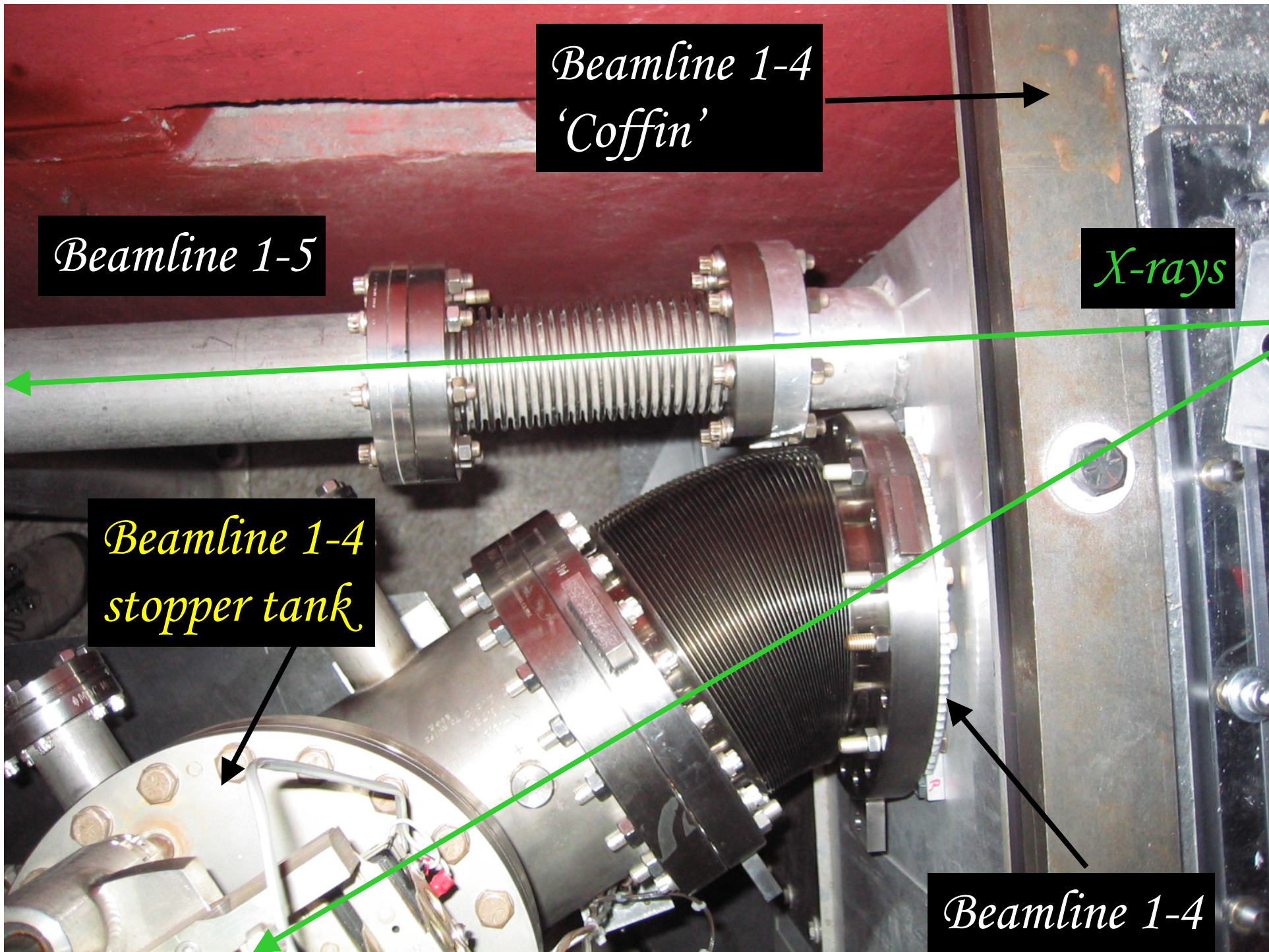


*Fan*

*Chiller*

*Recirculating  
bath*

*Helium  
filled  
'Coffin'*



*Beamline 1-4  
'Coffin'*

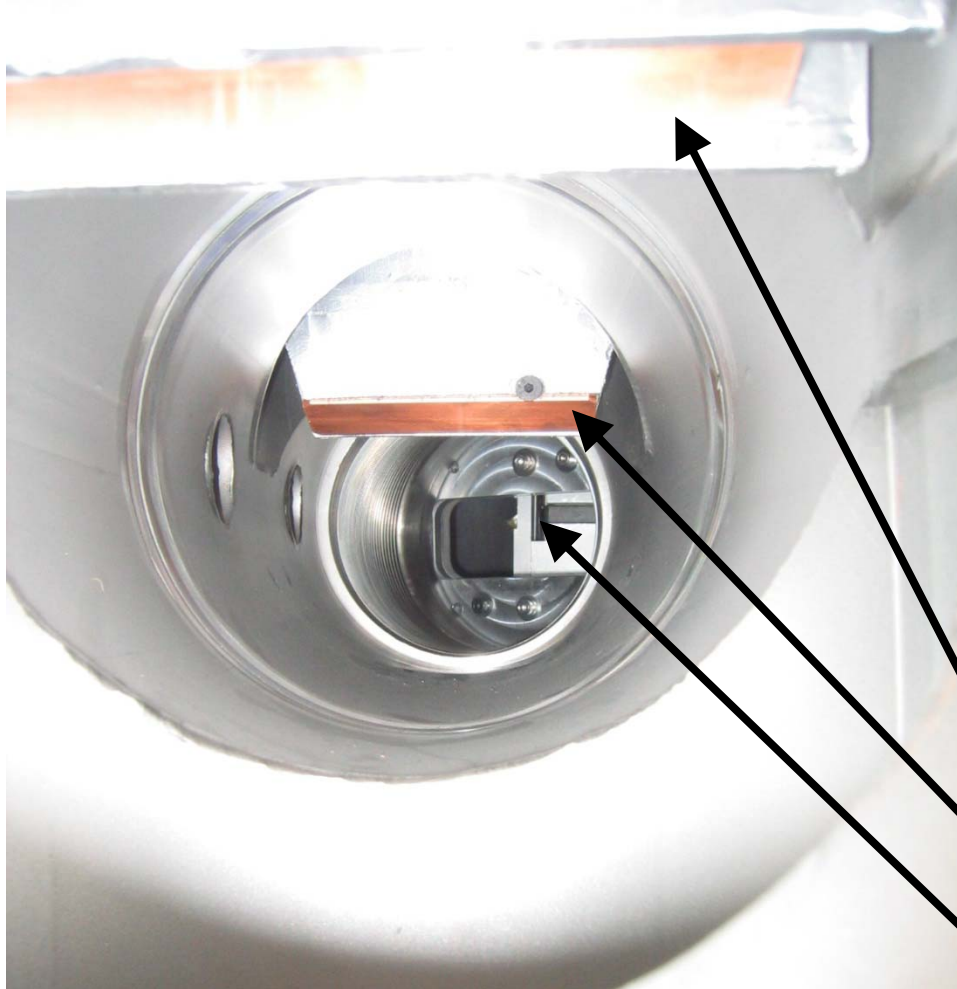
*Beamline 1-5*

*X-rays*

*Beamline 1-4  
stopper tank*

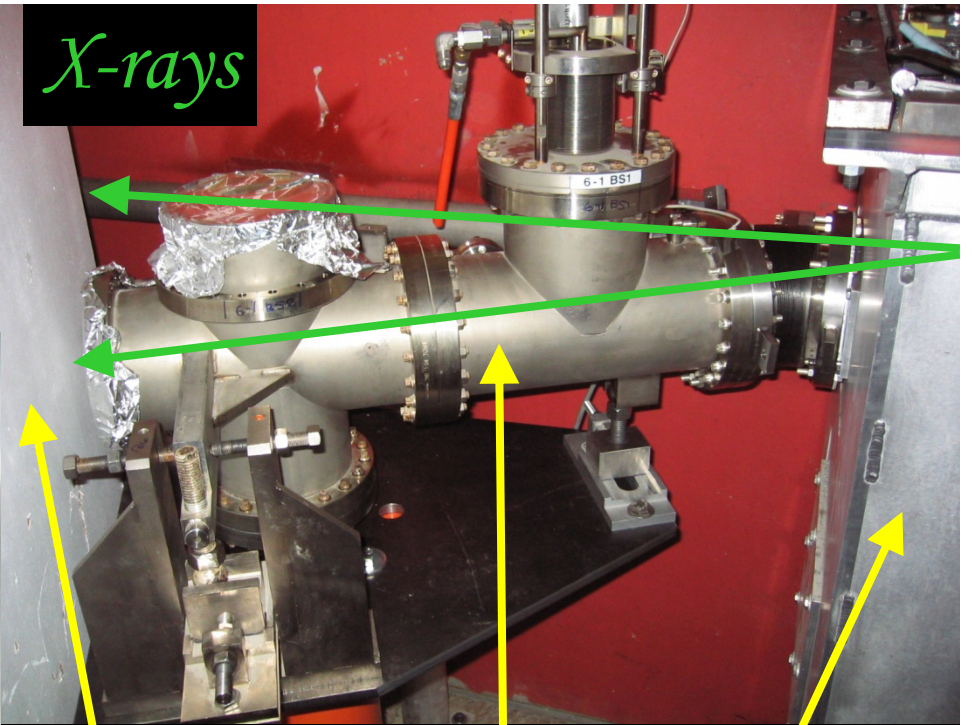
*Beamline 1-4*

*Beamline 1-4 stoppers*



*Inside 1-4 stopper tank*

*X-rays*



*Experimental Hutch*  
*Stopper Tank*  
*'Coffin'*

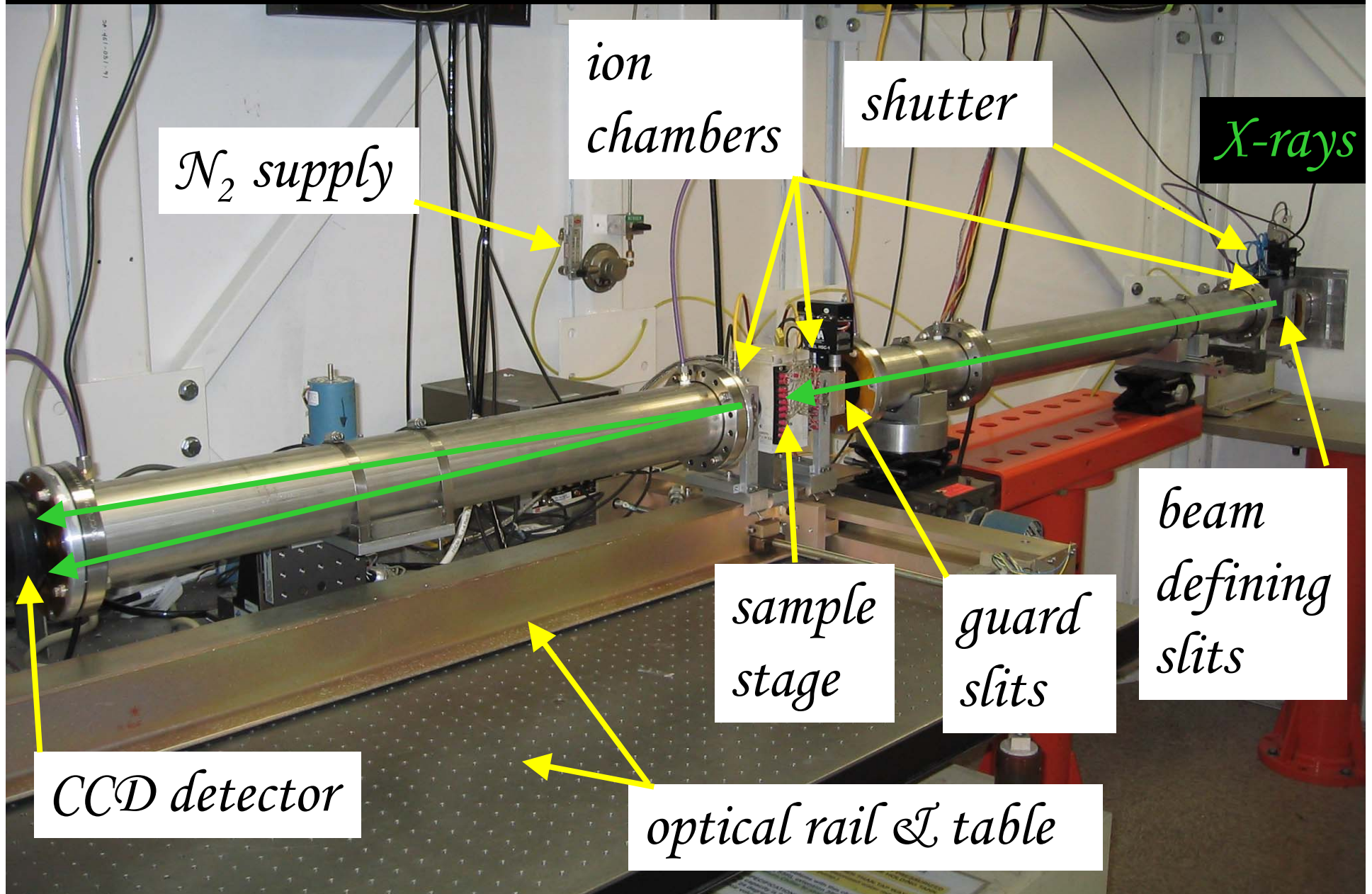
*stopper 2*

*stopper 1*

*Mono crystal*

*Each stopper*  
*1.25" Cu + 2 x*  
*3/16" Pb*

# SSRL Beamline 1-4: SAXS Materials Science



# *Experimental Hutch*

*Ion chamber readout*

*Motor position encoders*

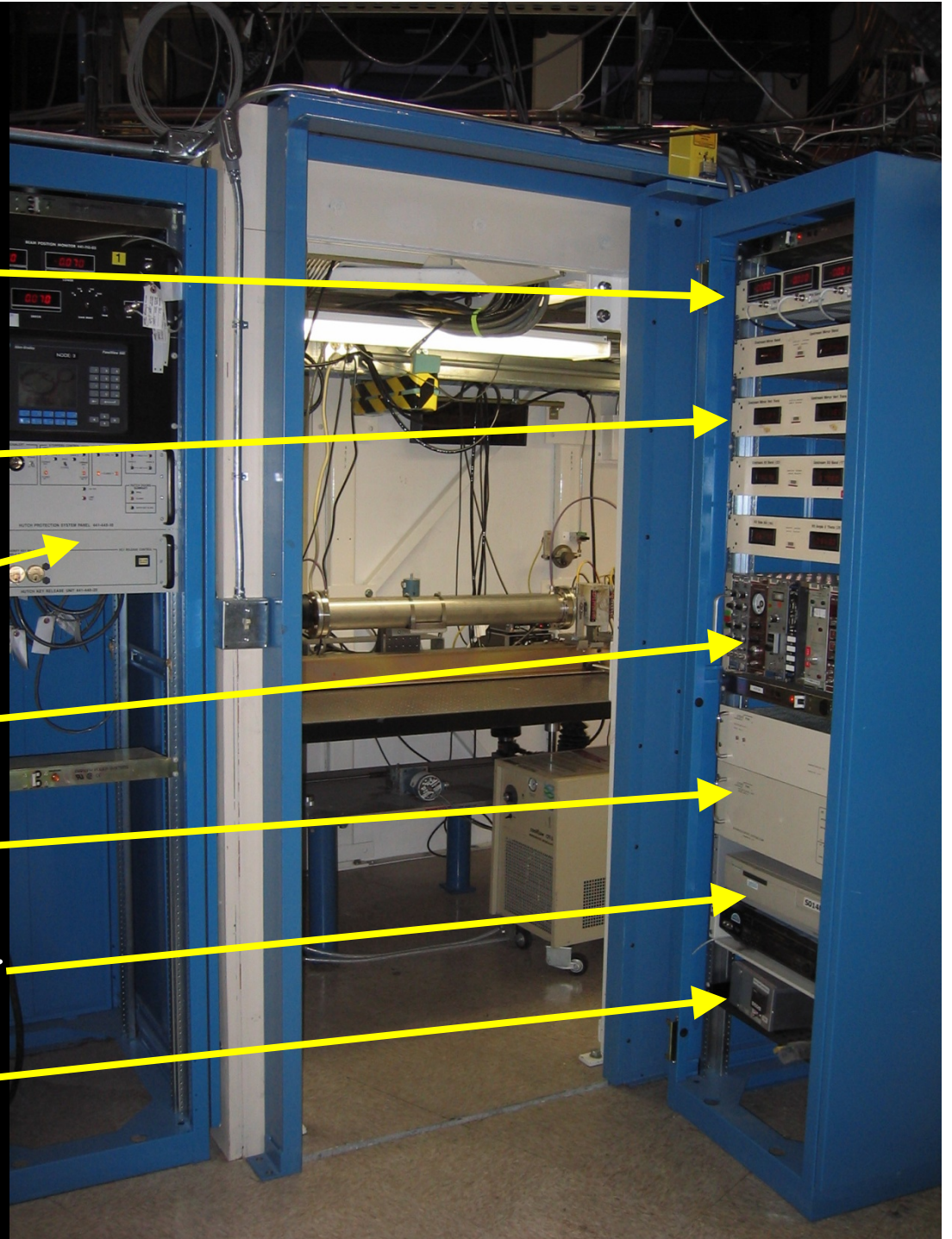
*Hutch stopper control*

*Electronics control chassis*

*Motor control chassis*

*Beamline control computer*

*Sample temperature control*

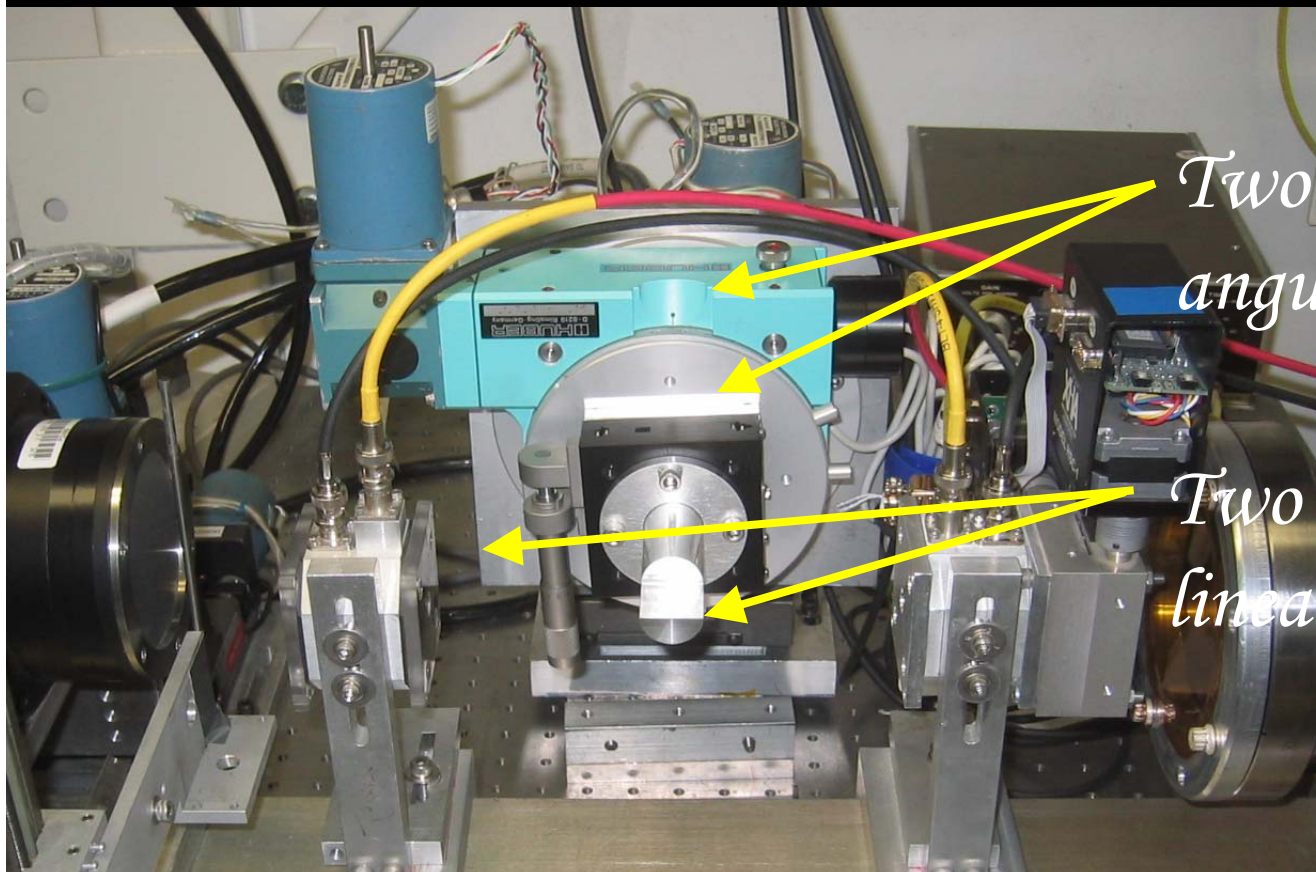




## *Sample Environments: Goniometer*

*Used for Reflection X-ray geometries*

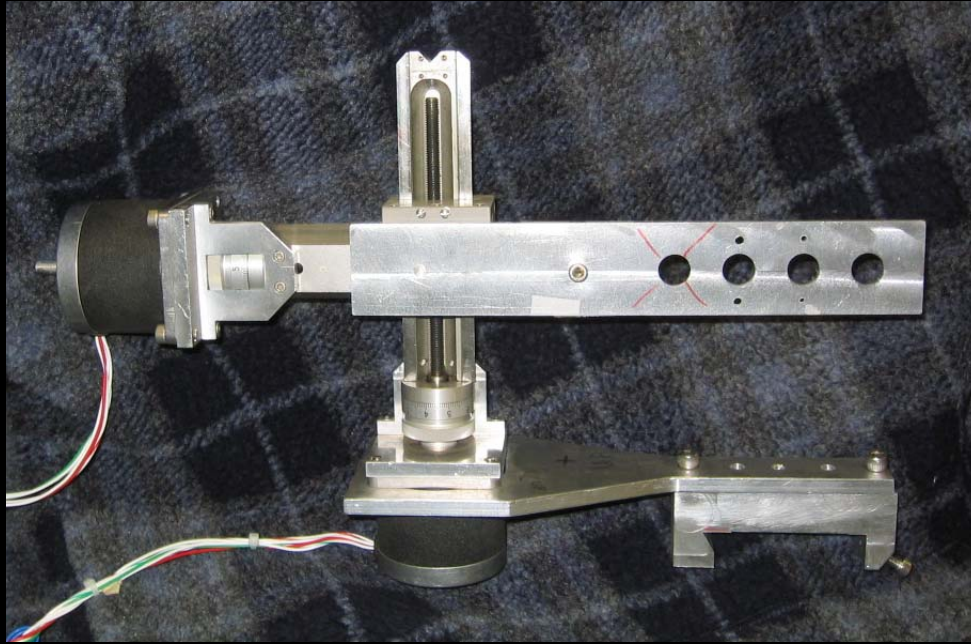
*Huber 410 Goniometer*



*Two axes  
angular translation*

*Two axes  
linear translation*

## *Sample Environments: X-Y drivable flat mount*



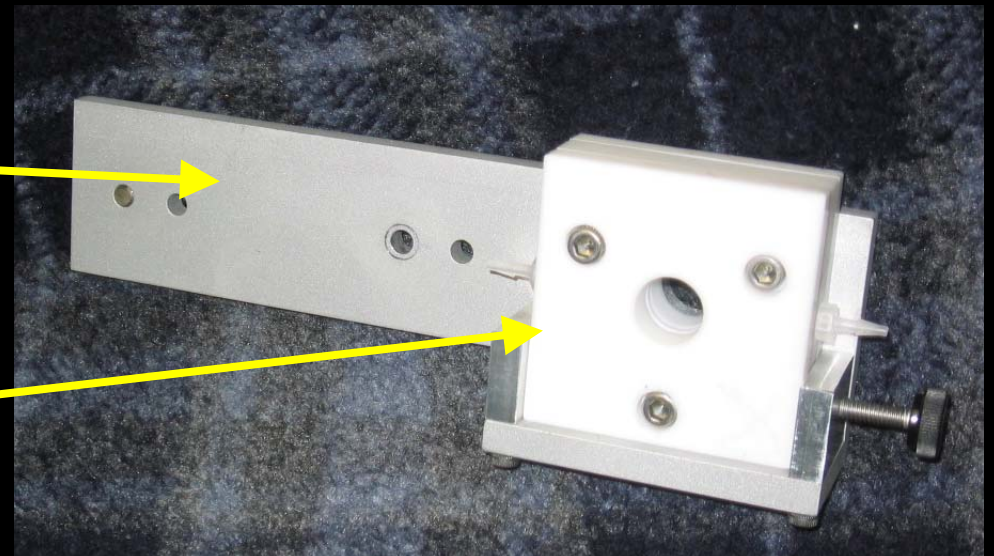
*Four sample positions*

*x and y drives  $\pm 2.25\mu\text{m}$*

*x and y throw  $\sim 100\text{mm}$*

*Adaptor to hold fluid cells*

*Fluid cell with flow feeds*



*Sample Environments: Oven*

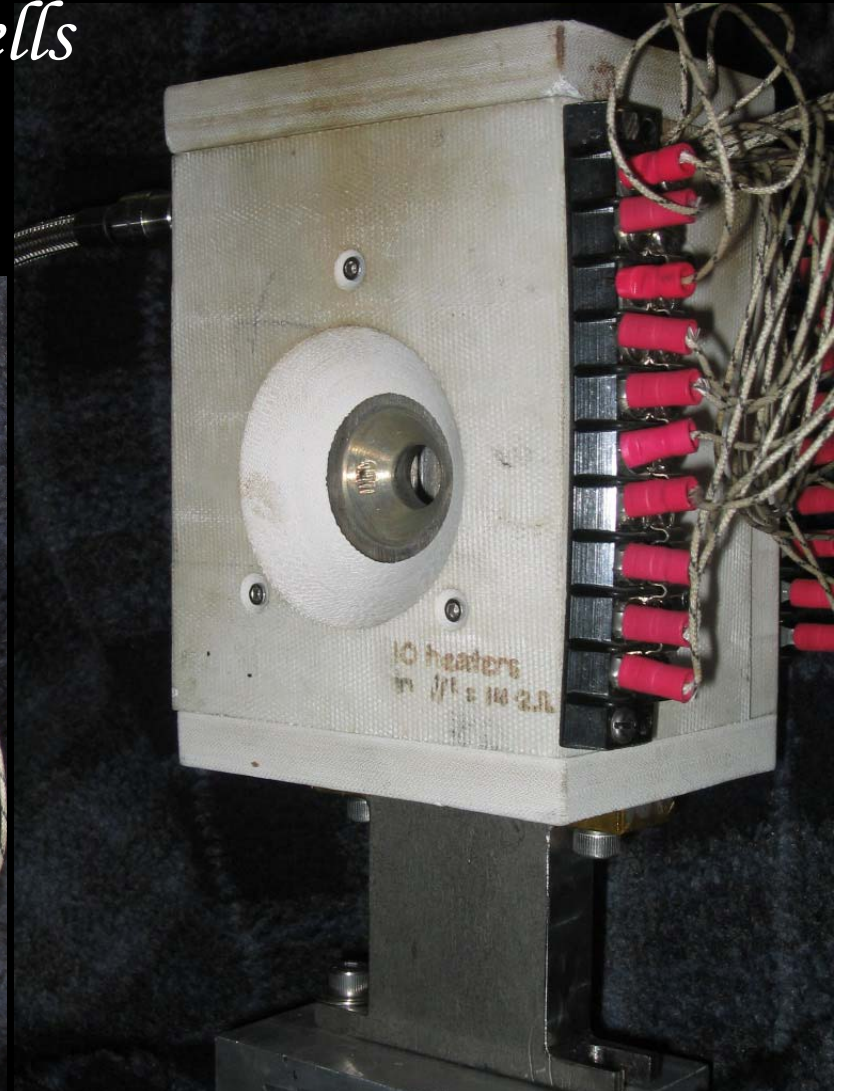
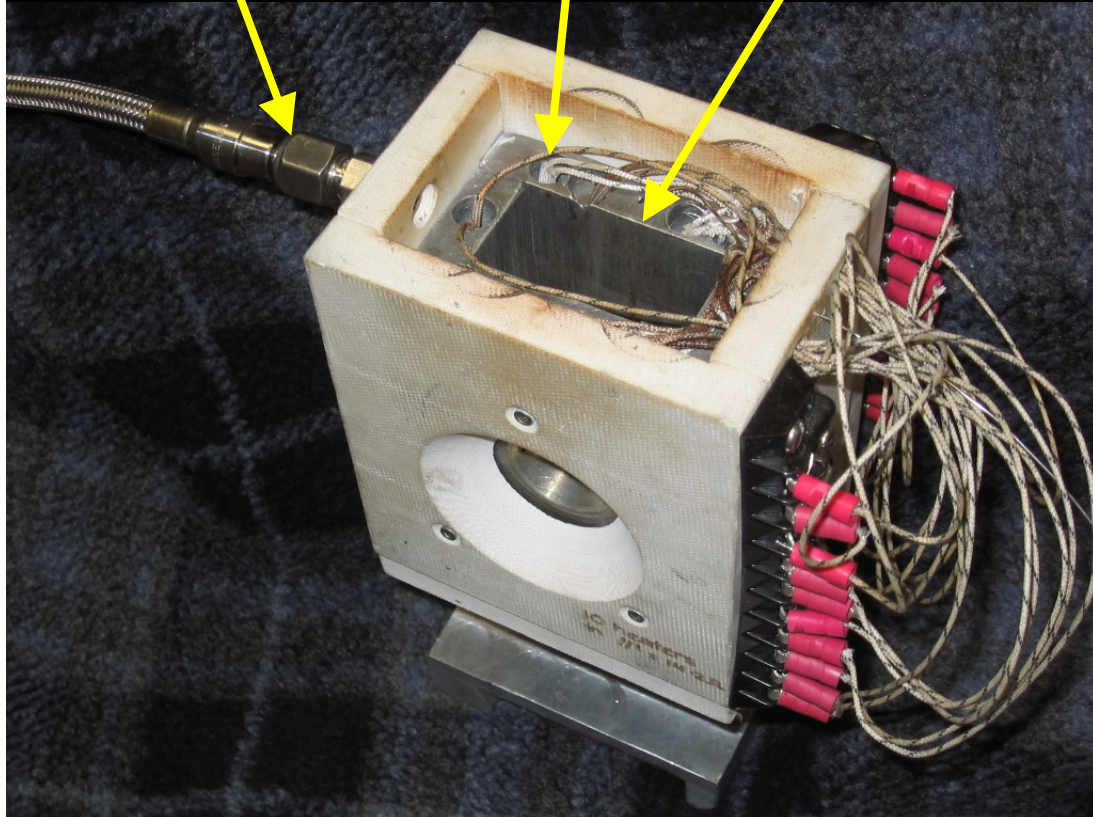
*Temp T:  $25^{\circ}\text{C} < T < 450^{\circ}\text{C}$*

*stability  $\pm 2^{\circ}\text{C}$*

*Feed for inert gas*

*Fit for fluid  
holder cells*

*10 soldering iron  
core heaters*



## *Sample Environments: Oven*

*Fluid holder cells: assemble as three parts with windows*

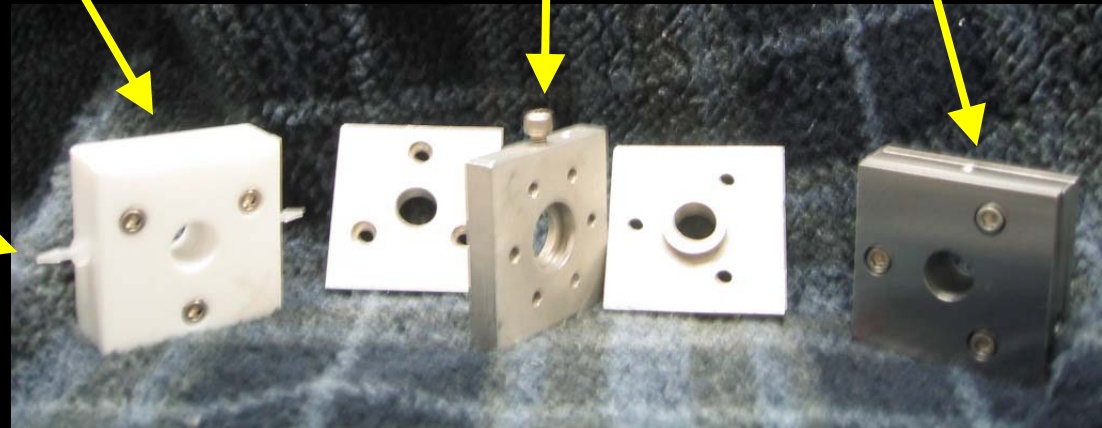
*Sample volume ~ 2.5 cc*

*Optical path length = 1 mm*

*Material: 5 each of*

*Polytetrafluoroethylene (Teflon); Aluminum & Steel*

*Teflon cells  
have flow  
couplings  
for in-situ  
titration*



## *Sample Environments: Tensiometer*

*Extension rate  $\dot{E}$ :*

$$0.001 \text{ mm s}^{-1} < \dot{E} < 25 \text{ mm s}^{-1}$$

*Oven Temp  $T$ :  $25^\circ\text{C} < T < 100^\circ\text{C}$*

*Temp stability  $\pm 2^\circ\text{C}$*

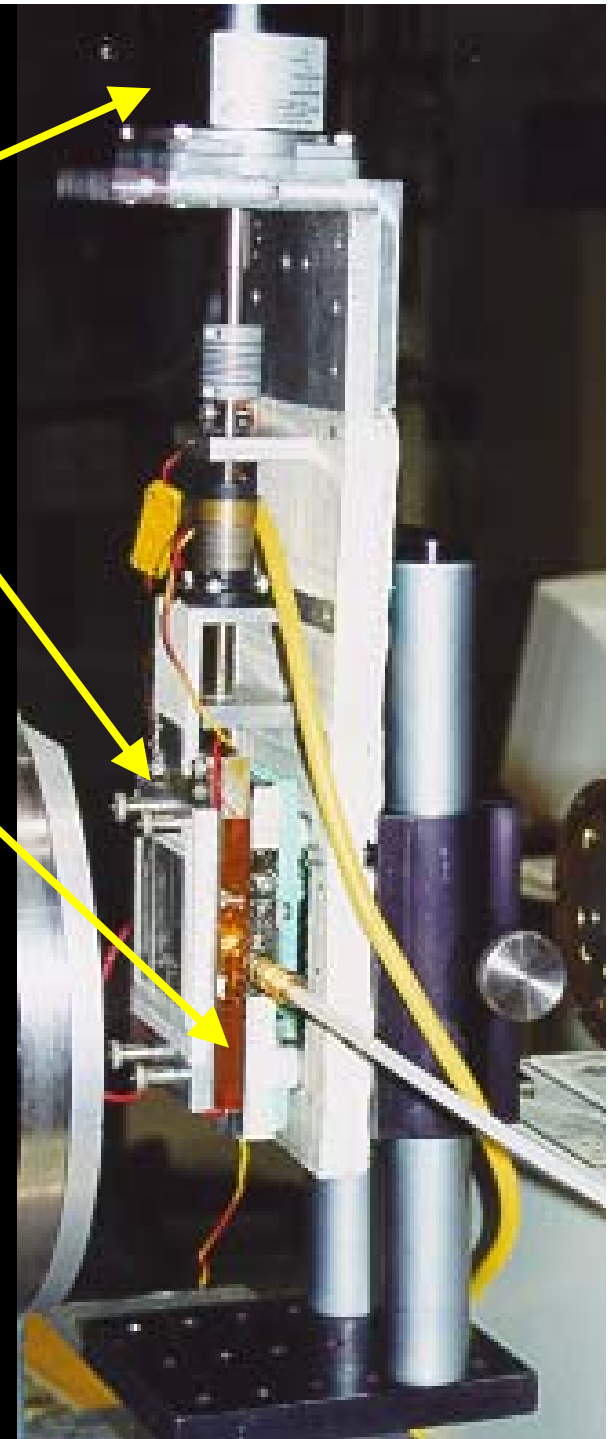
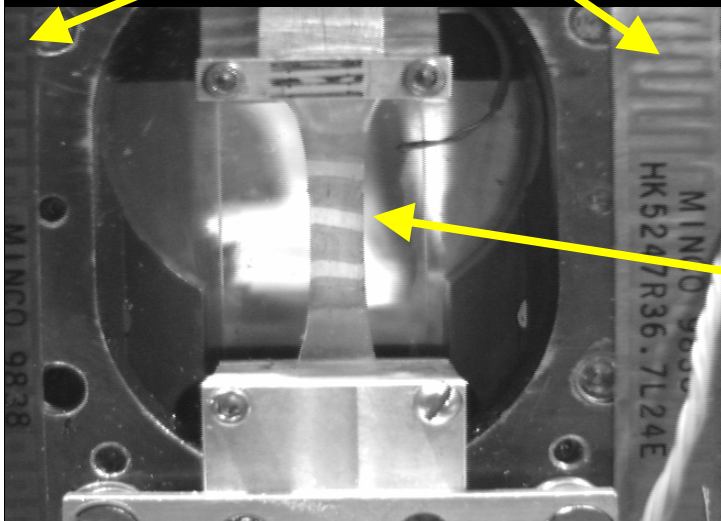
*Internal heater tapes*

*Drive motor*

*Oven*

*External  
heater tape*

*Elastomeric  
Polypropylene  
sample at  
300% extension*

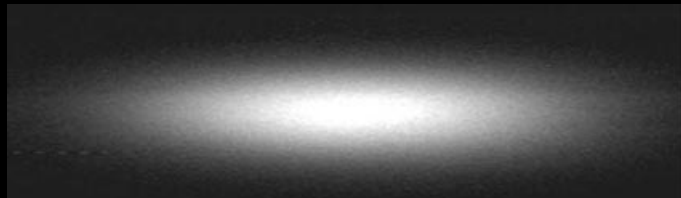


## *Principal Parameters for Scattering Experiments*

$q_{\min}$ :  $0.03 \text{ nm}^{-1}$  (c.f. pre 2004  $q_{\min} = 0.07 \text{ nm}^{-1}$ )

Can observe features  $d_{\max} \sim 200 \text{ nm}$  (c.f. pre-2004  $d_{\max} = 90 \text{ nm}$ )

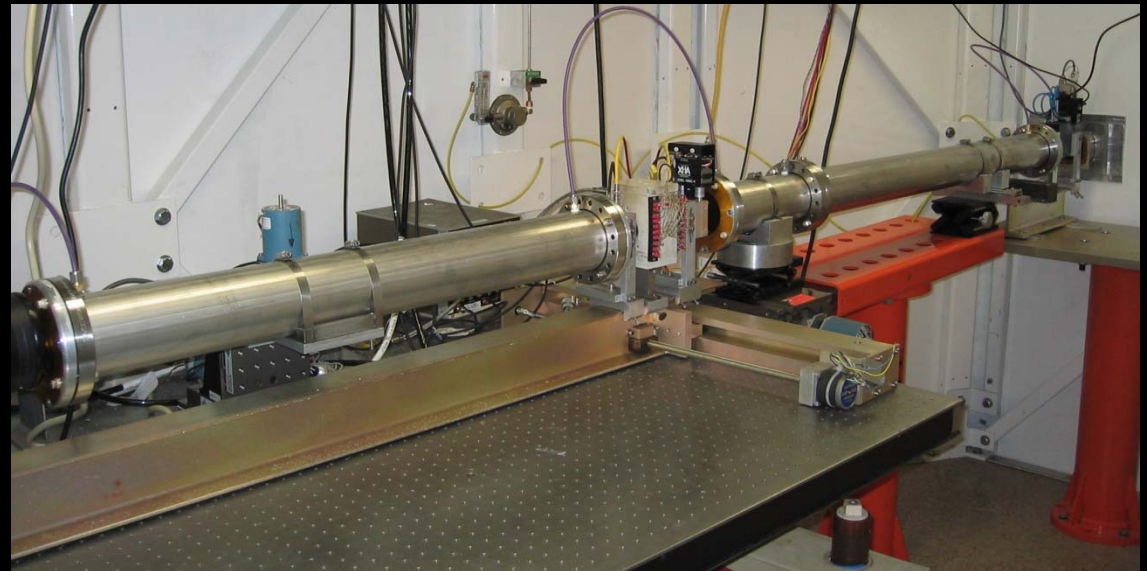
Focused Flux  $\Phi \sim 1 \times 10^{10} \text{ h}\nu \text{ s}^{-1} \text{ mA}^{-1}$



*pre 2004 source size*



*Current source size*



*Source size = 18 nm/rad*  
(c.f. pre 2004 = 130 nm/rad)

*Sample to detector distance*  
 $\mathcal{D} = 3 \text{ m}$  (c.f. pre 2004  $\mathcal{D} = 1.2 \text{ m}$ )