THE BIG
IDEA

You can describe the motion of an object by its position, speed, direction, and acceleration.

4.1 Motion Is Relative

An object is moving if its position relative to a fixed point is changing.

4.1 Motion Is Relative

Even things that appear to be at rest move.

When we describe the motion of one object with respect to another, we say that the object is moving **relative** to the other object.

- A book that is at rest, relative to the table it lies on, is moving at about 30 kilometers per second relative to the sun.

- The book moves even faster relative to the center of our galaxy.

4.1 Motion Is Relative

The racing cars in the Indy 500 move relative to the track.

4.1 Motion Is Relative

When we discuss the motion of something, we describe its motion relative to something else.

- The space shuttle moves at 8 kilometers per second relative to Earth below.

- A racing car in the Indy 500 reaches a speed of 300 kilometers per hour relative to the track.

- Unless stated otherwise, the speeds of things in our environment are measured relative to the surface of Earth.

4.1 Motion Is Relative

Although you may be at rest relative to Earth's surface, you're moving about 100,000 km/h relative to the sun.
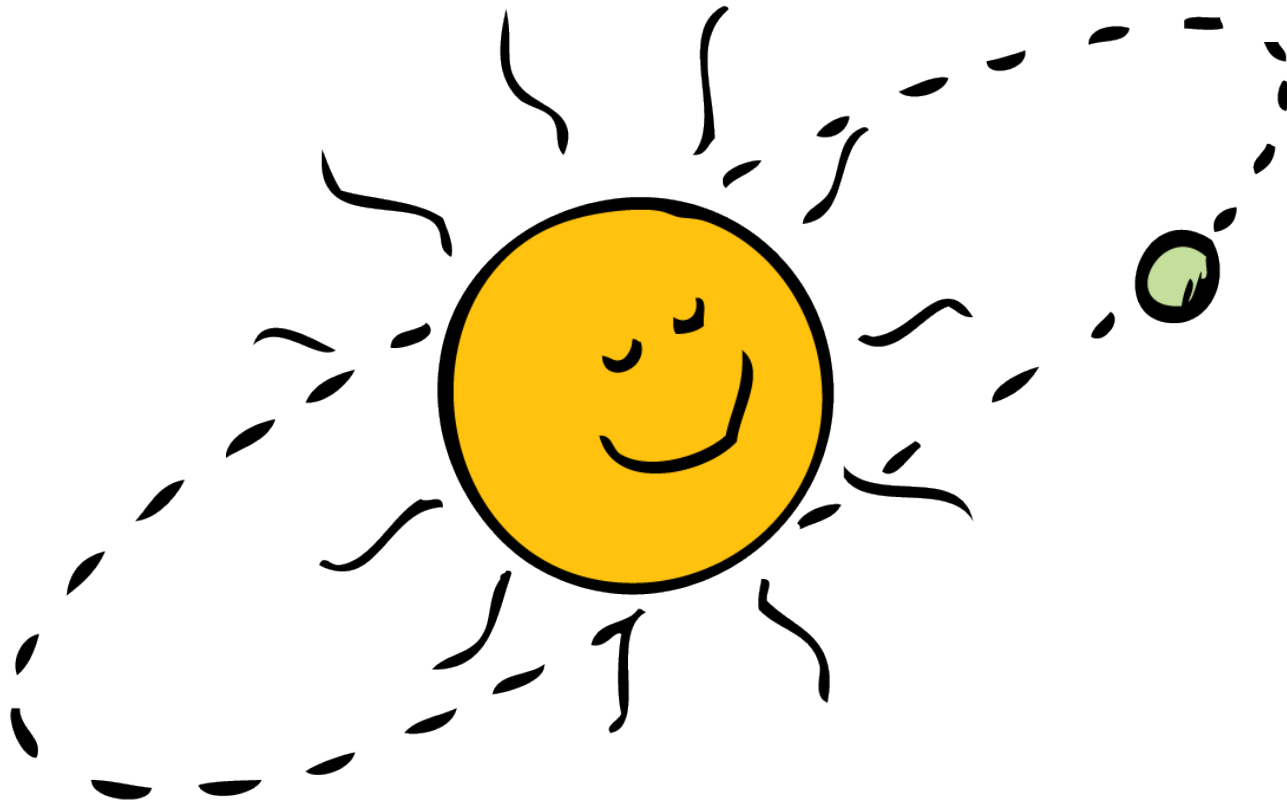
4.1 Motion Is Relative

think!

A hungry mosquito sees you resting in a hammock in a 3-meters-per-second breeze. How fast and in what direction should the mosquito fly in order to hover above you for lunch?

4.1 Motion Is Relative

think!

A hungry mosquito sees you resting in a hammock in a 3-meters-per-second breeze. How fast and in what direction should the mosquito fly in order to hover above you for lunch?

Answer: The mosquito should fly toward you into the breeze. When above you it should fly at 3 meters per second in order to hover at rest above you.

4.1 Motion Is Relative

CONCEPT CHECK **How can you tell if an object is moving?**

4.2 Speed

You can calculate the speed of an object by dividing the distance covered by time.

4.2 Speed

Before the time of Galileo, people described moving things as simply "slow" or "fast." Such descriptions were vague.

Galileo is credited as being the first to measure *speed* by considering the distance covered and the time it takes.

Speed is how fast an object is moving.

$$\text{Speed} = \frac{\text{distance}}{\text{time}}$$

4.2 Speed

Any combination of units for distance and time that are useful and convenient are legitimate for describing speed:

- miles per hour (mi/h)
- kilometers per hour (km/h)
- centimeters per day
- light-years per century

4.2 Speed

A cheetah is the fastest land animal over distances less than 500 meters and can achieve peak speeds of 100 km/h.

4.2 Speed

We will primarily use the unit *meters per second* (m/s) for speed.

If a cheetah covers 50 meters in a time of 2 seconds, its speed is 25 m/s.

4.2 Speed

Table 4.1	Approximate Speeds in Different Units		
12 mi/h =	20 km/h =	6 m/s	(bowling ball)
25 mi/h =	40 km/h =	11 m/s	(very good sprinter)
37 mi/h =	60 km/h =	17 m/s	(sprinting rabbit)
50 mi/h =	80 km/h =	22 m/s	(tsunami)
62 mi/h =	100 km/h =	28 m/s	(sprinting cheetah)
75 mi/h =	120 km/h =	33 m/s	(batted softball)
100 mi/h =	160 km/h =	44 m/s	(batted baseball)

4.2 Speed

Instantaneous Speed

A car does not always move at the same speed.

You can tell the speed of the car at any instant by looking at the car's speedometer.

The speed at any instant is called the **instantaneous speed.**

4.2 Speed

The speedometer gives readings of instantaneous speed in both mi/h and km/h.

4.2 Speed

Average Speed

In a trip by car, the car will certainly not travel at the same speed all during the trip.

The driver cares about the *average speed* for the trip as a whole.

The **average speed** is the total distance covered divided by the time.

4.2 Speed

Average speed can be calculated easily:

$$\text{average speed} = \frac{\text{total distance covered}}{\text{time interval}}$$

For example, a distance of 240 kilometers during a time of 4 hours is an average speed of 60 km/h:

$$\text{average speed} = \frac{\text{total distance covered}}{\text{time interval}} = \frac{240 \text{ km}}{4 \text{ h}} = 60 \text{ km/h}$$

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4.2 Speed

The average speed is often quite different from the instantaneous speed.

Whether we talk about average speed or instantaneous speed, we are talking about the rates at which distance is traveled.

4.2 Speed

If we know average speed and travel time, the distance traveled is easy to find.

total distance covered = average speed × travel time

For example, if your average speed is 80 kilometers per hour on a 4-hour trip, then you cover a total distance of 320 kilometers.

4.2 Speed

think!

If a cheetah can maintain a constant speed of 25 m/s, it will cover 25 meters every second. At this rate, how far will it travel in 10 seconds? In 1 minute?

4.2 Speed

think!

If a cheetah can maintain a constant speed of 25 m/s, it will cover 25 meters every second. At this rate, how far will it travel in 10 seconds? In 1 minute?

Answer: In 10 s the cheetah will cover 250 m, and in 1 min (or 60 s) it will cover 1500 m.

4.2 Speed

think!

The speedometer in every car also has an odometer that records the distance traveled. If the odometer reads zero at the beginning of a trip and 35 km a half hour later, what is the average speed?

4.2 Speed

think!

The speedometer in every car also has an odometer that records the distance traveled. If the odometer reads zero at the beginning of a trip and 35 km a half hour later, what is the average speed?

Answer:

$$\text{average speed} = \frac{\text{total distance covered}}{\text{time interval}} = \frac{35 \text{ km}}{0.5 \text{ h}} = 70 \text{ km/h}$$

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4.2 Speed

CONCEPT CHECK **How can you calculate speed?**
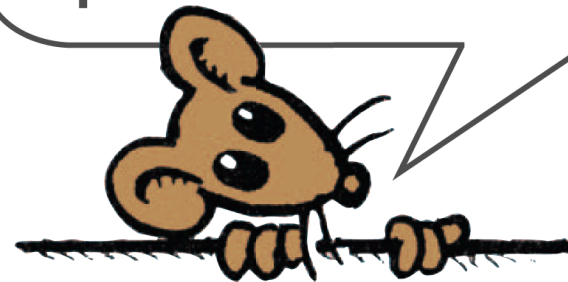
4.3 Velocity

Speed is a description of how fast an object moves; velocity is how fast and in what direction it moves.

4.3 Velocity

In physics, **velocity** is speed in a given direction.

- When we say a car travels at 60 km/h, we are specifying its speed.

- When we say a car moves at 60 km/h to the north, we are specifying its velocity.

Velocity is directed speed.

4.3 Velocity

A quantity such as velocity that specifies direction as well as magnitude is called a vector quantity.

- Speed is a scalar quantity.
- Velocity, like force, is a vector quantity.

4.3 Velocity

Constant Velocity

Constant speed means steady speed. Something with constant speed doesn't speed up or slow down.

Constant velocity means both constant speed *and* constant direction.

Constant direction is a straight line, so constant velocity means motion in a straight line at constant speed.
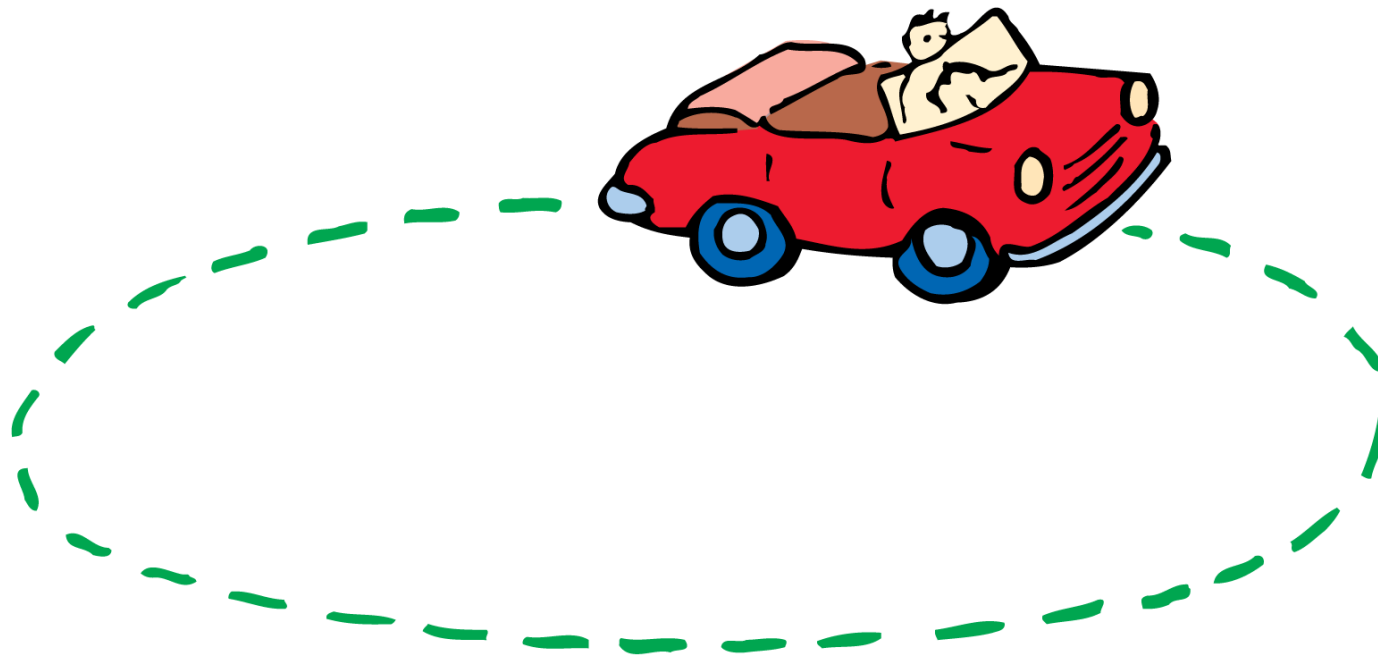
4.3 Velocity

Changing Velocity

If *either* the speed *or* the direction (or both) is changing, then the velocity is changing.

- Constant speed and constant velocity are not the same.

- A body may move at constant speed along a curved path but it does not move with constant velocity, because its direction is changing every instant.

4.3 Velocity

The car on the circular track may have a constant speed but not a constant velocity, because its direction of motion is changing every instant.

4.3 Velocity

think!

The speedometer of a car moving northward reads 60 km/h. It passes another car that travels southward at 60 km/h. Do both cars have the same speed? Do they have the same velocity?

4.3 Velocity

think!

The speedometer of a car moving northward reads 60 km/h. It passes another car that travels southward at 60 km/h. Do both cars have the same speed? Do they have the same velocity?

Answer: Both cars have the same speed, but they have opposite velocities because they are moving in opposite directions.

4.3 Velocity

CONCEPT CHECK

How is velocity different from speed?

4.4 Acceleration

You can calculate the acceleration of an object by dividing the change in its velocity by time.

4.4 Acceleration

We can change the state of motion of an object by changing its speed, its direction of motion, or both.

Acceleration is the rate at which the velocity is changing.

$$\text{acceleration} = \frac{\text{change of velocity}}{\text{time interval}}$$
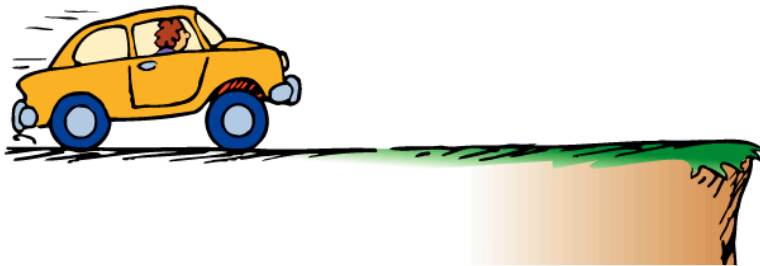
4.4 Acceleration

In physics, the term *acceleration* applies to decreases as well as increases in speed.

The brakes of a car can produce large retarding accelerations, that is, they can produce a large decrease per second in the speed. This is often called *deceleration.*

4.4 Acceleration

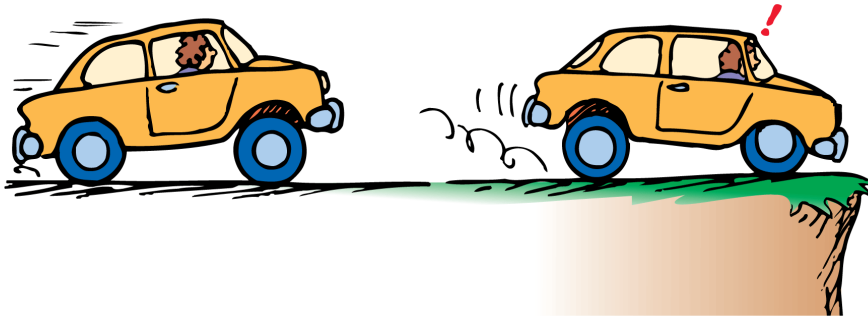A car is accelerating whenever there is a *change* in its state of motion.

Can you see that the gas pedal (accelerator), brakes, and steering wheel in an automobile are all controls for acceleration?

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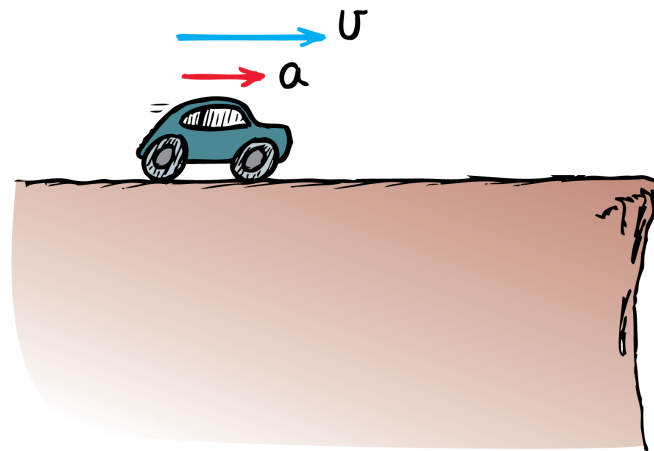
4.4 Acceleration

Change in Direction

Acceleration also applies to changes in *direction*.

- It is important to distinguish between speed and velocity.

- Acceleration is defined as the rate of change in *velocity,* rather than *speed.*

- Acceleration, like velocity, is a vector quantity because it is directional.
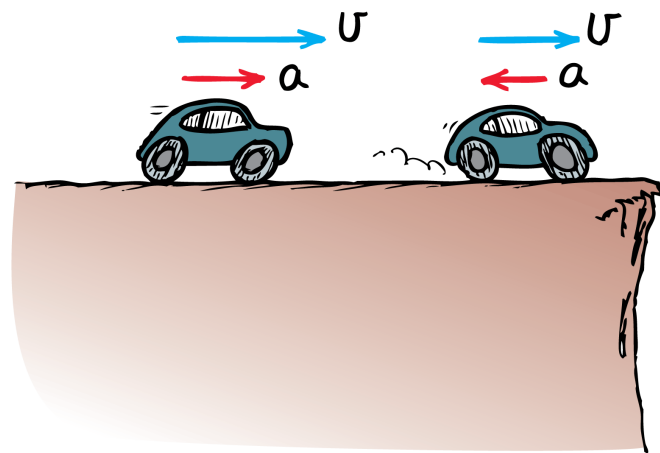
4.4 Acceleration

Accelerate in the direction of velocity–speed up

4.4 Acceleration

Accelerate in the direction of velocity–speed up

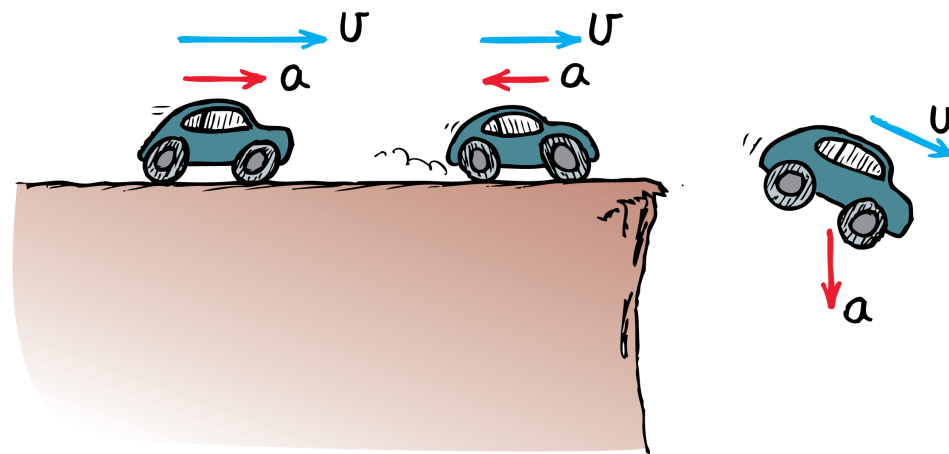Accelerate against velocity–slow down

4.4 Acceleration

Accelerate in the direction of velocity–speed up

Accelerate against velocity–slow down

Accelerate at an angle to velocity–change direction

4.4 Acceleration

Change in Speed

When straight-line motion is considered, it is common to use speed and velocity interchangeably.

When the direction is not changing, acceleration may be expressed as the rate at which *speed* changes.

$$\text{acceleration (along a straight line)} = \frac{\text{change in speed}}{\text{time interval}}$$

4.4 Acceleration

Speed and velocity are measured in units of distance per time.

- Acceleration is the change in velocity (or speed) per time interval.

- Acceleration units are speed per time.

- Changing speed, without changing direction, from 0 km/h to 10 km/h in 1 second, acceleration along a straight line is

$$\text{acceleration} = \frac{\text{change in speed}}{\text{time interval}} = \frac{10 \text{ km/h}}{1 \text{ s}} = 10 \text{ km/h·s}$$

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4.4 Acceleration

The acceleration is 10 km/h•s, which is read as "10 kilometers per hour-second."

Note that a unit for time appears twice: once for the unit of speed and again for the interval of time in which the speed is changing.

4.4 Acceleration

think!

Suppose a car moving in a straight line steadily increases its speed each second, first from 35 to 40 km/h, then from 40 to 45 km/h, then from 45 to 50 km/h. What is its acceleration?

4.4 Acceleration

think!

Suppose a car moving in a straight line steadily increases its speed each second, first from 35 to 40 km/h, then from 40 to 45 km/h, then from 45 to 50 km/h. What is its acceleration?

Answer: The speed increases by 5 km/h during each 1-s interval in a straight line. The acceleration is therefore 5 km/h•s during each interval.

4.4 Acceleration

think!

In 5 seconds a car moving in a straight line increases its speed from 50 km/h to 65 km/h, while a truck goes from rest to 15 km/h in a straight line. Which undergoes greater acceleration? What is the acceleration of each vehicle?

4.4 Acceleration

think!

In 5 seconds a car moving in a straight line increases its speed from 50 km/h to 65 km/h, while a truck goes from rest to 15 km/h in a straight line. Which undergoes greater acceleration? What is the acceleration of each vehicle?

Answer: The car and truck both increase their speed by 15 km/h during the same time interval, so their acceleration is the same.

4.4 Acceleration

CONCEPT CHECK

How do you calculate acceleration?

4.5 Free Fall: How Fast

The acceleration of an object in free fall is about 10 meters per second squared (10 m/s^2).

4.5 Free Fall: How Fast

Falling Objects

Imagine there is no air resistance and that gravity is the only thing affecting a falling object.

- An object moving under the influence of the gravitational force only is said to be in **free fall.**

- The **elapsed time** is the time that has elapsed, or passed, since the beginning of any motion, in this case the fall.

Free fall to a sky diver means fall before the parachute is opened, usually with lots of air resistance. Physics terms and everyday terms often mean different things.

4.5 Free Fall: How Fast

During each second of fall the instantaneous speed of the object increases by an additional 10 meters per second.

This gain in speed per second is the acceleration.

$$\text{acceleration} = \frac{\text{change in speed}}{\text{time interval}} = \frac{10 \text{ m/s}}{1 \text{ s}} = 10 \text{ m/s}^2$$

4.5 Free Fall: How Fast

When the change in speed is in m/s and the time interval is in s, the acceleration is in m/s^2, which is read as "meters per second squared."

The unit of time, the second, occurs twice—once for the unit of speed and again for the time interval during which the speed changes.

Since acceleration is a vector quantity, it's best to say the acceleration due to gravity is 10 m/s^2 *down*.

4.5 Free Fall: How Fast

For free fall, it is customary to use the letter *g* to represent the acceleration because the acceleration is due to gravity.

Although *g* varies slightly in different parts of the world, its average value is nearly 10 m/s^2.

Where accuracy is important, the value of 9.8 m/s^2 should be used for the acceleration during free fall.
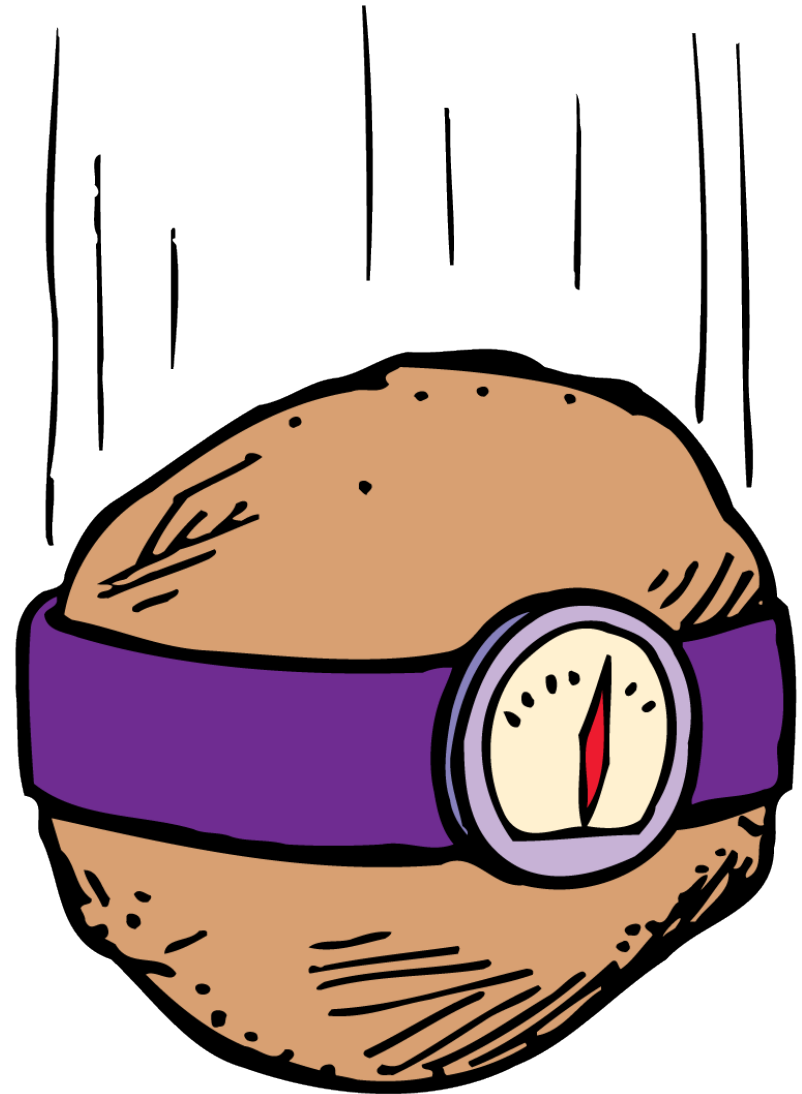
4.5 Free Fall: How Fast

The instantaneous speed of an object falling from rest is equal to the acceleration multiplied by the elapsed time.

$$v = gt$$

The letter *v* represents both speed and velocity. When the acceleration $g = 10 \text{ m/s}^2$ is multiplied by the elapsed time in seconds, the result is the instantaneous speed in meters per second.

4.5 Free Fall: How Fast

If a falling rock were somehow equipped with a speedometer, in each succeeding second of fall its reading would increase by the same amount, 10 m/s.

4.5 Free Fall: How Fast

Table 4.2	Free Fall Speeds of Objects
Elapsed Time (seconds)	Instantaneous Speed (meters/second)
0	0
1	10
2	20
3	30
4	40
5	50
t	$10t$

4.5 Free Fall: How Fast

The average speed of any object moving in a straight line with constant acceleration is the average of the initial speed and the final speed.

The average speed of a freely falling object in its first second of fall is the sum of the initial speed of zero and the final speed of 10 m/s, divided by 2, or 5 m/s.

4.5 Free Fall: How Fast

Rising Objects

Now consider an object thrown straight up:

- It moves upward for a while.

- At the highest point, when the object is changing its direction from upward to downward, its instantaneous speed is zero.

- It then falls downward as if it had been dropped from rest at that height.

4.5 Free Fall: How Fast

During the upward part of this motion, the object slows from its initial upward velocity to zero velocity.

The object is accelerating because its velocity is changing.

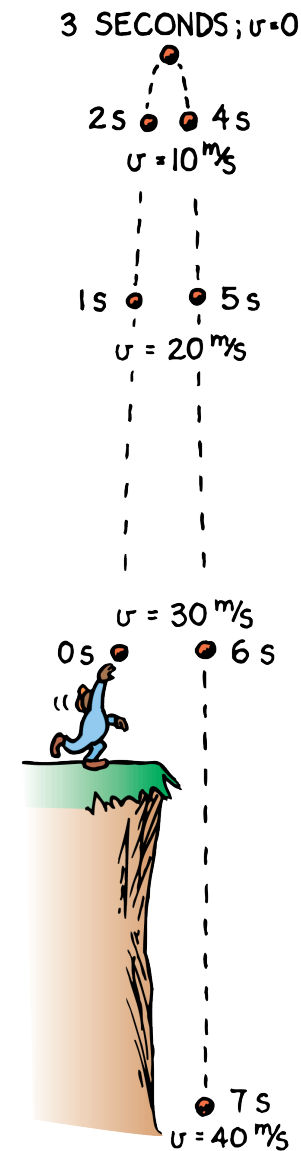How much does its speed decrease each second?

4.5 Free Fall: How Fast

The speed decreases at the same rate it increases when moving downward—at 10 meters per second each second.

- The *instantaneous speed* at points of equal elevation in the path is the same whether the object is moving upward or downward.

- The *velocities* are different because they are in opposite directions.

- During each second, the speed or the velocity changes by 10 m/s downward.

4.5 Free Fall: How Fast

The change in speed each second is the same whether the ball is going upward or downward.

3 SECONDS; $v = 0$

2 s   4 s
$v = 10 \text{ m/s}$

1 s   5 s
$v = 20 \text{ m/s}$

$v = 30 \text{ m/s}$
0 s   6 s

7 s
$v = 40 \text{ m/s}$

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4.5 Free Fall: How Fast

think!

During the span of the second time interval in Table 4.2, the object begins at 10 m/s and ends at 20 m/s. What is the average speed of the object during this 1-second interval? What is its acceleration?

4.5 Free Fall: How Fast

think!

During the span of the second time interval in Table 4.2, the object begins at 10 m/s and ends at 20 m/s. What is the average speed of the object during this 1-second interval? What is its acceleration?

Answer: The average speed is 15 m/s. The acceleration is 10 m/s^2.

4.5 Free Fall: How Fast

think!

What would the speedometer reading on the falling rock be 4.5 seconds after it drops from rest?

How about 8 seconds after it is dropped?

4.5 Free Fall: How Fast

think!

What would the speedometer reading on the falling rock be 4.5 seconds after it drops from rest?

How about 8 seconds after it is dropped?

Answer: The speedometer readings would be 45 m/s and 80 m/s, respectively.

4.5 Free Fall: How Fast

CONCEPT CHECK

What is the acceleration of an object in free fall?

4.6 Free Fall: How Far

For each second of free fall, an object falls a greater distance than it did in the previous second.
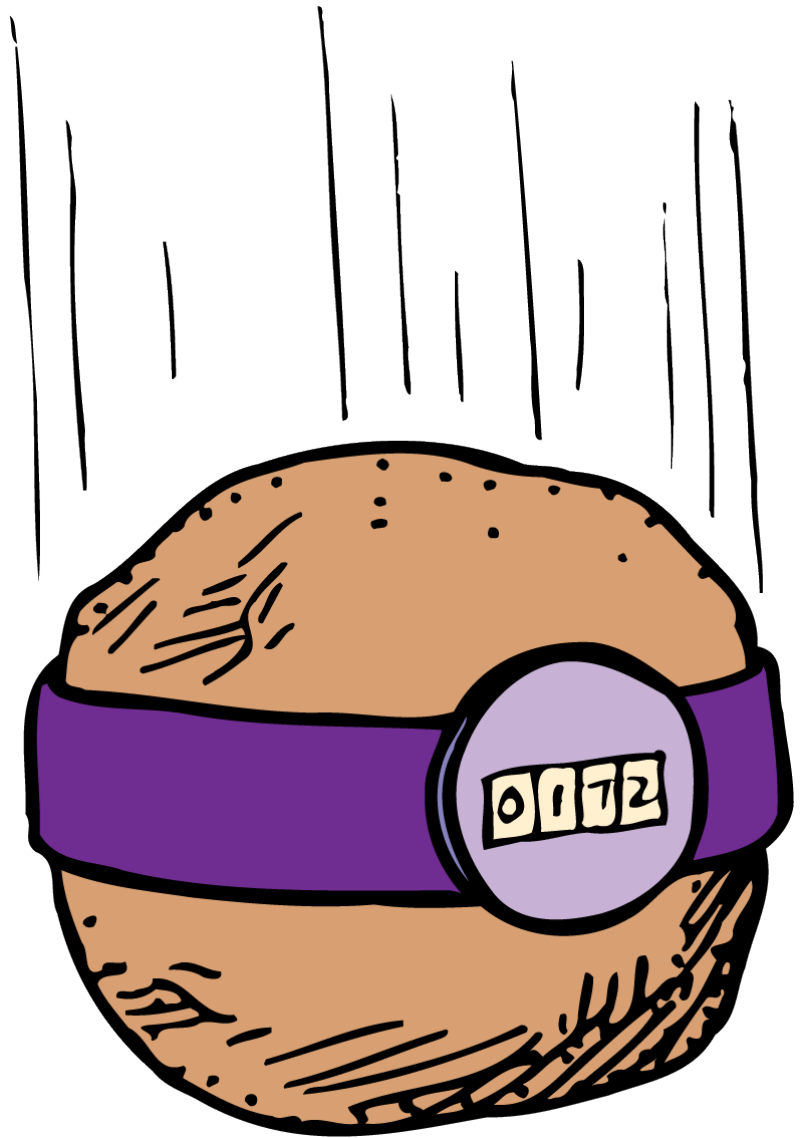
4.6 Free Fall: How Far

How far does an object in free fall travel in the first second?

- At the end of the first second, the falling object has an instantaneous speed of 10 m/s.

- The initial speed is 0 m/s.

- The average speed is 5 m/s.

- During the first second, the object has an average speed of 5 m/s, so it falls a distance of 5 m.

4.6 Free Fall: How Far

Pretend that a falling rock is somehow equipped with an *odometer*. The readings of distance fallen increase with time.

4.6 Free Fall: How Far

At the end of one second, the rock has fallen 5 meters.

At the end of 2 seconds, it has dropped a total distance of 20 meters.

At the end of 3 seconds, it has dropped 45 meters altogether.

4.6 Free Fall: How Far

These distances form a mathematical pattern: at the end of time t, the object starting from rest falls a distance d.

$$d = \frac{1}{2}gt^2$$

4.6 Free Fall: How Far

Table 4.3	Free Fall Distances of an Object
Elapsed Time (seconds)	**Distance Fallen (meters)**
0	0
1	5
2	20
3	45
4	80
5	125
t	$\frac{1}{2}gt^2$

4.6 Free Fall: How Far

We used freely falling objects to describe the relationship between distance traveled, acceleration, and velocity acquired.

The same principles apply to any accelerating object. Whenever an object's initial speed is zero and the acceleration a is constant, velocity and distance traveled are:

$$v = at \quad \text{and} \quad d = \frac{1}{2}at^2$$

4.6 Free Fall: How Far

think!

An apple drops from a tree and hits the ground in one second. What is its speed upon striking the ground? What is its average speed during the one second? How high above ground was the apple when it first dropped?

4.6 Free Fall: How Far

think!

An apple drops from a tree and hits the ground in one second. What is its speed upon striking the ground? What is its average speed during the one second? How high above ground was the apple when it first dropped?

Answer: The speed when it strikes the ground is 10 m/s. The average speed was 5 m/s and the apple dropped from a height of 5 meters.

4.6 Free Fall: How Far

CONCEPT CHECK

For a falling object, how does the distance per second change?

4.7 Graphs of Motion

On a speed-versus-time graph the slope represents speed per time, or acceleration.
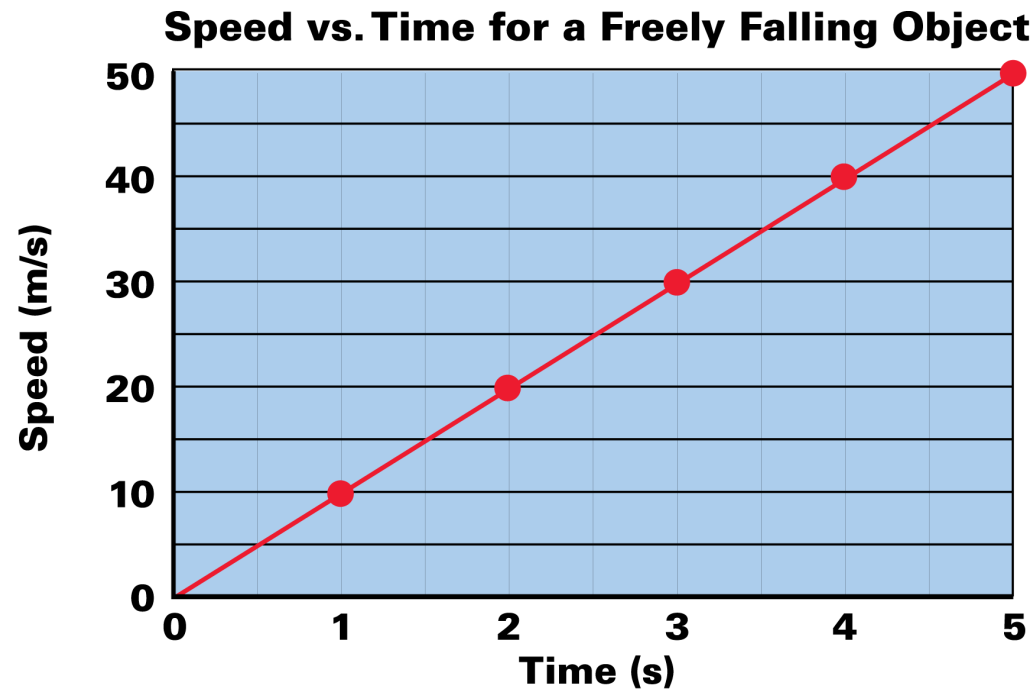
4.7 Graphs of Motion

Equations and tables are not the only way to describe relationships such as velocity and acceleration.

Graphs can visually describe relationships.

4.7 Graphs of Motion

Speed-Versus-Time

On a speed-versus-time graph, the speed *v* of a freely falling object can be plotted on the vertical axis and time *t* on the horizontal axis.

**Speed vs. Time for a Freely Falling Object**

4.7 Graphs of Motion

- The "curve" that best fits the points forms a straight line.

- For every increase of 1 s, there is the same 10 m/s increase in speed.

- Mathematicians call this *linearity*.

- Since the object is dropped from rest, the line starts at the origin, where both *v* and *t* are zero.

- If we double *t,* we double *v;* if we triple *t,* we triple *v;* and so on.

4.7 Graphs of Motion

• This particular linearity is called a *direct proportion,* and we say that time and speed are directly proportional to each other.

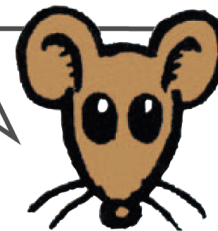**Speed vs. Time for a Freely Falling Object**
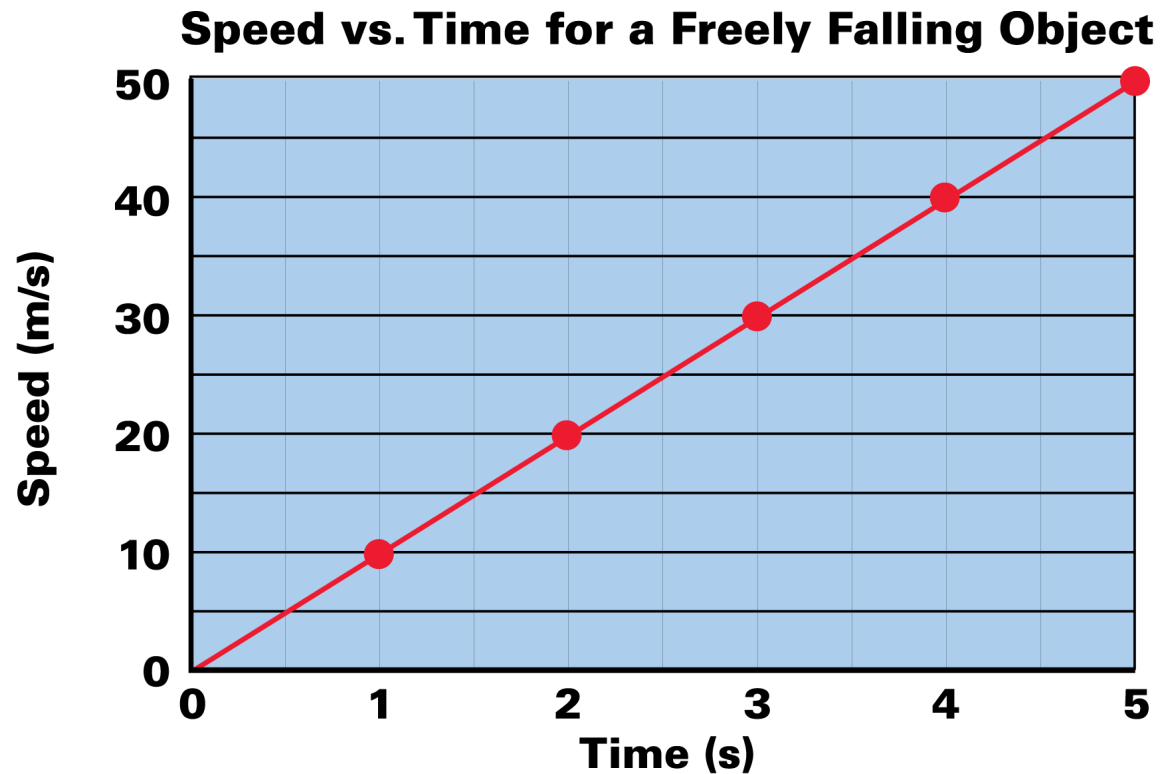
4.7 Graphs of Motion

The curve is a straight line, so its slope is constant.

Slope is the vertical change divided by the horizontal change for any part of the line.

The slope of a line on a graph is RISE/RUN.

4.7 Graphs of Motion

For 10 m/s of vertical change there is a horizontal change of 1 s.

The slope is 10 m/s divided by 1 s, or 10 m/s^2.

The straight line shows the acceleration is constant.

If the acceleration were greater, the slope of the graph would be steeper.
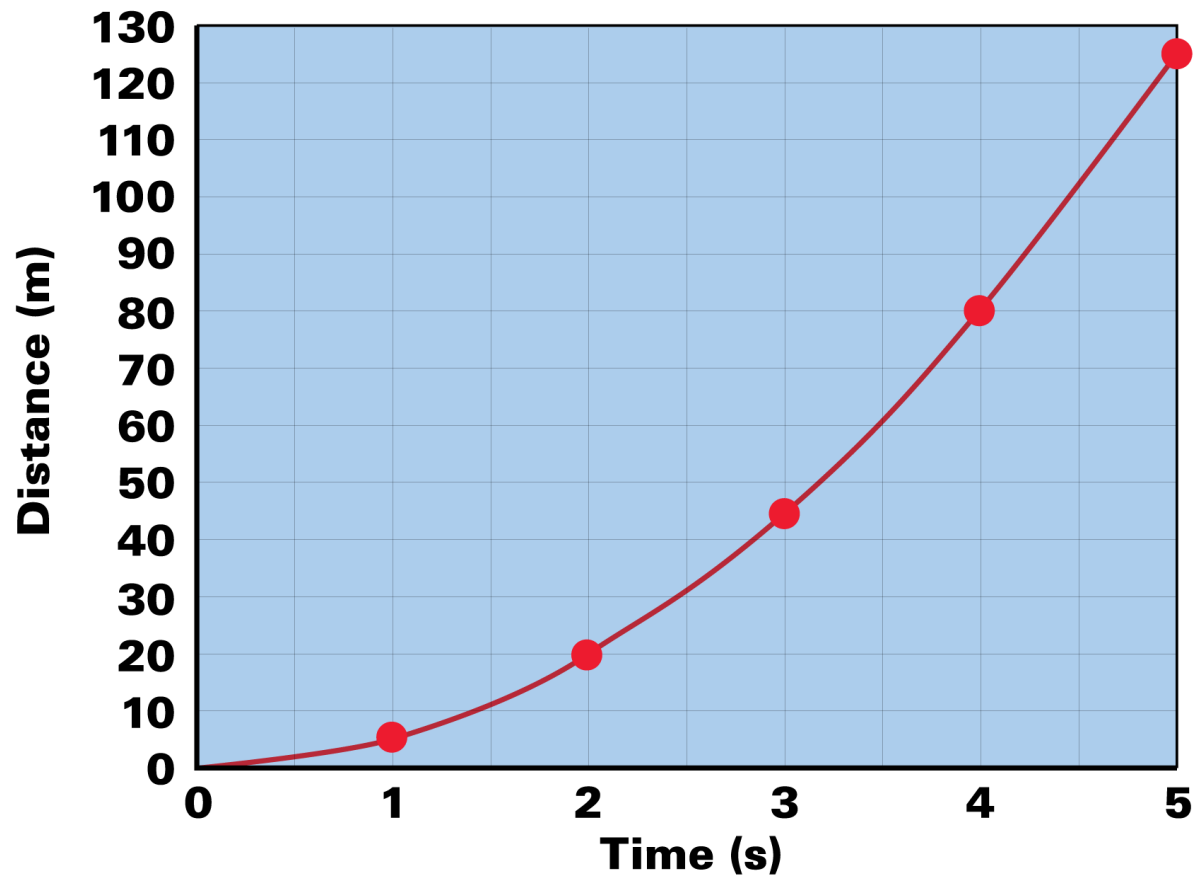
4.7 Graphs of Motion

Distance-Versus-Time

When the distance *d* traveled by a freely falling object is plotted on the vertical axis and time *t* on the horizontal axis, the result is a curved line.

4.7 **Graphs of Motion**

This distance-versus-time graph is parabolic.

Distance vs. Time for a Freely Falling Object

4.7 Graphs of Motion

The relationship between distance and time is *nonlinear*.

The relationship is *quadratic* and the curve is *parabolic*—when we double *t*, we do not double *d*; we quadruple it. Distance depends on time *squared!*

How fast something falls is entirely different than how far it falls. From rest, how fast is given by $v = gt$; how far by $d = \frac{1}{2}gt^2$.

4.7 Graphs of Motion

A curved line also has a slope—different at different points.

The slope of a curve changes from one point to the next.

The slope of the curve on a distance-versus-time graph is speed, the *rate* at which distance is covered per unit of time.

The slope steepens (becomes greater) as time passes, which shows that speed increases as time passes.

4.7 Graphs of Motion

CONCEPT CHECK

What does a slope of a speed-versus-time graph represent?

4.8 Air Resistance and Falling Objects

Air resistance noticeably slows the motion of things with large surface areas like falling feathers or pieces of paper. But air resistance less noticeably affects the motion of more compact objects like stones and baseballs.
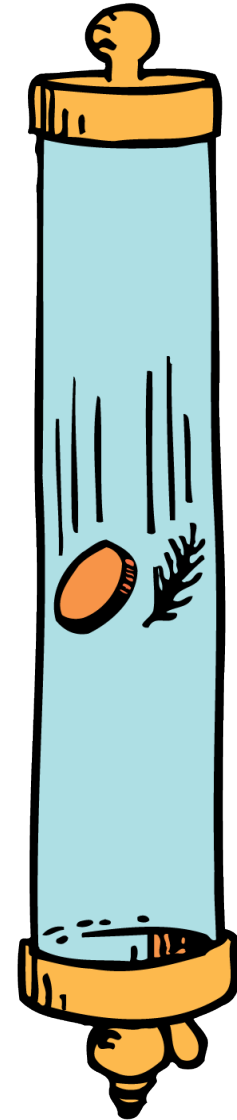
4.8 Air Resistance and Falling Objects

Drop a feather and a coin and the coin reaches the floor far ahead of the feather.

Air resistance is responsible for these different accelerations.

In a vacuum, the feather and coin fall side by side with the same acceleration, *g*.

4.8 Air Resistance and Falling Objects

A feather and a coin accelerate equally when there is no air around them.

4.8 Air Resistance and Falling Objects

In many cases the effect of air resistance is small enough to be neglected.

With negligible air resistance, falling objects can be considered to be falling freely.

4.8 Air Resistance and Falling Objects

CONCEPT CHECK

How does air resistance affect falling objects?

4.9 How Fast, How Far, How Quickly How Fast Changes

Acceleration is the rate at which velocity itself changes.

4.9 How Fast, How Far, How Quickly How Fast Changes

Don't mix up "how fast" with "how far."

- How fast something freely falls from rest after a certain elapsed time is speed or velocity. The appropriate equation is $v = gt$.

- How far that object has fallen is distance. The appropriate equation is $d = 1/2gt^2$.

4.9 How Fast, How Far, How Quickly How Fast Changes

One of the most confusing concepts encountered in this book is acceleration, or "how quickly does speed or velocity change."

What makes acceleration so complex is that it is *a rate of a rate*. It is often confused with velocity, which is itself a rate (the rate at which distance is covered).

Acceleration is not velocity, nor is it even a change in velocity.

4.9 How Fast, How Far, How Quickly How Fast Changes

CONCEPT CHECK

What is the relationship between velocity and acceleration?