## GCSE MATHEMATICS



# Y10 Higher Home Learning Pack

Name:			
Class: _	 	 	

Teacher: \_\_\_\_\_

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## Edexcel GCSE Practice Exam Papers

1H - Non Calculator paper, 2H – Calculator paper, 3H – Calculator Paper

## Useful websites to use at home:

- Mathswatch
- Onmaths
- GCSE Pod
- Genie Maths
- Mr Barton Maths
- www.methodmaths.com
- www.hegartymaths.com
- www.bbc.co.uk/schools/gcsebitesize

## Number Unit Standard Form

#### Things to remember: • a x 10<sup>b</sup>

- **a** x 10<sup>b</sup>  $1 \le a < 10$
- A floppy disk can store 1 440 000 bytes of data.
   (a) Write the number 1 440 000 in standard form.

	A har (b)		can store 2.4 $\times$ 10 <sup>9</sup> bytes of data. ulate the number of floppy disks needed to stor	(1) re the 2.4 $\times$ 10 <sup>9</sup> bytes of data.
				(3) (Total 4 marks)
2.	A nar (a)		ond is 0.000 000 001 second. e the number 0.000 000 001 in standard form.	
	A cor (b)	How	does a calculation in 5 nanoseconds. many of these calculations can the computer of your answer in standard form.	(1) to in 1 second?
				(2) (Total 3 marks)
3.	(a)	(i)	Write 40 000 000 in standard form.	
		(ii)	Write 3 x $10^{-5}$ as an ordinary number.	
	(b)	3 x 1	k out the value of 0 <sup>-5</sup> x 40 000 000 your answer in standard form.	(2)

(2) (Total 4 marks) 4. Work out  $(3.2 \times 10^5) \times (4.5 \times 10^4)$ Give your answer in standard form correct to 2 significant figures.

			(Total 2 marks)
5.	(a)	Write the number 40 000 000 in standard form.	
	(b)	Write 1.4 × 10 <sup>-5</sup> as an ordinary number.	(1)
	(c)	Work out (5 $\times$ 10 <sup>4</sup> ) $\times$ (6 $\times$ 10 <sup>9</sup> ) Give your answer in standard form.	(1)
6.	Write	in standard form	(2) (Total 4 marks)
0.	(a)	456 000	
	(b)	0.00034	(1)
	(C)	16 × 10 <sup>7</sup>	(1)
			(1) (Total 3 marks)
7.	(a)	Write 5.7× $10^{-4}$ as an ordinary number.	
(b)		out the value of $(7 \times 10^4) \times (3 \times 10^5)$ our answer in standard form.	(1)

(2)

(Total 3 marks)	e 30 000 000 in standard form.	(a)	8.
(1)	te 2 × 10 <sup>-3</sup> as an ordinary number.	(b)	
(1) (Total 2 marks)			
	Write 7900 in standard form.	(a)	9.
	Write 0. 00035 in standard form.		
(2)	k out $\frac{4 \times 10^3}{8 \times 10^{-5}}$ e your answer in standard form.		

	(2)
(Tota	l 4 marks)

10. Work out

 $2 \times 2.2 \times 10^{12} \times 1.5 \times 10^{12}$ 

 $2.2 \times 10^{12} - 1.5 \times 10^{12}$ 

Give your answer in standard form correct to 3 significant figures.

			(Total 3 marks)
11.	(a)	Write 6.4 × $10^4$ as an ordinary number.	
	(b)	Write 0.0039 in standard form.	(1)
	(c)	Write 0.25 × $10^7$ in standard form.	(1)

(1) (Total 3 marks)

## Laws of Indices

#### Things to remember:

$a^m \times a^n = a^{m+n}$	$a^{-n} = \frac{1}{a^n}$
$a^m \div a^n = a^{m-n}$	$(a^m)^n = a^{mn}$
$a^{0} = 1$	$a^{\frac{m}{n}} = \sqrt[n]{a^m}$

#### Questions:

**1.** (a) Simplify  $m^5 \div m^3$ 

(1)		,	plify $5x^4y^3 \times x^2y$	(b) Simp	
(2) (Total for Question is 3 marks)					
			e numbers in or he smallest nun		2.
	5°	-5	0.5	5-1	
(Total for Question is 2 marks)		25 <sup>2</sup> / <sub>3</sub>	n the value of 12	 Write down	3.
(Total for question is 1 mark)		ue of 10 <sup>-1</sup>	e down the valu	(a) Write	4.

(b) Find the value of  $27^{\frac{2}{3}}$ 

(2) (Total for Question is 3 marks)

(1)

5.	(a)	Find the value of	5°	
				(1)
	(b)	Find the value of	27 <sup>1/</sup> 3	
				(1)
	(c)	Find the value of	2 <sup>-3</sup>	
				(1)
				(Total for Question is 3 marks)
6.	(a)	Write down the valu	ue of $27^{1/3}$	
				(1)
	(b)	Find the value of 2	$7^{-1/3}$	
				(2) (Total for Question is 3 marks)
7.	(a)	Write down the valu	ue of $64^{\frac{1}{2}}$	
			2	(1)
		Find the value of $\left(\frac{1}{1}\right)$	$\left(\frac{8}{125}\right)^{-\frac{2}{3}}$	
	(b)	Find the value of $\Box$	125)	
				(2)
				(Total for question = 3 marks)
8.	(a)	Write down the valu	ue of 6 <sup>0</sup>	
		2		(1)
	(b)	Work out $64^{-\frac{2}{3}}$		

(2) (Total for question = 3 marks)

## **Calculating with Fractions**

#### Things to remember:

- If you have a mixed number, start by converting it to an improper fraction.
- Multiply fractions is easy just multiply the numerators and multiply the denominators.
- To divide fractions, flip the second fraction upside-down and multiply instead.
- If you need to add or subtract fractions, you will need to start by finding equivalent fractions with a common denominator.
- Make sure you leave your answer in its simplest form.
- To convert a recurring decimal to a fraction you will need to multiply by 10<sup>n</sup>, where n is the number of recurring digits. Then subtract the original number from the new one. Rearrange to find the fraction.

#### **Questions:**

**1.** (a) Work out  $1\frac{3}{4} + 3\frac{1}{2}$ 

(b) Work out  $\frac{3}{7} \times \pounds 28$ 

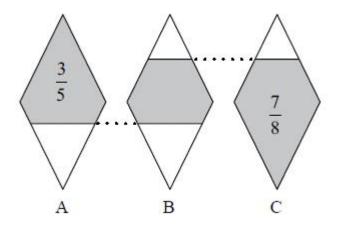
£.....(2)

(Total for question = 4 marks)

2. Work out  $3\frac{4}{5} + \frac{3}{7}$ Give your answer as a mixed number in its simplest form.

(Total for question = 3 marks)

**3.** The diagram shows three identical shapes A, B and C.  $\frac{3}{5}$  of shape A is shaded.  $\frac{7}{8}$  of shape C is shaded.



What fraction of shape B is shaded?

(Total for question = 3 marks)

4. Express the recurring decimal 0.15 as a fraction. Give your answer in its simplest form.

(Total for Question is 3 marks)

5. Work out  $3\frac{1}{3} \times 4\frac{2}{5}$ Give your answer as a mixed number in its simplest form.

(Total for question = 3 marks)

6. Work out  $\frac{3}{8} + \frac{1}{3}$ 

(Total for Question is 2 marks)

**7.** Express the recurring decimal 0.750 as a fraction.

(Total for Question is 3 marks)

**8.** Express the recurring decimal 0.281 as a fraction in its simplest form.

(Total for Question is 3 marks)

**9.** Work out  $3\frac{1}{3} \div 4\frac{3}{4}$ 

(Total for Question is 2 marks)

**10.** On a farm,  $4\frac{1}{2}$  out of every 15 acres of the land are used to grow crops. Wheat is grown on  $\frac{5}{8}$  of the land used to grow crops. What percentage of the total area of the land on the farm is used to grow wheat?

(Total for question = 3 marks)

## Percentages – compound interest

Things to remember:
<ul> <li>New amount = original amount x multiplier<sup>n</sup></li> <li>Number of years</li> </ul>
<ul> <li>Questions:</li> <li>1. Henry invests £4500 at a compound interest rate of 5% per annum. At the end of <i>n</i> complete years the investment has grown to £5469.78. Find the value of <i>n</i>.</li> </ul>
(Total 2 marks
<ul> <li>2. Bill buys a new machine. The value of the machine depreciates by 20% each year.</li> <li>(a) Bill says 'after 5 years the machine will have no value'. Bill is wrong. Explain why.</li> </ul>
(1) Bill wants to work out the value of the machine after 2 years. (b) By what single decimal number should Bill multiply the value of the machine when new?
(2 (Total 3 marks)
3. Gwen bought a new car. Each year, the value of her car depreciated by 9%. Calculate the number of years after which the value of her car was 47% of its value when new.
<ul> <li>4. The value of a car depreciates by 35% each year. At the end of 2007 the value of the car was £5460 Work out the value of the car at the end of 2006</li> </ul>
£(Total 3 marks

- Toby invested £4500 for 2 years in a savings account.
   He was paid 4% per annum compound interest.
   Hew much did Taby bays in his savings account after 2 years?
  - (a) How much did Toby have in his savings account after 2 years?

£ .....(3)

Jaspir invested £2400 for *n* years in a savings account. He was paid 7.5% per annum compound interest. At the end of the *n* years he had £3445.51 in the savings account. (a) Work out the value of *n*.

> (2) (Total 5 marks)

6. Mario invests £2000 for 3 years at 5% per annum **compound** interest. Calculate the value of the investment at the end of 3 years.

£ .....

(Total 3 marks)

Toby invested £4500 for 2 years in a savings account.
 He was paid 4% per annum compound interest.
 How much did Toby have in his savings account after 2 years?

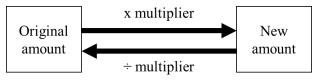
£.....

(Total 3 marks)

#### Percentages – reverse

#### Things to remember:

• Work out what the multiplier would have been;



#### **Questions:**

Loft insulation reduces annual heating costs by 20%.
 After he insulated his loft, Curtley's annual heating cost was £520.
 Work out Curtley's annual heating cost would have been, if he had not insulated his loft.

		£	
		~	(Total 3 marks)
2.	Andre The s	ale, normal prices are reduced by 20%. SALE 20% OFF we bought a saddle for his horse in the sale. ale price of the saddle was £220. late the normal price of the saddle.	
3.	This is	£ 's weekly pay this year is £240 s 20% more than her weekly pay last year.	(Total 3 marks)
	Bill is	ays 'This means Hajra's weekly pay last year was £192'. wrong,	
	(a)	Explain why.	
	(b)	Work out Hajra's weekly pay last year.	

£ .....

(2) (Total 3 marks)

- The price of all rail season tickets to London increased by 4%. 4.
  - The price of a rail season ticket from Cambridge to London increased by £121.60 (a) Work out the price before this increase.

£ .....

(b) After the increase, the price of a rail season ticket from Brighton to London was £2828.80

Work out the price before this increase.

£ ..... (3)

5. In a sale, normal prices are reduced by 25%. The sale price of a saw is £12.75 Calculate the normal price of the saw.

£ .....

(Total 3 marks)

(Total 5 marks)

(2)

6. In a sale, normal prices are reduced by 12%. The sale price of a DVD player is £242. Work out the normal price of the DVD player.

£ .....

(Total 3 marks)

7. A garage sells cars. It offers a discount of 20% off the normal price for cash. Dave pays £5200 cash for a car. Calculate the normal price of the car.

£ .....

(Total 3 marks)

## **Estimating Calculations**

#### Things to remember:

- Round each number to one significant figure first (e.g. nearest whole number, nearest ten, nearest one decimal place) – this earns you one mark.
- Don't forget to use the correct order of operations.

#### **Questions:**

1. Work out an estimate for  $\frac{3.1 \times 9.87}{0.509}$ 

(Total for Question is 3 marks)

2. Margaret has some goats. The goats produce an average total of 21.7 litres of milk per day for 280 days. Margaret sells the milk in ½ litre bottles. Work out an estimate for the total number of bottles that Margaret will be able to fill with the milk. You must show clearly how you got your estimate.

(Total for Question is 3 marks)

3. Work out an estimate for the value of  $\frac{89.3 \times 0.51}{4.8}$ 

(Total for Question is 2 marks)

## **Bounds**

#### Things to remember:

• Calculating bounds is the opposite of rounding – they are the limits at which you would round up instead of down, and vice versa.

#### **Questions:**

- **1.** A piece of wood has a length of 65 centimetres to the nearest centimetre.
  - (a) What is the least possible length of the piece of wood?

	(b)	What is the greatest possible length of the piece	of wood?
	()		
			(1) (Total for Question is 2 marks)
2.	Chel (a)	sea's height is 168 cm to the nearest cm. What is Chelsea's minimum possible height?	
	(b)	 What is Chelsea's maximum possible height?	cm (1)
			cm (1) (Total for Question is 2 marks)
3.	Each	ne has 60 golf balls. To of these golf balls weighs 42 grams to the nearest	•

Work out the greatest possible total weight of all 60 golf balls. Give your answer in kilograms.

(Total for Question is 3 marks)

**4.** The length, *L* cm, of a line is measured as 13 cm correct to the nearest centimetre. Complete the following statement to show the range of possible values of *L* 

#### <u>Surds</u>

#### Things to remember:

- $\sqrt{10}$  means square root;
- To simplify surds, find all its factors;
- To rationalise the denominator, find an equivalent fraction where the denominator is rational.

#### **Questions:**

1. Work out

$$\frac{(5+\sqrt{3})(5-\sqrt{3})}{\sqrt{3}}$$

 $\sqrt{22}$ 

Give your answer in its simplest form.

(Total 3 marks)

**2.** (a) Rationalise the denominator of 
$$\frac{1}{\sqrt{3}}$$

(1)

(b) Expand  $(2 + \sqrt{3})(1 + \sqrt{3})$ Give your answer in the form  $a + b\sqrt{3}$  where *a* and *b* are integers.

> (2) (Total 3 marks)

## Algebra Unit Expand and Factorise Quadratics

#### Things to remember:

- Use FOIL (first, outside, inside, last) or the grid method (for multiplication) to expand brackets.
- For any quadratic ax<sup>2</sup> + bx + c = 0, find a pair of numbers with a sum of b and a product of ac to factorise.

#### **Questions:**

**1.** Expand and simplify (m + 7)(m + 3)

2. (a) Factorise 6 + 9x(b) Factorise  $y^2 - 16$ (c) Factorise  $2p^2 - p - 10$ (Total for question = 2 marks) (1) (1) (1)

> (2) (Total for Question is 4 marks)

.....

**3.** Solve, by factorising, the equation  $8x^2 - 30x - 27 = 0$ 

(Total for Question is 3 marks)

(Total for question is 2 marks)

5. Write  $x^2 + 2x - 8$  in the form  $(x + m)^2 + n$  where m and n are integers.

(Total for question is 2 marks) Expand 4(3x+5)6. (a) ..... (1) Expand and simplify 2(x-4) + 3(x+5)(b) ..... (2) Expand and simplify (x + 4)(x + 6)(C) ..... (2) (Total for Question is 5 marks) Factorise  $x^2 + 5x + 4$ 7. (a) ..... (2) Expand and simplify (3x-1)(2x+5)(b)

(2)

8.	(a)	Ехра	nd 3(2 + <i>t</i> )		(Total for Question is 4 marks)
	(b)	Expa	nd 3 <i>x</i> (2 <i>x</i> + 9	5)	(1)
	(c)	Expa	nd and simpli	fy ( <i>m</i> + 3)( <i>m</i> + 10)	(2)
		E. (		2. –	(2) (Total for Question is 5 marks)
9.	(a)	Facto	orise	<i>x</i> <sup>2</sup> + 7 <i>x</i>	
	(b)	Facto	orise	<i>y</i> <sup>2</sup> – 10 <i>y</i> + 16	(1)
	*(c)	(i)	Factorise	$2t^2 + 5t + 2$	(2)
		(ii)	<i>t</i> is a positiv The express Explain why	e whole number. sion $2t^2 + 5t + 2$ can nev	ver have a value that is a prime number.
					(3) (Total for Question is 6 marks)

## Algebraic Fractions – Simplifying

#### Things to remember:

- Factorise the numerator and denominator;
- Cancel common factors;
- Then add/subtract/multiply divide if necessary.

#### **Questions:**

1. Simplify

plify  $\frac{p^2-9}{2p+6}$ 

	(Total	3 marks)

**2.** Simplify fully  $\frac{6x^2 + 3x}{4x^2 - 1}$ 

(Total 3 marks)

3. Simplify  $\frac{x^2+2x+1}{x^2+3x+2}$ 

(Total 3 marks)

4. Simplify fully 
$$\frac{x^2 + x - 6}{x^2 - 7x + 10}$$

(Total 3 marks)

5. Simplify fully  $\frac{x^2 - 8x + 15}{2x^2 - 7x - 15}$ 

(Total 3 marks)

6. Simplify fully 
$$\frac{2x^2+3x+1}{x^2-3x-4}$$

(Total 3 marks)

### **Solving Quadratic Inequalities**

#### Things to remember:

• Start by solving the quadratic to find the values of x, then sketch the graph to determine the inequality.

#### Questions:

**1.** Solve  $x^2 > 3x + 4$ 

\_\_\_\_\_

## (Total for question = 3 marks)

**2.** Solve the inequality  $x^2 > 3(x+6)$ 

(Total for question = 4 marks)

**3.** Solve the inequality  $x^2 + 5x > 6$ 

#### **Rearranging Formulae**

#### Things to remember:

- Firstly decide what needs to be on its own.
- Secondly move all terms that contain that letter to one side. Remember to move all terms if it appears in more than one.
- Thirdly separate out the required letter on its own.

#### **Questions:**

1. Make *u* the subject of the formula

 $D = ut + kt^2$ 

u = .....(Total 2 marks)

**2.** (a) Solve 4(x+3) = 6

x = .....(3)

(b) Make *t* the subject of the formula v = u + 5t

*t* = .....(2) (Total 5 marks)

3. (a) Expand and simplify  $(x - y)^2$ 

(b) Rearrange a(q - c) = d to make q the subject. (2)

*q* = .....(3)

4. Make x the subject of 5(x-3) = y(4-3x)

x = .....(Total 4 marks)

$$P = \frac{n^2 + a}{n + a}$$

5.

6.

Rearrange the formula to make *a* the subject.

a =.....(Total 4 marks)

$$\frac{x}{x+c} = \frac{p}{q}$$

Make x the subject of the formula.

x=....(Total 4 marks)

## Linear Simultaneous Equations

#### Things to remember:

- 1. Scale up (if necessary)
- 2. Add or subtract (to eliminate)
- 3. Solve (to find x)
- 4. Substitute (to find y) (or the other way around)

#### **Questions:**

- \*1. The Singh family and the Peterson family go to the cinema. The Singh family buy 2 adult tickets and 3 child tickets. They pay £28.20 for the tickets. The Peterson family buy 3 adult tickets and 5 child tickets.
  - They pay £44.75 for the tickets.

Find the cost of each adult ticket and each child ticket.

(Total for question = 5 marks)

- 2. Solve the simultaneous equations
  - 3x + 4y = 52x 3y = 9

x = .....
y = ....
(Total for Question is 4 marks)

Solve the simultaneous equations 3. 4x + 7y = 13x + 10y = 15

*x* = .....

*y* = ..... (Total for Question is 4 marks)

4.

Solve  $2x + 3y = \frac{2}{3}$ 3x - 4y = 18

> *x* = ..... *y* = ..... (Total for Question is 4 marks)

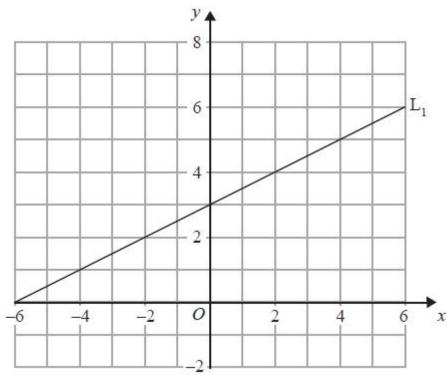
## Parallel and Perpendicular Graphs

#### Things to remember:

- The general equation of a linear graph is given by y = mx + c, where m is the gradient and c is the y-intercept.
- Parallel graphs have the same gradient.
- Gradients of perpendicular graphs have a product of -1.

#### **Questions:**

**1.** The diagram shows a straight line, L<sub>1</sub>, drawn on a grid.



A straight line,  $L_2$ , is parallel to the straight line  $L_1$  and passes through the point (0, -5). Find an equation of the straight line  $L_2$ .

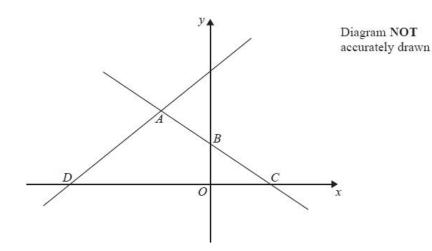
(Total for Question is 3 marks)

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2. The straight line L has equation y = 2x - 5Find an equation of the straight line perpendicular to L which passes through (-2, 3).

(Total for Question is 3 marks)

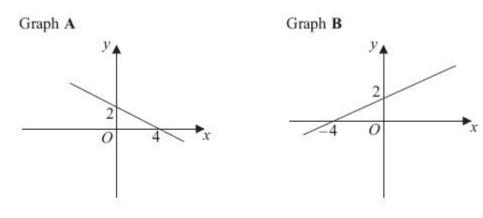
3. In the diagram, *ABC* is the line with equation  $y = -\frac{1}{2}x + 5$  *AB* = *BC D* is the point with coordinates (-13, 0)

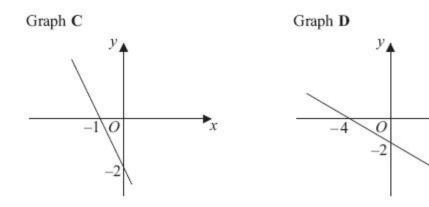


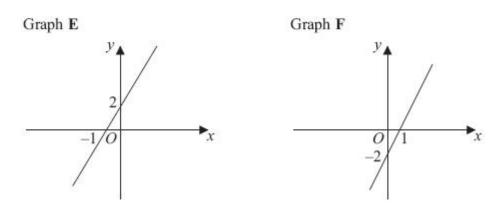
Find an equation of the line through A and D.

(Total for question = 5 marks)

4. Here are the graphs of 6 straight lines.







Match each of the graphs A, B, C, D, E and F to the equations in the table.

Equation	$y = \frac{1}{2}x + 2$	y = 2x - 2	$y = -\frac{1}{2}x + 2$	y = -2x - 2	y = 2x + 2	$y = -\frac{1}{2}x - 2$
Graph						

#### (Total for Question is 3 marks)

x

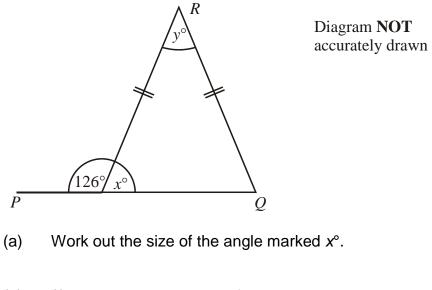
#### Shape Unit Angles in parallel lines and polygons

#### Things to remember:

- Angles in a triangle sum to 180°
- Angles on a straight line sum to 180°
- Angles around a point sum to 360°
- Vertically opposite angles are equal
- Alternate angles are equal
- Corresponding angles are equal
- Supplementary angles sum to 180°
- An exterior and an interior angle of a polygon sum to 180°
- An exterior angle = 360° ÷ number of sides

#### **Questions:**

**1.** *P*Q is a straight line.



(b) (i) Work out the size of the angle marked  $y^{\circ}$ .

(ii) Give reasons for your answer.

.....

(3) (Total 4 marks)

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(1)

2. Triangle ABC is isosceles, with AC = BC. Angle  $ACD = 62^{\circ}$ . BCD is a straight line.

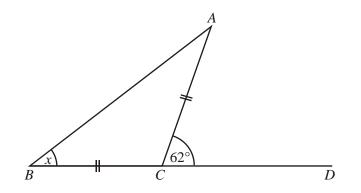
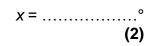


Diagram **NOT** accurately drawn

(a) Work out the size of angle *x*.



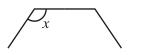
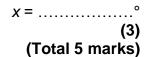
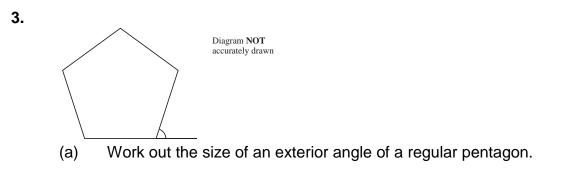


Diagram **NOT** accurately drawn

The diagram shows part of a **regular** octagon.(b) Work out the size of angle *x*.





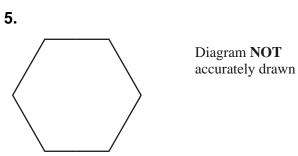
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## ABCD is a quadrilateral. A $100^{\circ}$ $2x^{\circ}$ $x^{\circ}$ $x^{\circ}$

4.

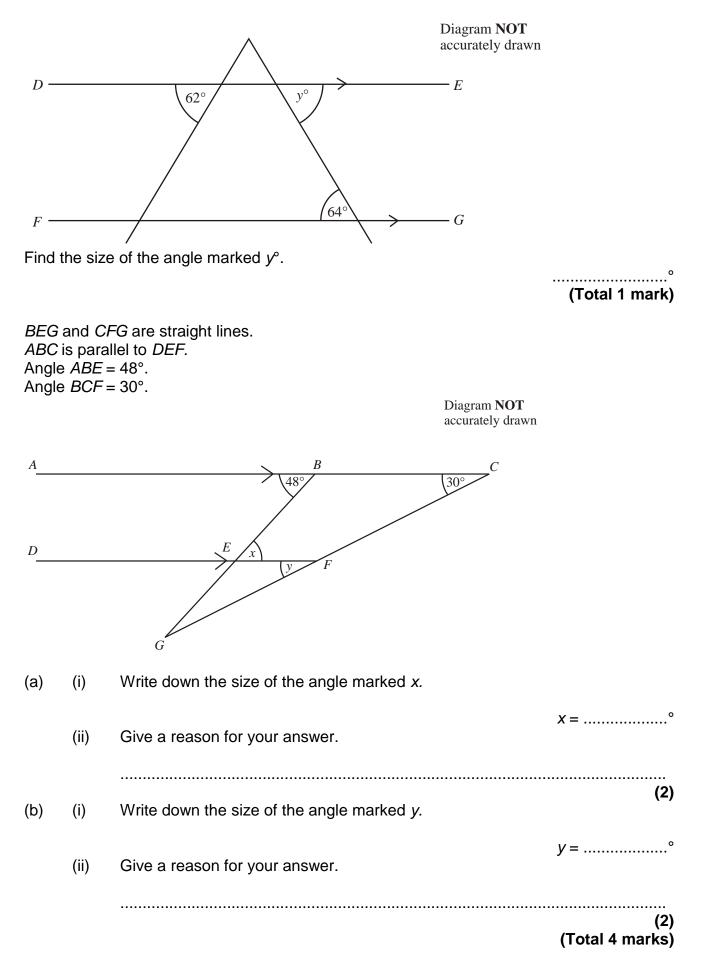
Work out the size of the largest angle in the quadrilateral.

(Total 4 marks)



Calculate the size of the exterior angle of a regular hexagon.

°..... (Total 2 marks) 7.



## Pythagoras' Theorem

#### Things to remember:

- $a^2 + b^2 = c^2$
- First you've got to square both sides of the triangle.
- Then decide whether to add or subtract.
- Finish off with a square root.
- Make sure you round your answer correctly.

#### **Questions:**

1.

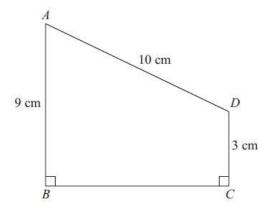
2.

ABCD is a trapezium. Diagram NOT accurately drawn AD = 10 cm AB = 9 cm DC = 3 cmAngle ABC = angle BCD = 90° Calculate the length of AC. Give your answer correct to 3 significant figures.

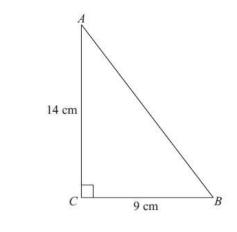
Diagram NOT accurately drawn

Give your answer correct to 1 decimal place.

Calculate the length of AB.

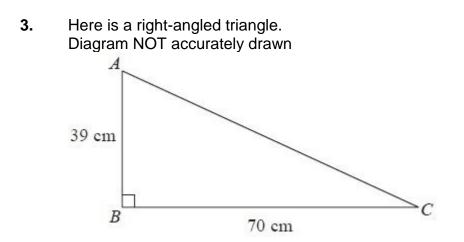


#### ..... cm (Total for Question is 5 marks)

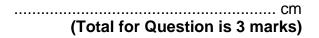


..... cm (Total for Question is 3 marks)

36



Work out the length of *AC*. Give your answer correct to 1 decimal place.



4. ABC is a right-angled triangle. AC = 6 cmAB = 13 cm

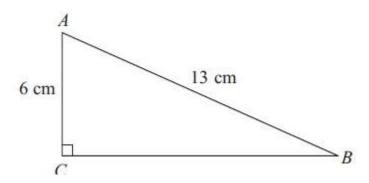


Diagram NOT accurately drawn

Work out the length of *BC*. Give your answer correct to 3 significant figures.

(Total for Question is 3 marks)